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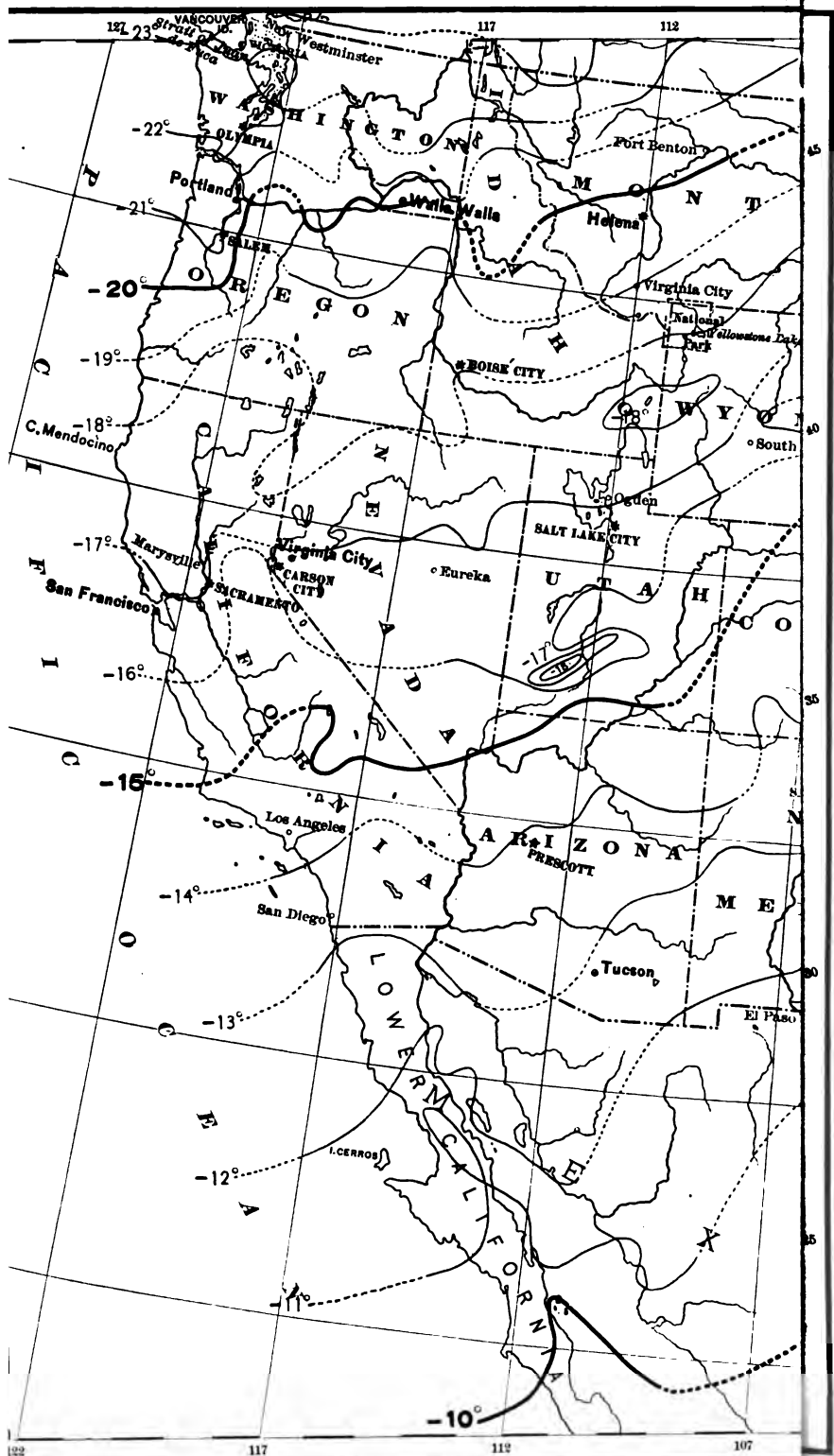
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# A TREATISE ON SURVEYING

*COMPRISING THE THEORY AND  
THE PRACTICE*

BY

WILLIAM M. GILLESPIE, LL. D.

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PART I

LAND SURVEYING AND DIRECT LEVELING

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## PREFACE.

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GILLESPIE'S "Land-Surveying" was first printed in 1851, for use in Professor Gillespie's classes in Union College. It was published in 1855, and very soon became the standard authority on land-surveying.

In the preface to the first edition Professor Gillespie says:

"Land-surveying is perhaps the oldest of the mathematical arts. Indeed, geometry itself, as its name—'land-measuring'—implies, is said to have arisen from the efforts of the Egyptian sages to recover and to fix the landmarks annually swept away by the inundations of the Nile. The art is also one of the most important at the present day, as determining the title to land, the foundation of the whole wealth of the world. It is, besides, one of the most useful as a study, from its striking exemplifications of the practical bearings of abstract mathematics. But, strangely enough, surveying has never yet been reduced to a systematic and symmetric whole. To effect this, by basing the art on a few simple principles and tracing them out into their complicated ramifications and varied applications (which extend from the measurement of 'a mowing-lot' to that of the heavens), has been the earnest endeavor of the present writer.

"The work, in its inception, grew out of the author's own needs. Teaching surveying, as preliminary to a course of civil engineering, he found none of the books in use (though very excellent in many respects) suited to his purpose. He was, therefore, compelled to teach the subject by a combination of familiar lectures on its principles and exemplifications of its practice. His notes continually swelling in bulk, gradually became systematized in nearly their present form. His system has thus been fully tested, and the present volume is the result.

"A double object has been kept in view in its preparation: viz., to produce a very plain introduction to the subject, easy to be mastered by the young scholar or the practical man of little previous acquirement, the only prerequisites being arithmetic and a little geometry; and at the same time to make the instruction of such a character as to lay a foundation broad enough and deep enough for the most complete superstructure which the professional student may subsequently wish to raise upon it."

In the preface to the "Land-Surveying," Professor Gillespie announced that another volume, on "Leveling and Higher Surveying," was to follow. This work was, at the time of his death in 1868, unfinished. It was completed by the writer and published in 1870.

The two volumes, "Land-Surveying" and "Leveling and Higher Surveying," were revised and united in one volume in 1887.

The rapid development of technical schools, and the demand for a more complete treatment of higher surveying for the use of students, have made it necessary to considerably enlarge the more advanced part of the work. As this will very much increase the size of the book, and as this advanced work is not needed in the preparatory schools, and in colleges where only a limited amount of surveying is taught, it has been deemed best to publish the work in two separate parts. Part I—plane surveying—will include land-surveying and direct leveling; and Part II—higher surveying—will include triangular surveying, geodesy, trigonometric leveling, barometric leveling, and precise leveling, topography, field astronomy, hydrographical surveying, mining surveying, city surveying, and other special topics.

By this arrangement those who desire only the land-surveying and direct leveling can have it separately, and those who wish to include the more advanced work can add Part II.

The best authorities have been consulted in order to render the work as reliable as possible.

The writer is under obligations to many friends for assistance in the work of revision. Their names will be noted in connection with their contributions.

CADY STALEY.

CASE SCHOOL OF APPLIED SCIENCE,  
CLEVELAND, OHIO, *November, 1895.*

# GENERAL DIVISION OF THE SUBJECT.

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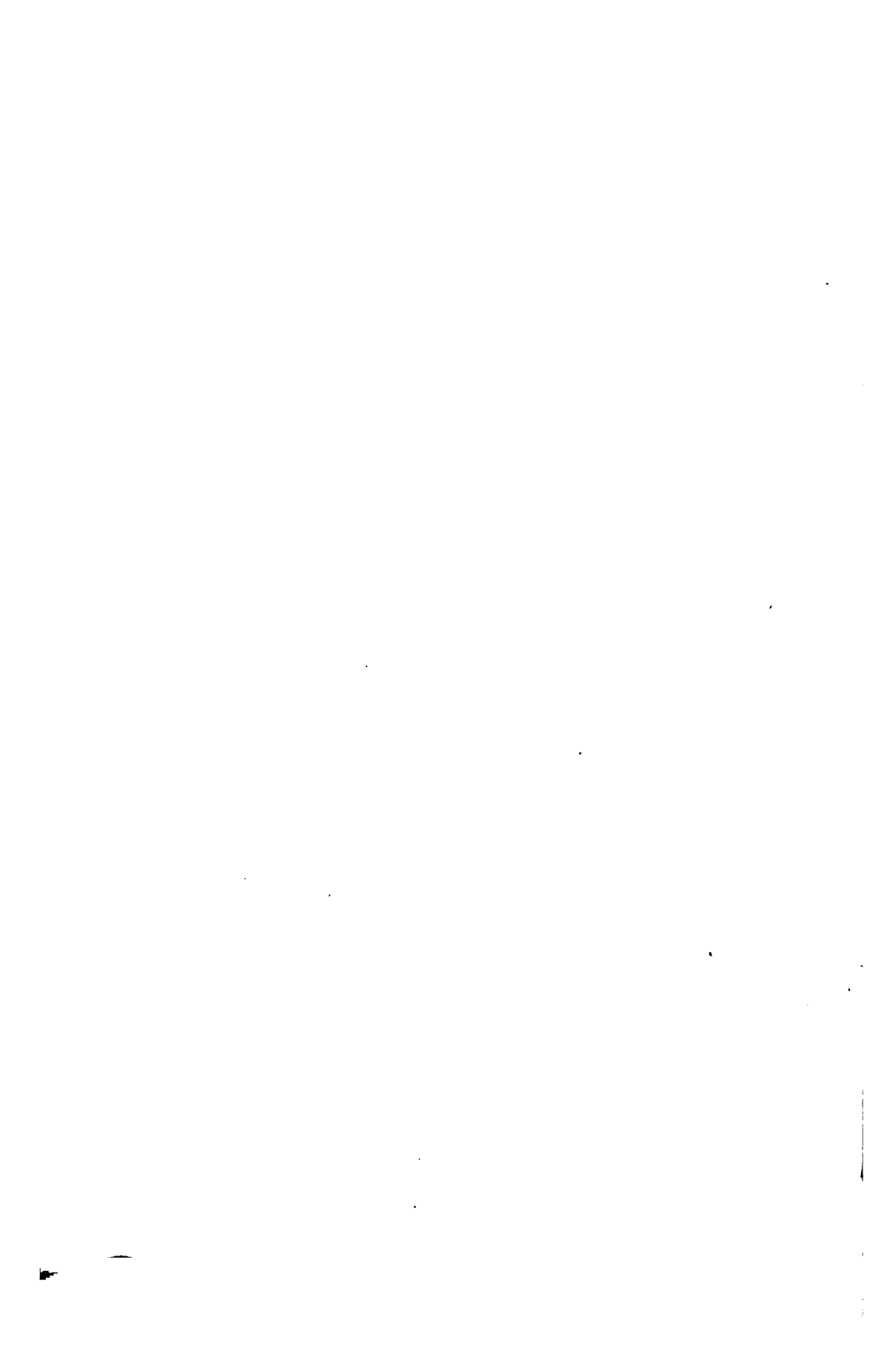
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# PART I.

## LAND-SURVEYING.

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### CHAPTER I.

#### GENERAL PRINCIPLES AND FUNDAMENTAL OPERATIONS.

##### DEFINITIONS AND METHODS.

1. SURVEYING is the art of making such measurements as will determine the relative positions of any points on the surface of the earth ; so that a *Map* of any portion of that surface may be drawn, and its *Content* calculated.

2. The position of a point is said to be *determined*, when it is known how far that point is from one or more given points, and in what direction therefrom ; or how far it is in front of them or behind them, and how far to their right or to their left, etc. ; so that the place of the first point, if lost, could be again found by repeating these measurements in the contrary direction.

The “points” which are to be determined in Surveying are not the mathematical points treated of in Geometry, but the corners of fences, boundary stones, trees, and the like, which are mere points in comparison with the extensive surfaces and areas which they are the means of determining. In strictness, their centers should be regarded as the points alluded to.

A straight *Line* is “determined,” that is, has its length and its position known and fixed, when the points at its extremities are determined ; and a plane *Surface* has its form and dimensions determined when the lines which bound it are determined. Consequently, the determination of the relative positions of *points* is all that is necessary for the principal objects of Surveying ; which

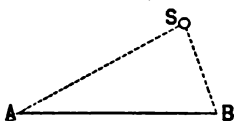
are to make a *map* of any surface, such as a field, farm, State, etc., and to calculate its *content* in square feet, acres, or square miles. The former is an application of Drafting, the latter of Mensuration.

The position of a point may be determined by a variety of methods. Those most frequently employed in Surveying are the following—all the points being supposed to be in the same plane :

**3. First Method.** *By measuring the distances from the required point to two given points.*

Thus, in Fig. 1, the point S is “determined,” if it is known to be one inch from A, and half an inch from B ; for its place, if lost, could be found by describing two arcs of circles, from A and B as centers, and with the given distances as radii. The required point would be at the intersection of these arcs.

FIG. 1.



In applying this principle in surveying, S may represent any station, such as a corner of a field, an angle of a fence, a tree, a house, etc. If, then, one corner of a field be 100 feet from a second corner, and 50 feet from a third, the place of the first corner is known and determined with reference to the other two.

There will be two points fulfilling this condition, one on each side of the given line, but it will always be known which of them is the one desired.

In *Geography*, this principle is employed to indicate the position of a town ; as when we say that Buffalo is distant (in a straight line) 295 miles from New York, and 390 from Cincinnati, and thus convey to a stranger acquainted with only the last two places a correct idea of the position of the first.

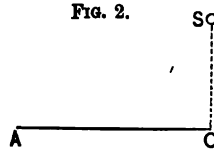
In *Analytical Geometry*, the lines AS and BS are known as “*Focal Co-ordinates*,” the general name “*co-ordinates*” being applied to the lines or angles which determine the position of a point.

**4. Second Method.** *By measuring the perpendicular distance from the required point to a given line, and the distance thence along the line to a given point.*

Thus, in Fig. 2, if the perpendicular distance SC be half an

inch, and CA be one inch, the point S is "determined"; for its place could be again found by measuring one inch from A to C, and half an inch from C, at right angles to AC, which would fix the point S.

The public lands of the United States are laid out by this method, as will be explained in Chapter VII.

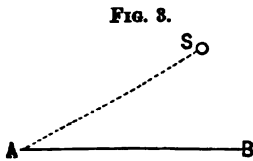


In *Geography*, this principle is employed under the name of Latitude and Longitude.

Thus, Philadelphia is one degree and fifty-two minutes of longitude east of Washington, and one degree and three minutes of latitude north of it.

In *Analytical Geometry*, the lines AC and CS are known as "*Rectangular Co-ordinates*." The point is there regarded as determined by the intersection of two lines, drawn parallel to two fixed lines, or "*Axes*," and at a given distance from them. These *Axes*, in the present figure, would be the line AC, and another line, perpendicular to it and passing through A, as the origin.

**5. Third Method.** *By measuring the angle between a given line and a line drawn from any given point of it to the required point; and also the length of this latter line.*



Thus, in Fig. 3, if we know the angle BAS to be a third of a right angle, and AS to be one inch, the point S is determined; for its place could be found by drawing from A, a line making the given angle with AB, and measuring on it the given distance.

In applying this principle in surveying, S, as before, may represent any station, and the line AB may be a fence, or any other real or imaginary line.

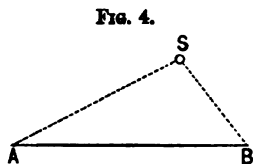
In "*Compass Surveying*," it is a north-and-south line, the direction of which is given by the magnetic needle of the compass.

In *Geography*, this principle is employed to determine the relative positions of places, by "*bearings and distances*"; as when we say, that San Francisco is 1,750 miles nearly due west from St.

Louis; the word "west" indicating the *direction*, or angle which the line joining the two places makes with a north-and-south line, and the number of miles giving the *length* of that line.

In *Analytical Geometry*, the line  $AS$ , and the angle  $BAS$ , are called "*Polar Co-ordinates*."

**6. Fourth Method.** *By measuring the angles made with a given line by two other lines starting from given points upon it, and passing through the required point.*

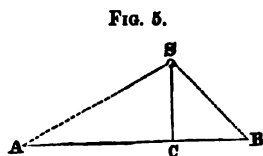


Thus, in Fig. 4, the point  $S$  is determined by being in the intersection of the two lines  $AS$  and  $BS$ , which make respectively angles of a half and of a third of a right angle with the line  $AB$ , which is one inch long; for the place of the point could be found, if lost, by drawing from  $A$  and  $B$  lines making with  $AB$  the known angles.

In *Geography*, we might thus fix the position of St. Louis, by saying it lay nearly due north from New Orleans, and due west from Washington.

In *Analytical Geometry*, these two angles would be called "*Angular Co-ordinates*."

**7.** In Fig. 5 are shown together all the measurements necessary for determining the same point  $S$ , by each of the four preceding methods. In the *First Method*, we measure the distances  $AS$  and  $BS$ ; in the *Second Method*, the distances  $AC$  and  $CS$ , the latter at right angles to the former; in the *Third Method*, the distance  $AS$ , and the angle  $SAB$ ; and, in the *Fourth Method*, the angles  $SAB$  and  $SBA$ . In all these methods the point is really determined by the intersection of two lines, either straight lines or arcs of circles. Thus, in the *First Method*, it is determined by the intersection of two circles; in the *Second*, by the intersection of two straight lines; in the *Third*, by the intersection of a straight line and a circle; and, in the *Fourth*, by the intersection of two straight lines.



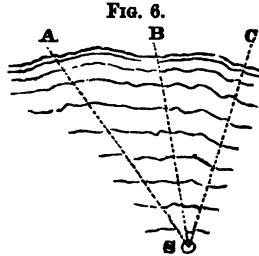


**8. Fifth Method.** *By measuring the angles made with each other by three lines of sight passing from the required point to three points whose positions are known.*

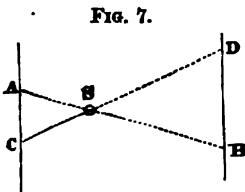
Thus, in Fig. 6, the point S is determined by the angles A S B and B S C, made by the three lines S A, S B, and S C.

Geographically, the position of Chicago would be determined by three straight lines passing from it to Washington, Cincinnati, and Mobile, and making known angles with each other; that of the first and second lines being about one third, and that of the second and third lines, about one half of a right angle.

From the *three lines* employed, this may be named the Method of *Trilinear Co-ordinates*.



**9.** The position of a point is sometimes determined by the intersection of two lines, which are themselves determined by their extremities being given. Thus, in Fig. 7, the point S is determined by its being situated in the intersection of A B and C D. This method is sometimes employed to fix the position of a station on a railroad line, etc., when it occurs in a place where a stake can not be driven, such as in a pond, and in a few other cases, but is not used frequently enough to require that it should be called a *sixth* principle of Surveying.



**10.** These five methods of determining the positions of points produce five corresponding systems of Surveying, which may be named as follows:

- I. DIAGONAL SURVEYING.
- II. PERPENDICULAR SURVEYING.
- III. POLAR SURVEYING.
- IV. TRIANGULAR SURVEYING.
- V. TRILINEAR SURVEYING.

The above division of Surveying has been made in harmony with the principles involved and the methods employed.

The subject is, however, sometimes divided with reference to the *instruments* employed; as the chain, either alone or with cross-staff; the compass; the transit or theodolite; the sextant; the plane-table, etc.

11. Surveying may also be divided according to its *objects*.

In *Land* Surveying, the content, in acres, etc., of the tract surveyed, is usually the principal object of the survey. A map, showing the shape of the property, may also be required. Certain signs on it may indicate the different kinds of culture, etc. This land may also be required to be divided up in certain proportions; and the lines of division may also be required to be set out on the ground. One or all of these objects may be demanded in Land Surveying.

In *Topographical* Surveying, the measurement and graphical representation of the inequalities of the ground, or its "relief," i. e., its hills and hollows, as determined by the art of "Leveling," is the leading object.

In *Maritime* or *Hydrographical* Surveying, the positions of rocks, shoals, and channels are the chief subjects of examination.

In *Mining* Surveying, the directions and dimensions of the subterranean passages of mines are to be determined.

12. Surveying may also be divided according to the *extent* of the district surveyed into *Plane* and *Geodesic*. Geodesy takes into account the curvature of the earth, and employs Spherical Trigonometry. *Plane* Surveying disregards this curvature, as a needless refinement except in very extensive surveys, such as those of a State, and considers the surface of the earth as plane, which may safely be done in surveys of moderate extent.

13. In all the methods of Land Surveying, there are three stages of operation:

1. *Measuring* certain lines and angles, and recording them;
2. *Drawing* them on paper to some suitable scale;
3. *Calculating* the content of the surface surveyed.

**MAKING THE MEASUREMENTS.**

14. The *Measurements* which are required in Surveying may be of lines or of angles, or of both, according to the Method employed. Each will be successively considered.

***Measuring Straight Lines.***

15. The lines, or distances, which are to be measured, may be either actual or visual.

*Actual lines* are such as really exist on the surface of the land to be surveyed, either bounding it, or crossing it; such as fences, ditches, roads, streams, etc.

*Visual lines* are imaginary lines of sight, either temporarily measured on the ground, such as those joining opposite corners of a field; or simply indicated by stakes at their extremities or otherwise. If long, they are "ranged out" by methods to be given.

Lines are usually measured with chains, tapes, or rods, divided into yards, feet, links, or some other unit of measurement.

FIG. 8.

**16. Gunter's Chain.**

This is the measure most commonly used in Land Surveying. It is 66 feet, or 4 rods long.\* Eighty such chains make one mile.

It is composed of one hundred pieces of iron or steel wire, or links, each bent at the end into a ring, and connected with the

\* This length was chosen (by Mr. Edward Gunter) because 10 square chains of 66 feet make one acre, and the computation of areas is thus greatly facilitated. For other surveying purposes, particularly for railroad work, a chain of 100 feet is preferable. On the United States Coast and Geodetic Survey the unit of measurement is the French *Mètre*, equal to 3.281 feet nearly.

ring at the end of the next piece by another ring. Sometimes two or three rings are placed between the links. The chain is then less liable to twist and get entangled or "kinked." Two or more swivels are also inserted in the chain, so that it may turn around without twisting. Every tenth link is marked by a piece of brass, having one, two, three, or four points, corresponding to the number of tens which it marks, counting from the nearest end of the chain.\* The middle or fiftieth link is marked by a round piece of brass.

The hundredth part of a chain is called a link.† The great advantage of this is that, since links are decimal parts of a chain, they may be so written down, 5 chains and 43 links being 5·43 chains, and all the calculations respecting chains and links can then be performed by the common rules of decimal arithmetic. Each link is 7·92 inches long, being =  $66 \times 12 \div 100$ .

The following table will be found convenient :

| CHAINS INTO FEET. |       |         |       | FEET INTO LINKS. |        |       |        |
|-------------------|-------|---------|-------|------------------|--------|-------|--------|
| Chains.           | Feet. | Chains. | Feet. | Feet.            | Links. | Feet. | Links. |
| 0·01              | 0·66  | 1·00    | 66·   | 0·10             | 0·15   | 10·   | 15·2   |
| 0·02              | 1·32  | 2·      | 132·  | 0·20             | 0·30   | 15·   | 22·7   |
| 0·03              | 1·98  | 3·      | 198·  | 0·25             | 0·38   | 20·   | 30·8   |
| 0·04              | 2·64  | 4·      | 264·  | 0·30             | 0·45   | 25·   | 37·9   |
| 0·05              | 3·30  | 5·      | 330·  | 0·40             | 0·60   | 30·   | 45·4   |
| 0·06              | 3·96  | 6·      | 396·  | 0·50             | 0·76   | 33·   | 50·0   |
| 0·07              | 4·62  | 7·      | 462·  | 0·60             | 0·91   | 35·   | 53·0   |
| 0·08              | 5·28  | 8·      | 528·  | 0·70             | 1·06   | 40·   | 60·6   |
| 0·09              | 5·94  | 9·      | 594·  | 0·75             | 1·13   | 45·   | 68·2   |
| 0·10              | 6 60  | 10·     | 660·  | 0·80             | 1·21   | 50·   | 75·8   |
| 0·20              | 13·20 | 20·     | 1320· | 0·90             | 1·36   | 55·   | 83·3   |
| 0·30              | 19·80 | 30·     | 1980· | 1·00             | 1·52   | 60·   | 90·9   |
| 0·40              | 26·40 | 40·     | 2640· | 2·               | 3·0    | 65·   | 98·5   |
| 0·50              | 33·00 | 50·     | 3300· | 3·               | 4·5    | 70·   | 106·1  |
| 0·60              | 39·60 | 60·     | 3960· | 4·               | 6·1    | 75·   | 113·6  |
| 0·70              | 46·20 | 70·     | 4620· | 5·               | 7·6    | 80·   | 121·2  |
| 0·80              | 52·80 | 80·     | 5280· | 6·               | 9·1    | 85·   | 128·8  |
| 0·90              | 59·40 | 90·     | 5940· | 7·               | 10·6   | 90·   | 136·4  |
| 1·00              | 66·00 | 100·    | 6600· | 8·               | 12·1   | 95·   | 143·9  |
|                   |       |         |       | 9·               | 13·6   | 100·  | 151·5  |

\* To prevent the very common mistake of calling forty, sixty; or thirty, seventy; it has been suggested to make the 11th, 21st, 31st, and 41st links of *brass*, which would at once show on which side of the middle of the chain was the doubtful mark. This would be particularly useful in Mining Surveying.

† This must not be confounded with the pieces of wire which have the same name, since one of them is shorter than the "link" used in calculation by half a ring or more, according to the way in which the chain is made.

To reduce links to feet, subtract from the number of links as many units as it contains hundreds ; multiply the remainder by 2 and divide by 3.

To reduce feet to links, add to the given number half of itself, and add one for each hundred (more exactly, for each ninety-nine) in the sum.

The chain is liable to be lengthened by its rings being pulled open, and to be shortened by its links being bent. It should therefore be frequently tested by a carefully measured length of 66 feet, set out by a standard measure on a flat surface, such as the top of a wall, or on smooth level ground between two stakes, their centers being marked by small nails. It may be left a little longer than the true length, since it can seldom be stretched so as to be perfectly horizontal and not hang in a curve, or be drawn out in a perfectly straight line.\* Distances measured with a perfectly accurate chain will always and unavoidably be recorded as longer than they really are. To insure the chain being always strained with the same force, a spring, like that of a spring-balance, is sometimes placed between one handle and the rest of the chain.

If a line has been measured with an incorrect chain, the true length of the line will be obtained by multiplying the number of chains and links in the measured distance by 100, and dividing by the length of the standard distance, as given by measurement of it with the incorrect chain. The proportion here employed is this : *As the length of the standard given by the incorrect chain is to the true length of the standard, so is the length of the line given by the measurement to the true length.* Thus, suppose that a line has been measured with a certain chain, and found by it to be ten chains long, and that the chain is afterward found to have been so stretched that the standard distance measured by it appears to be only 99 links long. The measured line is therefore longer than it had been thought to be, and its true length is obtained by multiplying 10 by 100, and dividing by 99.

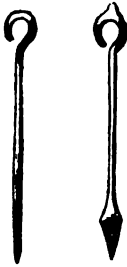
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\* The chain used by the Government surveyors of France, which is ten metres, or about half a Gunter's chain in length, is made from one fifth to two fifths of an inch longer than the standard. An inaccuracy of one five-hundredth of its length ( $= 1\frac{1}{2}$  inch on a Gunter's chain) is the utmost allowed not to vitiate the survey.

**17. Pins.** Ten iron pins, or "arrows," usually accompany the chain.\* They are about a foot long, and are made of stout iron wire, sharpened at one end, and bent into a ring at the other. Pieces of red and white cloth should be tied to their heads, so that they can be easily found in grass, dead leaves, etc.

They should be strung on a ring, which has a spring-catch to retain them. Their usual form is shown in Fig. 9. Fig. 10 shows another form, made very large, and therefore very heavy near the point, so that, when held by the top and dropped, it may fall vertically. The uses of this will be seen presently.

FIG. 9. FIG. 10.



On irregular ground, two stout stakes, about six feet long, are needed to put the forward chain-man in line, and to enable whichever of the two is lowest to raise his end of the chain in a truly vertical line, and to strain the chain straight.

A number of long and slender rods are also necessary for "ranging out" lines between distant points.

**18. How to Chain.** Two men are required—a forward chain-man and a hind chain-man, or leader and follower. The latter takes the handles of the chain in his left hand, and the chain itself in his right hand, and throws it out in the direction in which it is to be drawn. The former takes a handle of the chain and one pin in his right hand, and the other pins (and the staff, if used), in his left hand, and draws out the chain. The follower then walks beside it, examining carefully that it is not twisted or bent. He then returns to its hinder end, which he holds at the beginning of the line to be measured, puts his eye exactly over it and, by the words "Right," "Left," directs the leader how to put his staff, or the pin which he holds up, "in line," so that it may seem to cover and hide the flag-staff, or other object at the end of the line. The leader all the while keeps the chain tightly stretched, and his

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\* Eleven pins are sometimes used, one being of brass. Nine of iron, with four or eight of brass, may also be employed. Their uses are explained in Articles 18 and 19.

end of it touching his staff. Every time he moves the chain, he should straighten it by an undulating shake. When the staff (or pin) is at last put "in line," the follower says "Down." The leader then puts in the single pin precisely at the end of the chain, and replies "Down." The follower then (and never before hearing this signal that the point is fixed) loosens his end of the chain, retaining it in his hand. The leader draws on the chain, making a step to one side of the pin just set, to avoid dragging it out. He should keep his eye steadily on the object ahead, or, in a hollow, should line himself approximately by looking back. The follower should count his steps, so as to know where to look for the pin in high grass, etc. As he approaches the pin, he calls "Halt." On reaching it, he holds the handle of the chain against it, pressing his knee against both to keep the pin firm. He then, with his eye over the pin, "lines" the leader as before. When the "Down" has been again called by the follower, and answered by the leader, the former pulls out the pin with the chain-hand, and carries it in his other hand, and they go on as before.\* The operation is repeated till the leader has arrived at the end of the line, or has put down all his pins.

When the leader has put down his tenth pin, he draws on the chain its length farther, and, after being lined, puts his foot on the handle to keep it firm, and calls "Tally." The follower then drops his end of the chain, goes up to the leader and gives him back all the pins, both counting them to make sure that none have been lost. One pin is then put down at the forward end of the chain, and they go on as before.

Some surveyors cause the leader to call "tally" at the tenth pin, and then exchange pins; but then the follower has only the hole made by the pin, or some other indefinite mark, to measure from.

Eleven pins are sometimes preferred, the eleventh being of brass, or otherwise different from the rest, and being used to mark

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\* When a chain's length would end in a ditch, pool of water, etc., and the chainmen are afraid of wetting their feet, they can measure part of a chain, to the edge of the water, then stretch the chain across it, and then measure another portion of a chain, so that, with the former portion, it may make up a full chain.

the end of the eleventh chain ; another being substituted for it before the leader goes on.

The two chain-men may change duties at each change of pins, if they are of equal skill, but the more careful and intelligent of two laborers should generally be made "follower."

When the leader reaches the end of the line, he stops, and holds his end of the chain against it. The follower drops his end and counts the links beyond the last pin, noting carefully on which side of the "fifty" mark it comes. Each pin now held by the follower, including the one in the ground, represents one chain ; each time "tally" has been called, and the pins exchanged, represents ten chains, and the links just counted make up the total distance.

**19. Tallies.** In chaining very long distances, there is danger of miscounting the number of "tallies," or tens. To avoid mistakes, pebbles, etc., may be changed from one pocket into another at each change of pins ; or bits of leather on a cord may be slipped from one side to the other ; or knots tied on a string ; but the best plan is the following : Instead of ten iron pins, use nine iron pins, and four, or eight, or ten pins of brass, or very much longer than the rest. At the end of the tenth chain, the iron pins being exhausted, a brass pin is put down by the leader. The follower then comes up, and returns the nine iron pins, but retains the brass one, with the additional advantage of having this pin to measure from. At the end of the twentieth chain, the same operation is repeated ; and so on. When the measurement of the line is completed, each brass pin held by the follower counts ten chains, and each iron pin one, as before.

**20. Chaining on Slopes.** All the distances employed in Land-surveying must be measured horizontally, or on a level. When the ground slopes, it is therefore necessary to make certain allowances or corrections. If the slope be gentle, hold the up-hill end of the chain on the ground, and raise the down-hill end till the chain is level. To insure the elevated end being exactly over the desired spot, raise it along a staff kept vertical, or drop a pin held



by the point with the ring downward (if you have not the heavy pointed ones shown in Fig. 10), or, which is better, use a plumb-line. A person standing beside the chain, and at a little distance from it, can best tell if it be nearly level. If the hill be so steep that a whole chain can not be held up level, use only half or quarter of it at a time. Great care is necessary in this operation.

FIG. 11.



To measure down a steep hill, stretch the whole chain in line. Hold the upper end fast on the ground. Raise up the 20 or 30 link-mark, so that that portion of the chain is level. Drop a plumb-line or pin. Then let the follower come forward and hold down that link on this spot, and the leader hold up another short portion, as before. Chaining down a slope is more accurate than chaining up it, since in the latter case the follower can not easily place his end of the chain exactly over the pin.

A more accurate, though more troublesome, method, is to measure the angle of the slope, and make the proper allowance by calculation, or by a table, previously prepared. The correction being found, the chain may be drawn forward the proper number of links, and the correct distance of the various points to be noted will thus be obtained at once, without any subsequent calculation or reduction. If the survey is made with the Transit provided with a vertical circle, the slope of the ground can be measured directly. A "Tangent Scale," for the same purpose, may be formed on the sides of the sights of a Compass. It will be described when the instrument is explained.

In the following table, the first column contains the angle which the surface of the ground makes with the horizon; the second column contains its slope, named by the ratio of the perpendicular to the base; and the third, the correction in links for each chain measured on the slope, i. e., the difference between the hypotenuse, which is the distance measured, and the horizontal base, which is the distance desired.

TABLE FOR CHAINING ON SLOPES.

| Angle. | Slope.   | Correction in links. | Angle. | Slope.  | Correction in links. |
|--------|----------|----------------------|--------|---------|----------------------|
| 3°     | 1 in 19  | 0.14                 | 13°    | 1 in 4½ | 2.56                 |
| 4°     | 1 in 14  | 0.24                 | 14°    | 1 in 4  | 2.97                 |
| 5°     | 1 in 11½ | 0.38                 | 15°    | 1 in 3½ | 3.41                 |
| 6°     | 1 in 9½  | 0.55                 | 16°    | 1 in 3¼ | 3.87                 |
| 7°     | 1 in 8   | 0.75                 | 17°    | 1 in 3¼ | 4.37                 |
| 8°     | 1 in 7   | 0.97                 | 18°    | 1 in 3  | 4.89                 |
| 9°     | 1 in 6½  | 1.23                 | 19°    | 1 in 3  | 5.45                 |
| 10°    | 1 in 6   | 1.53                 | 20°    | 1 in 2¾ | 6.03                 |
| 11°    | 1 in 5½  | 1.84                 | 25°    | 1 in 2  | 9.37                 |
| 12°    | 1 in 4½  | 2.19                 | 30°    | 1 in 1½ | 13.40                |

21. Chaining is the fundamental operation in all kinds of Surveying. It has for this reason been very minutely detailed. The "follower" is the most responsible person, and the surveyor will best insure his accuracy by taking that place himself. If he has to employ inexperienced laborers, he will do well to cause them to measure the distance between any two points, and then remeasure it in the opposite direction. The difference of their two results will impress on them the necessity of great carefulness.

To "do up" the chain, take the middle of it in the left hand, and with the right hand take hold of the doubled chain just beyond the second link; double up the two links between your hands, and continue to fold up two double links at a time, laying each pair obliquely across the others, so that when it is all folded up the handles will be on the outside, and the chain will have an hour-glass shape, easy to strap up and to carry.

22. **Tape.** Though the chain is most usually employed for the principal measurements of Surveying, a *tape-line*, divided on one side into links, and on the other into feet and inches, is more convenient for some purposes. It should be tested very frequently, particularly after getting wet, and the correct length marked on it at every ten feet. A "Metallic Tape," less liable to stretch, is manufactured, in which fine wires form its warp. When the tape is being wound up, it should be passed between two fingers to prevent its twisting in the box, which would make it necessary to unscrew its nut to take it out and untwist it. While in use, it

should be made portable by being folded up by arm's lengths, instead of being wound up.

A "Steel Tape," made of a thin ribbon of steel, with the divisions and numbers etched on it, is one of the most accurate measuring instruments. Those intended for accurate measurement have at one end an arrangement for shortening and lengthening the tape to provide for variations in length, due to changes of temperature, and at the other end a level and a spring-balance, so that when measuring the ends of the tape may be held at the same height, and always with the same tension. For methods employed in making accurate measurements, see Chapter XV, Part II.

**23.** Substitutes for a chain or a tape may be found in leather driving-lines, marked off with a carpenter's rule, or in a cord knotted at the length of every link. A well-made rope (such as a "patent wove line," woven circularly with the strands always straight in the line of the strain), when once well stretched, wetted, and allowed to dry with a moderate strain, will not vary from a chain more than one foot in two thousand, if carefully used.

**24. Rods.** When unusually accurate measurements are required, rods are employed. They may be of well-seasoned wood, of glass, of iron, etc. They must be placed in line very carefully end to end, or made to coincide in other ways, as will be explained under "Triangular Surveying," in which the peculiarly accurate measurement of one line is required, as all the others are founded upon it.

**25.** Pacing, sound, and other approximate means, may be used for measuring the length of a line. The *Stadia* and *Gradiometer* will be described in Chapter IV.

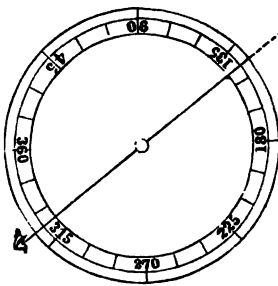
**26.** A *Perambulator*, or "Measuring-Wheel," is sometimes used for measuring distances, particularly roads. It consists of a wheel which is made to roll over the ground to be measured, and whose motion is communicated to a series of toothed wheels within the machine. These wheels are so proportioned that the index-wheel registers their revolutions, and records the whole distance passed

over. If the diameter of the wheel be  $31\frac{1}{2}$  inches, the circumference, and therefore each revolution, will be  $8\frac{1}{4}$  feet, or half a rod. The roughnesses of the road and the slopes necessarily cause the registered distances to exceed the true measure.

The *Odometer* is an instrument designed to register the number of revolutions of a wagon-wheel. Knowing the circumference of the wheel to which it is attached, and determining the number of revolutions by the odometer, the distance over which the wheel has passed may be approximately determined.

### Measuring Angles.

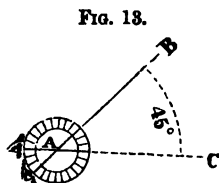
27. The angle made by any two lines—that is, the difference of their directions—may be obtained by a great variety of instruments. All of them are in substance mere modifications of the very simple one which will now be described, and which any one can make for himself:



Provide a circular piece of wood, and divide its circumference (by any of the methods of Geometrical Drafting) into three hundred and sixty equal parts, or “degrees,” and number them as in the figure. The divisions will be like those of a watch-face, but six times as many. These divisions are termed *graduations*. The figure shows only every fifteenth one. In the center of the circle fix a needle, or sharp-pointed wire, and upon this fix a straight stick, or thin ruler placed edgewise (called an *alidade*), so that it may turn freely on this point and nearly touch the graduations of the circle. Fasten the circle on a staff, pointed at the other end, and long enough to bring the alidade to the height of the eyes. The instrument is now complete. It may be called a *Goniometer*, or Angle-measurer.

Now let it be required to measure the angle between the lines *AB* and *AC*. Fix the staff in the ground, so that its center shall be exactly over the intersection of the two lines. Turn the alidade so that it points (as determined by sighting along it) to a rod, or

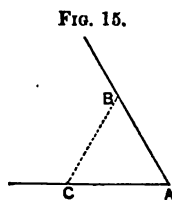
other mark at B, a point on one of the lines, and note what degree it covers—i. e., “The Reading.” Then, without disturbing the circle, turn the alidade till it points to C, a point on the other line. Note the new reading. The difference of these readings (in the figure, 45 degrees) is the difference in the directions of the two lines, or is the angle which one makes with the other. If the distance from A to C be now measured, the point C is “determined,” with respect to the points A and B, on the *Third Principle*. Any number of points may be thus determined.



Instead of the very simple and rude alidade, which has been supposed to be used, needles may be fixed on each end of the alidade; or sights may be added; or a small straight tube may be used, one end being covered with a piece of pasteboard in which a very small eye-hole is pierced, and threads, called “cross-hairs,” being stretched across the other end of it, as in the figure, so that their intersection may give a more precise line for determining the direction of any point.

When a telescope is substituted for this tube, and supported in such a way that it can turn over, so as to look both backward and forward, the instrument (with various other additions, which, however, do not affect the principle) is called a *Transit*.

**28. Chain Angles.** The angle made by any two lines can also be determined without the aid of an angle-measurer. Let it be required to find the angle made by the two lines A B and A C, Fig. 15. Measure off equal distances from A to B and C, and also the “tie-line” B C. It is evident that the tie-line is the chord of the angle to a radius equal to one of the equal distances measured on the sides. Therefore, divide the length of the tie-line by the length of this distance. The quotient will be the chord of the angle to a radius of one. In the TABLE OF CHORDS, at the end of this volume, find this quotient, and the number of degrees and minutes corre-



sponding to it gives the angle required. Otherwise, since the chord of any angle equals twice the sine of half the angle, we have this rule: Divide half the tie-line by the measured distance, find in a table of natural sines the angle corresponding to the quotient, and multiply this angle by two, to get the angle desired.

### *Surveying without Instruments.*

**29. Distances by Pacing.** Quite an accurate measurement of a line of ground may be made by walking over it at a uniform pace, and counting the steps taken. But the art of walking in a straight line must first be acquired. To do this, fix the eye on two objects in the desired line, such as two trees, or bushes, or stones, or tufts of grass. Walk forward, keeping the nearest of these objects steadily covering the other. Before getting up to the nearest object, choose a new one in line farther ahead, and then proceed as before, and so on. It is better not to attempt to make each of the paces three feet, but to take steps of the natural length, and to ascertain the value of each by walking over a known distance, and dividing it by the number of paces required to traverse it. Every person should thus determine the usual length of his own steps, repeating the experiment sufficiently often. The French "geographical engineers" accustom themselves to take regular steps of eight tenths of a *metre*, equal to two feet seven and a half inches. The United States military pace is two feet and six inches. This is regarded as a usual average. Quick pacing of 120 such paces per minute gives 3.41 miles per hour. Slow paces, of three feet each and sixty per minute, give 2.04 miles per hour.\*

The *Pedometer* is an instrument which counts the steps taken by one wearing it, without any attention on his part. It is made in the form of a watch, and carried in the pocket. The number of the steps given by the pedometer, multiplied by the length of the step, will give approximately any distance walked over. In one form of this instrument the number of steps is registered on a dial up to 2,500.

In another form the instrument is intended to be regulated ac-

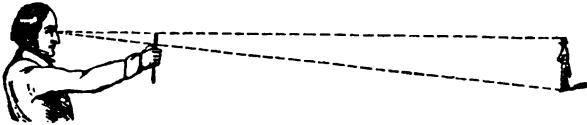
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\* A horse, on a walk, averages 330 feet per minute, on a trot 650, and on a common gallop 1,040. For longer times, the difference in horses is more apparent.

according to the length of step of the person carrying it, and then the distance is registered on the dial in miles.

**30. Distances by Visual Angle.** Prepare a *scale*, by marking off on a pencil what length of it, when it is held off at arm's length, a man's height appears to cover at different distances (previously

FIG. 16.



measured with accuracy) of 100, 500, 1,000 feet, etc. To apply this, when a man is seen at any unknown distance, hold up the pencil at arm's length, making the top of it come in the line from the eye to his head, and placing the thumb-nail in the line from the eye to his feet, as in Fig. 16. The pencil having been previously graduated by the method above explained, the portion of it now intercepted between these two lines will indicate the corresponding distance.

If no previous scale have been prepared, and the distance of a man be required, take a foot-rule, or any measure minutely divided, hold it off at arm's length as before, and see how much a man's height covers. Then, knowing the distance from the eye to the rule, a statement by the rule of three (on the principle of similar triangles) will give the distance required. Suppose a man's height, of 70 inches, covers one inch of the rule. He is then seventy times as far from the eye as the rule, and, if its distance be two feet, that of the man is 140 feet. Instead of a man's height, that of an ordinary house, of an apple-tree, the length of a fence-rail, etc., may be taken as the standard of comparison.

To keep the arm immovable, tie a string of known length to the pencil, and hold between the teeth a Knot tied at the other end of the string.

**31. Distances by Visibility.** The degree of visibility of various well-known objects will indicate approximately how far distant they

are. Thus, by ordinary eyes, the windows of a large house can be counted at a distance of about 13,000 feet, or  $2\frac{1}{2}$  miles; men and horses will be perceived as points at about half that distance, or  $1\frac{1}{2}$  mile; a horse can be clearly distinguished at about 4,000 feet; the movements of men at 2,600 feet, or half a mile; and the head of a man, occasionally, at 2,300 feet, and very plainly at 1,300 feet, or a quarter of a mile. The Arabs of Algeria define a mile as "the distance at which you can no longer distinguish a man from a woman." These distances of visibility will of course vary somewhat with the state of the atmosphere, and still more with individual acuteness of sight, but each person should make a corresponding scale for himself.

**32. Distances by Sound.** Sound passes through the air with a moderate and known velocity; light passes almost instantaneously. If, then, two distant points be visible from each other, and a gun be fired at night from one of them, an observer at the other, noting by a stop-watch the time at which the flash is seen, and then that at which the report is heard, can tell by the intervening number of seconds how far apart the points are, knowing how far sound travels in a second. Sound moves about 1,098 feet per second in dry air, with the temperature at the freezing-point,  $32^{\circ}$  Fahr. For higher or lower temperatures add or subtract  $1\frac{1}{2}$  foot for each degree of Fahrenheit. If a wind blows with or against the movement of the sound, its velocity must be added or subtracted. If it blows obliquely, the correction will evidently equal its velocity multiplied by the cosine of the angle which the direction of the wind makes with the direction of the sound. If the gun be fired at each end of the base in turn, and the means of the times taken, the effect of the wind will be eliminated.

If a watch is not at hand, suspend a pebble to a string (such as a thread drawn from a handkerchief) and count its vibrations. If it be  $39\frac{1}{8}$  inches long, it will vibrate in one second; if  $9\frac{1}{2}$  inches long, in half a second, etc. If its length is unknown at the time, still count its vibrations; measure it subsequently; and then will the time of its vibration, in seconds, =  $\sqrt{\left(\frac{\text{length of string}}{39\frac{1}{8}}\right)}$ .



**33. Angles.** Right angles are those most frequently required in this kind of survey, and they can be estimated by the eye with much accuracy. If other angles are desired, they will be determined by measuring equal distances along the lines which make the angle, and then the line, or chord, joining the ends of these distances, thus forming chain-angles, explained in Article 28.

***Noting the Measurements.***

**34.** The measurements which have been made, whether of lines or of angles, require to be very carefully noted and recorded. Clearness and brevity are the points desired. Different methods of notation are required for each of the systems of surveying which are to be explained, and will therefore be given in their appropriate places.

**DRAWING THE MAP.**

**35.** A Map of a survey represents the lines which bound the surface surveyed, and the objects upon it, such as fences, roads, rivers, houses, woods, hills, etc., in their true relative dimensions and positions. It is a miniature copy of the field, farm, etc., as it would be seen by an eye moving over it; or as it would appear, if, from every point of its irregular surface, plumb-lines were dropped to a level surface under it, forming what is called, in geometrical language, its *horizontal projection*.

**36. Platting.** A *plat* of a survey is a skeleton, or outline map. It is a figure "similar" to the original, having all its angles equal and its sides proportional. Every inch on it represents a foot, a yard, a rod, a mile, or some other length, on the ground; all the measured distances being diminished in exactly the same ratio.

PLATTING is repeating on paper, to a smaller scale, the measurements which have been made on the ground.

Its various operations may therefore be reduced, in accordance with the principles established in this chapter, to two, viz.: drawing a straight line in a given direction and of a given length;

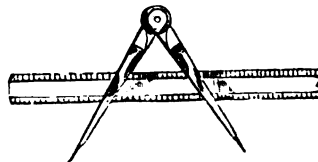


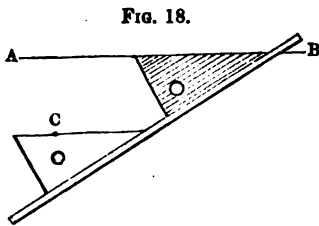
FIG. 17.

and describing an arc of a circle with a radius whose length is also given. The only instruments absolutely necessary for this are a straight ruler and a pair of "dividers" or "compasses." Others, however, are often convenient, and will be now briefly noticed.

**37. Straight Lines.** These are usually drawn by the aid of a straight-edged ruler. But to obtain a very long straight line upon paper, stretch a fine silk thread between any two distant points, and mark in its line various points near enough together to be afterward connected by a common ruler. The thread may also be blackened with burned cork and snapped on the paper, as a carpenter snaps his chalk-line; but this is liable to inaccuracies, from not raising the line vertically.

**38. Arcs.** The arcs of circles used in fixing the position of a point on paper are usually described with compasses, one leg of which carries a pencil-point. A convenient substitute is a strip of pasteboard, through one end of which a fine needle is thrust into the given center, and through a hole in which, at the desired distance, a pencil-point is passed, and can thus describe a circle about the center, the pasteboard keeping it always at the proper distance. A string is a still readier, but less accurate, instrument.

**39. Parallels.** The readiest mode of drawing parallel lines is by the aid of a triangular piece of wood and a ruler. Let A B

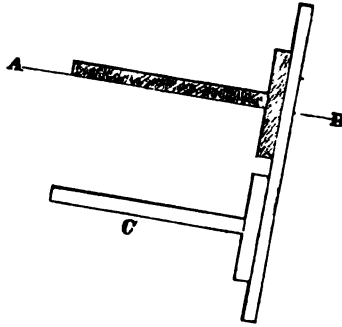


be the line to which a parallel is to be drawn, and C the point through which it must pass. Place one side of the triangle against the line, and place the ruler against another side of the triangle. Hold the ruler firm and immovable, and slide the triangle along it till the side of the triangle which had coincided with the given line passes through the given point. This side will then be parallel to that given line, and a line drawn by it will be the line required.

Another easy method of drawing parallels is by means of a T-

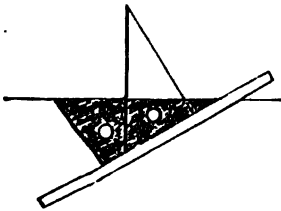
square, an instrument very valuable for many other purposes. It is nothing but a ruler let into a thicker piece of wood, very truly at right angles to it. For this use of it, one side of the cross-piece must be even or "flush" with the ruler. To use it, lay it on the paper so that one edge of the ruler coincides with the given line A B. Place another ruler against the cross-piece, hold it firm, and slide the T-square along till its edge passes through the given point C, as shown by the lower part of the figure. Then draw by this edge the desired line parallel to the given line.

FIG. 19:



**40. Perpendiculars.** These may be drawn by the various problems given in Geometry, but more readily by a triangle which has one right angle. Place the longest side of the triangle on the given line, and place a ruler against a second side of the triangle. Hold the ruler fast, and turn the triangle so as to bring its third side against the ruler. Then will the long side be perpendicular to the given line. By sliding the triangle along the ruler, it may be used to draw a perpendicular from any point of the line, or from any point to the line.

FIG. 20.

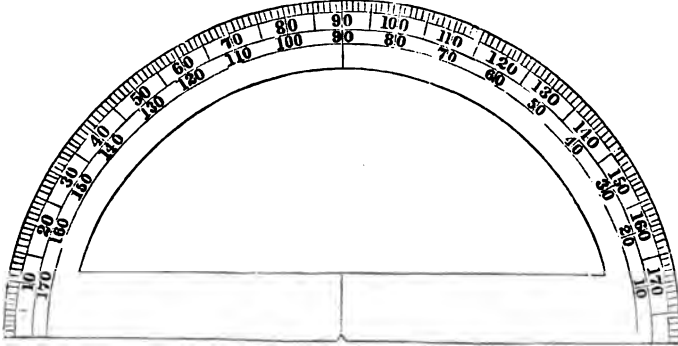


**41. Angles.** These are most easily set out with an instrument called a Protractor. This is usually a semicircle of brass, as in the figure, with its semi-circumference divided into 180 equal parts, or degrees, and numbered in both directions. It is, in fact, a miniature of the instrument (or of half of it) with which the angles have been measured. To lay off any angle at any point of a straight line, place the protractor so that its straight side, the diameter of the semicircle, is on the given line, and the middle of this diameter, which is marked by a notch, is at the given point. With a

needle or sharp pencil make a mark on the paper at the required number of degrees, and draw a line from the mark to the given point.

Sometimes the protractor has an arm turning on its center and

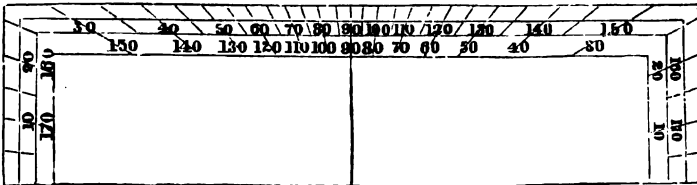
FIG. 21.



extending beyond its circumference, so that a line can be at once drawn by it when it is set to the desired angle. A Vernier scale is sometimes added to it to increase its precision.

A Rectangular Protractor is sometimes used, the divisions of degrees being engraved along three edges of a plane scale. The

FIG. 22.



semicircular one is preferable. The objection to the rectangular protractor is that the division corresponding to a degree is very unequal on different parts of the scale, being usually two or three times as great at its ends as at its middle.

A Protractor embracing an entire circle, with arms carrying verniers, is also sometimes employed, for the sake of greater accuracy.

**42. Drawing to Scale.** The operation of drawing on paper lines whose length shall be a half, a quarter, a tenth, or any other fraction of the lines measured on the ground, is called "Drawing to Scale."

To set off on a line any given distance to any required scale, determine the number of chains or links which each division of the scale of equal parts shall represent. Divide the given distance by this number. The quotient will be the number of equal parts to be taken in the dividers and to be set off.

For example, suppose the scale of equal parts to be a common carpenter's rule divided into inches and eighths. Let the given distance be twelve chains, which is to be drawn to a scale of two chains to an inch. Then six inches will be the distance to be set off. If the given distance had been twelve chains and seventy-five links, the distance to be set off would have been six inches and three eighths, since each eighth of an inch represents twenty-five links.

If the desired scale were three chains to an inch, each eighth of an inch would represent  $37\frac{1}{2}$  links; and the distance of 1,275 links would be represented by thirty-four eighths of an inch, or  $4\frac{1}{4}$  inches.

A similar process will give the correct length to be set off for any distance to any scale.

If the scale used had been divided into inches and tenths, as is much the most convenient, the above distances would have become on the former scale  $6\frac{3}{10}$  inches, or nearly  $6\frac{1}{4}$  inches; and on the latter scale  $4\frac{3}{10}$  inches, coming midway between the second and third tenth of an inch.

*Conversely*, to find the real length of a line drawn on paper to any known scale, reverse the preceding operation. Take the length of the line in the dividers, apply it to the scale, and count how many equal parts it includes. Multiply their number by the number of chains or links which each represents, and the product will be the desired length of the line on the ground.

This operation and the preceding one are greatly facilitated by the use of the scales to be described in Art. 47.

**43. Scales.** The choice of the scale to which a plat should be drawn—that is, how many times smaller its lines shall be than those which have been measured on the ground—is determined by several considerations. The chief one is that it shall be just large enough to express clearly all the details which it is desirable to know. A Farm Survey would require its plat to show every field and building. A State Survey would show only the towns, rivers, and leading roads. The size of the paper at hand will also limit the scale to be adopted. If the content is to be calculated from the plat, that will forbid it to be less than 3 chains to 1 inch.

Scales are named in various ways. *They should always be expressed fractionally*—i. e., they should be so named as to indicate what fractional part of the real line measured on the ground, the representative line drawn on the paper, actually is. When custom requires a different way of naming the scale, both should be given. It would be still better if the denominator could always be some power of 10, or at least some multiple of 2 and 5, such as  $\frac{1}{1000}$ ,  $\frac{1}{10000}$ ,  $\frac{1}{100000}$ , etc. For convenience in printing, these may be written thus: 1 : 500, 1 : 1,000, 1 : 2,000, 1 : 2,500, etc.

Plats of *Farm Surveys* are usually named as being so many chains to an inch.

Maps of *Surveys of States* are generally named as being made to a scale of so many miles to an inch.

Maps of *Railroad Surveys* are said to be so many feet to an inch, or so many inches to a mile.

**44. Farm Surveys.** If these are of small extent, two chains to one inch (which is  $= \frac{1}{2 \times 66 \times 12} = \frac{1}{1584} = 1 : 1,584$ ) is convenient.

A scale of one chain to one inch (1 : 792) is useful for plans of buildings. Three chains to one inch (1 : 2,376) is suitable for larger farms. It is the scale prescribed by the English Tithe Commissioners for their first-class maps.

In France, the *Cadaastre* Surveys are lithographed on a scale about equivalent to this, being 1 : 2,500. The original plans are drawn to a scale of 1 : 5,000. Plans for the division of property are made on the former scale. When the district exceeds 3,000 acres, the scale is 1 : 10,000. When it exceeds 7,500 acres, the scale is 1 : 20,000. A common scale in France for small surveys is 1 : 1,000, about  $1\frac{1}{2}$  chain to 1 inch.

**45. State Surveys.** On these surveys smaller scales are necessarily employed.

On the *United States Coast and Geodetic Survey* all the scales are expressed fractionally and decimally. "The surveys are generally platted originally on a scale of one to ten or twenty thousand, but in some instances the scale is larger or smaller.

"These original surveys are reduced for engraving and publication, and, when issued, are embraced in three general classes: 1, small harbor-charts; 2, charts of bays and sounds; and, 3, the General Coast Charts.

"The scales of the first class vary from 1: 10,000 to 1: 60,000, according to the nature of the harbor and the different objects to be represented.

"Where there are many shoals, rocks, or other objects, as in Nantucket Harbor and Hell Gate, or where the importance of the harbor makes it necessary, a larger scale of 1: 5,000, 1: 10,000, and 1: 20,000 is used. But where, from the size of the harbor or its ease of access, a smaller one will point out every danger with sufficient exactness, the scales of 1: 40,000 and 1: 60,000 are used, as in the case of New Bedford Harbor, Cat and Ship Island Harbor, New Haven, etc.

"The scale of the second class, in consequence of the large areas to be represented, is usually fixed at 1: 80,000, as in the case of New York Bay, Delaware Bay and River. Preliminary charts, however, are issued of various scales from 1: 80,000 to 1: 200,000.

"Of the third class, the scale is fixed at 1: 400,000 for the General Chart of the Coast from Gay Head to Cape Henlopen, although considerations of the proximity and importance of points on the coast may change the scales of charts of other portions of our extended coast."

The National Survey of *Great Britain* is called, from the corps employed on it, the "Ordnance Survey."

The "Ordnance Survey" of the southern counties of England was platted on a scale of 2 inches to 1 mile (1: 31,680), and reduced for publication to that of 1 inch to a mile (1: 63,360). The scale of 6 inches to a mile (1: 10,560) was adopted for the northern counties of England and for the southern counties of Scotland. The same scale was employed for plating and engraving in outline the "Ordnance Survey" of Ireland. But a map on a scale of 1 inch to 1 mile (1: 63,360) is now published, the former scale rendering the maps too unwieldy and cumbersome for consultation.

The Ordnance Survey of Scotland was at first platted on a scale of 6 inches to 1 mile (1: 10,560). That scale has since been abandoned, and it is now platted on a scale of 2 inches to 1 mile (1: 31,680), and the general maps are made to only half that scale.

The Ordnance Survey scale for the maps of London and other large towns is 5 feet to 1 mile (1: 1,056), or  $1\frac{1}{2}$  chain to 1 inch.

In the "Surveys under the Public Health Act" of England, the scale for the general plan is 2 feet to 1 mile (1: 2,640); and for the detailed plan 10 feet per mile (1: 528), or  $\frac{1}{2}$  of a chain per inch.

The Government Survey of *France* is platted to a scale of 1: 20,000. Copies are made to 1: 40,000; and the maps are engraved to a scale of 1: 80,000, or about  $\frac{1}{4}$  of an inch to 1 mile.

Cassini's famous map of France was on a scale of 1: 86,400.

The French War Department employ the scales of 1: 10,000, 1: 20,000, 1: 40,000, and 1: 80,000 for the topography of France.

**46. Railroad Surveys.** For these the New York Railroad Law of 1880 directs the horizontal scale of maps which are to be filed in the State Engineer's Office to be 500 feet to  $\frac{1}{8}$  of a foot ( $= 1: 5,000$ ), and vertical scale for profiles to be 100 feet to  $\frac{1}{8}$  of a foot ( $= 1: 1,000$ ).

For the New York Canal Maps a horizontal scale of 2 chains to 1 inch (1: 1,584), and a vertical scale of 20 feet to 1 inch, are employed.

The parliamentary "standing orders" prescribe the plans of railroads, prepared for parliamentary purposes, to be made on a scale of not less than 4 inches to the mile (1: 15,840); and the enlarged portions (as of gardens, court-yards, etc.) to be on a scale not smaller than 400 feet to the inch (1: 4,800). Accordingly, the practice of English railway engineers is to draw the whole plan to a scale of 6 chains, or 393 feet to the inch (1: 4,752), as being just within the parliamentary limits.

In France, the engineers of "Bridges and Roads" (Corps des Ponts et Chaussées) employ for the general plan of a road a scale of 1: 5,000, and for appropriations, 1: 500.

**In the United States Engineer Service** the following plans are prescribed: General plans of buildings, 1 inch to 10 feet (1: 120).

Maps of grounds, with horizontal curves one foot apart, 1 inch to 50 feet (1: 600).

Topographical maps, one mile and a half square, 2 feet to 1 mile (1: 2,640).

Do., comprising three miles square, 1 foot to one mile (1: 5,280).

Do., between four and eight miles square, 6 inches to one mile (1: 10,560).

Do., comprising nine miles square, 4 inches to one mile (1: 15,840).

Maps not exceeding 24 miles square, 2 inches to one mile (1: 31,680).

Maps comprising 50 miles square, 1 inch to one mile (1: 63,360).

Maps comprising 100 miles square,  $\frac{1}{2}$  inch to one mile (1: 126,720).

Surveys of roads, canals, etc., 1 inch to 50 feet (1: 600).

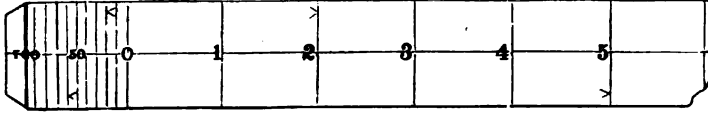
**47.** The most convenient scales of equal parts are those of box-wood, or ivory, which have a *fiducial* or feather edge, along which they are divided, so that distances can be at once marked off from this edge, without requiring to be taken off with the dividers; or the length of a given line can be at once read off. Box-wood is preferable to ivory, as much less liable to warp, or to vary in length with changes in the moisture in the air.

The student can, however, make for himself platting-scales of drawing-paper, or Bristol board. Cut a straight strip of this material, about an inch wide. Draw a line through its middle, and set



off on it a number of equal parts, each representing a chain to the desired scale. Subdivide the left-hand division into ten equal

FIG. 23.



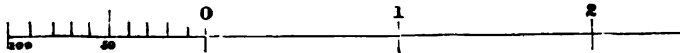
parts, each of which will therefore represent ten links to this scale. Through each point of division on the central line, draw (with the T-square) perpendiculars extending to the edges, and the scale is made. It explains itself. The above figure is a scale of 2 chains to 1 inch. On it the distance 220 links would extend between the arrow-heads above the line in the figure; 560 links extend between the lower arrow-heads, etc.

A paper scale has the great advantage of varying less from a plat which has been made by it, in consequence of changes in the weather, than any other. The mean of many trials showed the difference between such a scale and drawing-paper, when exposed alternately to the damp open atmosphere, and to the air of a warm dry room, to be equal to  $\cdot 005$ , while that between box-wood scales and the paper was  $\cdot 012$ , or nearly  $2\frac{1}{2}$  times as much. The difference with ivory would have been even greater.

Some of the more usual platting-scales are here given in their actual dimensions.

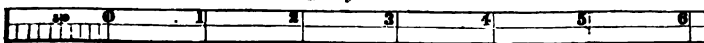
In these five figures, different methods of drawing the scales

FIG. 24.—Scale of 1 chain to 1 inch.



have been given, but each method may be applied to any scale. The first and second, being the most simple, are generally the best. In the third the subdivisions are made by a diagonal line: the dis-

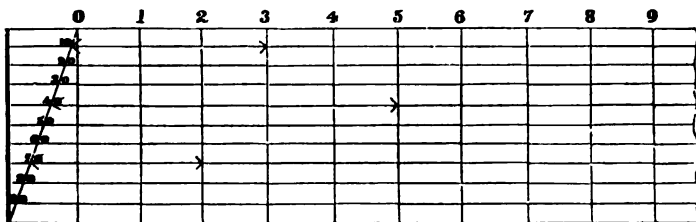
FIG. 25.—Scale of 2 chains to 1 inch



tances between the various pairs of arrow-heads, beginning with the uppermost, are respectively 310, 540, and 270 links.

In the fourth figure, the distances between the arrow-heads are respectively 310, 270, and 540 links.

FIG. 26.—Scale of 3 chains to 1 inch.



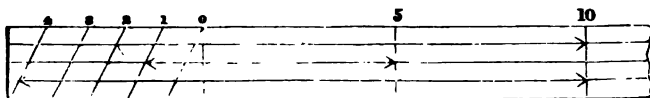
In the fifth figure, the scale of 5 chains to 1 inch is subdivided diagonally to only every quarter-chain, or 25 links. The distance

FIG. 26'.—Scale of 4 chains to 1 inch.



between the upper pair of arrow-heads on it is  $12\frac{1}{4}$  chains, or 12.25; between the next pair of arrow-heads it is 6.50; and between the lower pair 14.75.

FIG. 27.—Scale of 5 chains to 1 inch.



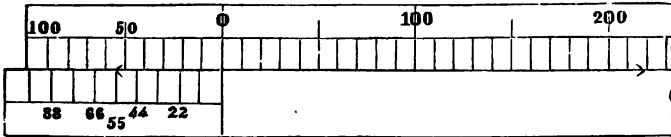
A diagonal scale for dividing an inch, or half an inch, into 100 equal parts, is found on the "plain scale" in every case of instruments.

**48. Vernier Scale.** This is an ingenious substitute for the diagonal scale. The one given in the following figure divides an inch into 100 equal parts, and, if each inch be supposed to represent a chain, it gives single links.

Make a scale of an inch divided into tenths, as in the upper scale of the above figure. Take in the dividers eleven of these divisions, and set off this distance from the 0 of the scale to the

left of it. Divide the distance thus set off into 10 equal parts. Each of them will be one tenth of eleven tenths of one inch, i. e.,

FIG. 28.



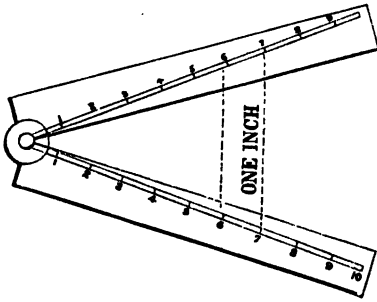
eleven hundredths, or a tenth and a hundredth, and the first division on the short, or vernier scale, will overlap, or be longer than the first division on the long scale, by just *one* hundredth of an inch; the second division will overlap *two* hundredths, and so on. The principle will be more fully developed in treating of "Verniers."

Now, suppose we wish to take off from this scale 275 hundredths of an inch. To get the last figure, we must take five divisions on the lower scale, which will be 55 hundredths, for the reason just given; 220 will remain, which are to be taken from the upper scale, and the entire number will be obtained at once by extending the dividers between the arrow-heads in the figure from 220 on the upper scale (measuring along its lower side) to 55 on the lower scale; 254 would extend from 210 on the upper scale to 44 on the lower; 318 would extend from 230 on the upper scale to 88 on the lower. Always begin then with subtracting 11 times the last figure from the given number; find the remainders on the upper scale, and the number subtracted on the lower scale.

**49.** A plat is sometimes made by a nominally reduced scale in the following manner: Suppose that the scale of the plat is to be ten chains to one inch, and that a diagonal scale of inches, divided into tenths and hundredths, is the only one at hand. By dividing all the distances by ten, this scale can then be used without any further reduction. But if the content is measured from the plat to the same scale, in the manner explained in the next chapter, the result must be multiplied by 10 times 10. This is called by old surveyors "raising the scale," or "restoring true measure."

**50. Sectoral Scales.** The *Sector* (called by the French "Compass of Proportion") is an instrument sometimes convenient for obtaining a scale of equal parts. It is in two portions, turning on a hinge, like a carpenter's pocket-rule. It contains a great number of scales, but the one intended for this use is lettered at its

FIG. 29.



ends L in English instruments, and consists of two lines running from the center to the ends of the scale, and each divided into ten equal parts, each of which is again subdivided into ten, so that each leg of the scale contains 100 equal parts. To illustrate its use, suppose that a scale of 7 chains to 1 inch is re-

quired. Take 1 inch in the dividers, and open the sector till this distance will just reach from the 7 on one leg to the 7 on the other. The sector is then "set" for this scale, and the angle of its opening must not be again changed. Now let a distance of 580 links be required. Open the dividers till they reach from 58 to 58 on the two legs, as in the dotted line in the figure, and it is the required distance. Again, suppose that a scale of  $2\frac{1}{2}$  chains to 1 inch is desired. Open the sector so that 1 inch shall extend from 25 to 25. Any other scale may be obtained in the same manner.

Conversely, the length of any known line to any desired scale can thus be readily determined.

**51.** Whatever scale may be adopted for platting the survey, it should be drawn on the map, both for convenience of reference and in order that the contraction and expansion caused by changes in the quantity of moisture in the atmosphere may affect the scale and the map alike. When the drawing-paper has been wet and glued to a board, and cut off when the map is completed, its contractions have been found by many observations to average from one fourth to one half per cent on a scale of 3 chains to an inch

(1 : 2,376), which would therefore require an allowance of from one half perch to one perch per acre.

A scale made as directed in Art. 47, if used to make a plat on unstretched paper, and then kept with the plat, will answer nearly the same purpose.

Such a scale may be attached to a map by slipping it through two or three cuts in the lower part of the sheet, and will be a very convenient substitute for a pair of dividers in measuring any distance upon it.

**52. Scale omitted.** It may be required to find the unknown scale to which a given map has been drawn, its superficial content being known. Assume any convenient scale, measure the lines of the map by it, and find the content by the methods to be given in the next chapter, proceeding as if the assumed scale were the true one. Then make this proportion, founded on the geometrical principle that the areas of similar figures are as the squares of their corresponding sides : *As the content found is to the given content, so is the square of the assumed scale to the square of the true scale.*

#### CALCULATING THE CONTENT.

**53.** The CONTENT of a piece of ground is its superficial *area*, or the number of square feet, yards, acres, or miles which it contains.

**54. Horizontal Measurement.** All ground, however inclined or uneven its surface may be, should be measured horizontally, or as if brought down to a horizontal plane, so that the surface of a hill, thus measured, would give the same content as the level base on which it may be supposed to stand, or as the figure which would be formed on a level surface beneath it by dropping plumb-lines from every point of it.

This method of procedure is required for both geometrical and social reasons.

*Geometrically*, it is plain that this horizontal measurement is absolutely necessary for the purpose of obtaining a correct plat. In Fig. 30, let A B C D and B C E F be two square lots of ground,

platted horizontally. Suppose the ground to slope in all directions from the point C, which is the summit of a hill. Then the lines

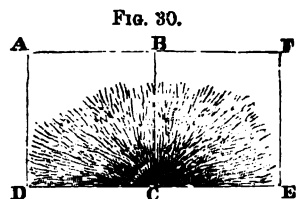


FIG. 30.

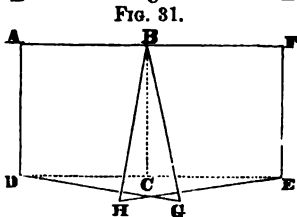


FIG. 31.

BC, DC, measured on the slope, are longer than if measured on a level, and the field ABCD, of Fig. 30, platted with these long lines, would take the shape ABGD in Fig. 31; and the field BCEF, of Fig. 30, would become BHEF, of Fig. 31. The two adjoining fields would thus overlap each other; and the same difficulty would occur in every case of platting any two adjoining fields by the measurements made on the slope.

Let us suppose another case, more simple than would ever occur in practice, that of a three-sided field, of equal sides, and composed of three portions, each sloping down uniformly (at the rate of one to one) from one point in the center, as in Fig. 32. Each slope being accurately platted, the three could not come together, but would be separated as in Fig. 33.



FIG. 32.

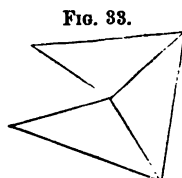


FIG. 33.

We have here taken the most simple cases, those of uniform slopes. But with the common irregularities of uneven ground, to measure its actual surface would not only be improper, but impossible.

In the *social* aspect of this question, the horizontal measurement is justified by the fact that no more houses can be built on a hill than could be built on its flat base; and that no more trees, corn, or other plants, which shoot up vertically, can grow on it; as is represented by the vertical lines in the figure.\* Even if a side-hill

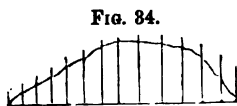


FIG. 34.

\* This question is more than two thousand years old, for Polybius writes: "Some even of those who are employed in the administration of states, or placed at the head

should produce more of certain creeping plants, the increased difficulty in their cultivation might perhaps balance this. For this reason the surface of the soil thus measured is sometimes called *the productive base* of the ground.

Again, a piece of land containing a hill and a hollow, if measured on the surface, would give a larger content than it would after the hollow had been filled up by the hill, while it would yet really be of greater value than before.

Horizontal measurement is called the "Method of Cultellation," and superficial measurement the "Method of Development." \*

An act of the State of New York prescribes that "the acre, for land-measure, shall be measured horizontally."

**55. Unit of Content.** The *Acre* is the unit of land-measurement. It contains 4 Roods. A *Rood* contains 40 Perches. A *Perch* is a square Rod; otherwise called a Pole. A *Rod* is  $5\frac{1}{2}$  yards, or  $16\frac{1}{2}$  feet.

Hence, 1 Acre = 4 Roods = 160 Perches = 4,840 square yards = 43,560 square feet.

One square mile =  $5,280 \times 5,280$  feet = 640 acres.

Since a chain is 66 feet long, a square chain contains 4,356 square feet; and, consequently, *ten square chains make one acre.* †

The French units of land-measure are the *Are* = 100 square *Metres* = 0.0247 acre = one fortieth of an acre, nearly; and the *Hectare* = 100 *Ares* = 2.47 acres, or nearly two and a half. Their old land-measures were the "Arpent of Paris," containing 36,800 square feet; and the "Arpent of Waters and Woods," containing 55,000 square feet.

**56.** When the content of a piece of land (obtained by any of the methods to be explained presently) is given in square links, as is

of armies, imagine that unequal and hilly ground will contain more houses than a surface which is flat and level. This, however, is not the truth. For, the houses, being raised in a vertical line, form right angles, not with the declivity of the ground, but with the flat surface which lies below, and upon which the hills themselves also stand."

\* The former from *cultellum*, a knife, as if the hills were sliced off; the latter so named because it strips off or unfolds, as it were, the surface.

† Let the young student beware of confounding 10 square chains with 10 chains square. The former make one acre; the latter space contains ten acres.

customary, cut off four figures on the right (i. e., divide by 10,000) to get it into square chains and decimal parts of a chain ; cut off the right-hand figure of the *square chains*, and the remaining figures will be *Acres*. Multiply the remainder by 4, and the figure, if any, outside of the new decimal-point will be *Roods*. Multiply the remainder by 40, and the outside figures will be *Perches*. The nearest round number is usually taken for the *Perches* ; fractions less than a half-perch being disregarded.\*

Thus, 86·22 square chains = 8 Acres 2 Roods 20 Perches.

Also, 64·1818 do. = 6 A. 1 R. 27 P.

“ 43·7564 do. = 4 A. 1 R. 20 P.

**57. Chain Correction.** When a survey has been made, and the plat has been drawn, and the content calculated ; and afterward the chain is found to have been incorrect, too short or too long, the true content of the land may be found by this proportion : *As* the square of the length of the standard given by the incorrect chain *is to* the square of the true length of the standard, *so is* the calculated content *to* the true content. Thus, suppose that the chain used had been so stretched that the standard distance measured by it appears to be only 99 links long ; and that a square field had been measured by it, each side containing 10 of these long chains, and that it had been so platted. This plat, and therefore the content calculated from it, will be smaller than it should be, and the correct content will be found by the proportion  $99^2 : 100^2 :: 100 \text{ square chains} : 102\cdot03 \text{ square chains}$ . If the chain had been stretched so as to be 101 *true* links long, as found by comparing it with a correct chain, the content would be given by this proportion :  $100^2 : 101^2 :: 100 \text{ square chains} : 102\cdot01 \text{ square chains}$ . In the former case, the elongation of the chain was  $1\frac{1}{9}$  true links ; and  $100^2 : (101\frac{1}{9})^2 :: 100 \text{ square chains} : 102\cdot03 \text{ square chains}$ .

**58. Boundary-Lines.** The lines which are to be considered as bounding the land to be surveyed are often very uncertain, unless specified by the title-deeds.

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\* To reduce square yards to acres, instead of dividing by 4,840, it is easier, and very nearly correct, to multiply by 2, cut off four figures, and add to this product one third of one tenth of itself.



If the boundary be a brook, the middle of it is usually the boundary-line. On tide-waters, the land is usually considered to extend to low-water mark.

Where hedges and ditches are the boundaries of fields, as is almost universally the case in England, the dividing line is generally the top edge of the ditch farthest from the hedge, both hedge and ditch belonging to the field on the hedge side. This varies, however, with the customs of the locality. From three to six feet from the roots of the quick-wood of the hedges are allowed for the ditches.

### *Methods of Calculation.*

**59.** The various methods employed in calculating the content of a piece of ground may be reduced to four, which may be called *Arithmetical, Geometrical, Instrumental, and Trigonometrical.*

**60. FIRST METHOD.—ARITHMETICALLY.** *From direct measurements of the necessary lines on the ground.*

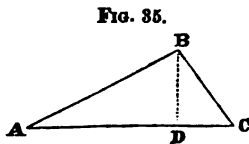
The figures to be calculated by this method may be either the shapes of the fields which are measured, or those into which the fields can be divided by measuring various lines across them.

The familiar rules of mensuration for the principal figures which occur in practice will be now briefly enunciated.

**61. Rectangles.** If the piece of ground be rectangular in shape, its content is found by multiplying its length by its breadth.

**62. Triangles.** When the given quantities are one side of a triangle and the perpendicular distance to it from the opposite angle, the content of the triangle is equal to half the product of the side and the perpendicular.

When the given quantities are the three sides of the triangle, add together the three sides and divide the sum by 2; from this half sum subtract each of the three sides in turn; multiply together the half sum and the three remainders; take the square root of the product; it is the content required. If the sides of the triangle be designated by  $a, b, c$ , and their sum by  $s$ , this rule will give its area =  $\sqrt{[\frac{1}{2}s (\frac{1}{2}s - a) (\frac{1}{2}s - b) (\frac{1}{2}s - c)]}$ .



When two sides of a triangle and the included angle are given, its content equals half the product of its sides into the sine of the included angle. Designating the angles of the triangle by

the capital letters A, B, C, and the sides opposite them by the corresponding small letters  $a, b, c$ , the area =  $\frac{1}{2} b c \sin. A$ .

When one side of a triangle and the adjacent angles are given, its content equals the square of the given side multiplied by the sines of each of the given angles, and divided by twice the sine of the sum of these angles. Using the same symbols as before, the area =  $a^2 \frac{\sin. B \cdot \sin. C}{2 \sin. (B + C)}$ .

When the three angles of a triangle and its altitude are given, its area, referring to the above figure, =  $\frac{1}{2} B D^2 \cdot \frac{\sin. B}{\sin. A \cdot \sin. C}$ .

**63. Parallelograms**, or four-sided figures whose opposite sides are parallel. The content of a Parallelogram equals the product of one of its sides by the perpendicular distance between it and the side parallel to it.

**64. Trapezoids**, or four-sided figures, two opposite sides of which are parallel. The content of a Trapezoid equals half the product of the sum of the parallel sides by the perpendicular distance between them.

If the given quantities are the four sides  $a, b, c, d$ , of which  $b$  and  $d$  are parallel; then, making  $q = \frac{1}{2} (a + b + c + d)$ , the area of the trapezoid will =  $\frac{b + d}{b - d} \sqrt{[q (q - a) (q - c) (q - b + d)]}$ .

When two parallel sides,  $b$  and  $d$ , and a third side,  $a$ , are given, and also the angle  $C$ , which this third side makes with one of the parallel sides, then the content of the trapezoid =  $\frac{b + d}{2} \cdot a \cdot \sin. C$ .

**65. Trapeziums**; four-sided figures, none of whose sides are parallel.

A very gross error, often committed as to this figure, is to take the average, or half sum of its opposite sides, and multiply them together for the area: thus, assuming the trapezium to be equivalent to a rectangle with these averages for sides.

In practical surveying, it is usual to measure a line across it from corner to corner, thus dividing it into two triangles, whose sides are known, and which can therefore be calculated by Art. 62.

When two opposite sides, and all the angles are given, take one side and its adjacent angles (or their supplements, when their sum exceeds  $180^\circ$ ), consider them as belonging to a triangle, and find its area by the second formula in Art. 62. Do the same with the other side and its adjacent angles. The difference of the two areas will be the area of the quadrilateral.

When three sides and their two included angles are given, multiply together the sine of one given angle and its adjacent sides. Do the same with the sine of the other given angle and its adjacent sides. Multiply together the two opposite sides and the sine of the supplement of the sum of the given angles. Add together the first two products, and add also the last product, if the sum of the given angles is more than  $180^\circ$ , or subtract it if this sum be less, and take half the result. Calling the given sides  $p, q, r$ , and the angle

between  $p$  and  $q = A$ ; and the angle between  $q$  and  $r = B$ ; the area of the quadrilateral

$$= \frac{1}{2} [p \cdot q \sin. A + q \cdot r \sin. B \pm p \cdot r \sin. (180^\circ - A - B)].$$

When the four sides and the sum of any two opposite angles are given, proceed thus: Take half the sum of the four given sides, and from it subtract each side in turn. Multiply together the four remainders, and reserve the product. Multiply together the four sides. Take half their product, and multiply it by the cosine of the given sum of the angles increased by unity. Regard the sign of the cosine. Subtract this product from the reserved product, and take the square root of the remainder. It will be the area of the quadrilateral.

When the four sides and the angle of intersection of the diagonals of the quadrilateral are given, square each side; add together the squares of the opposite sides; take the difference of the two sums; multiply it by the tangent of the angle of intersection, and divide by four. The quotient will be the area.

When the diagonals of the quadrilateral and their included angle are given, multiply together the two diagonals and the sine of their included angle, and divide by two. The quotient will be the area.

**66. SECOND METHOD.—GEOMETRICALLY.** From measurements of the necessary lines upon the plat.

**67. Division into Triangles.** The plat of a piece of ground having been drawn from the measurements made by any of the methods which will be hereafter explained, lines may be drawn upon the plat so as to divide it into a number of triangles. Four ways of doing this are shown in the figures, viz.: by drawing lines

FIG. 36.

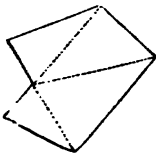


FIG. 37.

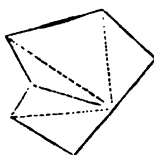


FIG. 38.

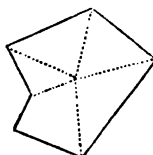
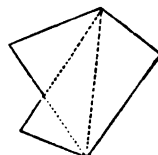


FIG. 39.



from one corner to the other corners; from a point in one of the sides to the corners; from a point inside of the figure to the corners; and from various corners to other corners. The last method is usually the best. The lines ought to be drawn so as to make the triangles as nearly equilateral as possible.

One side of each of these triangles, and the length of the perpendicular let fall upon it, being then measured, the content of

these triangles can be at once obtained by multiplying their base by their altitude, and dividing by two.

The easiest method of getting the length of the perpendicular, without actually drawing it, is to set one point of the dividers at the angle from which a perpendicular is to be let fall, and to open and shut their legs till an arc described by the other point will just touch the opposite side.

Otherwise, a platting scale may be placed so that the zero-point of its edge coincides with the angle, and one of its cross-lines coincides with the side to which a perpendicular is to be drawn. The length of the perpendicular can then at once be read off.

The method of dividing the plat into triangles is the one most commonly employed by surveyors for obtaining the content of a survey, because of the simplicity of the calculations required. Its correctness, however, is dependent on the accuracy of the plat, and on its scale, which should be as large as possible. Three chains to an inch is the smallest scale allowed by the English Tithe Commissioners for plats from which the content is to be determined.

In calculating in this way the content of a farm, and also of its separate fields, the sum of the latter ought to equal the former. A difference of one three-hundredth ( $\frac{1}{300}$ ) is considered allowable.

Some surveyors measure the perpendiculars of the triangles by a scale half of that to which the plat is made. Thus, if the scale of the plat be two chains to the inch, the perpendiculars are measured with a scale of one chain to the inch. The product of the base by the perpendicular thus measured, gives the area of the triangle at once, without its requiring to be divided by two.

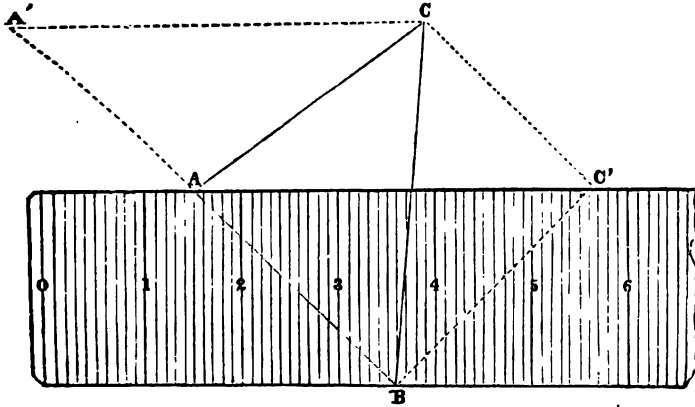
Another way of attaining the same end, with less danger of mistakes, is to construct a *new* scale of equal parts, longer than those by which the plat was made in the ratio  $\sqrt{2} : 1$ ; or  $1.414 : 1$ . When the base and perpendicular of a triangle are measured by this new scale, and then multiplied together, the product will be the content of the triangle, without any division by two. In this method there is the additional advantage of the greater size and consequent greater distinctness of the scale.

When the measurement of a plat is made some time after it has been drawn, the paper will very probably have contracted or expanded so that the scale used will not exactly apply. In that case a correction is necessary. Measure very precisely the present length of some line on the plat, of known length originally. Then make this proportion: *As the square of the present length of this line is to the square of its original length, so is the content obtained by the present measurement to the true content.*

**68. Graphical Multiplication.** Prepare a strip of drawing-paper, of a width exactly equal to two chains on the scale of the plat; i. e., one inch wide, as in the figure, for a scale of two chains to one inch; two thirds of an inch wide for a scale of three chains; half an inch for four chains, and so on. Draw perpendicular lines across the paper at distances representing one tenth

of a chain on the scale of the triangle to be measured, thus making a platting scale. Apply it to the triangle so that one edge of the scale shall pass through one corner, A, of the triangle, and the other edge through another corner, B; and note very precisely what divisions of the scale are at these points. Then slide the scale in such a way that the points of the scale which had coincided with A and B shall always remain on the line BA produced, till the edge arrives at the point C. Then will A'C—that is, the distance, or

**FIG. 40.**



**number of divisions on the scale, from the point to which the division A on the scale has arrived, to the third corner of the triangle—express the area of the triangle A B C in square chains.**

For, from O draw a parallel to AB, meeting the edge of the scale in C', and draw C'B. Then the given triangle  $ABC = ABC'$ . But the area of this last triangle =  $A'O$  multiplied by half the width of the scale, i. e.,  $= A'C' \times 1 = A'C'$ . But, because of the parallels,  $A'O = A'C'$ , therefore the area of the given triangle  $ABC = A'C'$ ; i. e., it is equal in square chains to the number of linear chains read off from the scale. This ingenious operation is due to *M. Cousinery*.

**69. Division into Trapezoids.** A line may be drawn across the field, as in Fig. 41, and perpendiculars drawn to it. The field

**FIG. 41.**

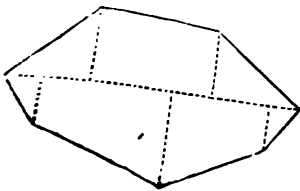
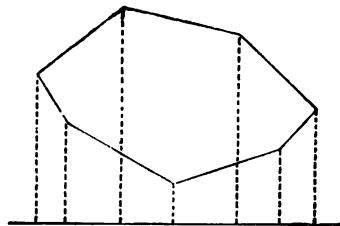


**FIG. 42.**

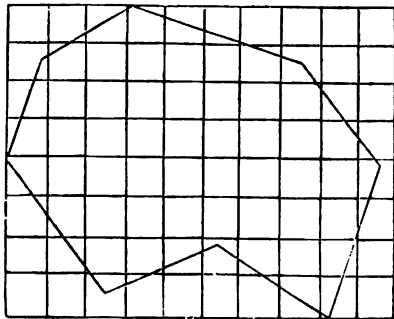


will thus be divided into trapezoids (excepting a triangle at each end), and their content can be calculated by Art. 64.

Otherwise : a line may be drawn outside of the figure, and perpendiculars to it be drawn from each angle. In that case the difference between the trapezoids formed by lines drawn to the outer angles of the figure, and those drawn to the inner angles, will be the content.

**70. Division into Squares.** Two sets of parallel lines, at right angles to each other, one chain apart (to the scale of the plat) may be drawn over the plat, so as to divide it into squares, as in the figure. The

FIG. 43.



number of squares which fall within the plat represent so many square chains; and the triangles and trapezoids which fall outside of these may then be calculated and added to the entire square chains which have been counted.

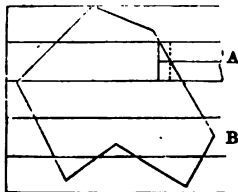
Instead of drawing the parallel lines on the plat, they may better be drawn on a piece of transparent "tracing-paper," which is simply laid upon the plat, and the squares counted as before. The same pa-

per will answer for any number of plats drawn to the same scale. This method is a valuable and easy check on the results of other calculations.

To calculate the fractional parts, prepare a piece of tracing-paper, or glass, by drawing on it one square of the same size as a square of the plat, and subdividing it, by two sets of ten parallels at right angles to each other, into hundredths. This will measure the fractions remaining from the former measurement, as nearly as can be desired.

**71. Division into Parallelograms.** Draw a series of parallel lines across the plat at equal distances depending on the scale. Thus, for a plat made to a scale of 2 chains to 1 inch, the distance between the parallels should be  $2\frac{1}{2}$  inches; for a scale of 3 chains to 1 inch,  $1\frac{1}{2}$  inch; for a scale of 4 chains to 1 inch,  $\frac{5}{8}$  inch; for a scale of 5 chains to 1 inch,  $\frac{4}{10}$  inch; and for any scale, make the distance between the parallels that fraction of an inch which would be expressed by 10 divided by the square of the number of chains to the inch. Then apply a common inch scale, divided on the edge into tenths, to these parallels; and every inch

FIG. 44.



in length of the spaces included between each pair of them will be an acre, and every tenth of an inch will be a square chain.

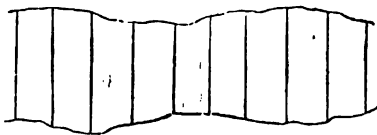
For, calling the number of chains to the inch,  $= n$ , and making the width between the parallels  $\frac{10}{n^2}$  inch, this width will represent  $\frac{10}{n^2} \times n = \frac{10}{n}$  chains; and as the inch length represents  $n$  chains, their product,  $\frac{10}{n} \times n = 10$  square chains  $= 1$  acre.

To measure the triangles at the ends of the strips between the parallels, prepare a piece of glass, or stout tracing-paper, of a width equal to the width between the parallels, and draw a line through its middle longitudinally. Apply it to the oblique line at the end of the space between two parallels, and it will bisect the line, and thus reduce the triangle to an equivalent rectangle, as at A in the figure. When an angle occurs between two parallels, as at B in the figure, the fractional part may be measured by any of the preceding methods.

A somewhat similar method is much used by some surveyors, particularly in Ireland—the plat being made on a scale of 5 chains to 1 inch, parallel lines being drawn on it, half an inch apart, and the distances along the parallels being measured by a scale, each large division of which is  $\frac{1}{16}$  inch in length. Each division of this scale indicates an acre; for it represents 4 chains, and the distance between the parallels is  $2\frac{1}{2}$  chains. This scale is called the “Scale of Acres.”

**72. Addition of Widths.** When the lines of the plat are very irregularly curved, as in the figure, draw across it a number of equidistant lines, as near together as the case may seem to require. Take a straight-edged piece of paper, and apply one edge of it to the middle of the first space, and mark its length from one end; apply the same edge to the middle of the next space, bringing the mark just made to one end, and making another mark at the end of the additional length; so go on, adding the length of each space to the previous ones. When all have been thus measured, the total length, multiplied by the uniform width, will give the content.

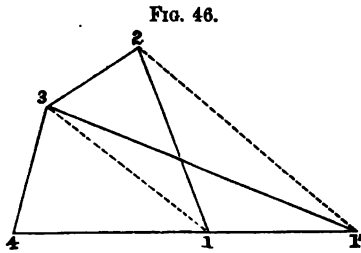
FIG. 45.



**73. THIRD METHOD.—INSTRUMENTALLY.** *By performing certain instrumental operations on the plat.*

**74. Reduction of a many-sided figure to a single equivalent triangle.** Any plane figure bounded by straight lines may be reduced to a single triangle, which shall have the same content. This can be done by any instrument for drawing parallel lines.

Let the trapezium, or four-sided figure, shown in Fig. 46, be required to be reduced to a single equivalent triangle. Produce one



side of the figure, as 4—1. Draw a line from the first to the third angle of the figure. From the second angle draw a parallel to the line just drawn, cutting the produced side in a point 1'. From the point 1' draw a line to the third angle. A triangle (1'—3—4 in the figure) will thus be

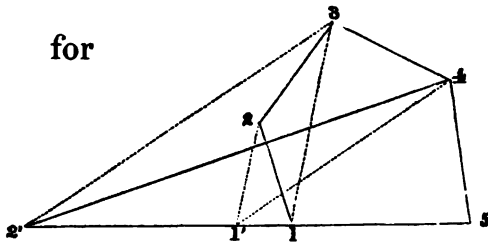
formed, which will be equivalent to the original trapezium.

For, the triangle 1—2—3 taken away from the original figure is equivalent to the triangle 1'—1—3 added to it; because both these triangles have the same base and also the same altitude, since the vertices of both lie in the same line parallel to the base.

The content of this final triangle can then be found by measuring its perpendicular, and taking half the product of this perpendicular by the base.

for

Fig. 47.



Let the given figure have five sides, as in Fig.

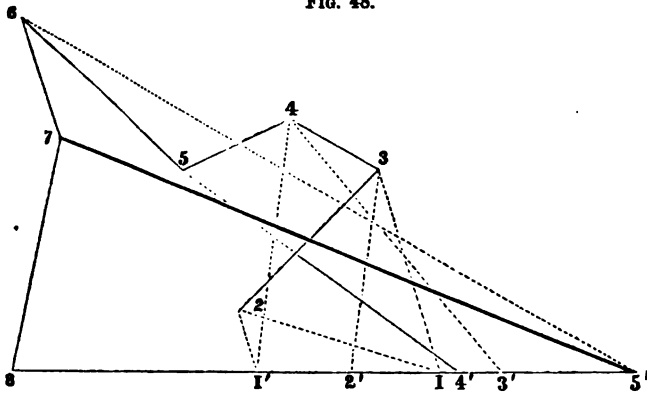
47. For brevity, the angles of the figure will be named as numbered in the engraving. Produce 5—1. Join 1—3. From 2 draw a parallel to 1—3, cutting the produced base in 1'. Join 1'—4. From 3 draw a parallel to it, cutting the base in 2'. Join 2'—4. Then will the triangle 2'—4—5 be equivalent to the five-sided figure 1—2—3—4—5, for similar reasons to those of the preceding case.

Let the given figure be 1—2—3—4—5—6—7—8, as shown in Fig. 48. All the operations are shown by dotted lines, and the finally resulting triangle, 5'—7—8, is equivalent to the original figure of eight sides.

It is best, in choosing the side to be produced, to take one which has a long side adjoining it on the end not produced; so that this long side may form one side of the final triangle, the base of which will therefore be shorter, and will not be cut so acutely by the final line drawn, as to make the point of intersection too indefinite.



FIG. 48.



**75. General Rule.** When the given figure has many sides, with angles sometimes salient and sometimes re-entering, the operations of reduction are very liable to errors if the draughtsman attempts to reason out each step. All difficulties, however, will be removed by the following *General Rule* :

1. Produce one side of the figure, and call it a base. Call one of the angles at the base the first angle, and number the rest in regular succession around the figure.

2. Draw a line from the 1st angle to the 3d angle. Draw a parallel to it from the 2d angle. Call the intersections of this parallel with the base the 1st mark.

3. Draw a line from the 1st mark to the 4th angle. Draw a parallel to it from the 3d angle. Its intersection with the base is the 2d mark.

4. Draw a line from the 2d mark to the 5th angle. Draw a parallel to it from the 4th angle. Its intersection with the base is the 3d mark.

5. In general terms, which apply to every step after the first, draw a line from the last mark obtained to the angle whose number is greater by three than the number of the mark. Draw a parallel to it through the angle whose number is greater by two than that of the mark. Its intersection with the base will be a mark whose number is greater by one than that of the preceding mark.

In the concise language of algebra, draw a line from the  $n$ th

mark to the  $n + 3$  angle. Draw a parallel to it through the  $n + 2$  angle, and the intersection with the base will be the  $n + 1$  mark.

6. Repeat this process for each angle, till you get a mark whose number is such that the angle having a number greater by three is the last angle of the figure—i. e., the angle at the other end of the base. Then join the last mark to the angle which precedes the last angle in the figure, and the triangle thus formed will be the equivalent triangle required.

In practice it is *unnecessary* to actually draw the lines joining the successive angles and marks, but the parallel ruler is merely laid on so as to pass through them, and the points where the parallels cut the base are alone marked.

76. It is generally more convenient to reduce half of the figure on one side and half on the other, as is shown in Fig. 49, which represents the same field as Fig. 47. The equivalent triangle is here  $1' - 8 - 2'$ .

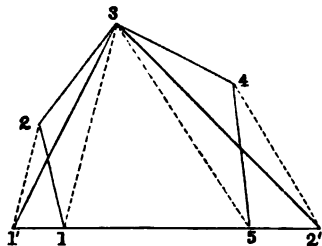
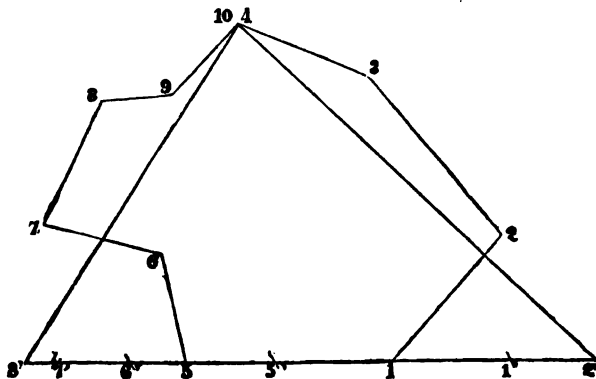


FIG. 49.

When the figure has many angles, they should not be numbered consecutively all the way around, but, after the numbers have gone around as far as the angle where it is intended to have the vertex of the final triangle, the numbers should be continued from the other angle of the base, as is shown in Fig. 50. In it only the intersections are marked.

A figure with curved boundaries may be reduced to a triangle in a similar manner. Straight lines must be drawn about the figure, so as to be partly in

FIG. 50.

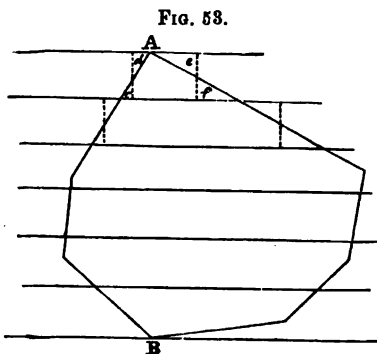


having been done, the equivalent straight-lined figure is reduced by the above method.

**FIG. 52.**

This instrument is used in connection with a sheet of transparent paper, ruled with parallel lines at distances apart each equal to one chain on the scale of the plat. It is plain that when the instrument is laid on this paper, with its edge on one of the parallel lines, and the slider is moved over one of the divisions of  $2\frac{1}{2}$  chains, that *one rood*, or a quarter of an acre, has been measured between two of the parallel lines on the paper (since 10 square chains make one acre); and that one of the smaller divisions measures *one perch* between the same parallels. Four of the larger divisions give one acre. The scale is generally made long enough to measure at once five acres.

To apply this to the plat of a field, or farm, lay the transparent paper over it in such a position that two of the ruled lines shall touch two of the exterior points of the boundaries, as at A and B. Lay the scale, with the slide set to zero, on the paper, in a direction parallel to the ruled lines, and so that the wire of the slide cuts the left-hand oblique line so as to make the spaces *e* and *d* about equal. Hold the scale firm, and move the slider till the wire cuts the right-hand oblique line in such a way as to equalize the spaces *e* and *f*. Without changing the slide, move the scale down the width of a



space and to the left-hand end of the next space; begin there again, and proceed as before.

So go on, till the whole length of the scale is run out (five acres having been measured), and then begin at the right-hand side and work backward to the left, reading the lower divisions, which run up to 10 acres. By continuing this process, the content of plats of any size can be obtained.

A still simpler substitute for this is a scale similarly divided, but without an attached slide. In place of

it there is used a piece of glass, having a line drawn across it and riveted to the end of a short scale of box-wood, divided like the former slide. It is used like the former, except that, at starting, the zero of the short scale and not the line on the glass is made to coincide with the zero of the long scale. The slide is to be held fast to the instrument when this is moved.

**78. Planimeters.** These determine the area of any figure, whether bounded by straight lines or curved, by merely moving a point around the outline of the surface. This causes motion in a train of wheel-work, which registers the algebraic sum of the product of ordinates to every point in that perimeter, by the increment of their abscissas, and therefore measures the included space.

There are several varieties of these instruments. One of the best of them is Amsler's Polar Planimeter. (For descriptions and theory of Planimeters, see "Mechanical Integrators," by Henry S. H. Shaw.)

**79.** A purely mechanical means of determining the area of any surface by means of its *weight*, may be placed here. The plat is cut out of paper and weighed by a delicate balance. The weight of a rectangular piece of the same paper containing just one acre

is also found; and the "Rule of Three" gives the content. A modification of this is to paste a tracing of the plat on thin sheet-lead, cut out the lead to the proper lines and weigh it.

**80. FOURTH METHOD.—TRIGONOMETRICALLY.** *By calculating, from the observed angles of the boundaries of the piece of ground, the lengths of the lines needed for calculating the content.*

This method is employed for surveys made with angular instruments, as the compass, etc., in order to obtain the content of the land surveyed, without the necessity of previously making a plat, thus avoiding both that trouble and the inaccuracy of any calculations founded upon it. It is therefore the most accurate method; but will be more appropriately explained in Part I, Chapter III, under the head of "Compass Surveying."

## CHAPTER II.

### *CHAIN-SURVEYING ; BY THE FIRST AND SECOND METHODS : OR DIAGONAL AND PERPENDICULAR SURVEYING.*

**81.** THE chain alone is abundantly sufficient, without the aid of any other instrument, for making an accurate survey of any surface, whatever its shape or size, particularly in a district tolerably level and clear. Moreover, since a chain, or some substitute for it, formed of a rope, of leather driving-reins, etc., can be obtained by any one in the most secluded place, this method of surveying deserves more attention than has usually been given to it.

### **SURVEYING BY DIAGONALS: OR BY THE FIRST METHOD.**

**82.** *Surveying by Diagonals* is an application of the *First Method* of determining the position of a point, given in Art. 3, to which the student should again refer. Each corner of the field or farm which is to be surveyed is "determined" by measuring its distances from two other points. The field is then "platted" by repeating this process on paper, for each corner, in a contrary order, and the "content" is obtained by some of the methods explained in Chapter I.

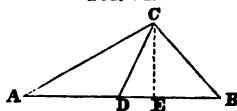
The lines which are measured in order to determine the corners of the field are usually *sides* and *diagonals* of the irregular polygon which is to be surveyed. They therefore divide it up into triangles; whence this mode of surveying is sometimes called "Chain Triangulation."

A few examples will make the principle and practice perfectly clear. Each will be seen to require the three operations of *measuring*, *platting*, and *calculating*.

**A three-sided field; as Fig. 54.**

**Field-work.** Measure the three sides,  $AB$ ,  $BC$ , and  $CA$ . Measure also, as a proof-line, the distance from one of the corners, as  $C$ , to some point in the opposite side, as  $D$ , at which a mark should have been left, when measuring from  $A$  to  $B$ , at a known distance from  $A$ . A stick or twig, with a slit in its top, to receive a piece of paper with the distance from  $A$  marked on it, is the most convenient mark.

FIG. 54.



**Platting.** Choose a suitable scale. Then draw a line equal in length, on the chosen scale, to one of the sides;  $AB$ , for example. Take in the compasses the length of another side, as  $AC$ , to the same scale, and with one leg in  $A$  as a center, describe an arc of a circle. Take the length of the third side,  $BC$ , and, with  $B$  as a center, describe another arc, intersecting the first arc in a point which will be the third corner  $C$ . Draw the lines  $AC$  and  $BC$ ; and  $ABC$  will be the *plat*, or miniature copy of the field surveyed.

Instead of describing two arcs to get the point  $C$ , two pairs of compasses may be conveniently used. Open them to the lengths, respectively, of the last two sides. Put one foot of each at the ends of the first side, and bring their other feet together, and their point of meeting will mark the desired third point of the triangle.

To "prove" the accuracy of the work, fix the point  $D$ , by setting off from  $A$  the proper distance, and measure the length of the line  $DC$ . If its length on the plat corresponds to its measurement on the ground, the work is correct.

It is a universal principle, in all surveying operations, that the work must be tested by some means independent of the original process; and that the same result must be arrived at by two different methods. The necessary length of this proof-line can also easily be calculated by the principles of trigonometry.

**Calculation.** The content of the field may now be found, either from the three sides, or more easily though not so accurately, by measuring on the plat, the length of the perpendicular  $CE$ , let fall from any angle to the opposite side, and taking half the product of these two lines.

**Example 1.** Fig. 54 is the plat, on a scale of two chains to one inch, of a field, of which the side  $AB$  is 200 links,  $BC$  is 100 links, and  $AC$  is 150 links. Its content, by the rule of Art. 62, is 0.726 of a square chain, or 0 A. 0 R. 12 P. If the perpendicular  $CE$  be accurately measured, it will be found to be  $72\frac{1}{2}$  links. Half the product of this perpendicular by the base will be found to give the same content.

**Ex. 2.** The three sides of a triangular field are respectively 89.39, 54.08, and 45.98. Required its content.

*Ans.* 100 A. 0 R. 10 P.

**A four-sided field; as Fig. 55.**

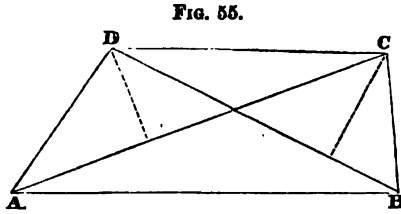
**Field-work.** Measure the four sides. Measure also a diagonal, as  $AC$ , thus dividing the four-sided field into two triangles. Measure also the other diagonal, or  $BD$ , for a "proof-line."

**Platting.** Draw a line, as  $AC$ , equal in length to the diagonal, to any

scale. On each side of it construct a triangle with the sides of the field, as directed above.

To prove the accuracy of the work, measure on the plat the length of the "proof-line,"  $BD$ , and if it agrees with the length of the same line measured on the ground, the field-work and platting are both proved to be correct.

*Calculation.* Find the content of each triangle separately, as in the preceding case, and add them together; or, more briefly, multiply either diagonal (the longer



one is preferable) by the sum of the two perpendiculars, and divide the product by two.

Otherwise: reduce the four-sided figure to one triangle, as in Art. 74; or, use any of the methods of the preceding chapter.

*Ex. 3.* In the field drawn in Fig. 55, on a scale of 8 chains to the inch,  $AB = 588$  links,  $BC = 210$ ,  $CD = 430$ ,  $DA = 274$ , the diagonal  $AC = 626$ , and the proof diagonal  $BD = 500$ . The total content will be  $7A. 0 R. 17 P.$

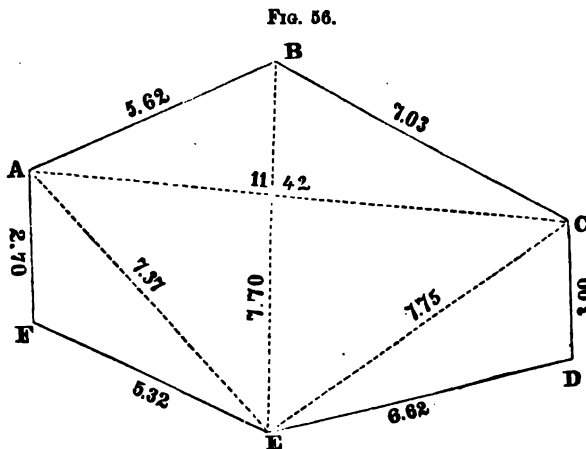
*Ex. 4.* The sides of a four-sided field are  $AB = 12.41$ ,  $BC = 5.86$ ,  $CD = 8.25$ ,  $DA = 4.24$ ; the diagonal  $BD = 11.55$ , and the proof-line  $AC = 11.04$ . Required the content. *Ans.*  $4 A. 2 R. 38 P.$

*Ex. 5.* The sides of a four-sided field are as follows:  $AB = 8.95$ ,  $BC = 5.83$ ,  $CD = 10.10$ ,  $DA = 6.54$ ; the diagonal from  $A$  to  $C$  is  $11.52$ ; the proof diagonal from  $B$  to  $D$  is  $10.92$ . Required the content. *Ans.*

*Ex. 6.* In a four-sided field,  $AB = 7.68$ ,  $BC = 4.09$ ,  $CD = 10.64$ ,  $DA = 7.24$ ,  $AC = 10.82$ ,  $BD = 10.74$ . Required the content. *Ans.*

**A many-sided field, as Fig. 56.**

*Field-work.* Measure all the sides of the field. Measure also diagonals





enough to divide the field into triangles, of which there will always be two less than the number of sides. Choose such diagonals as will divide the field into triangles as nearly equilateral as possible. Measure also one or more diagonals for "proof-lines." It is well for the surveyor himself to place stakes in advance at all the corners of the field, as he can then select the best mode of division.

*Platting.* Begin with any diagonal and plat one triangle. Plat a second triangle adjoining the first one. Plat another adjacent triangle, and so proceed till all have been laid down in their proper places. Measure the proof-lines as before.

*Calculation.* Proceed to calculate the content of the figure, precisely as directed for the four-sided field, measuring the perpendiculars and calculating the content of each triangle in turn; or taking in pairs those on opposite sides of the same diagonal; or using some of the other methods which have been explained.

*Ex. 7.* The six-sided field, shown in Fig. 56, has the lengths of its lines, in chains and links, written upon them, and is divided into four triangles, by three diagonals. The diagonal B E is a "proof-line." The figure is drawn to a scale of 4 chains to the inch. The content of the field is 5 A. 3 R. 22 P.

*Ex. 8.* In a five-sided field, the lengths of the sides are as follows: A B = 2·69, B C = 1·22, C D = 2·32, D E = 3·55, E A = 3·23. The diagonals are A D = 4·81, B D = 3·33. Required its content. *Ans.*

A field may be divided up into triangles, not only by measuring diagonals as in the last figure, but by any of the methods shown in the four figures of Art. 67. The one which we have been employing corresponds to the last of those figures.

Still another mode may be used when the angles can not be seen from one another, or from any one point within. Take two or more convenient points within the field, and measure from them to the corners, and thus form different sets of triangles.

### *Keeping the Field-Notes.*

**83. By Sketch.** The most simple method is to make a sketch of the field, as nearly correct as the unassisted hand and eye can produce, and note down on it the lengths of all the lines, as in Fig. 56. But when many other points require to be noted, such as where fences, or roads, or streams are crossed in the measurement, or any other additional particulars, the sketch would become confused, and be likely to lead to mistakes in the subsequent platting from it. The following is therefore the usual method of keeping the field-notes. A long, narrow book is most convenient for it.

**84. In Columns.** Draw two parallel lines, about an inch apart from the bottom to the top of the page of the field-book, as

in the margin. This column, or pair of lines, may be conceived to represent the measured line, *split in two*, its two halves being then separated, an inch apart, merely for convenience, so that the distances measured along the line may be written between these halves.

Hold the book in the direction of the measurement. At the *bottom* of the page write down the name, or number, or letter, which represents the station at which the survey is to begin.

A "station" is marked with a triangle or circle, as in the margin. The latter is more easily made.



In the complicated cases, which will be hereafter explained, and in which one long base-line is measured, and also many other subordinate lines; it will be well, as a help to the memory, to mark the stations on the base-line with a triangle, and the stations on the other lines with the ordinary circle.

The station from which the measurements are made is usually put on the left of the column; and the station which is measured to, is put on the right.

From A

|     |      |
|-----|------|
| ○   | to B |
| 562 |      |
| ○   |      |

But it is more compact, and avoids interfering with the notes of "offsets" (to be explained hereafter), to write the name or number of the station *in* the column, as in the margin.

The measurements to different points of a line are written above one another. The numbers all refer to the beginning of the line, and are counted from it.

|     |
|-----|
| B   |
| 400 |
| 250 |
| 100 |
| A   |

The end of a measured line is marked by a line drawn across the page above the numbers which indicate the measurements which have been made.

If the chaining does not continue along the adjoining line, but the chain-men go to some other part of the field to begin another measurement, *two* lines are drawn across the page.

When a line has been measured, the marks  $\Gamma$  or  $\Upsilon$  are made to show whether the following line turns to the right or to the left.

A line is named, either by the names of the stations between which it is measured, as the line A B ; or by its length, a line 562 links long, being called the line 562 ; or it is recorded as Line No. 1, Line No. 2, etc. ; or as Line on page 1, 2, etc., of the field-book.

When a mark is left at any point of a line, as at D, in Fig. 49, with the intention of coming back to it again, in order to measure to some other point, the place marked is called a *False Station*, and is marked in the field-book "F. S." ; or has a line drawn around it, to distinguish it ; or has a station mark  $\Delta$  placed outside of the column, to the right or left, according to the direction in which the measurement from it is to be made. Examples of these three modes are given in the margin.

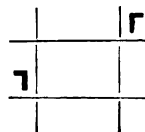
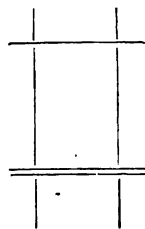
A false station is named by its position on the line where it belongs ; as thus—"200 on 562."

When a gate occurs in a measured line, the distance from the beginning of the line to the side of the gate first reached is the one noted.

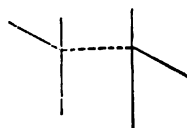
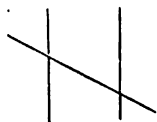
When the measured line crosses a fence, brook, road, etc., they are drawn on the field-notes in their true direction, as nearly as possible, but not in a continuous line across the column, as in the first figure in the margin, but as in the second figure, so that the two parts would form a continuous straight line, if the halves of the "split line" were brought together.

It is convenient to name the lines in the margin as being Sides, Diagonals, Proof-lines, etc.

85. The field-notes of the triangular field platted in Fig. 54 are given below, according to both the methods mentioned in the preceding article.



|       |          |
|-------|----------|
| 562   |          |
| 200   | f. s.    |
| 0     |          |
| 562   |          |
| (200) |          |
| 0     |          |
| 562   |          |
| 200   |          |
| 0     | $\Delta$ |



In the field-notes in the column on the right hand, it is not absolutely necessary to repeat the B and C.

|             |        |                |               |
|-------------|--------|----------------|---------------|
| PROOF-LINE. | From D | 89<br>F. S.    | to C          |
| SIDE.       | From C | 150<br>O       | to A<br>┐     |
| SIDE.       | From B | 100<br>O       | to O<br>┐     |
| SIDE.       | From A | 200<br>80<br>O | to B<br>F. S. |

|             |      |                       |        |
|-------------|------|-----------------------|--------|
| PROOF-LINE. | From | C<br>89<br>(80)       | on 200 |
| SIDE.       | ┐    | A<br>150<br>O         |        |
| SIDE.       | ┐    | O<br>100<br>B         |        |
| SIDE.       |      | B<br>200<br>(80)<br>A |        |

86. The field-notes of the survey platted in Fig. 56 are given below. They begin at the bottom of the left-hand column.

|       |                                                                                     |                        |             |
|-------|-------------------------------------------------------------------------------------|------------------------|-------------|
| SIDE. |                                                                                     | F<br>582<br>300<br>E   | Gate.<br>┐  |
| SIDE. |  | E<br>662<br>400<br>D   | Brook.<br>┐ |
| SIDE. |  | D<br>300<br>270<br>210 | Road.<br>┐  |
| SIDE. |  | 80<br>O                | ┐           |
| SIDE. |                                                                                     | C<br>703<br>150<br>B   | Gate.<br>┐  |
| SIDE. |                                                                                     | B<br>562<br>A          |             |

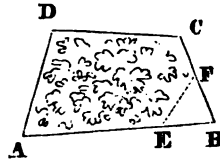
|             |                                                                                     |                             |            |
|-------------|-------------------------------------------------------------------------------------|-----------------------------|------------|
| PROOF-LINE. |                                                                                     | E<br>770<br>B               |            |
| DIAGONAL    | ┐                                                                                   | A<br>1142<br>O              |            |
| DIAGONAL    |  | C<br>775<br>480<br>420<br>E | Road.<br>┐ |
| DIAGONAL    |  | E<br>737<br>280<br>210<br>A | Road.<br>┐ |
| SIDE.       |  | A<br>270<br>180<br>80<br>F  | Road.<br>┐ |

## SURVEYING BY TIE-LINES.

**87.** *Surveying by Tie-lines* is a modification of the method explained in the last chapter. It frequently happens that it is impossible to measure the diagonals of a field of many sides, in consequence of obstacles to measurements, such as woods, water, houses, etc. In such cases, "tie-lines" (so called because they tie the sides together) are employed as substitutes for diagonals.

Thus, in the four-sided field shown in the figure, the diagonals can not be measured because of woods intervening. As a substitute, measure off from any convenient corner of the field, as B, any distances,  $BE$ ,  $BF$ , along the sides of the field. Measure also the "tie-line"  $EF$ . Measure all the sides of the field as usual.

FIG. 57.



To plat this field, construct the triangle  $BEF$ , as in Art. 82. Produce the sides  $BE$  and  $BF$ , till they become respectively equal to  $BA$  and  $BC$ , as measured on the ground. Then, with  $A$  and  $C$  as centers, and with radii respectively equal to  $AD$  and  $CD$ , describe arcs, whose intersection will be  $D$ , the remaining corner of the field.

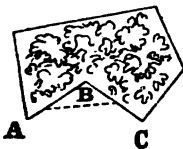
**88.** It thus appears that one tie-line is sufficient to determine a four-sided field, two a five-sided field, and so on. But, as a check on errors, it is better to measure a tie-line for each angle, and the agreement, in the plat, of all the measurements will prove the accuracy of the whole work.

Since any inaccuracy in the length of a tie-line is increased in proportion to the greater length of the sides which it fixes, the tie-lines should be measured as far from the point of meeting of these sides as possible—that is, they should be as long as possible.

The radical defect of the system is that it is "working from less to greater" (which is the exact converse of the true principle), thus magnifying inaccuracies at every step.

A tie-line may also be employed as a "proof-line," in the place of a diagonal, and tested in the same manner.

FIG. 58.



If any angle of the field is re-entering, as at B in the figure, measure a tie-line across the salient angle A B C.

**89. Chain-Angles.** It is convenient, though not necessary, to measure equal distances along the sides: B E, B F, in Fig. 57, and B A, B C, in Fig. 58. "Chain-angles" are thus formed. To reduce "chain-angles" to degrees and minutes, see Art. 28.

**90. Inaccessible Areas.** The method of tie-lines can be applied to measuring fields which can not be entered.

Thus, in the figure, A B C D is an inaccessible wooded field, of four sides. To survey it, measure all the sides, and at any corner, as D, measure any distance D E, in the line of A D produced. Measure also another distance D F in the line of C D produced. Measure the tie-line E F, and the figure can be platted as in the case of the field of

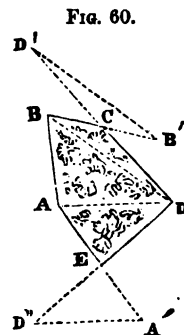
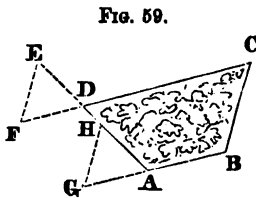
Fig. 57, the sides of the triangle being produced in the contrary direction.

The same end would be attained by prolonging only one side, as shown at the angle A of the same figure, and measuring A G, A H, and G H. It is better, in both cases, to tie *all* the angles in a similar manner.

This method may be applied to a figure of any number of sides by prolonging as many of them as are necessary; all of them, if possible.

**91.** If the sides C D and A D were prolonged by their full length, the content of the figure could be calculated without any plat; for the new triangle D E F would equal the triangle D A C, and the sides of the triangle A C B would then be known.

This principle may be extended still further. For a five-sided field, as in Fig. 60, produce two pairs of sides, a distance equal to



their length, forming two new triangles, as shown by the dotted lines, and measure the sides  $B'D'$  and  $A'D''$ . The three sides of each of these triangles will thus be known, and also the three sides of the triangle  $BAD$ , since  $AD = A'D''$ , and  $BD = B'D'$ .

The method of this article may be employed for a figure of six sides, as shown in Fig. 61 (in which the dotted lines within the wooded field have their lengths determined by the triangles formed outside of it), but not for figures of a greater number of sides.

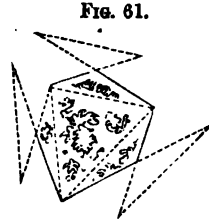


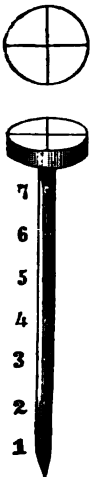
FIG. 61.

### SURVEYING BY PERPENDICULARS: OR BY THE SECOND METHOD.

92. The method of *Surveying by Perpendiculars* is founded on the *Second Method* of determining the position of a point, explained in Art. 4. It is applied in two ways, either to making a complete survey by "*Diagonals and Perpendiculars*," or to measuring a crooked boundary by "*Offsets*." Each will be considered in turn.

The best method of getting perpendiculars on the ground must, however, be first explained.

FIG. 62.



#### *To set out Perpendiculars.*

93. **Surveyor's Cross.** The simplest instrument for this purpose is the *Surveyor's Cross*, or *Cross-Staff*, shown in the figure. It consists of a block of wood, of any shape, having in it two saw-cuts, made very precisely at right angles to each other, about half an inch deep, and with center-bit holes made at the bottom of the cuts to assist in finding the objects. This block is fixed on a pointed staff, on which it can turn freely, and which should be precisely 8 links ( $63\frac{1}{2}$  inches) long, for the convenience of short measurements.

To use the cross-staff to erect a perpendicular, set it at the point of the line at which a perpendicular is wanted. Turn its head till, on looking through one

saw-cut, you see the ends of the line. Then will the other saw-cut point out the direction of the perpendicular, and thus guide the measurement desired.

To find where a perpendicular to the line, from some object, as a corner of a field, a tree, etc., would meet the line, set up the cross-staff at a point of the line which seems to the eye to be about the spot. Note about how far from the object the perpendicular at this point strikes, and move the cross-staff that distance; and repeat the operation till the correct spot is found.

94. To test the accuracy of the instrument, sight through one

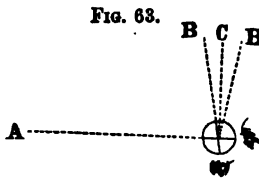


FIG. 63.

slit to some point A, and place a stake B in the line of sight of the other slit. Then turn its head a quarter of the way around, so that the second slit, looked through, points to A. Then see if the other slit covers B again, as it will if correct. If it does not do so, but sights

to some other point, as B', the apparent error is double the real one, for it now points as far to the right of the true point C as it did before to its left.

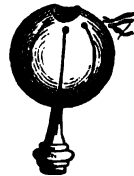
This is the first example we have had of the invaluable principle of *Reversion*, which is used in almost every test of the accuracy of surveying and astronomical instruments, its peculiar merit being that it doubles the real error, and thus makes it twice as easy to perceive and correct it.

The instrument, in its most finished form, is made of a hollow brass cylinder, which has two pairs of slits exactly opposite to each other, one of each pair being narrow and the other wide, with a horse-hair stretched from the top to the bottom of the latter. It is also, sometimes, made with eight faces, and two more pairs of slits added, so as to set off half a right angle.

Another form is a hollow brass sphere, as in the figure. This enables the surveyor to set off perpendiculars on very steep slopes.

Another form of the surveyor's cross consists of

FIG. 64.

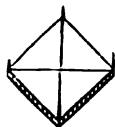




two pairs of plain "Sights," each shaped as in the figure, placed at the ends of two bars at right angles to each other. The slit, and the opening with a hair stretched from its top to its bottom, are respectively at the top of one sight and at the bottom of the opposite sight.\* This is used in the same manner as the preceding form, but is less portable, and more liable to get out of order.



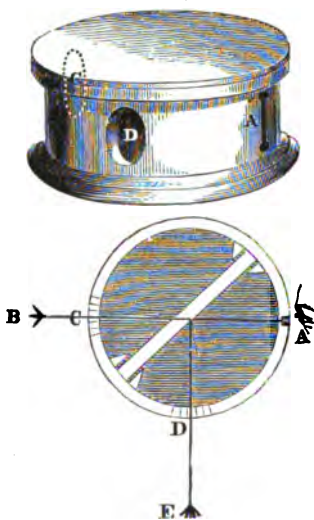
FIG. 66.



A temporary substitute for these instruments may be made by sticking four pins into the corners of a square piece of board, and sighting across them, in the direction of the line and at right angles to it.

**95. Optical Square.** The most convenient and accurate instrument is, however, the Optical Square. The figures give a perspective view of it, and also a plan with the lid removed. It is a small circular box, containing a strip of looking-glass, from the upper half of which the silvering is removed. This glass is placed so as to make precisely half a right angle with the line of sight, which passes through a slit on one side of the box, and a vertical hair stretched across the opening on the other side, or a mark on the glass. The box is held in the hand over the spot where the perpendicular is desired (a plumb-line in the hand will give perfect accuracy), and the observer applies his eye to the slit A, looking through the upper or unsilvered part of the glass, and turns the box till he sees the other end of the line B, through the opening C. The assistant, with a rod, moves along in the direction where the perpendicular is desired, being seen in the silvered

FIG. 67.



\* The French call the narrow opening *ailleton*, and the wide one *croisée*.

parts of the glass, by reflection through the opening D, till his rod, at E, is seen to coincide with, or to be exactly under, the object B. Then is the line D E at right angles to the line A B, by the optical principle of the equality of the angles of incidence and reflection.

To find where a perpendicular from a distant object would strike the line, walk along the line, with the instrument to the eye, till the image of the object is seen, in the silvered part of the glass, to coincide with the direction of the line seen through the unsilvered part.

The instrument may be tested by sighting along the perpendicular, and fixing a point in the original line, on the principle of "reversion."

The surveyor can make it for himself, fastening the glass in the box by four angular pieces of cork, and adjusting it by cutting away the cork on one side, and introducing wedges on the other side. The box should be blackened inside.

Another form of the optical square contains <sup>not do</sup> ~~an~~ <sup>is</sup> 70 glasses, fixed at an angle of  $45^\circ$ , and giving a right angle on the principle of the sextant.

Perpendiculars may be set out with the chain alone, by a variety of methods. These methods generally consist in performing on the ground, the operations executed on paper in practical geometry, the chain being used, in the place of the compasses, to describe the necessary arcs.

As these operations, however, are less often used for the method of surveying now to be explained, than for overcoming obstacles to measurement, it will be more convenient to consider them in that connection.

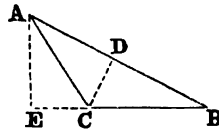
### *Diagonals and Perpendiculars.*

96. We have seen in the preceding pages that plats of surveys, made with the chain alone, have their contents most easily determined by measuring, on the plat, the perpendiculars of each of the triangles, into which the diagonals measured on the ground have divided the field. In the *Method of Surveying by Diagonals and Perpendiculars*, now to be explained, the perpendiculars are measured *on the ground*. The content of the field can, therefore,

be found at once (by adding together the half products of each perpendicular by the diagonal on which it is let fall), without the necessity of previously making a plat, or of measuring the sides of the field. This is, therefore, the most rapid and easy method of surveying when the content alone is required, and is particularly applicable to the measurement of the ground occupied by crops, for the purpose of determining the number of bushels grown to the acre, the amount to be paid for mowing by the acre, etc.

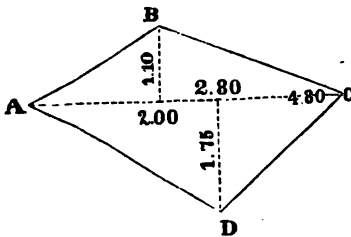
**A Three-sided Field.** Measure the longest side, as  $AB$ , and the perpendicular,  $CD$ , let fall on it from the opposite angle  $C$ . Then the content is equal to half the product of the side by the perpendicular. If obstacles prevent this, find the point, where a perpendicular let fall from an angle, as  $A$ , to the opposite side produced, as  $BC$ , would meet it, as at  $E$  in the figure. Then half the product of  $AE$  by  $CB$  is the content of the triangle.

FIG. 68.



**A Four-sided Field.** Measure the diagonal  $AC$ . Leave marks at the points on this diagonal at which perpendiculars from  $B$  and from  $D$  would meet it, finding these points by trial, as previously directed. The best marks at these "false stations" have been described. Return to these false stations and measure the perpendiculars. When these perpendiculars are measured before finishing the measurement of the diagonal, great care is necessary to avoid making mistakes in the length of the diagonal, when the chainmen return to continue its measurement. One check is to leave at the mark as many

FIG. 69.



pins as have been taken up by the hind-chainman in coming to that point from the beginning of the line.

*Ex. 9.* Required the content of the field of Fig. 69. *Ans.* 0 A. 2 R. 29 P.

The field may be platted from these measurements, if desired, but with more liability to inaccuracy than in the first method, in which the sides are measured. The plat of the figure is three chains to one inch.

The field-notes may be taken by writing the measurements on a sketch, as in the figure; or, in more complicated cases, by the column method, as below. A new symbol may be employed, this mark,  $\perp$ , or  $\neg$ , to show the false station, from which a perpendicular is to be measured.

|           |                 |                        |           |
|-----------|-----------------|------------------------|-----------|
| PERP.     | From 200 on 480 | 110<br>F. S.           | to B<br>┐ |
| PERP.     | From 280 on 480 | 175<br>F. S.           | to D<br>┐ |
| DIAGONAL. | From A          | 480<br>280<br>200<br>○ | to C<br>┐ |

*Ex. 10. Calculation.*

$$\begin{aligned} \text{sq. lks.} \\ ABC &= \frac{1}{2} \times 480 \times 110 = 26400 \\ ADC &= \frac{1}{2} \times 480 \times 175 = 42000 \\ \text{sq. chains } 6.8400 \\ \text{Acres } 0.684 \end{aligned}$$

It is still easier to take the two triangles together; multiplying the diagonal by the sum of the perpendiculars and dividing by two.

**A Many-sided Field.** Fig. 70 and the accompanying field-notes represent the field which was surveyed by the first method and platted in Fig. 56.

|                    |                            |           |
|--------------------|----------------------------|-----------|
| From 5.07 on 7.37  | 1.54<br>F. S.              | to F      |
| From 1.60 on 7.75  | 2.53<br>F. S.              | to D      |
| From 5.45 on 11.42 | 4.93<br>F. S.              | to E      |
| From 4.95 on 11.42 | 2.87<br>F. S.              | to B      |
| From E             | 7.37<br>5.07<br>○          | to A<br>┐ |
| From C             | 7.75<br>1.60<br>○          | to E<br>┐ |
| From A             | 11.42<br>5.45<br>4.95<br>○ | to O<br>┐ |

*Ex. 11. Calculation.* The content of the triangles may be expressed thus:

$$\begin{aligned} \text{sq. lks.} \\ ABC &= \frac{1}{2} \times 1142 \times 267 = 152457 \\ AEC &= \frac{1}{2} \times 1142 \times 493 = 281503 \\ CDE &= \frac{1}{2} \times 775 \times 253 = 98037 \\ \Delta EF &= \frac{1}{2} \times 787 \times 154 = 56749 \\ \text{sq. chains } 58.8746 \\ \text{Acres } 5.88746 \end{aligned}$$

or, 5 A. 3 R. 22 P.

The first two triangles might have been taken together, as in the previous field.

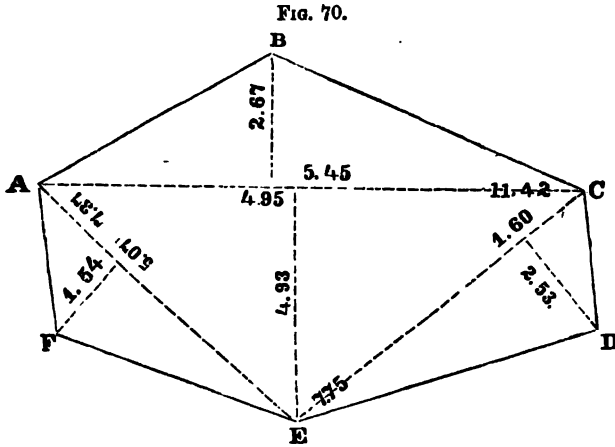
Content calculated from the perpendiculars will generally vary slightly from that obtained by measuring on the plat.

A small field which has many sides may sometimes be conveniently surveyed by taking one diagonal and measuring the perpendiculars let fall on it from each angle of the field, and thus dividing the whole area into triangles and trapezoids, as in Fig. 41.

The line on which the perpendiculars are to be let fall may also be outside of the field, as in Fig. 42.

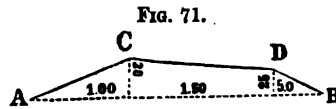
Such a survey can be platted very readily, but the length of the perpendiculars renders the plat less accurate.

This procedure supplies a transition to the method of "offsets," which is explained in the next article.



*Offsets.*

**97.** Offsets are short perpendiculars, measured from a straight line, to the angles of a crooked or zigzag line near which the straight line runs. Thus, in the figure, let A C D B be a crooked fence, bounding one side of a field. Chain along the straight line A B, which runs from one end of the fence to the other, and, when opposite each corner, note the distance from the beginning, or the point A; and also measure and note the perpendicular distance of each corner C and D from the line. These corners will then be "determined" by the *Second Method, Art. 4.*



|        |    |     |      |
|--------|----|-----|------|
|        |    |     |      |
|        | 0  | 300 | to B |
| D      | 25 | 250 |      |
| C      | 30 | 100 |      |
| From A | 0  | ⊙   |      |

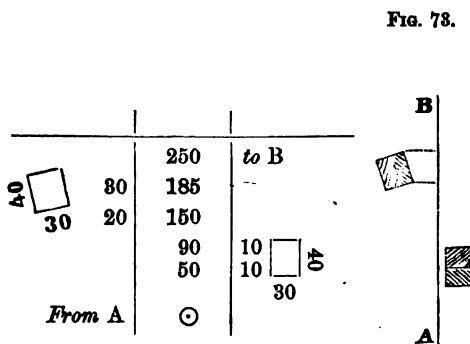
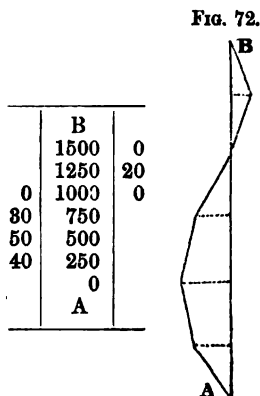
The field-notes, corresponding to Fig. 71, are as in the margin. The measurements along the line are written in the column, as before, counting from the beginning of the line, and the offsets are written beside it, on the right or left, opposite the distance at which they are taken. A sketch of the crooked line is

also usually made in the field-notes, though not absolutely necessary in so simple a case as this. The letters C and D would not be

used in practice, but are here inserted to show the connection between the field-notes and the plat.

In taking the field-notes, the widths of the offsets should not be drawn proportionally to the distances between them, but the breadths should be greatly exaggerated in proportion to the lengths.

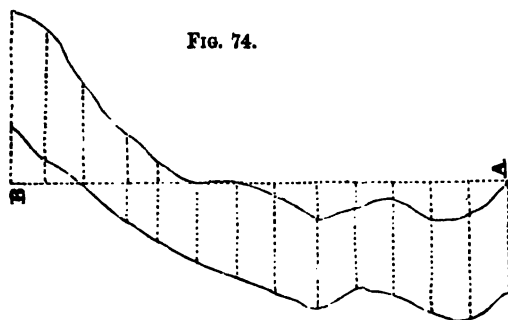
A more extended example, with a little different notation, is given below. In the figure, which is on a scale of eight chains to one inch for the distances along the line, the breadths of the offsets are exaggerated to four times their true proportional dimensions.



The plat and field-notes of the position of two houses, determined by offsets, are given above on a scale of two chains to one inch :

Double offsets are sometimes convenient ; and sometimes triple and quadruple ones. Below are given the notes and the plat, one chain to one inch, of a road of varying width, both sides of which are determined by double offsets. It will be seen that the line A B crosses one side of the road at 160 links from A, and the other side of it at 220.

Two methods of keeping the field-notes are given. In the first form, the offsets to each side of the road are given separately and connected by the sign +. In the second form, the total distance of the second offset is given, and the two measurements connected by the word "to." This is easier both for measuring and platting.



|         | B   |          | B   |
|---------|-----|----------|-----|
|         | 260 | 30 + 60  | 260 |
|         | 240 | 10 + 70  | 240 |
| 0       | 220 | 50       | 220 |
| 20      | 200 | 30       | 200 |
| 40      | 180 | 10       | 180 |
| 45      | 160 | 0        | 160 |
| 50 + 0  | 140 | 50 to 0  | 140 |
| 55 + 5  | 120 | 60 to 5  | 120 |
| 50 + 20 | 100 | 70 to 20 | 100 |
| 45 + 15 | 80  | 60 to 15 | 80  |
| 50 + 10 | 60  | 60 to 10 | 60  |
| 50 + 20 | 40  | 70 to 20 | 40  |
| 55 + 20 | 20  | 75 to 20 | 20  |
| 60 + 0  | A   | 60 to 0  | A   |

Offsets may generally be taken with sufficient accuracy by measuring them as nearly at right angles to the base-line as the eye can estimate. The surveyor should stand by the chain, facing the fence, at the place which he thinks opposite to the corner to which he wishes to take an offset, and measure "square" to it by the eye, which a little practice will enable him to do with much correctness.

The offsets may be measured, if short, with an *Offset-staff*, a light stick, 10 or 15 links in length, and divided accordingly; or, if they are long, with a tape. They are generally but a few links in length. A chain's length should be the extreme limit, as laid down by the English "Tithe Commissioners," and that should be employed only in exceptional cases. When the "cross-staff" is in use, its divided length of 8 links renders the offset-staff needless.

When offsets are to be taken, the method of chaining to the end of a line (described in Art. 18) is somewhat modified. After the leader arrives at the end of the line, he should draw on the chain

till the follower, with the back end of the chain, reaches the last pin set. This facilitates the counting of the links to the places at which the offsets are taken.

The offsets are to be taken to every angle of the fence or other crooked line; that is, to every point where it changes its direction. These angles or prominent bends can be best found by one of the party walking along the crooked fence and directing another at the chain what points to measure opposite to. If the line which is to be thus determined is *curved*, the offsets should be taken to points so near each other that the portions of the curved line lying between them may, without much error, be regarded as straight. It will be most convenient, for the subsequent calculations, to take the offsets at equal distances apart along the straight line from which they are measured.

In the case of a crooked brook, such as is shown in the figure given below, offsets should be taken to the most prominent angles, such as are marked *a a a* in the figure, and the intermediate bends may be merely sketched by the eye.

FIG. 75.



When offsets from lines measured around a field are taken inside of these bounding lines, they are sometimes distinguished as *insets*.

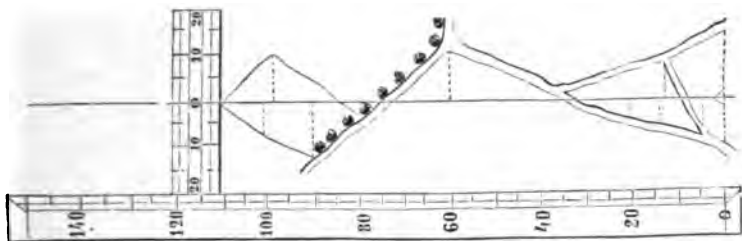
**98. Platting.** The most rapid method of platting the offsets is by the use of a *Platting Scale* (described in Art. 47) and an *Offset Scale*, which is a short scale divided on its edges like a platting scale, but having its zero in the middle, as in the figure.

The platting scale is placed parallel to the line, with its zero-point opposite to the beginning of the line. The offset scale is slid along the platting scale, till its edge comes to a distance on the latter at which an offset had been taken, the length of which is marked off with a needle-point from the offset scale. This is then



slid on to the next distance, and the operation is repeated. If one person reads off the field-notes, and another plats, the operation

FIG. 76.



will be greatly facilitated. The points thus obtained are joined by straight lines, and a miniature copy of the curved line is thus obtained; all the operations of the platting being merely repetitions of the measurements made on the ground.

If no offset scale is at hand, make one of a strip of thick drawing-paper, or pasteboard; or use the platting scale itself, turned crossways, having previously marked off from it the points from which the offsets had been taken.

In plats made on a small scale, the shorter offsets are best estimated by the eye.

On the ordnance survey of Ireland, the platting of offsets was facilitated by the use of a combination of the offset scale and the platting scale, the former being made to slide in a groove in the latter, at right angles to it.

**99. Calculating Content.** When the crooked line determined by offsets is the boundary of a field, the content, inclosed between it and the straight line surveyed, must be determined, that it may be added to, or subtracted from, the content of the field bounded by the straight lines. There are various methods of effecting this.

The area inclosed between the straight and the crooked lines is divided up by the offsets into *triangles and trapezoids*, the content of which may be calculated separately and then added together. The content of the plat on page 65 will, therefore, be  $1500 + 4125 + 625 = 6250$  square links =  $0.625$  square chain. The con-

tent of the plat on page 66 will in like manner be found to be, on the left of the straight line, 30,000 square links, and on its right, 5,000 square links.

**100.** *When the offsets have been taken at equal distances, the content may be more easily obtained by adding together half of the first and of the last offset, and all the intermediate ones, and multiplying the sum by one of the equal distances between the offsets. This rule is merely an abbreviation of the preceding one.*

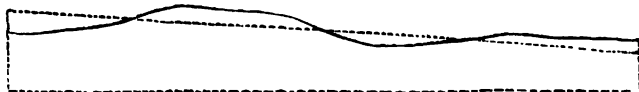
Thus, in the plat of page 66, the distances being equal, the content of the offsets on the left of the straight line will be  $120 \times 250 = 30,000$  square links, and on the right,  $20 \times 250 = 5,000$  square links; the same results as before.

When the line determined by the offsets is a curved line, "Simpson's rule" gives the content more accurately. To employ it, an *even* number of *equal* distances must have been measured in the part to be calculated. Then add together the first and last offset, four times the sum of the even offsets (i. e., the 2d, 4th, 6th, etc.), and twice the sum of the odd offsets (i. e., the 3d, 5th, 7th, etc.), not including the first and the last. Multiply the sum by one of the equal distances between the offsets, and divide by 3. The quotient will be the area.

*Ex. 12.* The offsets from a straight line to a curved fence were 8, 9, 11, 15, 16, 14, 9, links, at equal distances of 5 links. What was the content included between the curved fence and the straight line?  
*Ans.* 371·666.

**101.** *Equalizing, or giving and taking, is an approximate mode of calculation much used by practical surveyors. A crooked line,*

FIG. 77.



determined by offsets, having been platted, a straight line is drawn on the plat, across the crooked line, leaving as much space outside

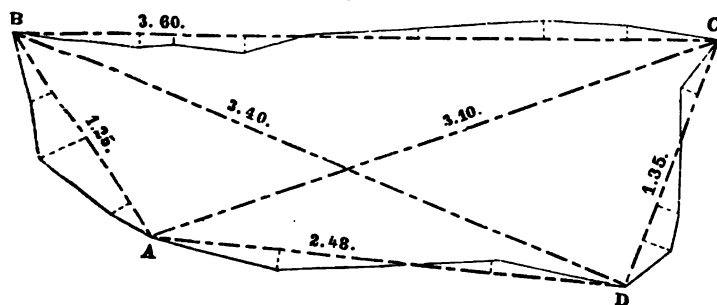
of the straight line as inside of it, as nearly as can be estimated by the eye, "equalizing" it, or "giving and taking" equal portions. The straight line is best determined by laying across the irregular outline the straight edge of a piece of transparent horn, or tracing-paper, or glass, or a fine thread or horse-hair stretched straight by a light bow of whalebone. In practical hands, this method is sufficiently accurate in most cases. The student will do well to try it on figures, the content of which he has previously ascertained by perfectly accurate methods.

### SURVEYING BY THE PRECEDING METHODS COMBINED.

102. All the methods which have been explained in the preceding sections—surveying by *Diagonals*, by *Tie-lines*, and by *Perpendiculars*, particularly in the form of offsets—are frequently required in the same survey. The method by *Diagonals* should be the leading one; in some parts of the survey obstacles to the measurements of diagonal may require the use of *Tie-lines*; and, if the fences are crooked, straight lines are to be measured near them, and their crooks determined by *Offsets*.

*Offsets* are necessary additions to almost every other method of surveying. In the smallest field surveyed by diagonals, unless all the fences are perfectly straight lines, their bends must be determined by offsets. The plat (scale of one chain to one inch) and field-notes of such a case are given below. A sufficient number of the sides, diagonals, and proof-lines, to prove the work, should be platted before platting the offsets.

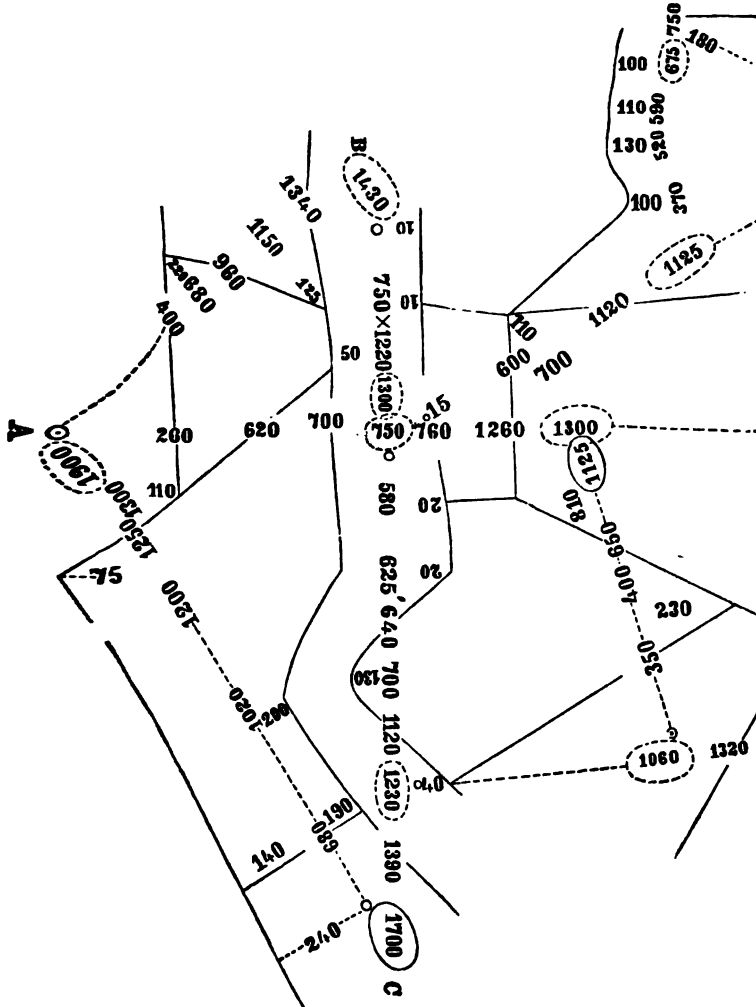
FIG. 78.





Field-Book No. 1.

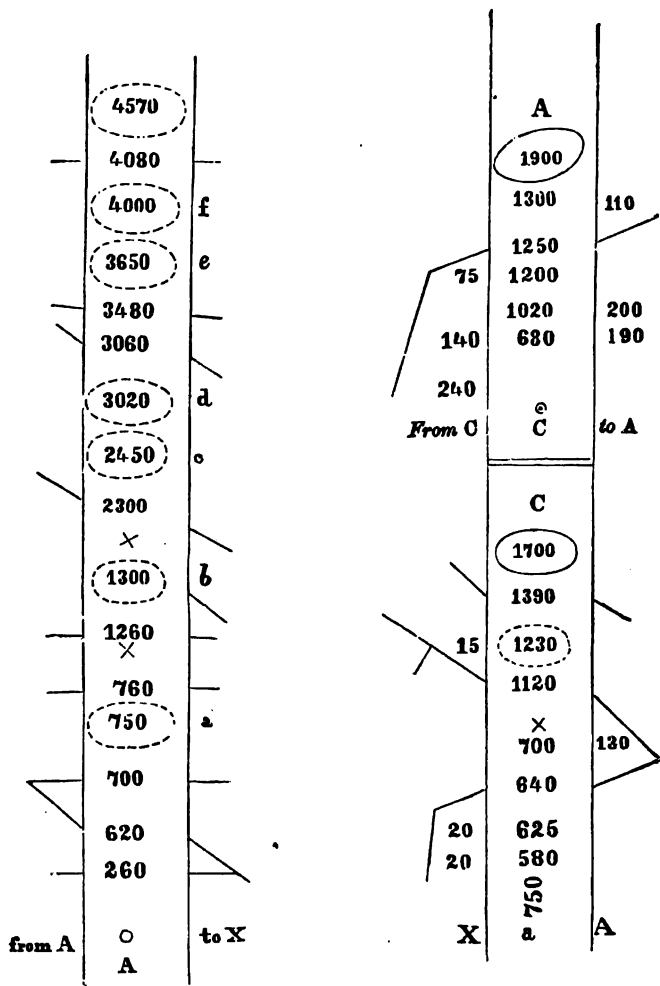
FIG. 79.



*Field-Book No. 1* (Fig. 79) shows the Sketch method, explained in Art. 83.

**Field-Book No. 2.**

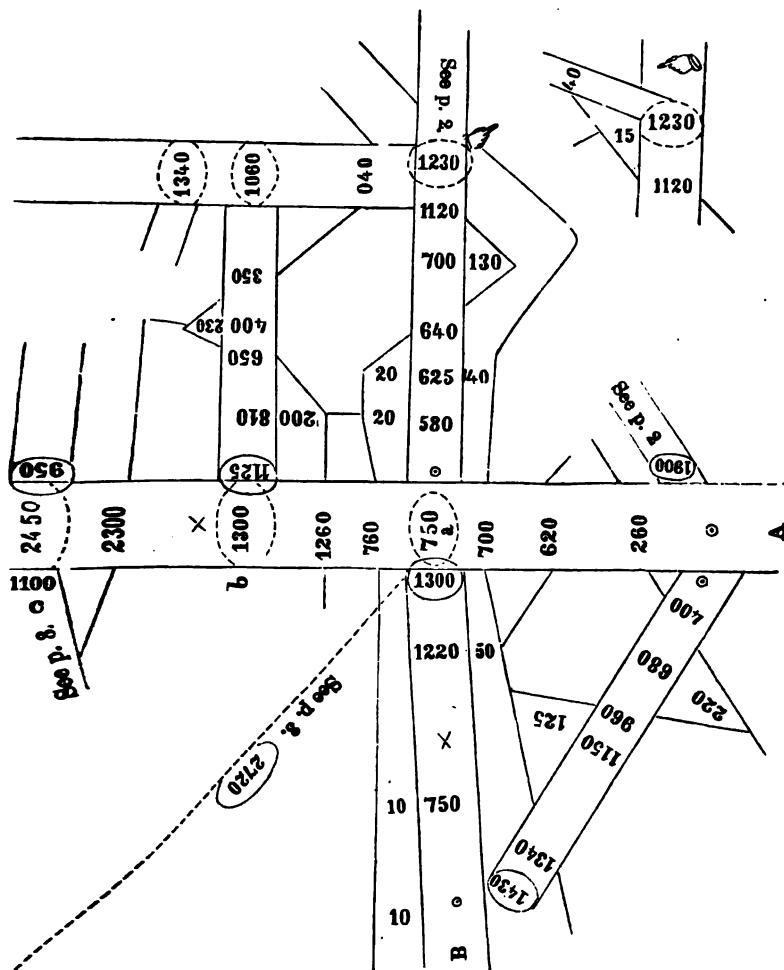
FIG. 80.



*Field-Book No. 2* (Fig. 80) shows the Column method, explained in Art. 84.

## Field-Book No. 3.

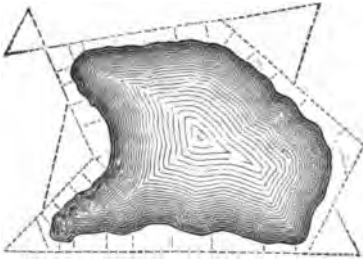
**FIG. 81.**



**Field-Book No. 3** (Fig. 81) is a convenient combination of the two preceding methods. The bottom of the book is at the side of this figure, at A.

**104. Inaccessible Areas.** A combination of offsets and tie-lines supplies an easy method of surveying an *inaccessible area*,

FIG. 82.



such as a pond, swamp, forest, block of houses, etc., as appears from the figure, in which external bounding lines are taken at will and measured, and tied by "tie-lines" measured between these lines, prolonged when necessary, while offsets

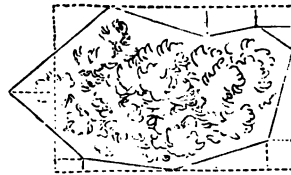
from them determine the irregularities of the actual boundaries of the pond, etc.

These *offsets* are *insets*, and their content is, of course, to be subtracted from the content of the principal figure.

Even a circular field might thus be approximately measured from the outside.

If the shape of the field admits of it, it will be preferable to measure four lines about the field in such directions as to inclose it in a rectangle, and to measure offsets from the sides of this to the angles of the field.

FIG. 83.



#### OBSTACLES TO MEASUREMENT IN CHAIN-SURVEYING.

**105.** In the practice of the various methods of surveying which have been explained, the hills and valleys which are to be crossed, the sheets of water which are to be passed over, the woods and houses which are to be gone through—all these form *obstacles* to the measurement of the necessary lines which are to join certain points, or to be prolonged in the same direction. Many special precautions and contrivances are therefore rendered necessary; and the best methods to be employed, when the chain alone is to be used, will now be given.

These methods for overcoming the various obstacles met with in practice constitute a **LAND-GEOMETRY**. Its problems are per-



formed on the ground instead of on paper; its *compasses* are a chain fixed at one end and free to swing around with the other; its *scale* is the chain itself; and its *ruler* is the same chain stretched tight. Its advantages are that its single instrument (or a substitute for it, such as a tape, a rope, etc.) can be found anywhere; and its only auxiliaries are equally easy to obtain, being a few straight and slender rods, and a plumb-line, for which a pebble suspended by a thread is a sufficient substitute.

Many of these problems require the employment of perpendicular and parallel lines. For this reason we will commence with this class of problems.

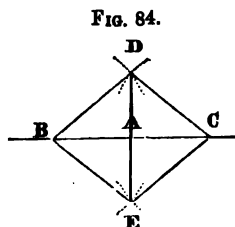
The demonstrations of most of these problems will be left as exercises for the student.

The elegant "Theory of Transversals" (Appendix B) will be an important element in some of these demonstrations.

### *Problems on Perpendiculars.\**

**Problem 1.** *To erect a perpendicular at any point of a line.*

**103. First Method.** Let A be the point at which a perpendicular to the line is to be set out. Measure off equal distances AB, AC, on each side of the point. Take a portion of the chain not quite  $1\frac{1}{2}$  time as long as AB or AC, fix one end of this at B, and describe an arc with the other end. Do the same from C. The intersection of these arcs will fix a point D. AD will be the perpendicular required. Repeat the operation on the other side of the line.

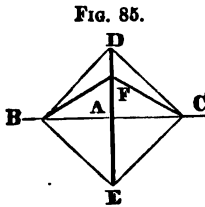


\* Many of these methods would seldom be required in practice, but cases sometimes occur, as every surveyor of much experience in field-work has found to his serious inconvenience, in which some peculiarity of the local circumstances forbids any of the usual methods being applied. In such cases the collection here given will be found of great value.

In all the figures, the given and measured lines are drawn with fine full lines, the visual lines, or lines of sight, with broken lines, and the lines of the result with heavy full lines. The points which are centers around which the chain is swung are enclosed in circles. The alphabetical order of the letters attached to the points shows in what order they are taken.

If that is impossible, repeat it on the same side with a different length of chain.

**107. Second Method.** Measure off as before, equal distances  $AB, AC$ , but each about only one third of the chain. Fasten the ends of the chain with two pins at  $B$  and  $C$ . Stretch it out on one side of the line and put a pin at the middle of it,  $D$ . Do the same on the other side of the line, and set a pin at  $E$ . Then is  $DE$  a perpendicular to  $BC$ . If it is impossible to perform the operation on both sides of the line, repeat it on the same side with a different length of chain, as shown by the lines  $BF$  and  $CF$  in the figure,

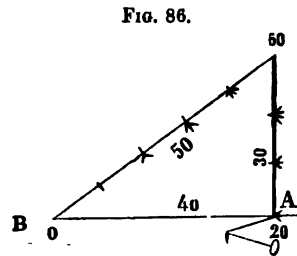


so as to get a second point.

**108. Other Methods.** All the methods to be given for the next problem may be applied to this.

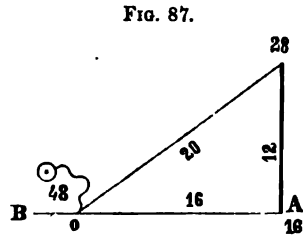
**Problem 2.** To erect a perpendicular to a line at a given point, when the point is at or near the end of the line.

**109. First Method.** Measure 40 links along the line. Let one assistant hold one end of the chain at that point; let a second hold the 20-link mark which is nearest the other end, at the given point  $A$ , and let a third take the 50-link mark, and tighten the chain, drawing equally on both portions of it. Then will the 50 link mark be in the perpendicular desired. Repeat the operation on the other side of the line so as to test the work.

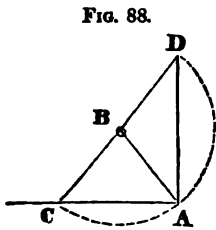


The above numbers are the most easily remembered, but the longer the lines measured the better; and nearly the whole chain may be used; thus: Fix down the 36th link from one end at  $A$ , and the 4th link from the same end on the line at  $B$ . Fix the other end of the chain also at  $B$ . Take the 40th-link mark from this last end, and draw the chain tight, and this mark will be in the perpendicular desired. The sides of the triangle formed by the chain will be 24, 32, and 40.

110. Otherwise : using a 50-foot tape, hold the 16-foot mark at A ; hold the 48-foot mark and the ring-end of the tape together on the line ; take the 28-foot mark of the tape, and draw it tight ; then will the 28-foot mark be in the perpendicular desired.



111. *Second Method.* Hold one end of the chain at A and fix the other end at a point B, taken at will. Swing the chain around B as a center, till it again meets the line at C. Then carry the same end around (the other end remaining at B) till it comes in the line of CB at D. AD is the perpendicular required.

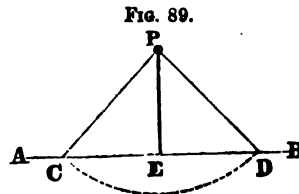


**Problem 3.** *To erect a perpendicular to an inaccessible line, at a given point of it.*

112. *First Method.* Get points in the direction of the inaccessible line prolonged, and from them set out a parallel to the line, by methods which are given in Art. 121, etc. Find by trial the point in which a perpendicular to this second line (and therefore to the first line) will pass through the required point.

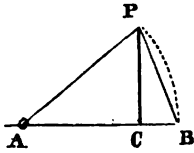
**Problem 4.** *To let fall a perpendicular from a given point to a given line.*

113. *First Method.* Let P be the given point, and AB the given line. Measure some distance, a chain or less, from C to P, and then fix one end of the chain at P, and swing it around till the same distance meets the line at some point D. The middle point E of the distance CD will be the required point, at which the perpendicular from P would meet the line.



**114. Second Method.** Stretch a chain, or a portion of it,

FIG. 90.



from the given point P, to some point, as A, of the given line. Hold the end of the distance at A, and swing round the other end of the chain from P, so as to set off the same distance along the given line from A to some point B. Measure BP. Then will the distance BC from B to the foot of the desired perpendicular

$$= \frac{BP^2}{2AB}$$

**Problem 5.** To let fall a perpendicular to a line from a point nearly opposite to the end of the line.

**115. First Method.** Stretch a chain from the given point P, to some point, as A, of the given line. Fix to the ground the middle point B of the chain AP, and swing around the end which was at P, or at A, till it meets the given line in a point C, which will be the foot of the required perpendicular.

FIG. 91.

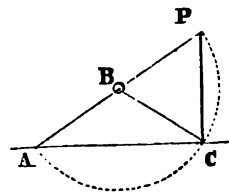


FIG. 92.

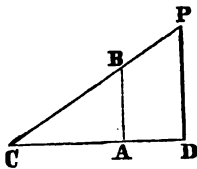
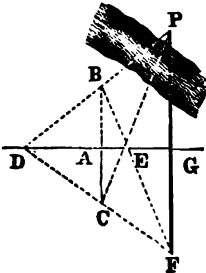


FIG. 93.



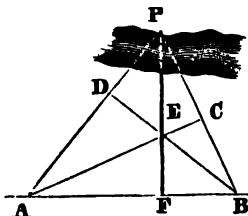
**116. Second Method.** At any convenient point, as A of the given line, erect a perpendicular of any convenient length, as AB, and mark a point C on the given line in the line of P and B. Measure CA, CB, and CP. Then the distance from C to the foot of the perpendicular, i. e.,  $CD = \frac{CA \times CP}{CB}$ .

**Problem 6.** To let fall a perpendicular to a line from an inaccessible point.

**117. First Method.** Let P be the given point. At any point A, on the given line, set out a perpendicular, AB, of any convenient length. Prolong it on the other side of

the line the same distance. Mark on the given line a point D in the line of P B, and a point E in the line of P C. Mark the point F at the intersection of D C and B E prolonged. The line F P is the line required, being perpendicular to the given line at the point G.

FIG. 94.

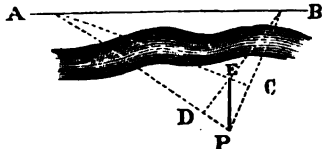


**118. Second Method.** Let A and B be two points of the given line. From A let fall a perpendicular, A C, to the visual line, B P; and from B let fall a perpendicular, B D, to the visual line, A P. Find the point at which these perpendiculars intersect, as at E, and the line P E, prolonged to F, will give the perpendicular required.

**Problem 7.** To let fall a perpendicular from a given point to an inaccessible line.

**119. First Method.** Let P be the given point, and A B the given line. By the preceding problem let fall perpendiculars from A to B P at C; and from B to A P at D; the line P E, passing from the given point to the intersection of these perpendiculars, is the desired perpendicular to the inaccessible line A B.

FIG. 95.



This method will apply when only two points of the line are visible.

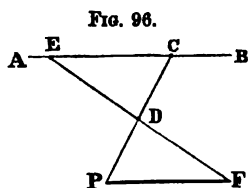
The proof of 118 and 119 is found in the "Theory of Transversals," Corollary 3.

**120. Second Method.** Through the given point set out a line parallel to the inaccessible line. At the given point erect a perpendicular to the parallel line, and it will be the required perpendicular to the inaccessible line.

#### Problems on Parallels.

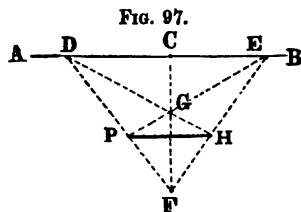
**Problem 1.** To run a line from a given point parallel to a given line.

**121. First Method.** Let fall a perpendicular from the point to the line. At another point of the line, as far off as possible, erect a perpendicular equal in length to the one just let fall. The line joining the end of this line to the given point will be the parallel required.



**122. Second Method.** Measure from P to any point, as C of the given line, and put a mark at the middle point D of that line. From any point, as E of the given line, measure a line to the point D, and continue it till  $DF = DE$ . Then will the line PF be parallel to AB.

**123. Third Method.** From any point, as C of the line, set off equal distances along the line to D and E. Take a point F, in the line of PD. Stake out the lines FC and FE, and also the line EP, crossing the line CF in the point G. Lastly, prolong the line DG till it meets the line EF in the point H. PH is the parallel required.

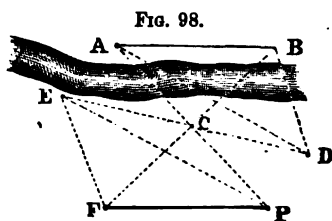


The proof is found in Corollary 4 of "Transversals."

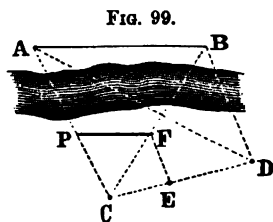
**Problem 2.** To run a line from a given point parallel to an inaccessible line.

**124. First Method.** Let AB be the given line, and P the given point. Set a stake at C, in the line of PA, and another at any convenient point, D. Through P set out, by the preceding problem, a parallel to DA, and set a stake at the point, as E, where this parallel intersects DC prolonged.

Through E set out a parallel to BD, and set a stake at the point F, where this parallel intersects BC prolonged. PF is the parallel required.



**125. Second Method.** Set a stake at any point C in the line of A P, and another at any convenient place, as at D. Through P set out a parallel to A D, intersecting C D in E. Through E set out a parallel to D B, intersecting C B in F. The line P F will be the parallel required.



**126. Alinement and Measurement.** We are now prepared, having secured a variety of methods for setting out Perpendiculars and Parallels in every probable case, to take up the general subject of overcoming Obstacles to Measurement.

Before a line can be measured its direction must be determined. This operation is called *Ranging* the line, or *Alining* it, or *Boning* it.\* The word *alinement*† will be found very convenient for expressing the direction of a line on the ground, whether between two points or in their direction prolonged.

This branch of our subject naturally divides itself into two parts, the first of which is preliminary to the second, viz. :

**I. Of Obstacles to Alinement; or how to establish the direction of a line in any situation.**

**II. Of Obstacles to Measurement; or how to find the length of a line which can not be actually measured.**

#### 1. Obstacles to Alinement.

**127.** All the cases which can occur under this head may be reduced to two, viz. :

A. To find points in a line *beyond* the given points, i. e., to *prolong* the line.

B. To find points in a line *between* two given points of it, i. e., to *interpolate* points in the line.

#### A. TO PROLONG A LINE.

**128. By ranging with Rods.** When two points in a line are given, and it is desired to prolong the line by ranging it out with

\* This word, like many others used in engineering, is derived from a French word, *borner*, to work out or limit, indicating that the Normans introduced the art of surveying into England.

† Slightly modified from the French *alignement*.

rods, three persons are required, each furnished with a straight, slender rod, and with a plumb-line, or other means of keeping

FIG. 100.



their rods vertical. One holds his rod at one of the given points, A in the figure, and another at B. A third, C, goes forward as far as he can

without losing sight of the first two rods, and then, looking back, puts himself "in line" with A and B—i. e., so that when his eye is placed at C the rod at B hides or covers the rod at A. This he can do most accurately by holding a plumb-line before his eye, so that it shall cover the first two rods. The lower end of the plumb-bob will then indicate the point where the third rod should be placed, and so with the rest. The first man, at A, is then signaled and comes forward, passes both the others, and puts himself at D, "in line" with C and B. The man at B then goes on to E, and "lines" himself with D and C; and so they proceed, in this "hand-over-hand" operation, as far as is desired. Stakes are driven at each point in the line as soon as it is determined.

**129.** The rods should be perfectly straight, either cylindrical or polygonal, and as slender as they can be without bending. They should be painted in alternate bands of red and white, each a foot or link in length. Their lower ends should be pointed with iron, and a projecting bolt of iron will enable them to be pressed down by the foot into the earth, so that they can stand alone. When this is done, one man can range out a line. A rod can be set perfectly vertical by holding a plumb-line before the eye at some distance from the rod, and adjusting the rod so that the plumb-line covers it from top to bottom, and then repeating the operation in a direction at right angles to the former. A stone dropped from top to bottom of the rods will approximately attain the same end.

FIG. 101.



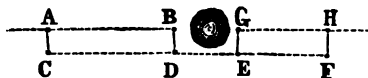
When the lines to be ranged are long, and great accuracy is required, the rods may have attached to them plates of tin with openings cut out of them, and black horse-hairs stretched from top to bottom of the openings.



A small telescope must then be used for ranging these hairs in line. In a hasty survey, straight twigs, with their tops split to receive a paper folded as in the figure, may be used.

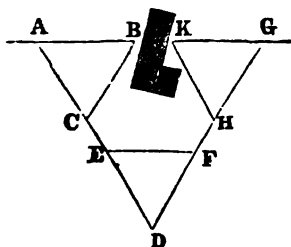
**130. By Perpendiculars.** The straight line, A B in the figure, is supposed to be stopped by a tree, a house, or other obstacle, and it is desired to prolong the line beyond this obstacle. From any two points, as A and B of the line, set off (by some of the methods which have been given) equal perpendiculars, A C and B D, long enough to pass the obstacle. Prolong this line beyond the obstacle, and from any two points in it, as E and F, measure the perpendiculars E G and F H equal to the first two, but in a contrary direction. Then will G and H be two points in the line A B prolonged which can be continued by the method of the last article. The points A and B should be taken as far apart as possible, as should also the points E and F. Three or more perpendiculars on each side of the obstacle may be set off, in order to increase the accuracy of the operation. The same thing may also be done on the other side of the line, as another confirmation or test of the accuracy of the prolonged line.

FIG. 102.



**131. By Equilateral Triangles.** The obstacles noticed in the last article may also be overcome by means of three equilateral triangles formed by the chain. Fix one end of the chain, and also the end of the first link from its other end, at B; fix the end of the 33d link at A; take hold of the 66th link and draw the chain tight, pulling equally on each part, and put a pin at the point thus found, C in the figure. An equilateral triangle will thus be formed, each side being 33 links. Prolong the line A C past the obstacle to some

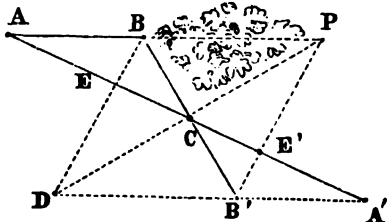
FIG. 103.



point, as D. Make another equilateral triangle, DEF, as before, and thus fix the point F. Prolong DF to a length equal to that of AD, and thus fix a point, G. At G form a third equilateral triangle, GHK, and thus fix a point, K. Then will KG give the direction of AB prolonged.

### 132. By Symmetrical Triangles.

Fig. 104.



Let AB be the line to be prolonged. Take any convenient point, as C. Range out the line, AC, to a point A', such that CA' = CA. Range out CB, so that CB' = CB. Range backward A'B' to some point D, such that DC prolonged will pass the obstacle. Find, by ranging, the intersection at E of DB and AC. From C measure, on CA', the distance CE' = CE. Then range out DC and B'E' to their intersection in P, which will be a required point in the direction of AB prolonged. The symmetrical points are marked by corresponding letters. Several other points should be obtained in the same manner.

In this, as in all similar operations, very acute intersections should be avoided as far as possible.

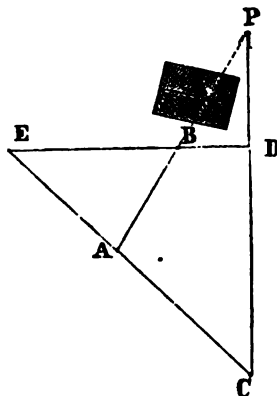
### 133. By Transversals.

Let AB be the given line. Take any two points C and D, such that the line CD will pass the obstacle. Take another point, E, in the intersection of CA and DB. Measure AE, AC, CD, BD, and BE. Then the distance from D to P, a point in the required prolongation, will

$$\text{be } DP = \frac{CD \times BD \times AE}{BE \times AC - BD \times AE}.$$

Other points in the prolongation may be obtained in the same manner, by merely moving the single point C in

Fig. 105.



the line of E A ; in which case the new distances, C A and C D, will alone require to be measured.

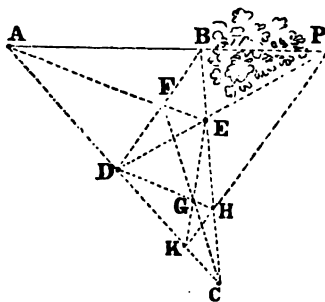
If A E be made equal to A C, then is  $DP = \frac{CD \times BD}{BE - BD}$ .

If B E be made equal to B D, then is  $DP = \frac{CD \times AE}{AC - AE}$ .

The *minus* sign in the denominators must be understood as only meaning that the difference of the two terms is to be taken, without regard to which is the greater.

**134. By Harmonic Conjugates.** Let A B be the given line. Set a stake at any point C. Set stakes at points D, on the line C A, and at E, on the line C B ; these points, D and E, being so chosen that the line D E will pass beyond the obstacle. Set a fourth stake, F, at the intersection of the lines A E and D B. Set a fifth stake, G, anywhere in the line C F ; a sixth stake, H, at the intersection of C B and D G prolonged ; and a seventh, K, at the intersection of C A and E G prolonged. Finally, range out the lines D E and K H, and their intersection at P will be in the line A B prolonged.

FIG. 106.

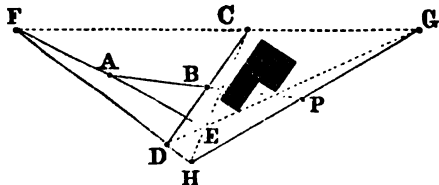


**135. By the Complete Quadrilateral.** Let A B be the given line.

Take any convenient point C ; measure from it to B, and onward, in the same line prolonged, an equal distance to D. Take any other convenient point, E, such that C E and D E produced will clear the obstacle.

Measure from E to A, and onward, an equal distance, to F. Range out the lines F C and D E to their intersection in G.

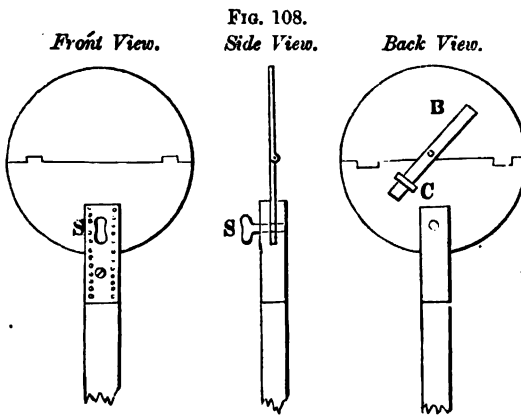
FIG. 107.



Range out  $FD$  and  $CE$  to intersect in  $H$ . Measure  $GH$ . Its middle point,  $P$ , is the required point in the line of  $AB$  prolonged. The unavoidable acute intersections in this construction are objectionable.

B. TO INTERPOLATE POINTS IN A LINE.

136. The most distant given point of the line must be made



as conspicuous as possible by any efficient means, such as placing there a staff bearing a flag : red and white, if seen against woods or other dark background ; and red and green, if seen against the sky.

A convenient and portable signal is shown in the figure.

The figure represents a disk of tin about six inches in diameter, painted white and hinged in the middle, to make it more portable. It is kept open by the bar,  $B$ , being turned into the catch,  $C$ . A screw,  $S$ , holds the disk in a slit in the top of the pole.

Another contrivance is a strip of tin, which has its ends bent horizontally in contrary directions. As the wind will take strongest hold of the side which is concave toward it, the bent strip will continually revolve, and thus be very conspicuous. Its upper half should be painted red, and its lower half white.

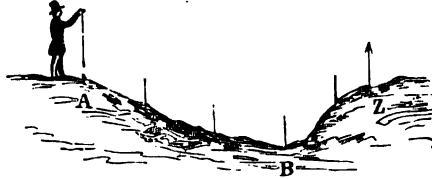
A bright tin cone set on the staff can be seen at a great distance when the sun is shining.

137. Ranging to a point thus made conspicuous is very simple when the ground is level. The surveyor places his eye at the nearest end of the line, or stands a little behind a rod placed on it, and by signs moves an assistant, holding a rod at some point as nearly

in the desired line as he can guess, to the right or left, till his rod appears to cover the distant point.

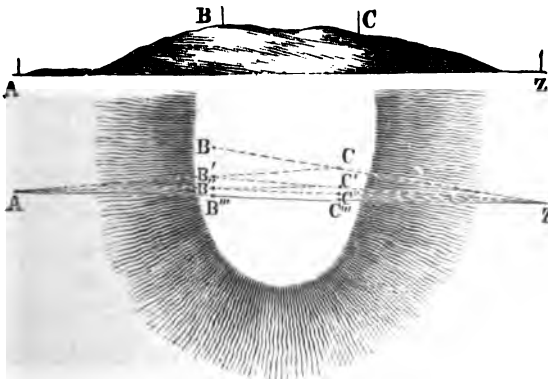
**138. Across a Valley.** When a valley or low spot intervenes between the two ends of the line, A and Z in the figure, a rod held in the low place, as at B, would seldom be high enough to be seen from A, to cover the distant rod at Z. In such a case, the surveyor at A should hold up a plumb-line over the point, at arm's length, and place his eye so that the plumb-line covers the rod at Z. He should then direct the rod held at B to be moved till it, too, is covered by the plumb-line. The point B is then said to be "in line" between A and Z. In geometrical language, B has now been placed in the vertical plane determined by the vertical plumb-line and the point Z. Any number of intermediate points can thus be "interpolated," or placed in line between A and Z.

FIG. 109.



**139. Over a Hill.** When a hill rises between two points and prevents one being seen from the other, as in the figure (the upper part of which shows the hill in

FIG. 110.



shows the hill in "elevation," and the lower part in "plan"), two observers, B and C, each holding a rod, may place themselves on the ridge, in the line between the two points, as nearly as they

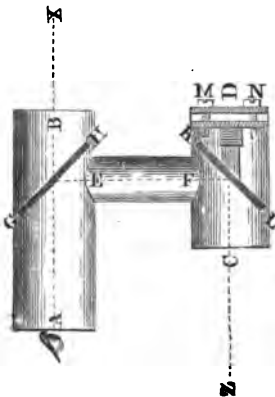
can guess, and so that each can at once see the other and the point

beyond him. B looks to Z, and by signals puts C "in line." C then looks to A, and puts B in line at B'. B repeats his operation from B', putting C at C', and is then himself moved to B'', and so they alternately "line" each other, continually approximating to the straight line between A and Z, till they at last find themselves both exactly in it, at B''' and C'''.

140. A single person may put himself in line between two points, on the same principle, by laying a straight stick on some support, going to each end of it in turn, and making it point successively to each end of the line. The "Surveyor's Cross," Art. 93, is convenient for this purpose, when set up between the two given points and moved again and again, until, by repeated trials, one of its slits sights to the given points when looked through in either direction.

141. **On Water.** A simple instrument for the same object is represented in the figure. A B and C D are two tubes, about  $1\frac{1}{2}$  inch in diameter, connected by a smaller tube, E F.

FIG. 111.

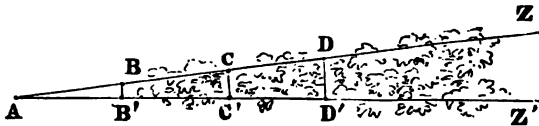


A piece of looking-glass, G H, is placed in the lower part of the tube A B, and another, K L, in the tube C D. The planes of the two mirrors are at right angles to each other. The eye is placed at A, and the tube A B is directed to any distant object, as X, and any other object behind the observer, as Z, will be seen, apparently under the first object in the mirror G H, by reflection from the mirror K L, when the observer has

succeeded in getting in line between the two objects. M N are screws by which the mirror K L may be adjusted. The distance between the two tubes will cause a small parallax, which will, however, be insensible except when the two objects are near together.

**142. Through a Wood.** When a wood intervenes between any two given points, preventing one from being seen from the other, as in the figure, in which A and Z are the given points, proceed thus: Hold a rod

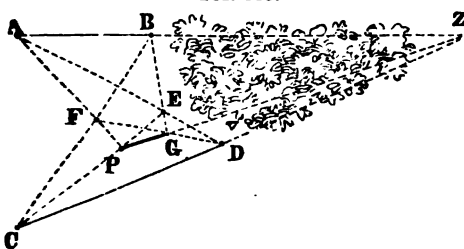
FIG. 112.



at some point B' as nearly in the desired line from A as can be guessed at, and as far from A as possible. To approximate to the proper direction, an assistant may be sent to the other end of the line, and his shouts will indicate the direction; or a gun may be fired there; or, if very distant, a rocket may be sent up after dark. Then range out the "random line" A B', by the method given in Art. 128, noting also the distance from A to each point found, till you arrive at a point Z', opposite to the point Z—i. e., at that point of the line from which a perpendicular there erected would strike the point Z. Measure Z' Z. Then move each of the stakes, perpendicularly from the line A Z', a distance proportional to their distances from A. Thus, if A Z' be 1,000 links, and Z' Z be 10 links, then a stake B', 200 links from A, should be moved 2 links to a point B, which will be in the desired straight line A Z; if C' be 400 links from A, it should be moved 4 links to C, and so with the rest. The line should then be cleared, and the accuracy of the position of these stakes tested by ranging from A to Z.

**143. To an Invisible Intersection.** Let A B and C D be two

FIG. 113.



lines, which, if prolonged, would meet in a point Z, invisible from either of them; and let P be a point from which a line is required to be set out tending to this invisible intersection.

Set stakes at the five given points, A, B, C, D, P. Set a sixth stake at E, in the

alinements of AD and CP; and a seventh stake at F, in the alinements of BC and AP. Then set an eighth stake at G, in the alinements of BE and DF. PG will be the required line. This is an application of the "Theory of Transversals."

*Otherwise:* Through P range out a parallel to the line BD. Note the points where this parallel meets AB and CD, and call these points Q and R. Then the distance from B, on the line BD, to a point which shall be in the required line running from P to the invisible point, will be  $= \frac{BD \times QP}{QR}$ .

## II. Obstacles to Measurement.

**144.** The cases in which the direct measurement of a line is prevented by various obstacles may be reduced to three:

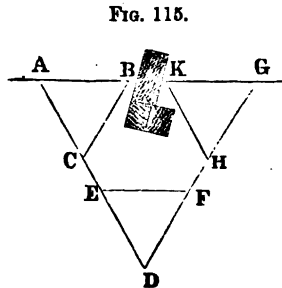
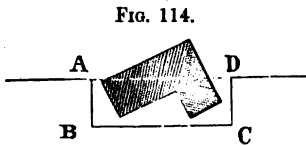
- A. When both ends of the line are accessible.
- B. When one end of it is inaccessible.
- C. When both ends of it are inaccessible.

### A. WHEN BOTH ENDS OF THE LINE ARE ACCESSIBLE.

**145. By Perpendiculars.** On reaching the obstacle, as at A in the figure, set off a perpendicular, AB; turn a second right angle at B, and measure past the obstacle; turn a third right angle at C, and measure to the original line at D. Then will the measured distance, BC, be equal to the desired distance, AD.

If the direction of the line is also unknown, it will be most easily obtained by the additional perpendiculars shown in Fig. 102 of Art. 130.

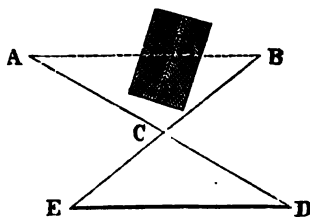
**146. By Equilateral Triangles.** The method given in Art. 131 for determining the direction of a line through an obstacle will also give its length; for in Fig. 115 the desired distance AG is equal to the measured distances AD or DG.





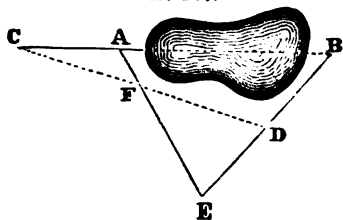
**147. By Symmetrical Triangles.** Let  $AB$  be the distance required. Measure from  $A$  obliquely to some point  $C$  past the obstacle. Measure onward, in the same line, till  $CD$  is as long as  $AC$ . Place stakes at  $C$  and  $D$ . From  $B$  measure to  $C$ , and from  $C$  measure onward, in the same line, till  $CE$  is equal to  $CB$ . Measure  $ED$ , and it will be equal to  $AB$ , the distance required. If more convenient, make  $CD$  and  $CE$  equal, respectively, to half of  $AC$  and  $CB$ ; then will  $AB$  be equal to twice  $DE$ .

FIG. 116.



**148. By Transversals.** Let  $AB$  be the required distance. Set a stake,  $C$ , in the line prolonged; set another stake,  $D$ , so that  $C$  and  $B$  can be seen from it; and a third stake,  $E$ , in the line of  $BD$  prolonged, and at a distance from  $D$  equal to the distance from  $D$  to  $B$ . Set a fourth stake,  $F$ , at the intersection of  $EA$  and  $CD$ .

FIG. 117.

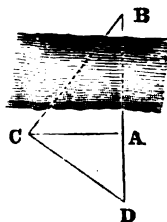


Measure  $AC$ ,  $AF$ , and  $FE$ . Then is  $AB = \frac{AC}{AF} (FE - AF)$ .

**B. WHEN ONE END OF THE LINE IS INACCESSIBLE.**

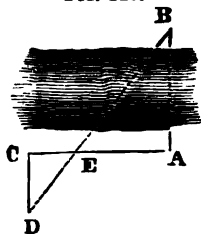
**149. By Perpendiculars.** This principle may be applied in a variety of ways. In Fig. 118 let  $AB$  be the required distance. At the point  $A$  set off  $AC$  perpendicular to  $AB$ , and of any convenient length. At  $C$  set off a perpendicular to  $CB$ , and continue it to a point,  $D$ , in the line of  $A$  and  $B$ . Measure  $DA$ . Then is  $AB = \frac{AC^2}{AD}$ .

FIG. 118.



**150. Otherwise:** At the point  $A$ , in Fig. 119, set off a perpendicular,  $AC$ . At  $C$  set off another perpendicular

FIG. 119.



lar, CD. Find a point, E, in the line of AC and BD. Measure AE and EC. Then is  $AB = \frac{AE \times CD}{CE}$ .

If EC be made equal to AE, and D be set in the line of BE, and also in the perpendicular from C, then will CD be equal to AB.

If  $EC = \frac{1}{2} AE$ , then  $CD = \frac{1}{2} AB$ .

**151. Otherwise:** At A, in Fig. 120, measure a perpendicular, AC, to the line AB; and at any point, as D in this line, set off a perpendicular to DB, and continue it to a point E, in the line of CB. Measure DE and also DA.

Then is  $AB = \frac{AC \times AD}{DE - AC}$ .

FIG. 120.

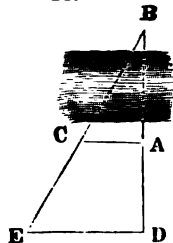
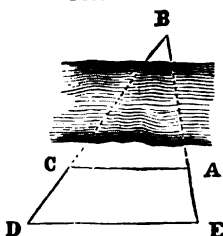


FIG. 121.

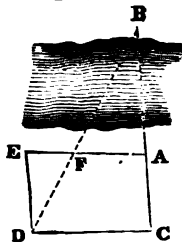


**152. By Parallels.** From A measure AC in any convenient direction. From a point D, in the line of BC, measure a line parallel to CA, to a point E in the line of AB. Measure also AE.

Then is  $AB = \frac{AC \times AE}{DE - AC}$ .

**153. By a Parallelogram.** Set a stake, C, in the line of A and B, and set another stake, D, wherever convenient. With a distance equal to CD, describe from A an arc on the ground; and, with a distance equal to AC, describe another arc from D intersecting the first arc in E. Or, take AC and CD so that together they make one chain; fix the ends of the chain at A and D; take hold of the chain at such a link that one part of it equals AC and the other CD, and draw it tight to fix the point E. Set a stake at F in the intersection

FIG. 122.



of A E and D B. Measure A F and E F. Then is  $AB = \frac{AC \times AF}{EF}$ ; or  $CB = \frac{AC \times CD}{EF}$ .

**154. By Symmetrical Triangles.** Let A B be the required distance. From A measure a line in any convenient direction, as A C, and measure onward, in the same direction, till  $CD = AC$ . Take any point E in the line of A and B. Measure from E to C, and onward in the same line, till  $CF = CE$ . Then find by trial a point G, which shall be at the same time in the line of C and B, and in the line of D and F. Measure the distance from G to D, and it will be equal to the required distance from A to B. If more convenient, make  $CD = \frac{1}{2} AC$ , and  $CF = \frac{1}{2} CE$ , as shown by the finely dotted lines in the figure. Then will  $DG = \frac{1}{2} AB$ .

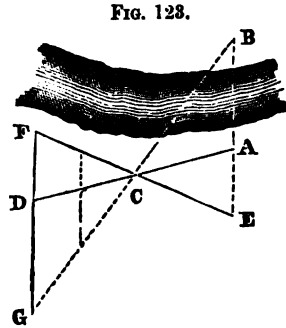


FIG. 123.

**155. Otherwise:** Prolong B A to some point C. Range out any convenient line C A', and measure  $CA' = CA$ . The triangle C A' B is now to be reproduced in a symmetrical triangle situated on the accessible ground. For this object take, on A C, some point D and measure  $CD' = CD$ . Find the point E at the intersection of A D' and A' D. Find the point F at the intersection of A' B and C E. Lastly, find the point B' at the intersection of A F and C A'. Then will  $A' B' = AB$ . The symmetrical points have corresponding letters affixed to them.

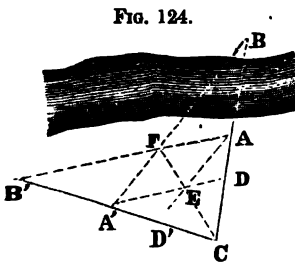
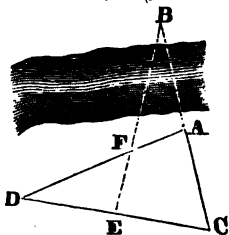


FIG. 124.

**156. By Transversals.** Set a stake, C, in the alinement of B A; a second, D, at any convenient point; a third, E, in the line CD; and a fourth, F, at the intersection of the aline-

FIG. 125.



ments of DA and EB. Measure AC, CE, ED, DF, and FA. Then is  $AB =$

$$\frac{AC \times AF \times DE}{CE \times DF - AF \times DE}$$

If the point E be taken in the middle of CD (as it is in the figure), then  $AB =$

$$\frac{AC \times AF}{DF - AF}$$

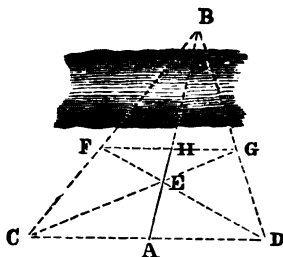
If the point F be taken in the middle of AD, then  $AB =$   
 $\frac{AC \times DE}{CE - DE}$

The *minus* signs must be interpreted as in Art. 121.

**157. By Harmonic Division.** Set stakes, C and D, on each side of A, and so that the three are in the same straight line. Set a third stake at any point, E, of the line AB. Set a fourth, F, at the intersection of CB and DE; and a fifth, G, at the intersection of DB and CE. Set a sixth stake, H, at the intersection of AB and FG. Measure AE and EH. Then is

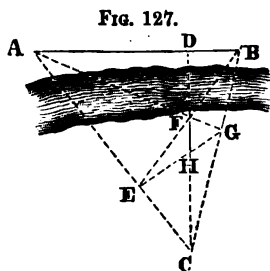
$$AB = \frac{AE \times AH}{AE - EH}$$

FIG. 126.



**158. To an Inaccessible Line.** The shortest distance, CD, from

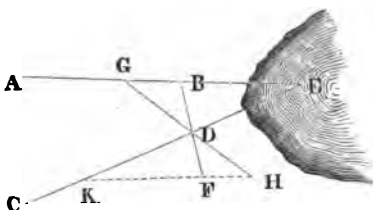
a given point, C, to an inaccessible straight line AB, is required. From C let fall a perpendicular to AB, by the method of Art 119. Then set a stake at any point, E, on the line AC; set a second, F, at the intersection of EB and CD; a third, G, at the intersection of AF and CB; and a fourth, H, at the intersection of EG and CD.



Measure CH and HF. Then is  $CD = \frac{CH \times CF}{CH - HF}$ ; or  $CD = CH \cdot \frac{CH + HF}{CH - HF}$ ; or  $CD = \frac{CH \times CF}{2CH - CF}$

**159. To an Inaccessible Intersection.** When two lines (as A B, C D, in the figure) meet in a river, a building, or any other inaccessible point, the distance from any point of either to their intersection, D E, for example, may be found thus: From any point B, on one line, measure B D, and continue it till D F = D B. From any other point G of the former line measure G D, and continue the line till D H = G D. Continue H F to meet D C in some point K. Measure K D. K D will be equal to the desired distance D E.

FIG. 128.



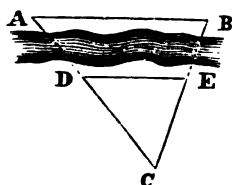
B E can be found by measuring F K, which is equal to it.

If D F and D H be made respectively equal to one half or one third, etc., of D B and D G, then will K D and K F be respectively equal to one half or one third, etc., of D E and B E.

C. WHEN BOTH ENDS OF THE LINE ARE INACCESSIBLE.

**160. By Similar Triangles.** Let A B be the inaccessible distance.

FIG. 129.



Set a stake at any convenient point C, and find the distances C A and C B by any of the methods just given. Set a second stake at any point, D, on the line C A.

Measure a distance equal to  $\frac{C B \times C D}{C A}$ , from C, on the line C B, to some point E.

Measure D E. Then is  $A B = \frac{A C \times D E}{C D}$ .

If more convenient, measure C D in the contrary direction from the river, as in Fig. 130, instead of toward it, and in other respects proceed as before.

**161. By Parallels.** Let A B be the inaccessible distance. From any point, as C, range out a parallel to A B, as in Art. 124, etc. Find the distance C A by Art. 149, etc. Set a stake at the point E, the

FIG. 130.

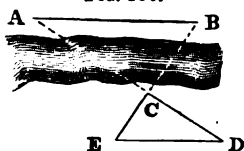
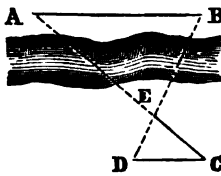


FIG. 131.

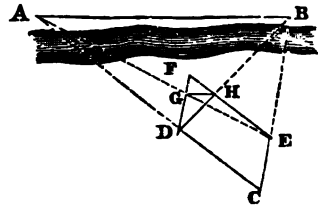


intersection of  $CA$  and  $DB$ , and measure  $CE$ . Then is  $AB = \frac{CD \times (AC - CE)}{CE}$ .

**162. By a Parallelogram.** Set a stake at any convenient point  $C$ . Set stakes  $D$  and  $E$  anywhere in the alineaments  $CA$  and  $CB$ .

With  $D$  as a center, and a length of the chain equal to  $CE$ , describe an arc; and with  $E$  as a center, and a length of the chain equal to  $CD$ , describe another arc, intersecting the former one at  $F$ . A parallelogram,  $CDEF$ , will thus be formed. Set stakes at  $G$  and  $H$ , where the alineaments  $DB$  and  $EA$  intersect the sides of this parallelogram. Measure  $CD$ ,  $DF$ ,  $GF$ ,  $FH$ , and  $HG$ . The inaccessible distance  $AB = \frac{CD \times DF \times GH}{FG \times FH}$ .

FIG. 132.

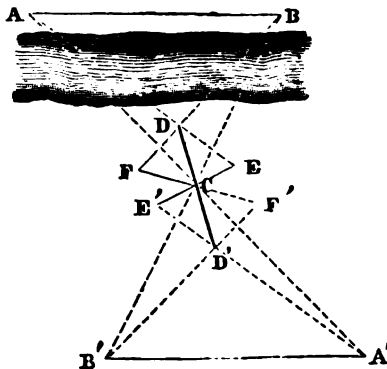


$$\text{If } CD = CE, \text{ then } AB = \frac{CD' \times GH}{FG \times FH}.$$

**163. By Symmetrical Triangles.**

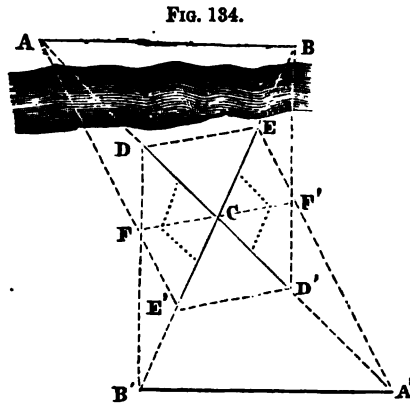
Take any convenient point, as  $C$ . Set stakes at two other points,  $D$  and  $D'$ , in the same line, and at equal distances from  $C$ . Take a point  $E$ , in the line of  $AD$ ; measure from it to  $C$ , and onward till  $CE' = CE$ . Take a point  $F$  in the line of  $BD$ ; measure from it to  $C$ , and onward till  $CF' = CF$ . Range out the lines  $AC$  and  $E'D'$ , and set a stake at their intersection,  $A'$ . Range out the

FIG. 133.



lines  $BC$  and  $F'D'$ , and set a stake at their intersection,  $B'$ . Measure  $A'B'$ . It will be equal to the desired distance  $AB$ .

**164. Otherwise:** Take any convenient point, as C, and set off equal distances on each side of it, in the line of CA, to D and D'. Set off the same distances from C, in the line of CB, to E and E'. Through C set out a parallel to DE or D'E', and set stakes at the points F and F' where this parallel intersects AE' and BD'. Range out the lines AD' and EF', and set a stake at their intersection A'. Range out the lines BE' and DF, and set a stake at their intersection B'. Measure A'B', and it will be equal to the desired distance AB.



## CHAPTER III.

### COMPASS-SURVEYING ; OR BY THE THIRD METHOD.

165. *Angular Surveying* determines the relative positions of points, and therefore of lines, on the THIRD PRINCIPLE, as explained in Art. 5.

Either the compass or the transit may be employed in angular surveying.

166. Surveying with the compass is a less direct operation than surveying with the transit. But as the use of the compass is much more rapid and easy, for this reason, as well as for its smaller cost, it is the instrument most commonly employed in land-surveying in spite of its imperfections and inaccuracies.

The method of *Polar Surveying* (or surveying by the third method) embraces two minor methods. The most usual one consists in going around the field with the instrument, setting it at each corner, and measuring there the angle which each side makes with its neighbor, as well as the length of each side. This method is called by the French the method of *Cheminement*. It has no special name in English, but may be called (from the American verb, to progress) the *Method of Progression*. The other system, the *Method of Radiation*, consists in setting the instrument at one point and thence measuring the direction and distance of each corner of the field or other object. The corresponding name of what we have called triangular surveying is the *Method of Intersections*, since it determines points by the intersections of straight lines.



**167.** When the two lines which form an angle lie in the same horizontal or level plain, the angle is called a *horizontal angle*.\*

When these lines lie in a plane perpendicular to the former, the angle is called a *vertical angle*.

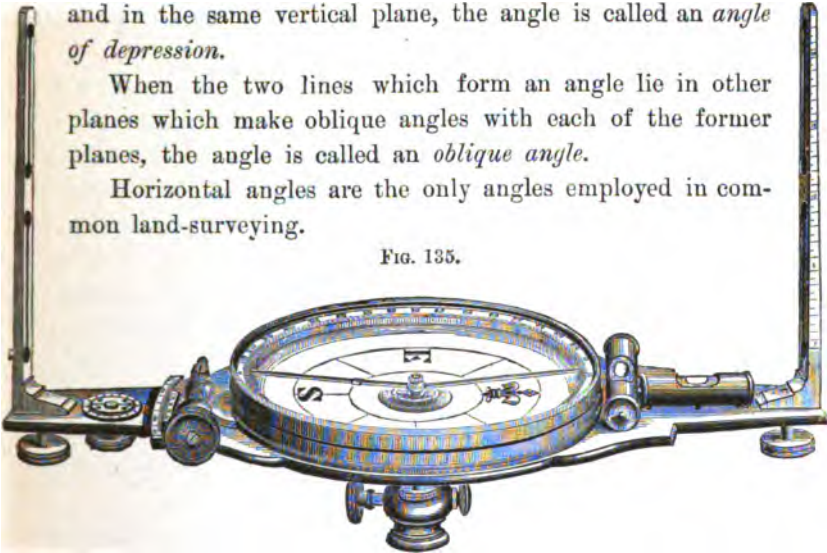
When one of the lines is horizontal, and the other line from the eye of the observer passes above the former, and in the same vertical plane, the angle is called an *angle of elevation*.

When the latter line passes below the horizontal line, and in the same vertical plane, the angle is called an *angle of depression*.

When the two lines which form an angle lie in other planes which make oblique angles with each of the former planes, the angle is called an *oblique angle*.

Horizontal angles are the only angles employed in common land-surveying.

FIG. 135.



### THE COMPASS.

**168. The Needle.** The most essential part of the compass is the magnetic needle. It is a slender bar of steel, usually five or six inches long, strongly magnetized, and balanced on a pivot, so that it may turn freely, and thus be enabled to continue pointing in the same direction (that of the "*magnetic meridian*," approximately north and south) however much the "*compass-box*," to which the pivot is attached, may be turned around.

As it is important that the needle should move with the least

\* A plane is said to be *horizontal* or *level* when it is parallel to the surface of standing water, or perpendicular to a plumb-line. A line is horizontal when it lies in a horizontal plane.

possible friction, the pivot should be of the hardest steel ground to a very sharp point; and in the center of the needle, which is to rest on the pivot, should be inserted a cap of agate, or other hard material. Iridium for the pivot, and ruby for the cap, are still better.

If the needle be balanced on its pivot before being magnetized, one end will sink, or "dip," after the needle is magnetized. To bring it to a level, several coils of wire are wound around the needle so that they can be slid along it, to adjust the weight of its two ends and balance it more perfectly.

The north end of the needle is usually cut into a more ornamental form than the south end for the sake of distinction.

The principal requisites of a compass-needle are intensity of directive force and susceptibility. Beyond a certain limit, say five inches, no additional power is gained by increasing the length of the needle. On the contrary, longer ones are apt to have their strength diminished by several consecutive poles being formed. Short needles, made very hard, are therefore to be preferred.

The needle should not come to rest very quickly. If it does, it indicates either that it is weakly magnetized, or that the friction on the pivot is great. Its sensitiveness is indicated by the number of vibrations which it makes in a small space before coming to rest.

A screw, with a milled head, on the under side of the plate which supports the pivot, is used to raise the needle off this pivot when the instrument is carried about, to prevent the point being dulled by unnecessary friction.

**169. The Sights.** Next after the needle, which gives the direction of the fixed line whose angles with the lines to be surveyed are to be measured, should be noticed the sights, which show the directions of these last lines. At each end of a line passing through the pivot is placed a "sight," consisting of an upright bar of brass, with openings in it of various forms—usually slits, with a circular aperture at their top and bottom; all these arrangements being intended to enable the line of sight to be directed to any desired object with precision.

A telescope which can move up and down in a vertical plane, i. e., a plunging telescope, or one which can turn completely over, is sometimes substituted for the sights. It has the great advantage of giving more distinct vision at long distances, and of admitting of sights up and down very steep slopes. Its accuracy of vision is, however, rendered nugatory by the want of precision in the readings of the needle. If a telescope be applied to the compass, a graduated circle with vernier should be added, thus converting the compass into a "transit."

**170. The Divided Circle.** We now have the means of indicating the directions of the two lines whose angle is to be measured. The number of degrees contained in it is to be read from a circle divided into degrees, in the center of which is fixed the pivot bearing the needle. The graduations are usually made to half a degree, and a quarter of a degree or less can then be "estimated." The pivot and needle are sunk in a circular box, so that its top may be on a level with the needle. The graduations are usually made on the top of the surrounding rim of the box, but should also be continued down its inside circumference so that it may be easier to see with what division the ends of the needle coincide.

The degrees are not numbered consecutively from  $0^\circ$  around to  $360^\circ$ , but run from  $0^\circ$  to  $90^\circ$ , both ways from the two diametrically opposite points at which a line, passing through the slits in the middle of the sights, would meet the divided circle.

The lettering of the surveyor's compass has one important difference from that of the mariner's compass.

When we stand facing the north, the east is on our right hand, and the west on our left. The graduated card of the mariner's compass, which is fastened to the needle and turns with it, is marked accordingly. But, in the surveyor's compass, one of the 0 points being marked N. or north (or indicated by a *fleur-de-lis*), and the opposite one S. or south, the 90-degrees-point on the *right* of this line, as you stand at the S. end and look toward the N., is marked W. or west; and the *left* hand 90-degrees-point is marked E. or east. The reason of this will be seen when the method of using the compass comes to be explained.

171. **The Points.** In ordinary land-surveying only four points of the compass have names, viz., north, south, east, and west;

FIG. 136.



the direction of a line being described by the angle which it makes with a north and south line to its east or to its west.

But, for nautical purposes, the circle of the compass is divided into thirty-two points, the names of which are shown in the figure.

Two rules embrace all the cases :

1. When the letters indicating two points are joined together, the point half-way between the two meant; thus, N. E. is

half-way between north and east; and N. N. E. is half-way between north and northeast. 2. When the letters of two points are joined together with the intermediate word *by*, it indicates the point which comes next after the first in going toward the second; thus, N. *by* E. is the point which follows north in going toward the east; S. E. *by* S. is the next point from southeast going toward the south.

172. **Eccentricity.** The center-pin, or pivot of the needle, ought to be exactly in the center of the graduated circle; the needle ought to be straight, and the line of the sights ought to pass exactly through this center and through the 0 points of the circle. If this is not the case, there will be an error in every observation. This is called the *error of eccentricity*.

When the maker of a compass is about to fix the pivot in place, he is in doubt of two things: whether the needle is perfectly straight, and whether the pivot is exactly in the center. In Figs. 137 and 138 both of these are represented as being excessively in error.

*First*, to examine if the needle be straight. Fix the pivot temporarily so that the ends of the needle may cut opposite degrees—i. e., degrees differing by  $180^\circ$ . The condition of things at

this stage of progress will be represented by Fig. 137. Then turn the compass-box half-way around. The error will now be doubled,

FIG. 137.

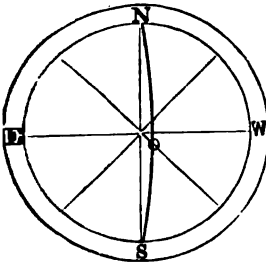


FIG. 138.

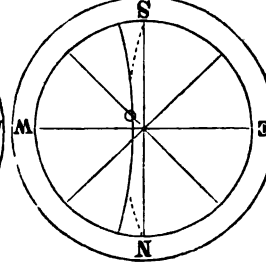
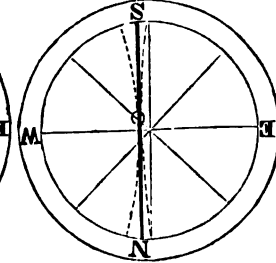


FIG. 139.



as is shown by Fig. 138, in which the former position of the needle is indicated by a dotted line.\* Now bend the needle, as in Fig. 139, till it cuts divisions midway between those cut by it in its present and in its former position. This makes it certain that the needle is straight, or that its two ends and its center lie in the same straight line.

*Second*, to put the pivot in the center. Move it till the straightened needle cuts opposite divisions. It is then certain that the direction of the needle passes through the center. Turn the compass-box one quarter around, and, if the needle does not then cut opposite divisions, move the pivot till it does. Repeat the operation in various positions of the box. It will be a sufficient test if it cuts the opposite divisions of  $0^\circ$ ,  $45^\circ$ , and  $90^\circ$ .

To fix the sights precisely in line, draw a hair through their slits and move them till the hair passes over the 0 points on the circle.

The surveyor can also examine for himself, by the principle of reversion, whether the line of the sights passes through the center or not. Sight to any very near object. Read off the number of degrees indicated by one end of the needle. Then turn the compass half around, and sight to the same object. If the two readings do not agree, there is an error of eccentricity, and the arithmetical mean, or half sum of the two readings, is the correct one.

In Fig. 140 the line of sight A B is represented as passing to

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\* This is another example of the fruitful principle of *reversion*.

one side of the center, and the needle as pointing to  $46^\circ$ . In Fig. 141 the compass is supposed to have been turned half around, and

FIG. 140.

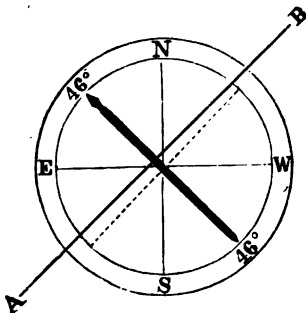
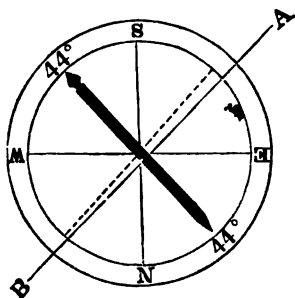


FIG. 141.



the other end of the sights to be directed to the same object. Suppose that the needle would have pointed to  $45^\circ$  if the line of sight had passed through the center; the needle will now point to  $44^\circ$ , the error being doubled by the reversion, and the true reading being the mean.

This does not, however, make it certain that the line of the sights passes through the 0 points, which can only be tested by the hair, as mentioned above.

**173. Levels.** On the compass-plate are two small spirit-levels. They consist of glass tubes slightly curved upward, and nearly filled with alcohol, leaving a bubble of air within them. One of them lies in the direction of the sights, and the other at right angles to this direction. To adjust them, move the plate until the bubbles are brought to the centers of the tubes, and then turn the plate half way around. If the bubbles remain in the center, no adjustment is necessary. If they do not, bring the bubbles half way back to the center by the screws which move the bubble tubes, and repeat the operation.

**174. Tangent Scale.** This is a convenient, though not essential, addition to the compass, for the purpose of measuring the slopes of ground, so that the proper allowance in chaining may be made. In the figure of the compass may be seen, on the edge of

the left-hand sight, a small projection of brass with a hole through it. On the edge of the other sight are engraved lines numbered from  $0^\circ$  to  $20^\circ$ , the  $0^\circ$  being of the same height above the compass-plate that the eye-hole is. To use this, set the compass at the bottom of a slope, and at the top set a signal of exactly the height of the eye-hole from the ground. Level the compass very carefully, particularly by the level which lies lengthwise, and, with the eye at the eye-hole, look to the signal and note the number of the division on the farther sight which is cut by the visual ray. That will be the angle of the slope; the distances of the engraved lines from the  $0^\circ$  line being tangents (for the radius equal to the distance between the sights) of the angles corresponding to the numbers of the lines.

**175. Vernier.** The compass-box is connected with the plate which carries it and the sights, so that it can turn around on this plate. This motion is given to it by a slow motion or tangent screw, shown on the left of the compass-box in the figure. The space through which the compass-box is moved is indicated by a vernier. For description of a vernier, and method of reading it, see subject *Verniers* under Transit-Surveying.

**176. Tripod.** The compass, like most surveying instruments, is usually supported on a tripod, consisting of three legs, shod with iron, and so connected at top as to be movable in any direction. There are many forms of these. Lightness and stiffness are the qualities desired. The most usual form is shown in the figures of the transit and the level. Of the two represented in Figs. 142 and 143 the first has the advantage of being very easily and cheaply made; and the second that of being light and yet capable of very firmly resisting horizontal torsion.

FIG. 142.



FIG. 143.



The joints by which the instrument is connected with the tripod are also various. Fig. 144 is the "ball-and-socket joint," most usual in this country. It takes its name from the ball in which terminates the covered spindle which enters a corresponding cavity under the compass-plate and the socket in which this ball turns. It admits of motion in any direction, and can be tightened or loosened by turning the upper half of the hollow piece inclosing

FIG. 144.

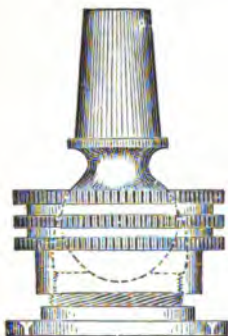


FIG. 145.

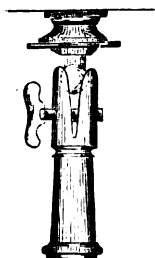
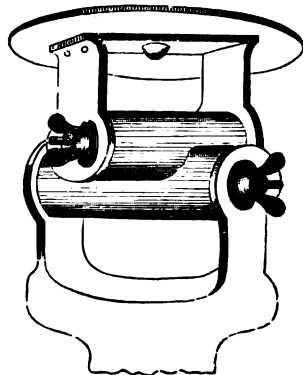


FIG. 146.



it, which is screwed on the lower half. Fig. 145 is called the "shell-joint." In it the two shell-shaped pieces inclosing the ball are tightened by a thumb-screw. Fig. 146 is "Cugnot's joint." It consists of two cylinders placed at right angles to each other, and through the axes of which pass bolts, which turn freely in the cylinder, and can be tightened or loosened by thumb-screws at their ends. The combination of the two motions which this joint permits enables the instrument which it carries to be placed in any desired direction. This joint is much the most stable of the three.

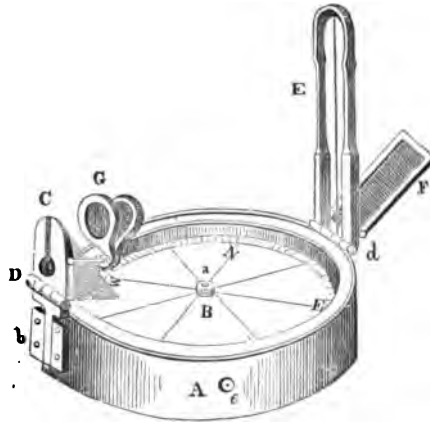
**177. Jacob's Staff.** A single leg, called a "Jacob's staff," has some advantages, as it is lighter to carry in the field, and can be made of any wood on the spot where it is to be used, thus saving the expense of a tripod and the trouble of its transportation. Its upper end is fitted into the lower end of a brass head which has a ball-and-socket joint and axis above. Its lower end should be shod



with iron, and a spike running through it is useful for pressing it into the ground with the foot. Of course, it can not be conveniently used on frozen ground or on pavements. It may, however, be set before or behind the spot at which the angle is to be measured, provided that it is placed very precisely in the line of direction from that station to the one to which a sight is to be taken.

**178. The Prismatic Compass.** The peculiarity of this instrument (often called Schmalcalder's) is that a glass triangular prism is substituted for one of the sights. Such a prism has this peculiar property that at the same time it can be seen through, so that a sight can be taken through it, and that its upper surface reflects like a mirror, so that the numbers of the degrees immediately under it can be read off at the same time that a sight to any object is taken. Another peculiarity necessary for profiting by the last one is that the divided circle is not fixed, but is a card fastened to the needle and moving around with it, as in the mariner's compass. The minute description which follows is condensed from Simms.

FIG. 147.



In the figure, A represents the compass-box and B the card, which, being attached to the magnetic needle, moves as it moves around the agate center *a*, on which it is suspended. The circumference of the card is usually divided to  $\frac{1}{4}$  or  $\frac{1}{2}$  of a degree. C is a prism which the observer looks through. The perpendicular thread of the sight-vane, E, and the divisions on the card appear *together* on looking through the prism, and the division with which the thread coincides when the needle is at rest, is the "bearing" of whatever object the thread may bisect—i. e., is the angle which the line of sight makes with the direction of the needle. The

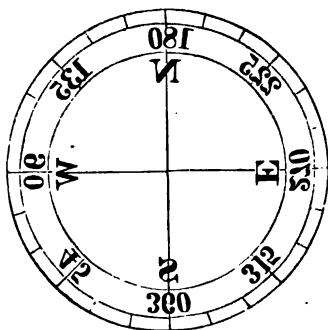
prism is mounted with a hinge-joint, D. The sight-vane has a fine thread stretched along its opening in the direction of its length, which is brought to bisect any object by turning the box around horizontally. F is a mirror made to slide on or off the sight-vane, E; and it may be reversed at pleasure—that is, turned face downward; it can also be inclined at any angle by means of its joint, *d*; and it will remain stationary on any part of the vane by the friction of its slides. Its use is to reflect the image of an object to the eye of an observer when the object is much above or below the horizontal plane. The colored glasses represented at G are intended for observing the sun. At *e* is shown a spring, which, being pressed by the finger at the time of observation and then released, checks the vibrations of the card, and brings it more speedily to rest. A stop is likewise fixed to the other side of the box, by which the needle may be thrown off its center.

The method of using this instrument is very simple: First raise the prism in its socket, *b*, until you obtain a distinct view of the divisions on the card. Then, standing over the point where the angles are to be taken, hold the instrument to the eye, and, looking through the slit, *C*, turn around till the thread in the sight-vane bisects one of the objects whose bearing is required; then, by touching the spring, *e*, bring the needle to rest, and the division on the card which coincides with the thread on the vane will be the bearing of the object from the north or south points of the magnetic meridian. Then turn to any other object and repeat the operation; the difference between the bearing of this object

and that of the former will be the angular distance of the objects in question. Thus, suppose the former bearing to be  $40^{\circ} 30'$ , and the latter  $10^{\circ} 15'$ , both east or both west, from the north or south, the angle will be  $30^{\circ} 15'$ . The divisions are generally numbered  $5^{\circ}$ ,  $10^{\circ}$ ,  $15^{\circ}$ , etc., around the circle to  $360^{\circ}$ .

The figures on the compass-

FIG. 148.



card are reversed or written upside down, as in the figure (in which only every fifteenth degree is marked), because they are again reversed by the prism.

The prismatic compass is generally held in the hand, the bearing being caught, as it were, in passing; but more accurate readings would, of course, be obtained if it rested on a support, such as a stake cut flat on its top.

In the former mode, the needle never comes completely to rest, particularly in the wind. In such cases, observe the extreme divisions between which the needle vibrates, and take their arithmetical mean.

**179. Defects of the Compass.** The compass is deficient in both precision and correctness.\*

The former defect arises from the indefiniteness of its mode of indicating the part of the circle to which it points. The point of the needle has considerable thickness; it can not quite touch the divided circle; and these divisions are made only to whole or half degrees, though a fraction of a division may be estimated or guessed at. The vernier does not much better this, as we shall see when explaining its use. Now, an inaccuracy of one quarter of a degree in an angle—i. e., in the difference of the directions of two lines—causes them to separate from each other  $5\frac{1}{4}$  inches at the end of 100 feet; at the end of 1,000 feet, nearly  $4\frac{1}{2}$  feet; and, at the end of a mile, 23 feet. A difference of only one tenth of a degree, or six minutes, would produce a difference of  $1\frac{1}{2}$  foot at the end of 1,000 feet; and  $9\frac{1}{4}$  feet at the distance of a mile. Such are the differences which may result from the want of *precision* in the indications of the compass.

But a more serious defect is the want of *correctness* in the compass. Its not pointing exactly to the true north does not, indeed, affect the correctness of the angles measured by it. But it does not point in the same or in a parallel direction during even the

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\* The student must not confound these two qualities. To say that the sun appears to rise in the eastern quarter of the heavens and to set in the western is *correct*, but not *precise*. A watch with a second-hand indicates the time of day *precisely*, but not always *correctly*. The statement that two and two make five is *precise*, but is not usually regarded as *correct*.

same day, but changes its direction between sunrise and noon nearly a quarter of a degree, as will be fully explained hereafter. The effect of such a difference we have just seen. This direction may also be greatly altered in a moment, without the knowledge of the surveyor, by a piece of iron being brought near to the compass, or by some other local attraction, as will be noticed in Art. 186. This is the weak point in the compass.

Notwithstanding these defects, the compass is a very valuable instrument, from its simplicity, rapidity, and convenience in use; and, though never precise, and seldom correct, it is generally not *very* wrong.

### THE FIELD-WORK.

**180. Taking Bearings.** The "bearing" of a line is the angle which it makes with the direction of the needle. The bearing and length of a line are named collectively the *Course*.

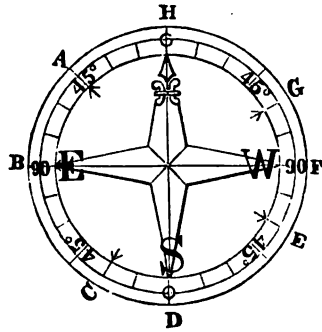
To take the bearing of any line, set the compass exactly over any point of it by a plumb-line suspended from beneath the center of the compass, or, approximately, by dropping a stone. Level the compass by bringing the air-bubbles to the middle of the level tubes. Direct the sights to a rod held truly vertical or "plumb" at another point of the line, the more distant the better. The two ends are usually taken. Sight to the lowest visible point of the rod. When the needle comes to rest, note what division on the circle it points to; taking the one indicated by the north end of the needle, if the north point on the circle is farthest from you, and *vice versa*.

In reading the division to which one end of the needle points, the eye should be placed over the other end, to avoid the error which might result from the "parallax," or apparent change of place of the end read from, when looked at obliquely.

The bearing is read and recorded by noting between what letters the end of the needle comes, and to what number; naming, or writing down, *first*, that letter, N. or S., which is at the  $0^{\circ}$  point nearest to that end of the needle from which you are reading; *second*, the number of degrees to which it points; and, *third*, the letter E. or W. of the  $90^{\circ}$  point which is nearest to the

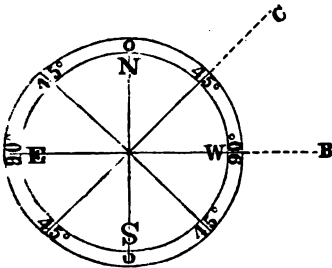
same end of the needle. Thus, in the figure, if when the sights were directed along a line (the north point of the compass being most distant from the observer) the north end of the needle was at the point A, the bearing of the line sighted on would be north  $45^\circ$  east; if the end of the needle was at B, the bearing would be *east*; if at C, S.  $30^\circ$  E.; if at D, *south*; if at E, S.  $60^\circ$  W.; if at F, *west*; if at G, N.  $60^\circ$  W.; if at H, *north*.

FIG. 149.



181. We can now understand why W. is on the right hand of the compass-box and E. on the left. Let the direction from the

FIG. 150.



center of the compass to the point B in the figure be required, and suppose the sights in the first place to be pointing in the direction of the needle, S. N., and the north sight to be ahead. When the sights (and the circle to which they are fastened) have been turned so as to point in the direction of B, the point of the circle marked E. will have come round to the north end of the needle (*since the needle remains immovable*), and the reading will therefore be “*east*,” as it should be. The effect on the reading is the same as if the needle had moved to the left the same distance which the sights have moved to the right, and the left side is therefore properly marked “*east*,” and *vice versa*. So, too, if the bearing of the line to C be desired half-way between north and east—i. e., N.  $45^\circ$  E.; when the sights and the circle have turned  $45^\circ$  to the right, the needle, really standing still, has apparently arrived at the point half-way between N. and E., i. e., N.  $45^\circ$  E.

Some surveyors' compasses are marked the reverse of this, the E. on the right and the W. on the left. These letters must

then be reversed in the mind before the bearing is noted down.

**182. Reading with Vernier.** When the needle does not point precisely to one of the division-marks on the circle, the fractional part of the smallest space is usually estimated by the eye, as has been explained. But this fractional part may be measured by the vernier as follows : Suppose the needle to point between N.  $31^{\circ}$  E. and N.  $31\frac{1}{2}^{\circ}$  E. Turn the tangent-screw which moves the compass-box till the smaller division (in this case  $31^{\circ}$ ) has come round to the needle. The vernier will then indicate through what space the compass-box has moved, and therefore how much must be added to the reading of the needle. Suppose it indicates ten minutes of a degree. Then the bearing is N.  $31^{\circ} 10'$  E. It is, however, so difficult to move the vernier without disturbing the whole instrument, that this is seldom resorted to in practice. The chief use of the vernier is to set the instrument for running lines and making an allowance for the variation of the needle, as will be explained in the proper place. A vernier arc is sometimes attached to one end of the needle and carried around by it.

**183. Practical Hints.** Mark every station or spot at which the compass is set by driving a stake, or digging up a sod, or piling up stones, or otherwise, so that it can be found if any error or other cause makes it necessary to repeat the survey.

Very often, when the line of which the bearing is required is a fence, etc., the compass can not be set upon it. In such cases, set the compass so that its center is a foot or two from the line, and set the flag-staff at precisely the same distance from the line at the other end of it. The bearing of the flag-staff from the compass will be the same as that of the fence, the two lines being parallel. The distances should be measured on the real line. If more convenient, the compass may be set at some point on the line prolonged, or at some intermediate point of the line, "in line" between its extremities.

In setting the compass level, it is more important to have it level crosswise of the sights than in their direction ; since, if it be

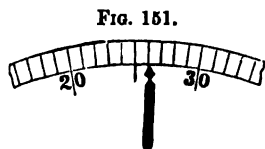
not so, on looking up or down hill through the upper part of one sight and the lower part of the other, the line of sight will not be parallel to the N. and S. or zero line on the compass, and an incorrect bearing will therefore be obtained.

The compass should *not* be leveled by the needle, as some books recommend—i. e., so leveled that the ends of the needle shall be at equal distances below the glass. The needle should be brought so originally by the maker, but, if so adjusted in the morning, it will not be so at noon, owing to the daily variation in the *dip*. If, then, the compass be leveled by it, the lines of sight will generally be more or less oblique, and therefore erroneous. If the needle touches the glass when the compass is leveled, balance it by sliding the coil of wire along it.

The same end of the compass should always go ahead. The north end is preferable. The south end will then be nearest to the observer. Attention to this and to the caution in the next paragraph will prevent any confusion in the bearings.

Always take the readings from the same end of the needle; from the north end, if the north end of the compass goes ahead, and *vice versa*. This is necessary, because the two ends will not always cut opposite degrees. With this precaution, however, the angle of two meeting lines can be obtained correctly from either end, provided the same one is used in taking the bearings of both the lines.

Guard against a very frequent source of error with beginners in reading from the wrong number of the two between which the needle points, such as reading  $34^\circ$  for  $26^\circ$  in a case like that in the figure.



Check the vibrations of the needle by gently raising it off the pivot so as to touch the glass, and letting it down again by the screw on the under side of the box.

The compass should be smartly tapped after the needle has settled, to destroy the effect of any adhesion to the pivot or friction of dust upon it.

All iron, such as the chain, etc., must be kept at a distance

from the compass, or it will attract the needle, and cause it to deviate from its proper direction.

The surveyor is sometimes troubled by the needle refusing to traverse and adhering to the glass of the compass after he has briskly wiped this off with a silk handkerchief, or it has been carried so as to rub against his clothes. The cause is the electricity excited by the friction. It is at once discharged by applying a wet finger to the glass.

A compass should be carried with its face resting against the side of the surveyor, and one of the sights hooked over his arm.

In distant surveys an extra center-pin should be carried (as it is very liable to injury, and its perfection is most essential), and also an extra needle. When two such are carried they should be placed so that the north pole of one rests against the south pole of the other.

**184.** When the magnetism of the needle is lessened or destroyed by time, it may be renewed as follows: Obtain two bar magnets. Provide a board with a hole to admit of the axis, so that its collar may fit fairly, and that the needle may rest flat on it without bearing at the center. Place the board before you with the north end of the needle to your right. Take a magnet in each hand, the left holding the north end of the bar, or that which has the mark across, downward, and the right holding the same mark upward. Bring the bars over the axis, about a foot above it, without approaching each other within two inches; bring them down vertically on the needle (the marks as directed) about an inch on each side of its axis; slide them outward to its ends with slight pressure; raise them up; bring them to their former position, and repeat this a number of times.

**185. Back-Sights.** To test the accuracy of the bearing of a line taken at one end of it, set up the compass at the other end or point sighted to, and look back to a rod held at the first station or point where the compass had been placed originally. The reading of the needle should now be the same as before.

If the position of the sights had been reversed, the reading



would be the *Reverse Bearing*; a former bearing of N.  $30^{\circ}$  E. would then be S.  $30^{\circ}$  W., and so on.

**186. Local Attraction.** If the back-sight does not agree with the first or forward sight, this latter must be taken over again. If the same difference is again found, this shows that there is *local attraction* at one of the stations—i. e., some influence, such as a mass of iron-ore, ferruginous rocks, etc., under the surface, which attracts the needle, and makes it deviate from its usual direction. Any high object, such as a house, a tree, etc., has been found to produce a similar effect.

To discover at which station the attraction exists, set the compass at several intermediate points in the line which joins the two stations, and at points in the line prolonged, and take the bearing of the line at each of these points. The agreement of several of these bearings, taken at distant points, will prove their correctness. Otherwise, set the compass at a third station, sight to each of the two doubtful ones, and then from them back to this third station. This will show which is correct.

When the difference occurs in a series of lines, such as around a field or along a road, proceed thus: Let C be the station at which the back-sight to B differs from the fore-sight from B to C. Since the back-sight from B to A is supposed to have agreed with the fore-sight from A to B, the local attrac-

FIG. 152.

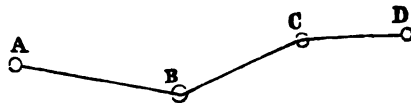
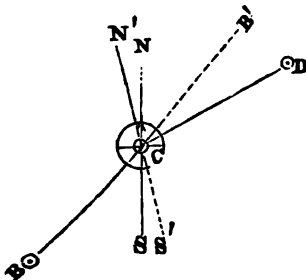


FIG. 153.



tion must be at C, and the forward bearing must be corrected by the difference just found between the fore-and back-sights, adding or subtracting it, according to circumstances. An easy method is to draw a figure for the case, as in Fig. 153. In it, suppose the true bearing of BC, as given by a fore-sight from B to C, to be N.  $40^{\circ}$  E., but that there is local attraction

at C, so that the needle is drawn aside  $10^\circ$ , and points in the direction  $S'N'$  instead of  $SN$ . The back-sight from C to B will then give a bearing of  $N. 50^\circ E.$ ; a difference or correction for the next fore-sight of  $10^\circ$ . If the next fore-sight, from C to D, be  $N. 70^\circ E.$ , this  $10^\circ$  must be subtracted from it, making the true fore-sight  $N. 60^\circ E.$

A general rule may also be given. *When the back-sight is greater than the fore-sight*, as in this case, subtract the difference from the next fore-sight, if that course and the preceding one have both their letters the same (as in this case, both being  $N.$  and  $E.$ ), or both their letters different; or add the difference if either the first or last letters of the two courses are different. *When the back-sight is less than the fore-sight*, add the difference in the case in which it has just been directed to subtract it, and subtract it where it was before directed to add it.

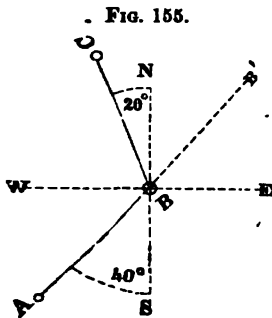
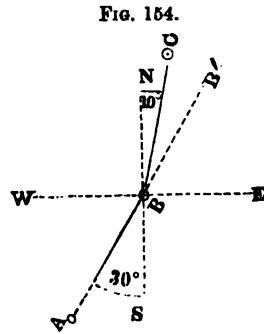
**187. Angles of Deflection.** When the compass indicates much local attraction, the difference between the directions of two meeting lines (or the "*angle of deflection*" of one from the other) can still be correctly measured by taking the difference of the bearings of the two lines, as observed at the same point. For the error caused by the local attraction, whatever it may be, affects both bearings equally, inasmuch as a "*bearing*" is the angle which a line makes with the direction of the needle, and that here remains fixed in some one direction, no matter what, during the taking of the two bearings. Thus, in Fig. 153, let the true bearing of  $BC$ —i. e., the angle which it makes with the line  $SN$ —be, as before,  $N. 40^\circ E.$ , and that of  $CD$ ,  $N. 60^\circ E.$  The true "*angle of deflection*" of these lines, or the angle  $B'CD$ , is therefore  $20^\circ$ . Now, if local attraction at C causes the needle to point in the direction of  $S'N'$ ,  $10^\circ$  to the left of its proper direction,  $BC$  will bear  $N. 50^\circ E.$ , and  $CD$   $N. 70^\circ E.$ , and the difference of these bearings—i. e., the angle of deflection—will be the same as before.

**188. Angles between Courses.** To determine the angle of deflection of two courses meeting at any point, the following simple rules, the reasons of which will appear from the accompanying figures, are sufficient:

**Case 1.** When the first letters of the bearing are alike (i. e., both N. or both S.), and the last letters also alike (i. e., both E. or both W.), take the difference of the bearings. *Example:* If A B bears N.  $30^{\circ}$  E., and B C bears N.  $10^{\circ}$  E., the angle of deflection C B B' is  $20^{\circ}$ .

**Case 2.** When the first letters are alike and the last letters different, take the sum of the bearings. *Ex.:* If A B bears N.  $40^{\circ}$  E. and B C bears N.  $20^{\circ}$  W., the angle C B B' is  $60^{\circ}$ .

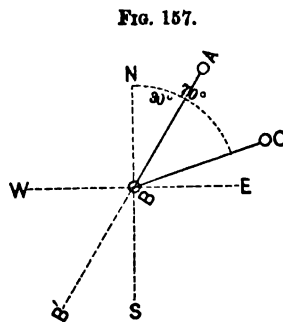
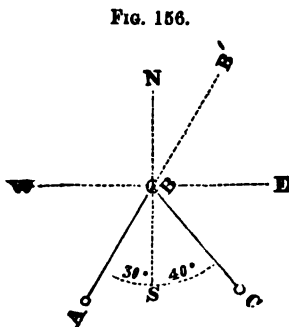
**Case 3.** When the first letters are different and the last letters alike, sub-



tract the sum of the bearings from  $180^{\circ}$ . *Ex.:* If A B bears N.  $30^{\circ}$  E. and B C bears S.  $40^{\circ}$  E., the angle C B B' is  $110^{\circ}$ .

**Case 4.** When both the first and last letters are different, subtract the difference of the bearings from  $180^{\circ}$ . *Ex.:* If A B bears S.  $30^{\circ}$  W. and B C bears N.  $70^{\circ}$  E., the angle C B B' is  $140^{\circ}$ .

*If the angles included between the courses are desired, they will be at once found by reversing one bearing and then applying the above rules; or by subtracting the results obtained as above from  $180^{\circ}$ ; or an analogous set of rules could be formed for them.*



**189. To change Bearings.** It is convenient in certain calculations to suppose one of the lines of a survey to change its direction so as to become due north and south; that is, to become a new meridian line. It is, then, necessary to determine what the bearings of the other lines will be, supposing them to change with it. The subject may be made plain by supposing the survey to be platted in the usual way, with the north uppermost, and the plat to be then turned around till the line to be changed is in the desired direction. The effect of this on the other lines will be readily seen. A *general rule* can also be formed :

Take the *difference* between the original bearing of the side which becomes a meridian, and each of those bearings which have both their letters the same as it, or both different from it. The changed bearings of these lines retain the same letters as before, if they were originally greater than the original bearing of the new meridian line; but, if they were less, they are thrown on the other side of the N. and S. line, and their last letters are changed, E. being put for W., and W. for E.

Take the *sum* of the original bearing of the new meridian line, and each of those bearings which have one letter the same as one letter of the former bearing and one different. If this sum exceeds  $90^\circ$ , this shows that the line is thrown on the other side of the east or west point, and the difference between this sum and  $180^\circ$  will be the new bearing, and the first letter will be changed, N. being put for S. and S. for N.

*Example:* Let the bearings of the sides of a field be as follows : N.  $32^\circ$  E. ; N.  $80^\circ$  E. ; S.  $48^\circ$  E. ; S.  $18^\circ$  W. ; N.  $73\frac{1}{2}^\circ$  W. ; North. Suppose the first side to become due north; the changed bearings will then be as follows : North ; N.  $48^\circ$  E. ; S.  $80^\circ$  E. ; S.  $14^\circ$  E. ; S.  $74\frac{1}{2}^\circ$  W. ; N.  $32^\circ$  W.

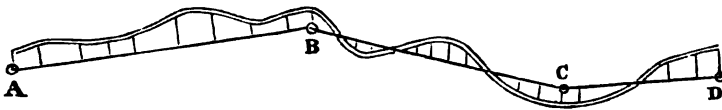
To apply the rule to the "North" course, as above, it must be called N.  $0^\circ$  W. ; and then, by the rule,  $32^\circ$  must be added to it.

The true bearings can, of course, be obtained from the changed bearings by reversing the operation, taking the sum instead of the difference, and *vice versa*.

**190. Line-Surveying.** This name may be given to surveys of lines, such as the windings of a brook, the curves of a road, etc., by way of distinction from *Farm-Surveying*, in which the lines surveyed inclose a space.

To survey a *brook*, or any similar line, set the compass at or near one end of it, and take the bearing of an imaginary or visual

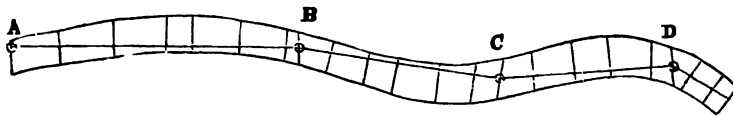
FIG. 158.



line running in the general average direction of the brook, such as A B in the figure. Measure this line, taking offsets to the various bends of the brook, as explained in Art. 97. Then set the compass at B, and take a back-sight to A, and, if they agree, take a fore-sight to C, and proceed as before, noting particularly the points where the line crosses the brook.

To survey a *road*, take the bearings and lengths of the lines

FIG. 159.



which can be most conveniently measured in the road, and measure offsets on each side to the outside of the road.

When the line of a new road is surveyed, the bearings and lengths of the various portions of its intended center-line should be measured, and the distance which it runs through each man's land should be noted. Stones should be set in the ground at recorded distances from each angle of the line, or in each line prolonged a known distance, so as not to be disturbed in making the road.

In surveying a wide river, one bank may be surveyed by the method just given, and points on the opposite banks, as trees, etc., may be fixed by the method of intersections founded on the fourth method of determining the position of a point.

**191. Checks by Intersecting Bearings.** At each station at which the compass is set take bearings to some remarkable object, such as a church-steeple, a distant house, a high tree, etc. At least three bearings should be taken to each object to make it of any use, since two are necessary to determine it (by our fourth method), and, till thus determined, it can be no check. When the line is platted, by the methods to be explained hereafter, plat also the lines given by these bearings. If those taken to the same object from three different stations intersect in the same point, this proves that there has been no mistake in the survey or platting of those stations.

If any bearing does not intersect a point fixed by previous bearings, it shows that there has been an error, either between the last station and one of those which fixed the point, or in the last bearing to the point. To discover which it was, plat the following line of the survey, and, at its extremity, set off the bearing from it to the point, and, if the line thus platted passes through the point, it proves that there was no error in the line, but only in the bearing to the point. If otherwise, the error was somewhere in the line between the stations from which the bearings to that point were taken.

**192. Keeping the Field-Notes.** The simplest and easiest method for a beginner is to make a rough sketch of the survey by eye, and write down on the lines their bearings and lengths.

An improvement on this is to actually lay down the precise bearings and lengths of the lines in the field-book in the manner to be explained in the section on Platting, Art. 209.

**193.** A *second* method is to draw a straight line up the page of the field-book, and to write on it the bearings and lengths of the lines. The only advantage of this method is that the line will not run off the side of the page, as it is apt to do in the preceding method.

**194.** A *third* method is to represent the line surveyed by a double column, as in Art. 84, which should be now referred to. The bearings are written obliquely up the columns. At the end of

each course its length is written in the column, and a line drawn across it. Dotted lines are drawn across the column at any intermediate measurement. Offsets are noted as explained in Art. 97.

The intersection bearings, described in Art. 191, should be entered in the field-book *before* the bearings of the line, in order to avoid mistakes of platting in setting off the measured distances on the wrong line.

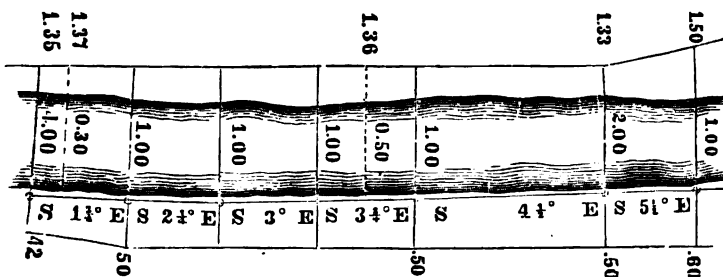
**195.** A *fourth* method is to write the stations, bearings, and distances in three columns. This is compact, and has the advantage, when applied to farm-surveying, of presenting a form suitable for the subsequent calculations of content, but does not give facilities for noting offsets.

Examples of these four methods are given in Art. 199, which contains the field-notes of the lines bounding a field.

**196. New York Canal-Maps.** The following is a description of the original maps of the survey of the line of the New York Erie Canal, as published by the Canal Commissioners. The figure represents a portion of such a map, but, necessarily, with all its lines black, red and blue lines being used on the real map :

"The RED LINE described along the inner edge of the towing-path is the *base-line*, upon which all the measurements in the di-

FIG. 160.



rection of the length of the canal were made. The *bearings* refer to the magnetic meridian at the time of the survey. The *lengths* of the several portions are inserted at the *end* of each in chains and links. The *offsets* at each station are represented by red lines drawn across the canal in such a direction as to bisect the angles

formed by the two contiguous portions of the red or base line upon the towing-path. The intermediate offsets are set off at right angles to the base-line, and the distances on both are given from it in links. The *intermediate offsets* are represented by *red dotted lines*, and the distances to them upon the base-line are reckoned, in each case, from the last preceding station. The same is likewise done with the other distances upon the base-line; those to the *bridges* being taken to the lines joining the nearest angles or corner posts of their abutments; those to the *locks* extending to the lines passing through the centers of the two nearest quoin-posts; and those to the *aqueducts* to the faces of their abutments. The space inclosed by the BLUE LINES represents the portion embraced within the limits of the survey as belonging to the State; and the names of the adjoining proprietors are given as they stood at the time of executing the survey. The distances are projected upon a *scale* of two chains to the inch."

**197. Farm-Surveying.** A farm or field or other space included within known lines is usually surveyed by the compass thus: Begin by walking around the boundary-lines and setting stakes at all the corners, which the flag-man should specially note, so that he may readily find them again. Then set the compass at any corner, and send the flag-man to the next corner. Take the bearing of the bounding-line running from corner to corner, which is usually a fence. Measure its length, taking offsets if necessary. Note where any other fence, or road, or other line crosses or meets it, and take their bearings. Take the compass to the end of this first bounding-line; sight back, and, if the back-sight agrees, take the bearing and distance of the next bounding-line; and so proceed till you have got back to the point of starting.

**198.** Where speed is more important than accuracy in a survey, whether of a line or a farm, the compass need be set only at every other station, taking a forward sight from the first station to the second; then, setting the compass at the third station, taking a back-sight to the second station (but with the north point of the compass always ahead), and a fore-sight to the fourth; then going to the fifth, and so on. This is, however, not to be recommended.



199. Field-Notes.

The field-notes of a farm-survey may be kept by any of the methods which have been described with reference to a line-survey. Below are given the field-notes of the same field recorded by each of the methods.

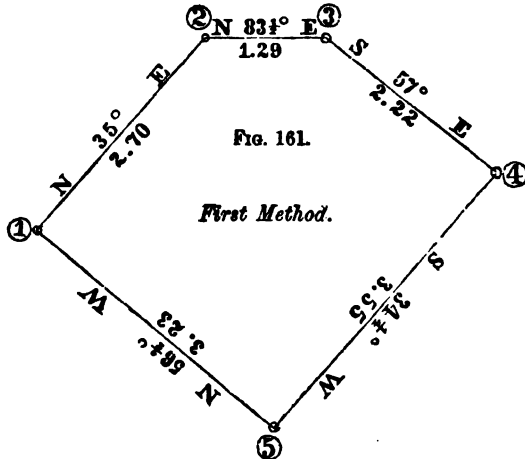


FIG. 161.

First Method.

Second Method.

Third Method.\*

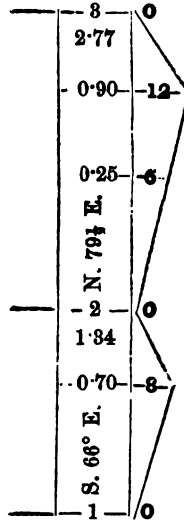
Fourth Method.

N. 35° E. 2.70 (1)  
 N. 83 1/4° E. 1.29 (2)  
 S. 57° E. 2.22 (3)  
 S. 84 1/4° W. 3.55 (4)  
 N. 56 1/4° W. 3.23 (5)

(1) N. 35° E. 2.70  
 (2) N. 83 1/4° E. 1.29  
 (3) S. 57° E. 2.22  
 (4) S. 84 1/4° W. 3.55  
 (5) N. 56 1/4° W. 3.23

| STATIONS. | BEARINGS.     | DISTANCES. |
|-----------|---------------|------------|
| 1         | N. 35° E.     | 2.70       |
| 2         | N. 83 1/4° E. | 1.29       |
| 3         | S. 57° E.     | 2.22       |
| 4         | S. 84 1/4° W. | 3.55       |
| 5         | N. 56 1/4° W. | 3.23       |

FIG. 162.



\* In the "third method" the bearings should be written obliquely upward, as directed in Art. 194, but are not so printed here, from typographical difficulties.

**200.** The field-notes of a field in which offsets occur may be most easily recorded by the third method, as in Fig. 162.

When the field-notes are recorded by the fourth method, the offsets may be kept in a separate table, in which the first column will contain the stations from which the measurements are made, the second column the distances at which they occur, the third column the lengths of the offsets, and the fourth column the side of the line, "right" or "left," on which they lie.

For calculation, four more columns may be added to the table, containing the intervals between the offsets, the sums of the adjoining pairs, and the products of the numbers in the two preceding columns, separated into right and left, one being additive to the field, and the other subtractive.

**201. Tests of Accuracy.** 1. The check of intersections described in Art. 191 may be employed to great advantage when some conspicuous object near the center of the farm can be seen from most of its corners.

2. When the survey is platted, if the last course meets the starting-point, it proves the work, and the survey is then said to "close."

3. Diagonal lines running from corner to corner of the farm, like the "proof-lines" in chain-surveying, may be measured and their bearings taken. When these are laid down on the plat, their meeting the points to which they had been measured proves the work.

4. The only certain and precise test is, however, that by "latitudes and departures."

**202. Method of Radiation.** *A field may be surveyed from one station, either within it or without it,* by taking the bearings and the distances from that point to each of the corners of the field. These corners are then "determined" by the third method, Art. 5. This modification of that method is called the *Method of Radiation*. All our preceding surveys with the compass have been by the *Method of Progression*.

The compass may be set at one corner of the field, or at a point

in one of its sides, and the same method of radiation employed.

This method is seldom used, however, since, unlike the method of progression, its operations are not checks upon each other.

**203. Method of Intersection.** A field may also be surveyed by measuring a *base-line*, either within it or without it, setting the compass at each end of the base-line, and taking from each end the bearings of each corner of the field, which will then be fixed and determined by the fourth method, Art. 6. This mode of surveying is the *Method of Intersections*, noticed in Art. 166.

**204. Running out Old Lines.** The original surveys of lands in the older States of the American Union were exceedingly deficient in precision. This arose from two principal causes: the small value of land at the period of these surveys, and the want of skill in the surveyors. The effect at the present day is frequent dissatisfaction and litigation. Lots sometimes contain more acres than they were sold for, and sometimes less. Lines which are straight in the deed and on the map are found to be crooked on the ground. The recorded surveys of two adjoining farms often make one overlap the other, or leave a gore between them. The most difficult and delicate duty of the land-surveyor is to run out these old boundary-lines. In such cases, his first business is to find monuments, stones, marked trees, stumps, or any other old "corners" or landmarks. These are his starting-points. The owners whose lands join at these corners should agree on them. Old fences must generally be accepted by right of possession, though such questions belong rather to the lawyer than to the surveyor.\* His business is to mark out on the ground the lines given in the deed. When the bounds are given by compass-bearings, the surveyor must be reminded that these bearings are very far from being the same now as originally, having been changing every year. The method of

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\* "In the description of land conveyed, the rule is that known and fixed monuments control courses and distances. So the certainty of metes and bounds will include and pass all the lands within them, though they vary from the given quantity expressed in the deed. In New York, to remove, deface, or alter landmarks maliciously is an indictable offense."—*Kent's Commentaries*, IV, 515.

determining this important change, and of making the proper allowance, will be found under "Declination of the Magnetic Needle."

### PLATTING THE SURVEY.

**205.** The platting of a survey made with the compass consists in drawing on paper the lines and the angles which have been measured on the ground. The angles are laid off and the lines are drawn "to scale," as has been explained in Chapter I.

**206. Platting Bearings.** Since "bearings" taken with the compass are the angles which the various lines make with the magnetic meridian, or the direction of the compass-needle, which, as we have seen, remains always (approximately) parallel to itself, it is necessary to draw these meridians through each station before laying off the angles of the bearings.

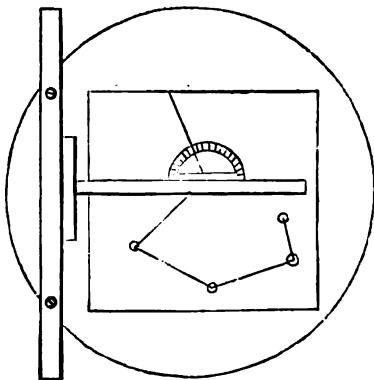
The T-square is the most convenient instrument for this purpose. The paper on which the plat is to be made is fastened on the board so that the intended direction of the north and south line may be parallel to one of the sides of the board. The inner side of the stock of the T-square being pressed against one of the other sides of the board and slid along, the edge of the long blade of the square will always be parallel to itself and to the first-named side of the board, and will thus represent the meridian passing through any station.

If a straight-edged drawing-board or table can not be procured, nail down on a table of any shape a straight-edged ruler, and slide along against it the outside of the stock of a T-square, one side of the stock being flush with the blade.

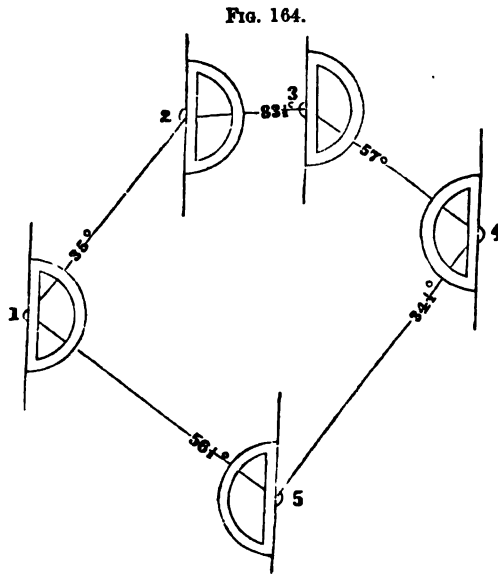
A parallel ruler may also be used, one part of it being screwed down to the board in the proper position.

If none of these means are at hand, approximately parallel meridians may be drawn by the edges of a common ruler at distances apart equal to its width, and the diameter of the protractor made parallel to them by measuring equal distances between it and them.

FIG. 163.



207. To plat a survey with these instruments, mark with a fine point inclosed in a circle a convenient spot in the paper to represent the first station, 1 in the figure. Its place must be so chosen that the plat may not "run off" the paper. With the T-square draw a meridian through it. The top of the paper is usually, though not necessarily, called north. With the protractor lay off the angle of the first bearing. Set off the length of the first line to the desired scale from 1 to 2. The line 1 --- 2 represents the first course.



Through 2 draw another meridian, lay off the angle of the second course, and set off the length of this course from 2 to 3.

Proceed in like manner for each course. When the last course is platted, it should end precisely at the starting-point, as the survey did, if it were a closed survey, as of a field. If the plat does not "close" or "come together," it shows some error or inaccuracy either in the original survey, if that have not been "tested" by latitudes and departures, or in the work of platting. The plat here given is the same as that of Fig. 161.

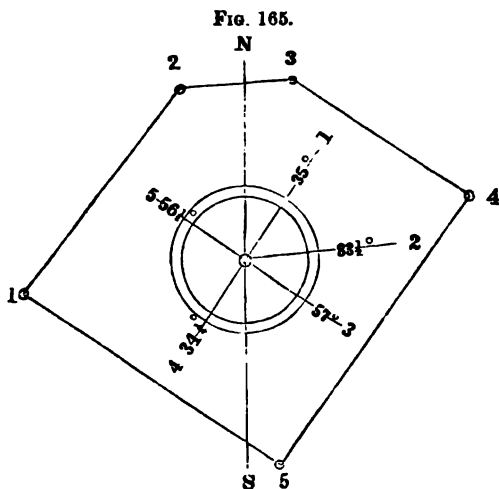
This manner of laying down the directions of lines by the angles which they make with a meridian line has a great advantage, in both accuracy and rapidity, over the method of platting lines by the angles which each makes with the line which comes before it. In the latter method, any error in the direction of one line makes all that follow it also wrong in their directions. In the former, the *direction* of each line is independent of the preceding line, though its *position* would be changed by a previous error.

Instead of drawing a meridian through each station, sometimes only one

is drawn, near the middle of the sheet, and all the bearings of the survey are laid off from some one point of it, as shown in the figure, and numbered to correspond with the stations from which these bearings were taken. The circular protractor is convenient for this. They are then transferred to the places where they are wanted by a triangle or other parallel ruler. Fig. 165 represents the same field platted by this method.

A semicircular protractor is sometimes attached to the stock end of the T-square so that its blade may be set at any desired angle with the meridian, and any bearing be thus protracted without drawing a meridian. It has some inconveniences.

The compass itself may be used to plat bearings. For this purpose



it must be attached to a square board so that the N and S line of the compass-box may be parallel to two opposite edges of the board. This is placed on the paper, and the box is turned till the needle points as it did when the first bearing was taken. Then a line drawn by one edge of the board will be in a

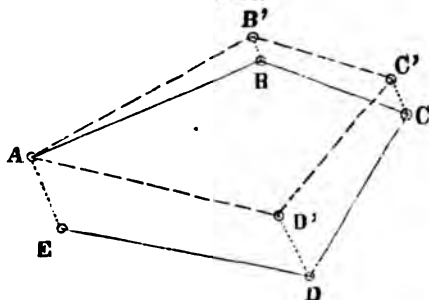
proper direction. Mark off its length, and plat the next and the succeeding bearings in the same manner.

208. When the plat of a survey does not "close," it may be corrected as follows: Let A B C D E be the boundary-lines platted according to the given bearings and distances, and suppose that the last course comes to E instead of ending at A, as it should. Suppose also that there is no reason to suspect any single great error, and that no one of the lines was measured over very rough ground, or was specially uncertain in its direction when observed. The inaccuracy must then be distributed among all the lines *in proportion to their length*. Each point in the figure, B, C, D, E, must

be moved in a direction parallel to  $EA$  by a certain distance which is obtained thus: Multiply the distance  $EA$  by the distance  $AB$ , and divide by the sum of all the courses. The quotient will be the distance  $BB'$ . To get  $CC'$ , multiply  $EA$  by  $AB + BC$ , and divide the product by the same sum of all the courses. To get  $DD'$ , multiply  $EA$  by  $AB + BC + CD$ , and divide as before. So for any course, multiply by the sum of the lengths of that course and of all those preceding it, and divide as before. Join the points thus obtained, and the closed polygon  $AB'C'D'A$  will thus be formed, and will be the most *probable* plat of the given survey.\*

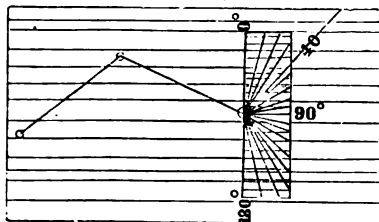
The method of latitudes and departures, to be explained hereafter, is, however, the best for effecting this object.

FIG. 166.



**209. Field Platting.** It is sometimes desirable to plat the courses of a

FIG. 167.

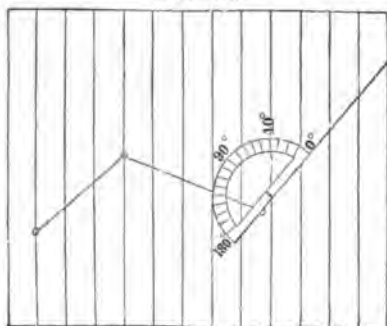


survey in the field as soon as they are taken, as was mentioned in Art. 192 under the head of "Keeping the Field-Notes." One method of doing this is to have the paper of the field-book ruled with parallel lines at *unequal* distances apart, and to use a rectangular protractor (which may be made of Bristol-board or other stout drawing-paper) with lines ruled across it at equal distances of some fraction of an inch. A bearing having been taken and noted, the protractor is laid on the paper and its center placed at the station where the bearing is to be laid off. It is then turned till one of its cross-lines coincides with some one of the lines on the paper, which represent east and west lines. The long side of the protractor will then be on a meridian, and the proper angle ( $40^\circ$  in the figure) can be at once marked off. The length of the course can also be set off by the equal spaces between the cross-lines, letting each space represent any convenient number of links.

ances of some fraction of an inch. A bearing having been taken and noted, the protractor is laid on the paper and its center placed at the station where the bearing is to be laid off. It is then turned till one of its cross-lines coincides with some one of the lines on the paper, which represent east and west lines. The long side of the protractor will then be on a meridian, and the proper angle ( $40^\circ$  in the figure) can be at once marked off. The length of the course can also be set off by the equal spaces between the cross-lines, letting each space represent any convenient number of links.

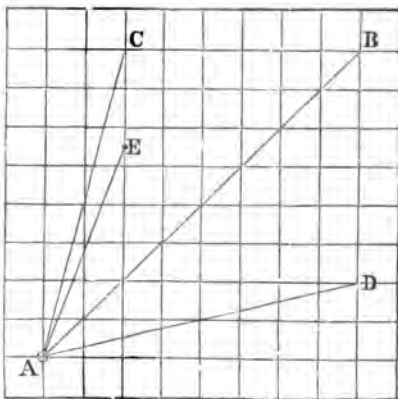
\* This was demonstrated by Dr. Bowditch in No. 4 of "The Analyst."

210. A common rectangular protractor without any cross-lines, or a semicircular one, can also be used for the same purpose. The parallel lines on the paper (which, in this method, may be equidistant, as in common ruled writing-paper) will now represent meridians. Place the center of the protractor on the meridian nearest to the station at which the angle is to be laid off, and turn it till the given number of degrees is cut by the meridian. Slide the protractor up or down the meridian (which must continue to pass through the center and the proper degree) till its edge passes



through the station, and then draw by this edge a line, which will have the bearing required.

211. *Paper ruled into squares* (as are sometimes the right-hand pages of surveyors' field-books) may be used for platting bearings in the field. The lines running up the page may be called north and south lines, and those running across the page will then be east and west lines. Any course of the survey will be the hypotenuse of a right-angled triangle, and the ratio of its other two sides will determine the angle. Thus, if the ratio of the two sides of the right-angled triangle, of which the line *AB* in the figure is the hypotenuse, is 1, that line makes an angle of  $45^\circ$  with the meridian. If the ratio of the long to the short side of the right-angled triangle, of which the line *AC* is the hypotenuse, is 4 to 1, the line *AC* makes an angle of  $14^\circ$  with the meridian. The line *AD*, the hypotenuse of an equal triangle which has its long side lying east and west, makes likewise an angle of  $14^\circ$  with that side, and therefore makes an angle of  $76^\circ$  with the meridian.

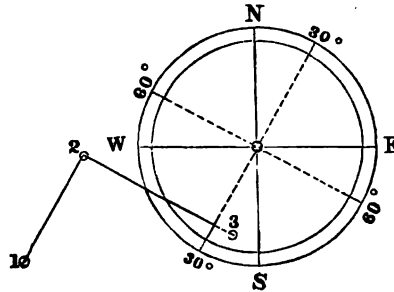


212. **With a Paper Protractor.** Engraved paper protractors may be obtained from the instrument-makers, and are very convenient. A circle of large size, divided into degrees and quarters, is engraved on copper, and impressions from it are taken on drawing-paper. The divisions are not num-



bered. Draw a straight line to represent a meridian through the center of the circle in any convenient direction. Number the degrees from  $0^{\circ}$  to  $90^{\circ}$  each way from the ends of this meridian, as on the compass-plate. The protractor is now ready for use. Choose a convenient point for the first station. Suppose the first bearing to be N.  $30^{\circ}$  E. The line passing through the center of the circle and through the opposite points N.  $30^{\circ}$  E. and S.  $30^{\circ}$  W. has the bearing required. But it does not pass through the station 1. Transfer it thither by drawing through station 1 a line parallel to it, which will be the course required, its proper length being set off on it from 1 to 2. Now, suppose the bearing from 2 to be S.  $60^{\circ}$  E. Draw through 2 a line parallel to the line passing through the center of the circle and through the opposite points S.  $60^{\circ}$  E. and N.  $60^{\circ}$  W., and it will be the line desired. On it set off the proper length from 2 to 3, and so proceed.

FIG. 170.



When the plat is completed, the engraved sheet is laid on a clean one and the stations "pricked through," and the points thus obtained on the clean sheet are connected by straight lines. The penciled plat is then rubbed off from the engraved sheet, which can be used for a great number of plats.

If the central circle be cut out, the plat, if not too large, can be made directly on the paper where it is to remain.

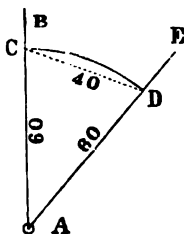
The surveyor can make such a paper protractor for himself with great ease by means of the *Table of Chords* at the end of this volume, the use of which is explained in Art. 215. The engraved ones may have shrunk after being printed.

Such a circle is sometimes drawn on the map itself. This will be particularly convenient if the bearings of any lines on the map not taken on the ground are likely to be required. If the map be very long, more than one may be needed.

**213. Drawing-Board Protractor.** Such a divided circle as has just been described, or a circular protractor, may be placed on a drawing-board near its center, and so that its  $0^{\circ}$  and  $90^{\circ}$  lines are parallel to the sides of the drawing-board. Lines are then to be drawn through the center and opposite divisions by a ruler long enough to reach the edges of the drawing-board on which they are to be cut in and numbered. The drawing-board thus becomes, in fact, a double rectangular protractor. A strip of white paper may have previously been pasted on the edges, or a narrow strip of white wood inlaid. When this is to be used for platting, a sheet of paper is put on the board as usual, and lines are drawn by a ruler laid across the  $0^{\circ}$  points and the  $90^{\circ}$  points, and the center of the circle is at once found, and should be marked  $\odot$ . The bearings are then platted as in the last method.

**214. With a Scale of Chords.** On the plane scale contained in cases of mathematical drawing instruments will be found a series of divisions numbered from 0 to 90, and marked CH or C. This is a scale of chords, and gives the lengths of the chords of any arc for a radius equal in length to the chord of 60° on the scale. To lay off an angle with this scale, as, for example, to draw a line making at A an angle of 40° with A B, take, in the dividers, the distances from 0 to 60 on the scale of chords; with this for radius and A for center, describe an indefinite arc CD. Take the distance from 0 to 40 on the same scale, and set it off on the arc as a chord from C to some point D. Join A D and prolong it. B A E is the angle required.

FIG. 171.



The sector, Fig. 29, supplies a modification of this method sometimes more convenient. On each of its legs is a scale marked C or CH. Open it at pleasure; extend the compass from 60 to 60, one on each leg, and with this radius describe an arc. Then extend the compasses from 40 to 40, and the distance will be the chord of 40° to that radius. It can be set off as above.

The smallness of the scale renders the method with a scale of chords practically deficient in exactness, but it serves to illustrate the next and *best* method.

**215. With a Table of Chords.** At the end of this volume will be found a table of the lengths of the chords of arcs for every degree and minute of the quadrant calculated for a radius equal to 1.

To use it, take in the compasses one inch, one foot, or any other convenient distance (the longer the better), divided into tenths and hundredths by a diagonal scale or otherwise. With this as radius describe an arc as in the last case. Find in the table of chords the length of the chord of the desired angle. Take it from the scale just used to the nearest decimal part which the scale will give. Set it off as a chord, as in the last figure, and join the point thus obtained to the starting-point. This gives the angle desired.

The superiority of this method to that which employs a protractor is due to the greater precision with which a straight line can be divided than can a circle.

A slight modification of this method is to take in the compasses ten equal parts of any convenient length, inches, half inches, quarter inches, or any other at hand, and with this radius describe an arc as before, and set off a chord ten times as great as the one found in the table—i. e., imagine the decimal-point moved one place to the right.

If the radius be 100 or 1,000 equal parts, imagine the decimal-point moved two or three places to the right.

Whatever radius may be taken or given, the product of that radius into a chord of the table will give the chord for that radius.

This gives an easy and exact method of getting a right angle by describing an arc with a radius of 1, and setting off a chord equal to 1.4142.

If the angle to be constructed is more than  $90^\circ$ , construct on the other side of the given point upon the given line prolonged an angle equal to what the given angle wants of  $180^\circ$ —i. e., its *supplement*, in the language of trigonometry.

This same table gives the means of measuring any angle. With the angular point for a center, and 1 or 10 for a radius, describe an arc. Measure the length of the chord of the arc between the legs of the angle, find this length in the table, and the angle corresponding to it is the one desired.

This table will also serve to find the *natural sine* or *cosine* of any angle. Multiply the given angle by two; find in the table the chord of this double angle; and half of this chord will be the natural sine required. For the chord of any angle is equal to twice the sine of half the angle. To find the *cosine*, proceed as above, with the angle which, added to the given angle, would make  $90^\circ$ .

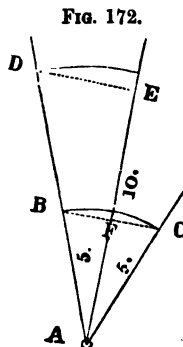
Another use of this table is to inscribe regular polygons in a circle by setting off the chords of the arcs which their sides subtend.

Still another use is to divide an arc or angle into any number of equal parts by setting off the fractional arc or angle.

**216. With a Table of Natural Sines.** In the absence of a table of chords, heretofore rare, a table of natural sines, which can be found anywhere, may be used as a less convenient substitute. Since the chord of any angle equals twice the sine of half the angle, divide the given angle by two; find in the table the natural sine of this half angle; double it, and the product is the chord of the whole angle. This can then be used precisely as was the chord in the preceding article.

An ingenious modification of this method has been much used. Describe an arc from the given point as center, as in the last two articles, but with a radius of five equal parts. Take from a table the length of the natural sine of half the given angle to a radius of ten. Set off this length as a chord on the arc just described, and join the point thus obtained to the given point.

The reason of this is apparent from the figure. DE is the sine of half the angle BAC to a radius of ten equal parts, and BC is the chord directed to be set off to a radius of five equal parts. BO is equal to DE, for  $BC = 2 \cdot BF$  by trigonometry, and  $DE = 2 \cdot BF$  by similar triangles; hence  $BO = DE$ .



**217. By Latitudes and Departures.** When the latitudes and departures of a survey have been obtained and corrected, either to test its accuracy or to obtain its content, they afford the easiest and best means of platting it. The description of this method will be given in Art. 246.

**COPYING PLATS.**

**218.** The plat of a survey necessarily has many lines of construction drawn upon it which are not needed in the finished map. These lines and the marks of instruments so disfigure the paper that a fair copy of the plat is usually made before the map is finished. The various methods of copying plats, etc., whether on the same scale, or reduced, or enlarged, will therefore now be described.

**219. Stretching the Paper.** If the map is to be colored, the paper must first be wetted and stretched, or the application of the wet colors will cause its surface to swell or blister and become uneven. Therefore, with a soft sponge and clean water, wet the back of the paper, working from the center outward in all directions. The "water-mark" reads correctly only when looked at from the front side, which it thus distinguishes. When the paper is thoroughly wet and thus greatly expanded, glue its edges to the drawing-board for half an inch in width, turning them up against a ruler, passing the glue along them, and then turning them down and pressing them with the ruler. Some prefer gluing down opposite edges in succession, and others adjoining edges. The paper must be moderately stretched smooth during the process. Hot glue is best. Paste or gum may be used, if the paper be kept wet by a damp cloth, so that the edges may dry first. "Mouth-glue" may be used by rubbing it (moistened in the mouth or in boiling water) along the turned-up edges, and then rubbing them dry by an ivory folder, a piece of dry paper being interposed. As this is a slower process, the middle of each side should first be fastened down, then the four angles, and lastly the intermediate portions. When the paper becomes dry, the creases and puckerings will have disappeared, and it will be as smooth and tight as a drum-head.

**220. Copying by Tracing.** Fix a large pane of clear glass in a frame so that it can be supported at any angle before a window, or, at night, in front of a lamp. Place the plat to be copied on this glass, and the clean paper upon it. Connect them by pins, etc. Trace all the desired lines of the original with a sharp pencil as

lightly as they can be easily seen. Take care that the paper does not slip. If the plat is larger than the glass, copy its parts successively, being very careful to fix each part in its true relative position. Ink the lines with India ink, making them very fine and pale if the map is to be afterward colored.

**221. Copying on Tracing-Paper.** A thin transparent paper is prepared expressly for the purpose of making copies of maps and drawings, but it is too delicate for much handling. It may be prepared by soaking tissue-paper in a mixture of turpentine and Canada balsam or balsam of fir (two parts of the former to one of the latter), and drying very slowly. Cold-drawn linseed-oil will answer tolerably, the sheets being hung up for some weeks to dry. Linen is also similarly prepared, and sold under the name of "vellum tracing-paper." It is less transparent than the tracing-paper, but is very strong and durable. Both of these are used rather for preserving duplicates than for finished maps.

**222. Copying by Photography.** This may be used for copying drawings, and is especially applicable when the drawings are to be very much reduced in size.

**223. Copying by Blue Prints.** Dissolve one ounce of ferricyanide of potassium in ten ounces of pure water. Also dissolve two ounces of ammonia citrate of iron in ten ounces of water. Mix the two solutions in a cup, and with a brush cover the surface of the paper on which the print is to be made with the mixture.

The surface should be thoroughly covered, but no more of the mixture should be applied than the paper will take up. The paper should become limp and moist but not wet. The work should be done in a room lighted with a lamp, and when the paper is dry it should be kept in a dark place.

To make a blue-print copy, a tracing of the drawing should first be made. Put the tracing over a sheet of the prepared paper and a sheet of glass over the tracing, in order to keep the tracing in contact with the prepared paper. Expose the paper to the sunlight, with the glass toward the sun, until the lines of the drawing are plainly seen on the prepared paper. Wash the paper until the

water running off is no longer colored yellow. When dried, the lines of the drawing will be white upon a blue ground. The prepared paper for blue prints can be bought of dealers in engineers' supplies.

There are several similar methods of making prints, differing in the chemicals used, and in the color of the lines and background.

**224. Copying by Transfer-Paper.** This is thin paper, one side of which is rubbed with black-lead, etc., smoothly spread by cotton. It is laid on the clean paper, the blackened side downward, and the plat is placed upon it. All the lines of the plat are then gone over with moderate pressure by a blunt point, such as the eye-end of a small needle. A faint tracing of these lines will then be found on the clean paper, and can be inked at leisure. If the original can not be thus treated, it may first be copied on tracing-paper, and this copy be thus transferred. If the transfer-paper be prepared by rubbing it with lampblack ground up with hard soap, its lines will be inoffaceable. It is then called "Camp-paper."

**225. Copying by Punctures.** Fix the clean paper on a drawing-board and the plat over it. Prepare a fine needle with a sealing-wax head. Hold it very truly perpendicular to the board, and prick through every angle of the plat, and every corner and intersection of its other lines, such as houses, fences, etc., or at least the two ends of every line. For circles, the center and one point of the circumference are sufficient. For irregular curves, such as rivers, etc., enough points must be pricked to indicate all their sinuosities. Work with system, finishing up one strip at a time, so as not to omit any necessary points nor to prick through any twice, though the latter is safer. When completed, remove the plat. The copy will present a wilderness of fine points. Select those which determine the leading lines, and then the rest will be easily recognized. A beginner should first pencil the lines lightly, and then ink them. An experienced draughtsman will omit the penciling. Two or three copies may be thus pricked through at once. The holes in the original plat may be made nearly invisible by rubbing them on the back of the sheet with a paper-folder, or the thumb-nail.

**226. Copying by Intersections.** Draw a line on the clean paper equal in length to some important line of the original. Two starting-points are thus obtained. Take in the dividers the distance from one end of the line on the original to a third point. From the corresponding end on the copy, describe an arc with this distance for radius and about where the point will come. Take the distance on the original from the other end of the line to the point, and describe a corresponding arc on the copy to intersect the former arc in a point which will be that desired. The principle of the operation is that of our "First Method" (Art. 8). Two pairs of dividers may be used, as explained in Art. 82. "Triangular compasses," having three legs, are used by fixing two of their legs on the two given points of the original,

and the third leg on the point to be copied, and then transferring them to the copy. All the points of the original can thus be accurately reproduced. The operation is, however, very slow. Only the chief points of a plat may be thus transferred, and the details filled in by the following method:

**227. Copying by Squares.** On the original plat draw a series of parallel and equidistant lines. The T-square does this most readily. Draw a similar series at right angles to these. The plat will then be covered with squares, as in Fig. 43. On the clean paper draw a similar series of squares. The important points may now be fixed as in the last article, and the rest copied by eye, all the points in each square of the original being properly placed in the corresponding square of the copy, noticing whether they are near the top or bottom of each square, on its right or left side, etc. This method is rapid, and in skillful hands quite accurate.

Instead of drawing lines on the original, a sheet of transparent paper containing them may be placed over it; or an open frame with threads stretched across it at equal distances and at right angles.

This method supplies a transition to the *Reduction* and *Enlargement* of plats in any desired ratio; under which head *Copying* by the Pantagraph and Camera Lucida will be noticed.

**228. Reducing by Squares.** Begin, as in the preceding article, by drawing squares on the original, or placing them over it. Then on the clean paper draw a similar set of squares, but with their sides one half, one third, etc. (according to the desired reduction), of those of the original plat. Then proceed as before to copy into each small square all the points and lines found in the large square of the plat in their true positions relative to the sides and corners of the square, observing to reduce each distance, by eye, or as directed in the following article, in the given ratio.

**229. Reducing by Proportional Scales.** Many graphical methods of finding the proportionate length of the copy, of any line of the original, may be used. The "angle of reduction" is constructed thus: Draw any line A B. With it for radius and A for center, describe an indefinite arc. With B for center and a radius equal to one half, one third, etc., of A B according to the desired reduction, describe another arc intersecting the former arc in C. Join A C. From A as center describe a series of arcs. Now, to reduce any distance, take it in the dividers, and set it off from A on A B, as to D. Then the distance from D to E, the other end of the arc passing through D, will be the proportionate length to be set off on the copy, in the manner directed in Art. 226.

The sector, or "compass of proportion," described in Art. 50, presents such an "angle of reduction," always ready to be used in this manner.

FIG. 173.

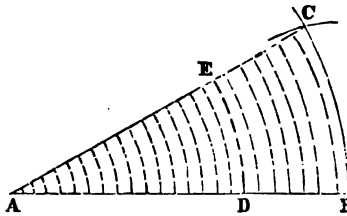
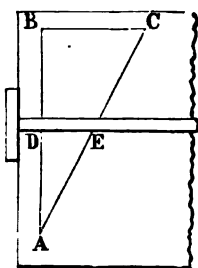


Fig. 174.



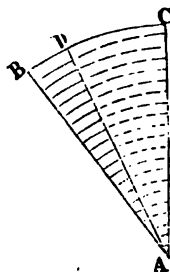
The "angle of reduction" may be simplified thus: Draw a line,  $AB$ , parallel to one side of the drawing-board, and another,  $BC$ , at right angles to it, and one half, etc., of it, as desired. Join  $AC$ . Then let  $AD$  be the distance required to be reduced. Apply a T-square so as to pass through  $D$ . It will meet  $AC$  in some point  $E$ , and  $DE$  will be the reduced length required.

Another arrangement for the same object is shown in Fig. 175. Draw two lines,  $AB$ ,  $AC$ , at any angle, and describe a series of arcs from their intersection,  $A$ , as in the figure. Suppose the reduced scale is to

be half the original scale. Divide the outermost arc into three equal parts, and draw a line from  $A$  to one of the points of division, as  $D$ . Then *each* arc will be divided into parts, one of which is twice the other. Take any distance on the original scale, and find by trial which of the arcs on the right-hand side of the figure it corresponds to. The other part of that arc will be half of it, as desired.

"Proportional compasses," being properly set, reduce lines in any desired ratio. A simple form of them, known as "wholes and halves," is often useful. It consists of two slender bars, pointed at each end, and united by a pivot which is twice as far from one pair of the points as from the other pair. The long ends being set to any distance, the short ends will give precisely half that distance.

Fig. 175.



**230. Reducing by a Pantagraph.** This instrument consists of two long and two short rulers, connected so as to form a parallelogram, and capable of being so adjusted that when a tracing-point attached to it is moved over the lines of a map, etc., a pencil attached to another part of it will mark on paper a precise copy, reduced on any scale desired. It is made in various forms. It is troublesome to use, though rapid in its work.

**231. Reducing by a Camera Lucida.** This is used in the Coast Survey Office. It can not reduce smaller than one fourth, without losing distinctness, and is very trying to the eyes. Squares drawn on the original are brought to apparently coincide with squares on the reduction, and the details are then filled in with the pencil, as seen through the prism of the instrument.

**232. Enlarging Plats.** Plats may be enlarged by the principal methods which have been given for reducing them, but this should be done as seldom as possible, since every inaccuracy in the original becomes magnified in the copy. It is better to make a new plat from the original data.

**233. Conventional Signs.** Various conventional signs or marks have been adopted, more or less generally, to represent on maps the inequalities of



the surface of the ground, its different kinds of culture or natural products, and to objects upon it, so as not to encumber and disfigure it with much writing or many descriptive legends. This is the purpose of what is called *Topographical Mapping*. (See Part III, TOPOGRAPHY.)

**234. Orientation.** The map is usually so drawn that the top of the paper may represent the north. A meridian line should also be drawn, both true and magnetic, as in Fig. 186. The number of degrees and minutes in the variation, if known, should also be placed between the two north points. Sometimes a compass-star is drawn and made very ornamental.

**235. Lettering.** The style in which this is done very much affects the general appearance of the map. The young surveyor should give it much attention and careful practice. It must all be in imitation of the best printed models. No writing, however beautiful, is admissible. The usual letters are the ordinary ROMAN CAPITALS, Small Roman, *ITALIC CAPITALS*, *Small Italic*, and **GOTHIC OR EGYPTIAN**. This last, when well done, is very effective. For the titles of maps, various fancy letters may be used. For very large letters, those formed only of the shades of the letters regarded as blocks (the body being rubbed out after being penciled as a guide to the placing of the shades) are most easily made to look well. The simplest lettering is generally the best. The sizes of the names of places, etc., should be proportional to their importance. Elaborate tables for various scales have been published. It is better to make the letters too small than too large. They should not be crowded. Pencil-lines should always be ruled as guides. The lettering should be in lines parallel to the bottom of the map, except the names of rivers, roads, etc., whose general course should be followed.

**236. Borders.** The *Border* may be a single heavy line, inclosing the map in a rectangle, or such a line may be relieved by a finer line drawn parallel and near to it. Time should not be wasted in ornamenting the border. The simplest is the best.

**237. Joining Paper.** If the map is larger than the sheets of paper at hand, they should be joined with a feather-edge, by proceeding thus: Cut, with a knife guided by a ruler, about one third through the thickness of the paper, and tear off, on the under side, a strip of the remaining thickness, so as to leave a thin, sharp edge. Treat the other sheet in the same way on the other side of it. When these two feather-edges are then put together (with paste, glue, or varnish), they will make a neat and strong joint. The sheet which rests upon the other must be on the right-hand side, if the sheets are joined lengthwise, or below if they are joined in that direction, so that the thickness of the edge may not cast a shadow when properly placed as to the light. The sheets must be joined before lines are drawn across them, or the lines will become distorted. Drawing-paper is now made in rolls of great length, so as to render this operation unnecessary.

**238. Mounting Maps.** A map is sometimes required to be mounted—i. e., backed with canvas or muslin. To do this, wet the muslin and stretch

it strongly on a board by tacks driven very near together. Cover it with strong paste, beating this in with a brush to fill up the pores of the muslin. Then spread paste over the back of the paper, and when it has soaked into it apply it to the muslin, inclining the board, and pasting first a strip, about two inches wide, along the upper side of the paper, pressing it down with clean linen in order to drive out all air-bubbles. Press down another strip in like manner, and so proceed till all is pasted. Let it dry very gradually and thoroughly before cutting the muslin from the board.

Maps may be varnished with picture-varnish, or by applying four or five coats of isinglass-size, letting each dry well before applying the next, and giving a full, flowing coat of Canada balsam diluted with the best oil of turpentine.

### LATITUDES AND DEPARTURES.

**239. Definitions.** The **LATITUDE** of a point is its distance north or south of some "*Parallel of Latitude*," or line running east or west. The **LONGITUDE** of a point is its distance east or west of some "*Meridian*," or line running north and south. In compass-surveying, the magnetic meridian—i. e., the direction in which the magnetic needle points—is the line from which the longitudes of points are measured or reckoned.

The distance which one end of a line is due north or south of the other end is called the *Difference of Latitude* of the two ends of the line; or its *northing* or *southing*; or simply its *latitude*.

The distance which one end of the line is due east or west of the other is here called the *Difference of Longitude* of the two ends of the line; or its *easting* or *westing*; or its *departure*.

*Latitudes* and *Departures* are the most usual terms, and will be generally used hereafter, for the sake of brevity.

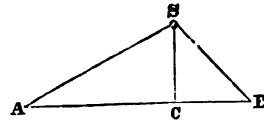
This subject may be illustrated geographically, by noticing that a traveler, in going from New York to Buffalo in a straight line, would go about one hundred and fifty miles due north, and two hundred and fifty miles due west. These distances would be the differences of latitude and of longitude between the two places, or his northing and westing. Returning from Buffalo to New York, the same distances would be his southing and easting.\*

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\* It should be remembered that the following discussions of the latitudes and longitudes of the points of a survey will not be perfectly applicable to those of distant places, such as the cities just named, in consequence of the surface of the earth not being a plane.

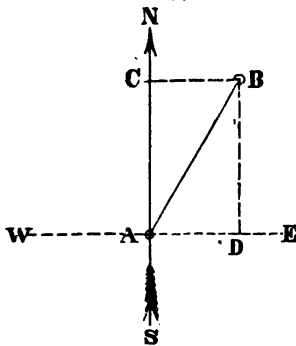
In mathematical language, the operation of finding the latitude and longitude of a line, from its bearing and length, would be called the transformation of Polar Co-ordinates into Rectangular Co-ordinates. It consists in determining, by our *Second Principle*, the position of a point which had originally been determined by the *Third Principle*. Thus, in the figure (which is the same as that of Art. 7), the point S is determined by the angle S A C and by the distance A S. It is also determined by the distances A C and C S, measured at right angles to each other; and then, supposing C S to run due north and south, C S will be the *latitude*, and A C the *departure* of the line A S.

FIG. 176.



**240. Calculation of Latitudes and Departures.** Let A B be a

FIG. 177.



given line, of which the length A B, and the bearing (or angle, B A C, which it makes with the magnetic meridian), are known. It is required to find the differences of latitude and of longitude between its two extremities A and B—that is, to find A C and C B; or, what is the same thing, B D and D A.

It will be at once seen that A B is the hypotenuse of a right-angled triangle, in which the “Latitude” and the “Departure” are the sides about the right angle. We therefore know, from the principles of trigonometry, that

$$A C = A B . \cos . B A C ,$$

$$B C = A B . \sin . B A C .$$

Hence, to find the *latitude* of any course, multiply the natural cosine of the bearing by the length of the course; and to find the *departure* of any course, multiply the natural sine of the bearing by the length of the course.

If the course be northerly, the *latitude* will be north, and will be marked with the algebraic sign +, *plus*, or additive; if it be

southerly, the latitude will be south, and will be marked with the algebraic sign  $-$ , *minus*, or subtractive.

If the course be easterly, the *departure* will be east, and marked  $+$ , or additive; if the course be westerly, the departure will be west, and marked  $-$ , or subtractive.

**241. Formulas.** The rules of the preceding article may be expressed thus :

$$\text{Latitude} = \text{distance} \times \cos. \text{ bearing.}$$

$$\text{Departure} = \text{distance} \times \sin. \text{ bearing.}^*$$

From these formulas may be obtained others, by which, when any two of the above four things are given, the remaining two can be found.

*When the Bearing and Latitude are given ;*

$$\text{Distance} = \frac{\text{latitude}}{\cos. \text{ bearing}} = \text{latitude} \times \sec. \text{ bearing,}$$

$$\text{Departure} = \text{latitude} \times \tan. \text{ bearing.}$$

*When the Bearing and Departure are given ;*

$$\text{Distance} = \frac{\text{departure}}{\sin. \text{ bearing}} = \text{departure} \times \csc. \text{ bearing.}$$

$$\text{Latitude} = \text{departure} \times \cot. \text{ bearing.}$$

*When the Distance and Latitude are given ;*

$$\cos. \text{ bearing} = \frac{\text{latitude}}{\text{distance}},$$

$$\text{Departure} = \text{latitude} \times \tan. \text{ bearing.}$$

*When the Distance and Departure are given ;*

$$\sin. \text{ bearing} = \frac{\text{departure}}{\text{distance}},$$

$$\text{Latitude} = \text{departure} \times \cot. \text{ bearing.}$$

*When the Latitude and Departure are given ;*

$$\tan. \text{ of bearing} = \frac{\text{departure}}{\text{latitude}},$$

$$\text{Distance} = \text{latitude} \times \sec. \text{ bearing.}$$

Still more simply, any two of these three—distance, latitude, and departure—being given, we have

$$\text{Distance} = \sqrt{(\text{latitude}^2 + \text{departure}^2)}$$

$$\text{Latitude} = \sqrt{(\text{distance}^2 - \text{departure}^2)}$$

$$\text{Departure} = \sqrt{(\text{distance}^2 - \text{latitude}^2)}$$

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\* Whenever sines, cosines, tangents, etc., are here named, they mean the natural sines, etc., of an arc described with a radius equal to *one*, or to the unit by which the sines, etc., are measured.

**242. Traverse-Tables.** The latitude and departure of any distance, for any bearing, could be found by the method given in Art. 240, with the aid of a table of natural sines. But to facilitate these calculations, which are of so frequent occurrence and of so great use, *traverse-tables* have been prepared, originally for navigators (whence the name *traverse*), and subsequently for surveyors.\*

The traverse-table at the end of this volume gives the latitude and departure for any bearing, to each quarter of a degree, and for distances from 1 to 9.

*To use it*, find in it the number of degrees in the bearing, on the left-hand side of the page, if it be less than  $45^\circ$ , or on the right-hand side if it be more. The numbers on the same line, running across the page,† are the latitudes and departures for that bearing, and for the respective distances—1, 2, 3, 4, 5, 6, 7, 8, 9—which are at the top and bottom of the page, and which may represent chains, links, rods, feet, or any other unit. Thus, if the bearing be  $15^\circ$ , and the distance 1, the latitude would be 0.966 and the departure 0.259. For the same bearing, but a distance of 8, the latitude would be 7.727 and the departure 2.071.

Any distance, however great, can have its latitude and departure readily obtained from this table; since, for the same bearing, they are directly proportional to the distance, because of the similar triangles which they form. Therefore, to find the latitude or departure for 60, multiply that for 6 by 10, which merely moves the decimal-point one place to the right; for 500, multiply the numbers found in the table for 5, by 100—i. e., move the decimal-point two places to the right, and so on. Merely moving the decimal-point to the right, one, two, or more places, will therefore enable this table to give the latitude and departure for any decimal multiple of the numbers in the table.

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\* The first traverse-table for surveyors seems to have been published in 1791, by John Gale. The most extensive table is that of Captain Boileau, of the British army, being calculated for every minute of bearing, and to five decimal places, for distances from 1 to 10. The table in this volume was calculated for it, and then compared with the one just mentioned.

† In using this or any similar table, lay a ruler across the page, just above or below the line to be followed out. This is a very valuable mechanical assistance.

For compound numbers, such as 873, it is only necessary to find separately the latitudes and departures of 800, of 70, and of 3, and add them together. But this may be done, with scarcely any risk of error, by the following simple rule :

Write down the latitude and departure for the first figure of the given number, as found in the table, neglecting the decimal-point ; write under them the latitude and departure of the second figure, setting them one place farther to the right ; under them write the latitude and departure of the third figure, setting them one place farther to the right ; and so proceed with all the figures of the given number. Add up these latitudes and departures, and cut off the three right-hand figures. The remaining figures will be the latitude and departure of the given number in links, or chains, or feet, or whatever unit it was given in.

For example : Let the latitude and departure of a course having a distance of 873 links, and a bearing of  $20^\circ$ , be required. In the table find  $20^\circ$ , and then take out the latitude and departure for 8, 7, and 3, in turn, placing them as above directed, thus :

| <i>Distances.</i> | <i>Latitudes.</i> | <i>Departures.</i> |
|-------------------|-------------------|--------------------|
| 800               | 7518              | 2736               |
| 70                | 6578              | 2394               |
| 3                 | 2819              | 1026               |
| <u>873</u>        | <u>820·399</u>    | <u>298·566</u>     |

Taking the nearest whole numbers and rejecting the decimals, we find the desired latitude and departure to be 820 and 299.\*

When a 0 occurs in the given number, the next figure must be set *two* places to the right, the reason of which will appear from the following example, in which the 0 is treated like any other number :

Given a bearing of  $35^\circ$ , and a distance of 3048 links.

| <i>Distances.</i> | <i>Latitudes.</i> | <i>Departures.</i> |
|-------------------|-------------------|--------------------|
| 3000              | 2457              | 1721               |
| 000               | 0000              | 0000               |
| 40                | 3277              | 2294               |
| 8                 | 6553              | 4589               |
| <u>3048</u>       | <u>2496·323</u>   | <u>1748·529</u>    |

\* It is frequently doubtful, in many calculations, when the final decimal is 5, whether to increase the preceding figure by one or not. Thus, 43·5 may be called 43 or 44 with equal correctness. It is better, in such cases, not to increase the whole number, so as to escape the trouble of changing the original figure, and the increased

Here the latitudes and departures are 2496 and 1749 links.

When the bearing is over  $45^\circ$ , the names of the columns must be read from the bottom of the page, the latitude of any bearing, as  $50^\circ$ , being the departure of the complement of this bearing, or  $40^\circ$ , and the departure of  $40^\circ$  being the latitude of  $50^\circ$ , etc. The reason of this will be at once seen on inspecting Fig. 177, and imagining the east and west line to become a meridian. For, if A C be the magnetic meridian, as before, and therefore B A C be the bearing of the course A B, then is A C the latitude, and C B the departure of that course. But if A E be the meridian and B A D (the complement of B A C) be the bearing, then is A D (which is equal to C B) the latitude, and D B (which is equal to A C) the departure.

As an example of this, let the bearing be  $63\frac{1}{4}^\circ$ , and the distance 3,469 links. Proceeding as before, we have—

| <i>Distances.</i> | <i>Latitudes.</i> | <i>Departures.</i> |
|-------------------|-------------------|--------------------|
| 3000              | 1350              | 2679               |
| 400               | 1800              | 3572               |
| 60                | 2701              | 5358               |
| 9                 | 4051              | 8037               |
| <hr/>             | <hr/>             | <hr/>              |
| 3469.             | 1561.061          | 3097.817           |

The required latitude and departure are 1561 and 3098 links.

In the few cases occurring in compass-surveying, in which the bearing is recorded as somewhere between the fractions of a degree given in the table, its latitude and departure may be found by interpolation. Thus, if the bearing be  $10\frac{3}{4}^\circ$ , take the half sum of the latitudes and departures for  $10\frac{1}{4}^\circ$  and  $10\frac{3}{4}^\circ$ . If it be  $10^\circ 20'$ , add one third of the difference between the latitudes and departures for  $10\frac{1}{4}^\circ$  and for  $10\frac{3}{4}^\circ$ , to those opposite to  $10\frac{1}{4}^\circ$ ; and so in any similar case.

The uses of this table are very varied. The principal applications of it, which will now be explained, are to *testing the accuracy of surveys*; to *supplying omissions in them*; to *plating them*; and to *calculating their content*.\*

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chance of error. If, however, more than one such case occurs in the same column to be added up, the larger and smaller number should be taken alternately.

\* The traverse-table admits of many other minor uses. Thus, it may be used

**243. Application to testing a Survey.** It is self-evident that, when the surveyor has gone completely around a field or farm, taking the bearings and distances of each boundary-line, till he has got back to the starting-point, he has gone precisely as far south as north, and as far west as east. But the sum of the north latitudes tells how far north he has gone, and the sum of the south latitudes how far south he has gone. Hence these two sums will be equal to each other, if the survey has been correctly made. In like manner, the sums of the east and of the west departures must also be equal to each other.

We will apply this principle to testing the accuracy of the survey of which Fig. 61 is a plat. Prepare seven columns, and head them as below. Find the latitude and departure of each course to the nearest link, and write them in their appropriate columns. Add up these columns. Then will the difference between the sums of the north and south latitudes, and between the sums of the east and west departures, indicate the degree of accuracy of the survey.

| STATIONS. | BEARINGS.  | DISTANCES. | LATITUDES. |      | DEPARTURES. |      |
|-----------|------------|------------|------------|------|-------------|------|
|           |            |            | N.         | S.   | E.          | W.   |
| 1         | N. 85° E.  | 2·70       | 2 21       |      | 1·55        |      |
| 2         | N. 83½° E. | 1·29       | ·15        |      | 1·28        |      |
| 3         | S. 57° E.  | 2·22       |            | 1·21 | 1·86        |      |
| 4         | S. 34½° W. | 3·55       |            | 2·93 |             | 2·00 |
| 5         | N. 56½° W. | 3·23       | 1·78       |      |             | 2·69 |
|           |            |            | 4·14       | 4·14 | 4·69        | 4·69 |

The entire work of the above example is given on the following page.

for solving, approximately, any right-angled triangle by mere inspection, the bearing being taken for one of the acute angles; the latitude being the side adjacent, the departure the side opposite, and the distance the hypotenuse. Any two of these being given, the others are given by the table. The table will therefore serve to show the allowance to be made in chaining on slopes (see Art. 20). Look in the column of bearings for the slope of the ground—i. e., the angle it makes with the horizon, find the given distance, and the latitude corresponding will be the desired horizontal measurement, and the difference between it and the distance will be the allowance to be made.



|      |                      |                      |                                                                                                  |                      |                      |
|------|----------------------|----------------------|--------------------------------------------------------------------------------------------------|----------------------|----------------------|
| 85°  | 1688<br>57840        | 1147<br>40150        | 84½°                                                                                             | 2480<br>4188<br>4188 | 1688<br>2814<br>2814 |
| 270° | 221·140              | 154·850              | 855°                                                                                             | 298·463              | 199·754              |
| 83½° | 118<br>226<br>1019   | 994<br>1987<br>8942  | 56½°                                                                                             | 1656<br>1104<br>1656 | 2502<br>1668<br>2502 |
| 129° | 14·579               | 128·212              | 823°                                                                                             | 178·296              | 269·882              |
| 57°  | 1089<br>1089<br>1089 | 1677<br>1677<br>1677 | The nearest link is taken to be inserted in the table, and the remaining decimals are neglected. |                      |                      |
| 222° | 120·879              | 186·147              |                                                                                                  |                      |                      |

In the preceding example the respective sums were found to be exactly equal. This, however, will rarely occur in an extensive survey. If the difference be great, it indicates some mistake, and the survey must be repeated with greater care; but if the difference be small it indicates, not absolute errors, but only inaccuracies, unavoidable in surveys with the compass, and the survey may be accepted.

How great a difference in the sums of the columns may be allowed, as not necessitating a new survey, is a dubious point. Some surveyors would admit a difference of 1 link for every 3 chains in the sum of the courses; others only 1 link for every 10 chains. One writer puts the limit at 5 links for each station; another at 25 links in a survey of 100 acres. But every practical surveyor soon learns how near to an equality his instrument and his skill will enable him to come in ordinary cases, and can therefore establish a standard for himself, by which he can judge whether the difference, in any survey of his own, is probably the result of an error, or only of his customary degree of inaccuracy, two things to be very carefully distinguished.\*

**244. Application to supplying Omissions.** Any two omissions in the field-notes can be supplied by a proper use of the method of latitudes and departures; as will be explained in Chapter V, which treats of "Obstacles to Measurement," under which head this

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\* A French writer fixes the allowable difference in chaining at 1·400 of level lines; 1·200 of lines on moderate slopes; 1·100 of lines on steep slopes.

subject most appropriately belongs. But a knowledge of the fact that any two omissions can be supplied, should not lead the young surveyor to be negligent in making every possible measurement, since an omission renders it necessary to assume all the notes taken to be correct, the means of testing them no longer existing.

**245. Balancing a Survey.** The subsequent applications of this method require the survey to be previously *balanced*. This operation consists in *correcting* the latitudes and departures of the courses, so that their sums *shall* be equal, and thus "balance." This is usually done by distributing the differences of the sums among the courses in proportion to their length; saying, *as* the sum of the lengths of all the courses *is* to the whole difference of the latitude, *so is* the length of each course *to* the correction of its latitude. A similar proportion corrects the departures.\*

It is not often necessary to make the exact proportion, as the correction can usually be made, with sufficient accuracy, by noting how much per chain it should be, and correcting accordingly.

In the example given below, the differences have purposely been made considerable. The corrected latitudes and departures have been here inserted in four additional columns, but in practice they should be written *in red ink* over the original latitudes and departures, and the latter crossed out with red ink.

| STATIONS. | BEARINGS.  | DISTANCES. | LATITUDES. |       | DEPARTURES. |       | CORRECTED LATITUDES. |       | CORRECTED DEPARTURES. |       |
|-----------|------------|------------|------------|-------|-------------|-------|----------------------|-------|-----------------------|-------|
|           |            |            | N. +       | S. —  | E. +        | W. —  | N. +                 | S. —  | E. +                  | W. —  |
| 1         | N. 52° E.  | 10·63      | 6·54       |       | 8·38        |       | 6·58                 |       | 8·34                  |       |
| 2         | S. 29½° E. | 4·10       |            | 3·56  | 2·03        |       |                      | 3·55  | 2·01                  |       |
| 3         | S. 81¼° W. | 7·69       |            | 6·54  |             | 4·05  |                      | 6·51  |                       | 4·08  |
| 4         | N. 61° W.  | 7·13       | 3·46       |       |             | 6·24  | 3·48                 |       |                       | 6·27  |
|           |            | 29·55      | 10·00      | 10·10 | 10·41       | 10·29 | 10·06                | 10·06 | 10·35                 | 10·35 |

The corrections are made by the following proportions; the nearest whole numbers being taken :

---

\* A demonstration of this principle was given by Dr. Bowditch, in No. 4 of "The Analyst."

| <i>For the Latitudes.</i> |                  | <i>For the Departures.</i> |                  |
|---------------------------|------------------|----------------------------|------------------|
| 29°55'                    | 10°63' :: 10 : 4 | 29°55'                     | 10°63' :: 12 : 4 |
| 29°55'                    | 4°10' :: 10 : 1  | 29°55'                     | 4°10' :: 12 : 2  |
| 29°55'                    | 7°69' :: 10 : 8  | 29°55'                     | 7°69' :: 12 : 8  |
| 29°55'                    | 7°13' :: 10 : 2  | 29°55'                     | 7°13' :: 12 : 8  |
|                           | <u>10</u>        |                            | <u>12</u>        |

This rule is not always to be strictly followed. If one line of a survey has been measured over very uneven and rough ground, or if its bearing has been taken with an indistinct sight, while the other lines have been measured over level and clear ground, it is probable that most of the error has occurred on that line, and the correction should be chiefly made on its latitude and departure.

If a slight change of the bearing of a long course will favor the balancing, it should be so changed, since the compass is much more subject to error than the chain. So, too, if shortening any doubtful line will favor the balancing, it should be done, since distances are generally measured too long.

**246. Application to Platting.** Rule three columns; one for stations, the next for total latitudes, and the third for total departures. Fill the last two columns by beginning at any convenient station (the extreme east or west is best) and adding up (algebraically) the latitudes of the following stations, noticing that the south latitudes are subtractive. Do the same for the departures, observing that the westerly ones are also subtractive.

Taking the example given in Art. 243, and beginning with station 1, the following will be the results :

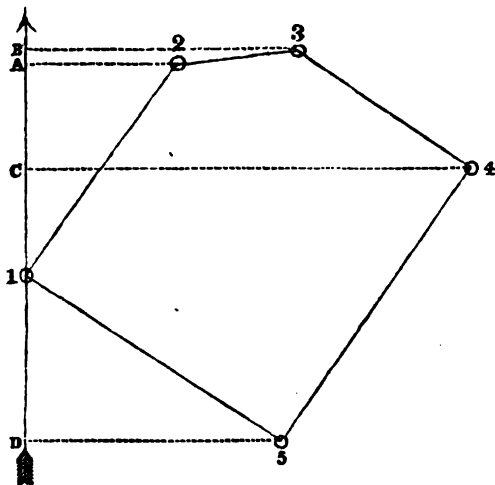
| STATIONS. | TOTAL LATITUDES FROM STATION 1. | TOTAL DEPARTURES FROM STATION 1. |
|-----------|---------------------------------|----------------------------------|
| 1         | 0°00                            | 0°00                             |
| 2         | + 2°21 N.                       | + 1°55 E.                        |
| 3         | + 2°36 N.                       | + 2°33 E.                        |
| 4         | + 1°15 N.                       | + 4°69 E.                        |
| 5         | - 1°78 S.                       | + 2°69 E.                        |
| 1         | 0°00                            | 0°00                             |

It will be seen that the work proves itself, by the total latitudes and departures for station 1, again coming out equal to zero.

To use this table, draw a meridian through the point taken for

station 1, as in Fig. 178. Set off, upward from this, along the meridian, the latitude, 221 links, to A, and from A, to the right

FIG. 178.



perpendicularly, set off the departure, 155 links.\* This gives the point 2. Join 1....2. From 1 again, set off, upward, 236 links, to B, and from B, to the right, perpendicularly, set off 283 links, which will fix the point 3. Join 2....3; and so proceed, setting off north latitudes along the meridian upward, and south latitudes along it downward; east

departures perpendicularly to the right, and west departures perpendicularly to the left.

The advantages of this method are its rapidity, ease, and accuracy; the impossibility of any error in platting any one course affecting the following points; and the certainty of the plat "coming together," if the latitudes and departures have been "balanced."

#### CALCULATING THE CONTENT.

**247. Methods.** When a field has been platted, by whatever method it may have been surveyed, its content can be obtained from its plat by dividing it up into triangles, and measuring on the plat their bases and perpendiculars; or by any of the other means explained in Chapter II.

But these are only approximate methods, their degree of accu-

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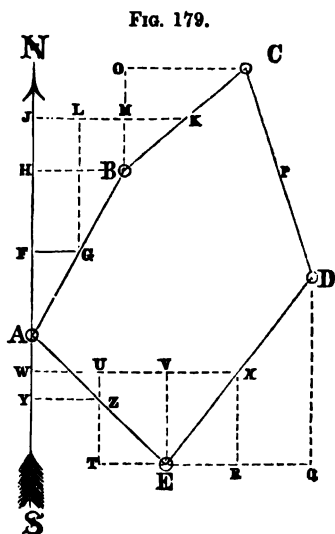
\* This is most easily done with the aid of a right-angled triangle, sliding one of the sides adjacent to the right angle along the blade of the square, to which the other side will then be perpendicular.

racy depending on the largeness of scale of the plat and the skill of the draughtsman. The invaluable method of latitudes and departures gives another means, perfectly accurate, and not requiring the previous preparation of a plat. It is sometimes called the rectangular, or the Pennsylvania, or Rittenhouse's method of calculation.\*

**248. Definitions.** Imagine a meridian line to pass through the extreme east or west corner of a field. According to the definitions established in Art. 239 (and here recapitulated for convenience of reference), the perpendicular distance of each station from that meridian is the *Longitude* of that station; additive, or *plus*, if east; subtractive, or *minus*, if west. The distance of the middle of any line, such as the side of the field, from the meridian, is called the *longitude* of that side.† The difference of the longitudes of the two ends of a line is called the *Departure* of that line. The difference of the latitudes of the two ends of a line is called the *Latitude* of the line.

**249. Longitudes.** To give more definiteness to the development of this subject, the figure in the margin will be referred to, and may be considered to represent any space inclosed by straight lines.

Let N S be the meridian passing through the extreme westerly station of the field A B C D E.



\* It is, however, substantially the same as Mr. Thomas Burgh's "Method to determine the Areas of Right-lined Figures universally," published nearly a century ago.

† The phrase "meridian distance" is generally used for what is here called "longitude"; but the analogy of "differences of longitude" with "differences of latitude," usually but anomalously united with the word "departure," borrowed from navigation, seems to put beyond all question the propriety of the innovation here introduced.

From the middle and ends of each side draw perpendiculars to the meridian. These perpendiculars will be the *longitudes* and *departures* of the respective sides. The longitude,  $FG$ , of the *first course*,  $AB$ , is evidently equal to half its departure,  $HB$ . The longitude,  $JK$ , of the *second course*,  $BC$ , is equal to  $JL + LM + MK$ , or equal to the longitude of the preceding course, plus half its departure, plus half the departure of the course itself. The longitude,  $YZ$ , of some other course, as  $EA$ , taken anywhere, is equal to  $WX - VX - UV$ , or equal to the longitude of the preceding course, minus half its departure, minus half the departure of the course itself—i. e., equal to the *algebraic* sum of these three parts, remembering that *westerly* departures are negative, and therefore to be subtracted when the directions are to make an *algebraic* addition.

To avoid fractions it will be better to double each of the preceding expressions. We shall then have a

#### GENERAL RULE FOR FINDING DOUBLE LONGITUDES.

*The double longitude of the FIRST COURSE is equal to its departure.*

*The double longitude of the SECOND COURSE is equal to the double longitude of the first course, plus the departure of that course, plus the departure of the second course.*

*The double longitude of the THIRD COURSE is equal to the double longitude of the second course, plus the departure of that course, plus the departure of the course itself.*

*The double longitude of ANY course is equal to the double longitude of the preceding course, plus the departure of that course, plus the departure of the course itself.\**

The double longitude of the *last* course (as well as of the first) is equal to its departure. Its “coming out” so, when obtained by the above rule, proves the accuracy of the calculation of all the preceding double longitudes.

**250. Areas.** We will now proceed to find the area or content of a field, by means of the “double longitudes” of its sides, which

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\* The last course is a “preceding course” to the first course, as will appear on remembering that these two courses join each other on the ground.

can be readily obtained by the preceding rule, whatever their number.

251. Beginning with a *three-sided field*,  $ABC$  in the figure, draw a meridian through  $A$ , and draw perpendiculars to it as in the last figure. It is plain that its content is equal to the difference of the areas of the trapezoid  $DBCE$ , and of the triangles  $ABD$  and  $ACE$ .

The area of the triangle  $ABD$  is equal to the product of  $AD$  by half of  $DB$ , or to the product of  $AD$  by  $FG$ ; i. e., equal to the product of the latitude of the first course by its longitude.

The area of the trapezoid  $DBCE$  is equal to the product of  $DE$  by half the sum of  $DB$  and  $CE$ , or by  $HJ$ ; i. e., to the product of the latitude of the second course by its longitude.

The area of the triangle  $ACE$  is equal to the product of  $AE$  by half  $EC$ , or by  $KL$ ; i. e., to the product of the latitude of the third course by its longitude.

FIG. 181.

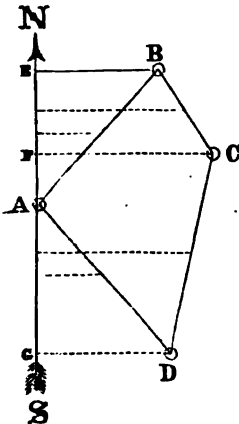
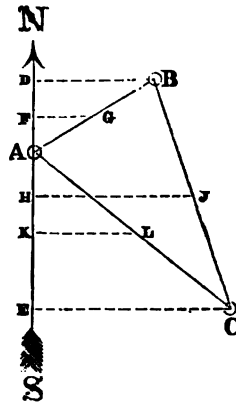


FIG. 180.



Calling the products in which the latitude was north, *North Products*, and the products in which the latitude was south, *South Products*, we shall find the area of the trapezoid to be a *south product*, and the areas of the triangles to be *north products*. The difference of the north products and the south products is therefore the desired area of the three-sided field  $ABC$ .

Using the *double longitudes* (in order to avoid fractions) in each of the preceding products, their difference will be the *double area* of the triangle  $ABC$ .

252. Taking now a *four-sided field*,  $ABCD$  in the figure, and drawing a meridian and longitudes as

before, it is seen, on inspection, that its area would be obtained by taking the two triangles,  $AEB$ ,  $ADG$ , from the figure  $EBCDGE$ , or from the sum of the two trapezoids  $EBCF$  and  $FCDG$ .

The area of the triangle  $AEB$  will be found, as in the last article, to be equal to the product of the latitude of the first course by its longitude. The product will be *North*.

The area of the trapezoid  $EBCF$  will be found to equal the latitude of the second course by its longitude. The product will be *South*.

The area of the trapezoid  $FCDG$  will be found to equal the product of the latitude of the third course by its longitude. The product will be *South*.

The area of the triangle  $ADG$  will be found to equal the product of the latitude of the fourth course by its longitude. The product will be *North*.

*The difference of the north and south products will therefore be the desired area of the four-sided field ABCD.*

Using the *double* longitude as before, in each of the preceding products, their difference will be *double* the area of the field.

**253.** Whatever the number or directions of the sides of a field, or of any space inclosed by straight lines, its area will always be equal to half of the difference of the north and south products arising from multiplying together the latitude and double longitude of each course or side.

We have, therefore, the following

#### GENERAL RULE FOR FINDING AREAS.

1. *Prepare ten columns, headed as in the example below, and in the first three write the stations, bearings, and distances.*
2. *Find the latitudes and departures of each course, by the traverse-table, as directed in Art. 242, placing them in the four following columns.*
3. *Balance them, as in Art. 245, correcting them in red ink.*
4. *Find the double longitudes, as in Art. 249, with reference*



to a meridian passing through the extreme east or west station, and place them in the eighth column.

5. Multiply the double longitude of each course by the corrected latitude of that course, placing the north products in the ninth column, and the south products in the tenth column.

6. Add up the last two columns, subtract the smaller sum from the larger, and divide the difference by two. The quotient will be the content desired.

254. To find the most easterly or westerly station of a survey, without a plat, it is best to make a rough hand-sketch of the survey, drawing the lines in an approximation to their true directions, by drawing a north and south, and east and west lines, and considering the bearings as fractional parts of a right angle, or  $90^\circ$ ; a course N.  $45^\circ$  E., for example, being drawn about half-way between a north and an east direction; a course N.  $28^\circ$  W. being not quite one third of the way around from north to west; and so on, drawing them of approximately true proportional lengths.

255. Example 1, given below, refers to the five-sided field, of which a plat is given in Fig. 161, and the latitudes and departures of which were calculated in Art. 243. Station 1 is the most westerly station, and the meridian will be supposed to pass through it. The double longitudes are best found by a continual addition and subtraction, as in the margin, where they are marked D. L. The double longitude of the last course comes out equal to its departure, thus proving the work.

The double longitudes being thus obtained, are multiplied by the corresponding latitudes, and the content of the field obtained as directed in the General Rule.

This example may serve as a pattern for the most compact manner of arranging the work.

| STA-<br>TIONS. |                                  |
|----------------|----------------------------------|
| 1              | + 1.55 D. L.<br>+ 1.55<br>+ 1.28 |
| 2              | + 4.38 D. L.<br>+ 1.28<br>+ 1.86 |
| 3              | + 7.52 D. L.<br>+ 1.86<br>- 2.00 |
| 4              | + 7.38 D. L.<br>- 2.00<br>- 2.69 |
| 5              | + 2.69 D. L.                     |

| STA-<br>TIONS. | BEARINGS.  | DIS-<br>TANCES. | LATITUDES. |      | DEPARTURES. |      | DOUBLE<br>LONGI-<br>TUDES. | DOUBLE AREAS.  |         |
|----------------|------------|-----------------|------------|------|-------------|------|----------------------------|----------------|---------|
|                |            |                 | N. +       | S. - | E. +        | W. - |                            | N. -           | S. +    |
| 1              | N. 35° E.  | 2.70            | 2.21       |      | 1.55        |      | +1.55                      | 8.4255         |         |
| 2              | N. 83½° E. | 1.29            | .15        |      | 1.28        |      | +4.38                      | 0.6570         |         |
| 3              | S. 57° E.  | 2.22            |            | 1.21 | 1.86        |      | +7.52                      |                | 9.0992  |
| 4              | S. 34½° W. | 3.55            |            | 2.98 |             | 2.00 | +7.38                      |                | 21.6234 |
| 5              | N. 56½° W. | 3.23            | 1.78       |      |             | 2.69 | +2.69                      | 4.7882         |         |
|                |            |                 | 4.14       | 4.14 | 4.69        | 4.69 |                            | 8.8707         | 30.7226 |
|                |            |                 |            |      |             |      |                            |                | 8.8707  |
|                |            |                 |            |      |             |      |                            | 2)21.8519      |         |
|                |            |                 |            |      |             |      |                            | square chains, | 10.9259 |

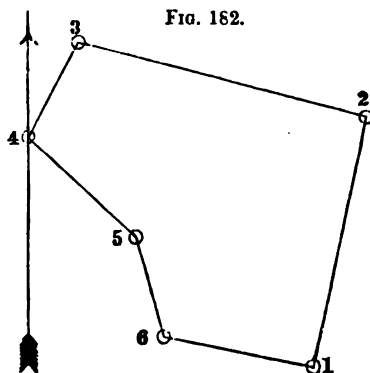
Content = 1 A. 0 R. 15 P.

| STA-<br>TIONS. |                                  |
|----------------|----------------------------------|
| 4              | - 2.00 D. L.<br>- 2.00<br>- 2.69 |
| 5              | - 6.69 D. L.<br>- 2.69<br>+ 1.55 |
| 1              | - 7.83 D. L.<br>+ 1.55<br>+ 1.28 |
| 2              | - 5.00 D. L.<br>+ 1.28<br>+ 1.86 |
| 3              | - 1.86                           |

256. The meridian might equally well have been supposed to pass through the most easterly station, 4 in the figure. The double longitudes could then have been calculated as in the margin. They will, of course, be all west, or minus. The products being then calculated, the sum of the north products will be found to be 29.9625, and of the south products 8.1106, and their difference to be 21.8519, the same result as before.

257. A number of examples, with and without answers, will now be given as ex-

ercises for the student, who should plat them by some of the methods given in the chapter on platting, using each of them at least once. He should then calculate their content by the method just given, and *check* it, by also calculating the area of the plat by some of the geometrical or instrumental methods given in Chapter I; for no single calculation is



ever reliable. All the examples (except the last) are from the author's actual surveys.

*Example 2*, given below, is also fully worked out, as another pattern for the student, who need have no difficulty with any possible case if he strictly follows the directions which have been given. The plat is on a scale of 2 chains to 1 inch (= 1:1584).

| STA-<br>TIONS. | BEARINGS.  | DIS-<br>TANCES. | LATITUDES. |      | DEPARTURES. |      | DOUBLE<br>LONGI-<br>TUDES. | DOUBLE AREAS.         |        |
|----------------|------------|-----------------|------------|------|-------------|------|----------------------------|-----------------------|--------|
|                |            |                 | N. +       | S. - | E. +        | W. - |                            | N. +                  | S. -   |
| 1              | N. 12½° E. | 2·81            | 2·75       |      | ·60         |      | + 6·56                     | 18·0400               |        |
| 2              | N. 76° W.  | 8·20            | ·77        |      |             | 8·11 | + 4·05                     | 8·1185                |        |
| 3              | S. 24½° W. | 1·14            |            | 1·04 |             | ·47  | + ·47                      |                       | ·4888  |
| 4              | S. 48° E.  | 1·53            |            | 1·02 | 1·14        |      | + 1·14                     |                       | 1·1628 |
| 5              | S. 12½° E. | 1·12            |            | 1·09 | ·24         |      | + 2·52                     |                       | 2·7468 |
| 6              | S. 77° E.  | 1·64            |            | ·37  | 1·60        |      | + 4·86                     |                       | 1·6132 |
|                |            |                 | 8·52       | 3·52 | 3·58        | 3·58 |                            | 21·1585               | 6·0116 |
|                |            |                 |            |      |             |      |                            | 6·0116                |        |
|                |            |                 |            |      |             |      |                            | 2)15·1469             |        |
|                |            |                 |            |      |             |      |                            | square chains, 7·5734 |        |

Content = 0 A. 3 R. 1 P.

2)15·1469

square chains, 7·5734

*Example 3.*

| STATIONS. | BEARINGS.  | DISTANCES. |
|-----------|------------|------------|
| 1         | N. 52° E.  | 10·64      |
| 2         | S. 29½° E. | 4·09       |
| 3         | S. 81½° W. | 7·68       |
| 4         | N. 61° W.  | 7·24       |

Ans. 4 A. 3 R. 28 P.

*Example 4.*

| STATIONS. | BEARINGS.  | DISTANCES. |
|-----------|------------|------------|
| 1         | S. 21° W.  | 12·41      |
| 2         | N. 83½° E. | 5·86       |
| 3         | N. 12° E.  | 8·25       |
| 4         | N. 47° W.  | 4·24       |

Ans. 4 A. 2 R. 37 P.

*Example 5.*

| STATIONS. | BEARINGS.  | DISTANCES. |
|-----------|------------|------------|
| 1         | N. 84½° E. | 2·78       |
| 2         | N. 85° E.  | 1·28       |
| 3         | S. 56½° E. | 2·20       |
| 4         | S. 84½° W. | 3·53       |
| 5         | N. 56½° W. | 3·20       |

Ans. 1 A. 0 R. 14 P.

*Example 6.*

| STATIONS. | BEARINGS.  | DISTANCES. |
|-----------|------------|------------|
| 1         | N. 85° E.  | 6·49       |
| 2         | S. 56½° E. | 14·15      |
| 3         | S. 84½° W. | 5·10       |
| 4         | N. 56° W.  | 5·84       |
| 5         | S. 29½° W. | 2·52       |
| 6         | N. 49½° W. | 8·73       |

*Example 7.*

| STATIONS. | BEARINGS.                     | DISTANCES. |
|-----------|-------------------------------|------------|
| 1         | S. $21\frac{1}{2}^{\circ}$ W. | 17.62      |
| 2         | S. $84^{\circ}$ W.            | 10.00      |
| 3         | N. $56^{\circ}$ W.            | 14.15      |
| 4         | N. $84^{\circ}$ E.            | 9.76       |
| 5         | N. $67^{\circ}$ E.            | 2.30       |
| 6         | N. $28^{\circ}$ E.            | 7.03       |
| 7         | N. $18\frac{1}{2}^{\circ}$ E. | 4.43       |
| 8         | S. $76\frac{1}{2}^{\circ}$ E. | 12.41      |

*Example 8.*

| STATIONS. | BEARINGS.                     | DISTANCES. |
|-----------|-------------------------------|------------|
| 1         | S. $65\frac{1}{2}^{\circ}$ E. | 4.98       |
| 2         | S. $58^{\circ}$ E.            | 8.56       |
| 3         | S. $14\frac{1}{2}^{\circ}$ W. | 20.69      |
| 4         | S. $47^{\circ}$ W.            | 0.60       |
| 5         | S. $57\frac{1}{2}^{\circ}$ W. | 8.98       |
| 6         | N. $56^{\circ}$ W.            | 12.90      |
| 7         | N. $84^{\circ}$ E.            | 10.00      |
| 8         | N. $21\frac{1}{2}^{\circ}$ E. | 17.62      |

*Example 9.*

| STATIONS. | BEARINGS.                     | DISTANCES. |
|-----------|-------------------------------|------------|
| 1         | S. $57^{\circ}$ E.            | 5.77       |
| 2         | S. $36\frac{1}{2}^{\circ}$ W. | 2.25       |
| 3         | S. $39\frac{1}{2}^{\circ}$ W. | 1.00       |
| 4         | S. $70\frac{1}{2}^{\circ}$ W. | 1.04       |
| 5         | N. $68\frac{1}{2}^{\circ}$ W. | 1.23       |
| 6         | N. $56^{\circ}$ W.            | 2.19       |
| 7         | N. $33\frac{1}{2}^{\circ}$ E. | 1.05       |
| 8         | N. $56\frac{1}{2}^{\circ}$ W. | 1.54       |
| 9         | N. $33\frac{1}{2}^{\circ}$ E. | 8.18       |

Ans. 2 A. 0 R. 32 P.

*Example 10.*

| STATIONS. | BEARINGS.              | DISTANCES. |
|-----------|------------------------|------------|
| 1         | N. $63^{\circ} 51'$ W. | 6.91       |
| 2         | N. $63^{\circ} 44'$ W. | 7.26       |
| 3         | N. $69^{\circ} 35'$ W. | 3.34       |
| 4         | N. $77^{\circ} 50'$ W. | 6.54       |
| 5         | N. $31^{\circ} 24'$ E. | 14.38      |
| 6         | N. $31^{\circ} 18'$ E. | 16.81      |
| 7         | S. $68^{\circ} 55'$ E. | 13.64      |
| 8         | S. $68^{\circ} 42'$ E. | 11.54      |
| 9         | S. $33^{\circ} 45'$ W. | 31.55      |

Ans. 74 acres.

*Example 11.*

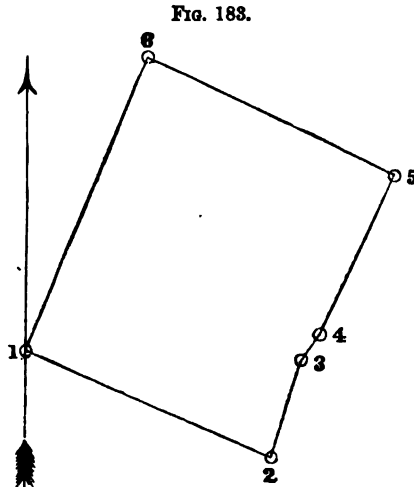
| STATIONS. | BEARINGS.                     | DISTANCES. |
|-----------|-------------------------------|------------|
| 1         | N. $18\frac{1}{2}^{\circ}$ E. | 1.98       |
| 2         | N. $9^{\circ}$ W.             | 1.29       |
| 3         | N. $14^{\circ}$ W.            | 2.71       |
| 4         | N. $74^{\circ}$ E.            | 0.95       |
| 5         | S. $48\frac{1}{2}^{\circ}$ E. | 1.59       |
| 6         | S. $14\frac{1}{2}^{\circ}$ E. | 1.14       |
| 7         | S. $19\frac{1}{2}^{\circ}$ E. | 2.15       |
| 8         | S. $23\frac{1}{2}^{\circ}$ W. | 1.22       |
| 9         | S. $5^{\circ}$ W.             | 1.40       |
| 10        | S. $30^{\circ}$ W.            | 1.02       |
| 11        | S. $81\frac{1}{2}^{\circ}$ W. | 0.69       |
| 12        | N. $32\frac{1}{2}^{\circ}$ W. | 1.98       |

*Example 12.*

| STATIONS. | BEARINGS.                     | DISTANCES. |
|-----------|-------------------------------|------------|
| 1         | N. $72\frac{1}{2}^{\circ}$ E. | 0.88       |
| 2         | S. $20\frac{1}{2}^{\circ}$ E. | 0.22       |
| 3         | S. $63^{\circ}$ E.            | 0.75       |
| 4         | N. $51^{\circ}$ E.            | 2.35       |
| 5         | N. $44^{\circ}$ E.            | 1.10       |
| 6         | N. $25\frac{1}{2}^{\circ}$ W. | 1.96       |
| 7         | N. $8\frac{1}{2}^{\circ}$ W.  | 1.05       |
| 8         | S. $29^{\circ}$ W.            | 1.63       |
| 9         | N. $71\frac{1}{2}^{\circ}$ W. | 0.81       |
| 10        | N. $13\frac{1}{2}^{\circ}$ W. | 1.17       |
| 11        | N. $68^{\circ}$ W.            | 1.28       |
| 12        | West.                         | 1.68       |
| 13        | N. $49^{\circ}$ W.            | 0.80       |
| 14        | S. $19\frac{1}{2}^{\circ}$ E. | 6.20       |

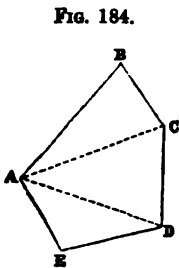
*Example 13.* A farm is described in an old deed as bounded thus: Beginning at a pile of stones, and running thence twenty-

seven chains and seventy links southeasterly sixty-six and a half degrees to a white-oak stump; thence eleven chains and sixteen links northeasterly twenty and a half degrees to a hickory-tree; thence two chains and thirty-five links northeasterly thirty-six degrees to the southeasterly corner of the homestead; thence nineteen chains and thirty-two links northeasterly twenty-six degrees to a stone set in the ground; thence twenty-eight chains and eighty links northwesterly sixty-six degrees to a pine-stump; thence thirty-three chains and nineteen



links southwesterly twenty-two degrees to the place of beginning, containing ninety-two acres, be the same more or less. Required the exact content.

**258. Mascheroni's Theorem.** *The surface of any polygon is equal to half the sum of the products of its sides (omitting any one side) taken two and two, into the sines of the angles which those sides make with each other.*

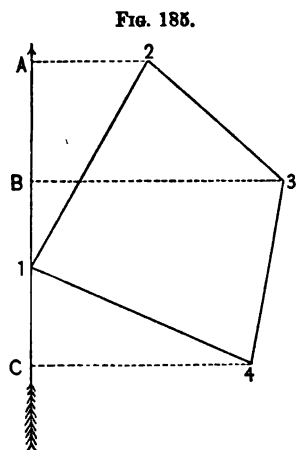


Thus, take any polygon, such as the five-sided one in the figure. Express the angle which the directions of any two sides, as  $AB$ ,  $CD$ , make with each other, thus  $(AB \wedge CD)$ . Then will the content of that polygon be, as below:

$$= \frac{1}{2} [AB \cdot BC \cdot \sin (AB \wedge BC) + AB \cdot CD \cdot \sin (AB \wedge CD) + AB \cdot DE \cdot \sin (AB \wedge DE) + BC \cdot CD \cdot \sin (BC \wedge CD) + BC \cdot DE \cdot \sin (BC \wedge DE) + CD \cdot DE \cdot \sin (CD \wedge DE)]$$

The demonstration consists merely in dividing the polygon into

triangles by lines drawn from any angle (as A); then expressing the area of each triangle by half the product of its base and the perpendicular let fall upon it from the above-named angle; and finally separating the perpendicular into parts which can each be expressed by the product of some one side into the sine of the angle made by it with another side. The sum of these triangles equals the polygon.



The expressions are simplified by dividing the proposed polygon into two parts by a diagonal, and computing the area of each part separately, making the diagonal the side omitted.

#### *A New Method of calculating Areas.*

**259.** In Fig. 185, let the total latitudes (Art. 246) of the stations 1, 2, 3, and 4 be represented by  $l_1$ ,  $l_2$ ,  $l_3$ , and  $l_4$ , respectively.

Let the departures of each course separately be represented by  $d_1$ ,  $d_2$ ,  $d_3$ , and  $d_4$ , respectively.

The double area of A B 23

$$\begin{aligned} &= AB (A2 + B3) \\ &= (l_2 - l_3) (d_1 + d_1 + d_2) \\ &= l_2 d_1 + l_2 d_1 + l_2 d_2 - l_3 d_1 - l_3 d_1 - l_3 d_2. \quad [1.] \end{aligned}$$

The double area of C B34

$$\begin{aligned} &= CB (B3 + C4) \\ &= (l_3 + l_4) (d_4 + d_4 + d_3) \\ &= l_3 d_4 + l_3 d_4 + l_3 d_3 + l_4 d_4 + l_4 d_4 + l_4 d_3. \quad [2.] \end{aligned}$$

The double area of 12 A = A1 (A2) =  $l_2 d_1$ . [3.]

The double area of 14 C = C1 (C4) =  $l_4 d_4$ . [4.]

Now, the double area of the figure 1234 is equal to the sum of [1] and [2] - the sum of [3] and [4].

Combining and reducing, we have :

$$\begin{aligned} \text{Double area of 1234} &= l_2 (d_1 + d_2) + l_3 (d_4 + d_4 + d_3 - d_1 - d_2) + l_4 (d_3 + d_4). \end{aligned}$$

Noting that  $d_4 + d_3 = d_1 + d_2$ , we have,

Double area of 1234 =  $l_2 (d_1 + d_2) + l_3 (d_2 - d_3) + l_4 (d_3 + d_4)$ .

Putting this in the form of a rule, we have: *Multiply the total latitude of each station by the algebraic sum of the departures of the two adjacent courses. One half of the algebraic sum of the products will be the area.*

As an exercise for the student, let him find, by the above method, an expression for the area of figures having five and six sides.

The following example, worked out by the method of double longitudes (on page 158), and below, by the new method, will show the difference between the two methods:

| STATIONS. | BEARINGS.  | DISTANCES. | LATITUDES. |      | DEPARTURES. |      | TOTAL LATITUDES. | ADJACENT DEPARTURES. | DOUBLE AREAS.          |
|-----------|------------|------------|------------|------|-------------|------|------------------|----------------------|------------------------|
|           |            |            | N. +       | S. - | E. +        | W. - |                  |                      |                        |
| 1         | N. 85° E.  | 2.70       | 2.21       |      | 1.55        |      |                  |                      |                        |
| 2         | N. 83½° E. | 1.29       | .15        |      | 1.28        |      | 2.21             | 2.88                 | 6.2548                 |
| 3         | S. 57° E.  | 2.22       |            | 1.91 | 1.86        |      | 2.86             | 3.14                 | 7.4104                 |
| 4         | S. 34½° W. | 3.55       |            | 2.93 |             | 2.00 | 1.15             | -0.14                | -0.1610                |
| 5         | N. 56½° W. | 3.23       | 1.78       |      |             | 2.69 | -1.78            | -4.69                | 8.8482                 |
|           |            |            | 4.14       | 4.14 | 4.69        | 4.69 |                  |                      | 2) 21.8519             |
|           |            |            |            |      |             |      |                  |                      | square chains, 10.9259 |

In computing the total latitudes, if the total latitude of the last station equals the latitude of the last course with sign changed, the total latitudes may be considered correct.

The station through which the meridian of the survey is supposed to pass, and from which the total latitude is reckoned, will have no latitude, and hence the product of its latitude and adjacent departures will be zero. There will therefore be one less product than there are stations.

Any station may be taken as the starting-point.

To verify the area obtained in any case, calculate a second time, using a different station as the starting-point.

This method was first published by J. Woodbridge Davis, C. E., Ph. D., in Van Nostrand's "Engineering Magazine," for April, 1879, where a general discussion of the method is given.

### THE DECLINATION OF THE MAGNETIC NEEDLE.

**260. Definitions.** The *magnetic meridian* is the direction indicated by the magnetic needle. The *true meridian* is a true north and south line, which, if produced, would pass through the poles of the earth. The *declination* of the needle is the angle which one of these lines makes with the other.

Fig. 186.



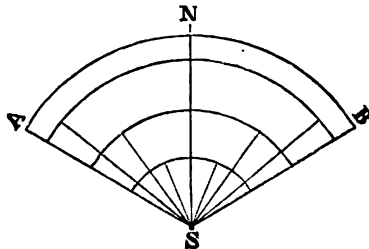
In the figure, if N S represent the direction of the true meridian, and N' S' the direction of the magnetic meridian at any place, then is the angle N A N' the *declination of the needle* at that place.

**261. Direction of the Needle.** The directions of these two meridians do not generally coincide, but the needle in most places points to the east or to the west of the true north, more or less according to the locality. Observations of the amount and the direction of this declination have been made in nearly all parts of the world. In the United States the declination in the Eastern States is westerly, and in the Western States is easterly, as will be given in detail, after the methods for determining the true meridian, and consequently the declinations, at any place have been explained.

### To determine the True Meridian.

**262. By Equal Shadows of the Sun.** On the south side of any level surface erect an upright staff, shown in horizontal projection at S. Two or three hours before noon, mark the extremity, A, of its shadow. Describe an arc of a circle with S, the foot of the staff, for center, and SA, the distance to the extremity of the shadow, for radius. About as many hours after noon as it had been before noon when the first mark was made, watch for the moment when the end of the shadow

Fig. 187.





touches the arc at another point, B. Bisect the arc A B at N. Draw S N, and it will be the true meridian, or north and south line required.

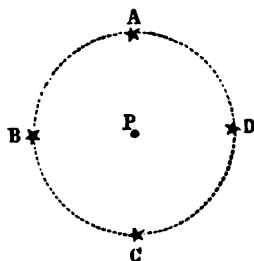
For greater accuracy, describe several arcs beforehand, mark the points in which each of them is touched by the shadow, bisect each, and adopt the average of all. The shadow will be better defined if a piece of tin with a hole through it be placed at the top of the staff, as a bright spot will thus be substituted for the less definite shadow. Nor need the staff be vertical, if from its summit a plumb-line be dropped to the ground, and the point which this strikes be adopted as the center of the arcs.

This method is a very good approximation, though perfectly correct only at the time of the solstices, about June 21st and December 22d. It was employed by the Romans in laying out cities.

To get the declination, set the compass at one end of the true meridian line thus obtained, sight to the other end of it, and take the bearing as of any ordinary line. The number of degrees in the reading will be the desired declination of the needle.

**263. By the North Star, when in the Meridian.** The north star, or pole star (called by astronomers *Alpha Ursæ Minoris*, or *Polaris*), is not situated precisely at the north pole of the heavens. If it were, the meridian could be at once determined by sighting to it, or placing the eye at some distance behind a plumb-line so that this line should hide the star. But the north star is about  $1\frac{1}{4}^{\circ}$  from the pole. Twice in twenty-four hours, however (more precisely, twenty-three hours fifty-six minutes), it is in the meridian, being then exactly above or below the pole, as at A and C in the figure. To know when it is so, is rendered easy by the aid of another star, easily identified, which at these times is almost exactly above or below the north star—i. e., situated in the same vertical plane. If, then, we watch for the moment at which a suspended plumb-line will cover both these stars, they will then be in the meridian.

FIG. 188.



The other star is in the well-known constellation of the Great Bear, called also the Plow, or the Dipper, or Charles's Wain.

FIG. 189.



FIG. 190.



Two of its five bright stars (the right-hand ones in Fig. 189) are known as the "Pointers," from their pointing near to the north star, thus assisting in finding it. The middle star in the tail or handle is the star which comes to the meridian at the same time with the north star, twice in twenty-four hours, as in Fig. 189 or 190. It is known as *Mizar*, or *Zeta Ursæ Majoris*.\*

To determine the meridian by this method, suspend a long plumb-line from some elevated point, such as a stick projecting from the highest window of a house suitably situated. The plumb-bob may pass into a pail of water to lessen its vibrations. South of this set up the compass, at such a distance from the plumb-line that neither of the stars will be seen above its highest point—i. e., in latitudes of  $40^\circ$  or  $50^\circ$ , not quite as far from the plumb-line as it is long. Or, instead of a compass, place a board on two stakes, so as to form a sort of bench, running east and west, and on it place one of the compass-sights, or anything having a small hole in it to look through. As the time approaches for the north star to be on the meridian (as taken from the table given below) place the compass, or the sight, so that, looking through it, the plumb-line shall seem to cover or hide the north star. As the star moves one way, move the eye and sight the other way, so as to constantly keep the star behind the plumb-line. At last *Mizar*, too, will be covered by the plumb-line. At that moment the eye and the

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\* The north pole is very nearly at the intersection of the line from *Polaris* to *Mizar*, and a perpendicular to this line from the small star seen to the left of it in Fig. 189.

plumb-line are (approximately) in the meridian. Fasten down the sight on the board till morning, or with the compass take the bearing at once, and the reading is the declination.

Instead of one plumb-line and a sight, two plumb-lines may be suspended at the end of a horizontal rod, turning on the top of a pole.

The line thus obtained points to the east of the true line when the north star is above Mizar, and *vice versa*. The north star is exactly in the meridian 0.85 of a minute after it has been in the same vertical plane with Mizar, and may be sighted to, after that interval of time, with perfect accuracy for 1895.

The interval between the time when Mizar and Polaris are on the same vertical circle and the time when Polaris is on the vertical circle through the north pole is increasing 0.35 of a minute a year, so that in 1900 the interval will be 2.6 minutes.

Another bright star, which is on the opposite side of the pole, and is known to astronomers as *Delta Cassiopeiæ*, also comes on the meridian nearly at the same time as the north star, and may be used in the same way as *Mizar* for finding the true meridian.

The interval between the time when *Delta Cassiopeiæ* and *Polaris* are on the same vertical circle and the time when *Polaris* is on the vertical circle through the north pole is 1.75 minutes for 1895, and is increasing 0.33 minute per year, so that in 1900 the interval will be 3.4 minutes.

**264.** The time \* at which the north star passes the meridian above and below the pole, for the first and fifteenth of each month, is given in the table in Art. 265 in astronomical time, the time being counted from zero at noon to twenty-four hours. The upper

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\* To calculate the time of the north star passing the meridian at its upper culmination: Find in the "American Ephemeris and Nautical Almanac" the right ascension of the star, and from it (increased by twenty-four hours if necessary to render the subtraction possible) subtract the right ascension of the sun at mean noon, or the sidereal time at mean noon, for the given day, as found in the "ephemeris of the sun" in the same almanac. From the remainder subtract the acceleration of sidereal on mean time corresponding to this remainder (3m. 56s. for 24 hours), and the new remainder is the required mean solar time of the upper passage of the star across the meridian, in "astronomical" reckoning, the astronomical day beginning at noon of the common civil day of the same date.

transit is the most convenient, since at the other transit Mizar is too high to be conveniently observed.

**265. By the North Star at its Extreme Elongation.\*** When the north star is at its greatest *apparent* angular distance east or west of the pole, as at B or D in Fig. 188, it is said to be at its extreme eastern or extreme western elongation. If it be observed at either of these times, the direction of the meridian can be easily obtained from the observation. The great advantage of this method over the preceding is that then the star's motion apparently ceases for a short time.

The north star, which is now about  $1^{\circ} 16'$  from the pole, was  $12^{\circ}$  distant from it when its place was first recorded. Its distance is now diminishing at the rate of about a third of a minute in a year, and will continue to do so till it approaches to within half a degree, when it will again recede. The brightest star in the northern hemisphere, *Alpha Lyræ*, will be the pole-star in about twelve thousand years, being then within about  $5^{\circ}$  of the pole, though now more than  $51^{\circ}$  distant from it.

The times of the elongations of Polaris is given in the following table, compiled from information furnished by the superintendent of the United States Coast and Geodetic Survey.

The time given in the table is astronomical time, in which the day begins at noon and runs twenty-four hours. The civil day begins at midnight, and is divided into two periods of twelve hours each, designated as A. M. and P. M.

The civil day begins twelve hours before the astronomical day, so that, for example; June 6th, 10 o'clock A. M., civil time, is June 5th, twenty-two hours astronomical time, and June 6th, 10 o'clock P. M., is June 6th, ten hours astronomical time.

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\* To calculate the times of the greatest elongation of the north star: Find in the "American Ephemeris and Nautical Almanac" its polar distance at the given time. Add the logarithm of its tangent to the logarithm of the tangent of the latitude of the place, and the sum will be the logarithm of the cosine of the hour angle before or after the culmination. Reduce the space to time; correct for sidereal acceleration (8m. 56s. for 24 hours) and subtract the result from the time of the star's passing the meridian on that day, to get the time of the eastern elongation, or add it to get the western.

# THE DECLINATION OF THE MAGNETIC NEEDLE. 169

APPROXIMATE LOCAL MEAN (ASTRONOMICAL) TIMES OF THE CULMINATIONS  
AND ELONGATIONS OF POLARIS IN THE YEAR 1895.

[Computed for latitude + 40° north, and longitude 6° west from Greenwich.]

| DATE.            | East elonga-<br>tion. | Upper cul-<br>mination. | West elonga-<br>tion. | Lower cul-<br>mination. |
|------------------|-----------------------|-------------------------|-----------------------|-------------------------|
|                  | H. M.                 | H. M.                   | H. M.                 | H. M.                   |
| January 1.....   | 0 39·8                | 6 34·7                  | 12 29·4               | 18 32·6                 |
| “ 15.....        | 23 40·6               | 5 39·4                  | 11 34·1               | 17 37·3                 |
| February 1.....  | 22 33·4               | 4 32·3                  | 10 27·0               | 16 30·2                 |
| “ 15.....        | 21 38·2               | 3 37·1                  | 9 31·8                | 15 34·9                 |
| March 1.....     | 20 43·0               | 2 41·8                  | 8 36·5                | 14 39·7                 |
| “ 15.....        | 19 47·9               | 1 46·7                  | 7 41·4                | 13 44·7                 |
| April 1.....     | 18 40·9               | 0 39·7                  | 6 34·4                | 12 37·7                 |
| “ 15.....        | 17 45·9               | 23 40·8                 | 5 39·4                | 11 42·7                 |
| May 1.....       | 16 43·1               | 22 38·0                 | 4 36·6                | 10 39·8                 |
| “ 15.....        | 15 48·2               | 21 43·0                 | 3 41·7                | 9 44·9                  |
| June 1.....      | 14 41·5               | 20 36·4                 | 2 35·0                | 8 38·3                  |
| “ 15.....        | 13 46·6               | 19 41·6                 | 1 40·1                | 7 43·4                  |
| July 1.....      | 12 44·0               | 18 38·9                 | 0 37·5                | 6 40·8                  |
| “ 15.....        | 11 49·1               | 17 44·1                 | 23 38·7               | 5 45·9                  |
| August 1.....    | 10 42·6               | 16 37·6                 | 22 32·2               | 4 39·4                  |
| “ 15.....        | 9 47·7                | 15 42·7                 | 21 37·3               | 3 44·4                  |
| September 1..... | 8 41·1                | 14 36·1                 | 20 30·6               | 2 37·9                  |
| “ 15.....        | 7 46·1                | 13 41·2                 | 19 35·8               | 1 43·0                  |
| October 1.....   | 6 43·4                | 12 38·4                 | 18 33·0               | 0 40·2                  |
| “ 15.....        | 5 48·4                | 11 43·4                 | 17 38·0               | 23 41·3                 |
| November 1.....  | 4 41·6                | 10 36·6                 | 16 31·2               | 22 34·4                 |
| “ 15.....        | 3 46·4                | 9 41·5                  | 15 36·0               | 21 39·1                 |
| December 1.....  | 2 43·4                | 8 38·4                  | 14 33·0               | 20 36·2                 |
| “ 15.....        | 1 48·1                | 7 43·2                  | 13 37·7               | 19 40·9                 |

For any day of the month other than the first and fifteenth, subtract 3·94 minutes for every day between it and the preceding tabular day, or add 3·94 minutes for every day between it and the succeeding tabular day. For use at other times and places than those for which the table was computed, the following corrections are necessary:

For any year after 1895 add 0·25 minute for each additional year. This will be correct for the first year after leap year. Besides this correction, for the second year after leap year, add 0·9 minute; for the third year, 1·7 minutes; for leap year before March 1st, add 2·6 minutes; and on and after March 1st, subtract 1·2 minutes.

For other longitudes than six hours west from Greenwich, add 0.16 minute for each hour east, or subtract 0.16 minute for each hour west.

For other latitudes than  $40^\circ$  north, add to the time of west elongation 0.13 minute for every degree north of  $40^\circ$ , and subtract 0.13 minute for every degree south of  $40^\circ$ .

When "standard" time is used, it should be noted that local time will differ from standard time four minutes for each degree east or west of the meridian of the standard time used.

**266. Observations.** Knowing from the preceding table the hour and minute of the extreme elongation on any day, a little before that time suspend a plumb-line, precisely as in Art. 263, and place yourself south of it as there directed. As the north star moves one way, move your eye the other, so that the plumb-line shall continually seem to cover the star. At last the star will appear to stop moving for a time and then begin to move backward. Fix the sight on the board (or the compass, etc.) in the position in which it was when the star ceased moving; for the star was then at its extreme apparent elongation, east or west, as the case may be.

The eastern elongations from October to March, and the western elongations from April to September, occurring in the daytime, they will generally not be visible except with the aid of a powerful telescope.

**267. Azimuths.** The angle which the line from the eye to the plumb-line makes with the true meridian—i. e., the angle between the meridian plane and the vertical plane passing through the eye and the star—is called the *Azimuth* of the star. It is given in the following table for different latitudes, and for a number of years to come. For the intermediate latitudes it can be obtained by a simple proportion.\*

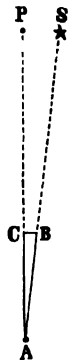
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\* To calculate this azimuth: From the logarithm of the sine of the polar distance of the star, subtract the logarithm of the cosine of the latitude of the place; the remainder will be the logarithm of the sine of the angle required. The polar distance can be obtained as directed in the last note.

AZIMUTHS (BEARINGS) OF THE NORTH STAR (POLARIS) AT EASTERN AND WESTERN ELONGATIONS.

| Lat. | 1893.  | 1896.  | 1897.  | 1898.  | 1899.  | 1900.  | 1901.  | 1902.  | 1903.  | 1904.  | 1905.  | 1906.  | 1907.  | 1908.  | 1909.  | 1910.  |
|------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 25°  | 1 22-9 | 1 22-5 | 1 22-2 | 1 21-8 | 1 21-5 | 1 21-2 | 1 20-8 | 1 20-5 | 1 20-1 | 1 19-8 | 1 19-4 | 1 19-1 | 1 18-7 | 1 18-4 | 1 18-1 | 1 17-7 |
| 26°  | 23-6   | 23-2   | 22-9   | 22-5   | 22-2   | 21-8   | 21-5   | 21-1   | 20-8   | 20-5   | 20-1   | 19-8   | 19-4   | 19-1   | 18-7   | 18-4   |
| 27°  | 24-3   | 24-0   | 23-6   | 23-3   | 22-9   | 22-5   | 22-2   | 21-9   | 21-5   | 21-2   | 20-8   | 20-5   | 20-1   | 19-8   | 19-4   | 19-1   |
| 28°  | 25-1   | 24-7   | 24-4   | 24-0   | 23-7   | 23-3   | 23-0   | 22-6   | 22-3   | 21-9   | 21-6   | 21-3   | 20-9   | 20-5   | 20-1   | 19-8   |
| 29°  | 25-9   | 25-5   | 25-2   | 24-8   | 24-5   | 24-1   | 23-8   | 23-4   | 23-0   | 22-7   | 22-4   | 22-1   | 21-7   | 21-3   | 20-9   | 20-5   |
| 30°  | 1 26-8 | 1 26-4 | 1 26-0 | 1 25-7 | 1 25-3 | 1 24-9 | 1 24-6 | 1 24-3 | 1 23-9 | 1 23-5 | 1 23-1 | 1 22-8 | 1 22-4 | 1 22-1 | 1 21-7 | 1 21-3 |
| 31°  | 27-6   | 27-3   | 26-9   | 26-5   | 26-2   | 25-8   | 25-5   | 25-1   | 24-7   | 24-4   | 24-0   | 23-6   | 23-2   | 22-9   | 22-5   | 22-1   |
| 32°  | 28-6   | 28-2   | 27-9   | 27-5   | 27-1   | 26-7   | 26-4   | 26-0   | 25-6   | 25-3   | 24-9   | 24-5   | 24-1   | 23-8   | 23-4   | 23-1   |
| 33°  | 29-6   | 29-2   | 28-8   | 28-5   | 28-1   | 27-7   | 27-3   | 27-0   | 26-6   | 26-2   | 25-9   | 25-5   | 25-1   | 24-7   | 24-3   | 24-0   |
| 34°  | 30-6   | 30-2   | 29-9   | 29-5   | 29-1   | 28-7   | 28-4   | 28-0   | 27-6   | 27-2   | 26-9   | 26-5   | 26-1   | 25-7   | 25-3   | 25-0   |
| 35°  | 1 31-7 | 1 31-3 | 1 30-9 | 1 30-6 | 1 30-2 | 1 29-8 | 1 29-4 | 1 29-0 | 1 28-7 | 1 28-3 | 1 27-9 | 1 27-5 | 1 27-1 | 1 26-8 | 1 26-4 | 1 26-0 |
| 36°  | 32-9   | 32-5   | 32-1   | 31-7   | 31-3   | 30-9   | 30-5   | 30-1   | 29-8   | 29-4   | 29-0   | 28-6   | 28-2   | 27-9   | 27-5   | 27-1   |
| 37°  | 34-1   | 33-7   | 33-3   | 32-9   | 32-5   | 32-1   | 31-7   | 31-3   | 30-9   | 30-5   | 30-1   | 29-7   | 29-3   | 29-0   | 28-6   | 28-2   |
| 38°  | 35-3   | 35-0   | 34-6   | 34-2   | 33-8   | 33-4   | 33-0   | 32-6   | 32-2   | 31-8   | 31-4   | 31-0   | 30-6   | 30-2   | 29-8   | 29-4   |
| 39°  | 36-7   | 36-3   | 35-9   | 35-5   | 35-1   | 34-7   | 34-3   | 33-9   | 33-5   | 33-1   | 32-7   | 32-3   | 31-8   | 31-4   | 31-0   | 30-6   |
| 40°  | 1 38-1 | 1 37-7 | 1 37-2 | 1 36-8 | 1 36-4 | 1 36-0 | 1 35-6 | 1 35-2 | 1 34-8 | 1 34-4 | 1 34-0 | 1 33-6 | 1 33-2 | 1 32-8 | 1 32-4 | 1 32-0 |
| 41°  | 39-6   | 39-1   | 38-7   | 38-3   | 37-9   | 37-5   | 37-1   | 36-7   | 36-2   | 35-8   | 35-4   | 35-0   | 34-6   | 34-2   | 33-8   | 33-4   |
| 42°  | 41-1   | 40-7   | 40-3   | 39-8   | 39-4   | 39-0   | 38-6   | 38-2   | 37-7   | 37-3   | 36-9   | 36-5   | 36-0   | 35-6   | 35-2   | 34-8   |
| 43°  | 42-7   | 42-3   | 41-9   | 41-4   | 41-0   | 40-6   | 40-2   | 39-8   | 39-3   | 38-9   | 38-5   | 38-1   | 37-6   | 37-2   | 36-8   | 36-3   |
| 44°  | 44-4   | 44-0   | 43-6   | 43-1   | 42-7   | 42-3   | 41-8   | 41-4   | 41-0   | 40-5   | 40-1   | 39-7   | 39-2   | 38-8   | 38-4   | 37-9   |
| 45°  | 1 46-2 | 1 45-8 | 1 45-4 | 1 44-9 | 1 44-5 | 1 44-0 | 1 43-6 | 1 43-2 | 1 42-7 | 1 42-3 | 1 41-8 | 1 41-4 | 1 40-9 | 1 40-5 | 1 40-1 | 1 39-6 |
| 46°  | 48-2   | 47-7   | 47-2   | 46-8   | 46-3   | 45-9   | 45-5   | 45-0   | 44-6   | 44-2   | 43-7   | 43-2   | 42-7   | 42-3   | 41-9   | 41-4   |
| 47°  | 50-2   | 49-7   | 49-2   | 48-8   | 48-3   | 47-9   | 47-4   | 46-9   | 46-5   | 46-0   | 45-6   | 45-1   | 44-6   | 44-2   | 43-7   | 43-3   |
| 48°  | 52-3   | 51-8   | 51-3   | 50-9   | 50-4   | 49-9   | 49-5   | 49-0   | 48-6   | 48-1   | 47-7   | 47-2   | 46-8   | 46-3   | 45-8   | 45-3   |
| 49°  | 54-5   | 54-1   | 53-6   | 53-1   | 52-6   | 52-1   | 51-7   | 51-2   | 50-7   | 50-2   | 49-8   | 49-3   | 48-8   | 48-4   | 47-9   | 47-4   |
| 50°  | 1 56-9 | 1 56-4 | 1 55-9 | 1 55-4 | 1 54-9 | 1 54-4 | 1 54-0 | 1 53-5 | 1 53-0 | 1 52-5 | 1 52-0 | 1 51-5 | 1 51-0 | 1 50-6 | 1 50-1 | 1 49-6 |
| 51°  | 59-4   | 58-9   | 58-4   | 57-9   | 57-4   | 56-9   | 56-4   | 55-9   | 55-4   | 54-9   | 54-4   | 54-0   | 53-5   | 53-0   | 52-5   | 52-0   |
| 52°  | 2 02-0 | 2 01-5 | 2 01-0 | 2 00-5 | 2 00-0 | 59-5   | 59-0   | 58-5   | 58-0   | 57-5   | 57-0   | 56-4   | 55-9   | 55-4   | 54-9   | 54-4   |
| 53°  | 04-8   | 04-3   | 03-8   | 03-2   | 02-7   | 02-2   | 01-7   | 01-2   | 00-7   | 00-2   | 59-6   | 59-1   | 58-6   | 58-1   | 57-6   | 57-1   |
| 54°  | 07-8   | 07-3   | 06-7   | 06-2   | 05-6   | 05-1   | 04-6   | 04-1   | 03-5   | 03-0   | 2 02-5 | 2 02-0 | 2 01-5 | 2 01-0 | 2 00-9 | 2 00-4 |
| 55°  | 2 11-0 | 2 10-5 | 2 09-9 | 2 09-4 | 2 08-8 | 2 08-3 | 2 07-8 | 2 07-2 | 2 06-6 | 2 06-1 | 2 05-6 | 2 05-0 | 2 04-4 | 2 03-9 | 2 03-4 | 2 02-8 |

FIG. 191.



**268. Setting out a Meridian.** When two points in the direction of the north star at its extreme elongation have been obtained, as in Art. 266, the true meridian can be found thus: Let A and B be the two points. Multiply the natural tangent of the azimuth given in the table by the distance A B. The product will be the length of a line which is to be set off from B, perpendicular to A B, to some point C. A and C will then be points in the true meridian. This operation may be postponed till morning.

If the directions of both the extreme eastern and extreme western elongations be set out, the line lying midway between them will be the true meridian.

**269. Determining the Declination.** The declination would, of course, be given by taking the bearing of the meridian thus obtained, but it can also be determined by taking the bearing of the star at the time of the extreme elongation, and applying the following rules:

When the azimuth of the star and its magnetic bearing are one east and the other west, the sum of the two is the magnetic declination, which is of the same name as the azimuth—i. e., east, if that be east, and west, if it be west.

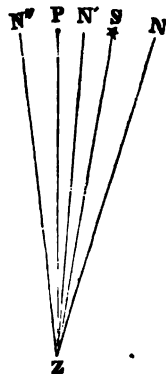
When the azimuth of the star and its magnetic bearing are both east or both west, their difference is the declination, which will be of the same name as the azimuth and bearing, if the azimuth be the greater of the two, or of the contrary name if the azimuth be the smaller.

All these cases are presented together in the figure, in which P is the north pole, Z the place of the observer, Z P the true meridian, S the star at its greatest eastern elongation, and Z N, Z N', Z N'' various supposed directions of the needle.

Call the azimuth of the star—i. e., the angle P Z S— $2^\circ$  east.

Suppose the needle to point to N, and the

FIG. 192.





bearing of the star—i. e., S Z N—to be  $5^\circ$  west of magnetic north. The declination P Z N will evidently be  $7^\circ$  east of true north.

Suppose the needle to point to N', and the bearing of the star—i. e., N' Z S—to be  $1\frac{1}{2}^\circ$  east of magnetic north. The declination will be  $\frac{1}{2}^\circ$  east of true north, and of the same name as the azimuth, because that is greater than the bearing.

Suppose the needle to point to N', and the bearing of the star—i. e., N' Z S—to be  $10^\circ$  east of magnetic north. The declination will be  $8^\circ$  west of true north, of the contrary name to the azimuth, because that is the smaller of the two.\*

If the star were on the other side of the pole, the rules would apply likewise.

**270. Other Methods.** Many other methods of determining the true meridian are employed; such as by equal altitudes and azimuths of the sun, or of a star; by one azimuth, knowing the time; by observations of circumpolar stars at equal times before and after their culmination, or before and after their greatest elongation, etc.

All these methods, however, require some degree of astronomical knowledge; and those which have been explained are abundantly sufficient for all the purposes of the ordinary land-surveyor.

“Burt's Solar Compass” is an instrument by which, “when adjusted for the sun's declination and the latitude of the place, the azimuth of any line from the true north and south can be read off, and the difference between it and the bearing by the compass will then be the variation.” (See Arts. 463 to 483.)

**271. Magnetic Declination in the United States.** The declination in any part of the United States can be approximately obtained by mere inspection of the map at the beginning of this volume.† Through all the places at which the needle, in 1890, pointed to the true north, a line is drawn on the map, and called

\* Algebraically, always subtract the bearing from the azimuth, and give the remainder its proper resulting algebraic sign. It will be the declination; east if *plus*, and west if *minus*. Thus, in the first case above, the declination =  $+2^\circ - (-5^\circ) = +7^\circ = 7^\circ$  east. In the second case, the declination =  $+2^\circ - (+1\frac{1}{2}^\circ) = +\frac{1}{2}^\circ = \frac{1}{2}^\circ$  east. In the third case, the declination =  $+2^\circ - (+10^\circ) = -8^\circ = 8^\circ$  west.

† Copied from “United States Coast and Geodetic Survey Report,” 1889.

the *line of no declination*. It will be seen to pass a little east of Charleston, South Carolina, thence in a northwesterly direction, passing near Columbus, Ohio, through the west end of Lake Erie, passing near Lansing, Michigan, and up through the east end of Lake Superior. This line is now slowly moving westward.

At all places situated to the east of this line (including the New England States, New York, New Jersey, Delaware, Maryland, Pennsylvania, most of Virginia, and the east half of North Carolina and Ohio) the declination is westerly—i. e., the north end of the needle points to the west of the true north. At all places situated to the west of this line (including the Western and Southern States) the declination is easterly—i. e., the north end of the needle points to the east of the true north. This declination increases in proportion to the distance of the place on either side of the line of no variation, reaching  $23^{\circ}$  of easterly declination in Washington Territory, and  $21^{\circ}$  of westerly declination in Maine.

Isogonics, or *lines of equal declination*, are lines drawn through all the places which have the same declination. On the map they are drawn for each degree. All the places situated on the line marked  $5^{\circ}$ , east or west, have  $5^{\circ}$  declination; those on the  $10^{\circ}$  line have  $10^{\circ}$  declination, etc. The declination at the intermediate places can be approximately estimated by the eye. These lines all refer to 1885.

The sign + indicates west declination, and the sign — indicates east declination. The annual change in the secular variation for stations is given in minutes and decimals, a + indicating increasing west declination or decreasing east declination, and a — sign indicating increasing east and decreasing west declination.

**272. To correct Magnetic Bearings.** The declination at any place and time being known, the magnetic bearings taken there and then may be reduced to their true bearings by these rules:

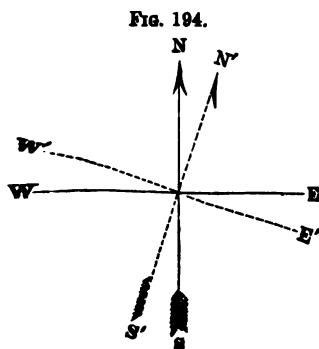
**RULE 1.** *When the declination is west*, as it is in the Northeastern States, the true bearing will be the *sum* of the declination, and a bearing which is north and west, or south and east; and the *difference* of the declination and a bearing which is north and east, or south and west. To apply this to the cardinal points, a

north bearing must be called N.  $0^{\circ}$  west, an east bearing N.  $90^{\circ}$  E., a south bearing S.  $0^{\circ}$  E., and a west bearing S.  $90^{\circ}$  W. ; counting around from N' to N, in the figure, and so onward, "with the sun."

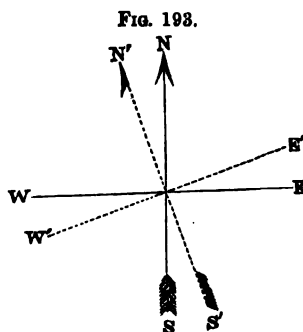
The reasons for these corrections are apparent from the figure, in which the dotted lines and the accented letters represent the direction of the needle, and the full lines and the unaccented letters represent the true north and south and east and west lines.

When the sum of the declination and the bearing is directed to be taken, and comes to more than  $90^{\circ}$ , the supplement of the sum is to be taken, and the first letter changed. When the difference is directed to be taken, and the declination is greater than the bearing, the last letter must be changed. A diagram of the case will remove all doubts. Examples of all these cases are given below for a declination of  $8^{\circ}$  west:

| MAGNETIC BEARINGS. | TRUE BEARINGS.     | MAGNETIC BEARINGS. | TRUE BEARINGS.     |
|--------------------|--------------------|--------------------|--------------------|
| North.             | N. $8^{\circ}$ W.  | South.             | S. $8^{\circ}$ E.  |
| N. $1^{\circ}$ E.  | N. $7^{\circ}$ W.  | S. $2^{\circ}$ W.  | S. $6^{\circ}$ E.  |
| N. $40^{\circ}$ E. | N. $32^{\circ}$ E. | S. $60^{\circ}$ W. | S. $52^{\circ}$ W. |
| East.              | N. $82^{\circ}$ E. | West.              | S. $82^{\circ}$ W. |
| S. $50^{\circ}$ E. | S. $58^{\circ}$ E. | N. $70^{\circ}$ W. | N. $78^{\circ}$ W. |
| S. $89^{\circ}$ E. | N. $83^{\circ}$ E. | N. $83^{\circ}$ W. | S. $89^{\circ}$ W. |



RULE 2. When the declination is east, as in the Western and Southern States, the preceding directions must be exactly reversed — i. e., the true bearing will be the *difference* of the declination, and a bearing which is north and west or south and east; and the *sum* of the declination and a bearing which is north and east or south and west. A north bearing



must be called N.  $0^{\circ}$  E., a west bearing N.  $90^{\circ}$  W., a south bearing S.  $0^{\circ}$  W., and an east bearing S.  $90^{\circ}$  E., counting from N' to N, and so onward, "against the sun." The reasons for these rules are seen in the figure. Examples are given below for a declination of  $5^{\circ}$  E.:

| MAGNETIC<br>BEARINGS. | TRUE<br>BEARINGS.  | MAGNETIC<br>BEARINGS. | TRUE<br>BEARINGS.  |
|-----------------------|--------------------|-----------------------|--------------------|
| North.                | N. $5^{\circ}$ E.  | South.                | S. $5^{\circ}$ W.  |
| N. $40^{\circ}$ E.    | N. $45^{\circ}$ E. | S. $60^{\circ}$ W.    | S. $65^{\circ}$ W. |
| N. $80^{\circ}$ E.    | N. $85^{\circ}$ E. | S. $87^{\circ}$ W.    | N. $88^{\circ}$ W. |
| East.                 | S. $85^{\circ}$ E. | West.                 | N. $85^{\circ}$ W. |
| S. $1^{\circ}$ E.     | S. $4^{\circ}$ W.  | N. $70^{\circ}$ W.    | N. $65^{\circ}$ W. |
| S. $50^{\circ}$ E.    | S. $45^{\circ}$ E. | N. $2^{\circ}$ W.     | N. $3^{\circ}$ E.  |

**273. To survey a Line with True Bearings.** The compass may be set, or adjusted, by means of the vernier, according to the declination in any place, so that the bearings of any lines then taken with it will be their true bearings. To effect this, turn aside the compass-plate by means of the tangent-screw which moves the vernier a number of degrees equal to the declination, moving the south end of the compass-box to the *right* (the north end being supposed to go ahead) if the declination be westerly, and *vice versa*; for that moves the north end of the compass-box in the contrary direction, and thus makes a line which, before was N. by the needle, now read, as it should truly, north, so many degrees west if the declination was west; and similarly in the reverse case.

#### *Variations of Magnetic Declination.*

**274.** The *variations* of the declination are of more practical importance than its absolute amount. The four kinds of most importance are: Irregular, diurnal, annual, and secular.

**275. Irregular Variation.** The needle is subject to sudden and violent changes, which have no known law. They are sometimes coincident with a thunder-storm, or an aurora borealis

(during which changes of nearly  $1^{\circ}$  in one minute,  $2\frac{1}{4}^{\circ}$  in eight minutes, and  $10^{\circ}$  in one night, have been observed), but often have no apparent cause, except an otherwise invisible "magnetic storm."

**276. The Diurnal Variation.** On continuing observations of the direction of the needle throughout an entire day, it will be found, in the northern hemisphere, that the north end of the needle moves westward from about 8 A. M. till about  $1\frac{1}{4}$  P. M., over an arc of from  $5'$  to  $15'$ , and then gradually returns to its former position. A similar but smaller movement takes place during the night. At Philadelphia, the most easterly deflection of the needle is at about 8 A. M. The north end of the needle then begins to move toward the west, crossing the mean magnetic meridian about  $10\frac{1}{2}$  A. M., and reaching its extreme western position about  $1\frac{1}{4}$  P. M. The total angular range averages about  $8'$ , being  $10\frac{1}{2}'$  in August, and  $6'$  in November.\* The period of this change being a day, it is called the *Diurnal Variation*. Its effect on the permanent variation is necessarily to cause it, in places where it is west, to attain its maximum at about  $1\frac{1}{4}$  P. M., and its minimum at about 8 A. M.; and the reverse where the declination is east.

This diurnal variation adds a new element to the inaccuracies of the compass, since the bearings of any line taken on the same day, at a few hours' interval, might vary a quarter of a degree, which would cause a deviation of the end of the line, amounting to nearly half a link at the end of a chain, and to 35 links, or 23 feet, at the end of a mile. The hour of the day at which any important bearing is taken should therefore be noted.

**277. The Annual Variation.** If the observations be continued throughout an entire year, it will be found that the diurnal changes vary with the seasons, being greater in summer than in winter. The period of this variation being a year, it is called the *Annual Variation*.

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\* For table of hourly variation of the declination, see "Report of United States Coast and Geodetic Survey," 1888.

**278. The Secular Variation.** When accurate observations on the declination of the needle in the same place are continued for several years, it is found that there is a continual and tolerably regular increase or decrease of the declination, continuing to proceed in the same direction for so long a period, that it may be called the *Secular Variation* of the declination.

The most ancient observations are those taken in Paris. In the year 1541 the needle pointed  $7^{\circ}$  east of north; in 1580 the declination had increased to  $11\frac{1}{2}^{\circ}$  east, being its maximum; the needle then began to move westward, and in 1666 it had returned to the meridian; the declination then became west, and continued to increase till in 1814 it attained its maximum, being  $22^{\circ} 34'$  west of north. It is now decreasing. January 1, 1879, it was  $16^{\circ} 56'$  west, and it is now about  $15^{\circ}$  west.

In this country the north end of the needle was moving eastward at the earliest recorded observations, and continued to do so till about the year 1810 (variously recorded as from 1765 to 1819), when it began to move westward, which it has ever since continued to do. Thus, in Boston, from 1700 to 1800, the declination changed from  $10^{\circ}$  west to  $7^{\circ}$  west, and, from 1800 to 1895, it changed from  $7^{\circ}$  west to  $12^{\circ}$  west.

In Philadelphia, from 1701 to 1802, the declination changed from  $8^{\circ} 30'$  west to  $2^{\circ}$  west, and, from 1802 to 1890, it changed from  $2^{\circ}$  west to  $7^{\circ}$  west.

For extensive tables of the declination of the needle, in various parts of the United States, see "Report of the United States Coast and Geodetic Survey," 1888, Appendix VII. The secular variation is noted on the declination-map in this volume.

An examination of the above-mentioned tables will show that the secular variation often differs greatly in places not far apart, and that it varies in amount at the same place from year to year.

**278<sup>1</sup>. Minor Variations in Declination.** There are some minor variations in the declination of the needle which depend upon the position of the moon and its phases; upon the revolution of the

sun on its axis; and upon the sun-spot cycle. These variations however, need not be taken into consideration for compass surveying. For a discussion of these, see Coast and Geodetic Survey Report, 1890, Appendix IX.

Those who desire to investigate the variations of the magnetic needle, and, in general, the phenomena of terrestrial magnetism, will find a description of the instruments used and the methods employed in the Coast and Geodetic Survey Report for 1881, Appendix VIII.

TABLE OF ANNUAL CHANGES IN DECLINATION.

| LOCALITY.                 | ANNUAL CHANGE. |       |       |
|---------------------------|----------------|-------|-------|
|                           | 1885.          | 1890. | 1895. |
| Eastport, Me.....         | +1·8'          | +0·8' | +0·2' |
| Boston, Mass.....         | +2·6           | +2·2  | +1·9  |
| New York City, N. Y.....  | +3·7           | +3·8  | +3·8  |
| Philadelphia, Pa.....     | +4·7           | +4·4  | +4·4  |
| Charleston, S. C.....     | +3·2           | +2·9  | +2·5  |
| Cleveland, Ohio.....      | +2·8           | +2·6  | +2·4  |
| Nashville, Tenn.....      | +4·4           | +4·6  | +4·7  |
| New Orleans, La.....      | +4·1           | +4·2  | +4·3  |
| Chicago, Ill.....         | +3·7           | +3·8  | +3·7  |
| Denver, Col.....          | +2·8           | +3·1  | +3·4  |
| Salt Lake City, Utah..... | +1·8           | +2·5  | +3·2  |
| San Francisco, Cal.....   | -0·4           | -0·2  | -0·1  |

**279. Determination of the Change, by Interpolation.** To determine the change at any place and for any interval not found in the recorded observations, an approximation, sufficient for most purposes of the surveyor, may be obtained by interpolation (by a simple proportion) between the places given on the map, assuming the movements to have been uniform between the given dates, and also assuming the change at any place not found on the map to have been intermediate between those of the lines of equal variation, which pass through the places of recorded observations on each side of it, and to have been in the ratio of its respective distances from those two lines; for example, taking their arithmetical mean, if the required place is midway between them; if it be twice as near one as the other, dividing the sum of twice the change of the nearest line, and once the change of the other, by three; and so in other cases—i. e., giving the change at each place, a

"weight" inversely as its distance from the place at which the change is to be found.

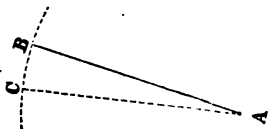
**280. Determination of the Change by Old Lines.** When the former bearing of any old line, such as a farm-fence, etc., is recorded, the change in the declination from the date of the original observation to the present time can be at once found by setting the compass at one end of the line and sighting to the other. The difference of the two bearings is the required change.

If one end of the old line can not be seen from the other, as is often the case when the line is fixed only by a "corner" at each end of it, proceed thus: Run a line from one corner with the old bearing and with its distance. Measure the distance from the end of this line to the other corner, to which it will be opposite. Multiply this distance by 57.3, and divide by the length of the line. The quotient will be the change of variation in degrees.\*

For example, a line 63 chains long, in 1827 had a bearing of north  $1^\circ$  east. In 1847 a trial line was run from one end of the former line with the same bearing and distance, and its other end was found to be 125 links to the west of the true corner. The change of declination was therefore  $\frac{1.25 \times 57.3}{63} = 1.137^\circ = 1^\circ 8'$  westerly.

**281. Effects of the Secular Change.** These are exceedingly important in the resurvey of farms by the bearings recorded in old deeds. Let  $SN$  denote the direction of the needle at the time of the original survey, and  $S'N'$  its direction at the time of the resurvey, a number of years later. Suppose the change to have been

FIG. 195.

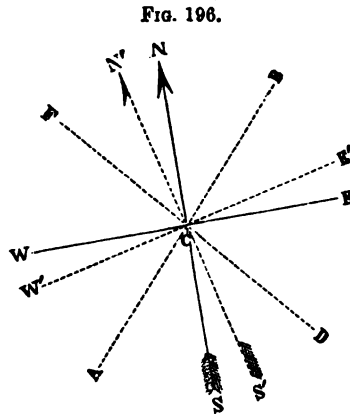


\* Let  $AB$  be the original line;  $AC$  the trial line, and  $BC$  the distance between their extremities.  $AB$  and  $AC$  may be regarded as radii of a circle and  $BC$  as a chord of the arc which subtends their angle. Assuming the chord and arc to coincide (which they will, nearly, for small angles), we have this proportion: Whole circumference : arc  $BC :: 360^\circ : BAC$  : or,  $2 \times AC \times 3.1416 : BC :: 360^\circ :$

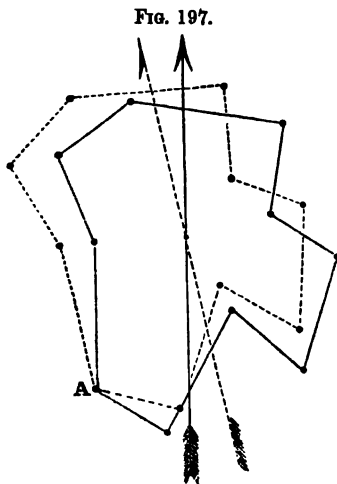
$BAC$ , whence  $BAC = \frac{BC}{AB} \times 57.3$ ; or, more precisely,  $57.29578$ .



3°, the needle pointing so much farther to the west of north. The line SN, which before was due north and south by the needle, will now bear N. 3° E. and S. 3° W. ; the line AB, which before was N. 40° E. will now bear N. 43° E. ; the line DF, which before was N. 40° W., will now bear N. 37° W., and the line WE, which before was due east and west, will now bear S. 87° E. and N. 87° W. Any line is similarly changed. The proof of this is apparent on inspecting the figure.



Suppose, now, that a surveyor, ignorant or neglectful of this change, should attempt to run out a farm by the old bearings of the deed, none of the old fences or corners remaining. The full



lines in the figure represent the original bounds of the farm, and the dotted lines those of the *new* piece of land which, starting from A, he would unwittingly run out. It would be of the same size and the same shape as the true one, but it would be in the wrong place. None of its lines would agree with the true ones, and in some places it would encroach on one neighbor, and in other places would leave a gore, which belongs to it, between itself and another neighbor. Yet this is often done, and is the source of a

great part of the litigation among farmers respecting their "lines."

**282. To run out Old Lines.** To succeed in retracing old lines, proper allowance must be made for the change in the variation

since the date of the original survey. That date must first be accurately ascertained ; for the survey may be much older than the deed, into which its bearings may have been copied from an older one. The amount and direction of the change is then to be ascertained by the methods of Art. 279 or 280. The bearings may then be corrected by the following RULES :

When the north end of the needle has been moving westerly, the present bearings will be the *sums* of the change and the old bearings which were northeasterly or southwesterly, and the *differences* of the change and the old bearings which were northwesterly or southeasterly.

If the change has been *easterly*, reverse the preceding rules, subtracting where it is directed to add, and adding where it is directed to subtract.

Run out the lines with the bearings thus corrected.

It will be noticed that the process is precisely the reverse of that in Art. 272. The rules, there given in more detail, may therefore be used : RULE 1. "When the declination is west," being employed when the *change* has been a movement of the N. end of the needle to the east ; and RULE 2, "when the declination is east," being employed when the N. end of the needle has been moving to the west.

If the compass has a vernier, it can be set for the change, once for all, precisely as directed in Art. 273, and then the courses can be run out as given in the deed, the correction being made by the instrument.

**Example.** The following is a remarkable case which came before the Supreme Court of New York : The north line of a large estate was fixed by a royal grant, dated in 1704, as a due east and west line. It was run out in 1715, by a surveyor, whom we will call Mr. A. It was again surveyed in 1765, by Mr. B., who ran a course N.  $87^{\circ} 30'$  E. It was run out for a third time in 1789, by Mr. C., who adopted the course N.  $86^{\circ} 18'$  E. In 1845 it was surveyed for the fourth time by Mr. D., with a course of N.  $88^{\circ} 30'$  E. He found old "corners," and "blazes" of a former survey, on his line. They are also found on another line, south of his. Which

of the preceding courses were correct, and where does the true line lie ?

The question was investigated as follows : There were no old records of variation at the precise locality, but it lies between the lines of equal variation which pass through New York and Boston, its distance from the Boston line being about twice its distance from the New York line. The records of those two cities (referred to in Art. 278) could therefore be used in the manner explained in Art. 279. For the later dates, observations at New Haven could serve as a check. Combining all these, the author inferred the variation at the desired place to have been as follows :

In 1715, variation  $8^{\circ} 02'$  west.

In 1765,       “      $5^{\circ} 32'$      “               Decrease since 1715,  $2^{\circ} 30'$ .

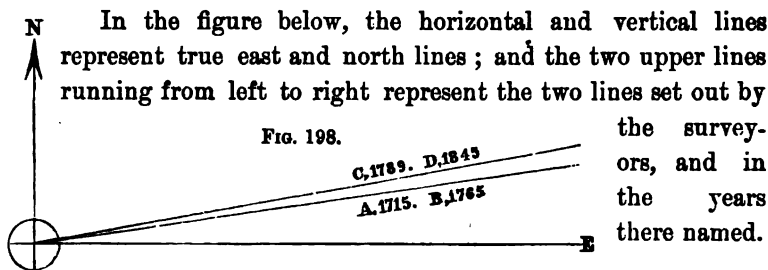
In 1789,       “      $5^{\circ} 05'$      “               Decrease since 1765,  $0^{\circ} 27'$ .

In 1845,       “      $7^{\circ} 23'$      “               Increase since 1789,  $2^{\circ} 18'$ .

We are now prepared to examine the correctness of the allowances made by the old surveyors.

The course run by Mr. B. in 1765, N.  $87^{\circ} 30'$  E., made an allowance of  $2^{\circ} 30'$  as the decrease of variation, agreeing precisely with our calculation. The course of Mr. C. in 1789, N.  $86^{\circ} 18'$  E., allowed a change of  $1^{\circ} 12'$ , which was wrong by our calculation, which gives only about  $27'$ , and was deduced from three different records. Mr. D., in 1845, ran a course of N.  $88^{\circ} 30'$  E., calling the increase of variation since 1789,  $2^{\circ} 12'$ . Our estimate was  $2^{\circ} 18'$ , the difference being comparatively small. Our conclusion, then, is this : The second surveyor retraced correctly the line of the first ; the third surveyor ran out a *new* and incorrect line ; and the fourth surveyor correctly retraced the line of the third, and found his marks, but this line was wrong originally, and therefore wrong now. All the surveyors ran their lines on the supposition that the original “due east and west line” meant east and west as the needle pointed at the time of the original survey.

The preponderance of the testimony as to old landmarks agreed with the results of the above reasoning, and the decision of the court was in accordance therewith.



**283. Remedy for the Evils of the Secular Change.** The only complete remedy for the disputes, and the uncertainty of bounds, resulting from the continued change in the declination, is this : Let a meridian—i. e., a true north and south line—be established, in every town or county, by the authority of the State ; monuments, such as stones, set deep in the ground, being placed at each end of it. Let every surveyor be obliged by law to test his compass by this line, at least once in each year, at a given hour in the day. This he could do as easily as in taking the bearing of a fence, by setting his instrument on one monument, and sighting to a staff held on the other. Let the variation thus ascertained be inserted in the notes of the survey, and recorded in the deed. Another surveyor, years or centuries afterward, could test his compass by taking the bearing of the same monuments, and the difference between this and the former bearing would be the change of declination. He could thus determine with entire certainty the proper allowance to be made (as in Art. 282) in order to retrace the original line, no matter how much, or how irregularly, the declination may have changed, or how badly adjusted was the compass of the original survey. Any permanent line employed in the same manner as the meridian line would answer the same purpose, though less conveniently, and every surveyor should have such a line, at least for his own use.\*

\* This remedy seems to have been first suggested by Rittenhouse. It has since been recommended by T. Sopwith, in 1822 ; by E. F. Johnson, in 1831, and by W. Roberts, of Troy, in 1839. The errors of resurveys, in which the change is neglected, were noticed in the "Philosophical Transactions," as long ago as 1679. On magnetic declination, see the following "Reports of the United States Coast and Geodetic Survey": 1881, 1882, 1888, and 1890.

## CHAPTER IV.

### TRANSIT-SURVEYING—BY THE THIRD METHOD.

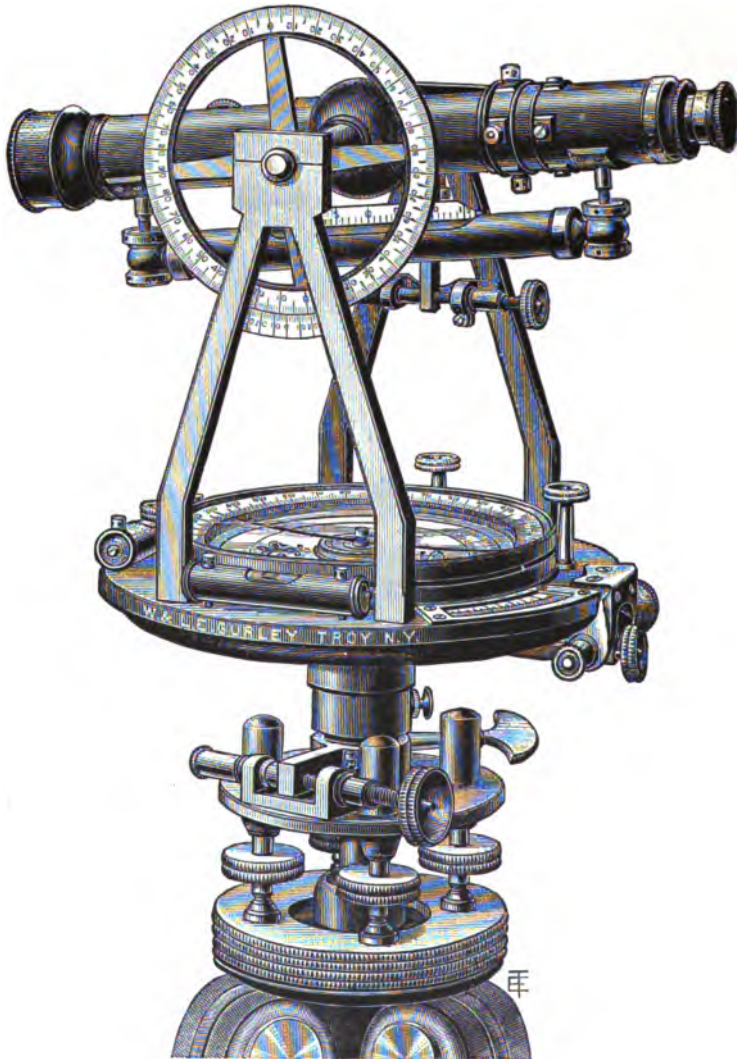
#### THE INSTRUMENTS.

284. THE TRANSIT is a *Goniometer*, or Angle-Measurer. It consists, essentially, of a circular plate of metal, supported in such a manner as to be horizontal, and divided on its outer circumference into degrees and parts of degrees. Through the center of this plate passes an upright axis, and on it is fixed a second circular plate, which nearly touches the first plate, and can turn freely around to the right and to the left. This second plate carries a telescope, which rests on upright standards firmly fixed to the plate, and which can be pointed upward and downward. By the combination of this motion and that of the second plate around its axis, the telescope can be directed to any object. The second plate has some mark on its edge, such as an arrow-head, which serves as a pointer or index for the divided circle, like the hand of a clock. When the telescope is directed to one object, and then turned to the right or to the left, to some other object, this index which moves with it, and passes around the divided edge of the other plate, points out the arc passed over by this change of direction, and thus measures the horizontal angle made by the lines imagined to pass from the center of the instrument to the two objects.

The great value of this instrument, and the accuracy of its measurements of angles, are due chiefly to two things : to the *telescope* with its cross-hairs, by which great precision in sighting to a point is obtained ; and to the *vernier scale*, which enables minute portions of any arc to be read with ease and correctness. The

former assists the eye in directing the line of sight, and the latter aids it in reading off the results. Arrangements for giving slow

FIG. 199.



and steady motion to the movable parts of the instrument add to the value of the above. A contrivance for *repeating* the observa-

tion of angles still further lessens the unavoidable inaccuracies of these observations.

**285. The Surveyor's Transit** (Fig. 199). In this instrument the telescope takes the place of the plain sights of the surveyor's compass, and the angles are read on the graduated limb to single minutes by the vernier.

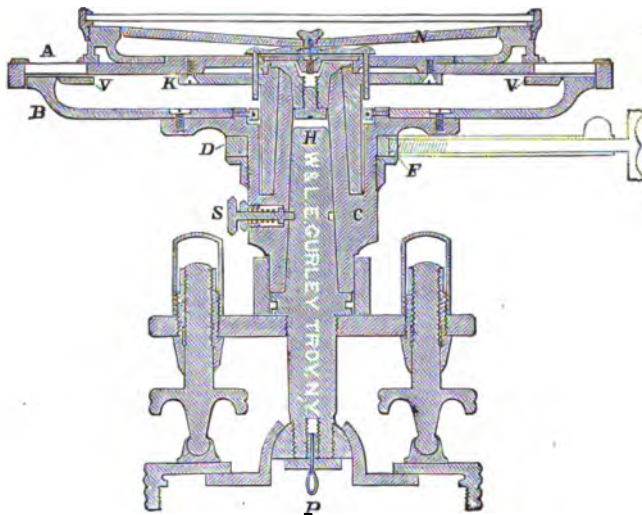
A level is attached to the telescope, and a vertical circle is attached to the telescope-axis inside of the left-hand standard. The vertical angles through which the telescope is moved may be read off from the vernier attached to the left-hand standard, and shown below the vertical circle. The slow-motion screw for the vertical circle is shown attached to the right-hand standard. The clamp for the axis is hidden by the telescope. The standards upon which the telescope-axis rests are fastened to the upper plate (the vernier-plate). This plate also carries the compass-circle. The compass-circle with its accessories is similar to that already explained in the Surveyor's Compass. The compass-circle can be turned on its center, so that the declination of the needle can be set off, and lines can be run with their true bearings. The vernier-plate covers the lower plate (the divided limb), so that only two short arcs of the divided limb are seen through openings where the verniers are placed. The screw which clamps the vernier-plate to the divided limb is shown on the right of the plate, together with the slow-motion screw. The lower clamp and the slow-motion screw are attached to the upper parallel plate.

**286.** As the value of this instrument depends greatly on the accurate fitting and bearings of the two concentric vertical axes, and as their connection ought to be thoroughly understood, a vertical section through the body of the instrument is given in Fig. 200.

The upper plate, or vernier-plate, A, A, carries the verniers, compass-box, and telescope. It is attached to its socket by the flange, K. This socket is fitted to the outside, conical surface of the main socket, C. The main socket, to which is attached the divided limb, B, B, is fitted to the conical spindle H, and held

on the spindle by the spring-catch S. A screw holds the conical center, whose upper flange keeps the sockets of the two plates

FIG. 200.



together. The clamp is at F. Two of the four leveling screws are shown in section. The spindle, H, passes through the upper parallel plate, and is attached to a movable section of the lower parallel plate by a ball-and-socket joint. The leveling screws pass through the upper parallel plate, and rest in cups on the lower parallel plate. As the leveling screws are movable on the lower parallel plate, the movable section of this plate enables the upper part of the instrument to be moved from side to side, so as to bring the center of the instrument precisely over any desired point. This arrangement is called a "shifting center." At the lower end of the spindle is a loop, P, from which the plumb-bob is suspended.

**287. The Telescope.** This is a combination of lenses, placed in a tube, and so arranged, in accordance with the laws of optical science, that an image of any object to which the telescope may be directed, is formed within the tube (by the rays of light coming from the object and bent in passing through the object-glass), and



there magnified by an eye-glass, or eye-piece, composed of several lenses. The arrangement of these lenses is very various. Those two combinations, which are preferred for surveying instruments, will be here explained :

Fig. 201 represents a telescope which inverts objects. Any object is rendered visible by every point of it sending forth rays of light in every direction. In this figure the highest and lowest points of the object, which here is an arrow, A, are alone considered. Those of the rays proceeding from them, which meet the object-glass, O, form a cone. The center line of each cone, and its extreme upper and lower lines, are alone shown in the figure. It will be seen that these rays, after passing through the object-glass, are refracted or bent by it, so as to cross one another, and thus to form at B an inverted image of the object. This would be rendered visible, if a piece of ground-glass, or other semi-transparent substance, were placed at the point B, which is called the *focus* of the object-glass. The rays which form this image continue onward and pass through the two lenses C and D, which act like one magnifying-glass, so that the rays, after being refracted by them, enter the eye at such angles as to form there a magnified and inverted image of the object. This combination of the two plano-convex-lenses, C and D, is known as "Ramsden's Eye-piece."

This telescope, inverting objects, shows them upside down, and the right side on the left. They can be shown erect by adding one or two more lenses, as in the marginal figure. But as these lenses absorb light and lessen the distinctness of vision, the former arrangement is sometimes preferred. A little practice makes it equally convenient for the observer, who soon becomes accustomed to seeing his flagmen standing on their heads, and soon learns to motion them to the right when he wishes them to go to the left, and *vice versa*.

FIG. 201.



FIG. 202.

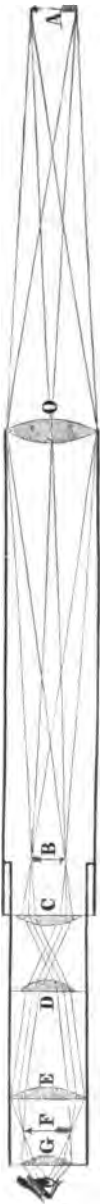


Fig. 202 represents a telescope which shows objects erect. Its eye-piece has four lenses. The eye-piece of the common terrestrial telescope, or spy-glass, has three. Many other combinations may be used, all intended to show the object achromatically, or free from false coloring, but the one here shown is that most generally preferred at the present day. It will be seen that an inverted image of the object A is formed at B, as before, but that the rays continuing onward are so refracted in passing through the lens C as to again cross, and thus, after further refraction by the lenses D and E, to form, at F, an erect image, which is magnified by the lens G.

In both these figures, the limits of the page render it necessary to draw the angles of the rays very much out of proportion.

**288. Cross-Hairs.** Since a considerable field of view is seen in looking through the telescope, it is necessary to provide means for directing the line of sight to the precise point which is to be observed. This could be effected by placing a very fine point, such as that of a needle, within the telescope, at some place where it could be distinctly seen. In practice, this fine point is obtained by the intersection of two very fine lines, placed in the common *focus* of the object-glass and of the eye-piece. These lines are called the *cross-hairs*, or *cross-wires*. Their intersection can be seen through the eye-piece, at the same time, and apparently at the same place, as the image of the distant object. The magnifying powers of the eye-piece will then detect the slightest deviation from perfect coincidence. "This application of the telescope may be considered as completely annihilating that part of the error of observation which might otherwise arise from an erroneous estimation of the direction in which an object lies from the observer's eye, or from the center of the in-

strument. It is, in fact, the grand source of all the precision of modern astronomy, without which all other refinements in instrumental workmanship would be thrown away." What Sir John Herschel here says of its utility to astronomy is equally applicable to surveying.

The imaginary line which passes through the intersection of the cross-hairs and the optical center of the object-glass is called the *line of collimation* of the telescope.\*

The cross-hairs are attached to a ring, or short, thick tube of brass, placed within the telescope - tube, through holes in which pass loosely four screws, whose threads enter and take hold of the ring, behind or in front of the cross-hairs, as shown (in front view and in section) in the two figures in the margin. Their movements will be explained in "ADJUSTMENTS."

FIG. 203.

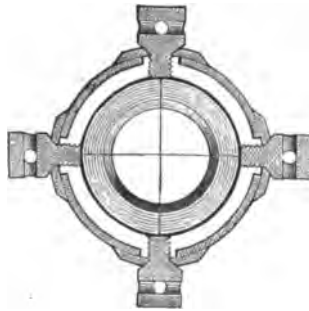


FIG. 204.



FIG. 205.

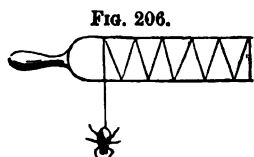


Usually, one cross-hair is horizontal, and the other vertical, as in Fig. 203, but sometimes they are arranged as in Fig. 205, which is thought to enable the object to be bisected with more precision. A horizontal hair is sometimes added.

The cross-hairs are best made of platinum wire, drawn out very fine by being previously inclosed in a larger wire of silver, and the silver then removed by nitric acid. Silk threads from a cocoon are sometimes used. Spiders' threads are, however, the most usual. If a cross-hair is broken, the ring must be taken out by removing two opposite screws, and inserting a wire with a screw cut on its end, or a stick of suitable size, into one of the holes thus left open

\* From the Latin word *collimo*, or *collineo*, meaning to direct one thing toward another in a straight line, or to aim at. The *line of aim* would express the meaning.

in the ring, it being turned sidewise for that purpose, and then removing the other screws. The spiders' threads are then stretched across the notches seen in the end of the ring, and are fastened by gum, or varnish, or beeswax. The operation is a very delicate one.



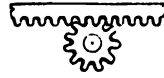
The following plan has been employed : A piece of wire is bent, as in the figure, so as to leave an opening a little wider than the ring of the cross-hairs. A cobweb is chosen, at the end of which a spider is hanging, and it is wound around the bent wire, as in the figure, the weight of the insect keeping it tight and stretching it ready for use, each part being made fast by gum, etc. When a cross-hair is wanted, one of these is laid across the ring and there attached. One method is to draw the thread out of the spider, persuading him to spin, if he sulks, by tossing him from hand to hand. Another method is to unwind the spider-web from the cocoons, frequently to be found in spider-webs. A stock of such threads must be obtained in warm weather for the winter's wants. A piece of thin glass, with a horizontal and a vertical line etched on it, may be made a substitute.

**289. Instrumental Parallax.** This is an apparent movement of the cross-hairs about the object to which the line of sight is directed, taking place on any slight movement of the eye of the observer. It is caused by the image and the cross-hairs not being precisely in the common focus, or point of distinct vision of the eye-piece and the object-glass. To correct it, move the eye-piece out or in till the cross-hairs are seen clearly and sharply defined against any white object. Then move the object-glass in or out till the object is also distinctly seen. The cross-hairs will then seem to be fixed to the object, and no movement of the eye will cause them to appear to change their place.

**290.** A milled-headed screw (on the farther side of the telescope, and not shown in the figure) passes into the telescope, and has a pinion at its other end entering a toothed rack (Fig.

207), and is used to move the object-glass, O, out and in, according as the object looked at is nearer or farther than the one last observed. Short distances require a long tube; long distances a short tube.

FIG. 207.



The eye-piece is moved in and out by a similar arrangement to the preceding. This movement is necessary in order to obtain a distinct view of the cross-hairs. Short-sighted persons require the eye-piece to be pushed farther in than persons of ordinary sight, and old or long-sighted persons to have it drawn farther out.

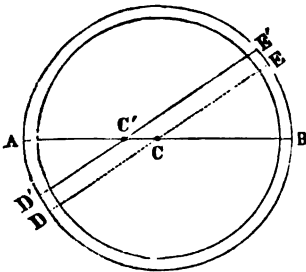
**291. Supports.** The telescope of the *transit* is supported by a hollow axis at right angles to it, which itself rests, at each end, on two upright pieces, or standards, spreading at their bases so as to increase their stability.

One end of the axis rests upon a movable block, which can be raised or lowered by a capstan-screw. The use of this will be shown in "ADJUSTMENTS."

**292. The Indexes.** The supports, or standards, of the telescope just described are attached to the upper or index-carrying circle. This, as has been stated, can turn freely on the lower or graduated circle, by means of its conical axis moving in the hollow conical axis of the latter circle. This upper circle carries the index, V,

which is an arrow-head or other mark on its edge, or the zero-point of a vernier scale. There are usually two of these, situated exactly opposite to each other, or at the extremities of a diameter of the upper circle, so that the readings on the graduated circle pointed out by them differ, if both are correct, exactly  $180^\circ$ . The object of this arrangement is to correct any

FIG. 208.



error of *eccentricity*, arising from the center of the axis which carries the upper circle (and with which it and its index-pointers

turn), not being precisely in the center of the graduated circle. In the figure, let  $C$  be the true center of the graduated circle, but  $C'$  the center on which the plate carrying the indexes turns. Let  $A C' B$  represent the direction of a sight taken to one object, and  $D' C' E'$  the direction when turned to a second object. The angle subtended by the two objects at the center of the instrument is required. Let  $D E$  be a line passing through  $C$ , and parallel to  $D' E'$ . The angle  $A C D$  equals the required angle, which is therefore truly measured by the arc  $A D$  or  $B E$ . But if the arc shown by the index is read, it will be  $A D'$  on one side, and  $B E'$  on the other; the first being too small by the arc  $D D'$ , and the other too large by the equal arc  $E E'$ . If, however, the half-sum of the two arcs  $A D'$  and  $B E'$  be taken, it will equal the true arc, and therefore correctly measure the angle. Thus, if  $A D'$  was  $19^\circ$ , and  $B E'$   $21^\circ$ , their half-sum,  $20^\circ$ , would be the correct angle.

Three indexes,  $120^\circ$  apart, are sometimes used. They have the advantage of *averaging* the unavoidable inaccuracies and inequalities of graduation on different parts of the limb, and thus diminishing their effect on the resulting angle.

**293. The Graduated Circle.** This is divided into three hundred and sixty equal parts, or degrees, and each of these is subdivided into two or three parts or more, according to the size of the instrument. In the first case, the smallest division on the circle will of course be  $30'$ ; in the second case  $20'$ . More precise reading, to single minutes or even less, is effected by means of the vernier of the index, all the varieties of which will be fully explained under "VERNIERS." The numbers run from  $0^\circ$  around to  $360^\circ$ , which number is necessarily at the same point as the 0, or *zero-point*. In most instruments there is another concentric circle, on which the degrees are also numbered from  $0^\circ$  to  $90^\circ$ , as on the compass-circle. Each tenth degree is usually numbered, each fifth degree is distinguished by a longer line of division, and each degree-division line is longer than those of the subdivisions. A magnifying-glass is needed for reading the divisions with ease. In large instruments it is attached to each vernier.

**294. Movements.** When the line of sight of the telescope is directed to a distant, well-defined point, the unaided hand of the observer can not move it with sufficient delicacy and precision to make the intersection of the cross-hairs exactly cover or "bisect" that point. To effect this, a clamp, and a tangent, or slow-motion, screw are required. This arrangement, as usually applied to the movement of the upper, or vernier plate, consists of a short post of brass, which is attached to the vernier-plate, and through which passes a long and fine-threaded "tangent-screw." The other end of this screw enters into and carries the *clamp*. This consists of two pieces of brass, which, by turning the clamp-screw, which passes through them on the outside, can be made to take hold of and pinch tightly the edge of the lower circle, which lies between them on the inside. The upper circle is now prevented from moving on the lower one, for the tangent-screw keeps them at a fixed distance apart, so that they can not move to or from one another, nor consequently the two circles to which they are respectively made fast. But when this tangent-screw is turned by its milled head, it gives the clamp and with it the upper plate a smooth and slow motion, backward or forward, whence it is called the "slow-motion screw," as well as "tangent-screw," from the direction in which it acts. Another form of clamp is shown in Fig. 200.

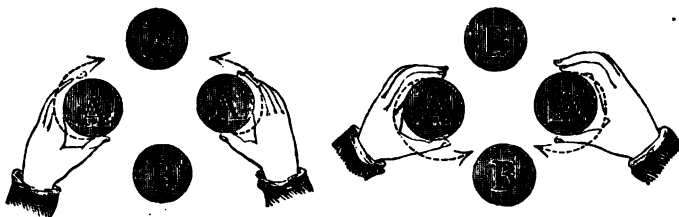
A little different arrangement is employed to give a similar motion to the lower circle on the body of the instrument. Its axis is embraced by a brass ring, into which enters a clamp-screw. The clamp-screw causes the ring to pinch and hold immovably the axis of the lower circle, while a turn of the tangent-screw will slowly move the clamp-ring itself, and therefore with it the lower circle. When the clamp is loosened, the lower circle, and with it everything above it, has a perfectly free motion.

**295. Levels.** Since the object of the instrument is to measure *horizontal* angles, the circular plate on which they are measured must itself be made horizontal. Whether it is so or not is known by means of two small levels placed on the plate at right angles to each other. Each consists of a glass tube, slightly curved upward in its middle, and so nearly filled with alcohol that only a small

bubble of air is left in the tube. This always rises to the highest part of the tubes. They are so "adjusted" that when this bubble of air is in the middle of the tubes, or its ends equidistant from the central mark, the plate on which they are fastened shall be level, which way soever it may be turned. One of the levels is sometimes fixed between the standards above one of the verniers, and the other on the plate at the north end of the compass-box.

**296. Parallel Plates.** To raise or lower either side of the circle, so as to bring the bubbles into the centers of the tubes, requires more gentle and steady movements than the unaided hands can give, and is attained by the parallel plates, and their four milled-headed screws, which hold the plates firmly apart, and, by being turned in or out, raise or lower one side or the other of the upper plate, and thereby of the graduated circle. The two plates are held together by a ball-and-socket joint. To level the instrument, loosen the lower clamp and turn the circle till each level is parallel to the vertical plane passing through a pair of opposite screws. Then take hold of two opposite screws and turn

FIG. 299.



them simultaneously and equally, but in contrary directions, screwing one in and the other out, as shown by the arrows in the figures. A rule easily remembered is that both thumbs must turn in, or both out. The movements represented in the first of these figures would raise the left-hand side of the circle and lower the right-hand side. The movements of the second figure would produce the reverse effect. Care is needed to turn the opposite screws equally, so that they shall not become so loose that the instrument will rock, or so tight as to be cramped. When this last occurs, one of the other pair should be loosened.



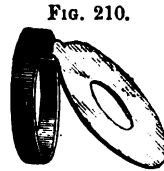
Sometimes one of each pair of the screws is replaced by a strong spring, against which the remaining screws act.

The French and German instruments, and most large instruments, are usually supported by only three screws. In such cases, one level is brought parallel to one pair of screws and leveled by them, and the other level has its bubble brought to its center by the third screw. If there is only one level on the instrument, it is first brought parallel to one pair of screws and leveled, and is then turned one quarter around so as to be perpendicular to them and over the third screw, and the operation is repeated.

**297. Watch-Telescope.** A second telescope is sometimes attached to the lower part of the instrument. When a number of angles are to be observed from any one station, direct the upper and principal telescope to the first object, and then direct the lower one to any other well-defined point. Then make all the desired observations with the upper telescope, and, when they are finished, look again through the lower one, to see that it and therefore the divided circle have not been moved by the movements of the vernier-plate. The French call this the *Witness-Telescope* (*Lunette témoin*).

**298. The Compass.** Upon the upper plate is fixed a compass. It has been fully explained in Chapter III. It is little used in connection with the transit, which is so incomparably more accurate, except as a "check," or rough test of the accuracy of the angles taken, which should about equal the difference of the magnetic bearings.

**299. The Reflector.** In making observations on Polaris at night, or in surveying mines, a reflector (Fig. 210) is used. This is a silvered plate with a hole in it for observing through with the telescope, while a light, held near the silvered surface, illuminates the cross-hairs. The reflector is attached to a ring, fitted to the object-glass slide, and is inclined at an angle of  $45^\circ$  to the ring.



**300. The Diagonal Prism (Fig. 211).** This is a prism attached to the eye-piece of the telescope, so that the rays of light, coming from the object sighted to, and passing through the telescope, are reflected to the eye at an angle of  $90^\circ$  to the line of sight of the telescope. The prism is attached to a movable plate so that it can be turned to suit the position of the observer.

FIG. 211.



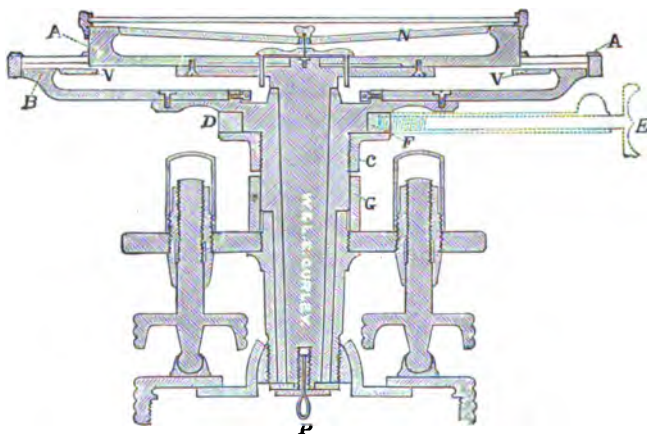
This prism enables larger vertical angles to be measured than would be possible without it.

#### *The Transit.*

**301. The Engineer's Transit (Fig. 213).** This instrument is similar in general construction to that shown in Fig. 199, but differs from it in several important particulars. The sockets for the axes of the plates are longer and differently arranged. These are shown in Fig. 212.

Both levels are attached to the upper plate. The verniers, instead of being placed at the sides between the legs of the standards, are

FIG. 212.

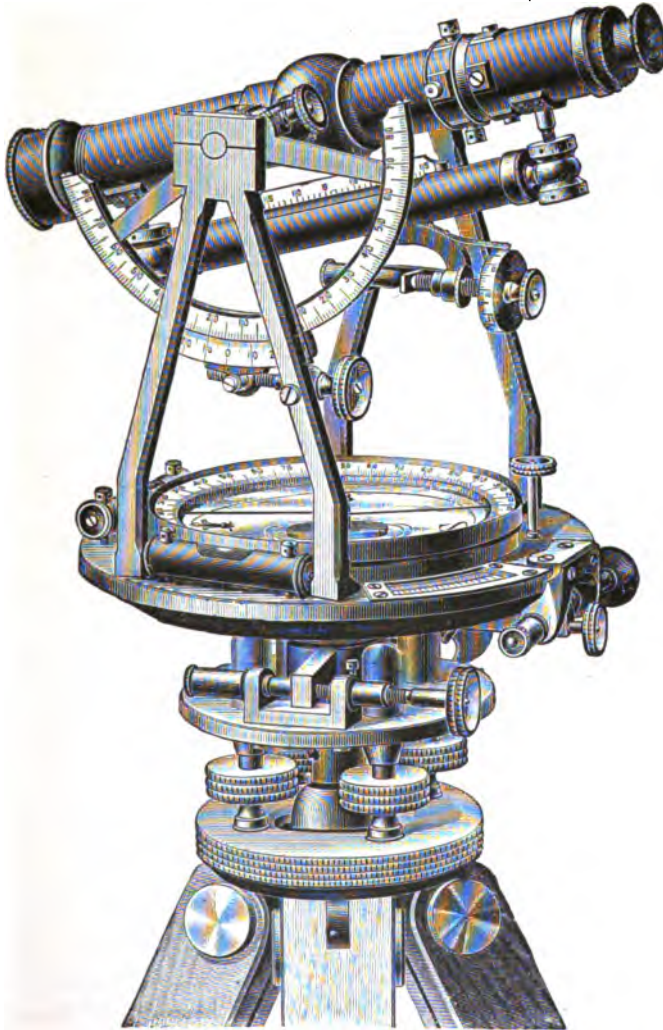


as is usual, are placed near the north and south points of the compass-circle, so that the observer can read the vernier without stepping to the side of the instrument. The slow motion, both of the upper and lower plate, is given by one tangent-screw. In each

case an opposing spiral spring prevents any shake in the tangent-screw.

The vertical arc is attached to the axis of the telescope by a clamp-screw, shown in the figure. The vernier and the slow-motion screw of the vertical arc are shown below the arc, and are attached to the left-hand standard.

FIG. 213.



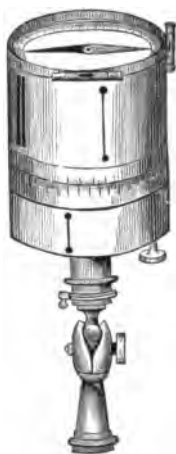
Attached to the right-hand standard is the "Gradienter" (shown in detail in Fig. 245).

**302.** A vertical section through the body of the engineer's transit is given in Fig. 212. The lower plate, or "divided limb," B, is supported by the hollow socket C. Through this hollow socket passes the conical spindle which supports the upper plate A.

The upper plate carries the telescope, compass-box, and the verniers. The vernier-scales, V, V, are attached to the upper plate, but lie in the same plane as the divisions of the lower plate (so that the two can be viewed together without parallax), and are covered with glass to exclude dust. E is the clamp-screw.

**303. The Theodolite.** The transit, when furnished with a vertical circle and telescope level, is sometimes called a Theodolite. This name is used almost exclusively in England and on the Continent of Europe. In one form of the theodolite the telescope can not be revolved on its horizontal axis. This form has been almost entirely superseded in this country by that having a reversible telescope. It is then called a Transit Theodolite, or simply a Transit.

FIG. 214.



**304. Goniastrometre.** A very compact instrument, to which this name has been given in France, where it is much used, is shown in the figure. The upper half of the cylinder is movable on its lower half. The observations may be taken through the slits, as in the surveyor's cross, or a telescope may be added to it. Readings may be taken both from the compass and from the divided edge of the lower half of the cylinder, by means of a vernier on the upper half.\*

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\* The proper care of instruments must not be overlooked. If varnished, they should be wiped gently with fine and clean linen. If polished with oil, they should be rubbed more strongly. The parts neither varnished nor oiled should be cleaned with Spanish-white and alcohol. Varnished wood, when spotted, should be wiped with very soft linen, moistened with a little olive-oil or alcohol. Unpainted wood is

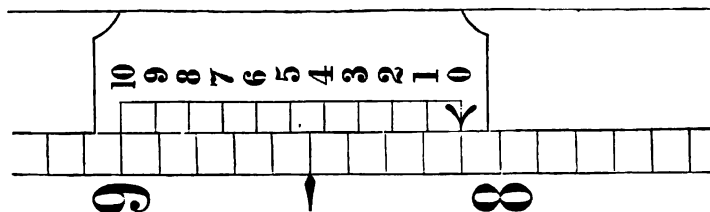
VERNIERS.

**305. Definition.** A vernier is a contrivance for measuring smaller portions of space than those into which a line is actually divided. It consists of a second line or scale, movable by the side of the first, and divided into equal parts, which are a very little shorter or longer than the parts into which the first line is divided. This small difference is the space which we are thus enabled to measure.\*

The vernier scale is usually constructed by taking a length equal to any number of parts on the divided line, and then dividing this length into a number of equal parts, one more or one less than the number into which the same length on the original line is divided.

**306. Illustration.** The figure represents (to twice the real size) a scale of inches divided into tenths, with a vernier scale beside it, by which hundredths of an inch can be measured. The vernier is

FIG. 215.



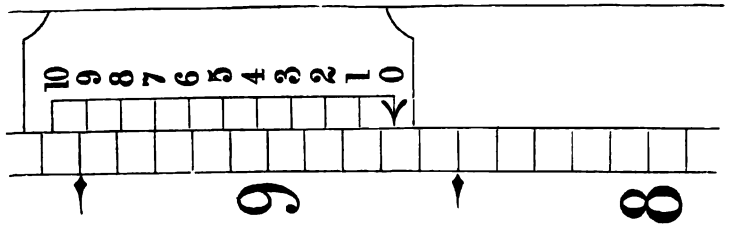
made by setting off on it nine tenths of an inch, and dividing that length into ten equal parts. Each space on the vernier is therefore equal to a tenth of nine tenths of an inch, or to nine hundredths of an inch, and is consequently one hundredth of an inch shorter than one of the divisions of the original scale. The first space of the vernier will therefore fall short of, or be overlapped by, the first

cleaned with sand-paper. Apply olive-oil where steel rubs against brass; and wax softened by tallow where brass rubs against brass. Clean the glasses with kid or buck skin. Wash them, if dirtied, with alcohol.

\* The vernier is so named from its inventor, in 1631. The name "Nonius," often improperly given to it, belongs to an entirely different contrivance for a similar object.

space on the scale by this one hundredth of an inch ; the second space of the vernier will fall short by two hundredths of an inch ; and so on. If, then, the vernier be moved up by the side of the original scale, so that the line marked 1 coincides, or forms one straight line, with the line of the scale which was just above it, we know that the vernier has been moved one hundredth of an inch. If the line marked 2 comes to coincide with a line of the scale, the

FIG. 216.



vernier has moved up two hundredths of an inch ; and so for other numbers. If the position of the vernier be as in this figure, the line marked 7 on the vernier corresponding with some line on the scale, the zero-line of the vernier is seven hundredths of an inch above the division of the scale next below this zero-line. If this division be, as in the figure, 8 inches and 6 tenths, the reading will be 8.67 inches.\*

A vernier like this is used on some leveling-rods, being engraved on the sides of the opening in the part of the target above its middle line. The rod being divided into hundredths of a foot, this vernier reads to thousandths of a foot. It is also used on some French mountain barometers, which are divided to hundredths of a *metre*, and thus read to thousandths of that unit.

**307. General Rules.** *To find what any vernier reads to—i. e., to determine how small a distance it can measure—observe how many parts on the original line are equal to the same number increased or diminished by one on the vernier, and divide the length*

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\* The student will do well to draw such a scale and vernier on two slips of thick paper, and move one beside the other till he can read them in any possible position ; and so with the following verniers.

of a part on the original line by this last number. It will give the required distance.\*

For verniers as usually constructed, the following rule will apply : *Divide the value of the smallest division on the original scale by the number of parts on the vernier.*

For example, if the limb of a transit be divided into half degrees, and thirty parts on the vernier are equal to twenty-nine on the limb, then the value of the smallest division on the limb (30 minutes), divided by the number of parts on the vernier (30) equals one minute. This is what the vernier reads to.

*To read any vernier*, first, look at the zero-line of the vernier (which is sometimes marked by an arrow-head), and if it coincides with any division of the scale, that will be the correct reading, and the vernier divisions are not needed. But if, as usually happens, the zero-line of the vernier comes between any two divisions of the scale, note the nearest next less division on the scale, and then look along the vernier till you come to some line on it which exactly coincides, or forms a straight line, with some line (no matter which) on the fixed scale. The number of this line *on the vernier* (the 7th, in the last figure) tells that so many of the subdivisions which the vernier indicates are to be added to the reading of the entire divisions on the scale.

When several lines on the vernier appear to coincide equally with lines of the scale, take the middle line.

When no line coincides, but one line on the vernier is on one side of a line on the scale, and the next line on the vernier is as far on the other side of it, the true reading is midway between those indicated by these two lines.

**308. Retrograde Verniers.** The spaces of the vernier in modern instruments are usually each shorter than those on the scale, a certain number of parts on the scale being divided into a larger number

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\* In algebraic language, let  $s$  equal the length of one part on the original line, and  $v$  the unknown length of one part on the vernier. Let  $m$  of the former =

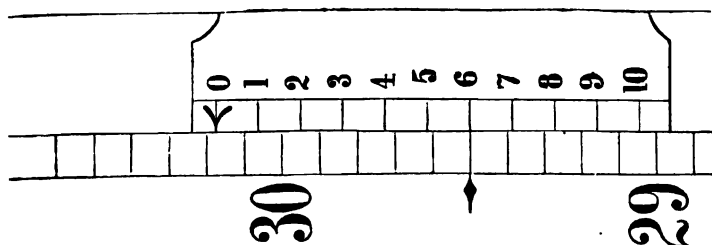
$m + 1$  of the latter. Then  $ms = (m + 1)v$ .  $v = \frac{m}{m + 1}s$ .  $s - v = s$ .

$\frac{m}{m + 1}s = \frac{s}{m + 1}$ . If  $ms = (m - 1)v$ , then  $v - s = \frac{s}{m - 1}$ .

of parts on the vernier.\* In the contrary case,† there is the inconvenience of being obliged to number the lines of the vernier and to count their coincidences with the lines of the scale, in a retrograde or contrary direction to that in which the numbers on the scale run. We will call such arrangements *retrograde verniers*.

**309. Illustration.** In this figure, the scale, as before, represents (to twice the real size) inches divided into tenths, but the vernier is made by dividing eleven parts of the scale into ten equal

FIG. 217.



parts, each of which is therefore one tenth of eleven tenths of an inch—i. e., eleven hundredths of an inch, or a tenth and a hundredth. Each space of the vernier therefore overlaps a space on the scale by one hundredth of an inch. The manner of reading this vernier is the same as in the last one, except that the numbers run in a reverse direction. The reading of the figure is 30.16.

This vernier is the one generally applied to the common barometer, the zero-point of the vernier being brought to the level of the top of the mercury, whose height it then measures. It is also employed for leveling-rods which read downward from the middle of the target.

**310.** Fig. 218 represents (to double size) the usual scale of the English mountain barometer. The scale is first divided into inches. These are subdivided into tenths by the longer

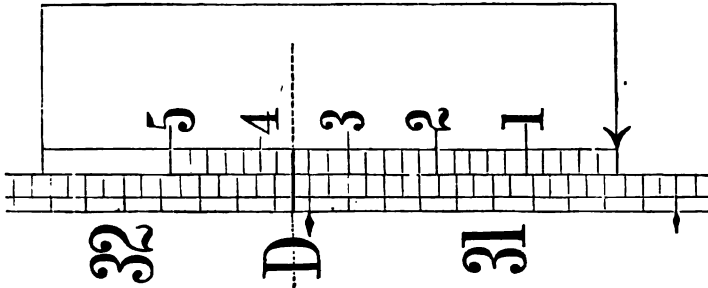
\* i. e., algebraically,  $v = \frac{m}{m+1}$ .

† i. e., when  $v = \frac{m}{m-1}$ .



lines, and the shorter lines again divide these into half tenths, or to 5 hundredths ; 24 of these smaller parts are set off on the ver-

FIG. 218.



nier, and divided into 25 equal parts, each of which is therefore  $= \frac{24 \times .05}{25} = .048$  inch, and is shorter than a division of the scale by  $.050 - .048 = .002$ , or two thousandths of an inch, a twenty-fifth part of a division on the scale, to which minuteness the vernier can therefore read. The reading in the figure is 30.686 (30.65 by the scale and .036 by the vernier), the dotted line marked D showing where the coincidence takes place.

**311. Circle divided into Degrees.** The following illustrations apply to the measurements of angles, the circle being variously divided. In this article, the circle is supposed to be divided into degrees.

If 6 spaces on the vernier are found to be equal to 5 on the circle, the vernier can read to one sixth of a space on the circle—i. e., to 10'.

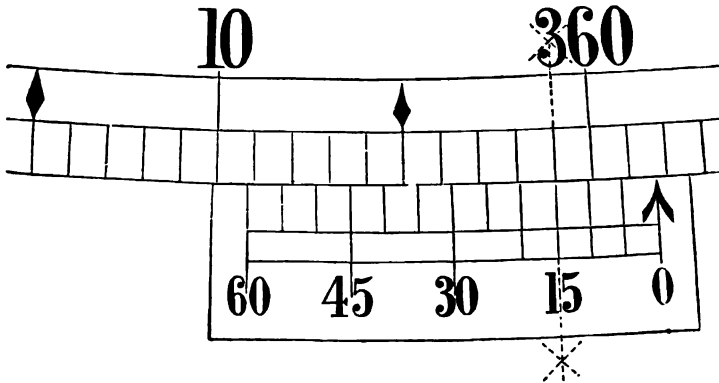
If 10 spaces on the vernier are equal to 9 on the circle, the vernier can read to one tenth of a space on the circle—i. e., to 6'.

If 12 spaces on the vernier are equal to 11 on the circle, the vernier can read to one twelfth of a space on the circle—i. e., to 5'.

Fig. 219 shows such an arrangement. The index, or zero, of the vernier is at a point beyond  $358^\circ$ , a certain distance, which the coincidence of the third line of the vernier (as indicated by the dotted and crossed line) shows to be 15'. The whole reading is therefore  $358^\circ 15'$ .

If 20 spaces on the vernier are equal to 19 on the circle, the vernier can read to one twentieth of a division on the circle—i. e.,

FIG. 219.

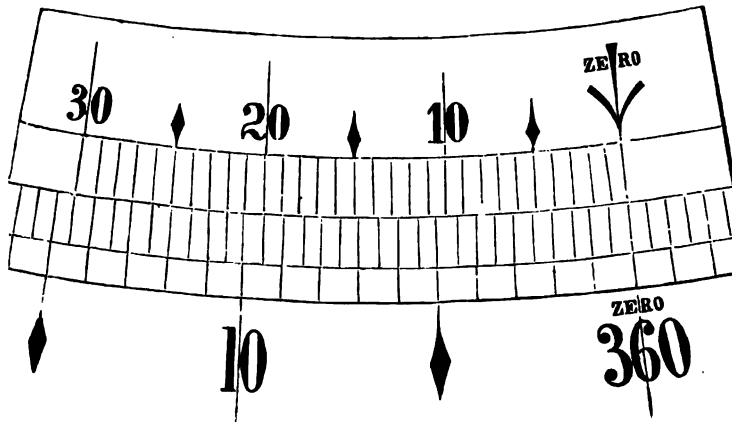


to 3'. English compasses, or "circumferentors," are sometimes thus arranged.

If 60 spaces on the vernier are equal to 59 on the circle, the vernier can read to one sixtieth of a division on the circle—i. e., to 1'.

**312. Circle divided to 30'.** Such a graduation is a very common one. The vernier may be variously constructed.

FIG. 220.

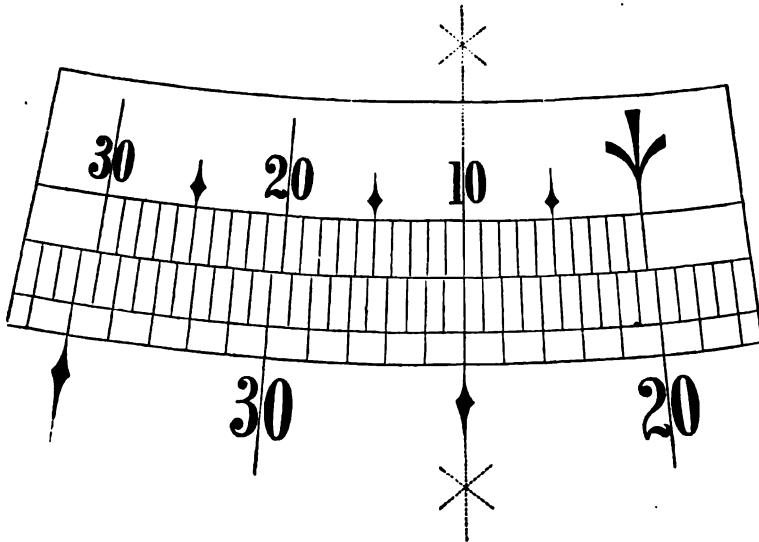


Suppose 30 spaces on the vernier to be equal to 29 on the circle. Each space on the vernier will be  $= \frac{29 \times 30'}{30} = 29'$ , and will therefore be less than a space of the circle by  $1'$ , to which the vernier will then read.

Fig. 220 shows this arrangement. The reading is  $0^\circ$ , or  $360^\circ$ .

In Fig. 221 the dotted and crossed line shows what divisions coincide, and the reading is  $20^\circ 10'$ ; the vernier being the same as in the preceding figure, and its zero being at a point of the circle  $10'$  beyond  $20^\circ$ .

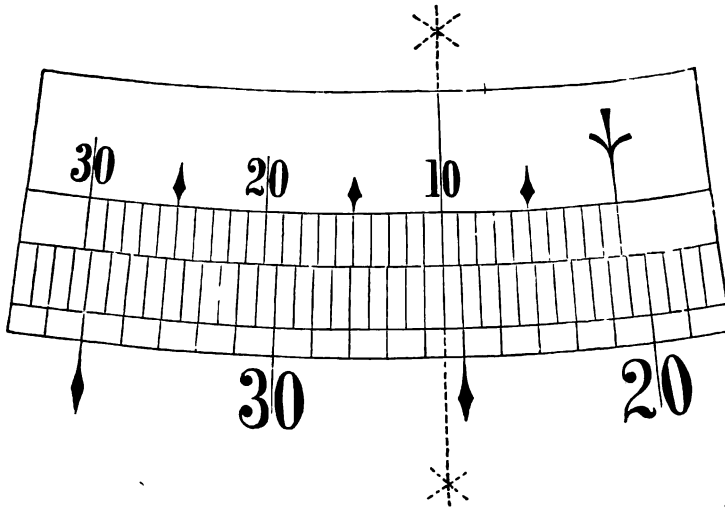
FIG. 221.



In Fig. 222, the reading is  $20^\circ 40'$ , the index being at a point beyond  $20^\circ 30'$ , and the additional space being shown by the vernier to be  $10'$ .

Sometimes 30 spaces on the vernier are equal to 31 on the circle. Each space on the vernier will therefore be  $= \frac{31 \times 30'}{30} = 31'$ , and will be longer than a space on the circle by  $1'$ , to which it will therefore read, as in the last case, but the vernier will be "retrograde." This is the vernier of the compass. The peculiar manner in which it is there applied is shown in Fig. 229.

FIG. 222.

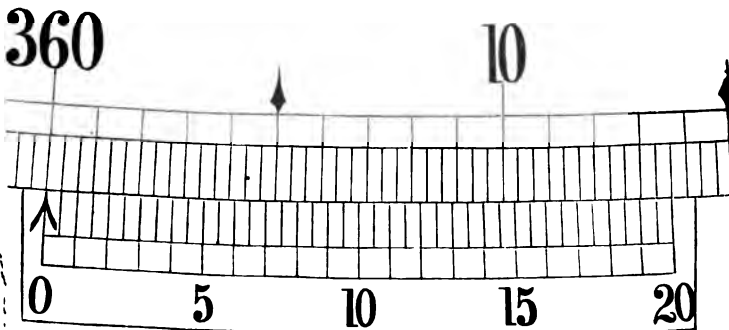


If 15 spaces on the vernier are equal to 16 on the circle, each space on the vernier will be  $= \frac{16 \times 30'}{15} = 32'$ , and the vernier will therefore read to 2'.

**313. Circle divided to 20'.** If 20 spaces of the vernier are equal to 19 on the circle, each space of the latter will be  $= \frac{19 \times 20'}{20} = 19'$ , and the vernier will read to  $20' - 19' = 1'$ .

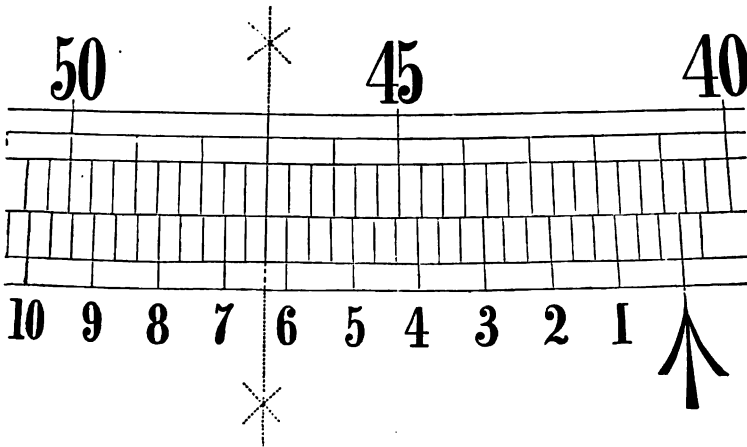
If 40 spaces on the vernier are equal to 41 on the circle, each

FIG. 223.



space on the vernier will be  $= \frac{41 \times 20'}{40} = 20\frac{1}{4}'$ , and the vernier will therefore read to  $20\frac{1}{4}' - 20' = 30''$ . It will be retrograde. In Fig. 223 the reading is  $360^\circ$ , or  $0^\circ$ ; and it will be seen that the

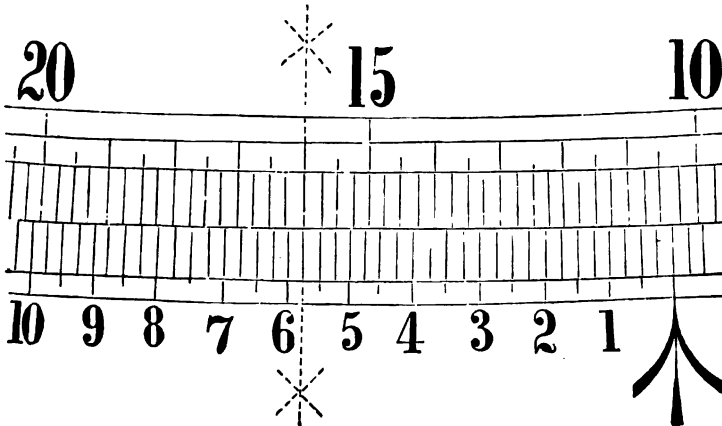
FIG. 224.



40 spaces on the vernier (numbered to whole minutes) are equal to  $13^\circ 40'$  on the limb—i. e., to 41 spaces, each of  $20'$ .

If 60 spaces on the vernier are equal to 59 on the circle, each of the former will be  $= \frac{59 \times 20}{60} = 19' 40''$ , and the vernier will

FIG. 225.

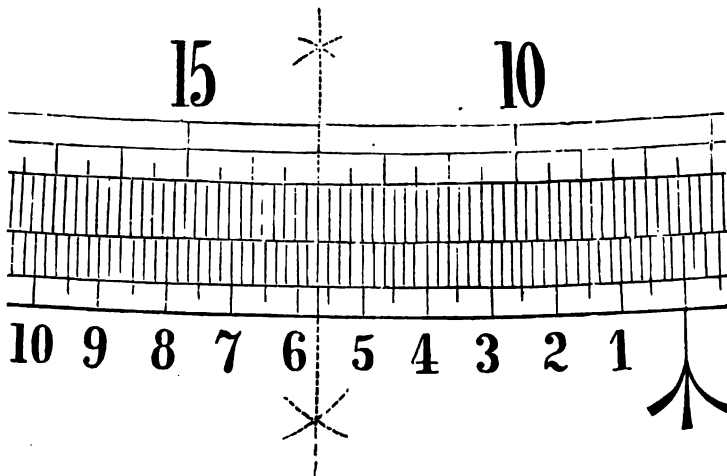


therefore read to  $20' - 19' 40'' = 20''$ . Fig. 224 shows such an arrangement. The reading in that position would be  $40^\circ 46' 20''$ .

**314. Circle divided to 15'.** If 60 spaces on the vernier are equal to 59 on the circle, each space on the vernier will be  $= \frac{59 \times 15'}{60} = 14' 45''$ , and the vernier will read to 15'. In Fig. 225 the reading is  $10^\circ 20' 45''$ , the index pointing to  $10^\circ 15'$ , and something more, which the vernier shows to be  $5' 45''$ .

**315. Circle divided to 10'.** If 60 spaces on the vernier be equal to 59 on the limb, the vernier will read to 10'. In Fig. 226 the reading is  $7^\circ 25' 40''$ , the reading on the circle being  $7^\circ 20'$ , and the vernier showing the remaining space to be  $5' 40''$ .

FIG. 226.



**316. Reading backward.** When an index carrying a vernier is moved backward, or in a contrary direction to that in which the numbers on the circle run, if we wish to read the space which it has passed over in this direction from the zero-point, the vernier must be read backward (i. e., the highest number be called 0), or its actual reading must be subtracted from the value of the smallest space on the circle. The reason is plain ; for, since the vernier

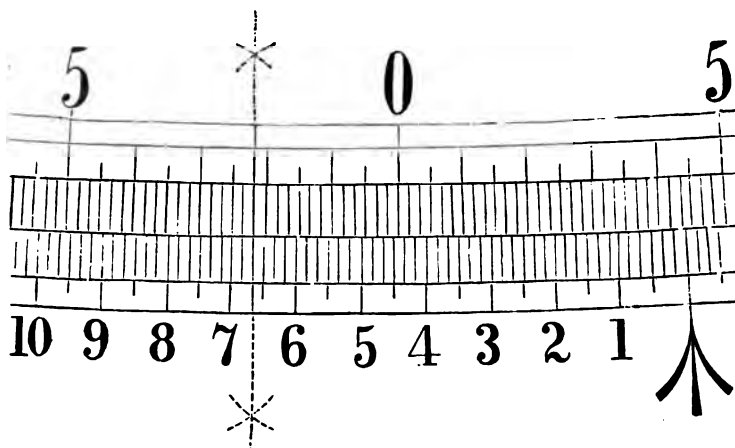
shows how far the index, moving in one direction, has gone past one division-line, the distance which it is from the next division-line (which it may be supposed to have passed, moving in a contrary direction) will be the difference between the reading and the value of one space.

Thus, in Fig. 219, the reading is  $358^{\circ} 15'$ . But, counting backward from the  $360^{\circ}$ , or zero-point, it is  $1^{\circ} 45'$ .

Caution on this point is particularly necessary in using small angles of deflection for railroad-curves.

**317. Arc of Excess.** On the sextant and similar instruments, the divisions of the limb are carried onward a short distance beyond the zero-point. This portion of the limb is called the "Arc of Excess." When the index of the vernier points to this arc, the

FIG. 227.

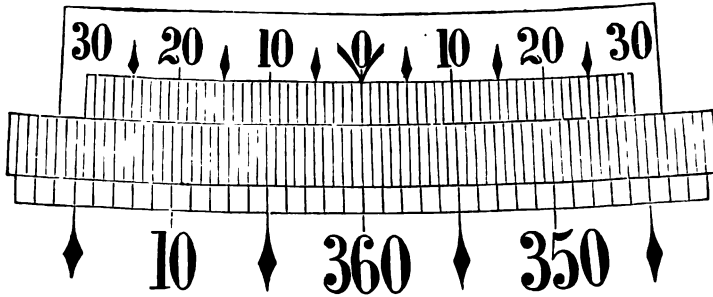


reading must be made as explained in the last article. Thus, in the figure, the reading on the arc from the zero of the limb to the zero of the vernier is  $4^{\circ} 20'$ , and something more, and the reading of the vernier from 10 toward the right, where the lines coincide, is  $3' 20''$  (or it is  $10' - 6' 40'' = 3' 20''$ ), and the entire reading is therefore  $4^{\circ} 23' 20''$ .

**318. Double Verniers.** To avoid the inconveniences of reading backward, double verniers are sometimes used. Fig. 228

shows one applied to a transit. Each of the verniers is like the one described in Art. 312, Figs. 220, 221, and 222. When the degrees are counted to the left, or as the numbers run, as is usual,

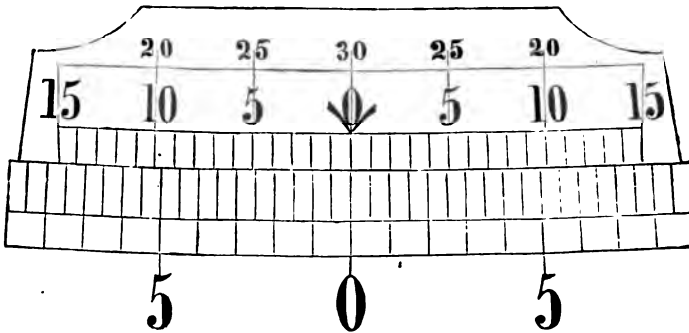
FIG. 228.



the left-hand vernier is to be read, as in Art. 312; but when the degrees are counted to the right, from the  $360^\circ$  line, the right-hand vernier is to be used.

**319. Compass-Vernier.** Another form of double vernier, often applied to the compass, is shown in Fig. 229. The limb is

FIG. 229.



divided to half-degrees, and the vernier reads to minutes, 30 parts on it being equal to 31 on the limb. But the vernier is only half as long as in the previous case, going only to  $15'$ , the upper figures on one half being a sort of continuation of the lower figures on the other half. Thus, in moving the index to the right, read the *lower* figures on the left-hand vernier (it being retrograde)



at any coincidence, when the space passed over is less than 15'; but if it be more, read the *upper* figures on the right-hand vernier, and *vice versa*.

## ADJUSTMENTS.

**320.** The purposes for which the transit (as well as most surveying and astronomical instruments) is to be used, require and presuppose certain parts and lines of the instrument to be placed in certain directions with respect to others; these respective directions being usually parallel or perpendicular. Such arrangements of their parts are called their *Adjustments*. The same word is also applied to placing these lines in these directions. In the following explanations the operations which determine whether these adjustments are correct, will be called their *Verifications*; and the making them right, if they are not so, their *Rectifications*.\*

**321.** In observations of horizontal angles with the transit it is required—

1. That the circular plates shall be horizontal in whatever way they may be turned around.

2. That the telescope, when pointed forward, shall look in precisely the reverse of its direction when pointed backward—i. e., that its two lines of sight (or lines of collimation) forward and backward shall lie in the same plane.

3. That the telescope, in turning upward or downward, shall move in a truly vertical plane, in order that the angle measured between a low object and a high one may be precisely the same as would be the angle measured between the low object and a point exactly under the high object, and in the same horizontal plane as the low one.

We shall see that all these adjustments are finally resolvable into these: 1. Making the vertical axis of the instrument perpendicular to the plane of the levels; 2. Making the line of collima-

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\* It has been well said that, "in the present state of science, it may be laid down as a maxim that every instrument should be so contrived that the observer may easily examine and rectify the principal parts; for, however careful the instrument-maker may be, however perfect the execution thereof, it is not possible that any instrument should long remain accurately fixed in the position in which it came out of the maker's hands." (Adams's "Geometrical and Graphical Essays," 1791.)

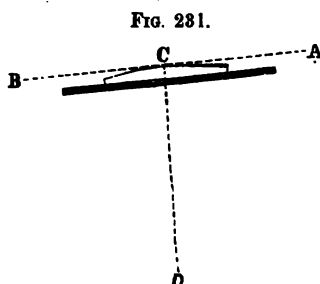
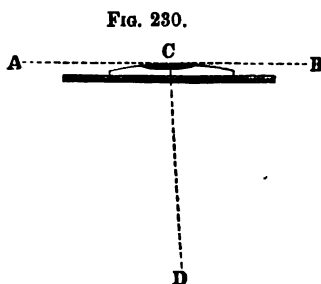
tion perpendicular to its axis ; and, 3. Making this axis parallel to the plane of the levels. They are all best tested by the invaluable principle of "reversion."

We have now, first, to examine whether these things *are* so—that is, to "verify" the adjustments ; and, second, if we find that they are not so, to *make* them so—i. e., to "rectify" or "adjust" them correctly. The above three requirements produce as many corresponding adjustments.

**322. First Adjustment.** *To cause the circle to be horizontal in every position.*

*Verification.* Turn the vernier-plate, which carries the levels, till one of them is parallel to one pair of the parallel plate-screws. The other will then be parallel to the other pair. Bring each bubble to the middle of its tube, by that pair of screws to which it is parallel. Then turn the vernier-plate half-way around—i. e., till the index has passed over  $180^\circ$ . If the bubbles remain in the centers of the tubes, they are in adjustment. If either of them runs to one end of the tube, it requires rectification.

*Rectification.* The fault which is to be rectified is that the plane of the level (i. e., the plane tangent to the highest point of the level tube) is not perpendicular to the vertical axis on which



the plate turns. For, let AB represent this plane, seen edgewise, and CD the center line of the vertical axis, which is here drawn as making an acute angle with this plane on the right-hand side. The first figure represents the bubble brought to the center of the tube. The second figure represents the plate turned half around. The center line of the axis is supposed to remain unmoved. The

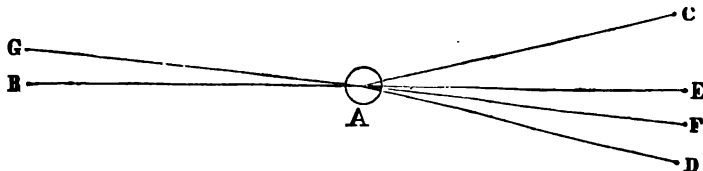
acute angle will now be on the left-hand side, and the plate will no longer be horizontal; consequently, the bubble will run to the higher end of the tube. The rectification necessary is evidently to raise one end of the tube and lower the other. The real error has been doubled to the eye by the reversion. Half of the motion of the bubble was caused by the tangent plane not being perpendicular to the axis, and half by this axis not being vertical. Therefore, raise or lower one end of the level by the screws which fasten it to the plate, till the bubble comes about *half-way* back to the center, and then bring it quite back by turning its pair of parallel plate-screws. Then again reverse the vernier-plate  $180^\circ$ . The bubble should now remain in the center. If not, the operation should be repeated. The same must be done with the other level, if required. Then the bubbles will remain in the center during a complete revolution. This proves that the axis of the vernier-plate is then vertical; and, as it has been fixed by the maker perpendicular to the plate, the latter must then be horizontal.

It is also necessary to examine whether the bubbles remain in the center, when the divided circle is turned round on its axis. If not, the axes of the two plates are not parallel to each other. The defect can be remedied only by the maker; for, if the bubbles be altered so as to be right for this reversal, they will be wrong for the vernier-plate reversal.

**323. Second Adjustment.** *To cause the line of collimation to revolve in a plane.*

*Verification.* Set up the transit in the middle of a level piece of ground, as at A in the figure. Level it carefully. Set a stake,

FIG. 232.



with a nail driven into its head, or a chain-pin, as far from the instrument as it is distinctly visible, as at B. Direct the telescope

to it, and fix the intersection of the cross-hairs very precisely upon it. Clamp the instrument. Measure from A to B. Then turn over the telescope, and set another stake at an equal distance from the transit, and also precisely in the line of sight. If the line of collimation has *not* continued in the same plane during its half-revolution, this stake will not be at E, but to one side, as at C. To discover the truth, loosen the clamp and turn the vernier-plate half around without touching the telescope. Sight to B, as at first, and again clamp it. Then turn over the telescope, and the line of sight will strike, as at D in the figure, as far to the right of the point as it did before to its left.

*Rectification.* The fault which is to be rectified is that the line of collimation of the telescope is not perpendicular to the horizontal axis on which the telescope revolves. This will be seen by

FIG. 233.



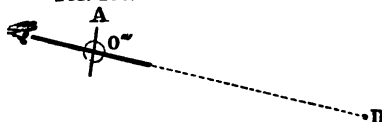
FIG. 234.



FIG. 235.



FIG. 236.



the figures, which represent the position of the lines in each of the four observations which have been made. In each of the figures the long, thick line represents the telescope, and the short one the axis on which it turns. In Fig. 233 the line of sight is directed to B. In Fig. 234 the telescope has been turned over, and with it the axis, so that the obtuse angle marked O in the first figure has taken the place, O', of the acute angle, and the telescope points to C instead of to E. In Fig. 235 the vernier-plate has been turned

half around so as to point to B again, and the same obtuse angle has got around to O'. In Fig. 236 the telescope has been turned over, the obtuse angle is at O'', and the telescope now points to D.

To make the line of collimation perpendicular to the axis, the former must have its direction changed. This is effected by moving the vertical hair the proper distance to one side. By loosening the left-hand screw and tightening the right-hand one, the ring, and with it the cross-hairs, will be drawn to the right, and *vice versa*. Two holes at right angles to each other pass through the outer heads of the screws. Into these holes a stout steel wire is inserted, and the screws can thus be turned around. Screws so made are called "capstan-headed." One of the other pair of screws may need to be loosened to avoid straining the threads. In some French instruments, one of each pair of screws is replaced by a spring.

To find how much to move this vertical hair, measure from C to D, Fig. 232: Set a stake at the middle point E, and set another at the point F, midway between D and E. Move the vertical hair till the line of sight strikes F. Then the instrument is adjusted; and, if the line of sight be now directed to E, it will strike B when the telescope is turned over, since the hair is moved half of the doubled error, D E. The operation will generally require to be repeated, not being quite perfected at first.

It should be remembered that, if the telescope used does not invert objects, its eye-piece will do so. Consequently, with such a telescope, if it seems that the vertical hair should be moved to the left, it must be moved to the right, and *vice versa*. An inverting telescope does not invert the cross-hairs.

If the young surveyor has any doubts as to the perfection of his rectification, he may set another stake exactly under the instrument by means of a plumb-line suspended from its center; and then, in like manner, set his transit over B or E. He will find that the other two stakes, A and the extreme one, *are* in the same straight line with his instrument.

In some instruments, the horizontal axis of the telescope can be taken out of its supports and turned over, end for end. In such a case, the line of sight may be directed to any well-defined point,

and the axis then taken out and turned over. If the line of sight again strikes the same point, this line is perpendicular to the axis.

FIG. 237.

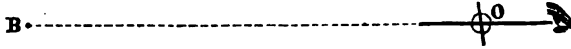
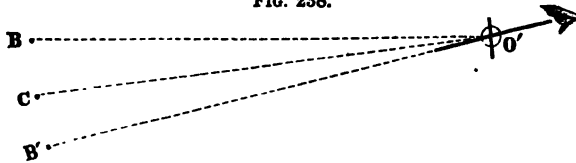


FIG. 238.



If not, the apparent error is double the real error, as appears from the figures, the obtuse angle  $O$  coming to  $O'$ , and the desired perpendicular line falling at  $C$  midway between  $B$  and  $B'$ . The rectification may be made as before; or, in some large instruments, in which the telescope is supported on  $Ys$ , by moving one of the  $Ys$  laterally.

**324. Third Adjustment.** *To cause the line of collimation to revolve in a vertical plane.*

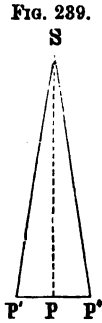
*Verification.* Suspend a long plumb-line from some high point. Set the instrument near this line, and level it carefully. Direct the telescope to the plumb-line, and see if the intersection of the cross-hairs follows and remains upon this line when the telescope is turned up and down. If it does, it moves in a vertical plane.

The angle of a new and well-built house will form an imperfect substitute for the plumb-line.

*Otherwise:* The instrument being set up and leveled as above, place a basin of some reflecting liquid (quicksilver being the best, though molasses, or oil, or even water will answer, though less perfectly) so that the top of a steeple, or other point of a high object, can be seen in it through the telescope by reflection. Make the intersection of the cross-hairs cover it. Then turn up the telescope, and, if the intersection of the cross-hairs bisects also the object seen directly, the line of sight has moved in a vertical plane. If a star be taken as the object, the star and its reflection will be

equivalent (if it be nearly overhead) to a plumb-line at least fifty million million miles long.

*Otherwise:* Set the instrument as close as possible to the base of a steeple or other high object; level it, and direct it to the top of the steeple, or to some other elevated and well-defined point. Clamp the plates. Turn down the telescope, and set up a pin in the ground precisely "in line." Then loosen the clamp, turn over the telescope, and turn it half-way around, or so far as to again sight to the high point. Clamp the plates, and again turn down the telescope. If the line of sight again strikes the pin, the telescope has moved in a vertical plane. If not, the apparent error is double the real error. For, let  $S$  be the top of the steeple (Fig. 239), and  $P'$  the pin; then the plane in which the telescope moves, seen edgewise, is  $SP'$ ; and, after being turned around, the line of sight moves in the plane  $SP''$ , as far to one side of the vertical plane  $SP$  as  $SP'$  was on the other side of it.

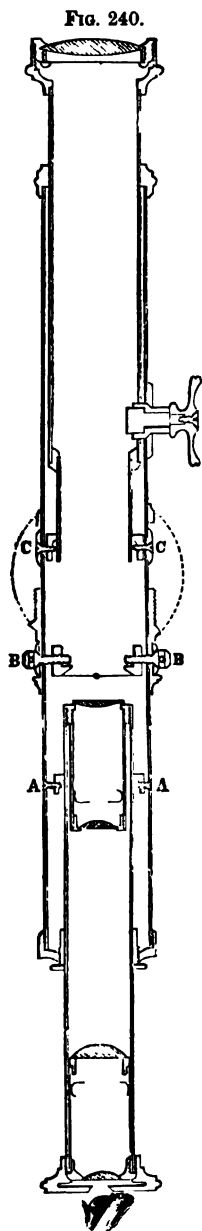


*Rectification.* Since the second adjustment causes the line of sight to move in a plane perpendicular to the axis on which it turns, it will move in a vertical plane if that axis be horizontal. It can be made so by raising or lowering one end of the axis by means of a screw placed in the standard for that purpose.

**325. Centering Eye-Piece.** In some instruments, such as that of which a longitudinal section is shown on page 220, the inner end of the eye-piece may be moved so that the cross-hairs shall be seen precisely in the center of its field of view. This is done by means of four screws, arranged in pairs, like those of the cross-hair ring-screws, and capable of moving the eye-piece up and down, and to right or left, by loosening one and tightening the opposite one. Two of them are shown at  $A, A$ , in the figure, in which  $B, B$ , are two of the cross-hair screws.

**326. Centering Object-Glass.** In some instruments four screws, similarly arranged, two of which are shown at  $C, C$ , can move, in any direction, the inner end of the slide which carries the object-

glass. The necessity for such an arrangement arises from the impossibility of drawing a tube perfectly straight. Consequently, the line of collimation, when the tube is drawn in, will not coincide with the same line when the tube is pushed out. If adjusted for one position, it will therefore be wrong for the other. These screws, however, can make it right in both positions. They are used as follows :



Sight to some well-defined point as far off as it can be distinctly seen. Then, having the plates firmly clamped, move out the object-glass slide, and fix a point in the line of sight as close to the instrument as can be distinctly seen. Then turn the limb half-way around horizontally, reverse the telescope, and again sight to the near point, by clamping the plates and bringing the vertical cross-hair on the point by means of the tangent-screw. Then draw in the object-glass slide until the distant object is distinctly seen. If the vertical cross-hair bisects it, no adjustment is necessary. If not, correct one half of the apparent error by means of the screws C C in Fig. 240. This may disturb the second adjustment. Try that over again, and again perform the operation of centering the object-glass.

This adjustment is always performed by the maker, and its screws are covered by a short tube.

All the adjustments should be meddled with as little as possible, lest the screws should get loose ; and, when once made right, they should be kept so by careful usage.



**327. Fourth Adjustment.** *To cause the line of collimation of the telescope to be horizontal when the bubble of the level attached to it is in the center of its tube.*

Drive two pegs several hundred feet apart, and set the instrument midway between them. Level, and sight to the rod held on each peg. The difference of the readings will be the true difference of the heights of the pegs, no matter how much the level may be out of adjustment.

Then set the instrument over one peg, and sight to the rod held at the other. Measure the height of the cross-hairs above the first peg. The difference of this height and the reading on the rod *should* equal the difference of the heights of the two points, as previously determined. If it does not, set the target to the sum or difference of the height of the cross-hairs above the first peg and the true difference of height of the points, according as the first point is higher or lower than the second, and hold the rod on the second point. Sight to it, and raise or lower one end of the bubble-tube until the horizontal cross-hair *does* bisect the target when the bubble is in the center.

Instead of setting *over* one peg, it is generally more convenient to set near to it, and sight to a rod held on it, and use this reading instead of the measured height of the cross-hairs.

**328. Fifth Adjustment.** *To make the vernier of the vertical circle read zero when the bubble of the telescope-level is in the center.*

This is verified in various ways:

1. *By simple inspection.*
2. *By reversion.* Sight to some point. Note the reading on the vertical circle. Turn the telescope half-way around horizontally. Turn over the telescope and again observe the same point, and note the reading. Half the difference (if any) of the two readings is the error.
3. *By reciprocal observations.* Observe successively from each of two points to the other. Half the difference of the readings equals the index-error.

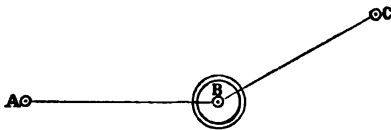
When the verification has been made, the error may be rectified

on the instrument by moving the vernier-plate, or the circle, or noted as a correction to each observation when the instrument is large and delicate.

### THE FIELD-WORK.

**329. To measure a Horizontal Angle.** Set up the instrument so that its center shall be exactly over the angular point, or in the intersection of the two lines whose difference of direction is to be measured, as at B in the figure. A plumb-line must be suspended from under the center. Dropping a stone is an imperfect substitute for this. Set the instru-

FIG. 241.



ment so that its *lower* parallel plate may be as nearly horizontal as possible. The levels will serve as guides if the four parallel-plate screws be

first so screwed up or down that equal lengths of them shall be above the upper plate. Then level the instrument carefully. Direct the telescope to a rod, stake, or other object, A in the figure, on one of the lines which form the angle. Tighten the clamps, and by the tangent-screw move the telescope so that the intersection of the cross-hairs shall very precisely bisect this object. Note the reading of the vernier. Then loosen the clamp of the vernier, and direct the telescope on the other line (as to C) precisely as before, and again read. The difference of the two readings will be the desired angle, A B C. Thus, if the first reading had been  $40^\circ$  and the last  $190^\circ$ , the angle would be  $150^\circ$ . If the vernier had passed  $360^\circ$  in turning to the second object,  $360^\circ$  should be added to the last reading before subtracting. Thus, if the first reading had been  $300^\circ$ , and the last reading  $90^\circ$ , the angle would be found by calling the last reading, as it really is,  $360^\circ + 90^\circ = 450^\circ$ , and then subtracting  $300^\circ$ .

It is best to sight first to the left-hand object and then to the right-hand one, turning "with the sun" or like the hands of a watch, since the numbering of the degrees usually runs in that direction.

It is convenient, though not necessary, to begin by setting the

vernier at zero by the upper movement (that of the vernier-plate on the circle), and then, by means of the lower motion (that of the whole instrument on its axis), to direct the telescope to the first object. Then fasten the lower clamp, and sight to the second object as before. The reading will then be the angle desired. An objection to this is that the two verniers seldom read alike.\*

After one or more angles have been observed from one point, the telescope must be directed back to the first object, and the reading to it noted, so as to make sure that it has not slipped. A watch-telescope renders this unnecessary.

The error arising from the instrument not being set precisely over the center of the station will be greater the nearer the object sighted to. Thus, a difference of one inch would cause an error of only 3" in the apparent direction of an object a mile distant, but one of nearly 3' at a distance of a hundred feet.

**330. Reduction of High and Low Objects.** When one of the objects sighted to is higher than the other, the "plunging telescope" of this instrument causes the angle measured to be the true horizontal angle desired—i. e., the same angle as if a point exactly under the high object and on a level with the low object (or *vice versa*) had been sighted to. For the telescope has been caused to move in a vertical plane by the third adjustment, and the angle measured is therefore the angle between the vertical planes which pass through the two objects, and which "project" the two lines of sight on the same horizontal plane.

This constitutes the great practical advantage of these instruments over those which are held in the planes of the two objects observed, such as the sextant and the "circle," much used by the French.

**331. Notation of Angles.** The angles observed may be noted in various ways. Thus, the observation of the angle  $ABC$ , in

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\* The learner will do well to gauge his own precision and that of the instrument (and he may rest assured that his own will be the one chiefly in fault) by measuring, from any station, the angles between successive points all around him, till he gets back to the first point, beginning at different parts of the circle for each angle. The sum of all these angles *should* exactly equal  $360^\circ$ . He will probably find quite a difference from that.

Fig. 241, may be noted "At B, from A to C,  $150^\circ$ ," or, better, "At B, between A and C,  $150^\circ$ ." In column form, this becomes

Between A  $150^\circ$  and C.

At        B

When the vernier had been set at zero before sighting to the first object, and other objects were then sighted to, those objects, the readings to which were less than  $180^\circ$ , will be on the left of the first line, and those to which the readings were more than  $180^\circ$  will be on its right, looking in the direction in which the survey is proceeding, from A to B, and so on.

In surveying a farm, the angle of deflection at station, or the traverse angle, may be noted, together with the lengths of the courses.

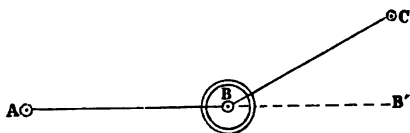
**332. To repeat an Angle.** Begin as in Art. 329, and measure the angle as there directed. Then unclamp below, and turn the circle around till the telescope is again directed to the first object, and made to bisect it precisely by the lower tangent-screw. Then unclamp above and turn the vernier-plate till the telescope again points to the second object, the first reading remaining unchanged. The angle will now have been measured a second time, but on a part of the circle adjoining that on which it was first measured, the second arc beginning where the first ended. The difference between the first and last readings will therefore be twice the angle.

This operation may be repeated a third, a fourth, or any number of times, always turning the telescope back to the first object by the lower movement (so as to start with the reading at which the preceding observation left off), and turning it to the second object by the upper movement. Take the difference of the first and last readings and divide by the number of observations.

The advantage of this method is that the errors of *observation* (i. e., sighting sometimes to the right and sometimes to the left of the true point) balance each other in a number of repetitions, while the constant error of *graduation* is reduced in proportion to this number. This beautiful principle has some imperfections in practice, probably arising from the slipping and straining of the clamps.

**333. Angles of Deflection.** The angle of deflection of one line from another is the angle which one line makes with the other line produced. Thus, in the figure, the angle of deflection of  $BC$  from  $AB$  is  $B'BC$ . It is evidently the supplement of the angle  $ABC$ .

FIG. 242.



To measure it with the *Transit*, set the instrument at  $B$ , direct the telescope to  $A$ , and then turn it over. It will now point in the direction of  $AB$  produced, or to  $B'$ , if the second adjustment has been performed. Note the reading. Then direct the telescope to  $C$ . Note the new reading, and their difference will be the required angle of deflection,  $B'BC$ .

If the vernier be set at zero before taking the first observation, the readings for objects on the right of the first line will be less than  $180^\circ$ , and more than  $180^\circ$  for objects on the left, conversely to Art. 331.

**334. Line-Surveying.** The survey of a line, such as a road, etc., can be made by the transit with great precision, measuring the angle which each line makes with the preceding line, and noting their lengths, and the necessary offsets on each side.

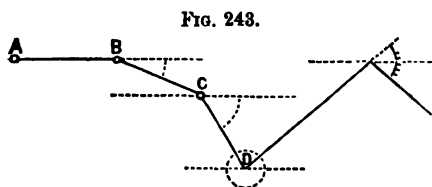
Short lines of sight should be avoided, since a slight inaccuracy in setting the center of the instrument exactly over or under the point previously sighted to would then much affect the angle. Very great accuracy can be obtained by using three tripods. One would be set at the first station and sighted back to from the instrument placed at the second station, and a forward sight be then taken to the third tripod placed at the third station. The instrument would then be set on this third tripod, a back-sight taken to the tripod remaining on the second station, and a fore-sight taken to the tripod brought from the first station to the fourth station, to which the instrument is next taken, and so on. This is especially valuable in surveys of mines.

The field-notes may be taken as directed in compass-surveying, the angles taking the place of the bearings. The "checks by

intersecting bearings," before explained, should also be employed. The angles made on each side of the stations may both be measured, and the equality of their sum to  $360^\circ$  would at once prove the accuracy of the work.

If the magnetic bearing of any one of the lines be given, and that of any of the other lines of the series be required, it can be deduced by constructing a diagram, or by modifications of the rules given for the reverse object.

**335. Traversing; or, surveying by the Back-Angle.** This is a method of observing and recording the different directions of suc-



cessive portions of a line (such as a road, the boundaries of a farm, etc.), so as to read off on the instrument, at each station, the angle which each line makes—not with the pre-

ceding line—but with the first line observed, or some other constant line. This line is, therefore, called the *meridian* of that survey.

The operation consists essentially in taking each back-sight by the lower motion (which turns the circle without changing the reading), and taking each forward sight by the upper motion, which moves the vernier over the arc measuring the new angle; and thus adds it to or subtracts it from the previous reading.

Set up the instrument at some station, as B; put the vernier at zero, and, by the lower motion, sight back to A. Tighten the lower clamp, reverse the telescope, loosen the upper clamp, sight to C by the upper motion, and clamp the vernier-plate again. Remove the instrument to C, sight back to B by the lower motion. Then clamp below, reverse the telescope, loosen the upper clamp, and sight to D by the upper motion. Then go to D and proceed as at C; and so on. The reading gives the angles measured to the right or "with the sun," as shown by the arcs in the figure.

Care should be taken to keep the same side of the instrument

ahead, and, if only one vernier is read, to read from the same vernier.

The chief advantage of this method is its greater rapidity in the field and in platting, the angles being all laid down from one meridian, as in compass-surveying.

**336. Use of the Compass.** The chief use of the compass attached to a transit is as a check on the observations; for the difference between the magnetic bearings of any two lines should be the same, approximately, as the angle between them, measured by the more accurate instruments. The bearing also prevents any ambiguity as to whether an angle was taken to the right or to the left.

The instrument may also be used like a simple compass, the telescope taking the place of the sights, and requiring similar tests of accuracy. A more precise way of taking a bearing is to turn the plate to which the compass-box is attached, till the needle points to zero, and note the reading of the vernier; then sight to the object, and again read the vernier. The bearing will thus be obtained more minutely than the divisions on the compass-box could give it.

**337. Ranging out Lines.** This is the converse of surveying-lines. The instrument is fixed over the first station with great precision, its telescope being very carefully adjusted to move in a vertical plane. A series of stakes, with nails driven in their tops, or otherwise well defined, are then set in the desired line as far as the power of the instrument extends. It is then taken forward to a stake three or four from the last one set, and is fixed over it, first by the plumb and then by sighting backward and forward to the first and last stake. The line is then continued as before. A good object for a long sight is a board painted like a target, with black and white concentric rings, and made to slide in grooves cut in the tops of two stakes set in the ground about in the line. It is moved till the vertical hair bisects the circles (which the eye can determine with great precision), and a plumb-line dropped from their center gives the place of the stake. "Mason and Dixon's Line" was thus ranged.

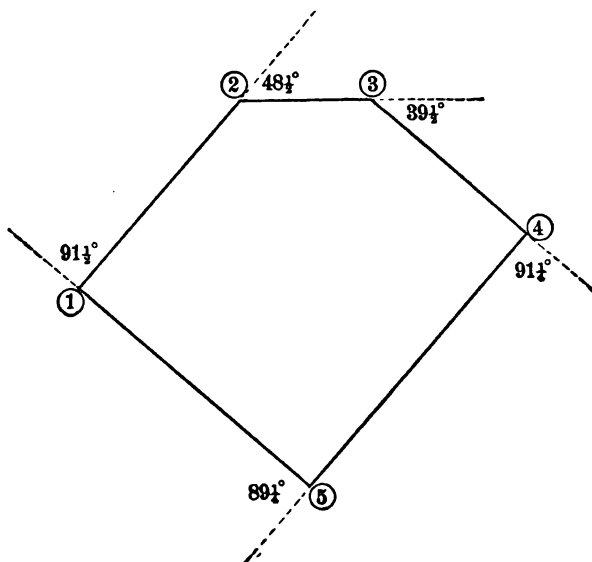
When the transit is used for ranging, its "Second Adjustment" is most important, to insure the accuracy of the reversal of its telescope.

**338. Farm-Surveying, etc.** A farm can be much more accurately surveyed with the transit than with the compass. The farm should be kept on the right hand, and then the angles measured will be the supplements of the interior angles. If the angles to the right be called *positive*, and those to the left *negative*, their algebraic sum should equal  $360^\circ$ .

If the boundary-lines be surveyed by "Traversing," the reading, on getting back to the last station and looking back to the first line, should be  $360^\circ$ , or  $0^\circ$ .

The content of any surface surveyed by "Traversing" with the transit can be calculated by the traverse-table, by the following modification: When the angle of deflection of any side from the first side, or meridian, is less than  $90^\circ$ , call this angle the bearing, find its latitude and departure, and call them both *plus*. When the angle is between  $90^\circ$  and  $180^\circ$ , call the difference between the

FIG. 244.





angle and  $180^\circ$  the bearing, and call its latitude *minus* and its departure *plus*. When the angle is between  $180^\circ$  and  $270^\circ$ , call its difference from  $180^\circ$  the bearing, and call its latitude *minus* and its departure *minus*. When the angle is more than  $270^\circ$ , call its difference from  $360^\circ$  the bearing, and call its latitude *plus* and its departure *minus*. Then use these as in getting the content of a compass-survey. The signs of the latitudes and departures follow those of the cosines and sines in the successive quadrants.

Fig. 244 is a plat of the survey worked out in Art. 255.

The following table gives the deflection angle at each station, the traverse angle (i. e., the angle which each line makes with the first one), and the reduced bearing, calling the first line (1 to 2) the meridian :

| STATIONS. | DEFLECTION ANGLES.    | TRAVERSE ANGLES.         | BEARINGS.                   |
|-----------|-----------------------|--------------------------|-----------------------------|
| 1         | $91\frac{1}{2}^\circ$ | $0^\circ$ or $360^\circ$ | North.                      |
| 2         | $48\frac{1}{2}^\circ$ | $48\frac{1}{2}^\circ$    | N. $48\frac{1}{2}^\circ$ E. |
| 3         | $89\frac{1}{2}^\circ$ | $88^\circ$               | N. $88^\circ$ E.            |
| 4         | $91\frac{1}{2}^\circ$ | $179\frac{1}{2}^\circ$   | S. $\frac{1}{2}^\circ$ E.   |
| 5         | $89\frac{1}{2}^\circ$ | $268\frac{1}{2}^\circ$   | S. $88\frac{1}{2}^\circ$ W. |

If the deflection angle at station 1 ( $91\frac{1}{2}^\circ$ ) be added to the traverse angle at station 5, the sum will be  $360^\circ$ .

Any side may be taken as the meridian of the survey.

If the true bearing of one side be known, the true bearings of the other sides may be determined by Art. 189.

The content is calculated by latitudes and departures, as in compass-surveying.

The latitudes and departures may be taken from the tables, interpolating for minutes as in Art. 242, or they may be calculated with a table of natural sines and cosines, as in Art. 240.

*Example.*

FIELD-BOOK.

| STATIONS. | ANGLES OF DEFLECTION. | DISTANCES IN CHAINS. |
|-----------|-----------------------|----------------------|
| 1         | $62^\circ 15'$        | 4.64                 |
| 2         | $86^\circ 38'$        | 3.60                 |
| 3         | $59^\circ 20'$        | 4.15                 |
| 4         | $80^\circ 6'$         | 4.22                 |
| 5         | $71^\circ 41'$        | 3.25                 |

**CALCULATION OF AREAS, CALLING COURSE 1 TO 3 THE MERIDIAN, AND USING  
SINES AND COSINES INSTEAD OF A TRAVERSE TABLE.**

| STATIONS. | BEARINGS.    | DISTANCES. | SINES. | COSINES. | LATI-<br>TUDES. |      | DEPART-<br>URES. |        | DOUBLE<br>LONGI-<br>TUDES. | DOUBLE AREAS.  |         |
|-----------|--------------|------------|--------|----------|-----------------|------|------------------|--------|----------------------------|----------------|---------|
|           |              |            |        |          | +               | -    | +                | -      |                            | +              | -       |
| 1         | + 00°, 00' + | 4.64       | .00000 | 1.00000  | 4.64            |      | 0.00             |        | 0.00                       | 0.0000         |         |
| 2         | + 86°, 38' + | 3.60       | .99827 | .05873   | 0.21            |      | 3.59             |        | + 3.59                     | .7539          |         |
| 3         | - 34°, 2' +  | 4.15       | .55968 | .82871   |                 | 3.44 | 2.32             |        | + 9.50                     |                | 32.6800 |
| 4         | - 46°, 4' -  | 4.22       | .72015 | .69382   |                 | 2.93 | 3.04             | + 8.78 |                            |                | 25.7254 |
| 5         | + 62°, 15' - | 3.25       | .88499 | .46561   | 1.52            |      | 2.87             | + 2.87 | 4.8624                     |                |         |
|           |              |            |        |          | 6.37            | 6.37 | 5.91             | 5.91   |                            | 5.1163         | 58.4054 |
|           |              |            |        |          |                 |      |                  |        |                            | 5.1163         |         |
|           |              |            |        |          |                 |      |                  |        |                            | 2)53.2891      |         |
|           |              |            |        |          |                 |      |                  |        |                            | Square chains, | 26.6445 |

**339.** When the lengths of the sides are measured with an engineer's chain, and the distances are determined in feet, the process of calculating the area is the same as for chains and decimals. The area is obtained in square feet instead of square chains, and to reduce it to acres it will be necessary to divide by 43560, the number of square feet in an acre.

**340. Platting.** Any of these surveys can be platted by any of the methods explained and characterized in Chapter III. A circular protractor may be regarded as a theodolite placed on the paper. "Platting Bearings" can be employed when the survey has been made by "Traversing." But the method of "Latitudes and departures" is by far the most accurate.

#### THE GRADIENTER.

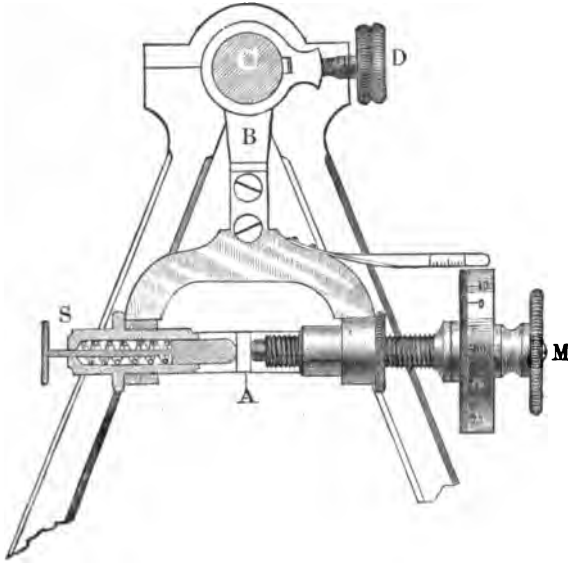
**341.** This is an attachment to the transit for determining grades and distances. It consists of an arm, attached to the axis of the telescope, and a micrometer-screw, by means of which the movement of the arm, and consequently of the telescope, can be accurately measured.

The arm is placed on the inside of one of the standards, and is attached to the telescope axis by means of a clamp-screw, so that it may be clamped or loosened at pleasure.

The method of measuring the movement of the arm is shown in Fig. 245.

C is a section of the axis of the telescope. B is the arm, which

FIG. 245.



is clamped to the axis by the screw D. M is the micrometer-screw. A is a lip projecting from a plate fastened to the standards.

The screw is accurately cut, so that one revolution of the screw will cause the horizontal cross-hair of the telescope to move over a given space (say one foot) on a rod held at a given distance, as 100 feet. The head of the screw is graduated into equal parts, usually 50 or 100. Above the graduated head is a scale so graduated that one revolution of the screw will move the head over one space on the scale. Thus the number of whole revolutions given to the screw may be read on the scale, and the parts of a revolution read on the graduated head.

The point of the screw presses against the lip, A, and is held firmly against it by the opposing spiral spring, S.

When the arm is made fast to the axis by the clamp-screw, D, and the grader-screw, M, is turned, it will turn the telescope vertically on its axis, and the distance which the horizontal cross-

hair will pass over on a rod, toward which the telescope is pointed, will vary directly with the distance from the transit to the rod.

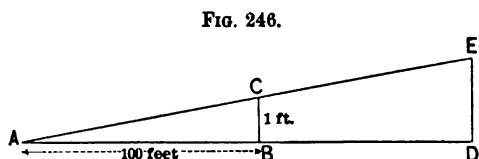
**342. To establish Grades.** Let us suppose that one revolution of the gradienter-screw will move the horizontal cross-hair over a space of one foot, on a rod held at a distance of 100 feet from the transit. Then, to set grades, we have only to level the telescope, clamp the gradienter-arm, and turn the micrometer-screw through as many divisions of the head (graduated into 100 parts) as there are hundredths of a foot rise or fall per hundred feet of horizontal distance; raising the cross-hair for an up-grade, and lowering it for a down-grade. The line of sight will then be on the required grade.

If the transit be set over a point of the required grade-line, set the target on the rod at the height of the center of the telescope-axis above the given point, and then the bottom of the rod, held at any point on the line, will be at a point in the desired grade-line when the horizontal cross-hair bisects the target.

Thus, if the grade is to be 1.64 feet per hundred, turn the screw one entire revolution and 64 of the divisions on the graduated head, and the line of sight will then be on the required grade.

**343. To measure Distances.** When the ground is level or approximately so, see what space on the rod the horizontal cross-hair moves over for one revolution of the gradienter-screw. Then the distance in feet will be equal to the space on the rod, expressed in feet and decimals, multiplied by 100.

Thus, if the space on the rod, moved over by the cross-hair



for one revolution of the gradienter-screw, was 4.27 feet, the distance at which the rod was held was 427 feet.

For, in Fig. 246, let A be the position of the transit; CB, the reading on the rod, held at a distance of 100 feet, for one revolution of the screw; and DE the space passed over on the rod for one revolution of the screw

when the rod is held at the unknown distance  $AD$ . It is evident that the triangles  $ABC$  and  $ADE$  are similar, and that

$$CB : AB :: ED : AD,$$

$$\text{or, } 1 : 100 :: 4.27 : 427.$$

If the rod sighted to is only graduated to feet—as an ordinary transit-rod—find how many revolutions and parts of revolutions will move the horizontal cross-hair over a whole number of feet on the rod. Then, since one revolution of the screw will move the cross-hair over a space of one foot on the rod at a distance of 100 feet, we have the proportion: *As the number of revolutions of the screw (whole numbers and decimals) is to 100 feet, so is the number of feet passed over on the rod by the cross-hair to the required distance.* For, from Fig. 246 we have, as before:

$$CB : AB :: DE : AD.$$

$CB$  now represents what the reading on the rod (in feet and decimals), held at a distance of 100 feet, would be for the given number of revolutions:  $AB$  is 100',  $DE$  is the reading on the rod in feet, and  $AD$  is the required distance.

Suppose, for example, the grader-screw be turned 1.25 time, and the space passed over on the rod by the cross-hair be 3 feet. Then we have:

$$1.25 : 100 :: 3 : 240.$$

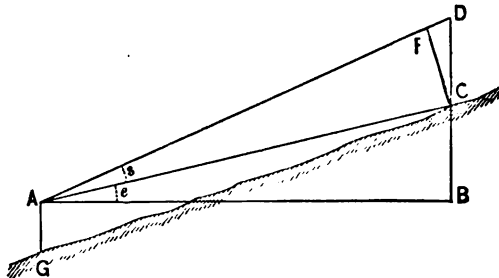
$\therefore$  The required distance is 240 feet.

*Problem.*—When no graduated rod is available, to determine a distance by using, in place of a rod, a stick whose length can afterward be measured.

On sloping ground, the methods given will apply, if the rod be held perpendicular to the line of sight. This, however, is not easily done. It will be better to apply methods specially adapted to sloping ground.

**344. On Sloping Ground.** In Fig. 247, let  $A$  be the position of the tran-

FIG. 247.



sit; G the point over which it is set; C where the rod is held; A B a horizontal line through the axis of the telescope; A C the distance from the horizontal axis of the telescope to the foot of the rod; and C D the distance, on a vertical rod, passed over by the horizontal cross-hair for one revolution of the gradienter-screw. Let C F be perpendicular to A C, and D B to A B.

Represent the angle of elevation, B A C, by  $e$ , the angle C A D by  $s$ , and the distance D C by  $k$ . Then we have :

$$D B = D C + C B.$$

$$\therefore A B \tan. (s + e) = k + A B \tan. e,$$

$$\text{and } A B = \frac{k}{\tan. (s + e) - \tan. e}.$$

For convenience of computation, this may be put in another form. Add and subtract  $100 k$ , and we have :

$$A B = 100 k - 100 k + \frac{k}{\tan. (s + e) - \tan. e}.$$

$$\text{And, since } \tan. s = \frac{1}{100},$$

$$A B = 100 k - k (100 \sin. e + \cos. e) \sin. e.*$$

TABLE FOR GRADIENTER.

| ANGLE OF ELEVATION. | (100 SIN. $e$ + COS. $e$ )<br>× SIN. $e$ . |
|---------------------|--------------------------------------------|
| 0°                  | ·0                                         |
| 1°                  | ·1                                         |
| 2°                  | ·2                                         |
| 3°                  | ·3                                         |
| 4°                  | ·5                                         |
| 5°                  | ·8                                         |
| 6°                  | 1·2                                        |
| 7°                  | 1·6                                        |
| 8°                  | 2·1                                        |
| 9°                  | 2·6                                        |
| 10°                 | 3·2                                        |
| 11°                 | 3·8                                        |
| 12°                 | 4·5                                        |
| 13°                 | 5·3                                        |
| 14°                 | 6·1                                        |
| 15°                 | 7·0                                        |
| 16°                 | 7·9                                        |
| 17°                 | 8·8                                        |
| 18°                 | 9·8                                        |
| 19°                 | 10·9                                       |
| 20°                 | 12·0                                       |

The quantity  $(100 \sin. e + \cos. e) \sin. e$ , for angles from  $1^\circ$  to  $20^\circ$  will be found in the table for the gradienter. Hence the rule :

Multiply the rod-reading by 100, and deduct the product of the rod-reading by the tabular number corresponding to the angle of elevation,  $e$ . The result will be the horizontal distance A B.

*Example.* Angle of elevation,  $4^\circ$ ; rod-reading, 2·63 feet.

$$2\cdot63 \times 100 = 263$$

$$2\cdot63 \times .5 = 1\cdot3$$

Horizontal distance, 261·7

The table for the correction is computed to tenths only, as the unavoid-

\* This formula and table is by Prof. T. W. Wright.

able errors in using the instrument would render any more exact computation useless.

For ordinary cases, when the angle of elevation is small, the computation for the distance and correction can be made mentally.

**345.** The horizontal distance,  $AB$ , is the one almost always required, as all measurements of distances in surveying and engineering should be made horizontally.

The distance from the transit to the point at which the rod is held (i. e.,  $AC$ ) is equal to the horizontal distance,  $AB$ , divided by  $\cos. e$ .

The distance  $GC$  may be found by solving the triangle  $CAG$ , of which the sides  $AG$  and  $AC$ , and the included angle  $CAG$ , are known.

When the angle  $e$  is an angle of depression, the top of the rod is taken for the point  $C$ , and the distance  $CD$  is measured downward from the top of the rod.

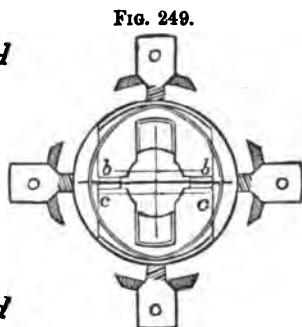
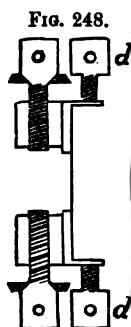
In using the micrometer-screw, care must be taken, when measuring, to always turn the screw in the same direction, in order to avoid any lost motion in the screw. In determining the space passed over by the cross-hair for one revolution of the screw, set the screw back of the first reading, and bring it up by turning the screw in the same direction in which it is to be turned for making the measurement.

### THE STADIA OR TELEMETER.

**346.** On the cross-hair ring of the telescope stretch two more horizontal cross-hairs of spider-web or platinum wire, at equal distances above and below the original one. The two additional wires are called *Stadia Wires*. The stadia wires may be either fixed or adjustable. In the former case they may be attached directly to the cross-hair ring. When they are adjustable, each may be fastened to a separate slide, actuated by a capstan-screw on the outside of the telescope-tube, as shown in Figs. 248 and 249.

The slides to which the stadia wires  $bb$  and  $cc$  are attached are held apart by the hoop-spring, shown in the figure, and are adjusted by the capstan-screws  $dd$ .

It is evident that, in looking through the telescope at a graduated rod, a certain portion



of the rod will be intercepted between the stadia wires, and that the greater the distance at which the rod is held, the longer will be the space on the rod intercepted by the stadia wires.

Referring to Art. 287,

Fig. 201, we see that the

objective of the telescope forms an image, B, of the arrow, A. A may represent the part of the rod intercepted by the stadia wires, and B the distance between the wires. The farther the rod is carried from the telescope, the nearer the image is formed to the objective. If the rod were at an infinite distance, the image would be formed at the *principal focus* of the objective.

Call the distance of the principal focus from the lens,  $f$ ; the distance from the lens to the rod held at any point,  $p$ ; the distance from the lens to the image,  $q$ ; the space intercepted on the rod by the stadia wires,  $k$ ; and the distance apart of the stadia wires,  $a$ .

As  $p$  increases,  $k$  increases,  $q$  decreases, and  $a$  remains constant.

From similar triangles, Fig. 201, we have :

$$p : q :: k : a, \quad [1.]$$

and from the principles of optics—

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}. \quad [2.]$$

$$\text{From [1]} \quad \frac{p}{q} = \frac{k}{a}.$$

$$\text{From [2]} \quad \frac{p}{q} = \frac{p}{f} - 1.$$

$$\therefore \frac{p}{f} - 1 = \frac{k}{a}.$$

$$\text{and } p = \frac{f}{a}k + f. \quad [3.]$$



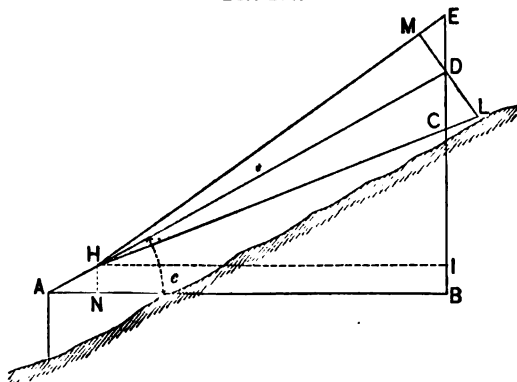
Formula [3] is not perfectly accurate, as  $p$  and  $q$  are measured from the surface of the lens instead of its center, and the objective of the telescope is not a simple double-convex lens. It is, however, sufficiently exact for this purpose.

We see by the formula [3] that, as  $f$  and  $a$  are constants, the distance,  $p$ , from the objective to the rod is equal to the reading on the rod, multiplied by a constant quantity, plus the principal focal distance of the objective. To obtain the distance from the center of the instrument to the rod, it is also necessary to add the distance from the center of the instrument to the objective. Call this distance  $c$ . Then, for the distance from the center of the instrument to the rod, we have :

$$\text{distance} = \frac{f}{a} k + f + c. \quad [4.]$$

The distance from the objective to the center of the instrument is not precisely the same for all lengths of sight. The farther off the object sighted to is, the nearer the image will be formed to the objective, and hence the objective must be drawn in, in order that the image may be formed at the cross-hairs. When the object sighted to is near, the image is formed farther from the objective, and the objective-slide must be moved out in order that the image may be formed at the cross-hairs. Hence, we see that the quantity  $c$  is not rigidly constant. The difference in value, however, is not enough to be taken into consideration. A mean value of  $c$  can be determined by sighting to some object at a distance of the mean length of sight (say five hundred feet), and then measuring the distance from the objective to the center of the telescope-axis.

**FIG. 250.**



**347.** Formula [4] is for level ground. For sloping ground, this must be modified. In Fig. 250 let A be the center of the telescope-axis; C E, the reading on the rod; D, the point on the rod where the center cross-hair intersects the rod; A B, the horizontal distance; H, a point in front of the object-glass, and at a distance equal to its focal length;  $e$ , the angle of elevation; M L, perpendicular to the line of sight;  $f$ ,  $a$ ,  $c$ , and  $k$  as in [4]. Then we have:

$$M L = C E \cos. e = k. \cos. e \text{ and } H D = \frac{f}{a} k \cos. e.$$

$$H I = H D \cos. e = \frac{f}{a} k \cos.^2 e.$$

$$A B = A N + N B (= H I).$$

$$\therefore A B = \frac{f}{a} k \cos.^2 e + (c + f) \cos. e. \quad [5.]$$

The height  $B D = A B \tan. e$

$$B D = \frac{f}{a} k \frac{\sin. 2e}{2} + (c + f) \sin. e. \quad [6.]$$

To find the value of  $a$  in any case, measure off from the point over which the instrument is set a base-line, B (say one thousand feet), and hold the stadia-rod at the farther end. Let the reading on the rod be  $k'$ .

$$\text{Then, by [4]} \quad B = \frac{f}{a} k' + f + c,$$

$$\text{and } a = \frac{f k'}{B - f - c}.$$

Substituting this value of  $a$  in equations [5] and [6], we have:

$$\text{Horizontal distance} = \frac{k}{k'} (B - f - c) \cos.^2 e + (c + f) \cos. e. \quad [7.]$$

$$\text{Difference of level} = \frac{k}{2 k'} (B - f - c) \sin. 2e + (c + f) \sin. e. \quad [8.]$$

**348.** The Stadia-Tables\* given in this volume were calculated from formulas [7] and [8], using the following values:

The measured base,  $B = 1,000$  feet, and  $k' =$  the reading on the rod for that distance—i. e., the distance indicated by the stadia-reading is 1,000 feet.

---

\* Calculated by Alfred Noble and William T. Casgrain, and used on the United States Lake Survey.

$$(c + f) = 1.4 \text{ feet.}$$

The quantities in the columns headed  $a$  and  $b$  are computed respectively from the expressions  $(c + f) \cos. e$ , and  $(c + f) \sin. e$ , in the formulas. They are constant for all readings if the angle  $e$  remains the same.

The horizontal distances, and the differences of level, are computed by the tables in a manner similar to that employed in calculating latitudes and departures with a table.

*Example.* Let  $e = 4^\circ 27'$ , and  $k =$  reading corresponding to 1,384 feet when the ground is horizontal.

Take from the table as follows:

| HORIZONTAL DISTANCE.     |                 | DIFFERENCE OF LEVEL.     |                |
|--------------------------|-----------------|--------------------------|----------------|
| For 1,000.....           | 992.6           | For 1,000.....           | 077.2          |
| " 300.....               | 297.78          | " 300.....               | 23.17          |
| " 80.....                | 79.407          | " 80.....                | 6.180          |
| " 4.....                 | 3.9708          | " 4.....                 | .3090          |
| " $(c + f) \cos. e$ .... | 1.3958          | " $(c + f) \sin. e$ .... | .1086          |
|                          | <hr/> 1375.1531 |                          | <hr/> 106.9676 |

The difference of level given by formula [8] is D B, the difference between the elevation of the axis of the telescope at A and the point where the central cross-wire strikes the rod at D. The point D upon the rod should be taken at a height above the ground equal to the height of the telescope-axis (A) above the ground at that point. Then the difference of level, D B, will be the difference in elevation of the ground at the two points.

If the point D is not taken as above, the difference between the height of the instrument and the height of the point D above the ground, must be applied as a correction to the difference of level obtained by the formula in order to get the true difference in elevation of the ground at the two points.

**349.** The stadia-wires may be adjusted to use with a rod already graduated to feet and decimals, or, if the wires are fixed, a rod may be graduated to suit the wires.

When the wires are fixed the necessity of verifying their distance at the beginning and end of each survey, and the introduction of an error due to their changing during the work is avoided.

The advantage of having the wires adjustable is that they may be set so as to use any stadia-rod previously graduated, or a self-reading level-rod.

**350.** The method to be used in graduating a rod will depend upon the table to be used in the reduction of the notes. If the tables given in this volume are to be used, the following method should be adopted :

A level base (B) of 1,000 feet should be measured, and the instrument set up at one end of the base and the rod at the other.

To graduate a rod for fixed wires, divide the distance intercepted on the rod into ten equal parts, each of which will represent 100 feet.

Generally, when the wires are not fixed, they are adjusted so that one foot is included between the wires at a given distance (50 or 100 feet) plus the constant  $(c + f)$ . Suppose the space included between the wires was one foot, at a distance from the center of the instrument of 100 feet  $+ (c + f)$ . Then, if the reading on the rod held at some unknown distance was 3.46 feet, the distance would be 346 feet  $+ (c + f)$ .

If the wires are fixed, measure off from the center of the instrument 500 feet  $+ (c + f)$ , and note the space on the rod, intercepted by the cross-hairs at that distance. Divide this space into five equal parts, subdivide the parts to tenths and hundredths, and graduate the remainder of the rod with similar divisions. This rod can then be used in the same way as the rod, graduated to feet, was in the first case. Suppose, on holding up this rod at an unknown distance, that the stadia-wires intercepted 3.67 of the parts. Then the distance is 367 feet  $+ (c + f)$ .

If the wires be adjustable, and it is desired to use a rod previously graduated, set up the rod and instrument as before and adjust the distance between the wires until the reading on the rod gives the length of the base—i. e., 1,000 feet. Readings taken with the above rods and reduced with the aid of tables given will give correct results only with instruments for which  $(f + c) = 1.4$  foot, the tables having been computed assuming that value. With instruments for which  $(f + c)$  has a different value there will be an error, not, how-

ever, greater than the small difference between 1.4 and this constant for the instrument used.

An inspection of the formulæ shows that the distance intercepted on the rod varies directly with its distance from a point a distance  $(f+c)$  in front of the instrument. If the rod were held at a distance 200 feet plus  $(f+c)$ , the distance intercepted on the rod would be just twice as great as when the rod was held at a distance 100 feet plus  $(f+c)$ .

The distance is more conveniently read when one of the wires, usually the lower, is set upon an even division of the rod, than when the central wire is set on the division corresponding to the height of the instrument. If the reading be made in the part of the rod near which the center wire should be set in reading the vertical angle, there will be no appreciable error in the distance read. But before reading the vertical angle the center wire should be set as described above.

The formulæ for the reduction of notes, taken using rods graduated according to this method, may be written as follows by substituting  $R$  for  $\frac{f}{a}k$  in [5] and [6],  $R$  being the distance as read on the rod.

$$A B = R \cos.^2 e + (f+c) \cos. e. \quad [5^1.]$$

$$B D = R \frac{1}{2} \sin. 2 e + (f+c) \sin. e. \quad [6^1.]$$

The best tables for the reduction of notes by the above formulæ are W. Jordan's *Tables Tachymétriques*, published by Gauthier-Villars, Quai des Augustins 55, Paris. These tables give  $R \cos.^2 e$  and  $R \frac{1}{2} \sin. 2 e$  for values of  $R$  from 10 to 250 and for values of  $e$  as high as are ever needed.

In all graphic diagrams for the reduction of stadia notes  $R \cos.^2 e$  and  $R \frac{1}{2} \sin. 2 e$  are the quantities determined. The quantities  $(f+c) \cos. e$  and  $(f+c) \sin. e$  must be added as a correction in the use either of the above tables or graphic diagrams.

The rod may be supplied with one or two targets, or may be used as a "speaking-rod"—that is, it may be graduated and marked so as to be read by the observer at the instrument.

For forms of targets, and methods of graduating and marking rods, see subject "Rods," Chapter VIII.

## CHAPTER V.

### OBSTACLES IN ANGULAR SURVEYING.

**353.** THE obstacles, such as trees, houses, hills, valleys, rivers, etc., which prevent the direct alinement or measurement of any desired course, can be overcome much more easily and precisely with any angular instrument than with the chain, methods for using which were explained in Chapter II. They will, however, be taken up in the same order. As before, the given and measured lines are drawn with fine full lines; the visual lines with broken lines; and the lines of the result with heavy full lines. Part of the demonstrations of the problems are given, and part are left as exercises for the student.

### PERPENDICULARS AND PARALLELS.

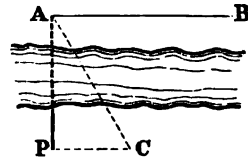
**354. Erecting Perpendiculars.** *To erect a perpendicular to a line at a given point,* set the instrument at the given point, and, if it be a compass, direct its sights on the line, and then turn them till the new bearing differs  $90^\circ$  from the original one. A convenient approximation is to file notches in the compass-plate, at the  $90^\circ$  points, and stretch over them a thread, sighting across which will give a perpendicular to the direction of the sights.

The *transit* being set as above, note the reading of the vernier, and then turn it till the new reading is  $90^\circ$  more or less than the former one.

**355.** *To erect a perpendicular to an inaccessible line, at a given point of it.* Let  $AB$  be the line and  $A$  the point. Calculate the distance from  $A$  to any point  $C$ , and the angle  $CAB$ , by the

method of Art. 381. Set the instrument at C, sight to A, turn an angle =  $\angle CAB$ , and measure in the direction thus obtained a distance  $CP = CA \cdot \cos. \angle CAB$ . PA will be the required perpendicular.

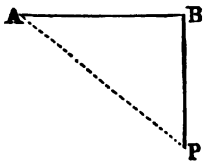
FIG. 251.



**356. Letting fall Perpendiculars. To**

*let fall a perpendicular to a line from a given point.* With the compass, take the bearing of the given line, and then from the given point run a line, with a bearing differing  $90^\circ$  from the original bearing, till it reaches the given line.

FIG. 252.



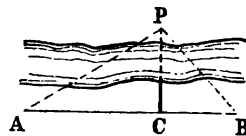
With the *transit*, set it at any point of the given line, as A, and observe the angle between this line and a line thence to the given point, P. Then set at P, sight to the

former position of the instrument, and turn a number of degrees equal to what the observed angle at A wanted of  $90^\circ$ . The instrument will then point in the direction of the required perpendicular PB.

**357. To let fall a perpendicular to a line from an inaccessible point.** Let AB be the line and P the point. Measure the angles  $\angle PAB$  and  $\angle PBA$ . Measure AB. The angles  $\angle APC$  and  $\angle BPC$  are known, being the complements of the angles measured. Then

$$\text{is } AC = AB \cdot \frac{\tan. APC}{\tan. APC + \tan. BPC}$$

FIG. 253.



*Proof:*  $AC = PC \cdot \tan. APC$ ; and  $CB = PC \cdot \tan. BPC$  [Trigonometry, Art. 4].

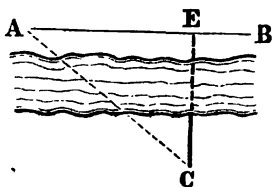
Hence  $AC : CB :: \tan. APC : \tan. BPC$ ; and

$$AC : AC + CB :: \tan. APC : \tan. APC + \tan. BPC.$$

Consequently, since  $AC + CB = AB$ ,  $AC = AB \cdot \frac{\tan. APC}{\tan. APC + \tan. BPC}$ .

**358. To let fall a perpendicular to an inaccessible line from a given point.** Let C be the point and AB the line. Calculate the

FIG. 254.

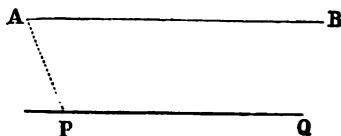


angle  $CAB$  by the method of Art. 381. Set the instrument at  $C$ , sight to  $A$ , and turn an angle  $= 90 - CAB$ . It will then point in the direction of the required perpendicular,  $CE$ .

**359. Running Parallels.** *To trace a line through a given point parallel to a given line.* With the compass, take the bearing of the given line, and then, from the given point, run a line with the same bearing.

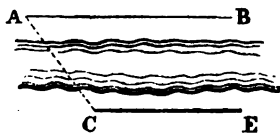
With the *transit* or *theodolite*, set it at any convenient point of the given line, as  $A$ , direct it on this line, and note the reading. Then turn the vernier till the cross-hairs bisect the given point,  $P$ . Take the instrument to this point and sight back to the former station, by the lower motion, without changing the reading. Then move the vernier till the reading is the same as it was when the telescope was directed on the given line, or  $180^\circ$  different. It will then be directed on  $PQ$ , a parallel to  $AB$ , since equal angles have been measured at  $A$  and  $P$ . The manner of reading them is similar to the method of "Traversing."

FIG. 255.



**360.** *To trace a line through a given point parallel to an inaccessible line.* Let  $C$  be the given point and  $AB$  the inaccessible line. Find the angle  $CAB$ , as in Art. 381. Set the instrument at  $C$ , direct it to  $A$ , and then turn it so as to make an angle with  $CA$  equal to the supplement of

FIG. 256.



the angle  $CAB$ . It will then point in a direction,  $CE$ , parallel to  $AB$ .



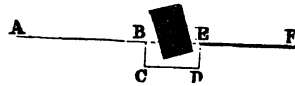
OBSTACLES TO ALINEMENT.

A. TO PROLONG A LINE.

**361.** The instrument being set at the farther end of a line and directed back to its beginning, the sights of the *compass*, if that be used, will at once give the forward direction of the line. A distant point being thus obtained, the compass is taken to it and the process repeated. The use of the *transit* for this purpose has been fully explained.

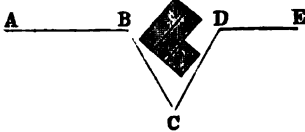
**362. By Perpendiculars.** When a tree or house obstructing the line is met with, place the instrument at a point B of the line, and set off there a perpendicular to C; set off another at C to D, a third at D to E, making  $DE = BC$ , and a fourth at E, which last will be in the direction of AB prolonged. If perpendiculars can not be conveniently used, let BC and DE make any equal angles with the line AB, so as to make CD parallel to it.

FIG. 257.



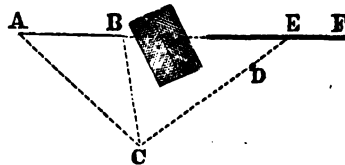
**363. By an Equilateral Triangle.** At B turn aside from the line at an angle of  $60^\circ$ , and measure some convenient distance BC. At C turn  $60^\circ$  in the contrary direction, and measure a distance  $CD = BC$ . Then will D be a point in the line AB prolonged. At D turn

FIG. 258.



$60^\circ$  from CD prolonged, and the new direction will be in the line of AB prolonged. This method requires the measurement of one angle less than the preceding.

FIG. 259.

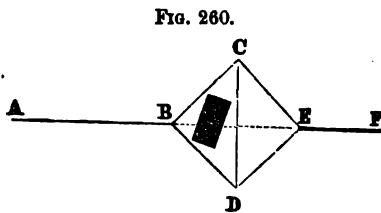


**364. By Triangulation.** Let AB be the line to be prolonged. Choose some station C, whence can be seen A, B, and a point beyond the obstacle. Measure AB

and the angles  $A$  and  $B$  of the triangle  $ABC$ , and thence calculate the side  $AC$ . Set the instrument at  $C$ , and measure the angle  $ACD$ ,  $CD$  being any line which will clear the obstacle. Let  $E$  be the desired point in the lines  $AB$  and  $CD$  prolonged. Then in the triangle  $ACE$  will be known the side  $AC$  and its including angles, whence  $CE$  can be calculated. Measure the resulting distance on the ground, and its extremity will be the desired point  $E$ . Set the instrument at  $E$ , sight to  $C$ , and turn an angle equal to the supplement of the angle  $AEC$ , and you will have the direction,  $EF$ , of  $AB$  prolonged.

**365. When the Line to be prolonged is inaccessible.** In this case, before the preceding method can be applied, it will be necessary to determine the lengths of the lines  $AB$  and  $AC$ , and the angle  $A$ , by the method given in Art. 381.

**366. To prolong a Line with only an Angular Instrument.** This



may be done when no means of measuring any distance can be obtained. Let  $AB$  be the line to be prolonged. Set the instrument at  $B$  and deflect angles of  $45^\circ$  in the directions  $C$  and  $D$ . Set at some point,  $C$ , on one of these lines and

deflect from  $CB$   $45^\circ$ , and mark the point  $D$  where this direction intersects the direction  $BD$ . Also, at  $C$ , deflect  $90^\circ$  from  $B$ . Then, at  $D$ , deflect  $90^\circ$  from  $DB$ . The intersections of these last directions will fix a point  $E$ . At  $E$  deflect  $135^\circ$  from  $EC$  or  $ED$ , and a line  $EF$ , in the direction of  $AB$ , will be obtained and may be continued.\*

#### B. TO INTERPOLATE POINTS IN A LINE.

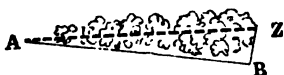
**367.** The instrument being set at one end of a line and directed to the other, intermediate points can be found, etc. If a valley in-

\* This ingenious contrivance is due to Mr. R. Hood, in whose practice, while running an air-line for a railroad, the necessity occurred.

tervenes, the sights of the compass (if the compass-plate be very carefully kept level crosswise), or the telescope of the transit, answer as substitutes for the plumb-line.

**368. By a Random Line.** When a wood, hill, or other obstacle prevents one end of the line, Z, from being seen from the other, A, run a random line A B with the compass or transit, etc., as nearly in the desired direction as can be guessed, till you arrive opposite the point Z. Measure the error, B Z, at right angles to A B, as an offset. Multiply this error by  $57\frac{3}{10}$ , and divide the product by the distance A B. The quotient will be the degrees and decimal parts of a degree contained in the angle B A Z. Add or subtract this angle to or from the bearing or reading with which A B was run, according to the side on which the error was, and start from A, with this corrected bearing or reading, to run another line, which will come out at Z, if no error has been committed.

FIG. 261.



*Example:* A random line was run, by compass, with a bearing of S.  $80^{\circ}$  E. At twenty chains distance a point was reached opposite to the desired point, and ten links distant from it on its right. Required the correct bearing.

*Ans.* By the rule,  $\frac{10 \times 57^{\circ}.3}{2,000} = 0^{\circ}.2865 = 17'$ . The correct bearing is therefore S.  $80^{\circ} 17'$  E. If the transit had been used, its reading would have been changed for the new line by the same  $17'$ . A simple diagram of the case will at once show whether the correction is to be added to the original bearing or angle, or subtracted from it.

If trigonometrical tables are at hand, the correction will be more precisely obtained from this equation:  $\text{Tan. } B A Z = \frac{B Z}{A B}$ . In this example,  $\frac{B Z}{A B} = \frac{10}{2,000} = .005 = \text{tan. } 17'$ .

The  $57^{\circ}.3$  rule, as it is sometimes called, may be variously modified. Thus, multiply the error by  $86^{\circ}$ , and divide by one and a half time the distance; or, to get the correction in minutes,

multiply by 3,438 and divide by the distance; or, if the error is given in feet and the distance in four-rod chains, multiply the former by 52 and divide by the distance, to get the correction in minutes.

The correct line may be run with the bearing of the random line by turning the vernier for the correction.

**369. By Latitudes and Departures.** When a single line, such as

FIG. 262.



A B, can not be run so as to come opposite to the given point Z, proceed thus with the *compass*: Run any number of zigzag courses, A B, B C, C D, D Z, in any convenient direction, so as at last to arrive at the desired point. Calculate the latitude and departure of each of these courses and take their *algebraic* sums. The sum of the latitudes will be equal to A X, and that of the departures to X Z. Then is  $\tan. Z A X = \frac{X Z}{X A}$ ; i. e., the algebraic sum of the departures divided by the algebraic sum of the latitudes is equal to the tangent of the bearing.\*

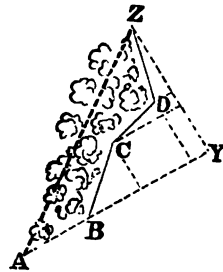
**370.** When the *transit* is used, any line may be taken as a meridian—i. e., as the line to which the following lines are referred; as in “Traversing,” Art. 335, all the successive lines were referred to the first line. In Fig. 263 the same lines as in the preceding figure are represented, but they are referred to the first course, A B, instead of to the magnetic meridian as before, and their latitudes are measured along its produced line, and its departures perpendicular to it. As before, a right-angled triangle will be formed, and the angle Z A Y will be the angle at A between the first line A B and the desired line A Z.

This method of operation has many useful applications, such as in obtaining data for running railroad-curves, etc., and the student should master it thoroughly.

\* The length of the line A Z can also be at once obtained, since it is equal to the square root of the sum of the squares of A X and X Z, or to the latitude divided by the cosine of the bearing.

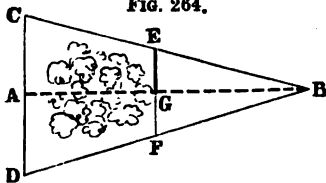
The desired angle (and at the same time the distance) can be obtained, approximately, in this and the preceding case, by finding in a traverse-table the final latitude and departure of the desired line (or a latitude and departure having the same ratio), and the bearing and distance corresponding to these will be the angle and distance desired.

FIG. 263.



**371. By Similar Triangles.** Through A measure any line CD.

FIG. 264.

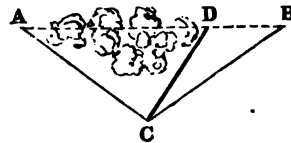


Take a point E, on the line CB, beyond the obstacle, and from it set off a parallel to CD, to some point, F, in the line DB. Measure EF, CD, and CA. Then this proportion,  $CD : CA :: EF : EG$ , will give the distance EG,

from E to a point in the line AB. So for other points.

**372. By Triangulation.** When obstacles prevent the preceding methods being used, if a point, C, can be found from which A and B are accessible, measure the distances CA, CB, and the angle ACB, and thence calculate the angle CAB. Then observe any angle ACD beyond the obstacle. In the triangle ACD a side and its including angles are known to find CD. Measure it, and a point, D, in the desired line will be obtained.

FIG. 265.

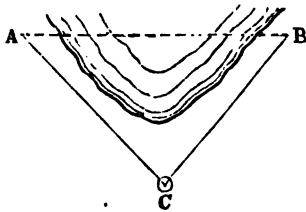


## OBSTACLES TO MEASUREMENT.

### A. WHEN BOTH ENDS OF THE LINE ARE ACCESSIBLE.

**373.** The methods given in the preceding articles for prolonging a line and for interpolating points in it will generally give the length of the line by the same operation. The method of latitudes and departures is very generally applicable. So is the following.

FIG. 266.



**374. By Triangulation.** Let  $AB$  be the inaccessible distance. From any point,  $C$ , from which both  $A$  and  $B$  are accessible, measure  $CA$ ,  $CB$ , and the angle  $ACB$ . Then in the triangle  $ABC$  two sides and the included angle are known to find the side  $AB$ .\*

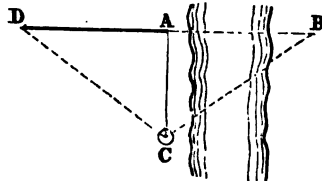
**375. By Angles to Known Points.** The length of a line, both ends of which are accessible, may also be determined by angles measured at its extremities between it and the directions of two or more known points. But, as the methods of calculation involve subsequent problems, they will be postponed.

#### B. WHEN ONE END OF THE LINE IS INACCESSIBLE.

**376. By Perpendiculars.** Many of the methods given for the chain may be still more advantageously employed with angular instruments, which can so much more easily and precisely set off the perpendiculars.

**377. By Equal Angles.** Let  $AB$  be the inaccessible line. At  $A$  set off  $AC$  perpendicular to  $AB$ , and as nearly equal to it, by estimation, as the ground will permit. At  $C$  measure the angle  $ACB$ , and turn the sights or vernier till  $ACD = ACB$ . Find the point,  $D$ , at the intersection of the lines  $CD$  and  $BA$  produced. Then is  $AD = AB$ .

FIG. 267.



**378. By Triangulation.** Measure a distance  $AC$ , about equal to  $AB$ . Measure the angles at  $A$  and  $C$ . Then, in the triangle  $ABC$ , two angles and the included side are known, to find another side,  $AB = \frac{AC \sin. ACB}{\sin. ABC}$ .

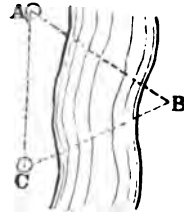
\* In this figure and the following ones the angular point inclosed in a circle indicates the place at which the instrument is set.

When the compass is used, the angles between the lines will be deduced from their respective bearings.

If the angle at A is  $90^\circ$ ,  $AB = AC \cdot \tan \angle ACB$ .

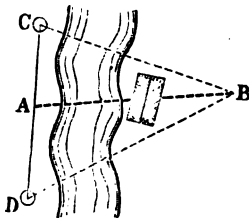
If the angle  $\angle ACB = 45^\circ$ , then  $AC = AB$ ; but this position could not easily be obtained, except by the use of the sextant, a reflecting instrument, described in Part V.

FIG. 268.



**379. When One Point can not be seen from the other.** Choose

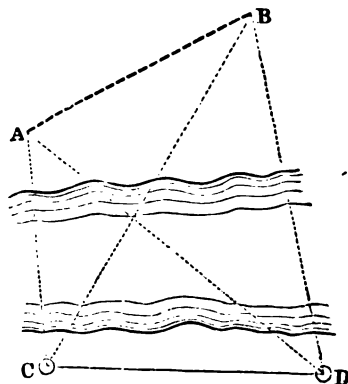
FIG. 268'.



two points, C and D, in the line of A, and such that from C, A, and B can be seen, and from D, A, and B. Measure AC, AD, and the angles C and D. Then, in the triangle BCD, are known two angles and the included side, to find CB. Then, in the triangle ABC, are known two sides and the included angle, to find the third side, AB.

**380. To find the Distance from a Given Point to an Inaccessible Line.** In Fig. 254, Art. 358, the required distance is CE. The operations therein directed give the line CA and the angle CAB, or CAE. The required distance  $CE = CA \cdot \sin \angle CAE$ .

FIG. 269.



C. WHEN BOTH ENDS OF THE LINE ARE INACCESSIBLE.

**381. General Method.** Let AB be the inaccessible line. Measure any convenient distance, CD, and the angles ACD, BCD, ADC, BDC.

Then, in the triangle CDA, two angles and the included side are given, to find CA. In the

triangle C D B, two angles and the included side are given, to find C B. Then, in the triangle A B C, two sides and the included angle are given, to find A B.

The work may be verified by taking another set of triangles, and finding A B from the triangle A B D instead of A B C.

The following formulas will, however, give the desired distances with less labor:

$$\text{Find an angle } K, \text{ such that } \tan. K = \frac{\sin. A D C . \sin. C B D}{\sin. C A D . \sin. B D C}.$$

Then find the difference of the unknown angles in the triangle C A B from the formula—

$$\tan. \frac{1}{2} (C A B - A B C) = \tan. (45^\circ - K) . \cot. \frac{1}{2} A C B.$$

$$\text{Then is } C A B = \frac{1}{2} (C A B - A B C) + \frac{1}{2} (C A B + A B C).$$

$$\text{Finally, } A B = C D \frac{\sin. B D C . \sin. A C B}{\sin. C B D . \sin. C A B}.$$

*Demonstration :* In the triangle A B C, designate the angles as A, B, C; and the sides opposite to them as  $a, b, c$ . Let  $C D = d$ . The triangle B C D gives [Trig., Art. 12, Theorem I],  $a = d \frac{\sin. B D C}{\sin. C B D}$ . The triangle A O D similarly gives  $b = d \frac{\sin. A D C}{\sin. C A D}$ .

In the triangle A B C, we have [Trig., Art. 12, Theorem II],

$$\tan. \frac{1}{2} (A - B) : \cot. \frac{1}{2} C :: a - b : a + b;$$

$$\text{whence } \tan. \frac{1}{2} (A - B) = \frac{a - b}{a + b} . \cot. \frac{1}{2} C. \quad [1.]$$

Let K be an auxiliary angle, such that  $b = a . \tan. K$ ; whence  $\tan. K = \frac{b}{a}$ .

Dividing the second member of equation [1], above and below, by  $a$ , and substituting  $\tan. K$  for  $\frac{b}{a}$ , we get  $\tan. \frac{1}{2} (A - B) = \frac{1 - \tan. K}{1 + \tan. K} . \cot. \frac{1}{2} C$ .

Since  $\tan. 45^\circ = 1$ , we may substitute it for 1 in the preceding equation, and we get  $\tan. \frac{1}{2} (A - B) = \frac{\tan. 45^\circ - \tan. K}{\tan. 45^\circ + \tan. K} . \cot. \frac{1}{2} C$ .

From the expression for the tangent of the difference of two arcs [Trig., Art. 8], the preceding fraction reduces to  $\tan. (45^\circ - K)$ ; and the equation becomes

$$\tan. \frac{1}{2} (A - B) = \tan. (45^\circ - K) . \cot. \frac{1}{2} C. \quad [2.]$$

In the equation  $\tan. K = \frac{b}{a}$ , substitute the values of  $b$  and  $a$  from the formulas at the beginning of this investigation. This gives

$$\tan. K = d . \frac{\sin. A D C}{\sin. C A D} + d . \frac{\sin. B D C}{\sin. C B D} = \frac{\sin. A D C . \sin. C B D}{\sin. C A D . \sin. B D C}.$$

(A - B) is then obtained by equation [2]; (A + B) is the supplement of C; therefore, the angle A is known.



$$\text{Then } c = AB = \frac{a \sin C}{\sin A} = \frac{d \sin BDC \sin CAB}{\sin CBD \sin CAB}.$$

The use of the auxiliary angle  $K$  avoids the calculation of the sides  $a$  and  $b$ .

*Example.* Let  $CD = 7,106.25$  feet;  $ACD = 95^\circ 17' 20''$ ;  $BCD = 61^\circ 41' 50''$ ;  $ADC = 39^\circ 38' 40''$ ;  $BDC = 78^\circ 35' 10''$ ; required  $AB$ .

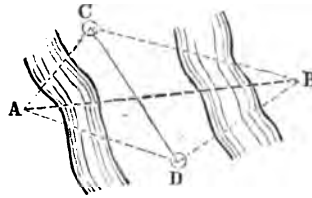
The figure is constructed with these data on a scale of 5,000 feet to 1 inch = 1 : 60000.

By the above formulas,  $K$  is found to be  $30^\circ 26' 5''$ ;  $CAB = 118^\circ 55' 37''$ ; and, lastly,  $AB = 6598.82$ .

Both the methods may be used as mutual checks in any important case.

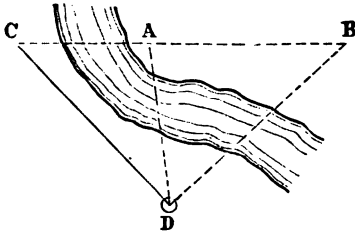
If the lines  $AB$  and  $CD$  crossed each other, as in Fig. 270, instead of being situated as in the preceding figure, the same method of calculation would apply.

FIG. 270.



**382. Problem.** To measure an inaccessible distance,  $AB$ , when a point,  $C$ , in its line can be obtained. Set the instrument at a point,  $D$ , from which  $A$ ,  $B$ , and  $C$  can be seen, and measure the angles  $CDA$  and  $ADB$ . Measure also the line  $DC$  and the angle  $C$ . Then in the triangle  $ACD$  two angles and the included side are given to find  $AD$ . In the triangle  $DAB$ , the angle  $DAB$  is known (being equal to  $ACD + CDA$ ), and  $AD$  having been found, we again have two angles and the included side to find  $AB$ .

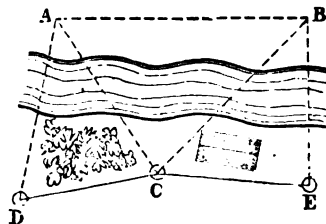
FIG. 271.



which both ends of the line can be seen. to be determined, having one end accessible. Determine them as in Art. 378, by choosing a point  $D$ , from which  $C$  and  $A$  are visible, and a point  $E$ , from which  $C$  and  $B$  are visible. At  $C$  observe the angles  $DCA$ ,  $ACB$ , and  $BCE$ . Measure the distances  $CD$  and  $CE$ . Observe the angles  $ADC$  and  $BEC$ . Then in the triangle  $ADC$ , two angles and the included side are given, to find  $CA$ ; and the same in the triangle  $CBE$ , to find  $CB$ . Lastly, in the triangle  $ACB$  two sides and the included angle are known, to find  $AB$ .

**383. Problem.** To measure an inaccessible distance,  $AB$ , when only one point,  $C$ , can be found from Consider  $CA$  and  $CB$  as distances

FIG. 272.



**384. Problem.** *To measure an inaccessible distance,  $AB$ , when no point can be found from which the two ends can be seen.* Let  $C$  be a point from which  $A$  is visible, and  $D$  a point from which  $B$  is visible, and also  $C$ .

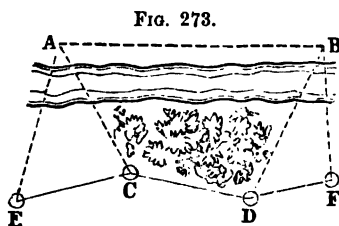


FIG. 273.

Measure  $CD$ . Find the distances  $CA$  and  $DB$ , as in the preceding problem, i. e., choose a point  $E$ , from which  $A$  and  $C$  are visible, and another point,  $F$ , from which  $D$  and  $B$  are visible. Measure  $EC$  and  $DF$ . Observe the angles  $AEC$ ,  $ECA$ ,  $BDF$ , and  $DFB$ ; and at the same time the angles  $ACD$  and  $ODB$ , for the subsequent work. Then  $CA$  and  $DB$  will be found, as were  $CA$

and  $CB$  in the last problem. Then in the triangle  $ODB$ , two sides and the included angle are known to find  $OB$  and the angle  $DOB$ ; and, lastly, in the triangle  $AOB$ , two sides and the included angle (the difference of  $ACD$  and  $DOB$ ) to find  $AB$ .

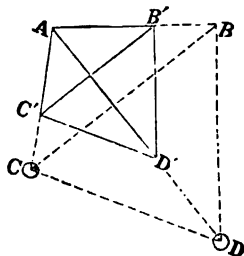
**385. Problem.** *Given the angles observed, at the ends of a line which can not be measured, between it and the ends of a line of known length but inaccessible, required the length of the former line.* This problem is the converse of that given in Art. 381. Its figure, 269, may represent the case, if the distance  $AB$  be regarded as known and  $CD$  as that to be found. Use the first and second formulas as before, and invert the last formula, obtaining

$$CD = AB \frac{\sin. OBD \cdot \sin. CAB}{\sin. BDC \cdot \sin. AOB}.$$

This problem may also be solved, indirectly, by assuming any length for  $CD$ , and thence calculating, as in the first part of Art. 381, the length of  $AB$  on this hypothesis. The imaginary figure thus calculated is *similar* to the true one; and the true length of  $CD$  will be given by this proportion: Calculated length of  $AB$  : true length of  $AB$  :: assumed length of  $CD$  : true length of  $CD$ .

The length of  $CD$  can also be obtained graphically. Take a line of any length, as  $C'D'$ , and from  $C'$  and  $D'$  lay off angles equal to those observed at  $C$  and  $D$ , and thus fix points  $A, B'$ . Produce  $A B'$  till it equals the given distance  $AB$ , on any desired scale. From  $B$  draw a parallel to  $B'D'$ , meeting  $A D'$  produced in  $D$ ; and from  $D$  draw a parallel to  $D'C'$  meeting  $A C'$  produced in  $C$ . Then  $CD$  will be the required distance to the same scale as  $AB$ .

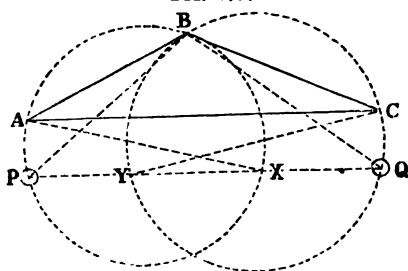
FIG. 274.



**386. Problem.** *Three points,  $ABC$ , being given by their distances from each other, and two other points,  $P$  and  $Q$ , being so situated that from each of them two of the three points can be seen and the angles  $APQ, BPQ, CQP, BQP$ , be measured, it is required to determine the positions of  $P$  and  $Q$ .*

**CONSTRUCTION.** Begin by describing a circle passing through A and B, and having the central angle subtended by A B, equal to twice the given angle A P B, and thus containing that angle. The point P will lie somewhere in its circumference. Describe another circle passing through B and C, and having a central angle subtended by B C equal to twice the given angle B Q C. The point Q will lie somewhere in its circumference. From A draw a line making with A B an angle = B P Q, and meeting at X the circle first drawn. From C draw a line making with C B an angle = B Q P, and meeting the second circle in Y. Join X Y and produce it till it cuts the circles in points P and Q, which will be those required; since  $B P X = B A X = B P Q$ ; and  $B Q Y = B C Y = B Q P$ .

FIG. 275.



**CALCULATION.** In the triangle A B C, the sides being given, the angle A B C is known. In the triangle A B X, a side and all the angles are known, to find B X. In the triangle C B Y, B Y is similarly found. By subtracting the angle A B C from the sum of the angles A B X and C B Y, the angle X B Y can be obtained. Then in the triangle X B Y, the sides B X, B Y, and the included angle are given to find the other angles. Then in the triangle B P X are known all the angles and the side B X to find B P. In the triangle B Q Y, B Q is found in like manner. Finally, in the triangle B P Q, P Q can then be found.

If desired, we can also obtain A P in the triangle A P B; and C Q in the triangle C B Q.

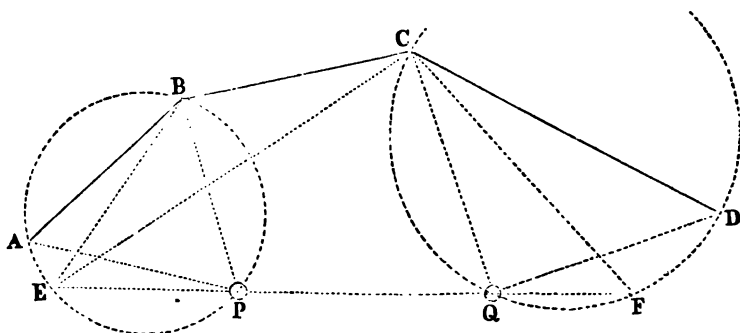
**387. Problem.** *Four points, A, B, C, D, being given in position, by their mutual distances and directions, and two other points, P and Q, being so situated that from each of them two of the four points can be seen and the angles A P B, A P Q, P Q C, and P Q D measured, it is required to determine the position of P and Q.*

**CONSTRUCTION.** Begin, as in the last article, by describing on A B the segment of a circle to contain an angle equal to A P B. From B draw a chord B E, making an angle with B A equal to the supplement of the angle A P Q. On C D describe another segment to contain an angle equal to C Q D. From C draw a chord C F, making an angle with C D equal to the supplement of the angle D Q P. Draw the line E F, and it will cut the two circles in the required points P and Q.

For, the angle A P Q in the figure equals the measured angle A P Q, because the supplement of the former, E P A, equals the supplement of the latter, since it is measured by the same arc as the angle A B E, equal to that supplement by construction. So too with the angle D Q P.

**CALCULATION.** To obtain  $PQ = EF - EP - QF$ , we proceed to find those three lines thus: In the triangle  $ABE$ , we know the side  $AB$ , the angle  $ABE$ , and the angle  $AEB = APB$ ; whence to find  $EB$ . In the same way, the triangle  $CFD$  gives  $FC$ . In the triangle  $EBC$  are known

FIG. 276.



$EB$  and  $BC$ , and the angle  $EBC = ABC - ABE$ ; whence  $EC$  and the angle  $ECB$  are found. In the triangle  $ECF$  are known  $EC$ ,  $FC$ , and the angle  $ECF = BCD - ECB - FCD$ ; whence we find  $EF$ , and the angles  $CEF$  and  $CFE$ .

In the triangle  $BEP$ , we have  $EB$ , the angle  $BEP = BEC + CEP$ , and the angle  $BPE = BPA + APE$ ; to find  $EP$  and  $PB$ . In the triangle  $QCF$ , we have  $CF$ , and the angles  $QCF$  and  $CFQ$ , to find  $QC$  and  $QF$ . Then we know  $PQ = EF - EP - QF$ .

The other distances, if desired, can be easily found from the above data, some of the calculations, not needed for  $PQ$ , being made with reference to them. In the triangle  $ABP$ , we know  $AB$ ,  $BP$ , and the angle  $BAP$ , to find the angle  $ABP$  and  $AP$ . In the triangle  $QDC$  we know  $QC$ ,  $CD$ , and the angle  $CQD$ , to find the angle  $QCD$  and  $QD$ . In the triangle  $PBC$ , we know  $PB$ ,  $BC$ , and the angle  $PBC = ABC - ABP$ , to find  $PC$ . Lastly, in the triangle  $QCB$ , we know  $QC$ ,  $CB$ , and the angle  $QCB = DCB - DCQ$ , to find  $QB$ .

The solution of this problem includes the two preceding; for, let the line  $BC$  be reduced to a point so that its two ends come together and the three lines become two, and we have the problem of Art. 386; and let the line  $AB$  be reduced to a point,  $B$ , and  $CD$  to a point,  $C$ , and we have but one line, and the problem becomes that of Art. 385.

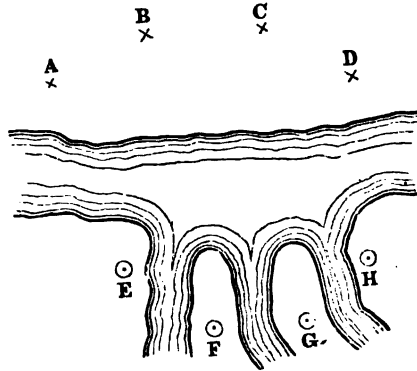
In these three problems, if the two stations lie in a right line with one of the given points, the problem is indeterminate.

**388. Problem of the Eight Points.** *Four points,  $A, B, C, D$ , are inaccessible, but visible from four other points,  $E, F, G, H$ ; it is required to find the relative distances of these eight points; the only data being the observa-*

tion, from each of the points of the second system, of the angles under which are seen the points of the first system.

This problem can be solved, but the great length and complication of the investigation and resulting formulas render it more a matter of curiosity than of utility. It may be found in Puissant's "Topographie," page 55; Lefevre's "Trigonométrie," page 90, and Lefevre's "Arpentage," No. 387.

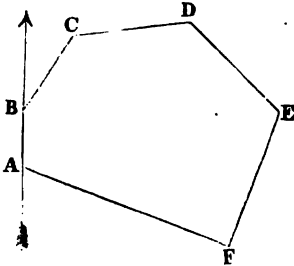
FIG. 277.



### TO SUPPLY OMISSIONS.

**389.** Any two omissions in a closed survey, whether of the direction or of the length, or of both, of one or more of the sides bounding the area surveyed, can always be supplied by a suitable application of the principle of latitudes and departures, although this means should be resorted to only in cases of absolute necessity, since any omission renders it impossible to "test the survey." In the following articles the survey will be considered to have been made with the compass. All the rules will, however, apply to a transit survey, the angles being referred to any line as a meridian, as in "traversing."

FIG. 278.



To save unnecessary labor, the examples in the various cases now to be examined will all be taken from the same survey, a plat of which is given in the margin on the scale of 40 chains to 1 inch (1 : 31,680), and the field-notes of which, with the latitudes and departures carried out to five decimal places, are given on page 258.\*

\* The teacher can make any number of examples for his own use by taking a tolerably accurate survey, striking out the bearing and distance of any one course, and calculating it precisely as in Case 1, given below. He can then omit any two quantities at will, to be supplied by the student by means of the rules now to be given.

| STA-<br>TIONS. | BEARINGS.         | DISTANCE<br>IN LINKS. | LATITUDES. |            | DEPARTURES. |            |
|----------------|-------------------|-----------------------|------------|------------|-------------|------------|
|                |                   |                       | N.         | S.         | E.          | W.         |
| A              | North.            | 1284                  | 1284·00000 |            | 0           | 0          |
| B              | N. 32° E.         | 1782                  | 1511·22171 |            | 944·81619   |            |
| C              | N. 80° E.         | 2400                  | 416·75568  |            | 2363·53872  |            |
| D              | S. 48° E.         | 2700                  |            | 1806·65262 | 2006·49096  |            |
| E              | S. 18° W.         | 2860                  |            | 2720·02159 |             | 883·78862  |
| F              | N. 73° 28' 21" W. | 4621½                 | 1314·69682 |            |             | 4430·55725 |
|                |                   |                       | 4526 67421 | 4526·67421 | 5314·34587  | 5314·34587 |

CASE 1. *When the length and the bearing of any one side are wanting.*

**390.** Find the latitudes and the departures of the remaining sides. The difference of the north and south latitudes of these lines is the latitude of the omitted line, and the difference of their departures is its departure. This latitude and departure are two sides of a right-angled triangle of which the omitted line is the hypotenuse. Its length is therefore equal to the square root of the sum of their squares, and the quotient of the departure divided by the latitude is the tangent of its bearing.

In the above survey, suppose the course from F to A to have been omitted or lost. The difference of the latitudes of the remaining courses will be found to be 1314·69682, and the difference of the departures to be 4430·55725. The square root of the sum of their squares is 4621·5; and the quotient of the departure divided by the latitude is the tangent of 73° 28' 21". The deficiencies were in north latitude and west departure, and the omitted course is therefore N. 73° 28' 21" W., 4621·5.

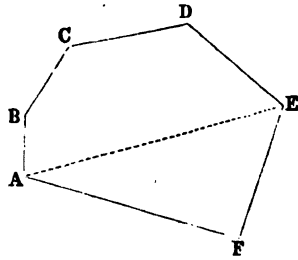
CASE 2. *When the length of one side and the bearing of another are wanting.*

**391. When the Deficient Sides adjoin Each Other.** Find, as in Case 1, the length and bearing of the line joining the ends of the remaining courses. This line and the deficient lines will form a triangle, in which two sides will be known, and the angle between the calculated side and the side whose bearing is given can be

found. The parts wanting can then be obtained by the common rules of trigonometry.

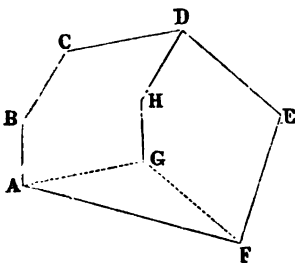
In the figure, let the length of  $EF$  and the bearing of  $FA$  be the omitted parts. The difference of the sums of the N. and S. latitudes, and the E. and W. departures of the complete courses from  $A$  to  $E$ , are respectively  $1405.32477$  north latitude, and  $5314.34587$  east departure. The course,  $EA$ , corresponding to this deficiency, we find, by proceeding as in Case 1, to be  $S. 75^\circ 11' 15'' W.$ ,  $5497.026$ . The angle  $AEF$  is therefore  $= 75^\circ 11' 15'' - 18^\circ = 57^\circ 11' 15''$ . Then in the triangle  $AEF$  are given the sides  $AE$ ,  $AF$ , and the angle  $AEF$  to find the remaining parts, viz., the angle  $AFE = 91^\circ 28' 21''$ , whence the bearing of  $FA = 91^\circ 28' 21'' - 18^\circ = N. 73^\circ 28' 21'' W.$ ; and the side  $EF = 28.60$ .

FIG. 279.



**392. When the Deficient Sides are separated from Each Other.** A modification of the preceding method will still apply. In this figure let the omissions be the bearing of  $FA$  and the length of  $CD$ .

FIG. 280.



Imagine the courses to change places without changing bearings or lengths, so as to bring the deficient lines next to each other by transferring  $CD$  to  $AG$ ,  $AB$  to  $GH$ , and  $BC$  to  $HD$ . This will not affect their latitudes or departures. Join  $GF$ . Then in the figure  $DEFGH$  the latitudes and departures of all the sides but  $FG$  are known, whence its length and bearing can be found as in Case 1. Then the triangle  $AGF$  may be treated like the triangle  $AEF$  in the last article, to obtain the length of  $AG = CD$ , and the bearing of  $FA$ .

*Otherwise, by changing the meridian.* Imagine the field to turn around till the side of which the distance is unknown be-

comes the meridian—i. e., comes to be due north and south—all the other sides retaining their *relative* positions, and continuing to make the same angles with each other. Change their bearings accordingly. Find the latitudes and departures of the sides in their new positions. Since the side whose length was unknown has been made the meridian, it has no departure, whatever may be its unknown length; and the difference of the columns of departure will therefore be the departure of the side whose bearing is unknown. The length of this side is given. It is the hypotenuse of a right-angled triangle, of which the departure is one side. Hence the other side, which is the latitude, can be at once found, and also the unknown bearing.

Put this latitude in the table in the blank where it belongs. Then add up the columns of latitude, and the difference of their sums will be the unknown length of the side which had been made a meridian.\*

Let the omitted quantities be, as in the last article, the length of CD and the bearing of FA. Make CD the meridian. The

| STATIONS. | OLD BEARINGS. | NEW BEARINGS. |
|-----------|---------------|---------------|
| A         | North.        | N. 80° W.     |
| B         | N. 32° E.     | N. 48° W.     |
| C         | N. 80° E.     | North.        |
| D         | S. 48° E.     | N. 52° E.     |
| E         | S. 18° W.     | S. 62° E.     |
| F         |               |               |

changed bearings can then be found to be as in the margin. To aid the imagination, turn the book around till CD points up and down, as north lines are usually placed on a map. Then obtain the latitudes of the courses with

their new bearings and old distances, and proceed as has been directed.

CASE 3. *When the lengths of two sides are wanting.*

**393. When the Deficient Sides adjoin Each Other.** Find the latitudes and departures of the other courses, and then, by Case 1, find the length and bearing of the line joining the extremities of the deficient courses. Then, in the triangle thus formed, are

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\* This conception of thus changing the bearings is stated to be due to Professor Robert Patterson, of Philadelphia, by whom it was communicated to Mr. John Gum-  
mere, and published by him, in 1814, in his "Treatise on Surveying."

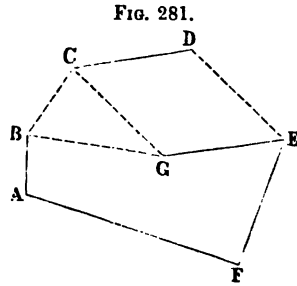


known one side and all the angles (deduced from the bearings) to find the lengths of the other two sides.

Thus, in Fig. 279, let  $EF$  and  $FA$  be the sides whose lengths are unknown.  $EA$  is then to be calculated, and its length will be found to be 5497.026, and its bearing  $S. 75^\circ 11' 15'' W.$ , whence the angle  $AEF = 75^\circ 11' 15'' - 18^\circ = 57^\circ 11' 15''$ ;  $A FE = 18^\circ + 73^\circ 28' 21'' = 91^\circ 28' 21''$ ; and  $EAF = 31^\circ 20' 24''$ ; whence can be obtained  $EF = 28.60$  and  $FA = 46.215$ .

### 394. When the Deficient Sides are separated from Each Other.

Let the lengths of  $BC$  and  $DE$  be those omitted. Again imagine the courses to change places, so as to bring the deficient lines together,  $DE$  being transferred to  $CG$ , and  $CD$  to  $GE$ . Join  $BG$ . Then in the figure  $ABGEFA$  are known the latitudes and departures of all the courses except  $BG$ , whence its length and bearing can be found, as in Case 1. Then in the triangle  $BCG$ , the angle  $CBG$  can be found from the bearings of  $CB$  and  $BG$ , and the angle  $CGB$  from the bearings of  $BG$  and  $GC$ . Then all the angles of the triangle are known and one side,  $BG$ , whence to find the required sides,  $BC = 1,782$ , and  $CG = DE = 2,700$ .



*Otherwise, by changing the meridian.* Imagine the field to turn around till one of the sides whose length is wanting becomes a meridian or due north and south. Change all the bearings correspondingly. Find the latitudes and departures of the changed courses. The difference of the columns of departure will be the departure of the second course of unknown length, since the course made meridian has now no departure. The new bearing of this second course being given in the right-angled triangle formed by this course as an hypotenuse, and its departure and latitude, we know one side, the departure, and the acute angles, which are the bearing and its complement. The length of the course is then readily calculated, and also its latitude. This latitude being in-

serted in its proper place, the difference of the columns of latitude will be the length of that wanting side which had been made a meridian.

Thus, let the lengths of B C and D E be wanting, as in the preceding example.

| STATIONS. | OLD BEARINGS.     | NEW BEARINGS.     |
|-----------|-------------------|-------------------|
| A         | North.            | N. 32° W.         |
| B         | N. 32° E.         | North.            |
| C         | N. 80° E.         | N. 48° E.         |
| D         | S. 48° E.         | S. 80° E.         |
| E         | S. 18° W.         | S. 14° E.         |
| F         | N. 73° 28' 21" W. | S. 74° 31' 59" W. |

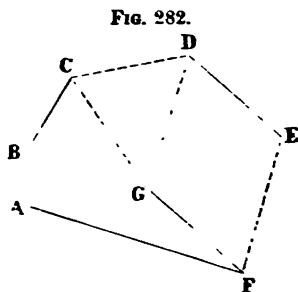
Make B C a meridian. The other bearings are then changed as in the margin. Calculate new latitudes and departures. The

difference of the departures will be the departure of D E, since B C, being a meridian, has no departure. Hence the length and latitude of D E are readily obtained. This latitude being put in the table, and the columns of latitude then added up, their difference will be the length of B C.

CASE 4. *When the bearings of two sides are wanting.*

**395. When the Deficient Sides adjoin Each Other.** Find the latitudes and departures of the other sides, and then, as in Case 1, find the length and bearing of the line joining the extremities of the deficient sides. Then, in the triangle thus formed, we have the three sides to find the angles and thence the bearings.

**396. When the Deficient Sides are separated from Each Other.** Change the places of the sides so as to bring the deficient ones next to each other. Thus, in the figure, supposing the bearings of C D and E F to be wanting, transfer E F to D G, and D E to G F. Then calculate, as in Case 1, the length and bearing of the line joining the extremities of the deficient sides, C G in the figure. This line and the deficient sides form a triangle in which the three sides are given to determine the angles and thence the required bearings.



## CHAPTER VI.

### LAYING OUT, PARTING OFF, AND DIVIDING UP LAND.

#### LAYING OUT LAND.

**397. Its Nature.** This operation is precisely the reverse of those of surveying properly so called. The latter measures certain lines as they are ; the former marks them out in the ground where they are required to be, in order to satisfy certain conditions. The same instruments, however, are used as in surveying.

Perpendiculars and parallels are the lines most often employed. Part of the demonstrations of the problems are left as exercises for the student.

**398. To lay out Squares.** Reduce the desired content to square chains, and extract its square root. This will be the length of the required side, which is to be set out by one of the methods indicated in the preceding article.

An *acre*, laid out in the form of a square, is frequently desired by farmers. Its side must be made  $316\frac{1}{4}$  links of a Gunter's chain ; or  $208\frac{11}{100}$  feet ; or  $69\frac{57}{100}$  yards. It is often taken at 70 paces.

The number of plants, hills of corn, loads of manure, etc., which an acre will contain at any uniform distance apart, can be at once found by dividing 209 by this distance in feet, and multiplying the quotient by itself, or by dividing 43,560 by the square of the distance in feet. Thus, at 3 feet apart, an acre would contain 4,840 plants, etc. ; at 10 feet apart, 436 ; at a rod apart, 160 ; and so on. If the distances apart be unequal, divide 43,560 by the product of these distances in feet ; thus, if the plants were in rows 6 feet apart, and the plants in the rows were 3 feet apart, 2,420 of them would grow on one acre.

**399. To lay out Rectangles.** *The content and length being given*, both as measured by the same unit, divide the former by the latter, and the quotient will be the required breadth. Thus, 1 acre or 10 square chains, if 5 chains long, must be 2 chains wide.

*The content being given and the length to be a certain number of times the breadth.* Divide the content in square chains, etc., by the ratio of the length to the breadth, and the square root of the quotient will be the shorter side desired, whence the longer side is also known. Thus, let it be required to lay out 30 acres in the form of a rectangle 3 times as long as broad; 30 acres = 300 square chains. The desired rectangle will contain 3 squares, each of 100 square chains, having sides of 10 chains. The rectangle will therefore be 10 chains wide and 30 long.

An acre laid out in a rectangle twice as long as broad will be 224 links by 448 links, nearly; or, 147½ feet by 295 feet; or, 49½ yards by 98¾ yards. Fifty paces by one hundred is often used as an approximation, easy to be remembered.

*The content being given, and the difference between the length and breadth.* Let  $c$  represent this content, and  $d$  this difference. Then the longer side =  $\frac{1}{2}d + \frac{1}{2}\sqrt{(d^2 + 4c)}$ .

*Example.* Let the content be 6.4 acres, and the difference 12 chains. Then the sides of the rectangle will be respectively 16 chains and 4 chains.

*The content being given, and the sum of the length and breadth.* Let  $c$  represent this content, and  $s$  this sum. Then the longer side =  $\frac{1}{2}s + \frac{1}{2}\sqrt{(s^2 - 4c)}$ .

*Example.* Let the content be 6.4 acres, and the sum 20 chains. The above formula gives the sides of the rectangle 16 chains and 4 chains as before.

**400. To lay out Triangles.** The content and the base being given, divide the former by half the latter to get the height. At any point of the base erect a perpendicular of the length thus obtained, and it will be the vertex of the required triangle.

The content being given and the base having to be  $m$  times the height, the height will equal the square root of the quotient obtained by dividing twice the given area by  $m$ .

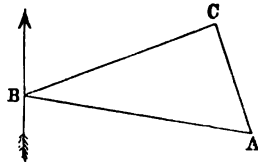
The content being given and the triangle to be equilateral, take the square root of the content and multiply it by 1.520. The product will be the length of the side required. This rule makes the sides of an equilateral triangle containing *one acre* to be 480½ links. A quarter of an acre laid out in the same form would have each side 240 links long. An equilateral triangle is very easily set out on the ground, as directed under "Platting," using a rope or chain for compasses.

The content and base being given, and one side having to make a given angle, as B, with the base AB,

the length of the side BC =  $\frac{2 \times \text{ABC}}{\text{AB} \cdot \sin. B}$ .

*Example.* Eighty acres are to be laid out in the form of a triangle, on a base, AB, of sixty chains, bearing N. 80° W., the bearing of the side BC being N. 70° E. Here the angle B is found from the bearings (reversing one of them) to be 30°. Hence BC = 53.33. The figure is on a scale of 50 chains to 1 inch = 1 : 39600.

FIG. 283.



Any right-line figure may be laid out by analogous methods.

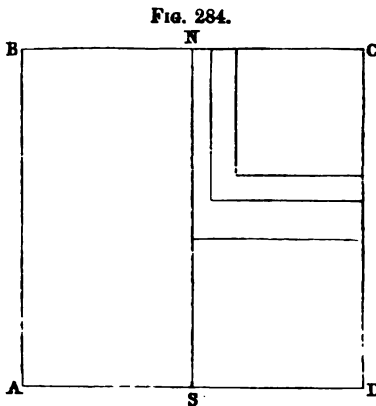
**401. To lay out Circles.** Multiply the given content by 7, divide the product by 22, and take the square root of the quotient. This will give the radius, with which the circle can be described on the ground with a rope or chain. A circle containing one acre has a radius of 178½ links. A circle containing a quarter of an acre will have a radius of 89 links.

**402. Town-Lots.** House-lots in cities are usually laid off as rectangles of 25 feet front and 100 feet depth, variously combined in blocks. Part of New York is laid out in blocks 200 feet by 800, each containing 64 lots, and separated by streets, 60 feet wide, running along their long sides, and avenues, 100 feet wide, on their short sides. The eight lots on each short side of the block front on the avenues, and the remaining forty-eight lots front on the streets. Such a block covers almost precisely 3½ acres, and 17½ such lots about make an acre. But, allowing for the streets, land

laid out into lots, 25 by 100, arranged as above, would contain only 11.9, or not quite 12 lots per acre.

Lots in small towns and villages are laid out of greater size and less uniformity: 50 feet by 100 is a frequent size for new villages, the blocks being 200 feet by 500, each therefore containing 20 lots.

**403. Land sold for Taxes.** A case occurring in the State of New York will serve as an application of the modes of laying out squares and rectangles. Land on which taxes are unpaid is sold at auction to the *lowest* bidder—i. e., to him who will accept the smallest portion of it in return for paying the taxes on the whole. The lot in question was originally the east half of the square lot ABCD, containing 500 acres. At a sale for taxes in 1830, 70 acres were bid off, and this area was set off to the purchaser in a square lot, from the northeast corner. Required the side of the square in links. Again, in 1834, 29 acres more were thus sold, to be set off in a strip of equal width around the square previously sold. Required the width of this strip. Once more: in 1839, 42 acres more were sold, to be set off around the preceding piece. Required the dimensions of this third portion. The answer can be proved by calculating if the dimensions of the remaining



rectangle will give the content which it should have, viz.,  $250 - (70 + 29 + 42) = 109$  acres.

The figure is on a scale of 40 chains to 1 inch = 1 : 31680.

**404. New Countries.** The operations of laying out land for the purposes of settlers are required on a large scale in new countries, in combination with their survey. There is great difficulty in uniting the necessary precision, rapidity, and cheapness. "Triangular surveying" will insure the first of these qualities, but is deficient in the last two, and leaves the laying out of lots to be

subsequently executed. "Compass-surveying" possesses the last two qualities, but not the first. The United States system for surveying and laying out the public lands admirably combines an accurate determination of standard lines (meridians and parallels) with a cheap and rapid subdivision by compass. The subject is so important and extensive that it will be explained by itself.

## PARTING OFF LAND.

**405.** It is often required to part off from a field, or from an indefinite space, a certain number of acres by a fence or other boundary-line, which is also required to run in a particular direction, to start from a certain point, or to fulfill some other condition. The various cases most likely to occur will be here arranged according to these conditions. Both graphical and numerical methods will generally be given.\*

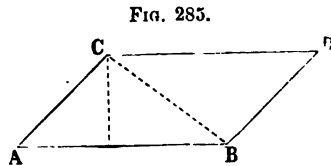
The given content is always supposed to be reduced to square chains and decimal parts, and the lines to be in chains and decimals.

## A. BY A LINE PARALLEL TO A SIDE.

**406. To part off a Rectangle.** If the sides of the field adjacent to the given side make right angles with it, the figure parted off by a parallel to the given side will be a rectangle, and its breadth will equal the required content divided by that side, as in Art. 398.

If the field be bounded by a curved or zigzag line outside of the given side, find the content between these irregular lines and the given straight side, by the method of offsets, subtract it from the content required to be parted off, and proceed with the *remainder* as above. The same directions apply to the subsequent problems.

**407. To part off a Parallelogram.** If the sides adjacent to the given side be parallel, the figure parted off will be a parallelogram, and its perpendicular width, CE,



\* The given lines will be represented by fine full lines, the lines of construction by broken lines, and the lines of the result by heavy full lines.

will be obtained as above. The length of one of the parallel sides,

$$\text{as } AC = \frac{CE}{\sin. A} = \frac{ABDC}{AB \cdot \sin. A}.$$

**408. To part off a Trapezoid.** When the sides of a field adjacent to the given side are not parallel, the figure parted off will be a trapezoid.

When the field or figure is given on the ground, or on a plat, begin as if the sides were parallel, dividing the given content by the base  $AB$ . The quotient will be an *approximate* breadth,  $CE$ , or  $DF$ ; too small if the sides converge, as in the figure, and *vice versa*. Measure  $CD$ . Calculate the content of  $ABDC$ . Divide

the difference of it and the required content by  $CD$ . Set off the quotient perpendicular to  $CD$  (in this figure, outside of it), and it will give a new line,  $GH$ , a still nearer approximation to that desired. The operation may be repeated, if found necessary.

**409.** When the field is given by bearings, deduce from them the angles at  $A$  and  $B$ . The required sides will then be given by these formulas :

$$CD = \sqrt{(AB^2 - \frac{2 \times AB \cdot CD \cdot \sin. (A+B)}{\sin. A \cdot \sin. B})}.$$

$$AD = (AB - CD) \frac{\sin. B}{\sin. (A+B)}.$$

$$BC = (AB - CD) \frac{\sin. A}{\sin. (A+B)}.$$

*Demonstration.* Produce  $BC$  and  $AD$  to meet in  $E$ .  
By similar triangles,

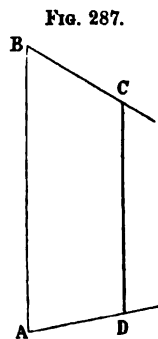
$$ABE : DCE :: AB^2 : DC^2.$$

$$ABE - DCE : ABE :: AB^2 - DC^2 : AB^2$$

Now  $ABE - DCE = ABDC$ ; also, by Art. 61, note,

$$ABE = AB^2 \cdot \frac{\sin. A \cdot \sin. B}{2 \cdot \sin. (A+B)}.$$

The above proportion, therefore, becomes





$$ABCD : AB^2 \cdot \frac{\sin. A \cdot \sin. B}{2 \cdot \sin. (A+B)} :: AB^2 - CD^2 : AB^2.$$

Multiplying extremes and means, canceling, transposing, and extracting the square root, we get  $CD = \sqrt{AB^2 - \frac{2 \cdot ABCD \cdot \sin. (A+B)}{\sin. A \cdot \sin. B}}$ .

When  $A + B > 180^\circ$ ,  $\sin. (A + B)$  is negative, and therefore the fraction in which it occurs becomes positive.

CF being drawn parallel to DA, we have

$$\begin{aligned} AD = FC = FB \cdot \frac{\sin. B}{\sin. BCF} &= FB \cdot \frac{\sin. B}{\sin. (180^\circ - A - B)} \\ &= (AB - CD) \frac{\sin. B}{\sin. (A + B)} \quad BC = (AB - CD) \frac{\sin. A}{\sin. (A + B)}. \end{aligned}$$

When the sides AD and BC diverge, instead of converging, as in the figure, the negative term, in the expression for CD, becomes positive; and, in the expressions for both AD and BC, the first factor becomes  $(CD - AB)$ .

The perpendicular breadth of the trapezoid  $= AD \cdot \sin. A$ ;  
or  $= BC \cdot \sin. B$ .

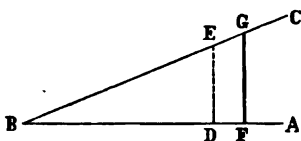
*Example.* Let AB run north, six chains; AD, N.  $80^\circ$  E.; BC, S.  $60^\circ$  E. Let it be required to part off one acre by a fence parallel to AB. Here  $AB = 6.00$ ,  $ABCD = 10$  square chains,  $A = 80^\circ$ ,  $B = 60^\circ$ . *Ans.*  $CD = 4.57$ ,  $AD = 1.92$ ,  $BC = 2.18$ , and the breadth  $= 1.89$ .

The figure is on a scale of 4 chains to an inch  $= 1 : 3168$ .

#### B. BY A LINE PERPENDICULAR TO A SIDE.

**410. To part off a Triangle.** Let FG be the required line.

FIG. 289.

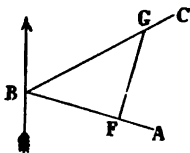


When the field is given on the ground, or on a plat, at any point, as D, of the given side AB, set out a "guess-line," DE, perpendicular to AB, and calculate the content of DEB. Then the required distance

BF, from the angular point to the foot of the desired perpendicular  $= BD \sqrt{\left(\frac{BFG}{BDE}\right)}$ .

Since similar triangles are as the squares of their homologous sides,  
 $BDE : BFG :: BD^2 : BF^2$ ; whence  $BF = BD \sqrt{\left(\frac{BFG}{BDE}\right)}$ .

FIG. 290.



*Example.* Let  $BD = 30$  chains;  $ED = 12$  chains; and the desired area = 24.8 acres. Then  $BF = 35.22$  chains.

The scale of the figure is 30 chains to 1 inch = 1 : 23760.

When the field is given by bearings, find the angle  $B$  from the bearings; then is

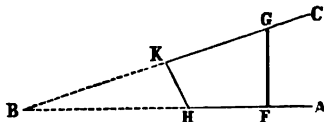
$$BF = \sqrt{\left(\frac{2 \times BFG}{\tan. B}\right)}.$$

*Example.* Let  $BA$  bear S.  $75^\circ$  E., and  $BC$  N.  $60^\circ$  E., and let five acres be required to be parted off from the field by a perpendicular to  $BA$ . Here the angle  $B = 45^\circ$ , and  $BF = 10.00$  chains.

The scale of the figure is 20 chains to 1 inch = 1 : 15840.

**411. To part off a Quadrilateral.** Produce the converging sides to meet at  $B$ . Calculate the content of the triangle  $HKB$ , whether on the ground or plat, or from bearings. Add it to the content of the quadrilateral required to be parted off, and it will give that of the triangle  $FGB$ , and the method of the preceding case can then be applied.

FIG. 291.



**412. To part off any Figure.** If the field be very irregularly shaped, find by trial any line which will part off a little less than the required area. This trial-line will represent  $HK$  in the preceding figure, and the problem is reduced to parting off, according to the required condition, a *quadrilateral*, comprised between the trial-line, two sides of the field, and the required line, and containing the difference between the required content and that parted off by the trial-line.

## C. BY A LINE RUNNING IN ANY GIVEN DIRECTION.

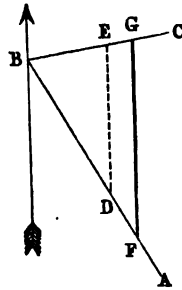
**413. To part off a Triangle.** By construction, on the ground or the plat, proceed nearly as in Art. 410, setting out a line in the required direction, calculating the triangle thus formed, and obtaining  $BF$  by the same formula as in that article.

**414.** If the field be given by bearings, find from them the angles  $CBA$  and  $GFB$ ; then is  $BF = \sqrt{\left(\frac{2 \times BFG \sin. (B + F)}{\sin. B \cdot \sin. F}\right)}$ .

*Example.* Let  $BA$  bear  $S. 30^\circ E.$ ;  $BC$ ,  $N. 80^\circ E.$ ; and a fence be required to run from some point in  $BA$ , a due north course, and to part off one acre. Required the distance from  $B$  to the point  $F$ , whence it must start. *Ans.* The angle  $B = 70^\circ$ , and  $F = 30^\circ$ . Then  $BF = 6.47$ .

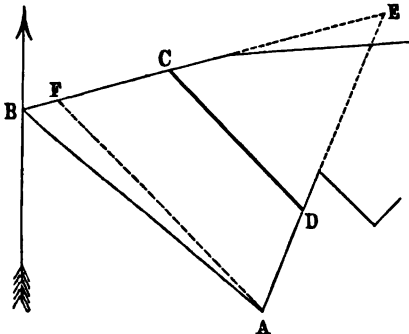
The scale of Fig. 292 is 6 chains to 1 inch = 1 : 4752.

FIG. 292.



**415. To part off a Quadrilateral.** Let it be required to part off, by a line running in a given direction, a quadrilateral from a field in which are given the side  $AB$ , and the directions of the two other sides running from  $A$  and from  $B$ .

FIG. 293.



On the ground or plat produce the two converging sides to meet at some point  $E$ . Calculate the content of the triangle  $ABE$ . Measure the side  $AE$ . From  $ABE$  subtract the area to be cut off, and the remainder will be the content of

the triangle  $CDE$ . From  $A$  set out a line  $AF$  parallel to the given direction. Find the content of  $ABF$ . Take it from

ABE, and thus obtain AFE. Then this formula,  $ED = AE \sqrt{\frac{CDE}{FAE}}$ , will fix the point D, since  $AD = AE - ED$ .

When the field and the dividing line are given by bearings, produce the sides as in the last article. Find all the angles from the bearings. Calculate the content of the triangle ABE, by the formula for one side and its including angles. Take the desired content from this to obtain CDE. Calculate the side  $AE = AB \frac{\sin. B}{\sin. E}$ . Then is  $AD = AE - \sqrt{\left( \frac{2 \times CDE \cdot \sin. DCE}{\sin. E \cdot \sin. CDE} \right)}$ .

*Demonstration.* Since triangles which have an angle in each equal, are as the products of the sides about the equal angles, we have

$$ABE : CDE :: AE \times BE : CE \times DE.$$

$$ABE = \frac{1}{2} \cdot AB^2 \cdot \frac{\sin. A \cdot \sin. B}{\sin. (A + B)}. \quad AE = AB \cdot \frac{\sin. B}{\sin. E}.$$

$$BE = AB \cdot \frac{\sin. A}{\sin. E}. \quad CE = DE \cdot \frac{\sin. CDE}{\sin. DCE}.$$

Substituting these values in the preceding proportion, canceling the common factors, observing that  $\sin. (A + B) = \sin. E$ , multiplying extremes and means, and dividing, we get  $DE = \sqrt{\left( \frac{2 \cdot CDE \cdot \sin. DCE}{\sin. E \cdot \sin. CDE} \right)}$ .

*Example.* Let DA bear S.  $20\frac{1}{4}^\circ$  W. ; AB, N.  $51\frac{1}{2}^\circ$  W., 8.19 ; BC, N.  $73\frac{1}{2}^\circ$  E ; and let it be required to part off two acres by a fence, DC, running N.  $45^\circ$  W. *Ans.* ABE = 32.56 square chains ; whence CDE = 12.56 square chains. Also,  $AE = 8.37$  ; and, finally,  $AD = 8.37 - 5.51 = 2.86$  chains.

The scale of Fig. 293 is 5 chains to 1 inch = 1 : 3960.

If the sum of the angles at A and B were more than two right angles, the point E would lie on the other side of AB. The necessary modifications are apparent.

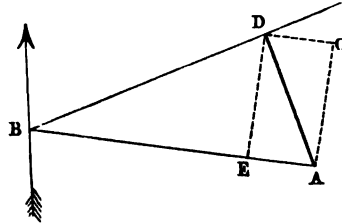
**416. To part off any Figure.** Proceed in a similar manner to that described in Art. 412, by getting a suitable trial-line, producing the sides it intersects, and then applying the method just given.

D. BY A LINE STARTING FROM A GIVEN POINT IN A SIDE.

**417. To part off a Triangle.** Let it be required to cut off from a corner of a field a triangular space of given content, by a line starting from a given point on one of the sides, A in the figure,

the base,  $AB$ , of the desired triangle being thus given. If the field be given on the ground or on a plat, divide the given content by half the base, and the quotient will be the height of the triangle. Set off this distance from any point of  $AB$ , perpendicular to it, as from  $A$  to  $C$ ; from  $C$  set out a parallel to  $AB$ , and its intersection with the second side, as at  $D$ , will be the vertex of the required triangle.

FIG. 294.



*Otherwise:* Divide the required content by half of the perpendicular distance from  $A$  to  $BD$ , and the quotient will be  $BD$ .

If the field be given by the bearings of two sides and the length of one of them, deduce the angle  $B$  (Fig. 294) from the bearings. Then is  $BD = \frac{2 \times ABD}{AB \cdot \sin. B}$ .

If it is more convenient to fix the point  $D$ , by the second method, that of rectangular co-ordinates, we shall have  $BE = BD \cdot \cos. B$ ; and  $ED = BD \cdot \sin. B$ .

The bearing of  $AD$  is obtained from the angle  $BAD$ , which is known, since  $\frac{ED}{EA} = \frac{ED}{AB - BE} = \tan. BAD$ .

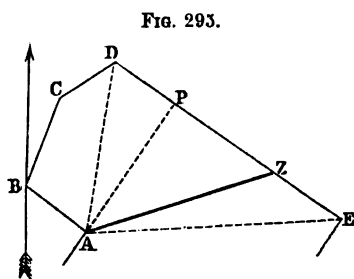
*Example.* Eighty acres are to be set off from a corner of a field, the course  $AB$  being  $N. 80^\circ W.$ , sixty chains; and the bearing of  $BD$  being  $N. 70^\circ E.$  *Ans.*  $BD = 53.33$ ;  $BE = 46.19$ ;  $ED = 26.67$ ; and the bearing of  $AD$ ,  $N. 17^\circ 23' W.$

The scale of Fig. 294 is 40 chains to 1 inch = 1 : 31680.

If the field were right-angled at  $B$ , of course  $DB = \frac{2 ABD}{AB}$ .

**418. To part off a Quadrilateral.** Imagine the two converging sides of the field produced to meet, as in Art. 415. Calculate the content of the triangle thus formed, and the question will then be reduced to the one explained in the last two articles.

**419. To part off any Figure.** Proceed as directed in Art. 416. Otherwise, proceed as follows :



The field being given on the ground or on a plat, find on which side of it the required line will end, by drawing or running "guess-lines" from the given point to various angles, and roughly measuring the content thus parted off. If, as in the figure, A being the given point, the guess-line AD parts off less than the required content, and

AE parts off more, then the desired division-line AZ will end in the side DE. Subtract the area parted off by AD from the required content, and the difference will be the content of the triangle ADZ. Divide this by half the perpendicular let fall from the given point A to the side DE, and the quotient will be the base, or distance from D to Z.

Or, find the content of ADE and make this proportion :  
 $ADE : ADZ :: DE : DZ$ .

The field being given by bearings and distances, find as before, by approximate trials on the plat, or otherwise, which side the desired line of division will terminate in, as DE in the last figure. Draw AD. Find the latitude and departure of this line, and thence its length and bearing. Then calculate the area of the space this line parts off, ABCD in the figure, by the usual method, explained in Part I, Chapter III. Subtract this area from that required to be cut off, and the remainder will be the area of the triangle ADZ. Then, as in Art. 415,  $DZ =$

$$\frac{2 ADZ}{AD \cdot \sin. ADZ}.$$

This problem may be executed without any other table than that of latitudes and departures, thus : Find the latitude and departure of DA, as before, the area of the space ABCD, and thence the content of ADZ. Then find the latitude and departure of EA, and the content of ADE. Lastly, make this proportion :  
 $ADE : ADZ :: DE : DZ$ .\*

---

\* The problem may also be performed by making the side on which the division-

*Example.* In the field A B C D E, etc., part of which is shown in Fig. 295 (on a scale of 4 chains to 1 inch = 1 : 3168), one acre is to be parted off on the west side, by a line starting from the angle A. Required the distance from D to Z, the other end of this dividing line.\*

The only courses needed are these : A B, N.  $53^{\circ}$  W., 1.55 ; B C, N.  $20^{\circ}$  E, 2.00 ; C D, N.  $53\frac{1}{4}^{\circ}$  E., 1.32 ; D E, S.  $57^{\circ}$  E., 5.79. A rough measurement will at once show that A B C D is less than an acre, and that A B C D E is more ; hence the desired line will fall on D E. The latitudes and departures of A B, B C, and C D are then found. From them the course A D is found to be N.  $8^{\circ} 1' 22''$  E., 3.634. The content of A B C D will be 3.19 square chains. Subtracting this from one acre, the remainder, 6.81 square chains, is the content of A D Z.  $A P = 3.63 \times \sin. 65^{\circ} = 3.29$ . Dividing A D Z by half of this, we obtain D Z = 4.14 chains.

By the second method, the latitude and departure of D A, the area of A B C D, and of A D Z, being found as before, we next find the latitude and departure of E A from those of A D and D E, and thence the area of A D E = 9.53. Lastly, we have the proportion  $9.53 : 6.81 :: 5.79 : D Z = 4.14$ , as before.

#### E. BY A LINE PASSING THROUGH A GIVEN POINT WITHIN THE FIELD.

##### 420. To part off a Triangle.

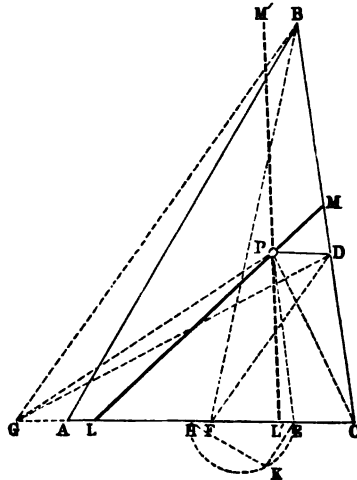
Let P be a point within a field through which it is required to run a line so as to part off from the field a given area in the form of a triangle.

When the field is given on

line is to fall, a meridian, and changing the bearings. The difference of the new departures will be the departure of the division-line. Its position can then be easily determined.

\* If the whole field has been surveyed and balanced, the balanced latitudes and departures should be used. We will here suppose the survey to have proved perfectly correct.

Fig. 296.



the ground or on a plat, the division can be made by construction, thus: Divide the given area by half of the perpendicular distance from P to A C, and set off the quotient from C to G. Bisect G C in H. From P draw P E, parallel to the side B C. On H E describe a semicircle. On it set off E K = E C. Join K H. Set off H L = H K. The line L M, drawn from L through P, will be the division-line required.\* If H K be set off in the contrary direction, it will fix another line L' P M', meeting C B produced, and thus parting off another triangle of the required content.

*Demonstration.* By construction, G P C = the required content. Now, G P C = G D C, since they have the same base and equal altitudes. We have now to prove that L M C = G D C. These two triangles have a common angle at C. Hence, they are to each other as the rectangles of the adjacent sides—i. e.,

$$G D C : L M C :: G C \times C D :: L C \times C M.$$

Here C M is unknown, and must be eliminated. We obtain an expression for it by means of the similar triangles L M C and L E P, which give

$$L E : L C :: E P = C D : C M.$$

Hence,  $C M = \frac{C D \times L C}{L E}$ . Substituting this value of C M in the first proportion, and canceling C D in the last two terms, we get

$$G D C : L M C :: G C : \frac{L C^2}{L E}; \text{ or } G D C : L M C :: G C \times L E : L C^2.$$

$$L C^2 = (L H + H C)^2 = L H^2 + 2 L H \times H C + H C^2.$$

But, by construction,

$$L H^2 = H K^2 = H E^2 - E K^2 = H E^2 - E C^2 = (H E + E C)(H E - E C) = H C(H E - E C).$$

Also,  $G C = 2 H C$ ; and  $L E = L H + H E$ .

Substituting these values in the last proportion, it becomes

$$\begin{aligned} G D C : L M C :: 2 \cdot H C (L H + H E) : H C (H E - E C) + 2 L H \times H C + H C^2. \\ :: 2 L H + 2 H E \quad : H E - E C + 2 L H + H C. \\ \quad \quad \quad : H E - E C + 2 L H + H E + E C. \\ \quad \quad \quad : 2 H E + 2 L H. \end{aligned}$$

The last two terms of this proportion are thus proved to be equal. Therefore, the first two terms are also equal—i. e., L M C = G D C = the required content.

Since H K =  $\sqrt{H E^2 - E K^2}$ , it will have a negative as well as a positive value. It may therefore be set off in the contrary direction from L—i. e., to L'. The line drawn from L' through P, and meeting O B produced beyond B, will part off *another* triangle of the required content.

*Example.* Let it be required to part off 31.175 acres by a fence passing through a point P, the distance P D of P from the side

\* As some lines in the figure are not used in the construction, though needed for the demonstration, the student should draw it himself to a large scale.



BC, measured parallel to AC, being 6 chains, and DC 18 chains. The angle at C is fixed by a "tie-line" AB = 48°00', BC being 42°00', and CA being 30°00'. *Ans.*

CL = 27.31 chains, or CL' = 7.69 chains.

The figure is on a scale of 20 chains to 1 inch = 1 : 15840.

If the angle of the field and the position of the point P are given by bearings or angles, proceed thus : Find the perpendicular distances, PQ and PR, from the given point to the sides, by the formulas  $PQ = PC \cdot \sin. PCQ$ ; and  $PR = PC \cdot \sin. PCR$ . Let  $PQ = q$ ,  $PR = p$ , and the required content =  $c$ . Then  $CL = \frac{c}{p} \pm \sqrt{\left(\frac{c^2}{p^2} - \frac{2qc}{p \sin. LCM}\right)}$ .

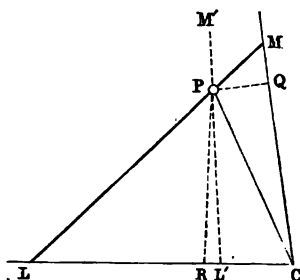


FIG. 297.

*Demonstration.* Suppose the line LM drawn. Then, by Art. 61, note, the required content,  $c = \frac{1}{2} \cdot CL \times OM \cdot \sin. LCM$ . This content will also equal the sum of the two triangles LCP and MCP—i. e.,  $c = \frac{1}{2} \cdot CL \times p + \frac{1}{2} \cdot OM \times q$ . The first of these equations gives  $CM = \frac{2c}{CL \cdot \sin. LCM}$ .

Substituting this in the second equation, we have

$$c = \frac{1}{2} \cdot CL \times p + \frac{c q}{CL \cdot \sin. LCM}.$$

Whence,  $\frac{1}{2} p \cdot CL^2 \cdot \sin. LCM + c q = c \cdot CL \cdot \sin. LCM$ .

Transposing and dividing by the coefficient of  $CL^2$ , we get

$$CL^2 - \frac{2c}{p} \cdot CL = - \frac{2cq}{p \cdot \sin. LCM}.$$

$$CL = \frac{c}{p} \pm \sqrt{\left(\frac{c^2}{p^2} - \frac{2cq}{p \cdot \sin. LCM}\right)}.$$

If the given point is *outside* of the lines CL and CM, conceive the desired line to be drawn from it, and another line to join the given point to the corner of the field. Then, as above, get expressions for the two triangles thus formed, and put their sum equal to the expression for the triangle which comprehends them both, and thence deduce the desired distance, nearly as above.

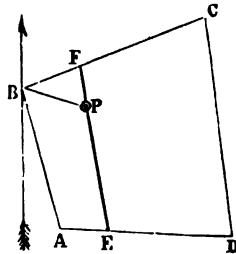
*Example.* Let the angle  $LCM = 82^\circ$ . Let it be required to part off the same area as in the preceding example. Let  $PC = 19.75$ ,  $PCQ = 17^\circ 30\frac{1}{2}'$ ,  $PCR = 64^\circ 29\frac{1}{2}'$ . Required CL. *Ans.*  $PQ = 5.94$ ,  $PR = 17.82$ , and therefore, by the formula,  $CL =$

27.31, or  $CL' = 7.69$ ; corresponding to the graphical solution. The figure is on the same scale.

If the given point were *without* the field, the division-line could be determined in a similar manner.

**421. To part off a Quadrilateral.** Conceive the two sides of the field which the division-line will intersect,  $DA$  and  $CB$ , produced till they meet at a point  $G$ , not shown in the figure. Calculate the triangle thus formed outside of the field. Its area, increased by the required area, will be that of the triangle  $EFG$ . Then the problem is identical with that in the last article. The following example is that given in Gummere's "Surveying." The figure represents it on a scale of 20 chains to 1 inch  $= 1 : 15840$ .

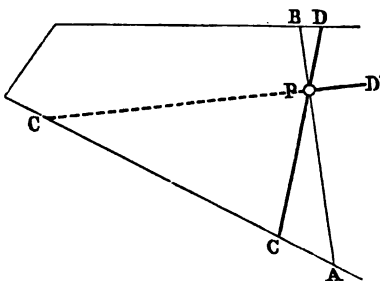
FIG. 298.



*Example.* A field is bounded thus: N.  $14^\circ$  W., 15.20; N.  $70\frac{1}{2}^\circ$  E., 20.43; S.  $6^\circ$  E., 22.79; N.  $86\frac{1}{2}^\circ$  W., 18.00. A spring within it bears from the second corner S.  $75^\circ$  E., 7.90. It is required to cut off 10 acres from the west side of the field by a straight fence through the spring. How far will it be from the first corner to the point at which the division-fence meets the fourth side? *Ans.* 4.6357 chains.

**422. To part off any Figure.** Let it be required to part off from

FIG. 299.



a field a certain area by a line passing through a given point  $P$  within the field. Run a guess-line  $AB$  through  $P$ . Calculate the area which it parts off. Call the difference between it and the required area  $= d$ . Let  $CD$  be the desired line of division, and let  $P$  represent the angle,  $APC$

or  $BPD$ , which it makes with the given line. Obtain the angles  $PAC = A$ , and  $PBD = B$ , either by measurement, or by de-

duction from bearings. Measure P A and P B. Then the desired angle P will be given by the following formula :

$$\begin{aligned} \text{Cot. } P = & -\frac{1}{2} \left( \text{cot. } A + \text{cot. } B - \frac{A P^2 - B P^2}{2d} \right) \pm \\ & \left[ \sqrt{\frac{A P^2 \cdot \text{cot. } B - B P^2 \cdot \text{cot. } A}{2d} - \text{cot. } A \cdot \text{cot. } B +} \right. \\ & \left. \frac{1}{2} \left( \text{cot. } A + \text{cot. } B - \frac{A P^2 - B P^2}{2d} \right)^2 \right]. \end{aligned}$$

If the guess-line be run so as to be perpendicular to one of the sides of the field, at A, for example, the preceding expression reduces to the following simpler form :

$$\begin{aligned} \text{Cot. } P = & -\frac{1}{2} \left( \text{cot. } B - \frac{A P^2 - B P^2}{2d} \right) \pm \\ & \sqrt{\left[ \frac{A P^2 \cdot \text{cot. } B}{2d} + \frac{1}{2} \left( \text{cot. } B - \frac{A P^2 - B P^2}{2d} \right)^2 \right]}. \end{aligned}$$

*Demonstration.* The difference  $d$ , between the areas parted off by the guess-line A B, and the required line C D, is equal to the difference between the triangles A P C and B P D.

$$\text{By Art. 61, note, the triangle A P C} = \frac{1}{2} \cdot A P^2 \cdot \frac{\sin. A \cdot \sin. P}{\sin. (A + P)}.$$

$$\text{Similarly, the triangle B P D} = \frac{1}{2} \cdot B P^2 \cdot \frac{\sin. B \cdot \sin. P}{\sin. (B + P)}.$$

$$\therefore d = \frac{1}{2} \cdot A P^2 \cdot \frac{\sin. A \cdot \sin. P}{\sin. (A + P)} - \frac{1}{2} B P^2 \cdot \frac{\sin. B \cdot \sin. P}{\sin. (B + P)}.$$

$$\text{By the expression for } \sin. (a + b) \text{ [Trigonometry, Art. 8], we have}$$

$$d = \frac{1}{2} A P^2 \cdot \frac{\sin. A \cdot \sin. P}{\sin. A \cdot \cos. P + \sin. P \cdot \cos. A} - \frac{1}{2} B P^2 \cdot \frac{\sin. B \cdot \sin. P}{\sin. B \cdot \cos. P + \sin. P \cdot \cos. B}$$

Dividing each fraction by its numerator, and remembering that  $\frac{\cos. a}{\sin. a} = \cot. a$ , we have

$$d = \frac{\frac{1}{2} A P^2}{\cot. P + \cot. A} - \frac{\frac{1}{2} B P^2}{\cot. P + \cot. B}.$$

For convenience, let  $p = \cot. P$ ;  $a = \cot. A$ ; and  $b = \cot. B$ . The above equation will then read, multiplying both sides by 2,

$$2d = \frac{A P^2}{p + a} - \frac{B P^2}{p + b}.$$

Clearing of fractions, we have

$$2dp^2 + 2dap + 2dbp + 2dab = p \cdot A P^2 + b \cdot A P^2 - p \cdot B P^2 - a \cdot B P^2.$$

Transposing, dividing through by  $2d$ , and separating into factors, we get

$$p^2 + \left( a + b - \frac{A P^2 - B P^2}{2d} \right) p = \frac{b \cdot A P^2 - a \cdot B P^2}{2d} - ab.$$

$$\therefore p = -\frac{1}{2} \left( a + b - \frac{A P^2 - B P^2}{2d} \right) \pm \sqrt{\left[ \frac{b \cdot A P^2 - a \cdot B P^2}{2d} \right]}$$

$$-ab + \frac{1}{2} \left( a + b - \frac{AP^2 - BP^2}{2d} \right)^2 \Big].$$

If  $A = 90^\circ$ ,  $\cot. A = 0$ ; and the expression reduces to the simpler form given in the article.

*Example.* It was required to cut off from a field twelve acres by a line passing through a spring P. A guess-line, A B, was run making an angle with one side of the field, at A, of  $55^\circ$ , and with the opposite side, at B, of  $81^\circ$ . The area thus cut off was found to be 13.10 acres. From the spring to A was 9.30 chains, and to B 3.30 chains. Required the angle which the required line, C D, must make with the guess-line, A B, at P. *Ans.*  $20^\circ 45'$ ; or  $-86^\circ 25'$ . The heavy broken line, C' D', shows the latter.

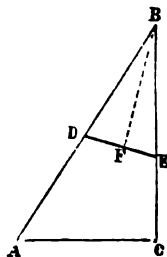
The scale of the figure is 10 chains to 1 inch = 1 : 7920.

If the given point were outside of the field, the calculations would be similar.

#### F. BY THE SHORTEST POSSIBLE LINE.

**423. To part off a Triangle.** Let it be required to part off a triangular space, B D E, of given content, from the corner of a field, A B C, by the shortest possible line, D E.

FIG. 300.



From B set off B D and B E each equal to  $\sqrt{\left( \frac{2 B D E}{\sin. B} \right)}$ . The line D E thus obtained will be perpendicular to the line, B F, which bisects the angle B. The length of D E =  $\frac{\sqrt{(2 \cdot D B E \cdot \sin. B)}}{\cos. \frac{1}{2} B}$ .

*Demonstration.* Conceive a perpendicular, B F, to be let fall from B to the required line D E. Let B represent the angle D B E, and  $\beta$  the unknown angle D B F. The angle B D F =  $90^\circ - \beta$ ; and the angle B E F =  $90^\circ - (B - \beta) = 90^\circ - B + \beta$ . By Art. 61, note, the area of the triangle D B E =  $\frac{1}{2} D E^2 \cdot \frac{\sin. B D E \cdot \sin. B E D}{\sin. (B D E + B E D)} = \frac{1}{2} \cdot D E^2 \cdot \frac{\sin. (90^\circ - \beta) \sin. (90^\circ - B + \beta)}{\sin. B}$ .

$$\text{Hence, } D E^2 = \frac{2 \times D B E \times \sin. B}{\sin. (90^\circ - \beta) \cdot (\sin. (90^\circ - B + \beta))} = \frac{2 \times D B E \times \sin. B}{\cos. \beta \cdot \cos. (B - \beta)}.$$

Now, in order that D E may be the least possible, the denominator of the last fraction must be the greatest possible. It may be transformed, by the formula,  $\cos. a \cdot \cos. b = \frac{1}{2} \cos. (a + b) + \frac{1}{2} \cos. (a - b)$  [Trigonometry, Art. 8], into  $\frac{1}{2} \cos. B + \frac{1}{2} \cos. (B - 2\beta)$ . Since B is constant, the value of

this expression depends on its second term, and that will be the greatest possible when  $B - 2\beta = 0$ , in which case  $\beta = \frac{1}{2}B$ .

It hence appears that the required line DE is perpendicular to the line, BF, which bisects the given angle B. This gives the *direction* in which DE is to be run.

Its starting-point, D or E, is found thus: The area of the triangle DBE  $= \frac{1}{2} BD \cdot BE \cdot \sin. B$ . Since the triangle is isosceles, this becomes

$$DBE = \frac{1}{2} BD^2 \cdot \sin. B; \text{ whence } BD = \sqrt{\left(\frac{2 DBE}{\sin. B}\right)}.$$

DE is obtained from the expression for DE<sup>2</sup>, which becomes, making  $\beta = \frac{1}{2}B$ ,

$$DE^2 = \frac{2 \times DBE \times \sin. B}{\cos. \frac{1}{2} B \cdot \cos. \frac{1}{2} B}, \text{ whence, } DE = \frac{\sqrt{(2 \cdot DBE \cdot \sin. B)}}{\cos. \frac{1}{2} B}.$$

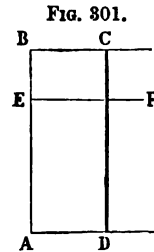
*Example.* Let it be required to part off 1·3 acre from the corner of a field, the angle, B, being 30°. *Ans.* BD = BE = 7·21; and DE = 3·73.

The scale of the figure is 10 chains to 1 inch = 1 : 7920.

#### G. LAND OF VARIABLE VALUE.

**424.** Let the figure represent a field in which the land is of two qualities and values, divided by the "quality-line" EF. It is required to part off from it a quantity of land worth a certain sum, by a straight fence parallel to AB.

Multiply the value per acre of each part by its length (in chains) on the line AB, add the products, multiply the value to be set off by 10, divide by the above sum, and the quotient will be the desired breadth, BC or AD, in chains.



*Demonstration.* Let  $a$  = value per acre of one portion of the land, and  $b$  that of the other portion. Let  $x$  = the width required, BC or AD. Then the value of BCFE  $= a \times \frac{x \times BE}{10}$ , and the value of ADFE  $= b \times \frac{x \times AE}{10}$ .

Putting the sum of these equal to the value required to be parted off, we obtain  $x = \frac{\text{value required} \times 10}{a \times BE + b \times AE}$ .

*Example.* Let the land on one side of EF be worth \$200 per acre, and on the other side \$100. Let the length of the former, BE, be 10 chains, and EA be 30 chains. It is required to part off

a quantity of land worth \$7,500. *Ans.* The width of the desired strip will be 15 chains.

The scale of the figure is 40 chains to 1 inch = 1 : 31680.

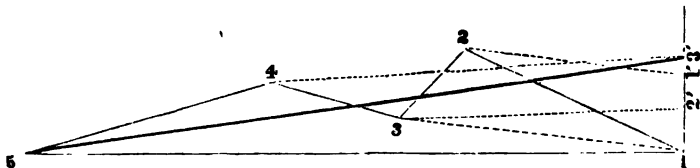
If the "quality-line" be not perpendicular to A B, it may be made so by "giving and taking," or as in the article following this one.

The same method may be applied to land of any number of different qualities ; and a combination of this method with the preceding problems will solve any case which may occur.

#### H. STRAIGHTENING CROOKED FENCES.

**425.** It is often required to substitute a straight fence for a crooked one, so that the former shall part off precisely the same quantity of land as did the latter. This can be done on a plat by

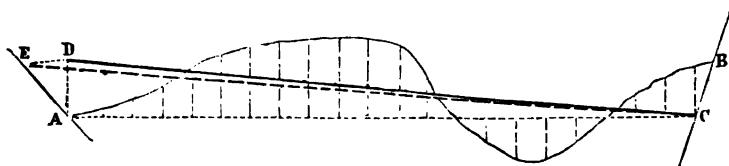
FIG. 302.



the method given in Art. 76, by which the irregular figure 1...2...3...4...5 is reduced to the equivalent triangle 1...5...3', and the straight line 5...3' therefore parts off the same quantity of land on either side as did the crooked one. The distance from 1 to 3', as found on the plat, can then be set out on the ground and the straight fence be then ranged from 3' to 5.

The work may be done on the ground more accurately by run-

FIG. 303.



ning a guess-line, A C, Fig. 303, across the bends of the fence which crooks from A to B, measuring offsets to the bends on each

side of the guess-line, and calculating their content. If the sums of these areas on each side of  $AC$  chanced to be equal, that would be the line desired; but if, as in the figure, it passes too far on one side, divide the difference of the areas by  $AC$ , and set off the quotient at right angles to  $AC$ , from  $A$  to  $D$ .  $DC$  will then be a line parting off the same quantity of land as did the crooked fence. If the fence at  $A$  was not perpendicular to  $AC$ , but oblique, as  $AE$ , then from  $D$  run a parallel to  $AC$ , meeting the fence at  $E$ , and  $EC$  will be the required line.

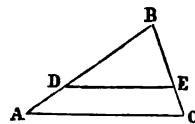
### DIVIDING UP LAND.

**426.** Most of the problems for "dividing up" land may be brought under the cases in the preceding articles, by regarding one of the portions into which the figure is to be divided as an area to be "parted off" from it. Many of them, however, can be most neatly executed by considering them as independent problems, and this will be here done. They will be arranged, first, according to the simplicity of the figure to be divided up, and then sub-arranged, according to the manner of the division.

#### Division of Triangles.

**427. By Lines parallel to a Side.** Suppose that the triangle  $ABC$  is to be divided into two equivalent parts by a line parallel to  $AC$ . The desired point,  $D$ , from which this line is to start, will be obtained by measuring  $BD = AB \sqrt{\frac{1}{2}}$ . So, too,  $E$  is fixed by  $BE = BC \sqrt{\frac{1}{2}}$ .

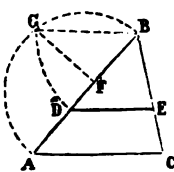
FIG. 304.



Generally, to divide the triangle into two parts,  $BDE$  and  $ACED$ , which shall have to each other a ratio

$$= m : n, \text{ we have } BD = AB \sqrt{\frac{m}{m+n}}.$$

FIG. 305.



This may be constructed thus: Describe a semicircle on  $AB$  as a diameter. From  $B$  set off  $BF = \frac{m}{m+n} \cdot BA$ . At  $F$  erect a perpendicular meeting the semicircle at  $G$ . Set off  $BG$  from  $B$  to  $D$ .  $D$  is the starting-point of the division.

line required. In the figure, the two parts are as 2 to 3, and  $BF$  is therefore  $= \frac{2}{5} BA$ .

To divide the triangle  $ABC$  into five equivalent parts, we should have, similarly,  $BD = AB \sqrt{\frac{1}{5}}$ ;  $BD' = AB \sqrt{\frac{2}{5}}$ ;  $BD'' = AB \sqrt{\frac{3}{5}}$ ;  $BD''' = AB \sqrt{\frac{4}{5}}$ .

The same method will divide the triangle into any desired number of parts having any ratios to each other.

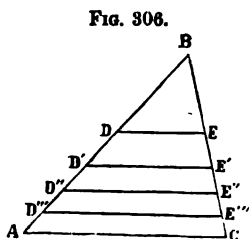


FIG. 306.

#### 428. By Lines perpendicular to a Side.

Suppose that  $ABC$  is to be divided into two parts having a ratio  $= m : n$ , by a line perpendicular to  $AC$ . Let  $EF$  be the dividing line whose position is required. Let  $BD$  be a perpendicular let fall from  $B$  to  $AC$ .

Then is  $AE = \sqrt{(AC \times AD \times \frac{m}{m+n})}$ . In this figure,  $AEF : EFBC :: m : n :: 1 : 2$ .

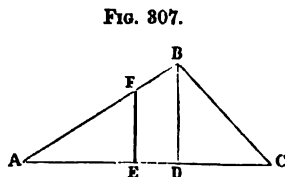


FIG. 307.

If the triangle had to be divided into two equivalent parts, the above expression would become  $AE = \sqrt{(\frac{1}{2} AC \times AD)}$ .

*Demonstration.* By hypothesis,  $AEF : EFBC :: m : n$ ; whence  $AEF : ABC :: m : m + n$ ; and  $AEF = ABC \frac{m}{m+n} = \frac{AC \times DB}{2} \cdot \frac{m}{m+n}$ . Also,  $AEF = \frac{1}{2} \cdot AE \times EF$ .

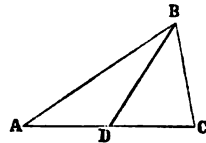
The similar triangles  $AEF$  and  $ABD$  give  $AD : DB :: AE : EF = \frac{DB \times AE}{AD}$ . The second expression for  $AEF$  then becomes  $AEF = \frac{1}{2} AE \cdot \frac{DB \times AE}{AD}$ . Equating this with the other value of  $AEF$ , we have  $\frac{AC \times DB}{2} \cdot \frac{m}{m+n} = \frac{AE^2 \times DB}{2 \cdot AD}$ ; whence  $AE = \sqrt{(AC \times AD \times \frac{m}{m+n})}$ .

**429. By Lines running in any Given Direction.** Let a triangle,  $ABC$ , be given to be divided into two parts, having a ratio  $= m : n$ , by a line making a given angle with a side. Part off, as in Art. 413 or 414, Fig. 292, an area  $BFG = \frac{m}{m+n} \cdot ABC$ .



**430. By Lines starting from an Angle.** Divide the side opposite to the given angle into the required number of parts, and draw lines from the angle to the points of division. In the figure the triangle is represented as being thus divided into two equivalent parts.

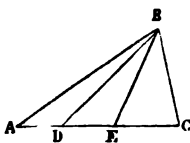
FIG. 308.



If the triangle were required to be divided into two parts, having to each other a ratio =

$m : n$ , we should have  $AD = AC \frac{m}{m+n}$ , and  $DC = AC \frac{n}{m+n}$ .

FIG. 309.



If the triangle had to be divided into three parts which should be to each other  $:: m : n$

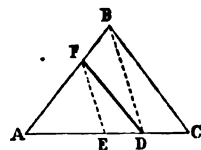
$: p$ , we should have  $AD = AC \frac{m}{m+n+p}$ ,

$DE = AC \frac{n}{m+n+p}$ , and  $EC = AC \frac{p}{m+n+p}$ .

Suppose that a triangular field,  $ABC$ , had to be divided among five men, two of them to have a quarter each, and three of them each a sixth. Divide  $AC$  into two equal parts, one of these again into two equal parts, and the other one into three equal parts. Run the lines from the four points thus obtained to the angle  $B$ .

**431. By Lines starting from a Point in a Side.** Suppose that the triangle  $ABC$  is to be divided into *two* equivalent parts by a line starting from a point  $D$  in the side  $AC$ . Take a point  $E$  in the middle of  $AC$ . Join  $BD$ , and from  $E$  draw a parallel to it, meeting  $AB$  in  $F$ .  $DF$  will be the dividing line required.

FIG. 310.



The point  $F$  will be most easily obtained

on the ground by the proportion  $AD : AB :: AE = \frac{1}{2} AC : AF$ .

The altitude of  $AFD$  of course equals  $\frac{1}{2} ABC \div \frac{1}{2} AD$ .

If the triangle is to be divided into two parts having any other ratio to each other, divide  $AC$  in that ratio, and then proceed as before. Let this ratio =  $m : n$ , then  $AF = \frac{AB \times AC}{AD} \cdot \frac{m}{m+n}$ .

*Demonstration.* In Fig. 810, conceive the line  $EB$  to be drawn. The triangle  $AEB = \frac{1}{2} ABC$ , having the same altitude and half the base; and  $AFD = AEB$ , because of the equivalency of the triangles  $EFD$  and  $EFB$ , which, with  $AEF$ , make up  $AFD$  and  $AEB$ .

The point  $F$  is fixed by the similar triangles  $ADB$  and  $AEF$ .

The expression for  $AF$ , in the last paragraph, is given by the proportion,

$$ABC : ADF :: AB \times AC : AD \times AF;$$

$$\text{whence, } AF = \frac{AB \times AC}{AD} \cdot \frac{ADF}{ABC} = \frac{AB \times AC}{AD} \cdot \frac{m}{m+n}.$$

Next suppose that the triangle  $ABC$  is to be divided into *three* equivalent parts, meeting at  $D$ . The altitudes,  $EF$  and  $GH$ , of the parts  $ADE$  and  $DCG$ , will be obtained by dividing  $\frac{1}{3} ABC$ , by half of the respective bases  $AD$  and  $DC$ .

If one of these quotients gives an altitude greater than that of the triangle  $ABC$ , it will show that the two lines  $DE$  and  $DG$  would both cut the same side, as in Fig. 312, in which  $EF$  is obtained as above, and  $GH = \frac{1}{3} ABC \div \frac{1}{2} AD$ .

In practice it is more convenient to determine the points  $F$  and  $G$ , by these proportions:

$$BK : AK :: EF : AF; \text{ and } BK : AK :: GH : AH.$$

The division of a triangle into a greater number of parts, having any ratios, may be effected in a similar manner.

This problem admits of a more elegant solution, analogous to that given for the division into two parts, graphically. Divide  $AC$  into three equal parts at  $L$  and  $M$ . Join  $BD$ , and from  $L$  and  $M$  draw parallels to it, meeting  $AB$  and  $BC$  in  $E$  and  $G$ . Draw  $ED$  and  $GD$ , which will be the desired lines of division. The figure is the same triangle as Fig. 311.

The points  $E$  and  $G$  can be obtained on the ground by measur-

Fig. 311.

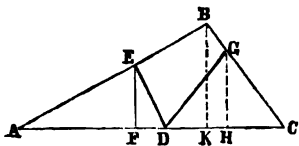


Fig. 312.

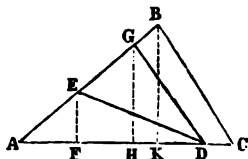
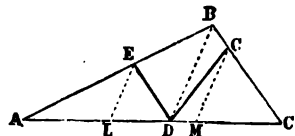


Fig. 313.

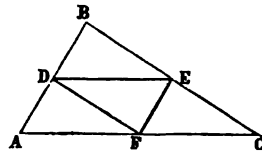


ing  $AD$  and  $AB$ , and making the proportion  $AD : AB :: \frac{1}{2} AC : AE$ . The point  $G$  is similarly obtained.

The same method will divide a triangle into a greater number of parts.

To divide a triangle into *four* equivalent triangles by lines terminating in the sides, is very easy. From  $D$ , the middle point of  $AB$ , draw  $DE$  parallel to  $AC$ , and from  $F$ , the middle of  $AC$ , draw  $FD$  and  $FE$ . The problem is now solved.

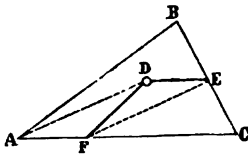
FIG. 314.



#### 432. By Lines passing through a Point

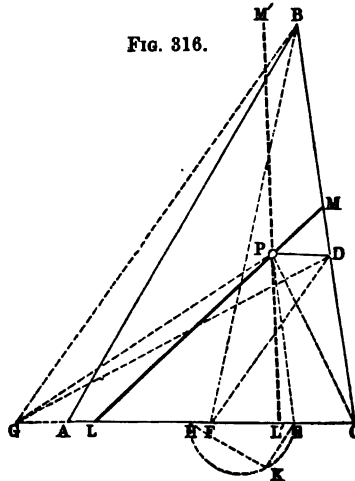
**within the Triangle.** Let  $D$  be a given point (such as a well, etc.) within a triangular field  $ABC$ , from which fences are to run so as to divide the triangle into *two* equivalent parts. Join  $AD$ . Take  $E$  in the middle of  $BC$ , and from it draw a parallel to  $DA$ , meeting  $AC$  in  $F$ .  $EDF$  is the fence required.

FIG. 315.



If it be required to divide a triangle into two equivalent parts by a straight line passing through a point within it, proceed thus: Let  $P$  be the given point. From  $P$  draw  $PD$  parallel to  $AC$ , and  $PE$  parallel to  $BC$ . Bisect  $AC$  at  $F$ . Join  $FD$ . From  $B$  draw  $BG$  parallel to  $DF$ . Then bisect  $GC$  in  $H$ . On  $HE$  describe a semicircle. On it set off  $EK = EC$ . Join  $KH$ . Set off  $HL = HK$ . The line  $LM$  drawn from  $L$ , through  $P$ , will be the division-line required.

FIG. 316.



This figure is the same as that of Art. 416. The triangle  $ABC$  contains 62.35 acres, and the distance  $CL = 27.31$  chains, as in the example in that article.

433. Next suppose that the triangle  $A B C$  is to be divided into three equivalent parts by lines starting from a point  $D$ , within the triangle, given by the rectangular co-ordinates  $A E$  and  $E D$ . Let  $E D$  be one of the lines of division, and  $F$  and  $G$  the other points required. The point  $F$  will be determined if  $A H$  is known;

$A H$  and  $H F$  being its rectangular co-ordinates. From  $B$  let fall the perpendicular  $B K$  on  $A C$ .

Then is  $A H = \frac{A K (\frac{2}{3} A B C - A E \times E D)}{A E \times B K - E D \times A K}$ . The position of the other point,  $G$ , is determined in a similar manner.

*Demonstration.* Let  $A E = x$ ,  $E D = y$ ,  $A H = x'$ ,  $H F = y'$ ,  $A K = a$ ,  $K B = b$ .

The quadrilateral  $A F D E$ , equivalent to  $\frac{1}{3} A B C$ , but which we will represent generally by  $m^2$ , is made up of the triangle  $A F H$  and the trapezoid  $F H E D$ .

$$A F H = \frac{1}{2} \cdot x' y'. \quad F H E D = \frac{1}{2} (x - x') (y + y').$$

$$\therefore A F D E = m^2 = \frac{1}{2} \cdot x' y' + \frac{1}{2} (x - x') (y + y') = \frac{1}{2} x (y + y') - \frac{1}{2} x' y'.$$

The similar triangles,  $A H F$  and  $A K B$ , give

$$a : b :: x' : y' = \frac{b x'}{a}.$$

Substituting this value of  $y'$  in the expression for  $m^2$ , we have

$$m^2 = \frac{1}{2} x \left( y + \frac{b x'}{a} \right) - \frac{1}{2} x' y;$$

$$\text{whence, } x' = \frac{a (2 m^2 - x y)}{b x - a y} = \frac{A K (\frac{2}{3} A B C - A E \times E D)}{K B \times A E - A K \times E D}.$$

The formula is general, whatever may be the ratio of the area  $m^2$  to that of the triangle  $A B C$ .

Let  $D B$ , instead of  $D E$ , be one of the required lines of division. Divide  $\frac{1}{3} A B C$  by half of the perpendicular  $D H$ , let fall from  $D$  to  $A B$ , and the quotient will be the distance  $B F$ . To find  $G$ , if, as in this figure, the triangle  $B D C (= B C \times \frac{1}{2} D K)$  is less than  $\frac{1}{3} A B C$ , divide the excess of the

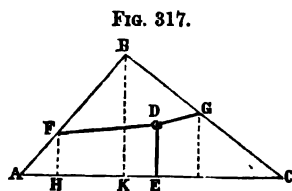


FIG. 317.

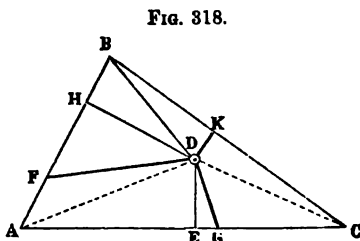


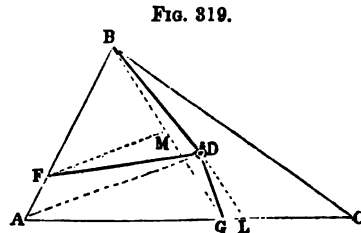
FIG. 318.

latter (which will be  $CDG$ ) by  $\frac{1}{2} DE$ , and the quotient will be  $CG$ .

*Example.* Let  $AB = 30.00$ ;  $BC = 45.00$ ;  $CA = 50.00$ . Let the perpendiculars from  $D$  to the sides be these:  $DE = 10.00$ ;  $DH = 20.00$ ;  $DK = 5.17\frac{1}{2}$ . The content of the triangle  $ABC$  will be  $666.6$  square chains. Each of the small triangles must therefore contain  $222.2$  square chains,  $BD$  being one division-line. We shall therefore have  $BF = 222.2 \div \frac{1}{2} DH = 22.2$  chains.  $BD C = 45 \times \frac{1}{2} \times 5.17\frac{1}{2} = 116.4$  square chains, not enough for a second portion, but leaving  $105.8$  square chains for  $CDG$ ; whence  $CG = 21.16$  chains. To prove the work, calculate the content of the remaining portion,  $G D F A$ . We shall find  $DGA = 144.2$  square chains, and  $ADF = 78.0$  square chains, making together  $222.2$  square chains, as required.

The scale of Fig. 318 is 30 chains to 1 inch = 1 : 23760.

**434.** The preceding case may be also solved graphically, thus: Take  $CL = \frac{1}{2} AC$ . Join  $DL$ , and from  $B$  draw  $BG$  parallel to  $DL$ . Join  $DG$ . It will be a second line of division. Then take a point,  $M$ , in the middle of  $BG$ , and from it draw a line,  $MF$ , parallel to  $DA$ .  $DF$  will be the third line of division. This method is neater on paper than the preceding, but less convenient on the ground.



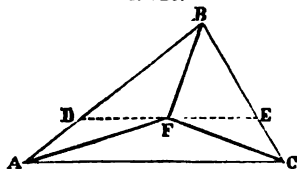
*Demonstration.* In Fig. 319  $DG$  is a second line of division, because, drawing  $BL$ , the triangle  $BLC = \frac{1}{2} ABC$ ; and  $BDGC$  is equivalent to  $BLC$ , because of the common part  $BCLD$ , and the equivalency of the triangles  $DLG$  and  $DLB$ .

To prove that  $DF$  is a third line of division, join  $MD$  and  $MA$ . Then  $BMA = \frac{1}{2} BGA$ . From  $BMA$  take  $MFA$  and add its equivalent  $MFD$ , and we have  $MDFB = \frac{1}{2} BGA = \frac{1}{2} (ABDG - BDG) = \frac{1}{2} (\frac{1}{2} ABC - BDG) = \frac{1}{4} ABC - \frac{1}{2} BDG$ . To  $MDFB$  add  $MDB$ , and add its equivalent,  $\frac{1}{2} BDG$ , to the other side of the equation, and we have  $MDFB + MDB = \frac{1}{4} ABC - \frac{1}{2} BDG + \frac{1}{2} BDG$ ; or,  $BDF = \frac{1}{4} ABC$ .

**435.** Let it be required to divide the triangle  $ABC$  into three equivalent triangles, by lines drawn from the three angular points

to some *unknown* point within the triangle. This point is now to

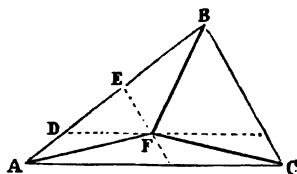
FIG. 320.



be found. On any side, as  $AB$ , take  $AD = \frac{1}{3} AB$ . From  $D$  draw  $DE$  parallel to  $AC$ . The middle,  $F$ , of  $DE$ , is the point required.

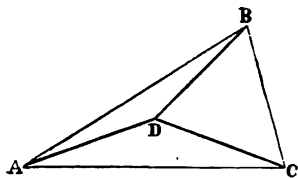
If the three small triangles are not to be equivalent, but are to have to each other the ratios  $m : n : p$ , divide a side,  $AB$ , into parts having these ratios, and through each point of division,  $D, E$ , draw a parallel to the side nearest to it. The intersection of these parallels, in  $F$ , is the point required. In the figure the parts  $ACF, ABF, BCF$ , are as  $2 : 3 : 4$ .

FIG. 321.



**436.** Let it be required to find the position of a point,  $D$ , situated within a given triangle,  $ABC$ , and equally distant from the points,  $A, B, C$ ; and to determine the ratios to each other of the three triangles into which the given triangle is divided.

FIG. 322.

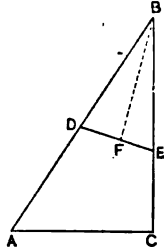


By construction, find the center of the circle passing through  $A, B, C$ . This will be the required point.

By calculation, the distance  $DA = DB = DC = \frac{AB \times BC \times CA}{4 \times \text{area } ABC}$ .

The three small triangles will be to each other as the sines of their angles at  $D$ —i. e.,  $ADB : ADC : BDC :: \sin. ADB : \sin. ADC : \sin. BDC$ . These angles are readily found, since the sine of half of each of them equals the opposite side divided by twice one of the equal distances.

FIG. 323.



**437. By the Shortest Possible Line.** Let it be required to divide the triangle  $ABC$  by the short-

est possible line, D E, into two parts, which shall be to each other  $:: m : n$ ; or  $D B E : A B C :: m : m + n$ .

From the smallest angle, B, of the triangle, measure along the sides, B A and B C, a distance  $B D = B E = \sqrt{\left(\frac{m}{m+n} \times A B \times B C\right)}$ .

D E is the line required. It is perpendicular to the line B F which bisects the angle A B C; and it is

$$= \frac{\sin. B}{\cos. \frac{1}{2} B} \sqrt{\left(\frac{m}{m+n} \times A B \times B C\right)}.$$

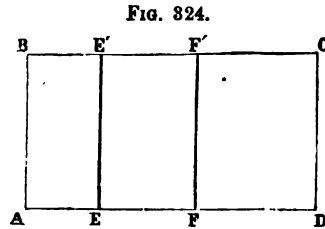
The formulas are obtained from Art. 419.

### Division of Rectangles.

**438. By Lines parallel to a Side.** Divide two opposite sides into the required number of parts, either equal or in any given ratio to each other, and the lines joining the points of division will be the lines desired.

The same method is applicable to any parallelogram.

*Example.* A rectangular field A B C D, measuring 15·00 chains by 8·00, is bought by three men, who pay respectively \$300, \$400, and \$500. It is to be divided among them in that proportion. *Ans.* The portion of the first, A E E' B, is obtained by making the proportion  $300 + 400 + 500 : 300 :: 15\cdot00 : A E = 3\cdot75$ . E F is in



like manner found to be 5·00; and  $F D = 6\cdot25$ .  $B E'$  is made equal to  $A E$ ;  $E' F'$  to  $E F$ ; and  $F' C$  to  $F D$ . Fences from E to  $E'$ , and from F to  $F'$ , will divide the land as required.

The scale of the figure is 10 chains to 1 inch = 1 : 7920.

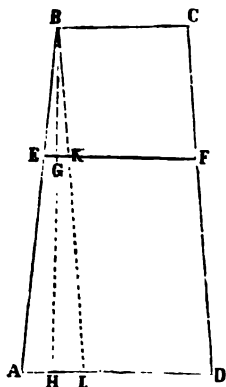
The other modes of dividing up rectangles will be given under the head of "Quadrilaterals," Art. 443, etc.

### Division of Trapezoids.

**439. By Lines parallel to the Bases.** Given the bases and a third side of the trapezoid, A B C D, to be divided into two parts, such that  $B C F E : E F D A :: m : n$ .

The length of the desired dividing line,

FIG. 325.



$$EF = \sqrt{\left( \frac{m \times AD^2 + n \times BC^2}{m + n} \right)}.$$

$$\text{The distance } BE = \frac{AB(EF - BC)}{AD - BC}.$$

*Demonstration.* In Fig. 325, conceive the sides AB and DC, produced, to meet in some point P. Then, by reason of the similar triangles, ADP : BCP :: AD<sup>2</sup> : BC<sup>2</sup>, whence, by "division," ADP - BCP = ABCD : BCP :: AD<sup>2</sup> - BC<sup>2</sup> : BC<sup>2</sup>.

In like manner, comparing EFP and BCP, we get EBCF : BCP :: EF<sup>2</sup> - BC<sup>2</sup> : BC<sup>2</sup>. Combining these two proportions, we have ABCD : EBCF :: AD<sup>2</sup> - BC<sup>2</sup> : EF<sup>2</sup> - BC<sup>2</sup>; or,  $m + n : m :: AD^2 - BC^2 : EF^2 - BC^2$ . Whence,  $(m + n)EF^2 - m \cdot BC^2 - nBC^2 = m \cdot AD^2 - m \cdot BC^2$ ;

$$\therefore EF = \sqrt{\left( \frac{m \times AD^2 + n \times BC^2}{m + n} \right)}.$$

Also, from the similar triangles formed by drawing BL parallel to CD, we have

$$AL : EK :: BA : BE = \frac{BA \times EK}{AL} = \frac{AB(EF - BC)}{AD - BC}.$$

*Example.* Let AD = 30 chains; BC = 20 chains; and AB = 54½ chains; and the parts to be as 1 to 2; required EF and BE.  
*Ans.* EF = 23.80; and BE = 20.65.

The figure is on a scale of 30 chains to 1 inch = 1: 23760.

440. Given the bases of a trapezoid, and the perpendicular distance, BH, between them; it is required to divide it as before, and to find EF, and the altitude, BG, of one of the parts. Let

$$BCFE : EFDA :: m : n. \text{ Then } BG = -\frac{BC \times BH}{AD - BC} +$$

$$\sqrt{\left[ \frac{m}{m + n} \times \frac{2 \times ABCD \times BH}{AD - BC} + \left( \frac{BC \times BH}{AD - BC} \right)^2 \right]}.$$

$$EF = BC + BG \times \frac{AD - BC}{BH}.$$

*Demonstration.* Let BEFCO =  $\frac{m}{m + n} \cdot ABCD = a$ ; let BC =  $b$ ; BH =  $h$ ; and AD - BC =  $c$ . Also, let BG =  $x$ ; and EF =  $y$ . Draw BL parallel to CD. By similar triangles, AL : EK :: BA : BE :: BH :



BG; or,  $AD - BC : EF - BC :: BH : BG$ ; i. e.,  $c : y - b :: h : x$ ;  
whence  $x = \frac{h(y - b)}{c}$ .

Also, the area  $BEFC = a = \frac{1}{2} \cdot BG (EF + BC) = \frac{1}{2} x (y + b)$ ; whence  
 $y = \frac{2a}{x} - b$ .

Substituting this value of  $y$  in the expression for  $x$ , and reducing, we obtain

$$x^2 + \frac{2bh}{c}x = \frac{2ah}{c}; \text{ whence we have } x = -\frac{bh}{c} \pm \sqrt{\left(\frac{2ah}{c} + \frac{b^2h^2}{c^2}\right)}.$$

The second proportion above gives  $y - b = \frac{cx}{h}$ ; whence  $y = b + \frac{c}{h} \cdot x$ .

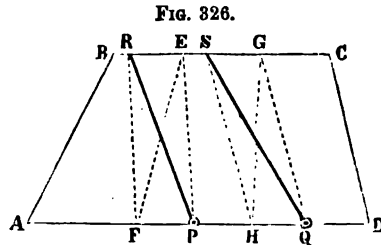
Replacing the symbols by their lines, we get the formulas in the text.

*Example.* Let  $AD = 30.00$ ;  $BC = 20.00$ ;  $BH = 54.00$ ; and the two parts to be to each other  $:: 46 : 89$ .

The above data give the content of  $ABCD = 1,350$  square chains. Substituting these numbers in the above formula, we obtain  $BG = 20.96$ , and  $EF = 23.88$ .

**441. By Lines starting from Points in a Side.** To divide a trapezoid into parts equivalent, or having any ratios, divide its parallel sides in the same ratios, and join the corresponding points.

If it be also required that the division-lines shall start from *given* points on a side, proceed thus: Let it be required to divide the trapezoid  $ABCD$  into three equivalent parts by fences starting from  $P$  and  $Q$ . Divide the trapezoid, as above directed, into three equivalent trapezoids by the lines  $EF$  and  $GH$ . These three trapezoids must now be transformed, thus: Join  $EP$ , and from  $F$  draw  $FR$  parallel to it. Join  $PR$ , and it will be one of the division-lines required.



The other division-line,  $QS$ , is obtained similarly.\*

**442. Other Cases.** For other cases of dividing trapezoids, apply those for quadrilaterals in general, given in the following articles.

\* If a line be drawn joining the middle points of the parallel bases of a trap-

*Division of Quadrilaterals.*

**443. By Lines parallel to a Side.** Let  $ABCD$  be a quadrilateral which it is required to divide, by a line  $EF$ , parallel to

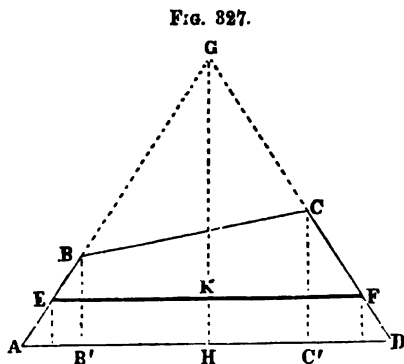


FIG. 327.

$AD$ , into two parts,  $BEFC$  and  $EFDA$ , which shall be to each other as  $m:n$ . Prolong  $AB$  and  $CD$  to intersect in  $G$ . Let  $a$  be the area of the triangle  $ADG$ , obtained by any method, graphical or trigonometrical, and  $a'$  = the area of the triangle  $BCG$ , obtained by subtracting the area of the given quadrilateral from that

of the triangle  $ADG$ . Then  $GK = GH \sqrt{\frac{ma + na'}{(m+n)a}}$ . Having measured this length of  $GK$  from  $G$  on  $GH$ , set off at  $K$  a perpendicular to  $GK$ , and it will be the required line of division.

*Demonstration.* In Fig. 327, since  $EF$  is parallel to  $AD$ , we have  $ADG : EGF :: GH^2 : GK^2$ .  $EGF$  is made up of the triangle  $BCG = a'$ , and the quadrilateral  $BEFC = \frac{m}{m+n}$ .  $ABCD = \frac{m}{m+n} \cdot (a - a')$ . Hence the above proportion becomes

$$a : a' + \frac{m}{m+n} (a - a') :: GH^2 : GK^2; \text{ or,}$$

$$(m+n)a : ma + na' :: GH^2 : GK^2; \text{ whence } GK = GH \sqrt{\frac{ma + na'}{(m+n)a}}.$$

$$GE \text{ is given by the proportion } GH : GK :: GA : GE = GA \cdot \frac{GK}{GH}.$$

In Fig. 328, the division into  $p$  parts is founded on the same principle. The triangle  $EFB = GBC + EFCB = a' + \frac{Q}{p}$ . Now  $ADG : EFG ::$

$$AG^2 : EG^2; \text{ or, } a' + \frac{Q}{p} : a' + \frac{Q}{p} :: AG^2 : EG^2;$$

$$\text{whence } GE = AG \sqrt{\frac{a' + \frac{Q}{p}}{a' + Q}}.$$

zoid, any line drawn through the middle of the first line, and intersecting the bases, will divide the trapezoid into two equivalent parts.

GL is obtained by taking the triangle LMG =  $a' + \frac{2Q}{p}$ ; and so for the rest.

Otherwise, take GE = GA  $\sqrt{\left(\frac{ma + na'}{(m+n)a}\right)}$ ; and from E run a parallel to AD.

If the two parts of the quadrilateral were to be equivalent,  $m = n$ , and we have GK = GH  $\sqrt{\left(\frac{a+a'}{2a}\right)}$ ; and consequently GE to GA in the same ratio.

*Example.* Let a quadrilateral, ABCD, be required to be thus divided, and let its angles, B and C, be given by rectangular coordinates, viz., AB' = 6.00; B'B = 9.00; DC' = 8.00; C'C = 13.00; B'C' = 24.00. Here GH is readily found to be 29.64; ADG = 563.16 square chains; and BGC = 220.16 square chains. Hence, by the formula, GK = 24.72; whence KH = GH - GK = 4.92; and the abscissas for the points E and F can be obtained by a simple proportion.

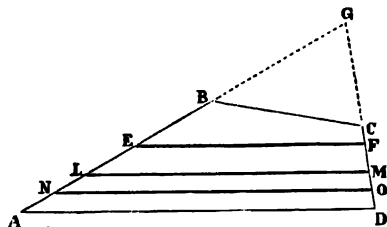
The scale of the figure is 20 chains to 1 inch = 1 : 15840.

If the quadrilateral be given by bearings, part off the desired area =  $\frac{n}{m+n} \cdot ABCD$ , by

FIG 328.

the formulas of Art. 403.

Suppose now that a quadrilateral, ABCD, is to be divided into  $p$  equivalent parts, by lines parallel to AD. Measure, or calculate by trigonometry, AG. Let Q be



the quadrilateral ABCD, and, as before,  $a' = BCG$ . Then

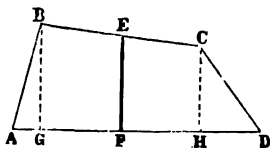
$$GE = AG \sqrt{\left\{ \frac{a' + \frac{Q}{p}}{a' + Q} \right\}}; \quad GL = AG \sqrt{\left\{ \frac{a' + \frac{2Q}{p}}{a' + Q} \right\}};$$

$$GN = AG \sqrt{\left\{ \frac{a' + \frac{3Q}{p}}{a' + Q} \right\}}; \text{ etc.}$$

If the quadrilateral be given by bearings, part off  $\frac{1}{p} \cdot ABCD$ , then part off  $\frac{2}{p} \cdot ABCD$ , etc.; so in any similar case.

- 444. By Lines perpendicular to a Side.** Let  $ABCD$  be a quadrilateral which is to be divided, by a line perpendicular to  $AD$ , into two parts having a ratio  $= m : n$ . By hypothesis,  $ABEF = \frac{m}{m+n} \cdot ABCD$ .

FIG. 329.

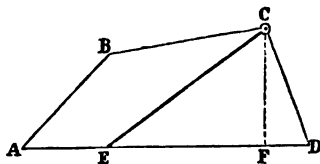


Taking away the triangle  $ABG$ , the remainder,  $GBEF$ , will be to the rest of the figure in a known ratio, and the position of  $EF$ , parallel to  $BG$ , will be found as in the last article.

- 445. By Lines running in any Given Direction.** To divide a quadrilateral  $ABCD$  into two parts  $: m : n$ , part off from it an area  $= \frac{m}{m+n} \cdot ABCD$ , by the methods of Art. 407 or 408, if the area parted off is to be a triangle, or Art. 409 if the area parted off is to be a quadrilateral.

- 446. By Lines starting from an Angle.**  $ABCD$  is to be divided, by the line  $CE$ , into two parts having the ratio  $m : n$ . Since the area of the triangle  $CDE = \frac{m}{m+n} \cdot ABCD$ ,  $DE$

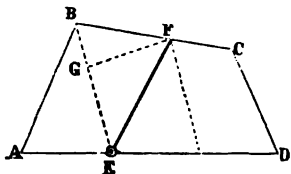
FIG. 330.



will be obtained by dividing this area by half of the altitude  $CF$ .

- 447. By Lines starting from Points in a Side.** Let it be required to divide  $ABCD$  into two parts  $: m : n$ , by a line starting from the point  $E$ . The area  $ABFE$  is known (being  $= \frac{m}{m+n} \cdot ABCD$ ) as also  $ABE$ ;  $AB$ ,  $BE$ , and  $EA$  being given on the ground.  $BEF$  will then be known  $= ABFE - ABE$ .

FIG. 331.

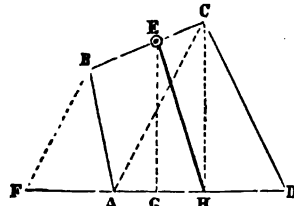


Then  $GF = \frac{BEF}{\frac{1}{2} BE}$ , and the point  $F$  is obtained by

running a parallel to  $BE$ , at a perpendicular distance from it  $= GF$ .

To divide a quadrilateral,  $ABCD$ , graphically, into *two equivalent* parts by a line from a point,  $E$ , on a side, proceed thus : Draw the diagonal  $CA$ , and from  $B$  draw a parallel to it, meeting  $DA$  prolonged in  $F$ . Mark the middle point,  $G$ , of  $FD$ . Join  $GE$ . From  $C$  draw a parallel to  $EG$ , meeting  $DA$  in  $H$ .  $EH$  is the required line. The quadrilateral could also be divided in any ratio  $= m : n$ , by dividing  $FD$  in that ratio.

FIG. 332.

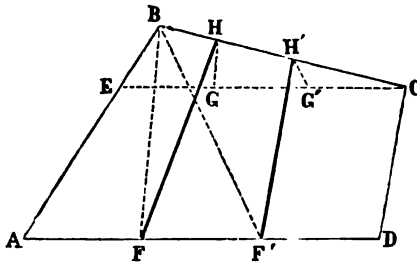


If the quadrilateral be given by bearings, proceed to part off the desired area, as in Art. 412 or 413.

**448.** Let it be required to divide a quadrilateral,  $ABCD$ , into *three equivalent* parts.

From any angle, as  $C$ , draw  $CE$ , parallel to  $DA$ . Divide  $AD$  and  $EC$ , each into three equal parts, at  $F, F'$ , and  $G, G'$ . Draw  $BF, BF'$ . From  $G$  draw  $GH$ , parallel to  $FB$ , and from  $G'$  draw  $G'H'$ , parallel to  $F'B$ .  $FH$  and

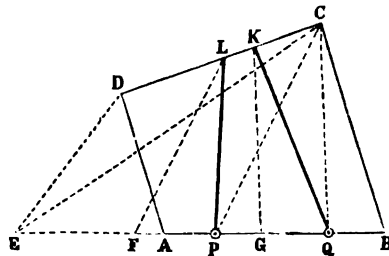
FIG. 333.



$F'H'$  are the required lines of division.

Let it be required to make the above division by *lines starting from two given points*,  $P$  and  $Q$ . Reduce the quadrilateral to an equivalent triangle  $CBE$ . Divide  $EB$  into three equal parts at  $F$  and  $G$ . Join  $CQ$ , and, from  $G$ , draw  $GK$  parallel

FIG. 334.

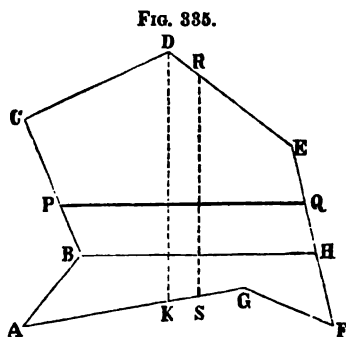


to it. Join  $CP$ , and from  $F$  draw  $FL$  parallel to it. Join  $PL$  and  $QK$ , and they will be the division-lines required.

**449. By Lines passing through a Point within the Figure.** Proceed to part off the desired area as in Art. 416 or 417, according to the circumstances of the case.

*Division of Polygons.*

**450. By Lines running in any Direction.** Let  $ABCDEFGH$



be a given polygon, and  $BH$  the direction parallel to which is to be drawn a line  $PQ$ , dividing the polygon into two parts in any desired ratio  $= m : n$ . The

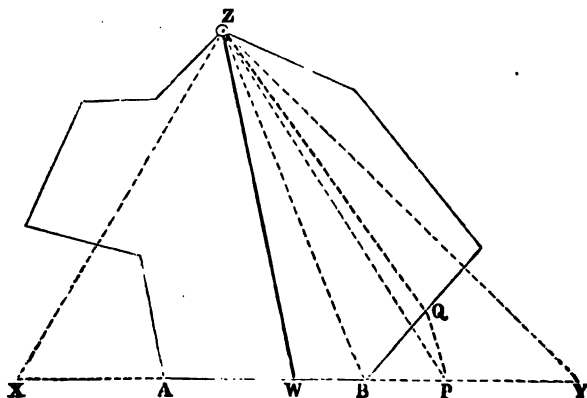
area  $PCDEQ = \frac{m}{m+n} \cdot ABC$

$DEFGH$ . Taking it from the area  $BCDEH$ , the remainder will be the area  $BPQH$ . The quadrilateral  $BCEH$ ,  $CE$  being

supposed to be drawn, can then be divided by the method of Art. 443 into two parts,  $BPQH$  and  $PQEC$ , having to each other a known relation.

If  $DK$  were the given direction, at right angles to the former, the position of a dividing line  $RS$  could be similarly obtained.

FIG. 336.



**451. By Lines starting from an Angle.** Produce one side, A B, of the given polygon, both ways, and reduce the polygon to a single equivalent triangle, X Y Z. Then divide the base, X Y, in the required ratio, as at W, and draw Z W, which will be the division-line desired. In this figure the polygon is divided into two equivalent parts.

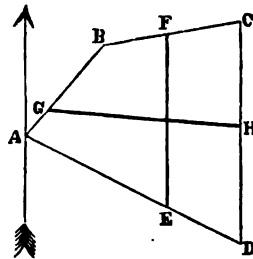
If the division-line should pass outside of the polygon, as does Z P, through P draw a parallel to B Z, meeting the adjacent side of the polygon in Q, and Z Q will be the division-line desired.

**452. By Lines starting from a Point on a Side.** See Articles 414 and 415.

**453. By Lines passing through a Point within the Figure.** Part off, as in Art. 416 or 418, if a straight line be required, or by guess-lines and the addition of triangles, as in Art. 433, if the lines have merely to start from the point, such as a spring or well.

**454. Other Problems.** The following is from Gummere's "Surveying": *Question.* A tract of land is bounded thus: N.  $35\frac{1}{4}^{\circ}$  E., 23·00; N.  $75\frac{1}{4}^{\circ}$  E., 30·50; S.  $3\frac{1}{4}^{\circ}$  E., 46·49; N.  $66\frac{1}{4}^{\circ}$  W., 49·64. It is to be divided into four equivalent parts by two straight lines, one of which is to run parallel to the third side; required the distance of the parallel division-line from the first corner, measured on the fourth side; also the bearing of the other division-line, and its distance from the same corner measured on the first side. *Ans.* Distance of the parallel division-line from the first corner, 32·50; the bearing of the other, S.  $88^{\circ} 22'$  E.; and its distance from the same corner 5·99.

FIG. 337.



The scale of the figure is 40 chains to 1 inch = 1 : 31680.

An indefinite number of problems on this subject might be proposed, but they would be matters of curiosity rather than of utility, and exercises in geometry and trigonometry rather than in surveying.

## CHAPTER VII.

### THE PUBLIC LANDS OF THE UNITED STATES.

**455. General System.** The public lands of the United States of America are generally divided and laid out into squares (approximately), the sides of which run truly north and south, or east and west.

This is effected by means of meridian lines and parallels of latitude, established six miles apart. The squares thus formed are called TOWNSHIPS. They contain 36 square miles, or 23,040 acres, "as nearly as may be." A *principal meridian*, running due north and south, and a *base-line*, running due east and west, are first established astronomically, and the half-mile, mile, and six-mile corners are permanently marked on them. These two lines form the basis of all the subsequent subdivision into townships and sections. All the townships, situated north or south of each other, form a RANGE. The ranges are named by their number east or west of the principal meridian. The

|   |    |    |    |    |       |
|---|----|----|----|----|-------|
| N |    |    |    |    |       |
|   | 6  | 5  | 4  | 3  | 2 1   |
|   | 7  | 8  | 9  | 10 | 11 12 |
| W | 18 | 17 | 16 | 15 | 14 13 |
|   | 19 | 20 | 21 | 22 | 23 24 |
|   | 30 | 29 | 28 | 27 | 26 25 |
|   | 31 | 32 | 33 | 34 | 35 36 |
| S |    |    |    |    |       |
| E |    |    |    |    |       |

The first range west of the meridian would be noted as Range 1 West (R. 1 W.), and the next R. 2 W., etc. The townships in each range are named by their number north or south of the base-line. They are noted as Township 1 North (T. 1 N.), and the next one T. 2 N., etc.

Each township is divided into 36 SECTIONS, each one mile square, and therefore containing, "as nearly as may be," 640 acres. The sections in each township are numbered, as in the margin, from 1 to 36, beginning at the northeast angle of the township, and going



west from 1 to 6, then east from 7 to 12, and so on alternately to section 36, which will be in the southeast angle of the township. The sections are subdivided into quarter-sections, half a mile square, and containing 160 acres, and sometimes into half-quarter-sections of 80 acres, and quarter-quarter-sections of 40 acres.

**456. Difficulty.** The law requiring that the lines of the public-land surveys shall be governed by the true meridian, and at the same time that the townships shall be six miles *square*, involves a mathematical impossibility; for strictly to conform to the meridian necessarily throws the township out of square, by reason of *the convergency of meridians*; hence, adhering to the true meridian renders it necessary to depart from the strict requirements of law as respects the precise area of townships, and the subdivisinal parts thereof, the township assuming something of a trapezoidal form, which inequality develops itself, more and more as such, the higher the latitude of the surveys.

\* In view of these facts, and under the provisions of section 2 of the act of May 18, 1796, that sections of a mile square shall contain 640 acres, *as nearly as may be*, and also under those of section 3 of the act of May 10, 1800, that "in all cases where the exterior lines of the townships, thus to be subdivided into sections and half-sections, shall exceed, or shall not extend six miles, the excess or deficiency shall be specially noted, and added to or deducted from the western or northern ranges of sections or half-sections in such township, according as the error may be in running lines from east to west, or from south to north; the sections and half-sections bounded on the northern and western lines of such townships shall be sold as containing only the quantity expressed in the returns and plats, respectively, and all others as containing the complete legal quantity," the public lands of the United States shall be surveyed under the methods of the system of rectangular surveying, which harmonizes the incompatibilities of the requirements of law and practice, as follows:

*First.* The establishment of a principal meridian conforming to the true meridian, and, at right angles to it, a base-line conforming to a parallel of latitude.

*Second.* The establishment of standard parallels conforming to parallels of latitude, initiated from the principal meridian at intervals of 24 miles and extended east and west of the same.

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\* These instructions (Articles 456 to 462) are taken from the "Manual of Surveying Instructions for the Survey of the Public Lands of the United States," prepared by the Commissioner of the General Land-Office.

*Third.* The establishment of guide meridians conforming to true meridians, initiated upon the base-line and successive standard parallels at intervals of 24 miles, resulting in tracts of land 24 miles square, *as nearly as may be*, which shall be subsequently divided into tracts of land six miles square by two sets of lines, one conforming to true meridians, crossed by others conforming to parallels of latitude at intervals of six miles, containing 28,040 acres, *as nearly as may be*, and designated *townships*.

Such townships shall be subdivided into thirty-six tracts, called sections, each of which shall contain 640 acres, *as nearly as may be*, by two sets of parallel lines, one set *parallel to a true meridian* and the other *conforming to parallels of latitude*, mutually intersecting at intervals of one mile and at right angles, *as nearly as may be*.

Any series of contiguous townships situated north and south of each other constitutes a *range*, while such a series situated in an east-and-west direction constitutes a *tier*.

The section-lines are surveyed from *south* to north and from *east* to west, in order to throw the excess or deficiency in measurement on the north and west sides of the township, as required by law. In case where a township has been partially surveyed, and it is necessary to complete the survey of the same, or where the character of the land is such that only the north or west portions of the township can be surveyed, this rule can not be strictly adhered to, but, in such cases, it will be departed from only so far as is absolutely necessary. It will also be necessary to depart from this rule where surveys close upon State or Territorial boundaries, or upon surveys extending from different meridians.

The tiers of townships will be numbered, to the north or south, commencing with No. 1, at the base-line; and the ranges of the townships, to the east or west, beginning with No. 1, at the principal meridian of the system.

The thirty-six sections into which a township is subdivided are numbered, commencing with No. 1 at the *northeast* angle of the township, and proceeding west to No. 6, and thence proceeding east to No. 12, and so on, alternately, to No. 36 in the southeast angle. In all cases of surveys of fractional townships, the sections will bear the same numbers they would have if the township was full.

Standard parallels shall be established at intervals of every 24 miles, north and south of the base-line, and guide-meridians at intervals of every 24 miles, east and west of the principal meridian; thus confining the errors resulting from convergence of meridians and inaccuracies in measurement within comparatively small areas.

**457. Making the Survey.** All work on the public-land surveys is done, and records made, in strict conformity with the instructions issued from time to time from the General Land-Office. Considerable changes have been made in the methods employed, so that in making a resurvey of any land originally surveyed by the Government it is necessary to know under what instructions the original survey was made, and, where practicable, to obtain a copy of the notes of the original survey.

**INITIAL POINTS.** Initial points from which the lines of the public surveys are to be extended will be established whenever necessary, under such special instructions as may be prescribed in each case by the Commissioner of the General Land-Office. The locus of such initial points will be selected with great care and due consideration for their prominence and easy identification, and must be established astronomically.

The lines of the public surveys are classified as follows:

Class 1. Base-lines and standard parallels.

Class 2. Principal and guide meridians.

Class 3. Township exteriors (or meridional and latitudinal township boundaries).

Class 4. Subdivision and meander lines.

The initial point having been established, the line of the public surveys will be extended therefrom, as follows:

**BASE-LINE.** 1. From the initial point the base-line will be extended east and west on a parallel of latitude, by the use of transit or solar instruments, as may be directed by the surveyor-general in his written special instructions. The *transit* should be designated for the alignment of all important lines.

2. The direction of base-lines will conform to parallels of latitude and will be controlled by true meridians; consequently the correct determination of true meridians by *observations on Polaris at elongation*\* is a matter of prime importance.

3. When transits are employed, certain reference-lines† having a known position and relation to the required parallel of latitude will be prolonged as straight lines, by two back and two fore sights at each setting of the instrument, the horizontal limb being revolved 180° in azimuth between the observations.

4. Where solar apparatus is used, the deputy will test the instrument, whenever practicable, by comparing its indications with a meridian determined by Polaris observations; and in all cases where error is discovered he will make the necessary corrections of his line before proceeding with the survey. All operations will be fully described in the field-notes.

5. The proper township, section, and quarter-section corners will be established at lawful intervals, and meander corners at the intersection of the line with all meanderable streams, lakes, or bayous.

6. In order to detect errors and insure accuracy in measurement, two sets of chainmen will be employed: one to note distances to intermediate points and to locate topographical features, the other to act as a check. Each will measure forty chains, and the proper corner will be placed midway between the ending-points of the two measurements.

The deputy will be present when said corner is thus established, and will record in the body of his field-notes the distances to the same, according to the measurement by each set of chainmen.

To obviate collusion between the sets of chainmen, the second set should

\* See page 171.

† For details see pages 334 to 342.

commence at a point in advance of the beginning corner of the first set, the initial difference in measurement thus obtained being known only to the deputy.

**PRINCIPAL MERIDIAN.** 1. This line shall conform to a true meridian and will be extended from the initial point, either north or south, or in both directions, as the conditions may require, by the use of transit or solar instruments, as may be directed by the surveyor-general in his special written instructions.

2. The methods used for determination of directions, and the precautions to be observed to secure accuracy in measurement, are fully stated above under the title "Base-Line," and will be complied with in every particular.

**STANDARD PARALLELS.** 1. Standard parallels, which are also called correction-lines, shall be extended east and west from the principal meridian, at intervals of every 24 miles north and south of the base-line, in the manner prescribed for running said line, and all requirements under the title "Base-Line" will be carefully observed.

2. Where standard parallels have been placed at intervals of 30 or 36 miles, regardless of existing instructions, and where gross irregularities require additional standard lines, from which to initiate new or upon which to close old surveys, an intermediate correction-line should be established to which a local name may be given—e. g., "Cedar Creek Correction-Line"—and the same will be run, in all respects, like the regular standard parallels.

**GUIDE-MERIDIANS.** 1. Guide-meridians shall be extended north from the base-line, or standard parallels, at intervals of every 24 miles east and west from the principal meridian, in the manner prescribed for running the principal meridian, and all the provisions for securing accuracy of alignment and measurement found, or referred to under the title "Principal Meridian," will apply to the survey of said guide-meridians.

2. When existing conditions require that such guide-meridians shall be run south from the base- or correction-lines, they will be initiated at properly established closing corners on such lines.

3. Where guide-meridians have been improperly placed at intervals greatly exceeding the authorized distance of 24 miles, and standard lines are required to limit errors of old or govern new surveys, a new guide-meridian may be run from a standard or properly established closing corner, and a local name may be assigned to the same—e. g., "Grass Valley Guide-Meridian." These additional guide-meridians will be surveyed in all respects like the regular guide-meridians.

**TOWNSHIP EXTERIORS.** 1. Whenever practicable, the township exteriors in a tract of land 24 miles square, bounded by standard lines, will be surveyed successively through the block, beginning with those of the south-western township.

2. The meridional boundaries of townships will have precedence in the order of survey and will be run from south to north on true meridians, with permanent corners at lawful distances; the latitudinal boundaries will be run from east to west on random or trial-lines, and corrected back on true lines.

The falling of a *random*, north or south of the township corner to be closed upon, will be carefully measured, and, with the resulting true return course, will be duly recorded in the field-notes.

Should it happen, however, that such *random* intersects the meridian of the objective corner, north or south of said corner, or falls short of or overruns the length of the south boundary of the township by more than *three chains* (due allowance being made for convergency), said *random*, and, if necessary, all the exterior boundaries of the township, will be retraced and remeasured to discover and correct the error.

When running *random* lines from east to west, temporary corners will be set at intervals of 40·00 chains, and proper *permanent* corners will be established upon the true line, corrected back in accordance with these instructions, thereby throwing the excess or deficiency against the west boundary of the township, as required by law.

3. Whenever practicable, the exterior boundaries of townships belonging to the *west* range, in a tract or block 24 miles square, will first be surveyed in succession, through the range, from south to north; and in a similar manner the other three ranges will be surveyed in regular sequence.

4. In cases where *impassable objects occur* and the foregoing rules can not be complied with, township corners will be established as follows:

In extending the *south* or *north* boundaries of a township to the *west*, where the *southwest* or *northwest* corners can not be established in the regular way by running a north and south line, such boundaries will be run *west on a true line*, allowing for convergency on the west half-mile; and from the township corner established at the end of such boundary the west boundary will be run *north* or *south*, as the case may be. In extending *south* or *north* boundaries of a township to the *east*, where the *southeast* or *northeast* corner can not be established in the regular way, the same rule will be observed, except that such boundaries will be run *east on a true line*, and the *east* boundary run *north* or *south*, as the case may be.

5. Allowance for the convergency of meridians will be made whenever necessary.

METHOD OF SUBDIVIDING. 1. The exterior boundaries of a full township having been properly established, the subdivision thereof will be made as follows:

At or near the *southeast* corner of the township a *true meridian* will be determined by Polaris or solar observations, and the deputy's instrument will be tested thereon; then from said corner the first mile of the east and south boundaries will be retraced, if subdivisions and survey of the exteriors have been provided for in *separate* contracts; but, if the survey of the exterior and subdivisional lines are included in the *same* contract, the retracements referred to will be omitted. All discrepancies resulting from disagreement of bearings or measurements will be carefully stated in the field-notes.

2. After testing his instrument on the true meridian thus determined, the deputy will commence at the corner to sections 35 and 36, on the south

boundary, and run a line *parallel to the range-line*,\* establishing at 40·00 chains, the quarter-section corner between sections 35 and 36, and at 80·00 chains the corner for sections 25, 26, 35, and 36.

3. From the last-named corner a random line will be run eastward, without blazing, *parallel to the south boundary of section 36*, to its intersection with the east boundary of the township, placing at 40·00 chains from the point of beginning, a post for temporary quarter-section corner. If the random line intersects said township boundary exactly at the corner for sections 25 and 36, it will be blazed back and established as the true line, the permanent quarter-section corner being established thereon, *midway* between the initial- and terminal-section corners.

If, however, the random intersects said township boundary to the north or south of said corner, the falling† will be carefully measured, and from the data thus obtained the true return course will be calculated‡ and the

\* The meridional section-lines will be made parallel to the range-line or east boundary of the township, by applying to the bearing of the latter a small correction, dependent on the latitude, taken from the following table, which gives, to the nearest whole minute, the *convergency* of two meridians 6 miles long and from 1 to 5 miles apart; and supplies directly the deviation of meridional section-lines *west of north*, when the range-line is a *true meridian*. Add the correction to the bearing of the range-line, if the same is *west of north*, but subtract when it bears *east of north*.

TABLE A.—*Corrections for Convergency, within a Township.*

| LATITUDE.       | CORRECTION TO BE APPLIED TO BEARING OF RANGE-LINES<br>AT A DISTANCE OF— |          |          |          |          |
|-----------------|-------------------------------------------------------------------------|----------|----------|----------|----------|
|                 | 1 mile.                                                                 | 2 miles. | 3 miles. | 4 miles. | 5 miles. |
| 30° to 35°..... | 1'                                                                      | 1'       | 2'       | 2'       | 3'       |
| 35° to 40°..... | 1'                                                                      | 1'       | 2'       | 3'       | 3'       |
| 40° to 45°..... | 1'                                                                      | 2'       | 2'       | 3'       | 4'       |
| 45° to 50°..... | 1'                                                                      | 2'       | 3'       | 4'       | 5'       |

*Example.* Latitude 47°. Range-line bears N. 0° 2' E.; then *parallel* meridional section-lines will be run as follows:

From the corner for sections—

35 and 36, N. 0° 1' E.

32 and 33, N. 0° 2' W.

34 and 35, north.

31 and 32, N. 0° 3' W.

33 and 34, N. 0° 1' W.

† See "Prescribed Limits," page 312.

‡ *Random* bearings, determined as directed above, are actually\* the *true* bearings of fractional true lines and are so used for running them. Any deviation from random bearings, derived from the application of the falling, changes the random bearing by an amount due to unavoidable errors, and should give for a final result a bearing *as near the true bearing* as the field-work will permit. A *true* bearing means the angular deviation from the *true meridian* in contradistinction to the *magnetic* bearing, or angle made with the *magnetic meridian*. A true line will be understood to refer to the line upon which the corners are established.

true line blazed and established and the position of the quarter-section corner determined, as directed above.

The details of the entire operation will be recorded in the field-notes.

4. Having thus established the line between sections 25 and 36; from the corner for sections 25, 26, 35, and 36, the *west* and *north* boundaries of sections 25, 24, 13, and 12, will be established as directed for those of section 36; with the exception that the random lines of said north boundaries will be run *parallel to the established south boundaries of the sections to which they belong*, instead of the south boundary of section 36—e. g., the random line between sections 24 and 25 will be run parallel to the established south boundary of section 25, etc.

5. Then, from the last-established section corner—i. e., the corner for sections 1, 2, 11, and 12—the line between sections 1 and 2 will be projected northward, on a random line, *parallel* to the east boundary of the township, setting a post for temporary quarter-section corner at 40·00 chains, to its intersection with the north boundary of the township. If the random intersects said north boundary exactly at the corner for sections 1 and 2, it will be blazed back and established as the true line, the temporary quarter-section corner being established permanently in its original position, and the fractional measurement thrown into that portion of the line between said corner and the north boundary of the township.

If, however, said random intersects the north boundary of the township, to the east or west of the corner for sections 1 and 2, the consequent falling will be carefully measured, and from the data thus obtained the true return course will be calculated and the true line established, the permanent quarter-section corner being placed upon the same at 40·00 chains from the initial corner of the random line, thereby throwing the fractional measurement in that portion lying between the quarter-section corner and the north boundary of the township.

When the north boundary of a township is a base-line or standard parallel, the line between sections 1 and 2 will be run *parallel to the range-line* as a *true line*, the quarter-section corner will be placed at 40·00 chains, and a *closing corner* will be established at the point of intersection with such base or standard line; and in such case the distance from said closing corner to the nearest standard corner on such base or standard line will be carefully measured and noted as a *connection line*.

6. Each successive range of sections progressing to the west, until the fifth range is attained, will be surveyed in a similar manner; then, from the section corners established on the west boundary of said range of sections, random lines will be projected to their intersection with the west boundary of the township, and the true return lines established as prescribed for the survey of the first or most eastern range of sections, with the exception that on the true lines thus established the quarter-section corners will be established at 40·00 chains from the initial corners of the randoms, the fractional measurements being thereby thrown into those portions of the lines situated between said quarter-section corners and the west boundary of the township.

7. The following general requirements are reiterated for emphasis:

The *random* of a latitudinal section-line will always be run *parallel to the south boundary of the section to which it belongs, and with the true bearing of said boundary*; and when a section has no linear south boundary, the *random* will be run *parallel to the south boundary of the range of sections in which it is situated, and fractional true lines will be run in a similar manner*.

8. The deputy is not required to complete the survey of the first range of sections from south to north before commencing the survey of the second or any subsequent range of sections, but the corner on which any random line closes shall have been previously established by running the line which determines its position, except as follows: Where it is impracticable to establish such section corner in the regular manner, it will be established by running the latitudinal section-line as a *true line*, with a *true bearing*, determined as above directed for *random* lines, setting the quarter-section corner at 40·00 chains and the section corner at 80·00 chains.

9. Quarter-section corners, both upon meridional and latitudinal section-lines, will be established at points *equidistant* from the corresponding section corners, *except* upon the lines closing on the north and west boundaries of the township, and in those situations the quarter-section corners will always be established at precisely *forty chains* to the north or west (as the case may be) of the respective section corners from which those lines respectively *start*, by which procedure the excess or deficiency in the measurements will be thrown, according to law, on the extreme tier or range of quarter-sections, as the case may be.

10. Where by reason of impassable objects only a portion of the south boundary of a township can be established, an auxiliary base-line (or lines, as the case may require) will be run through the portion which has no linear south boundary, first *random*, then corrected, connecting properly-established corresponding section corners (either interior or exterior) and as far south as possible, and from such line or lines the section-lines will be extended northwardly in the usual manner, and any fraction *south* of said line will be surveyed in the opposite direction from the section corners on the auxiliary base thus established.

11. Where by reason of impassable objects *no portion of the south boundary* of a township can be regularly established, the subdivision thereof will proceed from *north to south* and from east to west, thereby throwing all fractional measurements and areas against the west boundary, and the meanderable stream or other boundary limiting the township on the south.

If the *east* boundary is without regular section corners and the north boundary has been run eastwardly as a true line, with section corners at regular intervals of 80·00 chains, the subdivision of the township will be made from *west to east*, and fractional measurements and areas will be thrown against the irregular east boundary.

12. When the proper point for the establishment of a township or section corner is inaccessible, and a witness corner can be erected upon each of the two lines which approach the same, at distances not exceeding twenty chains therefrom, said witness corners will be properly established,



and the half-miles upon which they stand will be recognized as *surveyed lines*.

The witness corner will be marked as conspicuously as a section corner, and bearing-trees will be used wherever possible.

MEANDERING. 1. Proceeding *down* stream, the bank on the *left* hand is termed the *left bank* and that on the *right* hand the *right bank*. These terms will be universally used to distinguish the two banks of a river or stream.

2. Navigable rivers, as well as all rivers not embraced in the class denominated "navigable," the right-angle width of which is three chains and upward, will be meandered on both banks, at the ordinary *mean high-water mark*, by taking the general courses and distances of their sinuosities, and the same will be entered in the field-book. Rivers not classed as navigable will not be meandered above the point where the average right-angle width is less than three chains. Shallow streams, without any well-defined channel or permanent banks, *will not be meandered*; except tide-water streams, whether more or less than three chains wide, which should be meandered at ordinary high-water mark, as far as tide-water extends.

At every point where either standard, township, or section lines intersect the bank of a navigable stream, or any meanderable line, corners will be established at the time of running these lines. Such corners are called meander corners,\* and the deputy will commence at one of these corners, follow the bank or boundary-line, and measure the length of each course from the beginning corner to the next "meander corner." Compass courses, by the needle or solar, will be used in meanders. Transit angles are not allowed.

The crossing distance between meander corners on same line and the true bearing and distance between corresponding meander corners will be ascertained by triangulation, or direct measurement, in order that the river may be protracted with entire accuracy. The particulars will be given in the field-notes.

In meandering water-courses or lakes, where a distance is more than *ten chains* between successive stations, whole chains only should be taken; but if the distance is *less* than ten chains, and it is found convenient to employ chains and links, the number of links should be a *multiple of ten*, thereby saving time and labor in testing the closings, both in the field and office.

3. The meanders of all lakes, navigable bayous, and deep ponds, of the area of twenty-five acres and upward, will be commenced at a meander corner and continued, as above directed for navigable streams; from said corner the courses and distances of the entire margin of the same, and the intersections with all meander corners established thereon, will be noted.

All streams falling into the river, lake, or bayou will be noted, and the width at their mouths stated; also the position, size, and depth of springs, whether the water be pure or mineral; also the heads and mouths of all bayous; all islands, rapids, and bars will be noted, with intersections, to their upper and lower ends, to establish their exact situation. The eleva-

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\* These corners are the *regular* meander corners, and designated "meander corners"; they are distinguished from *special* and *auxiliary* meander corners.

tion of the banks of lakes, bayous, and streams, the height of falls and cascades, and the length and fall of rapids will be recorded in the field-notes.

To meander a lake or deep pond lying entirely within the boundaries of a section, two lines will be run from the two nearest corners on different sides of such lake or pond, the courses and length of which will be recorded, and if coincident with unsurveyed lines of legal subdivisions, that fact will also be stated in the field-notes, and at each of the points where said lines intersect the margin of the pond or lake a *special*\* meander corner will be established as above directed.

The relative position of these points being thus definitely fixed in the section, the meandering will commence at one of them and be continued to the other, noting the intersection, and thence to the beginning. The proceedings are to be fully entered in the field-notes.

4. Meander lines will not be established at the segregation line between dry and swamp or overflowed land, but at the *ordinary high-water mark* of the actual margin of the rivers or lakes on which such swamp or overflowed lands border.

5. The precise relative position of an island in a township made fractional by a river or lake in which the island is situated will be determined by triangulation from a special and carefully measured base-line, initiated upon the surveyed lines, on or near the lake or river-bank on the mainland, so as to connect by course and distance on a direct line the meander corner on the mainland with the corresponding point on the island, where the proper meander corner will be established.

6. In making the connection of an island lying entirely within a section with the mainland a special base will be measured from the most convenient meander corner, and from such base the location of an *auxiliary*† meander corner will be determined by triangulation, at which the meanders of the island will be initiated.

7. In the survey of lands bordering on *tide-water* "meander corners" will be established at the points where surveyed lines intersect *high-water mark*, and the meanders will follow the *high-water line*.

8. The field-notes of meanders will show the dates on which the work was performed. The field-notes of meanders will state and describe the corner from which the meanders commenced and upon which they closed, and will exhibit the meanders of each fractional section separately; following, and composing a part of such notes, will be given a description of the land, timber, depth of inundation to which the bottom is subject, and the banks, current, and bottom of the stream or body of water meandered. The utmost care will be taken to pass no object of topography, or *change therein*, without giving a particular description thereof in its proper place in the notes of the meanders.

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\* A "*Special Meander Corner*" is one established on a line of legal subdivision, not a standard, township, or section line.

† An "*auxiliary meander corner*" is one not on a line belonging to the system of rectangular surveying.

**458. Summary of Objects and Data required to be noted.** 1. The precise length of every line run, noting all necessary offsets therefrom, with the reason for making them, and method employed.

2. The kind and diameter of all bearing-trees, with the course and distance of the same from their respective corners; and the precise relative position of witness corners to the true corners.

3. The kind of materials of which corners are constructed.

4. *Trees on line.* The name, diameter, and distance on line to all trees which it intersects.

5. Intersections by line of *land objects.* The distance at which the line intersects the *boundary-lines* of every reservation, settler's claim, improvement, or rancho; prairie, bottom land, swamp, marsh, grove, and windfall, with the course of the same at all points of intersection; also the distances at which the line begins to ascend, arrives at the top, begins to descend, and reaches the foot of all *remarkable* hills and ridges, with their courses, and *estimated height in feet*, above the level land of the surrounding country, or above the bottom lands, ravines, or waters near which they are situated. Also distance to and across *large* ravines, their depth and course.

6. Intersections by line of *water objects.* All rivers, creeks, and smaller streams of water which the line crosses; the distances measured on the *true* line to the bank *first arrived at*, the course *down stream* at *points of intersection*, and their *widths on line*. In cases of *navigable* streams their width will be ascertained between the *meander corners*, as set forth under the proper head.

7. The land's *surface*—whether level, rolling, broken, hilly, or mountainous.

8. The *soil*—whether first, second, third, or fourth rate.

9. *Timber*—the several kinds of timber and undergrowth, in the order in which they predominate.

10. *Springs of water*—whether fresh, saline, or mineral, with the course of the streams flowing from them.

11. *Lakes and ponds*—describing their banks and giving their height, and also depth of water, and whether it be pure or stagnant.

12. *Improvements.* Towns and villages; houses or cabins, fields, or other improvements with owners' names; mill-sites, forges, and factories, mineral monuments, and all corners not belonging to the system of rectangular surveying; will be located by bearing and distance, or by intersecting bearings from given points.

13. *Coal* banks or beds; *peat* or turf grounds; *minerals* and ores; with particular description of the same as to quality and extent, and all *diggings* therefor; also *salt* springs and licks. All reliable information that can be obtained respecting these objects, whether they be on the line or not, will appear in the general description.

14. *Roads and trails*, with their directions, whence and whither.

15. Rapids, cataracts, cascades, or falls of water, with the estimated height of their fall in feet.

16. Precipices, caves, sink-holes, ravines, stone-quarries, ledges of rocks, with the kind of stone they afford.

17. *Natural curiosities*, interesting fossils, petrifications, organic remains, etc.; also all ancient works of art, such as mounds, fortifications, embankments, ditches, or objects of like nature.

18. The *magnetic declination* will be *incidentally* noted at all points of the lines being surveyed, where any *material change* in the same indicates the probable presence of iron-ores; and the position of such points will be perfectly identified in the field-notes.

**459. Prescribed Limits for Closings and Lengths of Lines.** 1. If in running a *random* township exterior such random falls short of or exceeds its proper length by more than *three chains*, or falls more than *three chains* north or south of its objective corner, it will be re-run, and, if found correct, so much of the remaining boundaries of the township will be retraced or resurveyed as may be found *necessary* to locate the error.

2. Every meridional section-line, except those terminating in the north boundary of the township, shall be *eighty chains* in length.

3. The *random* meridional section-lines through the north tier of sections shall fall within *fifty links* east or west of the section corners established on the north boundary of the township, *except* when closing on a base-line or standard parallel.

4. The actual length of meridional section-lines through the north tier of sections shall be within *one hundred and fifty links* of their theoretical length. The latter will be determined from the meridional boundaries of the north tier of sections.

5. All *random* latitudinal section-lines shall fall within *fifty links* north or south of their objective section corners.

In any range of sections the difference between the true bearing of a latitudinal section-line and that of the south boundary of the range shall not exceed twenty-one minutes of arc.

The *latitudinal* section-lines, except those terminating in the west boundary of the township, shall be within *fifty links* of the actual distance established on the south boundary-line of the township for the width of the range of sections to which they belong.

6. The north boundary and the south boundary of *any one section*, except in the extreme western range of sections, shall be within *fifty links* of equal length.

7. The meanders within each fractional section, or between any two successive meander corners, or of an island in the interior of a section, should close within a limit to be determined by allowing *five eighths of a link* for *each chain* of said meander line. Where the meander corners marking the ends of a meander line in a fractional section are located on standard, township, or section lines, the above limit, increased by *one fourth of the regular perimeter of the fractional section, expressed in miles, multiplied by seventy-one links*, will be allowed.

The extreme limit, however, will in no case be permitted to exceed *one hundred and fifty links*.

**460. Marking-Lines.** All lines on which are to be established the legal corner boundaries are to be marked after this method, viz.: Those trees which may intercept your line must have two chops or notches cut on each side of them, without any other marks whatever. These are called "*sight-trees*," or "*line-trees*."

A sufficient number of other trees standing nearest to your line, on either side of it, are to be *blazed* on two sides, diagonally or quartering toward the line, in order to render the line conspicuous and readily to be traced, the blazes to be opposite each other, coinciding in direction with the line where the trees stand very near it, and to approach nearer each other, the farther the line passes from the blazed trees. Due care must ever be taken to have the lines so well marked as to be readily followed.

**461. Marking-Corners.** After a true coursing, and most exact measurements, the corner boundary is the consummation of the work, for which all the previous pains and expenditure have been incurred. A boundary corner, in a timbered country, is to be a *tree*, if one be found at the precise spot; and if not, a stone or wooden *post* is to be planted thereat; and the position of the corner post is to be indicated by trees adjacent (called bearing-trees), the angular bearings and distances of which from the corner are facts to be ascertained and registered in your field-book.

Stone should be used for corners in all cases where practicable.

In a region where stone abounds, the corner boundary will be a small *monument of stones* alongside of a single marked stone, for a township corner—and a *single stone* for all other corners.

In a region where timber is not near, nor stone, the corner will be a *mound of earth*, of prescribed size, varying to suit the case.

Corners are to be fixed, for township boundaries, at intervals of every six miles; for section boundaries, at intervals of every mile, or 80 chains; and, for quarter-section boundaries, at intervals of every half-mile, or 40 chains.

**MEANDER CORNER POSTS** are to be planted at all those points where the township or section lines intersect the banks of such rivers, lakes, or islands as are by law directed to be meandered.

When stones are used for corners they should contain at least 504 cubic inches, and be inserted in the ground 7 or 8 inches, with their edges in the direction of the line.

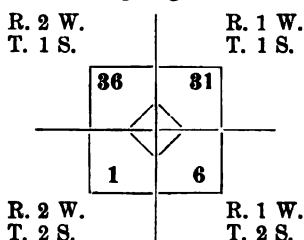
When wooden *posts* are used their length and size must be proportioned to the importance of the corner, whether township, section, or quarter-section, the first being at least twenty-four inches above ground, and four inches square.

Where a township post is a corner common to *four* townships, it is to be set in the earth *diagonally*, thus : W  E. On each surface of the post is to be marked the number of the particular township, and its range, which

it *faces*. Thus, if the post be a common boundary to four townships, say *one* and *two*, south of the base-line, of range *one*, west of the meridian; also to townships *one* and *two*, south of the base-line, of range *two*, west of the meridian—it is to be marked thus:

|               |                               |
|---------------|-------------------------------|
| From N. to E. | { R. 1 W.<br>T. 1 S.<br>S. 31 |
| From N. to W. | { 2 W.<br>1 S.<br>36          |
| From E. to S. | { 1 W.<br>2 S.<br>6           |
| From W. to S. | { 2 W.<br>2 S.<br>1           |

The position of the post, which is here taken as an example, is shown in the following diagram:



These marks are to be distinctly and neatly chiseled into the wood, at least the eighth of an inch deep; and to be also marked with *red chalk*. The *number* of the *sections* which they respectively *face* will also be marked on the township post.

*Section* or *mile* posts, being corners of sections, when they are common to *four* sections, are to be set *diagonally* in the earth (in the manner provided for township corner posts); and on each side of the squared surfaces is to be marked the appropriate *number* of the particular one of the *four sections*, respectively, which such side *faces*; also on one side thereof are to be marked the numbers of its *township* and *range*; and, to make such marks yet more conspicuous (in manner aforesaid), a streak of red chalk is to be applied.

In the case of an *isolated* township, subdivided into thirty-six sections, there are twenty-five interior sections, the southwest corner boundary of each of which will be *common* to *four* sections. On all the extreme sides of an isolated township the outer tiers of sections have corners *common* only to *two* sections then surveyed. The posts, however, must be planted precisely like the former, but presenting two *vacant* surfaces to receive the appropriate marks when the adjacent survey may be made.

A quarter-section or half-mile post is to have no other mark on it than  $\frac{1}{4}$  S., to indicate what it stands for.

Township corner stones or posts are to be NOTCHED with *six* notches on each of the four angles set to the cardinal points.

All mile-posts on *township lines* must have as many notches on them, on two opposite *angles* thereof, as they are miles distant from the township corners, respectively. Each of the posts at the corners of sections in the *interior* of a township must indicate, by a number of notches on each of its four corners directed to the cardinal points, the corresponding number of miles that it stands from the *outlines* of the township. The four sides of the post will indicate the number of the section they respectively *face*. Should a

tree be found at the place of any corner, it will be marked and notched as aforesaid, and answer for the corner in lieu of a post, the kind of tree and its diameter being given in the field-notes.

The position of all corner posts, or corner trees of whatever description, which may be established, is to be perpetuated in the following manner, viz.: From such post or tree the courses shall be taken, and the distances measured, to two or more adjacent trees, in opposite directions, as nearly as may be, which are called "*bearing-trees*," and are to be blazed near the ground, with a large blaze facing the post, and having one notch in it, neatly and plainly made with an axe, square across, and a little below the middle of the blaze. The kind of tree and the diameter of each are facts to be distinctly set forth in the field-book.

On each bearing-tree the letters B. T. must be distinctly cut into the wood, in the blaze, a little above the notch, or on the bark, with the number of the range, township, and section.

At all township corners, and at all section corners, on range or township lines, *four* bearing-trees are to be marked in this manner, one in each of the adjoining sections.

At interior section corners *four* trees, one to stand within each of the four sections to which such corner is common, are to be marked in the manner aforesaid, if such be found.

From quarter-section and meander corners two bearing-trees are to be marked, one within each of the adjoining sections.

Where no bearing-tree is at the corner, and suitable stones are not available, a conical mound of earth is to be placed around the corner post. Township mounds are to be two and a half feet high and five feet in diameter at the base. Other mounds are to be two feet high and four and a half feet in diameter at the base. The posts in the mounds shall be one foot in the earth below the mound, and extend one foot above the mound. At the foot of the post is to be deposited, as a witness for the future, some charcoal, or a glass bottle, or a marked stone, or a charred stake placed on the side of the post toward which the line is run.

DOUBLE CORNERS are to be found nowhere except on the standard parallels or correction-lines, whereon are to appear both the corners which mark the intersection of the lines which close thereon, and those from which the surveys start in the opposite direction.

The corners which are established on the standard parallel, at the time of running it, are to be known as "*Standard Corners*," and, in addition to all the *ordinary* marks (as herein prescribed), they will be marked with the letters S. C. The "*closing corners*" will be marked C. C.

**462. Field-Notes.** 1. The proper blank-books for *original field-notes* will be furnished by the surveyor-general, and in such books the deputy-surveyor will make a faithful, distinct, and minute record of everything done and observed by himself and his assistants, pursuant to instructions, in relation to running, measuring, and marking lines, establishing corners, etc., and present, as far as possible, full and complete topographical sketches of

all standard and exterior lines, drawn to the usual scale for township exteriors. These "original field-notes" are not necessarily the entries made in the field, in the deputy's pocket note-books called tablets; but they are to be fully and correctly written out in ink, from such tablets, for the permanent record of the work. Tablets should be so fully written as to verify the "original field-notes" whenever the surveyor-general requires them for inspection.

2. A full description of all corners belonging to *old* surveys, from which the lines of *new* surveys start, or upon which they close, will in all cases be furnished the deputy from the surveyor-general's office, when authority is given for commencing work; then, if the old corners are found to agree with said descriptions, the deputy will describe any one of them in this form, "Which is a stone firmly set, marked, and witnessed, as described by the surveyor-general"; but, should a corner *not* answer the description supplied, the deputy will give a *full description* of such corner and its accessories, following the proper approved form given in these instructions.

A full description of each corner established under any one contract will be given *once* only; subsequent reference to such corner will be made in the form, "heretofore described," or (e. g.) "the corner for sections 2, 8, 10, and 11," as the case may require.

In all cases where a corner is *re-established* the *original field-notes* will describe fully the manner in which it is done.

3. The *original field-notes* of the survey of base, standard, and meridian lines will describe all corners established thereon, how established, the crossings of streams, ravines, hills, and mountains; character of soil, timber, minerals, etc.; and after the description of each township corner established in running such lines, the deputy will note particularly in the "general description" the character of townships on each side of the lines run.

4. The *original field-notes* of the survey of exterior boundaries of townships will describe the corners and topography, as above required, and the "general description" at the end of such notes will describe the townships as fully as possible, and also state whether or not they should be subdivided.

5. The *original field-notes* of the subdivisional survey of townships will describe the corners and topography as above required, and the "general description" at the end of such notes will state minutely the character of the land, soil, timber, etc., found in such townships.

The topography will be given on the *true line* in all cases, and will be taken correctly, not estimated or approximated.

6. With the *original field-notes* of the survey of base-lines and standard parallels, and principal and guide meridians forming a tract twenty-four miles square, including those of the township exteriors therein, the deputy will submit a diagram of the lines surveyed, drawn to a scale of half an inch to one mile, upon which will be written the *true bearings and lengths of all surveyed lines*, except the lengths of those which are actually 40·00 or 80·00 chains. These diagrams will exhibit all water-courses, with the direction of each indicated by an arrow-head pointing *down stream*; also the intersection of the lines with all prairies, marshes, swamps, ravines, lakes, ponds,



mountains, hills, and all other natural or artificial topographical features mentioned in the *original field-notes*, to the fullest extent possible.

7. With the *special instructions* for making subdivisional surveys of townships into sections, the deputy will be furnished by the surveyor-general with *blank township diagrams* drawn to a scale of *one inch to forty chains*, upon which the *true bearings and lengths of the township and section lines, from which the surveys are to be projected, or upon which they are to close, will be carefully marked.*

8. Triangulations, offsets, or traverses, made to determine distances that can not be directly measured, such as those over (e. g.) deep streams, lakes, impassable swamps, cañons, etc., will be made on the *random lines*, when random lines are run. All particulars will be fully stated in the field-notes.

The exhibition of every mile of surveying, whether on standard, township, or subdivision lines, and the meanders in each section, will be complete in itself, and will be separated from other records by a black line drawn across that part of the page containing the body of notes. The description of the surface, soil, minerals, timber, undergrowth, etc., on *each mile of line* will follow the notes of survey of such line, and *not be mingled with them.*

Particular care will be taken to record at the end of each mile the number of chains of *mountainous land, heavily timbered land, or land covered with dense undergrowth.*

The date of each day's work will immediately follow the notes thereof.

9. Near the end of the *original field-notes* and immediately before the "general description," the deputy-surveyor will add a tabular statement of the latitude and departure of all boundary-lines of the township.

Besides the ordinary notes taken on line (and which will always be written down on the spot, leaving nothing to be supplied by memory), the deputy will subjoin, at the conclusion of his book, such further description or information touching any matter or thing connected with the township (or other) survey which he may be able to afford, and may deem useful or necessary to be known—with a *general description* of the township in the *aggregate*, as respects the face of the country, its soil and geological features, timber, minerals, waters, etc.

For full details of public-land surveying, see "Manual of Surveying Instructions for the Survey of the Public Lands of the United States," issued by the Commissioner of the General Land-Office. These "Instructions" are prepared for the direction of those engaged on the public-land surveys, and new editions are issued from time to time to note any changes in methods of work or of marking stations.

## SPECIMEN FIELD-NOTES.

*East boundary of T. 13 N., R. 21 E.*

| Chains. |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |
|---------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|         | North, bet. secs. 25 and 30.<br>Over level land, through cedar timber.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
| 9·00    | Creek 13 lks. wide, pure water, 1 ft. deep, gentle current, course S. 80° E.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |
| 20·40   | Creek 15 lks. wide, pure water, 2 ft. deep, gentle current, course S. 70° E.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |
| 27·50   | Leave cedar timber, begin ascent, bears S. 70° E. and N. 70° W.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |
| 39·50   | Top of ascent of 40 ft., enter level plain, bears E. and W.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| 40·00   | Set a cedar post, 3 ft. long, 3 in. sq., with charred stake, 24 in. in the ground, for $\frac{1}{4}$ sec. cor., marked $\frac{1}{4}$ S. on W. face; dig pits, 18×17×12 in., N. and S. of post, 3 ft. dist., and raise a mound of earth, 3 $\frac{1}{2}$ -ft. base, 1 $\frac{1}{2}$ ft. high, W. of cor.<br>September 9: At this $\frac{1}{4}$ sec. cor. I set off 5° 9' N., on the decl. arc; and at 11 <sup>h</sup> 57 <sup>m</sup> . 1 l. m. t., observe the sun on the meridian; the resulting lat. is 45° 38' 0", which is about 0·2' greater than the proper lat. |
| 75·00   | Creek 12 lks. wide, pure water, 1 ft. deep, gentle current, course S. 80° E.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |
| 80·00   | Set a cedar post, 3 ft. long, 4 in. sq., with quart of charcoal, 24 in. in the ground, for cor. of secs. 19, 24, 25, and 30, marked<br>T. 13 N., S. 19 on N. E.,<br>R. 22 E., S. 30 on S. E.,<br>S. 25 on S. W., and<br>R. 21 E., S. 24 on N. W. faces; with 4 notches on N. and 2 notches on S. edges; dig pits, 18×18×12 in., in each sec. 5 $\frac{1}{2}$ ft. dist.; and raise a mound of earth, 4 ft. base, 2 ft. high, W. of cor.<br>Land, level.<br>Soil, sandy loam; 2d rate.<br>Timber, cedar.                                                                 |

*Subdivision of T. 15 N., R. 20 E.*

| Chains.             |                                                                                                                                                                                                                                                                                                          |
|---------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|                     | S. 89° 55' E., on a random line, bet. secs. 13 and 24.<br>Over level land.                                                                                                                                                                                                                               |
| 40·00               | Set. temp. $\frac{1}{4}$ sec. cor.                                                                                                                                                                                                                                                                       |
| 80·01               | Intersect E. bdy. of the Tp. at the cor. of secs. 13, 18, 19, and 24, which is a locust post 1 ft. above ground, 4 in. sq., marked and witnessed as described by the surveyor-general.<br>Thence I run<br>N. 89° 55' W., on a true line bet. secs. 13 and 24,<br>Over sandy alkali land.                 |
| 40·00 $\frac{1}{2}$ | Set. a juniper post, 3 ft. long, 3 in. sq., with marked stone, 24 in. in the ground, for $\frac{1}{4}$ sec. cor. marked $\frac{1}{4}$ S., on N. face; dig pits, 18×18×12 in., E. and W. of post, 3 ft. dist., and raise a mound of earth, 3 $\frac{1}{2}$ ft. base, 1 $\frac{1}{2}$ ft. high, N. of cor. |
| 80·01               | The cor. of secs. 13, 14, 23, and 24.<br>Alkali creek (now dry), runs eastward about 4·00 chs. south of this line.<br>Land, level.<br>Soil, alkali sand; 4th rate.<br>No timber.                                                                                                                         |

## THE SOLAR COMPASS.

**463.** Nearly all of the lines required in the public-land surveys are meridians and parallels of latitude. Meridians may be located by the methods given in Chapter III, but the easiest method is with the *Solar Compass*.

There are several varieties of this instrument, all of which are constructed on the same principle, and are modifications of the instrument invented by William A. Burt, and patented by him in 1836.

Before describing the solar compass, it will be necessary to define the terms to be used.

**464. Definitions.** The *axis of the earth* is the imaginary line about which it revolves. The points in which the axis meets the surface of the earth are called the *poles* of the earth.

Meridians are great circles of the earth's surface, passing through the poles. The equator is a great circle of the earth's surface,  $90^\circ$  from the poles. *Parallels of latitude* are small circles of the earth's surface parallel to the equator. *Latitude* is the distance north or south from the equator, and is measured on a meridian circle. *Longitude* is distance east or west from some established meridian. The meridian of Greenwich, England, is usually taken as the *prime meridian*, from which longitude is reckoned.

*Astronomical Terms.* Conceive all of the heavenly bodies projected upon the concave surface of a sphere, of which the earth is the center, and whose radius is infinitely great when compared with that of the earth. This is called the *Celestial Sphere*.

If the axis of the earth be prolonged, the points in which it meets the celestial sphere are called the north and south poles of the heavens, and the line joining them is called the axis of the celestial sphere. The apparent revolution of the heavenly bodies about the axis of the celestial sphere is due to the rotation of the earth on its axis once in twenty-four hours.

A plane passed tangent to the earth at the feet of an observer is the *sensible horizon*; and a plane passed, parallel to this, through the center of the earth, is the *rational horizon*. Since the radius of the earth is infinitely small in comparison with that of the celestial sphere, if the planes of the rational horizon and sensible horizon be extended in every direction indefinitely, they will meet the celestial sphere in one great circle, called the *celestial horizon*. If the plane of the earth's equator be extended indefinitely, it will meet the celestial sphere in a great circle, called the *celestial equator*, or *equinoctial*.

If through any place a line be passed, perpendicular to the plane of the horizon, the point in which it meets the celestial sphere above the observer is called the *zenith*; and the point in which it meets the celestial sphere below the observer, the *nadir*.

Great circles passing through the zenith and nadir are *vertical circles*.

The *zenith distance* of a *heavenly body* is its angular distance from the zenith, and is measured on a vertical circle. The *altitude* of a body is its angular distance above the celestial horizon, and is measured on a vertical circle. Altitude and zenith distance are complements of each other.

Great circles passing through the poles of the celestial sphere are called *circles of declination*, or *hour-circles*. The *declination* of a heavenly body is its angular distance north or south from the equinoctial, and is measured on a circle of declination.

The celestial meridian of any place is a great circle passing through the zenith, and through the poles of the celestial sphere. The line in which the plane of the celestial meridian meets the plane of the horizon is the *terrestrial meridian*, or true north and south line.

The *hour-angle* of a heavenly body is the angle at the pole between the meridian and the declination circle passing through the *body*.

The *parallactic angle* is the angle at the body between the declination circle and vertical circle passing through the body.

The *azimuth* of a heavenly body is the angle between the celestial meridian and a vertical circle passing through the body, and is measured on the celestial horizon.

If an observer be at the equator, the celestial horizon will pass through the poles of the heavens, and the celestial equator through the zenith. For each degree which the observer travels northward on the earth, the north pole of the heavens will appear to rise *one degree* above the horizon, and the celestial equator will appear to move *one degree* southward from the zenith. The latitude of a place, then, is equal to the altitude of the elevated pole, or to the declination of the zenith. In the northern hemisphere the north pole of the heavens is the elevated pole.

The earth revolves around the sun in an elliptical orbit once in a year. This gives the sun an apparent motion around the earth. The path of the earth, or the apparent path of the sun in the heavens, is called the *ecliptic*. It is a great circle on the celestial sphere, making an angle with the celestial equator of about  $23^{\circ} 27'$ . The two points in which the ecliptic meets the equinoctial are called the *equinoxes*. The sun is on the equinoctial the 21st of March. This is the *vernal equinox*. It then moves north of the equator, increasing constantly in northern declination, until the 21st of June, when its declination is about  $23^{\circ} 27'$  north. This is the *northern summer solstice*. It then decreases in declination until September 21st, when it is again on the equinoctial. This is the *autumnal equinox*. It then moves south of the equator, increasing in southern declination until December 21st, when its declination is about  $23^{\circ} 27'$  south. This is the *northern winter solstice*. It then decreases in declination until March 21st, when it again arrives at the vernal equinox. The declination of the sun is given in the "Nautical Almanac" for every day in the year.

The *transit* of a heavenly body is its passage across the celestial meridian.

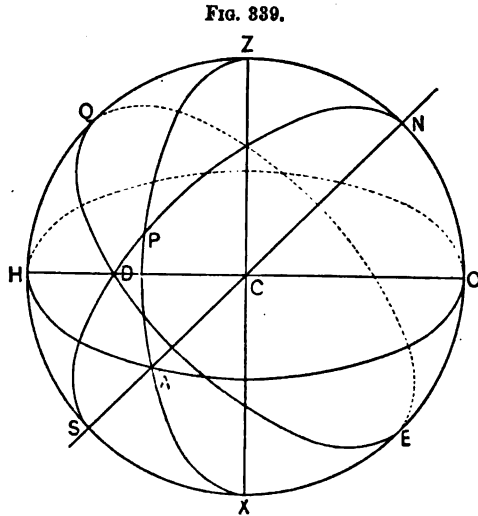
A *sidereal day* is the interval of time between two successive transits of

the vernal equinox. A *solar day* is the interval of time between two successive transits of the sun. The apparent motion of the sun is not uniform, and hence use is made of a fictitious, or mean sun, moving on the equinoctial with a uniform motion, and keeping *mean solar time*. This is the time kept by clocks and watches. The time indicated by the true sun is called *apparent solar time*. This is the time given by sun-dials. The difference between apparent solar time and mean solar time is called the *equation of time*. The equation of time is zero four times in a year, and its maximum value is about sixteen minutes. It is given in the "Nautical Almanac" for every day in the year.

A ray of light, passing from a rarer to a denser medium, is bent, or refracted, toward a perpendicular to the surface of the second medium at the point where the ray enters. The atmosphere surrounding the earth varies in density, being denser as we approach the surface of the earth. The light coming from a heavenly body, and passing through the atmosphere, will be constantly bent toward a perpendicular to the surface of the earth, and its path will be a curve, and not a straight line. The apparent direction of a heavenly body will be tangent to this curve where it meets the eye of the observer. The difference between the apparent and the true positions of a heavenly body is called *refraction*. It is zero at the zenith, and about  $38'$  at the horizon;  $45^\circ$  from the zenith it is about  $57''$ .

Refraction increases the altitude of a heavenly body and decreases the zenith distance.

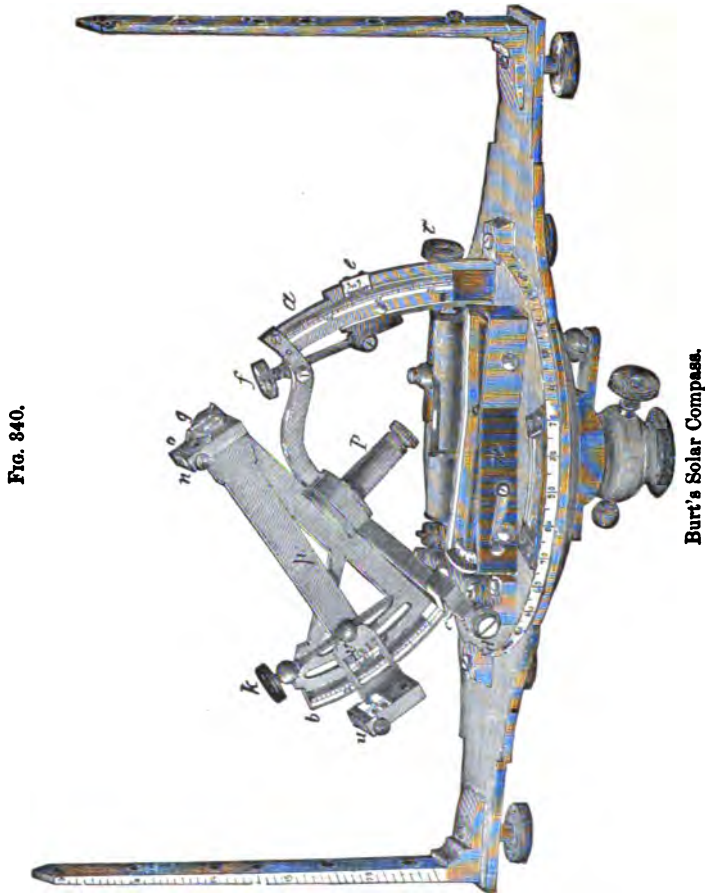
In Fig. 339,  $NS$  represents the axis of the celestial sphere,  $N$  the north pole, and  $S$  the south pole.  $EDQ$  is the equinoctial,  $HAO$  the horizon, and  $HZOX$  the meridian.  $ZAX$  is a vertical circle,  $ND S$  a declination-circle.  $O$  (the position of the earth) is the center of the celestial sphere.  $Z$  is the zenith and  $X$  the nadir. Let  $P$  be any point on the celestial sphere.  $AP$  is its altitude,  $PZ$  its zenith distance, and  $PD$  its declination;  $ZN P$  its hour-angle,  $Z P N$  its parallactic angle, and  $N Z P$  its azimuth.



**465.** The solar compass differs from the ordinary compass, Fig. 135, in having a solar apparatus, instead of a magnetic needle, for determining the meridian.

In the figure, *a* is the *latitude-arc*, whose center of motion is in two pivots, one of which is shown at *d*. It is furnished with a clamp, slow-motion screw, *f*, and vernier, *e*.

The *declination-arc* is shown at *b*. The movable arm, *h*, has its center of motion in a pivot at *g*, and is furnished with a clamp, vernier, *v*, and a slow-motion screw, *k*.



The plane of the *hour-arc*, *c*, is at right angles to the latitude-arc, and its center is in the *polar axis* *p*.

The declination-arc and latitude-arc are read to minutes by the verniers. The hour-arc is graduated to half-degrees, and is figured both for hours and degrees.

Attached to each end of the arm  $h$  is a rectangular block of brass, in which is set a convex lens, whose focus is on a silver plate attached to the face of the opposite block. The silver plate is marked by two sets of parallel lines, at right angles to each other, as shown in Fig. 341;  $bb$  are called the *hour-lines*, and  $cc$  the *equatorial lines*. The distance between the hour-lines and between the equatorial lines is equal to the diameter of the image of the sun, formed by the lens in the opposite block.



The needle-box  $n$  contains a magnetic needle, and is furnished with an arc of about  $36^\circ$  in extent, graduated to half-degrees. The needle-box can be moved about its center by the slow-motion screw  $t$ .

The sight and levels are similar to those of the ordinary compass.

The *equatorial sights*,  $u$  and  $n$ , attached to the upper side of the rectangular lens-blocks, are used in the adjustments.

The *adjuster*, also used in adjusting the instrument, is kept in the instrument-box, and is not shown in the figure.

The compass-sights are attached to the lower plate, and the solar apparatus, levels, and needle-box to the upper plate. The horizontal limb is read to single minutes by the vernier.

Suppose the instrument to be set up and leveled, with the latitude-arc toward the south. If, now, the latitude-arc be set to the latitude of the place of observation (that is, so that the plane of the hour-arc makes an angle with the vertical equal to the latitude of the place), the plane of the hour-arc will then be in the plane of the celestial equator, and the polar axis will be parallel to the axis of the earth, and will point toward the north pole of the heavens. If the sun be on the celestial equator, the declination-arm,  $h$ , may be set at zero on the declination-arc, and it will then lie in the plane in which the sun appears to move. If the declination-arc be turned so as to point toward the sun, the lens in the block toward the sun will form an image on the silver plate attached to the opposite block. By means of the polar axis,  $p$ , the declination-arm may be turned so as to follow the sun all day.

When the sun is not at the equinoxes, set off its declination on the declination-arc, and the declination-arm, when turned about on

the axis,  $p$ , will still turn in the plane in which the sun appears to move. When the sun is in south declination, turn the declination-arc away from the sun; and when the sun is in north declination, turn the declination-arc toward the sun.

When the instrument is in perfect adjustment, and is properly set up and leveled, the image of the sun can not be brought between the equatorial lines, unless the sights are in the plane of the meridian.

#### *Adjustments.*

**466.** The adjustments will be given in the order in which they should be made. In describing each adjustment, it will be supposed that the instrument has been properly set up and leveled, and the latitude-arc turned toward the south.

**467. First Adjustment.** *To cause the level-bubbles to remain in the center of the tubes when the instrument is turned around on its vertical axis.* The verification and rectification are the same as those given for the transit (322).

**468. Second Adjustment.** *To adjust the equatorial lines and solar lenses.* Detach the declination-arm,  $h$ , by removing the necessary screws, and attach in its place the *adjuster*, replacing the screws of the pivot, and also of the clamp.

Place the arm  $h$  on the adjuster, with the same side against the declination-arc as before it was detached. Then, by means of the vertical axis of the instrument, the declination and latitude arcs, and the leveling-screws, turn the arm in the direction of the sun, and bring the image of the sun between the equatorial lines. Then turn the arm half over, bringing the opposite faces of the blocks in contact with the adjuster.

If the sun's image remains between the equatorial lines, the silver plate is in its proper position. If not, loosen the screws which hold the plate, and move the plate so as to correct half of the apparent error. Verify the work by repeating the above operation, until the image remains between the lines in both positions of the arm.

To adjust the other plate, turn the arm end for end on the adjuster, and then proceed as for the first plate.



When both plates have been properly adjusted, remove the adjuster, and replace the declination-arm and its attachments.

**469. Third Adjustment.** *To adjust the vernier of the declination-arc.* Set the vernier of the declination-arc at zero. Turn the declination-arm *h* so as to point toward the sun. Bring the sun's image between the equatorial lines, by means of the slow-motion screw of the latitude-arc and the parallel plate-screws, as in the second adjustment. Then revolve the arm so as to bring the opposite solar lens toward the sun. If the sun's image now comes between the equatorial lines, no adjustment is necessary. If not, correct half of the apparent error by means of the slow-motion screw *k*. Verify the work by repeating the above operation until the image comes between the lines in both positions of the arm. The zero of the vernier will now not coincide with the zero of the arc. Make it do so by loosening the screws which hold the vernier, and moving the vernier.

**470. Fourth Adjustment.** *To adjust the Solar Apparatus to the Compass-Sights.* Set the vernier of the horizontal limb at  $90^\circ$ . Raise the latitude-arc until the polar axis is horizontal, and set the vernier of the declination-arc at zero. Direct the equatorial sights at some distant point. If the same point is seen through the sights, no adjustment is necessary. If not, the sights must be changed, or some equivalent adjustment made, which can only be done by an instrument-maker.

#### **Field-Work.**

**471.** Before the instrument can be used in the field, it is necessary to determine what angles are to be set off on the declination-arc and on the latitude-arc.

On the declination-arc, both the declination of the sun and the correction for refraction must be provided for.

**472. Declination.** The declination of the sun at noon at Greenwich, England, is given in the "Nautical Almanac" for every day in the year, together with the hourly change in declination.

To determine the declination at any place for any time, a correction will need to be applied for difference of declination due to

the difference of time corresponding to difference of longitude, and also for change of declination for different hours of the day.

For example, suppose we wish to find the declination of the sun at Schenectady, New York, for the different hours of the day on May 1, 1885. The longitude of Schenectady is  $73^{\circ} 55' 50''$  west. This in time is 4 h. 55 m. 43 sec., or approximately (and near enough for this purpose) 5 hours. From the "Nautical Almanac" we find that the declination of the sun at Greenwich, noon on May 1st, to be  $15^{\circ} 12' 37.5''$  north, and the hourly difference is  $45''$ .

When it is noon at Greenwich, it is 7 o'clock in the morning at Schenectady, and at that time the declination of the sun is  $15^{\circ} 12' 37''$ .

For the successive hours of the day we have only to add the hourly difference in declination,  $55''$  (the sun at that time having a motion northward from the equator).

**473. Refraction.** Tables of refraction have been calculated, giving the amount of refraction for different altitudes from the horizon. These tables, however, give the refraction in a vertical plane, and are not directly applicable for use as a correction in declination. It is evident that, in revolving the declination-arc around the polar axis, the declination-arc will not lie in the plane of a vertical circle, except when it is placed in the plane of the meridian. The correction for refraction, to be set off on the declination-arc, will not, therefore, be equal to the refraction given in the tables except at noon.

The proper correction for refraction to be set off on the declination-arc varies with the latitude, declination of the sun, and hour-angle of the sun.

From Chauvenet's "Astronomy," Art. 120, we have :

$$\text{Refraction in declination} = k' \cdot \tan. z \cdot \cos. q.$$

The value of  $k'$  may be taken from Table II, Chauvenet's "Astronomy." Its mean value is about  $57''$ , and this may be employed when very precise results are not required.

$z$  is the zenith distance, and  $q$  the parallactic angle.

From Art. 15, Chauvenet's "Astronomy," we have :

$$\tan. z \cdot \cos. q = \cot. (\delta + N),$$

in which  $\delta$  = declination of the sun, and  $N$  is an auxiliary quantity.  $\tan. N$  equals  $\cot. \phi . \cos. t$ , in which  $\phi$  is the latitude of the place, and  $t$  the hour-angle of the sun.

The tables of Refraction in Declination \* are calculated by the above formulas.

In the tables the hour-angle denotes the distance of the sun from the meridian in hours. Thus, at 7 o'clock A. M. the value of the hour-angle is five hours. The north declinations are indicated by + and the south declinations by -.

When the sun is in north declination, the refraction in declination given by the tables is additive. When the sun is in south declination, it is subtractive.

No tables of refraction can be relied upon for altitudes of less than five degrees.

To use the tables, suppose the declination, corrected for refraction, be required for each hour of the day, May 1, 1885, at Schenectady, New York.

By Art. 472 we found that the declination at 7 o'clock in the morning was  $15^{\circ} 12' 37''$ . The latitude of Schenectady is  $42^{\circ} 49'$ . (Take tabular values for  $42^{\circ} 30'$ .)

In the tables we find that the refraction in declination for latitude  $42^{\circ} 30'$ , when the sun's declination is  $15^{\circ}$ , and hour-angle 5 hours, is  $1' 36''$ . Adding this to  $15^{\circ} 12' 37''$ , we have  $15^{\circ} 14'$  to be set off on the declination-arc.

**474. To determine the Latitude.** Set off on the declination-arc the declination of the sun at noon on the given day (corrected for refraction).

A few minutes before noon, set up and level the instrument, set the declination-arc at 12 o'clock on the hour-arc, and turn the instrument horizontally until the declination-arm is directed toward the sun. Move the latitude-arc vertically so as to bring the sun's image between the equatorial lines. As the sun moves toward the meridian, turn the instrument horizontally so as to keep the image between the hour-lines, and move the latitude-arc so as to keep the

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\* These tables were calculated by Edward W. Arms, C. E., for W. & L. E. Gurley.

image between the equatorial lines. So long as the sun is ascending, the image will move downward on the plate. When the sun has passed the meridian, and begins to descend, the image will move upward. When the image begins to move upward, the reading on the latitude-arc will give the latitude of the place.

**475. To determine the "Meridian," or true North and South Line.** Set off on the latitude-arc the latitude of the place, and on the declination-arc the declination of the sun at the time, corrected for refraction. Level the instrument, clamp the horizontal plates at zero, turn the latitude-arc approximately south, and direct the declination-arm toward the sun. Then with one hand turn the instrument horizontally, and with the other revolve the declination-arm on the polar axis, until the image of the sun is brought between the equatorial lines. The sights will then point north and south.

**476. Running Lines.** The meridian being given by the solar compass, it can be used for determining the bearing of lines in the same way as an ordinary compass, but with greater precision, as the meridian is more accurately determined, and the angles are read by the vernier to single minutes.

**477. Use of the Magnetic Needle.** Since the solar compass gives the true meridian, and the magnetic needle the "magnetic meridian," the declination of the magnetic needle can be read off directly from the magnetic needle. If the needle be kept at zero of the compass-box arc, by turning the box with its tangent-screw, the declination of the needle can be read to minutes on the arc which shows the movement of the compass-box.

By constantly noting the declination of the needle, or by moving the needle-box so as to keep the needle reading zero, lines may be run by the needle, while the sun is obscured, or at such times as for any reason the solar apparatus is not reliable, as when the sun is near the horizon or the meridian.

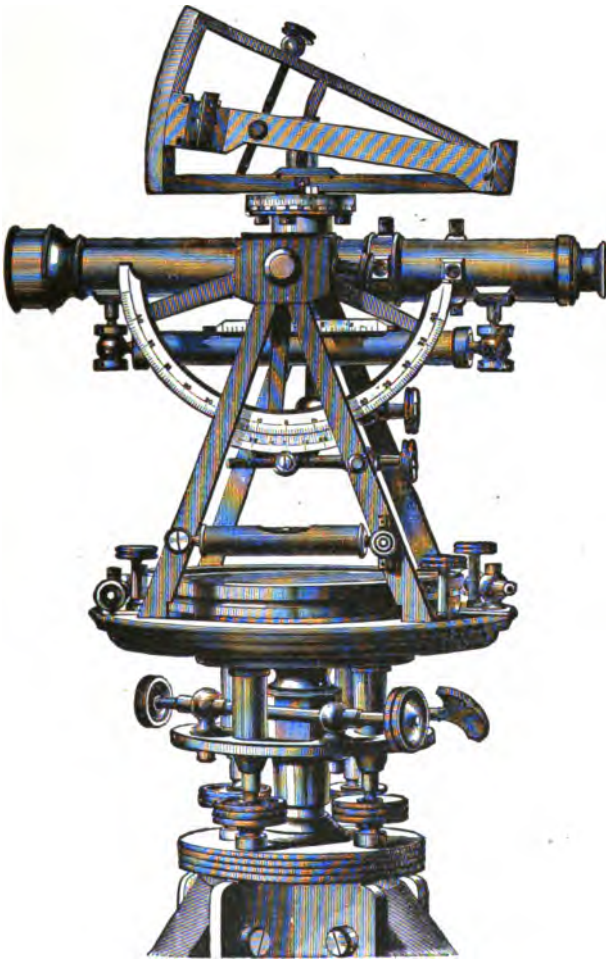
**478. Solar Attachment.\*** The solar apparatus may be attached to a transit, as shown in Fig. 342.

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\* This attachment, shown in Fig. 342, is manufactured by W. & L. E. Gurley, Troy, New York.

The "polar axis" of the solar apparatus is attached to the horizontal axis of the telescope, and projects upward. The "hour-circle" is the small graduated circle, shown above the telescope.

FIG. 342.



Engineer's Transit, with Solar Attachment.

On the "polar axis" rests the frame, which carries the "declination-arc," and the "arm" with its slow-motion attachments, "solar lenses," and "equatorial lines," as before described.

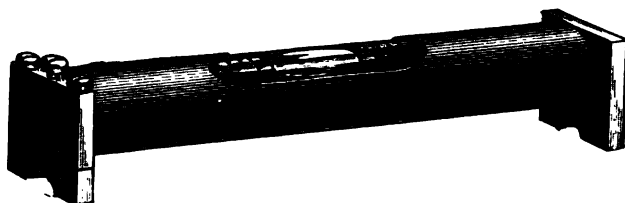
The vertical circle, or arc, of the transit, is used for a "latitude-arc."

*Adjustments.*

479. The first, second, and third adjustments are similar to those of the solar compass, already explained.

480. **To adjust the Polar Axis.** Level the instrument carefully, and then level the telescope by means of the level attached to it. Set the arm of the declination-arc at zero, and bring it parallel to the telescope. Place an adjusting level, shown in Fig. 343, on the

FIG. 343



rectangular blocks attached to the declination-arm. If the bubble remains in the center, the polar axis needs no adjustment in the plane of the axis of the telescope. If not, bring the bubble to the center by means of the two capstan-head screws under the hour-circle, and in line with the telescope. Then turn the declination-arm on the polar axis until it is parallel to the telescope axis, and at right angles to its former position. If the bubble now remains in the center, no adjustment is necessary. If not, bring the bubble to the center by means of the pair of capstan-head screws under the hour-circle and in line with the telescope axis. Verify, and repeat the above operations until the bubble of the adjusting level will remain in the center while the declination-arm is revolved horizontally on the polar axis.

481. **To adjust the Hour-Arc.** When the telescope is in the plane of the meridian, the index of the hour-circle should give apparent solar time—that is, mean solar time  $\pm$  the equation of time. If the index does not point to the proper division, it can be made to do so by loosening the screws on the top of the hour-circle, and turning it until the correct time is indicated by the index.

FIG. 344.



Transit, with Solar Attachment.

482. The method of using the solar apparatus on the transit is so nearly the same as that on the compass, already given, that no separate directions will be necessary.

483. Fig. 344 represents a transit with another form of solar attachment.\* It consists essentially of a small telescope and level, the telescope being mounted in standards, in which it can be elevated or depressed. The standard revolves around an axis, called the polar axis, which is fastened to the telescope axis of the transit instrument. The telescope, called the "solar telescope," can thus be moved in altitude and azimuth. It is provided with shade-glasses to subdue the glare of the sun, as well as a prism to observe with greater ease when the declination is far north. Two pointers attached to the telescope to approximately set the instrument are so adjusted that when the shadow of the one is thrown on the other the sun will appear in the field of view.

#### ADJUSTMENT OF THE APPARATUS.

1. The transit must be in perfect adjustment, especially the levels on the telescope and the plates; the cross axis of the telescope should be exactly horizontal, and the index error of the vertical circle carefully determined.

2. *The polar axis must be at right angles to the line of collimation and horizontal axis of main telescope.*

To effect this, level the instrument carefully and bring the bubble of each telescope level to the middle of its scale. Revolve the solar around its polar axis, and if the bubble remains central the adjustment is complete. If not, correct half the movement by the adjusting screws at the base of the polar axis, and the other half by moving the solar telescope on its horizontal axis.

3. *The line of collimation of the solar telescope and the axis of its level must be parallel.*

To effect this bring both telescopes in the same vertical plane and both bubbles to the middle of their scales. Observe a mark through the transit telescope, and note whether the solar telescope

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\* Invented and manufactured by G. N. Saegmüller, Washington, D. C., from whose catalogue the description is taken.



points to a mark above this, equal to the distance between the horizontal axes of the two telescopes. If it does not bisect this mark, move the cross-wires by means of the screws until it does. Generally the small level has no adjustments and the parallelism is effected only by moving the cross-hairs.

The adjustments of the transit and the solar should be *frequently* examined, and kept as nearly perfect as possible.

DIRECTIONS FOR USING THE ATTACHMENT.

*First.* Take the declination of the sun as given in the "Nautical Almanac" for the given day, and correct it for refraction and hourly change. Incline the *transit telescope* until this amount is indicated by its vertical arc. If the declination of the sun is north, depress it; if south, elevate it. Without disturbing the position of the transit telescope, bring the solar telescope into the vertical plane of the large telescope and to a horizontal position by means of its level. The two telescopes will then form an angle which equals the amount of the declination, and the inclination of the solar telescope to its polar axis will be equal to the polar distance of the sun.

*Second.* Without disturbing the *relative* positions of the two telescopes, incline them and set the vernier to the co-latitude of the place.

By moving the transit and the "Solar Attachment" around their respective *vertical* axes, the image of the sun will be brought into the field of the solar telescope, and after accurately bisecting it the *transit telescope must be in the meridian, and the compass-needle indicates its deviation at that place.*

483<sup>1</sup>. A series of observations were made for the Ohio Society of Surveyors and Civil Engineers, by Prof. C. S. Howe and Mr. J. B. Davis, to determine the accuracy attainable with solar attachments. The instruments used were Gurley's, Saegmüller's, and Buff & Berger's. In their report they say:

"It soon became evident that to secure the best results, instruments must not only be carefully adjusted, but must also be frequently tested on a known meridian line.

"Errors of one minute, or even one minute and a half, either way, are not infrequent, and any single observation would be uncertain to this extent; but the mean of twenty or more observations ought to be within less than half a minute."

For full details of the observations see "Transactions of the Ohio Society of Surveyors and Civil Engineers," 1895.

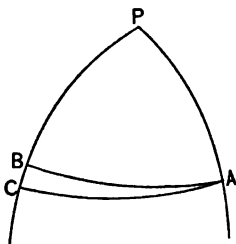
**To locate a Parallel of Latitude.**

**484.** If a line be run on the surface of the earth, having all of its points in the same vertical plane, as they will be when lined in by a properly adjusted transit, the line will be a great circle of the earth, and can not coincide with a parallel of latitude.

Points on a parallel of latitude are usually determined by offsets from a great circle. The following are some of the methods employed:

**485. By Offsets from a Tangent.** In Fig. 345, let P be the pole of the earth, P A and P B the meridians, and A B the desired parallel.

FIG. 345.



If from A a line be run perpendicular to the meridian A P, it is evident that, owing to the convergence of the meridians, the perpendicular will not coincide with the parallel of latitude through A. In north latitudes, as in the United States, the perpendicular, A C, will run to the south of the parallel, A B.

To find the distance C B, when the latitude of the starting point A, and the distance A C are known.

In the triangle P A C, right-angled at A:

$$\cos. PC = \cos. AP \times \cos. AC.$$

$$BC = PC - PB, \text{ and } AP = BP = \text{co-latitude.}$$

$$\therefore \cos. PC = \sin. \text{latitude} \times \cos. AC \quad . . . . . [1.]$$

A C, being a measured distance on an arc of a great circle, must be reduced to the corresponding angle.

$$\text{Angle of any arc in minutes} = \frac{\text{length of arc} \times 3437.7468}{\text{radius}}.$$

$$(3437 \cdot 7468 = 57 \cdot 29578 \times 60). \quad \text{Art. 280.}$$

Treating the earth as a sphere, this becomes :

$$\text{Angle of arc in minutes} = \text{length of arc} \frac{3437 \cdot 7468}{20912405}.$$

$$\text{Log. arc in minutes} = \text{log. length} - 3 \cdot 7841301 \quad . \quad . \quad [2.]$$

Then use the value obtained by [2] in formula [1].

BC is found as an angle. To reduce it to feet, we have :

$$\text{Length in feet} = \frac{\text{angle in minutes} \times \text{radius}}{3437 \cdot 7468}.$$

$$\text{Length in feet} = \frac{\text{angle in seconds} \times \text{radius}}{60 \times 3437 \cdot 7468}.$$

$$\text{Log. length in feet} = \text{log. angle in seconds} + 2 \cdot 0059789 \quad . \quad . \quad [3.]$$

*Otherwise.* Find the length of an arc subtending one second at the center.

$$\frac{2\pi \times 20912405}{360 \times 60 \times 60} = 101 \cdot 386 \text{ feet};$$

i. e., 101·386 feet subtends an angle of one second at the center of the earth. Then, angle in seconds =  $\frac{\text{distance in feet}}{101 \cdot 386}$ , and distance = angle in seconds  $\times$  101·386 . . . . . [4.]

*Approximately,*

$$BC \text{ in seconds} = \frac{1}{4} P^2 (\text{in seconds}) \times \sin. 2PA \times \sin. 1''. \quad . \quad [5.]$$

$$\text{To find } P. \quad \tan. P = \frac{\tan. AB}{\sin. AP}.$$

*Example.* Latitude  $45^\circ$  north, and distance 6 miles, required the offset BC.

$$6 \text{ miles} = 31680 \text{ feet.}$$

$$\begin{array}{r} \text{By [2]} \quad \log. 31680 = 4 \cdot 5007852 \\ \quad \quad \quad - 3 \cdot 7841301 \end{array}$$

$$\begin{array}{r} \log. 5' \cdot 207808 = \cdot 7166551 \\ 5' \cdot 207808 = 5' 12'' \cdot 468 \end{array}$$

$$\text{By [1]} \quad \log. \sin. 45^\circ = 9 \cdot 8494850$$

$$\log. \cos. 5' 12'' \cdot 468 = 9 \cdot 9999995$$

$$\log. \cos. PC = \log. \cos. 45^\circ 0' 0'' \cdot 237 = 9 \cdot 8494845$$

$$\therefore BC = 0'' \cdot 237$$

To reduce to feet by [3],  $\log. 0''\cdot237 = \overline{1}\cdot3747483$

$$\log. BC \text{ in feet} = \log. 24\cdot029 \text{ feet} = \overline{1}\cdot3807272$$

*Second Method :*

$$\text{Angle} = \frac{31680}{101\cdot386} = 312' = 5' 12''\cdot468.$$

Then, as above, we find  $BC = 0''\cdot237$  of arc.

$$BC \text{ in feet} = 0''\cdot237 \times 101\cdot386 = 24\cdot0289 \text{ feet.}$$

*Approximate Method :*

Solving by formula [5], we find  $BC = 24\cdot3$  feet.

**486. Spheroidal Formula.** The preceding methods suppose the earth to be a sphere. Treating it as a spheroid, the following formula is without material error for distances within 100 miles :

$$CB = \frac{1}{2} k^2 \tan. L \frac{(1 - [e^2 \cdot \sin.^2 L])^{\frac{1}{2}}}{a}$$

$k$  = distance in feet,  $L$  = latitude of initial point.

$a$  equatorial radius = 20926062 feet.

$e = \cdot08169683$ .

*Example.* Latitude  $45^\circ$  N. Distance 6 miles.

$$\log. e^2 = \overline{3}\cdot8244104$$

$$\log. \sin.^2 45^\circ = \begin{cases} 9\cdot8494850 \\ 9\cdot8494850 \end{cases}$$

$$\log. \cdot0033371 = \overline{3}\cdot5233804$$

$$1 - \cdot0033371 = \cdot9966628$$

$$\frac{1}{2} \log. 0\cdot9966628 = \overline{1}\cdot9992741 = \log. \text{numerator.}$$

$$\log. \frac{1}{2} = \overline{1}\cdot6989700$$

$$\log. k^2 = \begin{cases} 4\cdot5007852 \\ 4\cdot5007852 \end{cases}$$

$$\log. \tan. 45 = 10\cdot$$

$$\log. \text{numerator} = \begin{cases} \overline{1}\cdot9992741 \\ 8\cdot6998145 \end{cases}$$

$$\log. a = 7\cdot3206875$$

$$\log. 23\cdot941 \text{ feet} = \overline{1}\cdot3791270$$

**487.** Instead of making the great circle tangent at the starting-point, it may be run so as to be tangent at the three-mile point of

## AZIMUTHS OF THE TANGENT TO THE PARALLEL.

[The azimuth is the *smallest* angle the tangent makes with the true meridian and always measured from the north and toward the tangential points.]

| LAT. | 1 mile.    | 2 miles.   | 3 miles.   | 4 miles.   | 5 miles.   | 6 miles.   |
|------|------------|------------|------------|------------|------------|------------|
|      | ° ' "      | ° ' "      | ° ' "      | ° ' "      | ° ' "      | ° ' "      |
| 30°  | 89 59 30.0 | 89 58 59.9 | 89 58 29.9 | 89 57 59.9 | 89 57 29.9 | 89 56 59.8 |
| 31°  | 89 59 28.8 | 89 58 57.5 | 89 58 26.3 | 89 57 55.0 | 89 57 23.8 | 89 56 52.5 |
| 32°  | 89 59 27.5 | 89 58 55.0 | 89 58 22.5 | 89 57 50.0 | 89 57 17.5 | 89 56 45.0 |
| 33°  | 89 59 26.2 | 89 58 52.5 | 89 58 18.7 | 89 57 44.9 | 89 57 11.2 | 89 56 37.4 |
| 34°  | 89 59 24.9 | 89 58 49.9 | 89 58 14.8 | 89 57 39.7 | 89 57 04.6 | 89 56 29.6 |
| 35°  | 89 59 23.6 | 89 58 47.2 | 89 58 10.8 | 89 57 34.4 | 89 56 58.0 | 89 56 21.6 |
| 36°  | 89 59 22.2 | 89 58 44.4 | 89 58 06.8 | 89 57 28.9 | 89 56 51.1 | 89 56 13.4 |
| 37°  | 89 59 20.8 | 89 58 41.6 | 89 58 02.5 | 89 57 23.3 | 89 56 44.1 | 89 56 05.0 |
| 38°  | 89 59 19.4 | 89 58 38.8 | 89 57 58.2 | 89 57 17.5 | 89 56 36.9 | 89 55 56.3 |
| 39°  | 89 59 17.9 | 89 58 35.8 | 89 57 53.7 | 89 57 11.6 | 89 56 29.6 | 89 55 47.5 |
| 40°  | 89 59 16.4 | 89 58 32.8 | 89 57 49.2 | 89 57 05.5 | 89 56 21.9 | 89 55 38.3 |
| 41°  | 89 59 14.8 | 89 58 29.6 | 89 57 44.4 | 89 56 59.3 | 89 56 14.1 | 89 55 28.9 |
| 42°  | 89 59 13.2 | 89 58 26.4 | 89 57 39.6 | 89 56 52.8 | 89 56 06.0 | 89 55 19.2 |
| 43°  | 89 59 11.5 | 89 58 23.1 | 89 57 34.6 | 89 56 46.2 | 89 55 57.7 | 89 55 09.2 |
| 44°  | 89 59 09.8 | 89 58 19.6 | 89 57 29.5 | 89 56 39.3 | 89 55 49.1 | 89 54 58.9 |
| 45°  | 89 59 08.0 | 89 58 16.1 | 89 57 24.1 | 89 56 32.1 | 89 55 40.2 | 89 54 48.2 |
| 46°  | 89 59 06.2 | 89 58 12.4 | 89 57 18.6 | 89 56 24.8 | 89 55 31.0 | 89 54 37.2 |
| 47°  | 89 59 04.3 | 89 58 08.6 | 89 57 12.9 | 89 56 17.1 | 89 55 21.4 | 89 54 25.7 |
| 48°  | 89 59 02.3 | 89 58 04.6 | 89 57 06.9 | 89 56 09.2 | 89 55 11.5 | 89 54 18.8 |
| 49°  | 89 59 00.2 | 89 58 00.5 | 89 57 00.7 | 89 56 00.0 | 89 55 01.2 | 89 54 01.4 |
| 50°  | 89 58 58.1 | 89 57 56.2 | 89 56 54.3 | 89 55 52.6 | 89 54 50.5 | 89 53 48.5 |

| LAT. | 7 miles.   | 8 miles.   | 9 miles.   | 10 miles.  | 11 miles.  | 12 miles.  |
|------|------------|------------|------------|------------|------------|------------|
|      | ° ' "      | ° ' "      | ° ' "      | ° ' "      | ° ' "      | ° ' "      |
| 30°  | 89 56 29.8 | 89 55 59.8 | 89 55 29.8 | 89 54 59.7 | 89 54 29.7 | 89 53 59.7 |
| 31°  | 89 56 21.3 | 89 55 50.0 | 89 55 18.8 | 89 54 47.6 | 89 54 16.3 | 89 53 45.1 |
| 32°  | 89 56 12.5 | 89 55 40.0 | 89 55 07.6 | 89 54 35.1 | 89 54 02.6 | 89 53 30.1 |
| 33°  | 89 56 03.6 | 89 55 29.9 | 89 54 56.1 | 89 54 22.3 | 89 53 48.5 | 89 53 14.8 |
| 34°  | 89 55 54.5 | 89 55 19.4 | 89 54 44.4 | 89 54 09.3 | 89 53 34.2 | 89 52 59.1 |
| 35°  | 89 55 45.2 | 89 55 08.8 | 89 54 32.3 | 89 53 55.9 | 89 53 19.5 | 89 52 43.1 |
| 36°  | 89 55 35.6 | 89 54 57.8 | 89 54 20.0 | 89 53 42.3 | 89 53 04.5 | 89 52 26.7 |
| 37°  | 89 55 25.8 | 89 54 46.6 | 89 54 07.4 | 89 53 28.2 | 89 52 49.1 | 89 52 09.9 |
| 38°  | 89 55 15.7 | 89 54 35.1 | 89 53 54.5 | 89 53 13.9 | 89 52 33.2 | 89 51 52.6 |
| 39°  | 89 55 05.4 | 89 54 23.3 | 89 53 41.2 | 89 52 59.1 | 89 52 17.0 | 89 51 34.9 |
| 40°  | 89 54 54.7 | 89 54 11.1 | 89 53 27.5 | 89 52 43.8 | 89 52 00.2 | 89 51 16.6 |
| 41°  | 89 54 43.7 | 89 53 58.5 | 89 53 13.4 | 89 52 28.2 | 89 51 43.0 | 89 50 57.8 |
| 42°  | 89 54 32.4 | 89 53 45.6 | 89 52 58.8 | 89 52 12.0 | 89 51 25.2 | 89 50 38.4 |
| 43°  | 89 54 20.8 | 89 53 32.3 | 89 52 43.8 | 89 51 55.4 | 89 51 06.9 | 89 50 18.5 |
| 44°  | 89 54 08.7 | 89 53 18.5 | 89 52 28.4 | 89 51 38.2 | 89 50 48.0 | 89 49 57.8 |
| 45°  | 89 53 56.3 | 89 53 04.3 | 89 52 12.3 | 89 51 20.4 | 89 50 28.4 | 89 49 36.4 |
| 46°  | 89 53 43.4 | 89 52 49.5 | 89 51 55.7 | 89 51 01.9 | 89 50 08.1 | 89 49 14.3 |
| 47°  | 89 53 30.0 | 89 52 34.3 | 89 51 38.6 | 89 50 42.9 | 89 49 47.2 | 89 48 51.4 |
| 48°  | 89 53 16.1 | 89 52 18.4 | 89 51 20.7 | 89 50 23.0 | 89 49 25.3 | 89 48 27.6 |
| 49°  | 89 53 01.7 | 89 52 01.9 | 89 51 02.1 | 89 50 02.4 | 89 49 02.6 | 89 48 02.8 |
| 50°  | 89 52 46.6 | 89 51 44.7 | 89 50 42.8 | 89 49 40.9 | 89 48 39.0 | 89 47 37.1 |

## OFFSETS, IN FEET, FROM TANGENT TO PARALLEL.

| LAT. | 1 mile. | 2 miles. | 3 miles. | 4 miles. | 5 miles. | 6 miles. |
|------|---------|----------|----------|----------|----------|----------|
|      | Feet.   | Feet.    | Feet.    | Feet.    | Feet.    | Feet.    |
| 30°  | 0·39    | 1·54     | 3·47     | 6·17     | 9·64     | 13·88    |
| 31°  | 0·40    | 1·60     | 3·61     | 6·42     | 10·03    | 14·44    |
| 32°  | 0·42    | 1·67     | 3·76     | 6·67     | 10·42    | 15·02    |
| 33°  | 0·43    | 1·73     | 3·90     | 6·93     | 10·82    | 15·60    |
| 34°  | 0·45    | 1·80     | 4·05     | 7·20     | 11·25    | 16·20    |
| 35°  | 0·47    | 1·87     | 4·20     | 7·47     | 11·68    | 16·81    |
| 36°  | 0·48    | 1·94     | 4·36     | 7·75     | 12·11    | 17·44    |
| 37°  | 0·50    | 2·01     | 4·52     | 8·04     | 12·57    | 18·09    |
| 38°  | 0·52    | 2·08     | 4·69     | 8·33     | 13·02    | 18·75    |
| 39°  | 0·54    | 2·16     | 4·86     | 8·63     | 13·49    | 19·43    |
| 40°  | 0·56    | 2·24     | 5·03     | 8·95     | 13·98    | 20·11    |
| 41°  | 0·58    | 2·32     | 5·21     | 9·27     | 14·48    | 20·85    |
| 42°  | 0·60    | 2·40     | 5·40     | 9·59     | 14·99    | 21·59    |
| 43°  | 0·62    | 2·48     | 5·59     | 9·93     | 15·52    | 22·35    |
| 44°  | 0·64    | 2·57     | 5·79     | 10·29    | 16·07    | 23·14    |
| 45°  | 0·67    | 2·66     | 5·99     | 10·65    | 16·64    | 23·96    |
| 46°  | 0·69    | 2·76     | 6·20     | 11·02    | 17·21    | 24·80    |
| 47°  | 0·71    | 2·85     | 6·42     | 11·41    | 17·83    | 25·68    |
| 48°  | 0·74    | 2·95     | 6·65     | 11·82    | 18·47    | 26·59    |
| 49°  | 0·76    | 3·06     | 6·88     | 12·24    | 19·12    | 27·54    |
| 50°  | 0·79    | 3·17     | 7·13     | 12·68    | 19·80    | 28·52    |

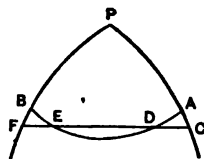
| LAT. | 7 miles. | 8 miles. | 9 miles. | 10 miles. | 11 miles. | 12 miles. |
|------|----------|----------|----------|-----------|-----------|-----------|
|      | Feet.    | Feet.    | Feet.    | Feet.     | Feet.     | Feet.     |
| 30°  | 18·89    | 24·67    | 31·23    | 38·55     | 46·65     | 55·32     |
| 31°  | 19·66    | 25·68    | 32·49    | 40·12     | 48·54     | 57·77     |
| 32°  | 20·44    | 26·69    | 33·78    | 41·71     | 50·47     | 60·06     |
| 33°  | 21·23    | 27·74    | 35·10    | 43·34     | 52·44     | 62·41     |
| 34°  | 22·05    | 28·80    | 36·45    | 45·00     | 54·45     | 64·80     |
| 35°  | 22·89    | 29·89    | 37·83    | 46·71     | 56·62     | 67·26     |
| 36°  | 23·74    | 31·01    | 39·25    | 48·45     | 58·63     | 69·77     |
| 37°  | 24·62    | 32·16    | 40·70    | 50·24     | 60·79     | 72·35     |
| 38°  | 25·52    | 33·33    | 42·19    | 52·08     | 63·02     | 75·00     |
| 39°  | 26·44    | 34·54    | 43·71    | 53·97     | 65·30     | 77·71     |
| 40°  | 27·40    | 35·78    | 45·29    | 55·91     | 67·65     | 80·51     |
| 41°  | 28·37    | 37·06    | 46·90    | 57·91     | 70·07     | 83·39     |
| 42°  | 29·38    | 38·38    | 48·57    | 59·97     | 72·56     | 86·35     |
| 43°  | 30·42    | 39·74    | 50·29    | 62·09     | 75·13     | 89·41     |
| 44°  | 31·50    | 41·14    | 52·07    | 64·28     | 77·78     | 92·57     |
| 45°  | 32·61    | 42·59    | 53·91    | 66·55     | 80·53     | 95·84     |
| 46°  | 33·76    | 44·10    | 55·81    | 68·90     | 83·37     | 99·22     |
| 47°  | 34·95    | 45·65    | 57·78    | 71·34     | 86·32     | 102·72    |
| 48°  | 36·19    | 47·27    | 59·83    | 73·86     | 89·37     | 106·36    |
| 49°  | 37·48    | 48·95    | 61·96    | 76·49     | 92·55     | 110·15    |
| 50°  | 38·82    | 50·70    | 64·17    | 79·22     | 95·86     | 114·08    |

the township line. This will require shorter offsets. The azimuths and offsets in any case may be taken from the tables of azimuths and offsets from tangents, noting that for a township the great circle runs three miles each way from the point of tangency. Suppose it is required to run such a tangent to the  $45^\circ$  parallel. From the tables we find the azimuth for the three-mile point is  $89^\circ 57' 24.1''$ , and the offset 5.99 feet. Then determine a point on the meridian through A and 5.99 feet south. From this point run a line having an azimuth of  $89^\circ 57' 24.1''$ , and it will be tangent to the latitude arc at the three-mile point. All required azimuths and offsets are given in the table.

The azimuth or bearing of the tangent at successive mile points will be taken from the table to the nearest whole minute only, *except* when *test sights* are taken. The offsets at intervals of one mile are inserted in the table; to obtain the length of offsets at the half-mile points, take one fourth of the offset corresponding to twice the distance of the half-mile point from the tangential point.

*Example.* Required the offset at  $5\frac{1}{2}$  miles, in latitude  $45^\circ 34.5'$ . The offset at 11 miles (interpolated for the given latitude) is 82.16 feet, which divided by 4 gives 20.54 feet, the offset required. The tables are extended to 12 miles, in order to provide necessary data; but the tangent will be limited to six miles.

**488. By Offsets from a "Secant."**—Instead of running the great circle so as to be tangent to the latitude arc it may be run so as to intersect it at given points, as, for example, at the beginning and end of the six-mile arc, or at the one-mile and the five-mile points. In this last case the line run out keeps nearer the latitude arc than in any of the other methods, so that the offsets are shorter.



The method consists in running a great circle for six miles (the width of a township), the starting-point and the original bearing being such that the line run will intersect the parallel at points one mile and five miles from the starting-point. For example, suppose it is desired to determine points on the  $45^\circ$  parallel, represented by A B Fig. 354<sup>1</sup>, B being six

miles from A. An arc of a great circle is run from C to F, cutting the parallel at D and E, D being one mile and E five miles from C. For convenience the line CF is called a "*secant*." The distance of the secant from the latitude arc at any point may be calculated by the methods employed in Art. 484.

The table \* (page 341) gives angles and offsets from a secant to a parallel of latitude.

The true bearing of the secant at each mile and half-mile point will be expressed by the tabular azimuth preceded by the initial meridional letter N, when the distance argument is found at the top of the table; but when this argument is found at the bottom of the table the meridional letter S will be placed before the azimuth; while the departure letter E or W will be made to agree with the direction of the survey, east or west, as the case may require.

The direction of the offsets from the secant to the parallel is indicated by the letter N or S following the offsets.

*Examples.* Standard parallel run west, latitude  $48^{\circ}$  N.; distance from initial point of secant 2 miles. The bearing is N.  $89^{\circ} 59'$  W., and the offset is 2.22 feet S. At  $5\frac{1}{2}$  miles the bearing is S.  $89^{\circ} 57'$  W., and the offset is 1.66 feet N.

The bearing is taken to the nearest minute.

The offsets for minutes of latitudes may be determined by interpolating by simple proportion.

**489. Length of Parallels.** The radius of any parallel of latitude equals the radius at the equator multiplied by the cos. latitude.

Then length in feet of  $1^{\circ} = \frac{\pi}{180} \cdot \text{radius in feet} \times \text{cos. latitude.}$

Then length in feet of  $1^{\circ} = \frac{\pi}{180} \times 20912405 \times \text{cos. latitude.}$

log. length in feet of  $1^{\circ} = \text{log. cos. latitude} + 5.5622814.$

*Example.* To find the length of a degree on the  $45^{\circ}$  parallel.

$$\text{log. cos. } 45 = 9.8494855.$$

$$\underline{5.5622814}$$

$$\text{log. } 258087 = 5.4117669.$$

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\* From "Instructions" issued by the General Land Office.



# A PARALLEL OF LATITUDE.

341

## AZIMUTHS OF THE SECANT, AND OFFSETS, IN FEET, TO THE PARALLEL.\*

Arguments; latitude in left-hand column and distance from starting-point at top or bottom of the table.

| Lat.                     | AZIMUTHS AND OFFSETS AT— |                        |                    |                        |                       |                        |                           | Deflection angle and nat. tan. to Rad. 66 ft. |
|--------------------------|--------------------------|------------------------|--------------------|------------------------|-----------------------|------------------------|---------------------------|-----------------------------------------------|
|                          | 0 miles.                 | $\frac{1}{2}$ mile.    | 1 mile.            | 1 $\frac{1}{2}$ miles. | 2 miles.              | 2 $\frac{1}{2}$ miles. | 3 miles.                  |                                               |
| 30°                      | 89° 58' 5"<br>1·98 N.    | 89° 58' 7"<br>0·87 N.  | 89° 59' 0"<br>0·00 | 89° 59' 2"<br>0·67 S.  | 89° 59' 5"<br>1·15 S. | 89° 59' 7"<br>1·44 S.  | 90° (E. or W.)<br>1·54 S. | 3' 00·2"<br>0·69 ins.                         |
| 31°                      | 89° 58' 4"<br>2·01 N.    | 89° 58' 6"<br>0·91 N.  | 89° 58' 9"<br>0·00 | 89° 59' 2"<br>0·70 S.  | 89° 59' 5"<br>1·20 S. | 89° 59' 7"<br>1·50 S.  | 90° (E. or W.)<br>1·60 S. | 3' 07·4"<br>0·72 ins.                         |
| 32°                      | 89° 58' 4"<br>2·09 N.    | 89° 58' 6"<br>0·94 N.  | 89° 58' 9"<br>0·00 | 89° 59' 2"<br>0·73 S.  | 89° 59' 5"<br>1·25 S. | 89° 59' 7"<br>1·56 S.  | 90° (E. or W.)<br>1·67 S. | 3' 15·0"<br>0·75 ins.                         |
| 33°                      | 89° 58' 3"<br>2·17 N.    | 89° 58' 5"<br>0·97 N.  | 89° 58' 8"<br>0·00 | 89° 59' 1"<br>0·76 S.  | 89° 59' 4"<br>1·30 S. | 89° 59' 7"<br>1·62 S.  | 90° (E. or W.)<br>1·73 S. | 3' 22·6"<br>0·78 ins.                         |
| 34°                      | 89° 58' 2"<br>2·25 N.    | 89° 58' 5"<br>1·01 N.  | 89° 58' 8"<br>0·00 | 89° 59' 1"<br>0·79 S.  | 89° 59' 4"<br>1·35 S. | 89° 59' 7"<br>1·69 S.  | 90° (E. or W.)<br>1·80 S. | 3' 30·4"<br>0·81 ins.                         |
| 35°                      | 89° 58' 2"<br>2·33 N.    | 89° 58' 5"<br>1·05 N.  | 89° 58' 8"<br>0·00 | 89° 59' 1"<br>0·82 S.  | 89° 59' 4"<br>1·40 S. | 89° 59' 7"<br>1·75 S.  | 90° (E. or W.)<br>1·87 S. | 3' 38·4"<br>0·84 ins.                         |
| 36°                      | 89° 58' 1"<br>2·42 N.    | 89° 58' 4"<br>1·09 N.  | 89° 58' 7"<br>0·00 | 89° 59' 0"<br>0·85 S.  | 89° 59' 4"<br>1·46 S. | 89° 59' 7"<br>1·82 S.  | 90° (E. or W.)<br>1·94 S. | 3' 46·4"<br>0·87 ins.                         |
| 37°                      | 89° 58' 0"<br>2·51 N.    | 89° 58' 3"<br>1·13 N.  | 89° 58' 6"<br>0·00 | 89° 58' 9"<br>0·88 S.  | 89° 59' 3"<br>1·51 S. | 89° 59' 7"<br>1·89 S.  | 90° (E. or W.)<br>2·01 S. | 3' 55·0"<br>0·90 ins.                         |
| 38°                      | 89° 58' 0"<br>2·61 N.    | 89° 58' 3"<br>1·17 N.  | 89° 58' 6"<br>0·00 | 89° 58' 9"<br>0·91 S.  | 89° 59' 3"<br>1·56 S. | 89° 59' 7"<br>1·95 S.  | 90° (E. or W.)<br>2·08 S. | 4' 03·6"<br>0·93 ins.                         |
| 39°                      | 89° 57' 9"<br>2·70 N.    | 89° 58' 2"<br>1·21 N.  | 89° 58' 6"<br>0·00 | 89° 58' 9"<br>0·94 S.  | 89° 59' 3"<br>1·62 S. | 89° 59' 7"<br>2·02 S.  | 90° (E. or W.)<br>2·16 S. | 4' 12·6"<br>0·97 ins.                         |
| 40°                      | 89° 57' 8"<br>2·79 N.    | 89° 58' 1"<br>1·25 N.  | 89° 58' 5"<br>0·00 | 89° 58' 9"<br>0·98 S.  | 89° 59' 3"<br>1·68 S. | 89° 59' 7"<br>2·10 S.  | 90° (E. or W.)<br>2·24 S. | 4' 21·6"<br>1·00 ins.                         |
| 41°                      | 89° 57' 7"<br>2·89 N.    | 89° 58' 0"<br>1·30 N.  | 89° 58' 4"<br>0·00 | 89° 58' 8"<br>1·02 S.  | 89° 59' 2"<br>1·74 S. | 89° 59' 6"<br>2·17 S.  | 90° (E. or W.)<br>2·32 S. | 4' 31·2"<br>1·04 ins.                         |
| 42°                      | 89° 57' 7"<br>3·00 N.    | 89° 58' 0"<br>1·35 N.  | 89° 58' 4"<br>0·00 | 89° 58' 8"<br>1·05 S.  | 89° 59' 2"<br>1·80 S. | 89° 59' 6"<br>2·25 S.  | 90° (E. or W.)<br>2·40 S. | 4' 40·8"<br>1·08 ins.                         |
| 43°                      | 89° 57' 6"<br>3·11 N.    | 89° 58' 0"<br>1·40 N.  | 89° 58' 4"<br>0·00 | 89° 58' 8"<br>1·08 S.  | 89° 59' 2"<br>1·86 S. | 89° 59' 6"<br>2·33 S.  | 90° (E. or W.)<br>2·48 S. | 4' 50·8"<br>1·12 ins.                         |
| 44°                      | 89° 57' 5"<br>3·22 N.    | 89° 57' 9"<br>1·45 N.  | 89° 58' 3"<br>0·00 | 89° 58' 7"<br>1·12 S.  | 89° 59' 2"<br>1·93 S. | 89° 59' 6"<br>2·41 S.  | 90° (E. or W.)<br>2·57 S. | 5' 01·0"<br>1·16 ins.                         |
| 45°                      | 89° 57' 4"<br>3·33 N.    | 89° 57' 8"<br>1·50 N.  | 89° 58' 3"<br>0·00 | 89° 58' 7"<br>1·16 S.  | 89° 59' 1"<br>2·00 S. | 89° 59' 5"<br>2·49 S.  | 90° (E. or W.)<br>2·66 S. | 5' 11·8"<br>1·20 ins.                         |
| 46°                      | 89° 57' 3"<br>3·44 N.    | 89° 57' 7"<br>1·55 N.  | 89° 58' 2"<br>0·00 | 89° 58' 6"<br>1·21 S.  | 89° 59' 1"<br>2·07 S. | 89° 59' 5"<br>2·59 S.  | 90° (E. or W.)<br>2·76 S. | 5' 22·8"<br>1·24 ins.                         |
| 47°                      | 89° 57' 2"<br>3·57 N.    | 89° 57' 6"<br>1·61 N.  | 89° 58' 1"<br>0·00 | 89° 58' 6"<br>1·25 S.  | 89° 59' 1"<br>2·14 S. | 89° 59' 5"<br>2·67 S.  | 90° (E. or W.)<br>2·86 S. | 5' 34·2"<br>1·28 ins.                         |
| 48°                      | 89° 57' 1"<br>3·70 N.    | 89° 57' 5"<br>1·66 N.  | 89° 58' 0"<br>0·00 | 89° 58' 5"<br>1·30 S.  | 89° 59' 0"<br>2·22 S. | 89° 59' 5"<br>2·78 S.  | 90° (E. or W.)<br>2·96 S. | 5' 46·2"<br>1·33 ins.                         |
| 49°                      | 89° 57' 0"<br>3·82 N.    | 89° 57' 5"<br>1·72 N.  | 89° 58' 0"<br>0·00 | 89° 58' 5"<br>1·34 S.  | 89° 59' 0"<br>2·30 S. | 89° 59' 5"<br>2·87 S.  | 90° (E. or W.)<br>3·06 S. | 5' 58·6"<br>1·38 ins.                         |
| 50°                      | 89° 56' 9"<br>3·96 N.    | 89° 57' 4"<br>1·78 N.  | 89° 57' 9"<br>0·00 | 89° 58' 4"<br>1·39 S.  | 89° 59' 0"<br>2·38 S. | 89° 59' 5"<br>2·97 S.  | 90° (E. or W.)<br>3·17 S. | 6' 11·4"<br>1·43 ins.                         |
| Lat.                     | 6 miles.                 | 5 $\frac{1}{2}$ miles. | 5 miles.           | 4 $\frac{1}{2}$ miles. | 4 miles.              | 3 $\frac{1}{2}$ miles. | 3 miles.                  | Deflection angle and nat. tan. to Rad. 66 ft. |
| AZIMUTHS AND OFFSETS AT— |                          |                        |                    |                        |                       |                        |                           |                                               |

\* From "Instructions" issued by the General Land Office.

*Conversely.* The angle, in minutes, subtended by *any* arc =  

$$\frac{\text{length of arc} \times 3437.7468}{\text{radius} \times \cos. \text{latitude}}.$$

log. angle in minutes = log. arc in feet - 3.7841301 - cos. latitude.

*Example.* Latitude 45° N. and distance 6 miles.

$$\begin{array}{r} \log. 31680 = 4.5007852 \\ \quad - 3.7841301 \\ \hline \quad \quad .7166551 \\ \text{co-log. cos. } 45^\circ = .1505150 \\ \log. 7' 21''.897 \quad \quad .8671701 \end{array}$$

**490.** The difference of lengths of any two parallels is called the convergence of the meridians between those parallels. This may be obtained more easily, since the distances between the meridians are as the cosines of the latitudes.

*Example.* Two "range-lines" (meridians) are 6 miles (480 chains) apart on the base-line of 46°.

Required their convergence at 47° north.

$$\text{Length at } 47^\circ = 480 \frac{\cos. 47^\circ}{\cos. 46^\circ} = 471.252.$$

$$480 - 471.252 = 8 \text{ chains } 74.8 \text{ links.}$$

## CHAPTER VIII.

### *RESURVEYS.*

**491. Introduction.** In making a resurvey of a piece of ground the problem usually presented is to make the description of a parcel of ground given in a deed or lot description agree with the boundaries of the same parcel indicated on the ground.

Where the original survey was properly made, and the monuments of the original survey remain, the problem is an easy one. But if, as is frequently the case, the original survey was inaccurate, and even erroneous, and all, or many, of the corners and line-marks spoken of in the deed have disappeared, the problem becomes very perplexing.

As a rule, in the older States the original farm surveys were not very carefully made, and few permanent monuments were set. Stakes driven in the ground were the usual corner and line marks, and these soon disappeared.

One of the principal difficulties in resurveying arises from the fact that many of the old surveyors did not understand the declination of the magnetic needle, and therefore either took no account of it or did not make the proper correction. If some of the original monuments remain, such errors can be at once detected and corrected, but if none of the original monuments remain the question of determining the proper bearings is a difficult one to solve.

In the newer States, where the original surveys were made by the United States Government on lines running north and south and east and west, the difficulties are not so great, but are still considerable. The proper direction of the lines is known, and more marks and monuments are to be found, but the inaccuracies of the

original work and the disappearance of corner-marks make the determination of section-lines and subdivisions anything but simple.

**492. Standards of Measurement.** Another source of trouble in resurveys arises from the fact that the instruments for measuring distances used by some of the old surveyors were inaccurate, and there were no Government standards of measurement. The first standard of length in the United States having any official sanction was the standard yard, legalized by the British Parliament in 1855, a copy of which was sent to the United States Office of Weights and Measures. The metric system of weights and measures was legalized by the United States Government in 1866. In 1875 seventeen governments, including that of the United States, united in forming an International Bureau of Weights and Measures, the object being to prepare and distribute standards of weights and measures.

The copies have been distributed, and the standard sets for the United States were unsealed in Washington Jan. 2, 1892. This gives us available standards in both systems. Any one can have his measuring-tape compared with the Government standard at Washington by applying to the Bureau of Weights and Measures and paying a small fee.

The United States Government has placed duplicates of the standards of weights and measures in all of the States, so that steps have been taken toward the proper distribution of the standards. One step further is needed. The standards should be so distributed as to be readily available for all. In every town of any considerable size, and in at least one town in every county, there should be a true meridian, plainly and permanently marked, as a standard for bearings or azimuths; and standards of measurements should be so placed that not only engineers and surveyors might test their measuring instruments, but that any one who needs to use a tape-line can test it and know whether it is correct or not.

In comparing a tape with the standard it should be tested under the same conditions in which it is to be used—that is, it should be supported at points the same distance apart, and under the same tension as it will be when in use. This will avoid the necessity of computing the corrections for sag, elongation from pull, etc. The

temperature at which the test is made should also be noted, so that the proper correction for temperature may be applied. Steel tapes expand from 0.000005 to 0.000007 of their length for every degree Fahr. of rise in temperature. On accurate measurement with a steel tape, see Chapter XV, Part II.

In making a resurvey where there is considerable uncertainty, as in the case of disputed boundaries, the surveyor has no official power to decide any disputed point. He can only act as an expert, and give an opinion as to what is the most probable solution of the difficulties in question. If the interested parties do not agree to accept his decision, the question must be settled in the courts.

Many of the questions which arise in such cases have been decided in the courts, and these decisions will guide the surveyor so far as they cover the points which may arise in his practice.

#### **SOME RULES OF LAW GOVERNING RESURVEYS.**

BY JUDGE HUGH J. CALDWELL.

493. In the older States it seems to have been the practice in making surveys to run the lines according to the magnetic meridian, and not according to the true meridian. Where, therefore, there was nothing in the deed or patent to control the call for courses and distances, the land was to be taken as bounded by the courses and distances of the deed or patent according to the magnetic meridian.

In 1796 Congress passed an act providing for the sale of the lands of the United States in the territory northwest of the river Ohio and above the mouth of the Kentucky River. What is known as the rectangular system of surveys was adopted. This system requires that the meridian lines shall be run on the true meridians.

Section 2395 of the Revised Statutes of the United States provides that "the public lands shall be divided by north, and south lines run according to the true meridian, and by others crossing them at right angles." Where this system was adopted there can be no presumption that the lines of a survey were run by the magnetic meridian.

***Where Description of Lands is Inconsistent or Uncertain.***

1. Parts of the description which are most certain prevail. Where there are two conflicting descriptions in a deed, or two conflicting parts of the same description, that which is more certain and stable, and the least likely to have been mistaken, or to have been inserted inadvertently, must prevail if it sufficiently identifies the land. This rule is particularly true where one of the descriptions or parts of the description is expressed in certain and definite terms, while the other is vaguely and uncertainly stated to be "about" a certain distance, or the like.

2. If both descriptions are equally stable and certain, that which is most favorable to the grantee is to be preferred.

3. Where a deed contains two descriptions, one particular and definite, showing the location and bounds of the land, and the other general in its terms, and they conflict, the former controls.

4. Where the particular description is in any degree obscure or uncertain, the general description may be resorted to for the purpose of establishing the identity of the premises, and items of the particular description which do not harmonize with the general description may be rejected.

Wherever the general description is clear, definite, and certain, the particular will not control it, especially where the latter is uncertain in some of its terms.

5. Where there is uncertainty the prime object is to arrive at the intention of the parties.

6. Where the general description refers to a deed or other instrument which gives the boundaries, then it becomes a particular description.

7. A description which sufficiently identifies the land, and is in accord with the obvious intention of the parties, will not be vitiated by the insertion of erroneous calls for monuments or other particulars which are repugnant to that description; such error will be rejected as "false demonstration," and what remains will pass the tract.

8. An exception too uncertain and indefinite to have any meaning may be dropped, and the previous description, complete in itself, allowed to stand.

9. No part of a description is to be rejected unless absolutely necessary to uphold the deed.

10. Where there are several particulars given in a conveyance, all of which are necessary to identify the premises, nothing will pass which does not satisfy every particular.

***Monuments, Courses, and Distances.***

1. Monuments, courses, and distances are only witnesses of the intention of the parties to the deed, and as such that which is most stable, certain, and least liable to be mistaken is to prevail when they do not agree. Monuments are fixed facts; they visibly indicate the extent of the land and the direction of the boundaries, while courses and distances are merely descriptive of the facts, based upon measurement, estimation, and calculation, and hence the value of each as a witness is in the order above named, and amount of land, which is purely calculation, is the most unreliable of all.

2. Monuments prevail over the plan or plat of the survey referred to in the deed.

3. Monuments established or marked on the ground and recognized for twenty-one years or more as designating the true boundary, will prevail over a description of the original laying out of the land contained in the original proprietor's records.

4. The existence of marked lines obviates a mistake in the plat, certificate of survey, and grant, in calling "west" "north," and the like.

5. A line which is marked part of the way, though not a right line from corner to corner, will control the boundary, and such boundary for the residue of the distance will be a direct line to the corner or point called for.

6. Where there are no express calls to fix the location of a line with certainty, evidence is admissible to show where the line was run, and it, when thus established, will control courses and distances laid down in the survey and deed.

7. Monuments subsequently erected by the parties to a conveyance by mutual consent, as being those called for therein, will control specifications of quantity and courses and distances.

8. There is a preference among monuments. Natural monu-

ments, such as rivers and the like, are generally of a more permanent and notorious character than artificial monuments. Hence, the rule that natural rather than artificial monuments called for in a deed will prevail where they conflict.

9. But where it is clear that the artificial monument is more reliable than the natural it will prevail.

10. Where the reason on which the above rules are based fails the rule fails, hence the true rule can be determined in many cases from the facts alone. And where the facts of the case make courses and distances more reliable than monuments then they prevail. The general rule is never to be adhered to when it would lead to an absurdity. Nor where it would defeat the grant. Nor where it would defeat the manifest intent of the parties.

11. Monuments called for as "supposed" to be, or "near," or about the intended line, are not definite enough to prevail over definite courses and distances.

12. If a monument called for in a deed is gone the surveyor can not establish himself a legal monument to take its place; this can be done only upon the agreement of the parties interested.

13. If no monuments are called for in the deed, or if the monuments called for are gone, then courses and distances control the survey and all the terms of description.

14. If the courses and distances can not be closed on the plot they do not wholly control, but in such a case resort may be had to the subordinate parts of the description.

15. In determining the location of a boundary, course prevails over distance where they do not harmonize. The same is true in restoring lost lines or corners.

16. The last rule does not prevail where by so doing the intent of the parties will not be carried out; but the very reverse may be the true rule if it best carries out the intent of the parties or obviates an absurdity.

17. Quantity is the least reliable, and is the last to be resorted to of all the descriptive particulars in a deed. But if there is a clear intent to give only a certain quantity it may control the other parts of the description.

18. A plot referred to in a deed becomes a part of it and con-



trols a line subsequently established in surveying another contiguous tract, and it may control courses and distances.

19. If a town lot is described by number, the town plot becomes a part of the conveyance.

The description by number of section makes the map and field notes of the public surveys a part of the description.

20. Where the numbers in a deed, as written, vary from the numerals, also used, the former control.

21. A line to be run between certain points is presumed to be a straight line, but may be deflected to take in a designated object.

22. Where the point at which a survey begins is lost, and the next corner and the course and distance between the two are known, the first point may be found by reversing the first course from the second point. This is the rule of law as to any lost point in a survey of premises.

23. If no monument is found at the point of intersection of two lines of a survey, such point of intersection will be presumed to be a corner.

24. If the description is a definite quantity out of a larger tract at some designated corner, then the same is to be laid off out of the designated corner in a square form, and if certain objects are included in the grant, then the survey of the part is to be as nearly in a square form as possible and include the designated objects.

#### ***Boundaries on Streams, Lakes, and other Waters.***

The decisions of the different States are so much at variance as to boundaries on waters that it is difficult to give here any general rules as a guide in resurveys. The only safe guide is for the surveyor to consult the law of the State where the survey is to be made.

1. Streams are classified as navigable and non-navigable. The courts differ as to what is a navigable stream. The rule most frequently adopted is, that it is a stream susceptible of navigation for purposes of commerce during some portions of the year.

2. Some States hold the bed of a navigable stream is vested in the State, while others hold it is vested in the adjoining proprietors, and when an adjoining proprietor conveys his land he is pre-

sumed to convey to the center of the stream unless he in terms limits it to the bank or high or low water, or in express terms reserves the bed of the stream from the grant. The same is true of flats lying between the land described and the stream upon which it abuts.

3. When a stream is not navigable, or if navigable the grantor owns the bed of it, the general rule is that all grants of land bordering upon it vest title in the grantee to the thread of the stream, unless an intent to limit it to some other line clearly appears from the deed.

4. The thread of the stream is the line running equidistant from the two banks at the ordinary stage of the water. It may or may not be the middle of the channel.

5. If the grantor owned to the center of the stream, and the deed gives boundaries, one of which extends into or along a stream, the conveyance extends to the center of the stream, though the stream be not named in the deed.

6. The purpose of meander-lines along or near the bank of streams is to designate the course of the stream and to aid in determining the amount of land. They are not to have the effect of restricting the boundary-line or to prevent it from extending to the thread of the stream.

7. It becomes important to know what language in a deed will be construed as an intent on the part of the grantor to reserve to himself the bed of the stream. Here courts differ to such an extent that but few general rules can be formulated. To almost any rule there are exceptions.

8. The fact that one or more of the courses in a deed extends to a monument on the bank or by the side of a stream is not sufficient to indicate an intent on the part of the grantor to limit the boundaries of his grant, nor to prevent their reaching the thread of the stream, where the boundary between the monuments is described as running with, by, along, or upon the stream.

9. Where the deed describes the boundary as running along the bank of a stream, the word "bank" restricts the boundary and does not permit it to reach the thread of the stream. The word "bank" is not construed to be the top of the rise of ground or the bottom

of it, but as the grantor in using it has not designated any part of it the deed is construed most strongly against him, and it is held to be low-water mark. So a line running to the waters of a stream runs to low-water mark.

10. Where a deed makes the shore a boundary-line, the courts vary so much as to what is conveyed that an attempt at a rule would only confuse. "Shore" is the land covered and uncovered by the ebb and flow of the ordinary tides. The term should never be used in describing lands abutting upon waters without tides. The improper use of the term has led to much of the diversity of holding as to its meaning. Some courts extend the conveyance to the thread of the stream, some to the low-water line, and others to the high-water line.

## CHAPTER IX.

### LEVELING.

#### INTRODUCTION.

**494. Leveling in General.** A *level surface* is one which is everywhere perpendicular to the direction of gravity, as indicated by a plumb-line, etc., and consequently parallel to the surface of standing water. It is, therefore, spherical (more precisely, spheroidal), but, for a small extent, may be considered as plane. Any line lying in it is a *level line*.

A *vertical line* is one which coincides with the direction of gravity.

The *height* of a point is its distance from a given level surface, measured perpendicularly to that surface, and therefore in a vertical line.

LEVELING is the art of determining the difference of the heights of two or more points.

To obtain a level surface or line, usually the latter, is the first thing required in leveling.

When this has been obtained, by any of the methods to be hereafter described, the desired height of a point may be determined *directly* or *indirectly*.

**Direct Leveling.** In this method of leveling, a level line is so directed and prolonged, either actually or visually, as to pass exactly over or under the point in question—i. e., so as to be in the same vertical plane with it—and the height (or depth) of the point above (or below) this level line is measured by a vertical rod, or by some similar means. The height of any other point being determined in

the same manner, the difference of the two will be the height of one of the points above the other. So on, for any number of points.

DIRECT LEVELING is the method most commonly employed. It will form Chapter IX.

**Indirect Leveling.** In this method of leveling the desired height is obtained by calculation from certain co-ordinate measured lines or angles, which fix the place of the point.

Thus, the horizontal distance from any point to a tree being known, and also the angle with the horizon made by a straight line passing from the point to the top of the tree, its height above the point can be readily calculated. This is the most simple and most usual form of this method.

Methods similar to those employed for determining the length of a line, one end or both ends of which are inaccessible, may be used in this method of leveling. See Chapter V, Obstacles in Angular Surveying.

In the problems which are there solved, the lines employed lie in a horizontal plane. By conceiving the plane of the lines to be vertical, many of the solutions will apply to the determination of vertical distances—that is, differences of level. This method of leveling is employed in determining the difference of level of the stations of a geodetic survey, where the stations are long distances apart and the horizontal distances between them are determined by the survey.

INDIRECT LEVELING will be developed in Chapter X, Part II.

**Barometric Leveling.** This determines the difference of the heights of two points by the difference of the weights of the portions of the atmosphere which are above each of them, as indicated by a barometer. An important advantage in this method of leveling is that the distances between stations do not need to be known in order to determine the differences of level. It is, therefore, available for explorations, reconnaissance, and preliminary work, which needs to be carried on before any accurate measurements of distances are made. It is explained in Chapter XI, Part II.

**Precise Leveling.** While, in general, the methods employed in Precise Leveling are the same as in ordinary Direct Leveling, the instruments used are capable of more accurate adjustment; and repetitions of observations are systematically arranged, so as to reduce the errors to the least possible amount. This is the method employed in geodetic surveying for determining in the most precise manner possible the difference of level of a series of stations extending over long distances, as from the ocean to the Great Lakes, or across the continent. It will be explained in Chapter XII, Part II.

#### DIRECT LEVELING.

#### GENERAL PRINCIPLES.

**495. Leveling Instruments.** The instruments employed to obtain a level line may be arranged in three classes, depending on these three principles :

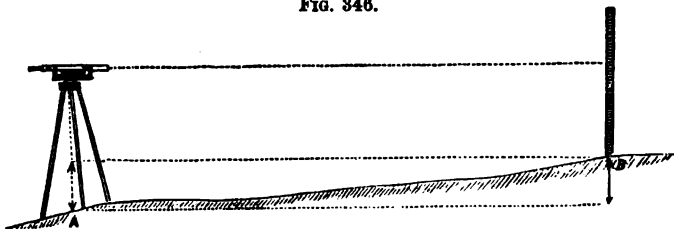
1. That a line perpendicular to a vertical line is a horizontal or level line.
2. That the surface of a liquid in repose is horizontal.
3. That a bubble of air, confined in a vessel otherwise full of a liquid, will rise to the highest point of that liquid.

They will be described in the following pages.

**496. Methods of Operation.** When a level line has been obtained, by any means, the difference of heights of any two points may be found by either of these two methods :

*First Method.* Set the leveling instrument over one of the

FIG. 346.



points, as A, in Fig. 346. Measure the height of the level line above the point. Then direct this line to a rod held on the other

point, and note the reading. The difference of the two measurements at A and B will be the difference of their heights.

*Second Method.* Let A and B, Fig. 347, represent the two

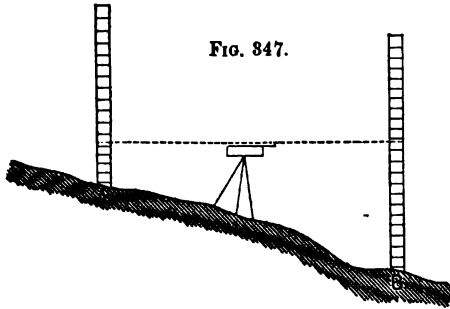


FIG. 347.

points. Set the instrument on any spot from which both the points can be seen, and at such a height that the level line will pass above the highest one. Sight to a rod held at A, and note the reading. Then turn the instrument toward B, and note the height

observed on the rod held at that point. The difference of the two readings will be the difference of the heights required. The *absolute* height of the level line itself is a matter of indifference.

**497. Curvature.** The level line given by an instrument is tangent to the surface of the earth. Therefore, the line of *true level* is always below the line of *apparent level*. In Fig. 348, A D represents the line of apparent level, and A B the line of true level. D B is the correction for the earth's curvature. By geometry we have :  $AD^2 = DB \times (DB + 2 BO)$ . But DB, being very small, compared with the diameter of the earth, may be dropped from the quantity in the parenthesis, and we have :

$$DB = \frac{AD^2}{2 BO};$$

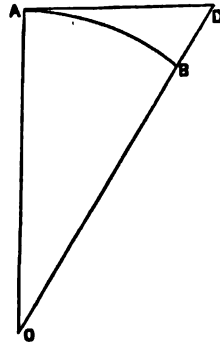
i. e., the correction equals the square of the distance divided by the diameter of the earth.

The difference of height for a distance of

$$1 \text{ mile} = \frac{1}{7916} = \frac{5280 \times 12}{7916} = 8 \text{ inches.}$$

This varies as the square of the distance. The effect, if neglected, is to make distant objects appear lower than they really are.

FIG. 348.



The effect is destroyed by setting the instrument midway between the two points.

**498. Refraction.** Rays of light coming through the air are curved downward. The effect is, to make objects look higher than they really are. Its amount is about one seventh that of curvature, and it operates in a contrary direction.

#### PERPENDICULAR LEVELS.

**499. Principle.** The principle upon which these are constructed is, that a line perpendicular to the direction of gravity is a level line.

**500. Plumb-line Levels.** The A level, Fig. 349, is so adjusted that, when the plumb-line coincides with the mark on the cross-piece, the feet of the level shall be at the same height. It is adjusted by reversion thus: Place its feet on any two points. Mark on the cross-bar the place of the plumb-line. Turn the instrument end for end, resting it on the same points, and mark the new place of the plumb-line. The point midway between the two is the right one.

FIG. 349.

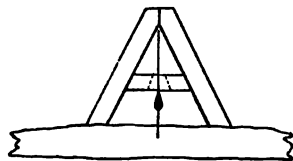
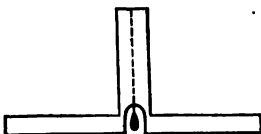


FIG. 350.

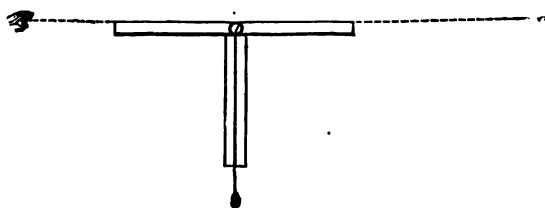


Another form is shown in Fig. 350.

The above forms are not convenient for prolonging a level line. To do this, invert the preceding form, as in Fig. 351.

To test and adjust this, sight to some distant point nearly on a level, and mark where the plumb-line comes to on the bottom of the

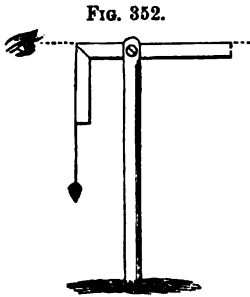
FIG. 351.



rod. Turn the instrument around and sight again, and note the place of the plumb-line. The midway point is the right one.



A modification of the last form is to fasten a common carpenter's square in a slit in the top of a staff, by means of a screw, and then tie a plumb-line at the angle so that it may hang beside one arm. When it has been brought to do so, by turning the square, then the other arm will be level.



**501. Reflecting Levels.** In these, the perpendicular to the direction of gravity is not an actual line, but an imaginary reflected line.

It depends on the optical principle that a ray of light which meets a reflecting plane at right angles is reflected back in the same line.

When the eye sees itself in a plane mirror, the imaginary line which passes from the eye to its image is perpendicular to the mirror. Therefore, if the mirror be vertical, the line will be horizontal. It may therefore be used like any other line of sight for determining points at the same height as itself.

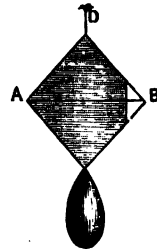
The first form, Fig. 353 (Colonel Burel's), consists of a rhomb of lead, of about two inches on a side, and one inch thick.

One side (the shaded part of the figure) is faced with a mirror. The right-hand corner of the rhomb is cut off, as seen in the figure, and a wire, A B, is stretched across the mirror.

To use this, hold up the instrument, with the mirror opposite the eye, by the string D, so that the eye seems bisected in the mirror by the wire A B. Then glance through the opening at B, and any point in the line of the eye and wire will be in the same horizontal plane with them.

The correctness of the instrument may be verified in the following manner : Hold up the instrument before any plane surface, as a wall, and determine the height of some point, as previously directed. Then, without changing the height of the instrument, turn it half around, place yourself between it and the wall, and

FIG. 353.



note the point of the wall which is seen in the mirror to coincide with the image of the eye.

If the two points on the wall coincide, the instrument is correct. If they do not, the mirror does not hang plumb, and the point midway between the two is the true one.

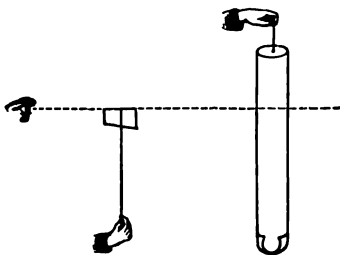
The instrument is rectified, or made to hang plumb, by means of the pear-shaped piece of lead seen attached to the lower corner of the rhomb.

The second form consists of a hollow brass cylinder, with an opening at the upper end, as seen in Fig. 354. At the opening is a small mirror, whose vertical plane makes an angle with the vertical plane of section by which the cylinder was cut in forming the aperture. The edge of the mirror is marked thus (x) in the first half of Fig. 354.

The mirror is made to hang plumb by means of a one-sided weight within the cylinder.

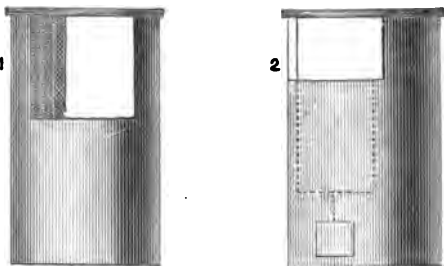
This is used by setting it on a stake driven into the ground, or by holding it in the hand, making the lower edge of the opening answer the same purpose as the wire in the other case.

Fig. 355.



To use this, hold it up by the thread with one hand, and with the other hand hold a card between the eye and instrument, using

Fig. 354.



The same methods of verification and rectification are used as with the first form of the instrument.

The instrument, in its third form, is simply a small steel cylinder, 4" or 5" long, and  $\frac{1}{4}$ " in diameter, highly polished, and suspended from the center of one end by a fine thread.

the upper edge of the card, as seen reflected in the mirror, the same as the wire in the first form.

This instrument is the invention of M. Cousinery.

### WATER-LEVELS.

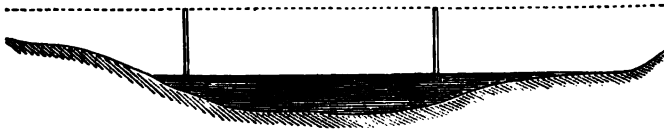
**502. Continuous Water-Levels.** These may consist of a channel connecting the two points, and filled with water; or of a tube, usually flexible, with the ends turned up, and extending from one point to the other.

By measuring up or down, from the surface of the water at each end, the relative heights of the two points may be determined.

**503. Visual Water-Levels.** The simplest one is a short surface of water prolonged by sights at equal distances above it, as in Fig. 356.

A portable form is a tube bent up at each end, and nearly filled

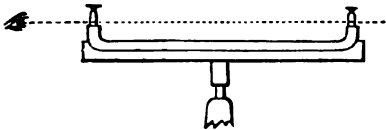
FIG. 356.



with water. The surface of the water in one end will always be at the same height as that in the other, however the position of the

tube may vary. It may be easily constructed with a tube of tin, lead, copper, etc., by bending up, at right angles, an inch or two of each end, and supporting the tube, if

FIG. 357.



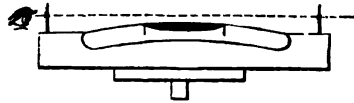
too flexible, on a wooden bar. In these ends, cement (with putty, twine dipped in white-lead, etc.) thin vials, with their bottoms broken off, so as to leave a free communication between them. Fill the tube and the vials, nearly to their top, with colored water. Blue vitriol or cochineal may be used for coloring it. Cork their mouths, and fit the instrument, by a steady but flexible joint, to a tripod.

To use it, set it in the desired spot, place the tube by eye nearly level, remove the corks, and the surfaces of the water in the two vials will come to the same level. Stand about a yard behind the nearest vial, and let one eye, the other being closed, glance along the right-hand side of one vial, and the left-hand side of the other. Raise or lower the head till the two surfaces seem to coincide, and this line of sight, prolonged, will give the level line desired. Sights of equal height, floating on the water, and rising above the tops of the vials, would give a better-defined line.

#### AIR-BUBBLE OR SPIRIT LEVELS.

**504.** The "*spirit-level*" consists essentially of a curved glass tube nearly filled with alcohol, but with a bubble of air left within, which always seeks the highest spot in the tube, and will therefore, by its movements, indicate any change in the position of the tube. Whenever the bubble, by raising or lowering one end, has been brought to stand between two marks on the tube, or, in case of expansion or contraction, to extend an equal distance on either side of them, the bottom of the block (if the tube be in one), or sights at each end of the tube, previously properly adjusted, will be on the same level line. It may be placed on a board fixed to the top of a staff or tripod.

FIG. 358.



When, instead of the sights, a telescope is made parallel to the level, and various contrivances to increase its delicacy and accuracy are added, the instrument becomes the engineer's spirit-level.

The upper surface of the tube is usually the arc of a circle, and, when we speak of lines parallel to a "level," we mean parallel to the tangent of this arc at its highest point, as indicated by the middle of the bubble.

**505. Sensibility.** This is estimated by the distance which the bubble moves for any change of inclination. It is directly proportional to the radius of curvature of the tube. To determine the radius, proceed thus :



half-way back to the middle by this means, and the other half by raising or lowering one end of the block, because the reversion has doubled the error.

Repeat this, if necessary.

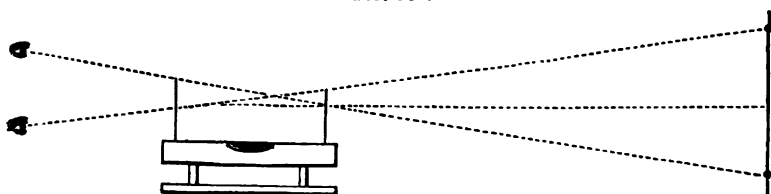
**Circular Level.** The upper surface of this is spherical. It will therefore indicate a level in *every* direction, instead of only one, as does the preceding. It is adjusted like the last one, but in two directions, at right angles to each other.

FIG. 361.



**507. Level with Sights.** The line of sight is made parallel to the tangent of the level. It may be tested thus :

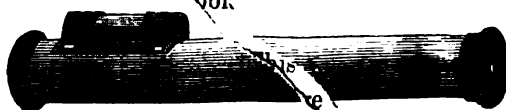
FIG. 362.



Bring the bubble to the center of the tube and make a mark, in the line of sight, as far off as can be seen. Then turn the level end for end, and sight again. If the bubble remains in the same place, "all right." If not, rectify it by altering the sights, or by altering the marks for the bubble to come to, bringing the bubble half-way back, and trying it again.

**508. Hand-Reflected Level.** This consists of a brass tube, about six inches long, and one inch in diameter. To the inside of the

FIG. 363.

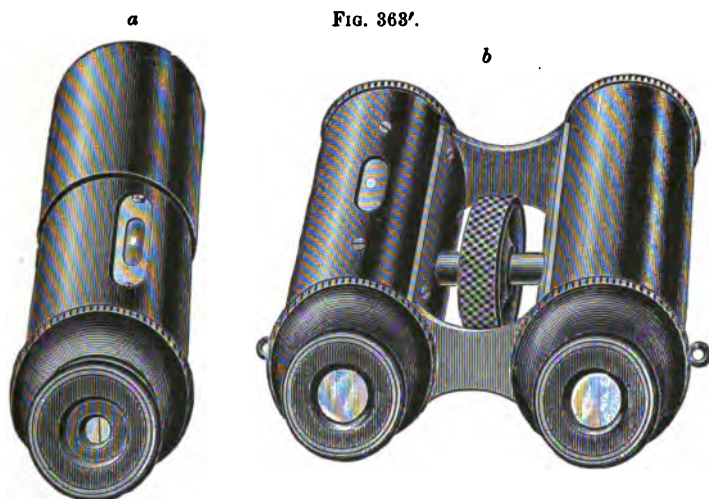


upper portion of the tube is attached a small level. A small mirror is placed at an angle in the lower side of the tube, so that it will reflect the point to which the bubble must come, in order to have the instrument level, to the eye.

A small hole at one end, and a horizontal cross-hair at the other, give the desired level line. It is used by holding it in the hand.

Fig. 363 is an approved form, made by Young, of Philadelphia. The improvement consists in the patent "Locke sight," which enables the near cross-hair to be distinctly seen at the same time as the distant object.

**509. Gurley's Telescopic Hand-Level** (Fig. 363', *a*). "This consists of a tube to which are fitted the lenses of a single opera-



glass, and containing in addition thereto a reflecting prism, cross-wire, and small spirit-level, the last being shown in the open part of the tube.

"The eye-lens, as indicated in the cut, is made of two separate pieces, the larger one being the usual concave eye-lens of the opera-glass, the smaller one a segment of a plano-convex lens having its focus in a cross-wire under the level-vial and above the reflecting prism.

"The observer holds the tube horizontal, with the level opening uppermost, and with the same eye sees the object toward which the instrument is directed, and observes the position of the bubble. When the level is truly horizontal, the cross-wire will

bisect the bubble, and will also determine the level of any object seen through the telescope.

“In the binocular form of this level (Fig. 363', *b*) the tube on the right incloses the usual lenses of the opera-glass, while that on the left contains only the prism, level-vial, and cross-wire. The binocular hand-level gives a clearer view of an object than is possible with a single tube, there being no light lost by the interference of the prism and level-vial.”

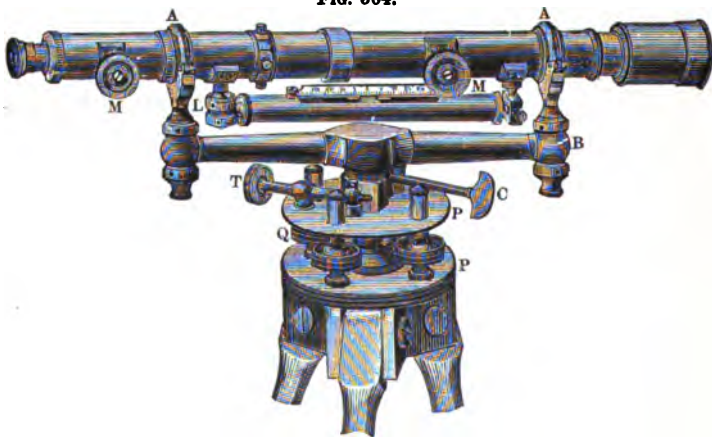
**510. The Telescope-Level.** In this the line of collimation of the telescope corresponds to the sights of Fig. 362, and is made parallel to the level—i. e., this line is so adjusted as to be horizontal when the bubble of its level is in the center.

There are many different forms of the telescope-level, of which the most important ones will now be given.

**511. The Y-Level.** This is so named from the shape of the supports of the telescope. It is the variety most used by American engineers.

Fig. 364 represents a Y-level of the usual form. The telescope is held in the wyes by the clips, A A, which are fastened to the

FIG. 364.

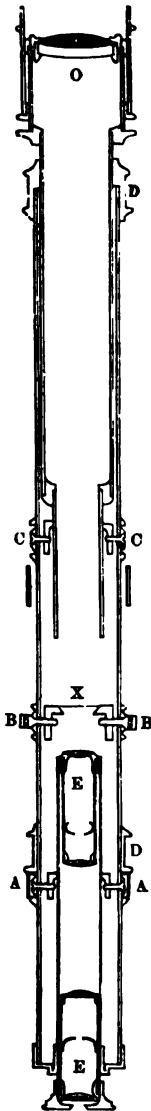


wyes by tapering pins, so that the telescope can be clamped in any position. The milled-headed screws at M and M are used to move



the object-glass and eye-piece in and out, so as to adjust them for long and short sights, and for short-sighted and long-sighted persons.

FIG. 365.



L is a spirit-level ; P and P are parallel plates ; C is the clamp-screw, which fastens the spindle on which the level-bar, B, which supports the wyes, turns ; T is the tangent-screw, by which the telescope may be slowly turned around horizontally.

**512. The Telescope.** The arrangement of the parts of the telescope is shown in Fig. 365. O is the object-glass, by which an image of any object, toward which the telescope may be directed, is formed within the tube. E E is the eye-piece—a combination of lenses, so arranged as to magnify the small image formed by the object-glass. The cross-hairs are at X. They are moved by means of the screws shown at B B. A A are screws used for centering the eye-piece. C C are screws used for centering the object-glass. At D D are rings, or collars, of exactly the same diameter, turned very truly, by which the telescope revolves in the wyes.

The telescope shown in the figure forms the image erect. Other combinations of lenses are used, some of which invert the image ; but the one here shown is generally preferred.

**513. The Cross-Hairs.** These are made of very fine platinum wire or of spider-threads. They are attached to a short, thick tube, placed within the telescope-tube, through which pass loosely four screws whose threads enter and take hold of the cross-hair ring, as shown in Fig. 366.

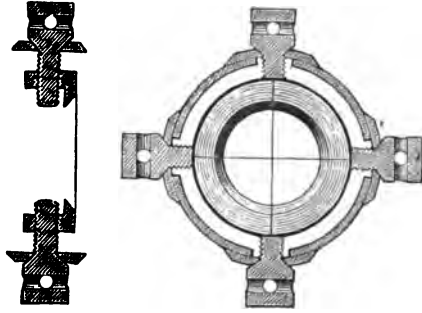
In some instruments, one of each pair of opposite screws is replaced by a spring ; and the screws, instead

of being capstan-headed, and moved by an "adjusting-pin," have square heads, and are moved by a "key," like a watch-key.

The line of collimation (or *line of aim*) is the imaginary line passing through the intersection of the cross-hairs and the optical center of the object-glass.

The image formed by the object-glass should coincide precisely with the cross-hairs. When this is not the case, there will be an apparent movement of the cross-hairs, about the objects sighted to, on moving the eye of the observer. This is called *instrumental parallax*. To correct it, move the eye-piece out or in, till the cross-hairs are sharply defined against any white object. Then move the object-glass in or out, till the object is also distinctly seen. The image is now formed where the cross-hairs are, and no movement of the eye will cause any apparent motion of the cross-hairs.

FIG. 366.

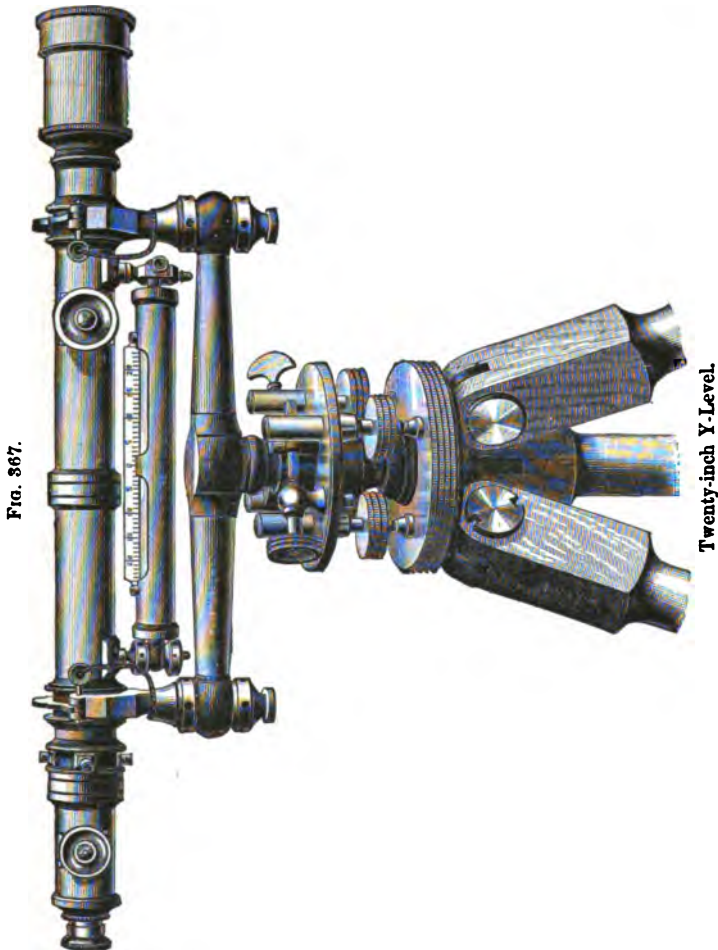


**514. The Level.** This consists of a thick glass tube, slightly curved upward, and so nearly filled with alcohol that only a small bubble of air remains in the tube. This always rises to the highest part. The brass case, in which this is inclosed, is attached to the under side of the telescope, and is furnished with the means of moving, at one end vertically, and at the other horizontally. Over the aperture, in the case, through which the bubble-vial is seen, is a graduated level-scale, numbered each way from zero at the center.

**515. Supports.** The wyes in which the telescope rests are supported by the level-bar, B, and fastened to it by two nuts at each end (one above, one below the bar), which may be moved with an adjusting-pin. The use of these nuts will be explained under "Adjustments." Attached to the center of the level-bar is a steel

spindle, made so as to turn smoothly and firmly in a hollow cylinder of bell-metal ; this, again, is fitted to the main socket of the upper parallel plate.

**516. Parallel Plates.** It is by the aid of these that the instrument is leveled. The plates are united by a ball-and-socket joint,



and are held apart by the four plate-screws, Q Q Q Q, which pass through the upper one, and press against the lower one.

To level the instrument, turn the telescope till it is brought over a pair of opposite parallel plate-screws. Then turn the pair of screws, to which the telescope has been made parallel, equally in opposite directions, screwing one in and the other out, till the bubble is brought to the center. Then turn the telescope so as to bring it over the other pair of opposite screws, and bring the bubble to the center, as before.

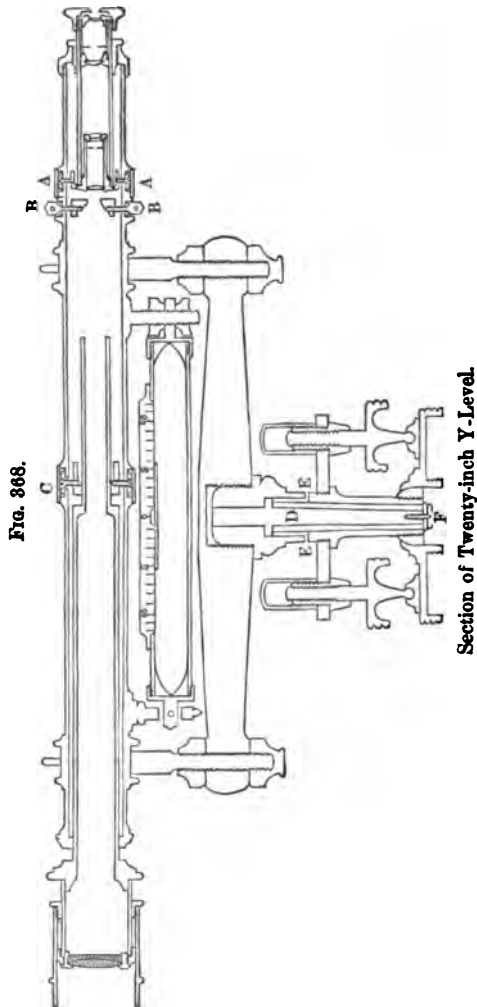
Repeat the operation, as moving one pair of screws may affect the other.

Sometimes one of each pair of opposite screws is replaced by a strong spring, and in some instruments only three screws are used.

The lower plate is screwed on to the tripod-head.

517. Fig. 367 is a twenty-inch Y-level, and Fig. 368 is a longitudinal section of it, showing its construction.

In Fig. 368, B B are the screws attached to the cross-hair ring. At A are four screws holding a ring through which the inner end of the eye-piece passes. At C are four screws holding a ring, through which the inner



end of the object-glass slide passes. The use of these sets of screws will be explained under "Adjustments."

The interior spindle, D, which supports the instrument, and on which it turns, is made of steel, and is carefully fitted to the interior of a hollow socket of bell-metal, which has its exterior surface fitted to the main socket, E, of the tripod-head. The hollow bell-metal socket is held in place by a washer and screw, shown at F.

A screw, passing through the main socket, E, enters a groove in the exterior of the bell-metal socket, and fastens the instrument to the tripod-head.

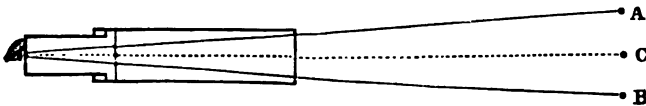
### ADJUSTMENTS.

**518.** The line of collimation of the telescope should be horizontal when the bubble is in the center of the tube ; which will be the case when this line is parallel to the plane of the level. But both this line and this plane are imaginary, and can not be compared together directly. They are therefore compared indirectly. The line of collimation is made parallel to the bottom of the collars, and the plane of the level is then made parallel to them.

**519. First Adjustment.** *To make the line of collimation parallel to the bottoms of the collars.*

Sight to some well-defined point, as far off as it can be dis-

FIG. 369.



tinctly seen. Then revolve the telescope half around in its supports—i. e., turn it upside down. If the line of collimation was not in the imaginary axis of the rings, or collars, on which the telescope rests, it will now no longer bisect the object sighted to. Thus, if the horizontal hair was too high, as in Fig. 369, this line of collimation would point at first to A, and, after being turned over, it would point to B. The error is doubled by the reversion, and it should point to C, midway between A and B. Make it do

so, by unscrewing the upper capstan-headed screw, and screwing in the lower one, till the horizontal hair is brought half-way back to the point B. Remember that, in an erecting telescope, the cross-hairs are reversed, and *vice versa*. Bring it the rest of the way by means of the parallel plate-screws. Then revolve it in the wyes back to its original position, and see if the intersection of the cross-hairs now bisects the point, as it should. If not, again revolve, and repeat the operation till it is perfected. If the vertical hair passes to the right or to the left of the point when the telescope is turned half around; it must be adjusted in the same manner by the other pair of cross-hair screws. One of these adjustments may disturb the other, and they should be repeated alternately. When they are perfected, the intersection of the cross-hairs, when once fixed on a point, will not move from it when the telescope is revolved in its supports. This double operation is called *adjusting the line of collimation*.

It has now been brought into the center line, or axis, of the collars, and is therefore parallel to their bottoms, or the points on which they rest, if they are of equal diameters. We have to assume this as having been effected by the maker.

In making this adjustment, the level should be clamped, but need not be leveled.

**520. Second Adjustment.** *To make the bottoms of the collars parallel to the plane of the level—i. e., to insure their being horizontal when the bubble is in the center.*

Clamp the instrument, and bring the bubble to the center by the parallel plate-screws. Take the telescope out of the wyes, and turn it end for end. If the bubble returns to the center, "all right." If not, rectify it, by bringing the bubble half-way back, by means of the nuts which are above and below one end of the bubble-tube, and which work on a screw. Bring it the rest of the way by the plate-screws, and again turn end for end. Repeat the operation, if necessary.

If, in revolving the telescope (as in the first adjustment), the bubble runs toward either end, it must be adjusted sidewise, by means of two screws which press horizontally against the other end

of the bubble-tube. This part of the adjustment may derange the preceding part, which must, therefore, be tried again.

**521. Third Adjustment.** *To cause the bubble to remain in the center of the tube when the telescope is turned around horizontally.*

To verify this, bring the bubble to the center of the tube, and then turn the telescope half-way around horizontally. If the bubble does not remain in the center, adjust it by bringing it half-way back by means of the nuts at the end of the level-bar. Test it by bringing it the rest of the way back by the parallel plate-screws, and again turning half-way around.

The cause of the difficulty is, that the plane of the level is not perpendicular to the axis about which it turns, and that this axis is not vertical. The above operations correct both these faults.

This adjustment is mainly for convenience, and not for accuracy, except in a very small degree.

Some instruments have no means of making the third adjustment. They must be treated thus :

Use the screws at the end of the bubble-tube, to cause the bubble to remain in the center when the level is turned around horizontally. Then make the line of collimation parallel to the level by raising or lowering the cross-hairs.

**522.** When levels are provided with the means of centering the eye-piece and object-glass, these operations should precede the first three which we have just explained.

*Centering the Object-Glass.* After adjusting the line of collimation for a distant object (as explained in the "First Adjustment") move out the slide, which carries the object-glass, until a point ten or fifteen feet distant can be distinctly seen. Then turn the telescope half over, as before, and see if the intersection of the cross-hairs bisects the point. If not, bring it half-way back by the screws C C, Fig. 365, moving only one pair of screws at a time. Repeat the operation for a distant point, and then again for a near one, if necessary. We have now adjusted the line of collimation for long and short sights, and may assume it to be in adjustment for intermediate ones, since the bearings of the slides are supposed to be true, and their planes parallel to each other.

*Centering the Eye-Piece.* This is to enable the observer to see the intersection of the cross-hairs precisely in the center of the field of view of the eye-piece. It is adjusted by means of four screws, two of which are shown at A A.

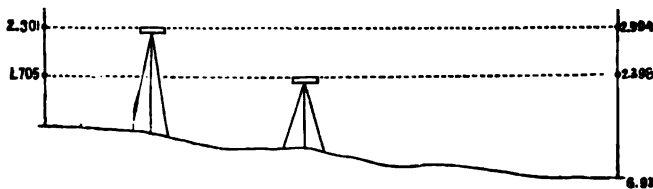
These operations are performed by the maker so permanently as to need no further attention from the engineer, and the heads of the screws, by which these adjustments are made, are covered by a thin ring which protects them from disturbance.

**523.** Adjustment by setting between two points, or the "*Peg-Method.*" Drive two pegs several hundred feet apart, and set the instrument midway between them. Level, and sight to the rod held on each peg. The difference of the readings will be the true difference of the heights of the pegs, no matter how much the level may be out of adjustment.

Then set the level over one peg, and sight to the rod at the other. Measure the height of the cross-hairs above the first peg. The difference of this and the reading on the rod *should* equal the difference of the heights of the two points, as previously determined. If it does not, set the target to the sum or difference of the height of the cross-hairs above the first peg, and the true difference of height of the points, according as the first point is higher or lower than the second, and hold the rod on the second point. Sight to it, and raise or lower one end of the bubble-tube until the horizontal cross-hair *does* bisect the target when the bubble is in the center. Then perform the "third adjustment."

Instead of setting *over* one peg, it is generally more convenient

FIG. 370.



to set near to it, and sight to a rod held on it, and use this reading instead of the measured height of the cross-hairs.



N. B.—This verification should *always* be used for every level, even after the three usual adjustments have been made ; for it is independent of the equality of the collars.

In running a long line of levels, let the last sight at night be taken midway between the last two “turning-point” pegs, and in the morning try their difference by setting close to the last one. This tests the level every day with very little extra labor.

**524. Egault's Level.** In this level the bubble-tube is not connected with the telescope. It is used thus :

Level and sight as usual. Then turn the telescope upside down, end for end, and half-way around horizontally, and sight again. Half the sum of the two readings is the correct one, no matter how much the instrument is out of adjustment (assuming the collars to

be of equal size) ; for the errors then cancel each other. This is the one used principally in France.

The rod used with it is marked with numbers only half the real heights above its bottom. Then

the *sum* of the readings is the true one. Thus the rod itself takes the mean of the readings.

FIG. 371.

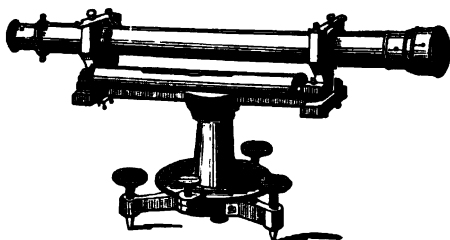
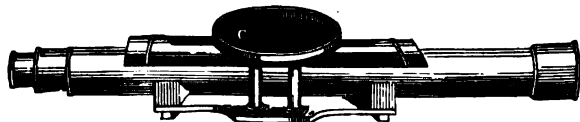


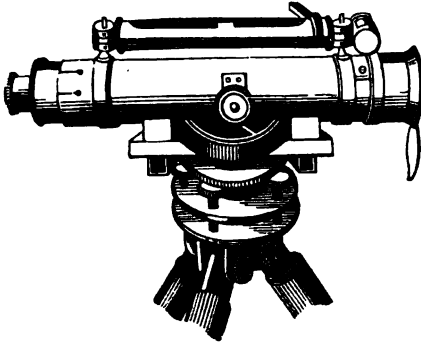
FIG. 372.



**525. Troughton's Level.** In this the bubble-tube is permanently fastened in the top of the telescope-tube. It is adjusted by the “peg method,” or some similar one, the cross-hair being moved up or down until the observation gives the true difference of height of the pegs when the bubble is in the center. Then make the “third adjustment,” by means of the screws under the telescope.

**526. Gravatt's Level, or the "Dumpy Level."** This level has a very large telescope tube and object glass, thus giving more light.

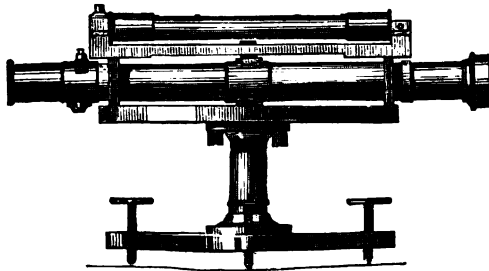
FIG. 373.



The bubble tube is on top of the telescope, and the bubble can be seen by the observer in a small inclined mirror. There is also a cross level, shown at the right-hand end of the longitudinal bubble tube, which enables the instrument to be leveled without turning the telescope through a quarter revolution

several times to make sure that the instrument is properly leveled. Although originally made without Ys, as shown in the figure, it is now also made with Ys.

FIG. 374.



**527. Lenoir's Level.** In this the telescope carries, at each end, a steel block, whose upper and lower faces are made perfectly parallel. They

are placed on a brass circle, which is made level by reversing a level placed upon the upper surface of the steel blocks.

**528. Tripods.** These consist of three legs, shod with iron, and connected by joints at the top. The most common form is given in Fig. 367. Other forms are given in Art. 176. Lightness and stiffness are the desired qualities.

In Gurley's *extension tripod*, Fig. 374', an adjustable piece is held in any desired position by two clamp screws, shown on the legs. The figure shows each of the three legs of different lengths.

"Quick-leveling" tripod-heads, for quickly setting the leveling-

plates nearly level, are made of various patterns. Gurley's attachment for this purpose is given below. The arrangement of this attachment will be readily understood by inspection of the cut.

To use the quick-leveling attachment, screw the instrument on the tripod as usual; if not nearly level, unscrew the leveling-head a very little—a bare loosening of the screw is sufficient. The instrument will then be free to move upon the spherical surfaces, A, B, C, in any direction required to bring the plates approximately level, and will be held in this position by the friction of the same surfaces.

Now screw the head fast again, firmly clamping the whole instrument to the tripod. The final adjustment of the levels is then completed by the use of the leveling screws.

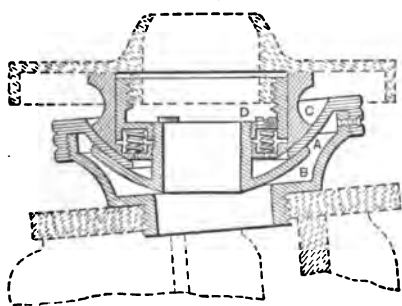
The friction of the spherical surfaces may be increased or diminished at will, by turning the screws (D) which compress the spiral-springs.

The cut shows the Quick-Leveling Attachment as screwed fast to a tripod of any pattern now in use.

FIG. 374'.



FIG. 374''.



**529. Rods.** These should be made of light, well-seasoned wood. To detect whether the rod leans to or from the instrument, its front may be angular or curved. If angular, when held leaning toward the instrument, the lines of

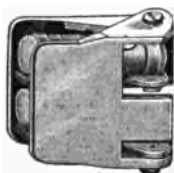
division will appear as in Fig. 375. When leaning from the instrument, they will appear as in Fig. 376. They are usually divided to feet, tenths, and hundredths.

A rod level, made by Gurley, for plumbing the rod, is shown in Fig. 376'. On the left the level is shown folded for carrying, and on the right, attached to the rod.

FIG. 376'.

FIG. 375.

FIG. 376.



**530. Target.** This is a plate of iron or brass, attached to the rod in such a way that it may be moved up and down the rod and clamped in any position. Some of the many varieties of marking are given in Figs. 377-385.

FIG. 377.



FIG. 378.



FIG. 379.



FIG. 380.

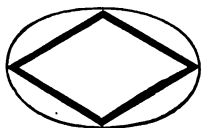


FIG. 381.

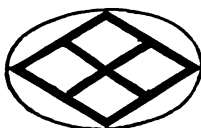


FIG. 382.

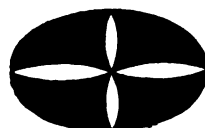


FIG. 383.



FIG. 384.

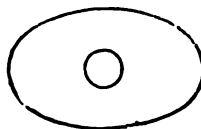
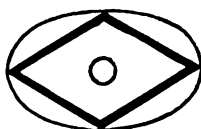


FIG. 385.



Those represented in Figs. 377, 378, and 379 are bad, because the cross-hair may be above or below the middle of the target by its full thickness, as magnified by the eye-piece of the telescope without the error being perceptible. The next three, Figs. 380,

381, and 382, depend upon the nicety with which the eye can determine if a line bisects an angle. Fig. 383 depends upon the accuracy with which the eye can bisect a space. Fig. 384 depends upon the accuracy with which the eye can bisect a circle. Figs. 381, 382, and 385 are the best forms for use. Red and white are the best colors.

**531. Vernier.** The target carries a vernier, by which smaller spaces may be measured than those into which the rod is divided. It may be placed on the side of an aperture, in the face of the target, through which the divisions on the rod can be seen, or carried on the back or side of the rod by the target-clamp.

**532. The New York Rod (Fig. 386).** This is usually in two pieces, sliding one upon the other, and connected by a tongue. It is graduated to tenths and hundredths of a foot, and can be read to thousandths by the vernier. Up to six feet and a

FIG. 386.



FIG. 387.



FIG. 388.



half the target is used as on other rods. For greater heights, the target is fixed at six and a half feet, and the back part of the rod, which carries the target, is shoved up (Fig. 386) until the target is bisected by the cross-hairs. Its height is then read off on the side of the rod, on which the numbers run downward, and on

FIG. 389.



which is a second vernier, which gives the precise reading. It is convenient for its portability, but apt to be too tight or too loose, as the weather is moist or dry. Sometimes it is in three pieces, as in Fig. 387.

**533. The Boston Rod (Fig. 388).** This is usually in two parts, like the New York rod. The target is rectangular, and is fastened to one of the pieces near its extremity. For heights less than six feet, the rod is held with the target-end down, and the target is moved up by sliding up the piece which carries it. For heights above six feet, the rod is turned end for end, bringing the target-end up, and then sliding up the piece which carries the target.

**534. The Philadelphia Rod (Fig. 389).** This is in two parts, held together by brass clamps, and is furnished with a *target*. It is graduated and painted so as to be used as a "speaking-rod," or with a target. When the target is used, the vernier on the target is read for height up to seven feet. For greater heights, the target is clamped at seven feet, and the part to which the target is clamped is slid up, and the vernier on the upper clamp is used.

**535. Speaking-Rods.** These are rods which are read without targets, the divisions and subdivisions being great painted on the face of the rod. They produce great saving of time and increase of accuracy.

In one form (Fig. 390) the face of the rod is divided into tenths of feet, and smaller divisions estimated.

In Bourdaloue's rod the divisions are each four centimetres

(1·6 inch), and are numbered at half their value. He arranges them as in Fig. 391.

*Gravatt's Rod* (Fig. 392). This is divided to 0·01 foot. The upper hundredth of each tenth extends across the rod. Each half-tenth is marked by a dot; each half-foot by two dots. Every other tenth is numbered, and the numbers are each 0·1 high. It is in three parts, which slide into each other like a telescope.

*Barlow's Rod* (Fig. 393). In this the divisions are marked by triangles, each 0·02 foot high, so that it

FIG. 390.



FIG. 391.



FIG. 392.

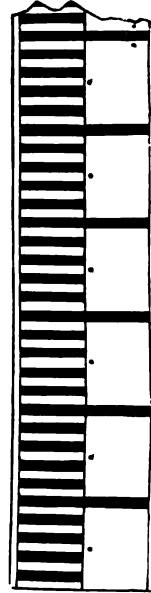


FIG. 393.

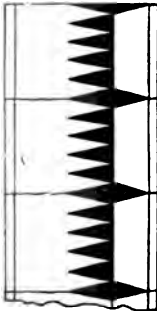
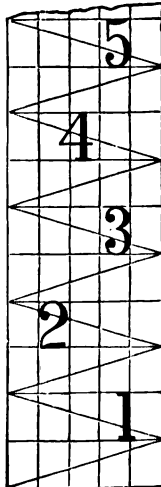


FIG. 394.



reads to hundredths, and less by estimation. This is based on the power the eye has in bisecting angles.

*Stephenson's Rod* (Fig. 394). This is based upon the principle of the diagonal scale. Each tenth is bisected by a horizontal line, and the diagonals enable the observer to read to hundredths.

*Conybeare's Rod* (Fig. 395). It reads to hundredths of a foot by means of the cross-hair bisecting the tops and bottoms and angles of hexagons. The

odd tenths are made white and the even ones black. The figures are placed so that their centers are opposite the divisions they refer to.

FIG. 395.

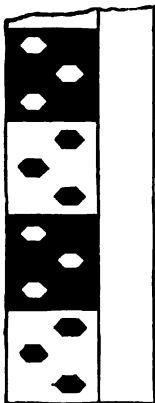
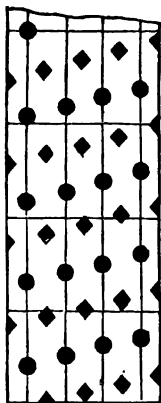


FIG. 396.



### *Pemberton's Rod* (Fig. 396).

This is on the principle of nine verniers placed side by side. It reads to hundredths, which are given by counting up from the dot which the hair bisects, to the dot in the same vertical line which is bisected by one of the horizontal lines which mark the tenths. The inventor claims that it can be read nine times as far as Gravatt's.

On all speaking-rods, to avoid confounding numbers, such as 3 and 8, they may be marked thus :

1 . 2 . III . 4 . V . 6 . 7 . 8 . IX . X . 11 . XII.

The French, who go by tenths, use the following :

1 . 2 . T . 4 . V , 6 . 7 . 8 . N . X.

The figures are sometimes placed with their tops on a level with the tops of the dimensions they mark—e. g., feet ; and sometimes with their middles on the dividing line.

### THE PRACTICE.

**536. Field Routine ;** or, how to start and go on :

1. The rodman holds the rod on the starting-point, which may be a peg, a door-sill, or other "bench-mark." He stands square behind his rod, and holds it as nearly vertical as possible.

2. The leveler sets up the instrument, somewhere in the direction in which he is going, but not necessarily, or usually, in the precise line. He then levels the instrument by the parallel plate-screws, sights to the rod, and notes the reading, whether of target or speaking-rod, as a "back-sight" (B. S.), or + (plus) sight ; entering it in the proper column of one of the tabular forms of field-book, given in the following articles.



3. The rodman is then sent ahead about as far as he was behind, and he there drives a "level-peg" nearly to the surface of the ground, or finds a hard, well-defined point, and holds the rod upon it.

4. The leveler then again sights to the rod, and notes the reading as a "fore-sight" (F. S.), or — (minus) sight. The difference of the two readings is the difference of the heights of the points.

5. He then takes up the instrument, goes beyond the rod, any convenient distance, sets up again, and proceeds as in paragraph 2; and so on for any number of points, which will form a series of pairs. The successive observations of each pair give their difference of heights, and the combination of all these gives the difference of heights of the first and last points of the series.

6. If the vertical cross-hair be strictly vertical, it will determine whether the rod leans to the right or left. To know whether the cross-hair is vertical or not, try whether it coincides with a plumb-line, or sight to some fixed point, turn the telescope from side to side horizontally, and see if the horizontal cross-hair continues to cover the spot. If it does not, turn the telescope around in the wyes till it does; then it is truly horizontal, and the other hair, being perpendicular to it, is truly vertical. To know whether the rod leans forward or backward, have the rodman move it from and to himself. If the line bisected by the cross-hair descends in both motions, the rod was vertical; if the line rises, the rod was leaning. The lowest reading is the true one.

7. When a target is used, signals are made by the leveler with the hand, "up" and "down," to indicate in which direction to move the target. Drawing the hand to the side signifies "stop," and both hands brought together above the head signifies "all right." The rodman should move the target fast at first, and slowly after having passed the right point. When signaled "all right," he should clamp the target and show again. Then call out the reading before moving, and show it to the leveler, as either passes the other.

8. We have thus far supposed that only the difference of heights of the two extreme points is desired. But when a section or profile of the ground is required, the rod must be held and observed, at

each change of slope of the ground, or at regular distances; usually, for railroad-work, at every hundred feet, and also at any change of slope between those points.

Any number of points, within sight, may have their relative heights determined at one setting of the level.

The names back-sight (B. S.) and fore-sight (F. S.) do not necessarily mean sights taken looking forward or backward (though they are generally so for turning-points), but the first sight taken, after setting up the instrument, is a B. S. or + (plus) sight, and all following ones, taken before removing the instrument, are F. S.'s, or - (minus) sights. The full meaning of this will appear in considering the forms of field-book.

All but the first and last points sighted to are called *intermediate points*, or "*intermediates*." The last point sighted to before moving the instrument is called a *turning-point*, or *changing-point*.

The first and last sights, taken at any one setting of the instrument, require the greatest possible accuracy. The intermediate points may be taken only to the nearest tenth, or hundredth at most; because any error in them will not affect the final result, but only the height of that single point at which it was taken.

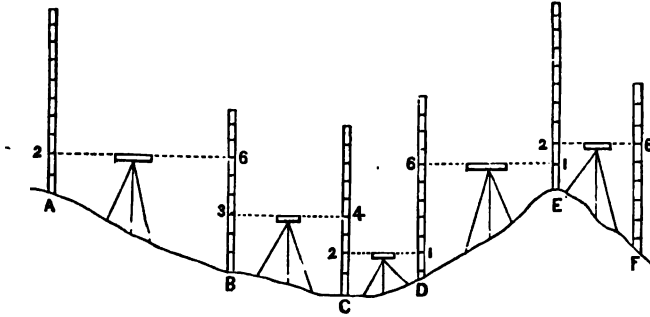
Two rodmen are often used to save the time of the leveler. Then it is well to use a target-rod for the "turning-points," which are often distant and need most precision, and a speaking-rod for the intermediate points. Where one rod is used, the rodman should keep notes of the readings at the turning-points.

**537. Field-Notes.** The beginner may sketch the heights and distances measured, in a profile or side view, as in Fig. 397. But when the observations are numerous, they should be placed in one of the tabular forms given on the following pages.

**538. First Form of Field-Book.** In this, the names of the points or "stations," whose heights are demanded, are placed in the first column, and their heights, as finally ascertained, in reference to the first point, in the last column. The heights above the starting-point are marked +, and those below it are marked -. The back-

sight to any station is placed on the line below the point to which it refers. When a back-sight exceeds a fore-sight, their difference

FIG. 397.



is placed in the column of "Rise"; when it is less, their difference is a "Fall." The following table represents the same observations as the last figure, and their careful comparison will explain any obscurities in either :

| STATIONS. | DISTANCES. | BACK-SIGHTS. | FORE-SIGHTS. | RISE. | FALL. | TOTAL HEIGHTS. |
|-----------|------------|--------------|--------------|-------|-------|----------------|
| A         |            |              |              |       |       | 0·00           |
| B         | 100        | 2·00         | 6·00         |       | —4·00 | —4·00          |
| C         | 60         | 3·00         | 4·00         |       | —1·00 | —5·00          |
| D         | 40         | 2·00         | 1·00         | +1·00 |       | —4·00          |
| E         | 70         | 6·00         | 1·00         | +5·00 |       | +1·00          |
| F         | 50         | 2·00         | 6·00         |       | —4·00 | —3·00          |
|           |            | 15·00        | 18·00        |       | —3·00 |                |

The above table shows that B is 4 feet below A ; that C is 5 feet below A ; that E is 1 foot above A ; and so on. To test the calculations, add up the back-sights and fore-sights. The difference of the sums should equal the last "total height."

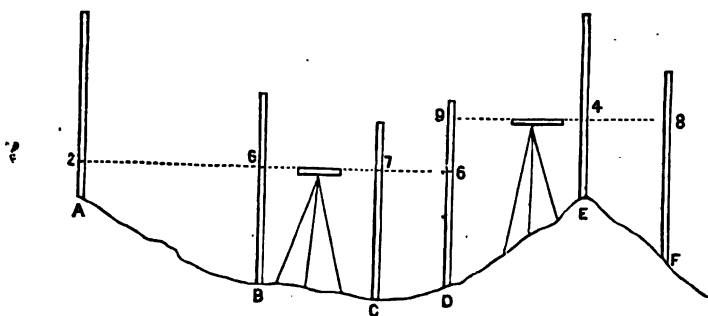
An objection to this form is that the back-sights come on the line *below* the station to which they are taken, which is embarrassing to a beginner.

When "intermediate" observations are taken, the "fore-sights" taken to these intermediate points are put down in their proper column, and are also set down in the column of "back-sights"; so that, when the two columns are added up, any error in

these intermediate sights (which are usually not taken very accurately) will be canceled, and will not affect the final result. The effect is the same as if, after the fore-sight to the intermediate point had been taken, the instrument had been taken up and set down again at precisely the same height as before, and a back-sight had then been taken to the same point. Hence, in this form, the "turning-points" are those stations which have different back-sights and fore-sights, while those which have them the same are "intermediates."

The following figure and table represent the same ground as the

FIG. 398.



preceding one, but with only two settings of the instrument. D is the turning-point :

| STATIONS. | DISTANCES. | BACK-SIGHTS. + | FORE-SIGHTS. — | RISE. | FALL. | TOTAL HEIGHTS. |
|-----------|------------|----------------|----------------|-------|-------|----------------|
| A         |            |                |                |       |       | 0·00           |
| B         |            | 2·00           | 6·00           |       | 4·00  | —4·00          |
| C         |            | 6·00           | 7·00           |       | 1·00  | —5·00          |
| D         |            | 7·00           | 6·00           | 1·00  |       | —4·00          |
| E         |            | 9·00           | 4·00           | 5·00  |       | +1·00          |
| F         |            | 4·00           | 8·00           |       | 4·00  | —3·00          |
|           |            | +28·00         | —81·00         |       | 3 00  |                |

In leveling for "sections," the distances between the points leveled must be recorded. They are usually put down after the stations *to* which they are measured ; although in surveying with the compass, etc., they are put down after the stations *from* which they are measured. In the following notes, which contain inter-

mediate stations, they are put down *before* the stations *to* which they are measured. It should be remembered that these distances are measured between the points at which the rod is held, and have no reference to the points at which the instrument is set up :

| DISTANCES. | STATIONS. | BACK-SIGHTS. + | FORE-SIGHTS. — | RISE. | FALL.   | TOTAL HEIGHTS. |
|------------|-----------|----------------|----------------|-------|---------|----------------|
|            | 260       |                |                |       |         | 91·397         |
| 100        | 261       | 4·576          | 3·726          | 0·850 |         | 92·247         |
| 100        | 262       | 5·420          | 4·500          | 0·920 |         | 93·167         |
| 100        | 263       | 4·500          | 3·170          | 1·330 |         | 94·497         |
| 40         | 263·40    | 4·910          | 4·988          |       | 0·028   | 94·469         |
| 60         | 264       | 4·938          | 6·886          |       | 1·448   | 93·021         |
| 100        | 265       | 3·880          | 4·640          |       | 1·260   | 91·761         |
| 100        | 266       | 4·640          | 5·400          |       | 0·760   | 91·001         |
| 70         | 266·70    | 2·760          | 3·070          |       | 0·310   | 90·691         |
| 30         | 267       | 3·070          | 3·750          |       | 0·680   | 90·011         |
| 100        | 268       | 6·750          | 5·925          |       | 3·175   | 86·836         |
|            |           | 41·944         | 46·505         |       | —4·561  |                |
|            |           |                | 41·944         |       | +91·397 |                |
|            |           |                | —4·561         |       | 86·836  |                |

**539. Second Form of Field-Book.** This is presented below. It refers to the same stations and levels noted in the first table, and shown in Fig. 397 :

| STATIONS. | DISTANCES. | BACK-SIGHTS. | HEIGHT OF INSTRUMENT ABOVE DATUM. | FORE-SIGHTS. | TOTAL HEIGHTS. |
|-----------|------------|--------------|-----------------------------------|--------------|----------------|
| A         |            |              |                                   |              | 0·00           |
| B         | 100        | 2·00         | +2·00                             | 6·00         | —4·00          |
| C         | 60         | 3·00         | —1·00                             | 4·00         | —5·00          |
| D         | 40         | 2·00         | —3·00                             | 1·00         | —4·00          |
| E         | 70         | 6·00         | +2·00                             | 1·00         | +1·00          |
| F         | 50         | 2·00         | +3·00                             | 6·00         | —3·00          |
|           |            | 15·00        |                                   | 18·00        | —3·00          |

In the preceding form it will be seen that a new column is introduced, containing the height of the instrument—i. e., of its line of sight—not above the ground where it stands, but above the *Datum*, or starting-point, of the levels. The former columns of “rise” and “fall” are omitted. The preceding notes are taken thus : The height of the starting-point, or “datum,” at A, is 0·00. The instrument being set up and leveled, the rod is held at A.

The back-sight upon it is 2·00 ; therefore the height of the instrument is also 2·00. The rod is next held at B. The fore-sight to it is 6·00. That point is therefore 6·00 below the instrument, or  $2\cdot00 - 6\cdot00 = -4\cdot00$  below the datum. The instrument is now moved, and again set up, and the back-sight to B, being 3·00, the height of the instrument is  $-4\cdot00 + 3\cdot00 = -1\cdot00$ , and so on ; the height of the instrument being always obtained by adding the back-sight to the height of the peg on which the rod is held, and the height of the next peg being obtained by subtracting the fore-sight to the rod held on that peg, from the height of the instrument.

This form is better than the first form, in leveling for a section of the ground to make a profile ; or when several observations are to be made at one setting of the level ; or when points of desired heights are to be established, as in "leveling-location."

This form may be modified by putting the back-sights on the same line with the stations to which they are taken. This avoids the defect of the first form, but introduces the new defect of writing them down after the number which they precede, in a back-handed way, which may be a source of error.

This modification is shown in the following table, which corresponds to Fig. 398. In the column of fore-sights, the "turning-points" (T. P.), and "intermediate points" (Int.), are put in separate columns ; so that, to prove the work, the difference of the sum of the back-sights and of the sum of the turning-point fore-sights, is the number which should equal the difference of the heights of the first and last points :

| STATIONS. | DISTANCES. | BACK-SIGHTS. + | HEIGHT OF INSTRUMENT. | FORE-SIGHTS. — |      | TOTAL HEIGHTS. |
|-----------|------------|----------------|-----------------------|----------------|------|----------------|
|           |            |                |                       | T. P.          | INT. |                |
| A         |            | 2·00           |                       |                |      | 0·00           |
| B         |            |                | +2·00                 |                | 6·00 | -4·00          |
| C         |            |                |                       |                | 7·00 | -5·00          |
| D         |            | 9·00           |                       | 6·00           |      | -4·00          |
| E         |            |                | +5·00                 |                | 4·00 | +1·00          |
| F         |            |                |                       | 8·00           |      | -3·00          |
|           |            |                |                       | -14·00         |      |                |
|           |            |                |                       | +11·00         |      |                |
|           |            | +11·00         |                       | -3 00          |      |                |

When a line is divided up into stations of 100 feet each, as on railroad-work, the number of the station indicates its distance from the starting-point. When an observation is taken at a point between these hundred-foot stations, it is noted as a decimal, thus: Station 4·60 is 460 feet from the starting-point. In the field-notes of such work, the column of distances may be omitted. The turning-points and intermediate stations of the foresights may be placed in the same column. In the following table the column of stations indicates the distances of the stations from the starting-point, and the foresights are placed in one column. The heights and distances are the same as in the last table in Article 538. This form of field-book is much used.

| STATIONS. | BACK-SIGHTS. | HEIGHT OF INSTRUMENT. | FORE-SIGHTS. | TOTAL HEIGHTS. |
|-----------|--------------|-----------------------|--------------|----------------|
| 260       | 4·576        | 95·973                |              | 91·397         |
| 261       | 5·420        | 97·667                | 3·726        | 92·247         |
| 262       |              |                       | 4·500        | 93·167         |
| 263       | 4·910        | 99·407                | 3·170        | 94·497         |
| 263·40    |              |                       | 4·038        | 94·469         |
| 264       | 3·380        | 96·401                | 6·386        | 93·021         |
| 265       |              |                       | 4·640        | 91·761         |
| 266       | 2·760        | 93·761                | 5·400        | 91·001         |
| 266·70    |              |                       | 3·070        | 90·691         |
| 267       |              |                       | 3·750        | 90·011         |
| 268       |              |                       | 6·925        | 86·836         |

**540. Third Form of Field-Book.** In this the back-sights are placed directly under the height of the station to which they are taken, which lessens the chance of making mistakes in adding to get the height of instrument. The height of instrument is distinguished by being included between two horizontal lines. The following table refers to the same ground as the preceding one :

| STATIONS. | FORE-SIGHTS. | HEIGHTS.        | REMARKS. |
|-----------|--------------|-----------------|----------|
| 260       |              | 91·397<br>4·576 |          |
|           |              | 95·973          |          |
| 261       | 3·726        | 92·247<br>5·420 |          |
|           |              | 97·667          |          |
| 262       | 4·500        | 93·167          |          |
| 263       | 3·170        | 94·497<br>4·910 |          |
|           |              | 99·407          |          |
| + 40      | 4·938        | 94·469          |          |
| 264       | 6·886        | 93·021<br>3·380 |          |
|           |              | 96·401          |          |
| 265       | 4·640        | 91·761          |          |
| 266       | 5·400        | 91·001<br>2·760 |          |
|           |              | 93·761          |          |
| + 70      | 3·070        | 90·691          |          |
| 267       | 3·750        | 90·011          |          |
| 268       | 6·925        | 86·836          |          |

**541. Best Length of Sight.** There are two classes of inaccuracies. With very long sights, the errors of imperfect adjustment and curvature are greatest; the former varying as the length, and the latter as the square of the length. With very short sights, and therefore more numerous, the errors of inaccurate sighting at the target are greatest. The best usual mean is from 200 feet to 300 feet, or more if equal distances for back-sights and fore-sights to turning-points can be obtained.

**542. Equal Distances of Sight.** They are always very desirable. They are most easily determined, when no stakes have been previously set, by "stadia" cross-hairs in the telescope of the level.

**543. Datum-Level.** This is the plane of reference, from which, above it or below it, usually the former, the heights of all points of the line are reckoned.



It may be taken as the height of the starting-point. If the line descends, it is better to call the starting-point 10 feet or 100 feet above some imaginary plane, so that points below the starting-point may not have minus-signs.

It is desirable to refer all levels in a country to some one datum. This is usually the surface of the sea, and, for general purposes, *mean tide* is best. *Low-water* mark should be the datum when the levelings are connected with harbor-surveys, whose soundings always refer to low water. *High-water* mark should be used when the levelings relate to the drainage of a country.

**544. Bench-Marks (B. M.).** These are permanent objects, natural or artificial, whose heights above the datum are determined and recorded for future reference.

Good objects are these: Pointed tops of rocks, tops of mile-stones, stone door-sills, tops of gate-posts or hinges, and generally any object not easily disturbed, and easily described and found.

A knob made on the spreading root of a tree is good. A nail may be driven in it, and the tree "blazed" and marked, as in Fig. 399. A stake will do till frost.

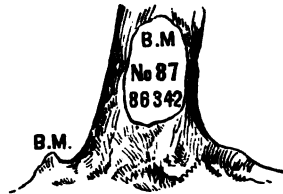
Bench-marks should be made near the starting-point of a line of levels; near where the line crosses a road; on each side of a river crossed by it; at the top and bottom of any high hill passed over; and *always* at every half-mile or mile.

The precise location and description of every bench-mark should be noted very fully and precisely, and in such a way that an entire stranger could find it, with the aid of the notes.

**545. Check-Levels, or Test-Levels.** No *single* set of levels is to be trusted; but they must be tested by another set, run between the bench-marks (B. M.'s), though not necessarily over the same ground.

A set of levels will verify themselves if they come around to the starting-point again.

FIG. 399.



**546. Limits of Precision.** Errors and inaccuracies should be carefully distinguished. For the latter, every leveler must make a standard for himself, so as to be able, in testing his work, to distinguish any *real error* from his *usual inaccuracy*.

The result of four sets of levelings, in France, of from 45 to 140 miles, averaged a difference of  $\frac{1}{10}$  foot in 43 miles, and the greatest error was  $\frac{1}{2}$  foot in 56 miles.

A French leveler, M. Bourdaloue, contracted to level the benchmarks of a railroad survey to within 0.002 foot per mile, or  $\frac{1}{10}$  foot per 50 miles.

In Scotland, the difference of two sets of levels of 26 miles was 0.02 foot.

**547. Trial-Levels, or Flying-Levels.** Their object is to get a general approximate idea of the comparative heights of a portion of the country, as a guide in choosing lines to be leveled more accurately. More rapidity is required, and less precision is necessary. The distances may be measured at the same time by stadia-hairs.

**548. Leveling for Sections.** The object of this is to measure all the ascents and descents of the line, and the distances between the points at which the slope changes ; so that a section or profile of it can be made from the observations taken.

The line of a railroad is usually set out by a party with compass or transit, who drive at every hundred feet a large stake with the number of the station on it, and beside it a small level-peg, even with the surface of the ground. On this the rod is held for the observations. The level-peg is set in "line," and the large stake a foot or two to one side.

**549. Profiles.** A profile is a section of ground by a vertical plane or cylindrical surface,\* passing through the line along which a profile is desired. It represents to any desired scale the heights and distances of the various points of a line, its ascents and descents, as seen in a side view. It is made thus : Any point on the

---

\* A cylindrical surface is here understood to mean that formed by a line moving parallel to itself along any line, instead of only a circle, as in elementary geometry.

paper being assumed for the first station, a horizontal line is drawn through it; the distance to the next station is measured along it, to the required scale; at the termination of this distance a vertical line is drawn; and the given height of the second station above or below the first is set off on this vertical line. The point thus fixed determines the second station, and a line joining it to the first station represents the slope of the ground between the two. The process is repeated for the next station, etc.

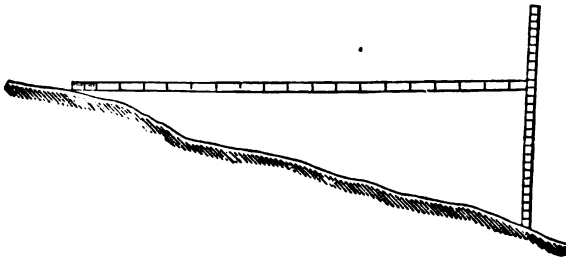
But the rises and falls of a line are always very small in proportion to the distances passed over, even mountains being merely as the roughnesses of the rind of an orange. If the distances and the heights were represented on a profile to the same scale, the latter would be hardly visible. To make them more apparent, it is usual to "exaggerate the vertical scale" tenfold, or more—i. e., to make the representation of a foot of height ten times as great as that of a foot of length, as in Fig. 397, in which one inch represents one hundred feet for the distances, and ten feet for the heights.

In practice, engraved profile-paper is generally used, which is ruled in squares or rectangles, to which any arbitrary values may be assigned.

When the line leveled over is not straight, the profile, whose length is that of the line straightened out, will extend beyond the "plan" when both are on the same sheet.

**550. Cross-Levels.** These show the heights of the ground on a line at right angles to the main line. They give "cross-sections"

FIG 400.



of it. In the note-book they are put on the right-hand page. They may be taken at the same time with the other levels, or inde-

pendently. In taking cross-levels where the slopes are quite steep, as in mountain districts, frequent settings of the instrument are necessary.

A much more rapid method is by the use of "cross-section rods." These are two rods, one of which is about ten or twelve feet long, provided with a bubble-tube near each end, so as to be held level, and graduated to feet, tenths, and hundredths. The other is simply a graduated rod. The manner of using them is shown in Fig. 400.

A slope-level is sometimes used. (See "Angular Surveying.")

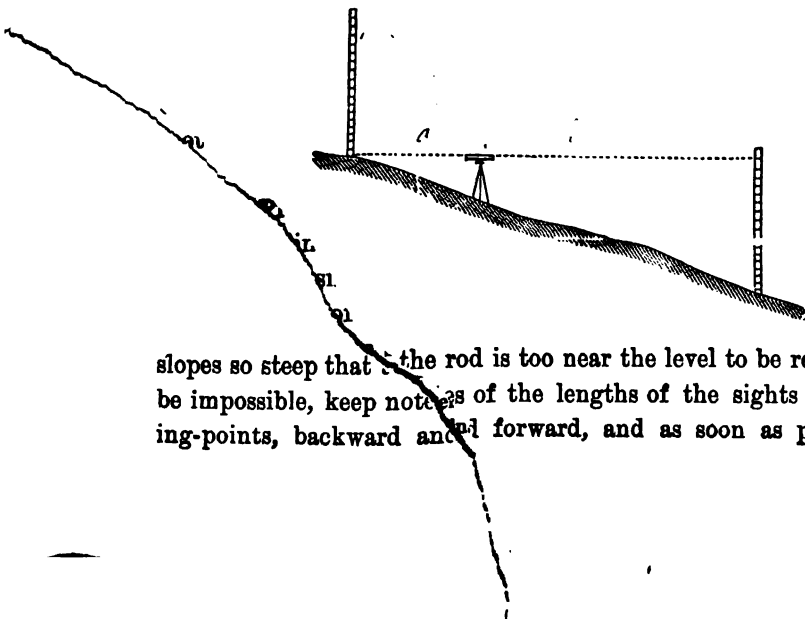
### DIFFICULTIES.

**551. Steep Slopes.** In descending or ascending a hill, the instrument and the rod should be so placed that the sight should strike as near as possible to the bottom of the rod on the up-hill side, and the top of the rod on the down-hill side.

Try this by leveling over two screws, setting the instrument so that one pair of opposite plate-screws shall point in the direction of the line, but do not be too particular; it is a waste of time.

Doing this produces sights of unequal length. The rod being about three times as high as the instrument, the down-hill sights will be about double the length of the up-hill ones, as shown in Fig. 401. Then set to one side of the line. This is necessary on

FIG. 401.



slopes so steep that the rod is too near the level to be read. If this be impossible, keep notes of the lengths of the sights to the turning-points, backward and forward, and as soon as possible take

$$\frac{a}{1} = \frac{1}{3}$$

$$a + b = c$$

# DIFFICULTIES.

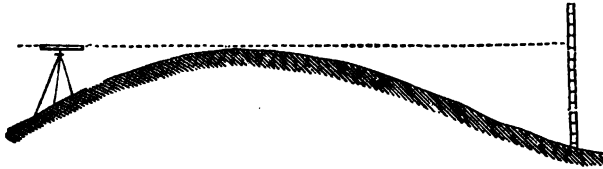
393

sights unequal in the contrary direction till the differences of lengths balance the former ones. When approaching a long ascent or descent, make these compensations in advance.

In leveling over a line of stakes already set, as on a railroad, at every 100 feet, if the line of sight strikes not quite up to one, drive a peg as high as you can see it, and make it a turning-point, noting it "peg" in the field-book.

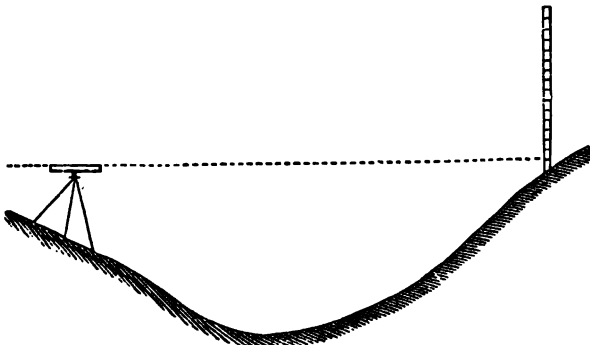
In leveling across a hill or hollow, instead of setting the instru-

FIG. 402.



ment on the top of the hill or bottom of the hollow, time will be saved by the method represented in Figs. 402 and 403.

FIG. 403.



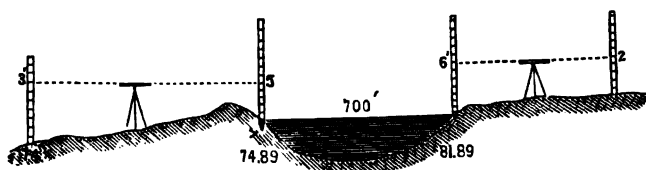
**552.** *When the rod is a little too low, raise it alongside of a stake, or the body, and put the top of the rod "right"; then measure down from the bottom of the rod, and add it to its length.*

**553.** *When the rod is a little too high, so that the line of sight strikes the peg below the bottom of the rod, measure down from the top of the peg, and put down the sight with a contrary sign to what it would have had—i. e., if a back-sight make it minus, and if a fore-sight make it plus.*

**554. When the rod is too near.** When no figure is visible, raise the rod slowly till a figure comes in sight. If too near to read, and there is no target, use a field-book as target. If the instrument is exactly over the peg, measure up to the height of the cross-hairs, as given by the side-screws.

**555. WATER. A.—A pond too wide to be sighted across.** Drive a peg to the level of the water, on the first side, and observe its height, as an F. S. Then drive a peg on the other side of the pond, also to the surface of the water. Hold the rod on it. Set

FIG. 404.



up the level beyond it, and sight to it as a B. S., and put down the observation as if it had been taken to the first peg.

| FORE-SIGHTS. | STATIONS. | HEIGHTS. | BACK-SIGHTS. | Σ     |
|--------------|-----------|----------|--------------|-------|
| 5.0          | 74        | 50.00    | 3.00         | 53.00 |
|              | 74.89 }   | 48.00    |              |       |
|              | 81.89 }   |          | 6.00         | 54.00 |

There must be no wind in the direction of the line of level.

**B.—For leveling across a running stream.** Set the two pegs in a line at right angles to the current, although the line to be leveled may cross it obliquely.

If a profile or section of the ground under the water be required, find the height of the surface, and measure the depths below this at a sufficient number of points, measuring the distances also, and put these depths down as fore-sights.

**556. A Swamp, or Marsh.** This can not be treated like a pond, for the water may seem nearly stagnant while its surface has considerable slope, its flow being retarded by vegetation. If only slightly "shaky," have an observer at each end of the level. If

more so, push the legs down as far as they will go, and let both observers lie down on their sides. If still more "shaky," drive three stakes or piles, to support the legs of the tripod, and stand the tripod on them.

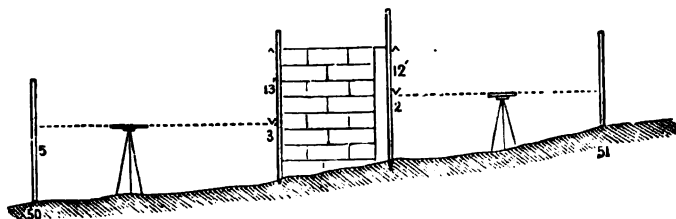
A water-level will level itself. Use that for intermediate points on the swamp, and test the result by leveling *around* the swamp with the spirit-level.

**557. Underwood.** If it can not be cut away, set the instrument on some eminence, natural or artificial.

**558. Board Fence.** Run a knife-blade through one of the boards, and hold the rod upon it on each side of the fence, as if it were a peg, keeping the blade in the same horizontal position while the rod and instrument are taken over.

**559. A Wall. First Method.** Drive a peg at the bottom of the wall, on the first side, and observe on it. Measure the height of the wall above the peg, and put this down as a B. S. Drive another peg on the other side of the wall; measure down to it from the top of the wall, and put that down as an F. S., just as if the level had been set in the air at the height of the top of the

FIG. 406.



wall, and this B. S. and F. S. had been really taken. Set up the instrument beyond the wall, take a B. S. to this peg, and go on as usual.

| FORE-SIGHTS. | STATIONS. | HEIGHTS. | BACK-SIGHTS. | Σ     |
|--------------|-----------|----------|--------------|-------|
|              | 50        | 74·00    | 5·00         | 79·00 |
| 3·00         | Peg.      | 76·00    | 13·00        | 89·00 |
| 12·00        | Peg.      | 77·00    | 2·00         | 79·00 |
| 1·00         | 51        | 78·00    |              |       |

*Second Method.* Mark where the line of sight strikes the wall ; measure up to the top of the wall, and put this down as an F. S., with a plus-sign, as in 553, where the line of sight struck below the top of the peg.

On the other side of the wall, sight back to it, and mark where the line of sight strikes. Measure to the top of the wall, and put this down as a B. S., with a minus-sign, and then go on as usual.

**560. House.** First try to find some place for the instrument from which you can see through, by opening doors or windows. Or, find some place in the house where you can set the instrument and see both ways, or hold the rod at some point inside, and look to it from front and back. A straight stick may be used if the rod can not be held upright, and the height measured on the rod.

**561. The Sun.** It often causes the leveler much difficulty—

1. By shining in the object-glass. If the instrument has a shade on it, draw it out. If not, shade the glass with your hand or hat, or set the instrument to one side of the line.

2. By heating the level unequally in all its parts. Holding an umbrella over it will remedy this.

3. By causing irregular refraction. Some parts of the ground become heated more than others, and therefore rarefy the air at those places. This can not be avoided nor corrected.

**562. Wind.** Watch for lulls of wind, and observe then several times, and take the mean. The least wind is at daybreak.

**563. Idiosyncrasies.** Different persons do not see things precisely alike. Each individual may have an inaccuracy peculiar to himself. One may read an observation higher or lower than another equal in skill. Also, a person's right and left eye may differ. This difference in individuals is termed their "personal equation."

To test the accuracy of your eye, turn the head so as to bring the eyes in the same vertical line, and sight to the rod held horizontally. Note where the vertical hair strikes. Then turn the

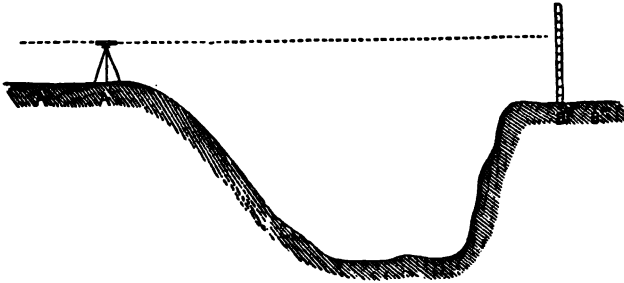


head to the other side, so as to invert the position of the eyes, and then sight again. As before, the mean of the two readings is the correct one.

**564. Reciprocal Leveling.** This is to be used when it is impossible to set midway between the two points, and the distance can not be readily determined.

Set the instrument over A, and sight to a rod at B, and note

FIG. 406.



reading. The difference of the reading and of the height of the cross-hairs gives a difference of height of A and B. Then set up at B, and observe to A, similarly. A new difference of height is obtained. The mean of these two is the correct one.

|                                                        |                                        |
|--------------------------------------------------------|----------------------------------------|
| Ht. of cross-hairs above peg at A=4·3'                 | Ht. of cross-hairs above peg at B=4·9' |
| Observation to B=7·0'                                  | Observation to A=4·2'                  |
| Diff. of height =2·7'                                  | Diff. of height =0·7'                  |
| True difference = $\frac{1}{2} (2·7' + 0·7') = 1·7'$ . |                                        |

Otherwise, set the instrument at an equal distance from each point, as A' and B', and observe to each in turn. The mean of the two differences of height obtained will be the true difference, as before.

#### LEVELING LOCATION.

**565. Its Nature.** It is the converse of the general problem of leveling, which is to find the difference of heights of two given points. *This* consists in determining the place of a point of any *required* height above or below any given point.

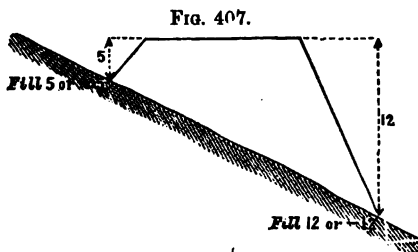
To do this, hold the rod on some point of known height above

the datum-level ; sight to it, and thus determine the height of the cross-hairs. Subtract from this the desired height of the required point, and set the target at the difference. Hold the rod at the place where the height is desired, and raise or lower it till the cross-hair bisects the target. Then the bottom of the rod is at the desired height. Usually, a peg is driven till its top is at the given height above the datum.

**566. Difficulties.** If the difference of height be too much to be measured at one setting of the instrument, take a series of levels up or down to the desired point. So, too, if they be far apart ; and thus find a place where, the instrument having a known height of cross-hairs, the target can finally be set, as before.

If the ground be so low or so high that a peg can not be set with its top at the required height, drive a peg till its top is just above the surface of the ground. Observe to the rod on it, determine its height above or below the desired point, and note this on a large stake driven beside it ; or, place its top a whole number of feet above or below the required height, and mark the difference on it, or on a stake beside it.

**567. Staking out Work.** When embankments and excavations are to be made for roads, etc., side-stakes are set at points in their



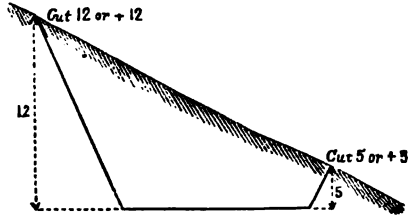
intended outside edges—i. e., where their slopes will meet the surface of the ground ; and the height which the ground at those points is above or below the required height or depth of the top or bottom of the finished work, is marked on

these stakes with the words “cut,” or “fill,” or the signs + or —.

The places of the stakes are found by trial. (See Gillespie's “Road-Making,” page 145.) These stakes are set to prepare the work for contractors. When the work is nearly finished, other stakes are set at the exact required height.

In staking out *foundation-pits*, set temporary stakes exactly above the intended bottom angles of the completed pit, thus marking out on the surface of the ground its intended shape. Take the heights of each of these stakes and move them outward such distances that cutting down from them with the proper depth and slope will bring you to the desired bottom angle.

FIG. 408.



**568. To locate a Level-Line.** This consists in determining on the surface of the ground a series of points which are at the same level—i. e., at the same height above some datum. Set one peg at the desired height, as in Art. 565. Sight to the rod held thereon, and make fast the target when bisected. Then send on the rod in the desired direction, and have it moved up or down along the slope of the ground, until the target is again bisected. This gives a second point. So go on as far as sights can be correctly taken, keeping unchanged the instrument and target. Make the last point sighted to a “turning-point.” Carry the instrument beyond it, set up again, take a B. S., and proceed as at first.

The rod should be held and pegs driven at points so near together that the level-line between them will be approximately straight.

**569. Applications.** One use of this operation is to mark out the line which will be the edge of the water of a pond to be formed by a dam. In that case, a point of a height equal to that of the top of the proposed dam, *plus* the height which the water will stand on it (to be determined by hydraulic formulas), will be the starting-point. Then proceed to set stakes as directed in the last article.

The line from stake to stake may then be surveyed like the sides of a field, and the area to be overflowed thus determined.

Strictly, the surface of the water behind a dam is not level,

but is curved concavely upward, and is therefore higher and sets back farther than if level. The backing up of the water is called *Remous*.

Another important application of this problem is to obtain "contour-lines" for topography.

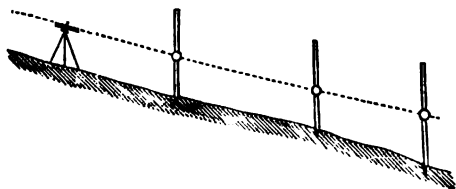
**570. To run a Grade-Line.** This consists in setting a series of pegs so that their tops shall be points in a line which shall have any required slope, ascending or descending.

When a grade-line is to be run straight between two given points, set the level over one point, set the target at the height of the cross-hairs, hold the rod on the other point, and raise or lower one end of the instrument till the cross-hair bisects the target. Then send the rod along the line, and drive pegs to such heights that when the rod is held on them the cross-hair will bisect the target. A stake may be driven at the extreme point to the height of the target.

*Another Method.* Knowing the horizontal distance between

the two given points, and their difference of level, determine the rise or fall per hundred feet. Then drive stakes at every hundred feet, so that the top of each succeeding one is the given

FIG. 409.



grade per hundred feet higher or lower, according as the grade is ascending or descending.

For example, suppose the horizontal distance from A to B is 1,200 feet, and that B is 16.8 feet higher than A. The rise per hundred feet from A is 1.4 foot. Beginning at A, set stakes at every hundred feet, so that the top of each one is 1.4 foot higher than the preceding one.

A line of uniform grade or slope is not a straight line. Calling the globe spherical, this line, when traced in the plane of a great circle, would be a logarithmic spiral. On a length of six miles, the difference in the middle between it and its straight chord would be six feet.

# APPENDIX.

## APPENDIX A.

### SYNOPSIS OF PLANE TRIGONOMETRY.\*

**1. Definition.** Plane Trigonometry is that branch of mathematical science which treats of the relations between the sides and angles of plane triangles. It teaches how to find any three of these six parts, when the other three are given, and one of them, at least, is a side.

**2. Angles and Arcs.** The *angles* of a triangle are measured by the *arcs* described, with any radius, from the angular points as centers, and intercepted between the legs of the angles. These arcs are measured by comparing them with an entire circumference, described with the same radius. Every circumference is regarded as being divided into 360 equal parts, called *degrees*. Each degree is divided into 60 equal parts, called *minutes*, and each minute into 60 *seconds*. These divisions are indicated by the marks  $^{\circ}$   $'$   $''$ . Thus 28 degrees, 17 minutes, and 49 seconds, are written  $28^{\circ} 17' 49''$ . Fractions of a second are best expressed decimally. An arc, including a quarter of a circumference and measuring a right angle, is therefore  $90^{\circ}$ . A semi-circumference comprises  $180^{\circ}$ . It is often represented by  $\pi$ , which equals  $3.14159$ , etc., or  $3\frac{1}{2}$  approximately, the radius being unity.

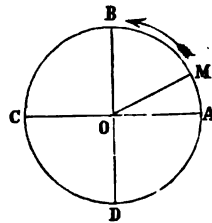
The length of  $1^{\circ}$  in parts of radius =  $0.01745329$ ; that of  $1'$  =  $0.00029089$ ; and that of  $1''$  =  $0.00000485$ .

The length of the radius of a circle in degrees, or 360ths of the circumference =  $57.29578^{\circ} = 57^{\circ} 17' 24.8'' = 3437.747' = 206264.8''$ . †

An arc may be regarded as generated by a point, M, moving from an origin, A, around a circle, in the direction of the arrow. The point may thus describe arcs of any lengths, such as AM;  $AB = 90^{\circ} = \frac{1}{2}\pi$ ;  $ABC = 180^{\circ} = \pi$ ;  $ABCD = 270^{\circ} = \frac{3}{2}\pi$ ;  $ABCD A = 360^{\circ} = 2\pi$ .

The point may still continue its motion, and generate arcs greater than a

FIG. 410.



\* For merely solving triangles, only Articles 1, 2, 3, 5, 6, 10, 11, and 12 are needed.

† The number of seconds in any arc which is given in parts of radius, radius being unity, equals the length of the arc so given divided by the length of the arc of one second; or multiplied by the number of seconds in radius.

circumference, or than two circumferences, or than three; or even infinite in length.

While the point, *M*, describes these arcs, the radius, *OM*, indefinitely produced, generates corresponding angles.

If the point, *M*, should move from the origin, *A*, in the contrary direction to its former movement, the arcs generated by it are regarded as *negative*, or *minus*; and so too, of necessity, the angles measured by the arcs.

Arcs and angles may therefore vary in length from 0 to  $+\infty$  in one direction, and from 0 to  $-\infty$  in the contrary direction.

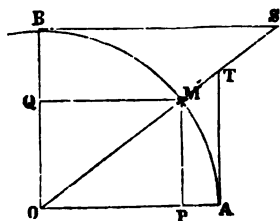
The *Complement* of an arc is the arc which would remain after subtracting the arc from a quarter of the circumference, or from  $90^\circ$ . If the arc be more than  $90^\circ$ , its complement is necessarily negative.

The *Supplement* of an arc is what would remain after subtracting it from half the circumference, or from  $180^\circ$ . If the arc be more than  $180^\circ$ , its supplement is necessarily negative.

**3. Trigonometrical Lines.** The relations of the sides of a triangle to its angles are what is required; but it is more convenient to replace the angles by arcs; and, once more, to replace the arcs by certain straight lines depending upon them, and increasing and decreasing with them, or, conversely, in such a way that the length of the lines can be found from that of the arcs, and *vice versa*. It is with these lines that the sides of a triangle are compared.\* These lines are called *Trigonometrical Lines*, or *Circular Functions*, because their length is a function of that of the circular arcs. The principal trigonometrical lines are *Sines*, *Tangents*, and *Secants*. Chords and versed sines are also used.

The *SINE* of an arc, *AM*, is the perpendicular, *MP*, let fall, from one extremity of the arc, upon the diameter which passes through the other extremity.

FIG. 411.



The *TANGENT* of an arc, *AM*, is the distance, *AT*, intercepted, on the tangent drawn at one extremity of the arc, between that extremity and the prolongation of the radius which passes through the other extremity.

The *SECANT* of an arc, *AM*, is the part, *OT*, of the prolonged radius, comprised between the center and the tangent.

The sine, tangent, and secant of the complement of an arc are called the *Co-sine*, *Co-tangent*, and *Co-secant* of that arc. Thus, *MQ* is the cosine of *AM*, *BS* its cotangent, and *OS* its cosecant. The cosine *MQ* is equal to *OP*, the part of the radius comprised between the center and the foot of the sine.

The *chord* of an arc is equal to twice the sine of half that arc.

The *versed-sine* of an arc, *AM*, is the distance, *AP*, comprised between the origin of the arc and the foot of the sine. It is consequently equal to the difference between the radius and the sine.

\* For the great value of this indirect mode of comparing the sides and angles of triangles, see Comte's "Philosophy of Mathematics" (Harper's, 1857), page 225.

The trigonometrical lines are usually written in an abbreviated form. Calling the arc  $AM = a$ , we write,

$$\begin{array}{lll} MP = \sin. a. & AT = \tan. a. & OT = \sec. a. \\ MQ = \cos. a. & BS = \cot. a. & OS = \csc. a. \end{array}$$

The period after  $\sin.$ ,  $\tan.$ , etc., indicating abbreviation, is frequently omitted.

The arcs whose sines, tangents, etc., are equal to a line  $= a$ , are written,

$$\begin{array}{l} \sin. \overline{a}, \text{ or arc } (\sin. = a); \\ \tan. \overline{a}, \text{ or arc } (\tan. = a); \text{ etc.} \end{array}$$

**4. The Lines as Ratios.** The ratios between the trigonometrical lines and the radius are the same for the same angles, or number of degrees in an arc, whatever the length of the radius or arc. Consequently, radius being unity, these lines may be expressed as simple ratios. Thus, in the right-angled triangle  $ABC$ , we would have

$$\begin{array}{ll} \sin. A = \frac{BC}{AB} = \frac{\text{opposite side}}{\text{hypotenuse}}, & \cos. A = \frac{AC}{AB} = \frac{\text{adjacent side}}{\text{hypotenuse}}, \\ \tan. A = \frac{BC}{AC} = \frac{\text{opposite side}}{\text{adjacent side}}, & \cot. A = \frac{AC}{BC} = \frac{\text{adjacent side}}{\text{opposite side}}, \\ \sec. A = \frac{AB}{AC} = \frac{\text{hypotenuse}}{\text{adjacent side}}, & \csc. A = \frac{AB}{BC} = \frac{\text{hypotenuse}}{\text{opposite side}}. \end{array}$$

When the radius of the arcs which measure the angles is unity, these ratios may be used for the lines. If the radius be any other length, the results which have been obtained by the above supposition must be modified by dividing each of the trigonometrical lines in the result by radius, and thus rendering the equations of the results "homogeneous." The same effect would be produced by multiplying each term in the expression by such a power of radius as would make it contain a number of *linear* factors equal to the greatest number in any term. The radius is usually represented by  $r$ , or  $R$ .

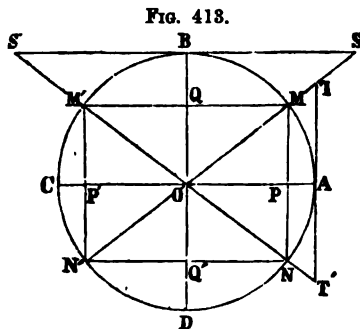


FIG. 418.

### 5. Their Variations in Length.

As the point  $M$  moves around the circle, and the arc thus increases, the sines, tangents, and secants, starting from zero, also increase; till, when the point  $M$  has arrived at  $B$ , and the arc has become  $90^\circ$ , the sine has become equal to radius, or unity, and the tangent and secant have become infinite. The complementary lines

have decreased, the cosine being equal to radius or unity at starting and becoming zero, and the cotangent and cosecant passing from infinity to zero.

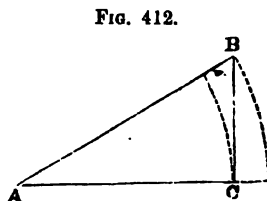


FIG. 412.

When the point M has passed the first quadrant at B, and is proceeding toward C, the sines, tangents, and secants begin to decrease, till, when the point has reached C, they have the same values as at A. They then begin to increase again, and so on. The table on page 405 indicates these variations.

The sines and tangents of very small arcs may be regarded as sensibly proportional to the arcs themselves; so that for  $\sin. a''$ , we may write  $a \cdot \sin. 1''$ ; and similarly, though less accurately, for  $\sin. a'$ , we may write  $a \cdot \sin. 1'$ .

The sines and tangents of very small arcs may similarly be regarded as sensibly of the same length as the arcs themselves.\*

$a$  being the length of any arc expressed in parts of radius, the lengths of its sine and cosine may be obtained by the following series:

$$\sin. a = a - \frac{a^3}{2 \cdot 3} + \frac{a^5}{2 \cdot 3 \cdot 4 \cdot 5} - \frac{a^7}{2 \cdot 3 \cdot 4 \cdot 5 \cdot 6 \cdot 7} +, \text{ etc.}$$

$$\cos. a = 1 - \frac{a^2}{2} + \frac{a^4}{2 \cdot 3 \cdot 4} - \frac{a^6}{2 \cdot 3 \cdot 4 \cdot 5 \cdot 6} +, \text{ etc.}$$

Let it be required to find  $\cos. 30^\circ$ , by the above series.

$$30^\circ = \frac{30}{180} \pi = \frac{1}{6} \times 3.1416 = .5236.$$

Substituting this number for  $a$ , the series becomes, taking only three terms of it,

$$1 - \frac{(.5236)^2}{2} + \frac{(.5236)^4}{24} -, \text{ etc.} = 1 - 0.137078 + 0.008130 = .866052;$$

which is the correct value of  $\cos. 30^\circ$  for the first four places of decimals.

The lengths of the other lines can be obtained from the mutual relations given in Art. 7. Some particular values are given below:

|                                       |                                         |                                         |
|---------------------------------------|-----------------------------------------|-----------------------------------------|
| $\sin. 30^\circ = \frac{1}{2}$        | $\sin. 45^\circ = \frac{1}{2} \sqrt{2}$ | $\sin. 60^\circ = \frac{1}{2} \sqrt{3}$ |
| $\tan. 30^\circ = \frac{1}{\sqrt{3}}$ | $\tan. 45^\circ = 1$                    | $\tan. 60^\circ = \sqrt{3}$             |
| $\sec. 30^\circ = \frac{2}{\sqrt{3}}$ | $\sec. 45^\circ = \sqrt{2}$             | $\sec. 60^\circ = 2$                    |

**6. Their Changes of Sign.** Lines measured in contrary directions from a common origin usually receive contrary algebraic signs. If, then, all the lines in the first quadrant are called positive, their signs will change in some of the other quadrants. Thus the *sines* in the first quadrant being all measured upward, when they are measured downward, as they are in the third and fourth quadrants, they will be negative. The *cosines* in the first quadrant are measured from left to right, and when they are measured from right to left, as in the second and third quadrants, they will be negative. The *tangents* and *secants* follow similar rules.

The variations in length and the changes of sign are all indicated in the following table, radius being unity. The terms "increasing" and "decreasing" apply to the lengths of the lines without any reference to their signs:

---

\* Consequently, the note on page 401 may read thus: The number of seconds in any very small arc given in parts of radius, radius being unity, is equal to the length of the arc so given divided by  $\sin. 1$ .



*Lengths and Signs of the Trigonometrical Lines for Arcs from 0° to 360°.*

| ARCS.         | 0°           | BETWEEN 0° AND 90°. | 90°          | BETWEEN 90° AND 180°. | 180°         |
|---------------|--------------|---------------------|--------------|-----------------------|--------------|
| Sine.....     | 0            | +, and increasing,  | +1           | +, and decreasing,    | 0            |
| Tangent.....  | 0            | +, and increasing,  | $\pm \infty$ | —, and decreasing,    | 0            |
| Secant.....   | +1           | +, and increasing,  | $\pm \infty$ | —, and decreasing,    | —1           |
| Cosine.....   | +1           | +, and decreasing,  | 0            | —, and increasing,    | —1           |
| Cotangent.... | $\pm \infty$ | +, and decreasing,  | 0            | —, and increasing,    | $\mp \infty$ |
| Cosecant....  | $\pm \infty$ | +, and decreasing,  | +1           | +, and increasing,    | $\pm \infty$ |

| ARCS.         | 180°         | BETWEEN 180° AND 270°. | 270°         | BETWEEN 270° AND 360°. | 360°         |
|---------------|--------------|------------------------|--------------|------------------------|--------------|
| Sine.....     | 0            | —, and increasing,     | —1           | —, and decreasing,     | 0            |
| Tangent.....  | 0            | +, and increasing,     | $\pm \infty$ | —, and decreasing,     | 0            |
| Secant.....   | —1           | —, and increasing,     | $\mp \infty$ | +, and decreasing,     | +1           |
| Cosine.....   | —1           | —, and decreasing,     | 0            | +, and increasing,     | +1           |
| Cotangent.... | $\mp \infty$ | +, and decreasing,     | 0            | —, and increasing,     | $\mp \infty$ |
| Cosecant....  | $\pm \infty$ | —, and decreasing,     | —1           | —, and increasing,     | $\mp \infty$ |

From this table, and Fig. 418, we see that *an arc and its supplement* have the same sine; and that their tangents, secants, cosines, and cotangents are of equal length but of contrary signs; while the cosecants are the same in both length and sign.

We also deduce from the figure the following consequences:

$$\begin{aligned}
 \sin. (a^\circ + 180^\circ) &= -\sin. a^\circ. & \cos. (a^\circ + 180^\circ) &= -\cos. a^\circ. \\
 \tan. (a^\circ + 180^\circ) &= \tan. a^\circ. & \cot. (a^\circ + 180^\circ) &= \cot. a^\circ. \\
 \sec. (a^\circ + 180^\circ) &= -\sec. a^\circ. & \operatorname{cosec}. (a^\circ + 180^\circ) &= -\operatorname{cosec}. a^\circ. \\
 \sin. (-a^\circ) &= -\sin. a^\circ. & \cos. (-a^\circ) &= \cos. a^\circ. \\
 \tan. (-a^\circ) &= -\tan. a^\circ. & \cot. (-a^\circ) &= -\cot. a^\circ. \\
 \sec. (-a^\circ) &= \sec. a^\circ. & \operatorname{cosec}. (-a^\circ) &= -\operatorname{cosec}. a^\circ.
 \end{aligned}$$

An infinite number of arcs have the same trigonometrical lines; for, an arc  $a$ , the same arc plus a circumference, the same arc plus two circumferences, and so on, would have the same sine, etc.

"To bring back to the first quadrant" the trigonometrical lines of any large arc, proceed thus: Let  $1029^\circ$  be an arc the sine of which is desired. Take from it as many times  $360^\circ$  as possible. The remainder will be  $309^\circ$ . Then we shall have  $\sin. 309^\circ = \sin. (180^\circ - 309^\circ) = \sin. -129^\circ = -\sin. 129^\circ = -\sin. (180^\circ - 129^\circ) = -\sin. 51^\circ$ .

## 7. Their Mutual Relations. Radius being unity,

$$\tan. a^\circ = \frac{\sin. a^\circ}{\cos. a^\circ}. \quad \cot. a^\circ = \frac{\cos. a^\circ}{\sin. a^\circ}.$$

$$\sec. a^\circ = \frac{1}{\cos. a^\circ} \quad \operatorname{cosec}. a^\circ = \frac{1}{\sin. a^\circ}.$$

$$\tan. a^\circ \times \cot. a^\circ = 1. \quad (\sin. a^\circ)^2 + (\cos. a^\circ)^2 = 1.*$$

$$1 + (\tan. a^\circ)^2 = (\sec. a^\circ)^2. \quad 1 + (\cot. a^\circ)^2 = (\operatorname{cosec}. a^\circ)^2.$$

\* The square, etc., of the sine, etc., of an arc, is often expressed by placing the exponent between the abbreviation of the name of the trigonometrical line and the

Hence, any one of the trigonometrical lines being given, the rest can be found from some of these equations.

**8. Two Arcs.** Let  $a$  and  $b$  represent any two arcs,  $a$  being the greater. Then the following formulas apply :

$$\begin{aligned}\sin. (a + b) &= \sin. a \cdot \cos. b + \cos. a \cdot \sin. b. \\ \sin. (a - b) &= \sin. a \cdot \cos. b - \cos. a \cdot \sin. b. \\ \cos. (a + b) &= \cos. a \cdot \cos. b - \sin. a \cdot \sin. b. \\ \cos. (a - b) &= \cos. a \cdot \cos. b + \sin. a \cdot \sin. b. \\ \tan. (a + b) &= \frac{\tan. a + \tan. b}{1 - \tan. a \cdot \tan. b}. \\ \tan. (a - b) &= \frac{\tan. a - \tan. b}{1 + \tan. a \cdot \tan. b}. \\ \cot. (a + b) &= \frac{\cot. a \cdot \cot. b - 1}{\cot. b + \cot. a}. \\ \cot. (a - b) &= \frac{\cot. a \cdot \cot. b + 1}{\cot. b - \cot. a}. \\ \sin. a \cdot \sin. b &= \frac{1}{2} \cdot \cos. (a - b) - \frac{1}{2} \cos. (a + b). \\ \cos. a \cdot \cos. b &= \frac{1}{2} \cdot \cos. (a + b) + \frac{1}{2} \cos. (a - b). \\ \sin. a \cdot \cos. b &= \frac{1}{2} \cdot \sin. (a + b) + \frac{1}{2} \sin. (a - b). \\ \cos. a \cdot \sin. b &= \frac{1}{2} \cdot \sin. (a + b) - \frac{1}{2} \sin. (a - b). \\ \sin. a + \sin. b &= 2 \sin. \frac{1}{2} (a + b) \cos. \frac{1}{2} (a - b). \\ \cos. a + \cos. b &= 2 \cos. \frac{1}{2} (a + b) \cos. \frac{1}{2} (a - b). \\ \sin. a - \sin. b &= 2 \sin. \frac{1}{2} (a - b) \cos. \frac{1}{2} (a + b). \\ \cos. b - \cos. a &= 2 \sin. \frac{1}{2} (a - b) \sin. \frac{1}{2} (a + b). \\ \tan. a + \tan. b &= \frac{\sin. (a + b)}{\cos. a \cdot \cos. b}. \\ \tan. a - \tan. b &= \frac{\sin. (a - b)}{\cos. a \cdot \cos. b}. \\ \cot. b + \cot. a &= \frac{\sin. (a + b)}{\sin. a \cdot \sin. b}. \\ \cot. b - \cot. a &= \frac{\sin. (a - b)}{\sin. a \cdot \sin. b}.\end{aligned}$$

**9. Double and Half Arcs.** Letting  $a$  represent any arc, as before, we have the following formulas:

$$\begin{aligned}\sin. 2a &= 2 \sin. a \cdot \cos. a. \\ \cos. 2a &= (\cos. a)^2 - (\sin. a)^2 = 2 (\cos. a)^2 - 1 = 1 - 2 (\sin. a)^2. \\ \tan. 2a &= \frac{2 \tan. a}{1 - (\tan. a)^2} = \frac{2 \cot. a}{(\cot. a)^2 - 1} = \frac{2}{\cot. a - \tan. a}. \\ \cot. 2a &= \frac{(\cot. a)^2 - 1}{2 \cot. a} = \frac{1}{2} (\cot. a - \tan. a).\end{aligned}$$

number of the degrees in the arc, thus:  $\text{Sin.}^2 a^\circ$ ,  $\text{tan.}^2 a^\circ$ , etc. But the notation given above places the index as used by Gauss, Delambre, Arbogast, etc., though the first two omit the parentheses.

$$\sin. \frac{1}{2} a = \sqrt{\left[\frac{1}{2}(1 - \cos. a)\right]}.$$

$$\cos. \frac{1}{2} a = \sqrt{\left[\frac{1}{2}(1 + \cos. a)\right]}.$$

$$\tan. \frac{1}{2} a = \frac{\sin. a}{1 + \cos. a} = \frac{1 - \cos. a}{\sin. a} = \sqrt{\left(\frac{1 - \cos. a}{1 + \cos. a}\right)}.$$

$$\cot. \frac{1}{2} a = \frac{1 + \cos. a}{\sin. a} = \frac{\sin. a}{1 - \cos. a} = \sqrt{\left(\frac{1 + \cos. a}{1 - \cos. a}\right)}.$$

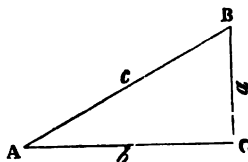
**10. Trigonometrical Tables.** In the usual tables of the natural trigonometrical lines, the degrees from  $0^\circ$  to  $45^\circ$  are found at the top of the table, and those from  $45^\circ$  to  $90^\circ$  at the bottom; the latter being complements of the former. Consequently, the columns which have *Sine* and *Tangent* at top have *Cosine* and *Cotangent* at bottom, since the cosine or cotangent of any arc is the same thing as the sine or tangent of its complement. The minutes to be added to the degrees are found in the left-hand column, when the number of degrees at the top of the page are used, and in the right-hand column for the degrees when at the bottom of the page. The lines for arcs intermediate between those in the tables are found by proportion. The lines are calculated for a radius equal unity. Hence, the values of the sines and cosines are decimal fractions, though the point is usually omitted. So too are the tangents from  $0^\circ$  to  $45^\circ$ , and the cotangents from  $90^\circ$  to  $45^\circ$ . Beyond those points they are integers and decimals.

The calculations, like all others involving large numbers, are shortened by the use of logarithms, which substitute addition and subtraction for multiplication and division; but the young student should avoid the frequent error of regarding logarithms as a necessary part of trigonometry.

### SOLUTION OF TRIANGLES.

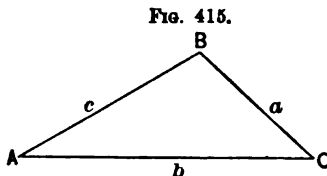
**11. Right-angled Triangles.** Let  $ABC$  be any right-angled triangle. Denote the sides opposite the angles by the corresponding small letters. Then any one side and one acute angle, or any two sides being given, the other parts can be obtained by one of the following equations:

FIG. 414.



| GIVEN. | REQUIRED. | FORMULAS.                                                                    |
|--------|-----------|------------------------------------------------------------------------------|
| $a, b$ | $c, A, B$ | $c = \sqrt{a^2 + b^2}$ ; $\tan. A = \frac{a}{b}$ ; $\cot. B = \frac{a}{b}$ . |
| $a, c$ | $b, A, B$ | $b = \sqrt{c^2 - a^2}$ ; $\sin. A = \frac{a}{c}$ ; $\cos. B = \frac{a}{c}$ . |
| $a, A$ | $b, c, B$ | $b = a \cdot \cot. A$ ; $c = \frac{a}{\sin. A}$ ; $B = 90^\circ - A$ .       |
| $b, A$ | $a, c, B$ | $a = b \cdot \tan. A$ ; $c = \frac{b}{\cos. A}$ ; $B = 90^\circ - A$ .       |
| $c, A$ | $a, b, B$ | $a = c \cdot \sin. A$ ; $b = c \cos. A$ ; $B = 90^\circ - A$ .               |

**12. Oblique-angled Triangles.** Let  $ABC$  be any oblique-angled triangle, the angles and sides being noted as in the figure. Then any three of its six parts being given, and one of them being a side, the other parts can be obtained by one of the following methods, which are founded on these three theorems:



**THEOREM I.**—*In every plane triangle, the sines of the angles are to each other as the opposite sides.*

**THEOREM II.**—*In every plane triangle, the sum of two sides is to their difference as the tangent of half the sum of the angles opposite those sides is to the tangent of half their difference.*

**THEOREM III.**—*In every plane triangle, the cosine of any angle is equal to a fraction whose numerator is the sum of the squares of the sides adjacent to the angle, minus the square of the side opposite to the angle, and whose denominator is twice the product of the sides adjacent to the angle.*

All the cases for solution which can occur may be reduced to four:

**CASE 1.**—*Given a side and two angles.* The third angle is obtained by subtracting the sum of the two given angles from  $180^\circ$ . Then either unknown side can be obtained by Theorem I.

Calling the given side  $a$ , we have  $b = a \frac{\sin. B}{\sin. A}$ ; and  $c = a \frac{\sin. C}{\sin. A}$ .

**CASE 2.**—*Given two sides and an angle opposite one of them.* The angle opposite the other given side is found by Theorem I. The third angle is obtained by subtracting the sum of the other two from  $180^\circ$ . The remaining side is then obtained by Theorem I.

Calling the given sides  $a$  and  $b$ , and the given angle  $A$ , we have  $\sin. B = \frac{b}{a} \sin. A$ .

Since an angle and its supplement have the same sine, the result is ambiguous; for the angle  $B$  may have either of the two supplementary values indicated by the sine, if  $b > a$ , and  $A$  is an acute angle.

$$C = 180^\circ - (A + B). \quad c = \sin. C \frac{a}{\sin. A}.$$

**CASE 3.**—*Given two sides and their included angle.* Applying Theorem II (obtaining the sum of the angles opposite the given sides by subtracting the given included angle from  $180^\circ$ ), we obtain the difference of the unknown angles. Adding this to their sum we obtain the greater angle, and subtracting it from their sum we get the less. Then Theorem I will give the remaining side.

Calling the given sides  $a$  and  $b$ , and the included angle  $C$ , we have  $A + B = 180^\circ - C$ . Then

$$\tan \frac{1}{2} (A - B) = \tan \frac{1}{2} (A + B) \cdot \frac{a - b}{a + b}.$$

$$\frac{1}{2} (A + B) + \frac{1}{2} (A - B) = A. \quad \frac{1}{2} (A + B) - \frac{1}{2} (A - B) = B. \quad c = a \frac{\sin. C}{\sin. A}.$$

In the first equation  $\cot. \frac{1}{2} C$  may be used in the place of  $\tan. \frac{1}{2} (A + B)$ .

CASE 4.—*Given the three sides.* Let  $s$  represent half the sum of the three sides  $= \frac{1}{2} (a + b + c)$ . Then any angle, as  $A$ , may be obtained from either of the following formulas, founded on Theorem III:

$$\sin. \frac{1}{2} A = \sqrt{\left[ \frac{(s-b)(s-c)}{bc} \right]}.$$

$$\cos. \frac{1}{2} A = \sqrt{\left[ \frac{s(s-a)}{bc} \right]}.$$

$$\tan. \frac{1}{2} A = \sqrt{\left[ \frac{(s-b)(s-c)}{s(s-a)} \right]}.$$

$$\sin. A = \frac{2 \sqrt{s(s-a)(s-b)(s-c)}}{bc}.$$

$$\cos. A = \frac{b^2 + c^2 - a^2}{2bc}.$$

The first formula should be used when  $A < 90^\circ$ , and the second when  $A > 90^\circ$ . The third should not be used when  $A$  is nearly  $180^\circ$ ; nor the fourth when  $A$  is nearly  $90^\circ$ ; nor the fifth when  $A$  is very small. The third is the most convenient when all the angles are required.

## APPENDIX B.

### TRANSVERSALS.

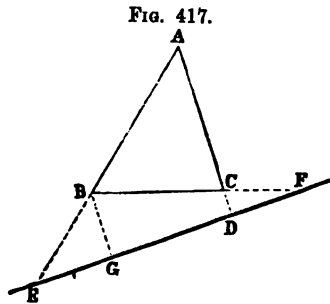
**THEOREM I.**—*If a straight line be drawn so as to cut any two sides of a triangle, and the third side prolonged, thus dividing them into six parts (the prolonged side and its prolongation being two of the parts), then will the product of any three of those parts, whose extremities are not contiguous, equal the product of the other three parts.*

That is, in Fig. 416,  $ABO$  being the triangle, and  $DF$  the transversal,  $BE \times AD \times CF = EA \times DC \times BF$ .

To prove this, from  $B$  draw  $BG$ , parallel to  $CA$ . From the similar triangles  $BEG$  and  $AED$ , we have  $BG : BE :: AD : AE$ . From the similar triangles  $BFG$  and  $CFD$ , we have  $CD : CF :: BG : BF$ . Multiplying these proportions together, we have  $BG \times CD : BE \times CF :: AD \times BG : AE \times BF$ . Multiplying extremes and means, and suppressing the common factor  $BG$ , we have  $BE \times AD \times CF = EA \times DC \times BF$ .

These six parts are sometimes said to be *in involution*.

If the transversal passes entirely outside of the triangle and cuts the prolongations of all three sides, as in Fig. 417, the theorem still holds good. The same demonstration applies without any change.\*



**THEOREM II.**—*Conversely : If three points be taken on two sides of a triangle, and on the third side prolonged, or on the prolongations of the three sides, dividing them into six parts, such that the product of three non-consecutive parts equals the product of the other three parts, then will these three points lie in the same straight line.*

This theorem is proved by a *reductio ad absurdum*.

**THEOREM III.**—*If, from the summits*

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\* This theorem may be extended to polygons.

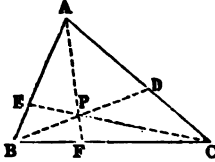
of a triangle, lines be drawn, to a point situated either within or without the triangle, and prolonged to meet the sides of the triangle, or their prolongations, thus dividing them into six parts, then will the product of any three non-consecutive parts be equal to the product of the other three parts.

That is, in Fig. 418, or Fig. 419,

$$A E \times B F \times C D = E B \times F C \times D A.$$

For, the triangle  $ABF$ , being cut by the transversal  $EC$ , gives the relation (Theorem I).

FIG. 418.



$$A E \times B C \times F P = E B \times F C \times P A.$$

The triangle  $AOF$ , being cut by the transversal  $DB$ , gives

$$D O \times F B \times P A = A D \times O B \times F P.$$

Multiplying these equations together, and suppressing the common factors  $PA$ ,  $OB$ , and  $FP$ , we have  $A E \times B F \times C D = E B \times F C \times D A$ .

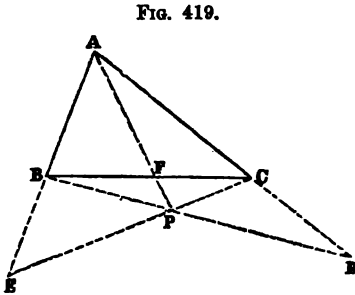


FIG. 419.

THEOREM IV. — Conversely: If

three points are situated on the three sides of a triangle, or on their prolongations (either one, or three, of these points being on the sides), so that they divide these lines in such a way that the product of any three non-consecutive parts equals the product of the other three parts, then will lines drawn from these points to the opposite angles meet in the same point.

This theorem can be demonstrated by a *reductio ad absurdum*.

#### COROLLARIES OF THE PRECEDING THEOREMS.

COROLLARY 1.—The MEDIANS of a triangle (i. e., the lines drawn from its summits to the middles of the opposite sides) meet in the same point.

For, supposing, in Fig. 418, the points  $D$ ,  $E$ , and  $F$  to be the middles of the sides, the products of the non-consecutive parts will be equal—i. e.,  $A E \times B F \times C D = D A \times E B \times F C$ ; since  $A E = E B$ ,  $B F = F C$ ,  $C D = D A$ . Then Theorem IV applies.

COR. 2.—The BISSECTRICES of a triangle (i. e., the lines bisecting its angles) meet in the same point.

For, in Fig. 418, supposing the lines  $AF$ ,  $BD$ ,  $CE$  to be bissectrices, we have (Legendre, IV, 17):

$$\left. \begin{array}{l} B F : F C :: A B : A C \\ C D : D A :: B C : B A \\ A E : E B :: C A : C B \end{array} \right\} \text{whence } \left\{ \begin{array}{l} B F \times A C = F C \times A B, \\ C D \times B A = D A \times B C, \\ A E \times C B = E B \times C A. \end{array} \right.$$

Multiplying these equations together, and omitting the common factors, we have  $B F \times C D \times A E = F C \times D A \times E B$ . Then Theorem IV applies.

COR. 3.—The ALTITUDES of a triangle (i. e., the lines drawn from its summits perpendicular to the opposite sides) meet in the same point.

For, in Fig. 418, supposing the lines  $AF$ ,  $BD$ , and  $CE$  to be altitudes, we have three pairs of similar triangles,  $BCD$  and  $FCA$ ,  $CAE$  and  $DAB$ ,  $ABF$  and  $ECB$ , by comparing which we obtain relations from which it is easy to deduce  $BF \times CD \times AE = EB \times FC \times DA$ ; and then Theorem IV again applies.

COR. 4.—If, in Fig. 418, or Fig. 419, the point  $F$  be taken in the middle of  $BC$ , then will the line  $ED$  be parallel to  $BC$ .

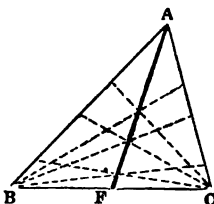
For, since  $BF = FC$ , the equation of Theorem III reduces to  $AE \times CD = EB \times DA$ ; whence  $AE : EB :: AD : DC$ ; consequently  $ED$  is parallel to  $BC$ .

COR. 5.—Conversely: If  $ED$  be parallel to  $BC$ , then is  $BF = FC$ .

For, since  $AE : EB :: AD : DC$ , we have  $AE \times DC = EB \times AD$ ; whence, in the equation of Theorem III, we must have  $BF = FC$ .

COR. 6.—From the preceding corollary, we derive the following:

FIG. 420.



If two sides of a triangle are divided proportionally, starting from the same summit, as  $A$ , and lines are drawn from the extremities of the third side to the points of division, the intersections of the corresponding lines will all lie in the same straight line joining the summit  $A$ , and the middle of the base.

COR. 7.—A particular case of the preceding corollary is this:

In any trapezoid, the straight line which joins the intersection of the diagonals and the point of meeting of the non-parallel sides produced, passes through the middle of the two parallel bases.

COR. 8.—If the three lines drawn through the corresponding summits of two triangles cut each other in the same point, then the three points in which the corresponding sides, produced if necessary, will meet, are situated in the same straight line.

This corollary may be otherwise enunciated, thus:

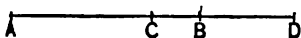
If two triangles have their summits situated, two and two, on three lines which meet in the same point, then, etc.

This is proved by obtaining by Theorem I three equations, which, being multiplied together, and the six common factors canceled, give an equation to which Theorem II applies.

Triangles thus situated are called *homologic*; the common point of meeting of the lines passing through their summits is called the *center of homology*; and the one on which the sides meet, the *axis of homology*.

## HARMONIC DIVISION.

FIG. 421.



DEFINITIONS.—A straight line,  $AB$ , is said to be *harmonically divided* at the points  $C$  and  $D$ , when these points determine two additive segments,  $AC$ ,  $BC$ , and two sub-



tractive segments,  $AD$ ,  $BD$ , proportional to one another; so that  $AC : BC :: AD : BD$ . It will be seen that  $AC$  must be more than  $BC$ , since  $AD$  is more than  $BD$ .\*

This relation may be otherwise expressed, thus: The product of the whole line by the middle part equals the product of the extreme parts.

Reciprocally, the line  $DC$  is harmonically divided at the points  $B$  and  $A$ , since the preceding proportion may be written  $DB : CB :: DA : CA$ .

The four points,  $A$ ,  $B$ ,  $C$ ,  $D$ , are called *harmonics*. The points  $C$  and  $D$  are called *harmonic conjugates*. So are the points  $A$  and  $B$ .

When a straight line, as  $AB$ , is divided harmonically, its half is a mean proportional between the distance from the middle of the line to the two points,  $C$  and  $D$ , which divide it harmonically.

If, from any point,  $O$ , lines be drawn so as to divide a line harmonically, these lines are called an *harmonic pencil*.

The four lines which compose it,  $OA$ ,  $OC$ ,  $OB$ ,  $OD$ , in the figure, are called its *radii*, and the pairs which pass through the conjugate points are called *conjugate radii*.

**THEOREM V.**—In any harmonic pencil, a line drawn parallel to any one of the radii is divided by the three other radii into two equal parts.

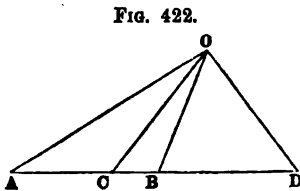


FIG. 422.

Let  $EF$  be the line, drawn parallel to  $OA$ . Through  $B$  draw  $GH$ , also parallel to  $OA$ . We have,

$$GB : OA :: BD : AD; \text{ and}$$

$$BH : OA :: BC : AC.$$

But, by hypothesis,  $AC : BC :: AD : BD$ .

Hence, the first two proportions reduce to  $GB = BH$ ; and, consequently,  $EK = KF$ .

The reciprocal is also true—i. e.,

If four lines radiating from a point are such that a line drawn parallel to one of them is divided into two equal parts by the other three, the four lines form an harmonic pencil.

**THEOREM VI.**—If any transversal to an harmonic pencil be drawn, it will be divided harmonically.

Let  $LM$  be the transversal. Through  $K$ , where  $LM$  intersects  $OB$ , draw  $EF$  parallel to  $OA$ . It is bisected at  $K$  by the preceding theorem; and the

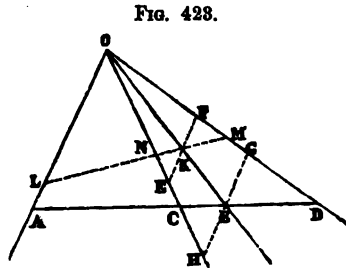


FIG. 423.

\* Three numbers,  $m$ ,  $n$ ,  $p$ , arranged in decreasing order of size, form an *harmonic proportion*, when the difference of the first and the second is to the difference of the second and the third, as the first is to the third. Such are the numbers 6, 4, and 3; or 6, 3, and 2; or 15, 12, and 10; etc. So, in Fig. 421, are the lines  $AD$ ,  $AB$ , and  $AC$ , which thus give  $BD : CB :: AD : AC$ ; or  $AC : CB :: AD : BD$ . The series of fractions,  $\frac{1}{2}$ ,  $\frac{1}{3}$ ,  $\frac{1}{4}$ , etc., is called an *harmonic progression*, because any consecutive three of its terms form an *harmonic proportion*.

similar triangles, FMK and LMO, EKN and LNO, give the proportions

$LM : KM :: OL : FK$ , and  $LN : NK :: OL : EK$ ; whence,

since  $FK = EK$ , we have  $LN : NK :: LM : KM$ .

**COROLLARY.**—*The two sides of any angle, together with the bissectrices of the angle and of its supplement, form an harmonic pencil.*

**THEOREM VII.**—*If, from the summits of any triangle, ABC, through any point, P, there be drawn the transversals AD, BE, OF, and the transversal ED be drawn to meet AB prolonged in F', the points F and F' will divide the base AB harmonically.*

This may be otherwise expressed, thus :

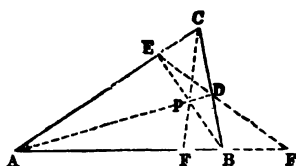
*The line, OP, which joins the intersection of the diagonals of any quadrilateral, ABDE, with the point of meeting, C, of two opposite sides prolonged, cuts the side AB in a point F, which is the harmonic conjugate of the point of meeting, F' of the other two sides, ED and AB, prolonged.*

For, by Theorem I,  $AF' \times BD \times CE = F'B \times DC \times EA$ ; and

by Theorem III,  $AF \times BD \times CE = FB \times DC \times EA$ ;

whence  $AF : FB :: AF' : F'B$ .

FIG. 424.



### THE COMPLETE QUADRILATERAL.

A *Complete Quadrilateral* is formed by drawing any four straight lines, so that each of them shall cut each of the other three, so as to give six different points of intersection. It is so called

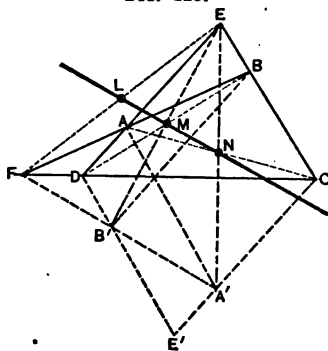
because in the figure thus formed are found three quadrilaterals; viz., in Fig. 425, ABCD, a common *convex* quadrilateral; EAFC, a *uni-concave* quadrilateral; and EBAFD, a *bi-concave* quadrilateral, composed of two opposite triangles.

The complete quadrilateral, AEBODF, has three diagonals; viz., two interior, AC, BD; and one exterior, EF.

**THEOREM VIII.**—*In every COMPLETE QUADRILATERAL the middle points of its three diagonals lie in the same straight line.*

AEBODF is the quadrilateral, and LMN the middle points of its three diagonals. From A and D draw parallels to BC, and from B and C draw parallels to AD. The triangle EDC being cut by the transversal BF, we have (Theorem I),  $DF \times CB \times EA = CF \times EB \times DA$ . From the equality of parallels between parallels, we have  $CB = E'B'$ ,  $EA = OA'$ ,  $EB = DB'$ ,  $DA = E'A'$ . Hence, the above equation becomes  $DF \times E'B' \times OA'$

FIG. 425.



$= CF \times DB' \times E'A'$ ; therefore, by Theorem II, the points,  $F, B', A'$ , lie in the same straight line. Now, since the diagonals of the parallelogram  $ECA'A$  bisect each other at  $N$ , and those of the parallelogram  $EBB'D$  at  $M$ , we have  $EN : NA' :: EM : MB'$ . Then  $MN$  is parallel to  $FA'$ , and we have  $EN : NA' :: EL : LF$ , or  $EL = LF$ , so that  $L$  is the middle of  $EF$ , and the same straight line passes through  $L, M$ , and  $N$ .

**THEOREM IX.**—*In every complete quadrilateral each of the three diagonals is divided harmonically by the two others.*

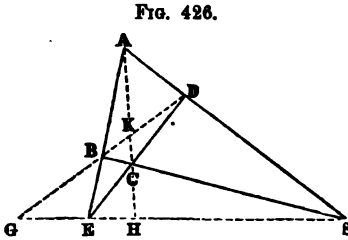


FIG. 426.

$CEBADF$  is the complete quadrilateral. The diagonal  $EF$  is divided harmonically at  $G$  and  $H$  by  $DB$  and  $AC$  produced; since  $AH, DE$ , and  $FB$  are three transversals drawn from the summits of the triangle  $AEF$  through the same point  $C$ ; and therefore, by Theorem VII,  $DBG$  and  $ACH$  divide  $EF$  harmonically.

So too, in the triangle  $ABD, CB, CA, CD$ , are the three transversals passing through  $C$ ; and  $G$  and  $K$  therefore divide the diagonal  $BD$  harmonically.

So, too, in the triangle,  $ABC, DA, DB, DC$  are the transversals, and  $H$  and  $K$  the points which divide the diagonal  $AC$  harmonically.

**THEOREM X.**—*If from a point,  $A$ , any number of lines be drawn, cutting the sides of an angle  $POQ$ , the intersections of the diagonals of the quadrilaterals thus formed will all lie in the same straight line passing through the summit of the angle.*

By the preceding theorem, the diagonal  $BC'$  of the complete quadrilateral,  $BAB'C'CO$ , is divided harmonically at  $D$  and  $E$ . Hence,  $OA, OP, OD$ , and  $OQ$ , form an harmonic pencil. So do  $OA, OP, OD'$ , and  $OQ$ . Therefore, the lines  $OD, OD'$ , coincide. So for the other intersections.

If the point  $A$  moves on  $OA$ , the line  $OD$  is not displaced. If, on the contrary,  $OA$  is displaced,  $OD$  turns around the point  $O$ . Hence, the point  $A$  is said to be a *pole* with respect to the line  $OD$ , which is itself called the *polar* of the point  $A$ . Similarly,  $D$  is a pole of  $OA$ , which is the polar of  $D$ .  $OD$  is likewise the polar of any other point on the line  $OA$ ; and this property is necessarily reciprocal for the two conjugate radii  $OA, OD$ , with respect to the lines  $OP, OQ$ , which are also conjugate radii. Hence: in every harmonic pencil, each of the radii is a *polar* with respect to each point of its conjugate; and each point of this latter line is a *pole* with respect to the former.

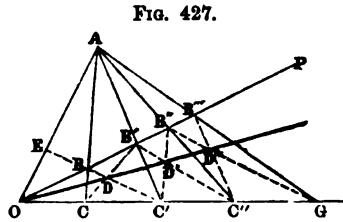


FIG. 427.

## APPENDIX C.

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### *PROBLEMS IN FIELD-WORK.*

THE following problems in field-work are arranged for students, and are intended as a suggestion to instructors, who can extend them to suit the needs of their classes.

Students should keep full, plain, and accurate notes of all field-work. These notes should contain concise descriptions of the methods used, and the results in plats or tabular form when practicable.

Record should also be made of dates, names of helpers, nature of ground, weather, and any other circumstance which may influence the accuracy and reliability of the work.

The numbers given in parentheses in the problems refer to articles in Surveying and Leveling.

### CHAIN-SURVEYING.

1. Throw out and do up a surveyor's chain and a steel tape. (21.)
2. Estimate the lengths of several given lines, such as the length or breadth of a building or the distance between any two convenient points. Measure the same, and note the discrepancies between the estimates and the measured distances. (18-20).
3. Locate two points by one of the methods of determining the position of points and measure the distance between them. Destroy the points and relocate them. Measure the distance between them again and note the result. (3-8.)
4. Lay out one hundred feet, and ascertain by repeated trials the number of paces in that distance at an ordinary natural walk. When this has been determined satisfactorily, pace off a distance of one hundred yards several times and assume the average as the correct distance. Then measure off the one hundred yards with a tape, and note the error of the average and of each separate estimate. (29.)
5. Drop a pin from a fixed point to the ground. Try it point down and head down, and record in each case the distance it strikes away from the true point on the ground as determined by a plumb-bob.
6. Measure with a link-chain the distance between two designated points which shall be at least ten chains apart. Use only four pins in this problem, so that there will be at least two tallies. Measure from the first to the

second point, and then from the second to the first. Repeat these measurements, the head and rear chain-men changing positions, thus obtaining four results. Note the distance along the line to any object of interest, as a bridge, fence, or tree, and indicate the positions of the same on the sketch. (18), (20), (188), (189), (88), (84.)

7. Measure the distance between two designated points with a steel tape. Drive a stake at the end of each tape length, and also at some even foot-mark on the tape. Mark each measurement very carefully on the top of the stake with a pencil. Repeat the measurement as in Problem 6.

8. Measure a line several chains in length on sloping ground, first by plumbing down, and then measuring directly along the surface. Compare the results. (20.)

9. *Testing Chain or Tape.* With the chain or tape lying flat, measure the difference between it and the standard, pulling to tensions of twelve, sixteen, and twenty pounds. Hold the chain or tape over the standard and project its length upon the standard by means of plumb bobs, and note the distances indicated by tensions of twelve, sixteen, and twenty pounds.

10. Lay out a line one hundred and fifty feet long, and at one end of it erect a perpendicular by the method of Articles 109 and 110. Extend the perpendicular one hundred and fifty feet. Measure the hypotenuse of the triangle thus formed and compare the measured length with the computed value of the hypotenuse of the right-angled triangle, whose base and altitude are each one hundred and fifty feet.

11. Erect a perpendicular from a given point to a given line, the point being more than one hundred feet away from the given line. Test as in Problem 10. (106-120.)

12. Lay out a square, beginning at one angle, measuring the sides and laying out the angles. Make the sides not less than two chains. Note the error of closure.

13. Lay out two parallel lines; extend them about five chains, and test by measuring the perpendicular distance between their extremities. (121.)

14. Measure a line one end of which is visible but supposed to be inaccessible, and afterward test the computed length by measuring it directly. (149, 150.)

15. Prolong a line in azimuth and distance past an imaginary obstacle—first, by rectangular offsets (180), second, by an equilateral triangle (181). Extend the resulting line in each case back over the imaginary obstacle, and note the amount by which it varies from the original line.

16. Locate two points several hundred feet apart so that a wood intervenes to prevent one being visible from the other. Establish stakes at distances of one hundred feet on the line joining the two points. (142.)

17. Lay off lines making angles of 15°, 30°, 45°, 60°, 75°, and 90° from a given line at a given point. (28.)

18. Locate permanently an irregular pentagon whose sides are about three hundred feet in length. Measure all the angles by the method of Article 28. Measure the sides. Assume one side as meridian, and from the measured angles compute the corresponding bearings of the other sides and

the latitude and departure of each. Put the results in the tabular form of Article 243.

19. Measure the area of the pentagon of Problem 18 by perpendiculars and diagonals. (82-92.)

#### COMPASS-SURVEYING.

20. Set up the compass at any point, read and record the declination, and take the bearings of any four well-defined objects. Then change the declination slightly, record the reading, and again take the bearings of the four points. Take four such sets of readings. From each set of bearings thus obtained compute the angles between the four points, and compare the results by placing them in tabular form.

21. Determine the declination of the needle by taking the bearing of an established meridian. (260.)

22. Run out a line of constant bearing for a distance of half a mile, setting stakes every two hundred feet. Let the rodman pace the distances between the stations. Avoid setting the compass near anything that would be liable to attract the needle, and take a back-sight whenever local attraction is suspected. After completing the line, run back over it again by the reverse bearing. The rodman will note the discrepancy at each station between the old and the new stakes, and then destroy the old stakes.

23. Make a chain and compass survey by progression (166). Select an area bounded on one side by the edge of a bank or by a stream, and run a meander along the same, choosing the stations so as to inclose all of the desired area. The sketch should be drawn as nearly to scale as possible, and should contain information concerning all the features of the ground. Put the notes in tabular form, compute the latitude and departure of all the courses, and see that they check. Make a plat and calculate the area.

24. Measure a line along the surface of a sloping tract of ground. Measure the slope with the tangent scale of the compass, correct for the slope, and test the line by the ordinary method of chaining.

#### TRANSIT-SURVEYING.

25. Set up the transit at any point, and measure the angle between any two well-defined objects by repeating the angle five times, as described in Article 332. Read the vernier, and record the reading after the first and last measurement of the angle. If, in repeating, the  $360^\circ$  point be passed, add  $360^\circ$  the required number of times to the last reading. Divide the sum by five, and compare it with the single reading of the angle.

26. Survey the pentagon of Problem 18 by measuring the sides and interior angles. Calculate the bearings from the same assumed meridian, and note their agreement with those derived from the chain-survey.

27. Run out a square from one corner and note the error of closure. Make the sides several hundred feet long.

28. Repeat Problem 15—to prolong a line in azimuth and distance, using the transit to obtain the desired angles.

29. Survey a seven-sided field by traversing. (385.)

80. Measure a distance supposed to be inaccessible (874), and afterward compare result with a direct measurement.

81. Measure a line one end of which is supposed to be inaccessible (878), and then check the result by direct measurement.

82. *Traversing with Stadia Measurements.* Lay out an irregular polygon with sides from one hundred and fifty to two hundred and fifty feet in length. Read the traverse angles as in Problem 29, except that in taking a back-sight keep the telescope direct and change the readings of the verniers by  $180^\circ$ . Read the length of the sides and the vertical angle both when taking a fore-sight and when taking a back-sight. Find the corrected horizontal distances and differences of elevation. Note whether the algebraic sum of the latter is zero.

83. Measure a line supposed to be inaccessible, and afterward check by direct measurement. (881.)

84. Test the adjustments of the transit. (820-828.)

#### LEVELING.

85. Sight to a level-rod held at a distance of about two hundred feet, and have the rodman set the target as directed. The rodman will then read the rod and displace the target. Sight again at the rod, again direct the setting of the target, and have the rodman record the rod readings. Repeat this operation ten times and tabulate the results.

86. Sight to a speaking-rod like Fig. 887, and have the leveler read the rod. The rodman will read the vernier at the side at this same setting. Have the rodman move the front of the rod up slightly. Read the rod again, and have the rodman note the vernier reading again. The difference between the rod readings by the leveler and between the vernier readings should be the same in each case. Make ten observations of this kind and tabulate the results.

87. Run a line of levels over a series of designated stations, making a complete circuit and closing on the original starting-point. Use the third form of field-notes. (540.)

88. Make a profile of a designated line. (549.)

89. Determine the radius of curvature of the bubble-tube of the level. (505.)

40. Test the adjustments of the level. (518-528.)

#### GENERAL PROBLEMS.

41. From a point over three hundred feet from a given line let fall a perpendicular to the line, using successively the chain alone, the compass, and the transit, and note the difference in the results by the three different methods.

42. Select a point from which a series of points may be seen in different directions (such as lightning-rods, edges of buildings or chimneys, marks on posts or trees), so that a set of adjacent angles may be measured which will include the whole horizon. Measure and record these angles separately,

using successively the chain alone, the compass, and the transit, and note how near the sum of the angles in each of the three methods equals  $360^\circ$ .

43. Measure the height to a window in a building, treating it as a line, one end of which is inaccessible (Fig. 267). Let  $AB$  in that figure be the desired height, and  $AC$  a distance measured out from the building. Note the point on the building where the line of sight strikes when the telescope is level. This is the point  $A$ . Measure the angle of elevation,  $ACB$ , calculate the altitude,  $AB$ , and afterward check the result by measuring down from the window with a tape. It is best to have the distance out approximately equal to the height.

44. *Stadia Measurements.* Set up the transit over a point. Mark with stakes a series of points at distances varying from one hundred feet to five hundred feet from the instrument. Measure the height of the telescope axis above the ground. Measure the distances to points located in the following manner: Have the center cross-wire near to the point on the board corresponding to the height of instrument, making, however, the lower wire coincide with an even foot. This avoids the necessity of reading both wires. Read the distance, then set center wire at the exact height of instrument and read the vertical angle (page 241). Reduce the distance by (348). Measure the distances with a steel tape and compare with those given by the stadia.

45. Produce a line through a building by methods of (362), (363), and (366), using the transit, and compare results.

46. Measure a line with the gradienter (341-345), and check the result by measuring the line with a tape.



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**OR,**  
**LATITUDES AND DEPARTURES OF COURSES**  
**CALCULATED TO**  
**THREE DECIMAL PLACES:**  
**FOR**  
**EACH QUARTER DEGREE OF BEARING.**

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| Bearing. | 1     |       | 2     |       | 3     |       | 4     |       | 5     | Bearing. |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
|          | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  |          |
| 0°       | 1.000 | 0.000 | 2.000 | 0.000 | 3.000 | 0.000 | 4.000 | 0.000 | 5.000 | 90°      |
| 0 1/4    | 1.000 | 0.004 | 2.000 | 0.009 | 3.000 | 0.013 | 4.000 | 0.017 | 5.000 | 89 1/4   |
| 0 1/2    | 1.000 | 0.009 | 2.000 | 0.017 | 3.000 | 0.026 | 4.000 | 0.035 | 5.000 | 89 1/2   |
| 0 3/4    | 1.000 | 0.013 | 2.000 | 0.026 | 3.000 | 0.039 | 4.000 | 0.052 | 5.000 | 89 3/4   |
| 1°       | 1.000 | 0.017 | 2.000 | 0.035 | 3.000 | 0.052 | 3.999 | 0.070 | 4.999 | 89°      |
| 1 1/4    | 1.000 | 0.022 | 2.000 | 0.044 | 2.999 | 0.065 | 3.999 | 0.087 | 4.999 | 88 1/4   |
| 1 1/2    | 1.000 | 0.026 | 1.999 | 0.052 | 2.999 | 0.079 | 3.999 | 0.105 | 4.998 | 88 1/2   |
| 1 3/4    | 1.000 | 0.031 | 1.999 | 0.061 | 2.999 | 0.092 | 3.998 | 0.122 | 4.998 | 88 3/4   |
| 2°       | 0.999 | 0.035 | 1.999 | 0.070 | 2.998 | 0.105 | 3.998 | 0.140 | 4.997 | 88°      |
| 2 1/4    | 0.999 | 0.039 | 1.998 | 0.079 | 2.998 | 0.118 | 3.997 | 0.157 | 4.996 | 87 1/4   |
| 2 1/2    | 0.999 | 0.044 | 1.998 | 0.087 | 2.997 | 0.131 | 3.996 | 0.174 | 4.995 | 87 1/2   |
| 2 3/4    | 0.999 | 0.048 | 1.998 | 0.096 | 2.997 | 0.144 | 3.995 | 0.192 | 4.994 | 87 3/4   |
| 3°       | 0.999 | 0.052 | 1.997 | 0.105 | 2.996 | 0.157 | 3.995 | 0.209 | 4.993 | 87°      |
| 3 1/4    | 0.998 | 0.057 | 1.997 | 0.113 | 2.995 | 0.170 | 3.994 | 0.227 | 4.992 | 86 1/4   |
| 3 1/2    | 0.998 | 0.061 | 1.996 | 0.122 | 2.994 | 0.183 | 3.993 | 0.244 | 4.991 | 86 1/2   |
| 3 3/4    | 0.998 | 0.065 | 1.996 | 0.131 | 2.994 | 0.196 | 3.991 | 0.262 | 4.989 | 86 3/4   |
| 4°       | 0.998 | 0.070 | 1.995 | 0.140 | 2.993 | 0.209 | 3.990 | 0.279 | 4.988 | 86°      |
| 4 1/4    | 0.997 | 0.074 | 1.995 | 0.148 | 2.992 | 0.222 | 3.989 | 0.296 | 4.986 | 85 1/4   |
| 4 1/2    | 0.997 | 0.078 | 1.994 | 0.157 | 2.991 | 0.235 | 3.988 | 0.314 | 4.985 | 85 1/2   |
| 4 3/4    | 0.997 | 0.083 | 1.993 | 0.166 | 2.990 | 0.248 | 3.986 | 0.331 | 4.983 | 85 3/4   |
| 5°       | 0.996 | 0.087 | 1.992 | 0.174 | 2.989 | 0.261 | 3.985 | 0.349 | 4.981 | 85°      |
| 5 1/4    | 0.996 | 0.092 | 1.992 | 0.183 | 2.987 | 0.275 | 3.983 | 0.366 | 4.979 | 84 1/4   |
| 5 1/2    | 0.995 | 0.096 | 1.991 | 0.192 | 2.986 | 0.288 | 3.982 | 0.383 | 4.977 | 84 1/2   |
| 5 3/4    | 0.995 | 0.100 | 1.990 | 0.200 | 2.985 | 0.301 | 3.980 | 0.401 | 4.975 | 84 3/4   |
| 6°       | 0.995 | 0.105 | 1.989 | 0.209 | 2.984 | 0.314 | 3.978 | 0.418 | 4.973 | 84°      |
| 6 1/4    | 0.994 | 0.109 | 1.988 | 0.218 | 2.982 | 0.327 | 3.976 | 0.435 | 4.970 | 83 1/4   |
| 6 1/2    | 0.994 | 0.113 | 1.987 | 0.226 | 2.981 | 0.340 | 3.974 | 0.453 | 4.968 | 83 1/2   |
| 6 3/4    | 0.993 | 0.118 | 1.986 | 0.235 | 2.979 | 0.353 | 3.972 | 0.470 | 4.965 | 83 3/4   |
| 7°       | 0.993 | 0.122 | 1.985 | 0.244 | 2.978 | 0.366 | 3.970 | 0.487 | 4.963 | 83°      |
| 7 1/4    | 0.992 | 0.126 | 1.984 | 0.252 | 2.976 | 0.379 | 3.968 | 0.505 | 4.960 | 82 1/4   |
| 7 1/2    | 0.991 | 0.131 | 1.983 | 0.261 | 2.974 | 0.392 | 3.966 | 0.522 | 4.957 | 82 1/2   |
| 7 3/4    | 0.991 | 0.135 | 1.982 | 0.270 | 2.973 | 0.405 | 3.963 | 0.539 | 4.954 | 82 3/4   |
| 8°       | 0.990 | 0.139 | 1.981 | 0.278 | 2.971 | 0.418 | 3.961 | 0.557 | 4.951 | 82°      |
| 8 1/4    | 0.990 | 0.143 | 1.979 | 0.287 | 2.969 | 0.430 | 3.959 | 0.574 | 4.948 | 81 1/4   |
| 8 1/2    | 0.989 | 0.148 | 1.978 | 0.296 | 2.967 | 0.443 | 3.956 | 0.591 | 4.945 | 81 1/2   |
| 8 3/4    | 0.988 | 0.152 | 1.977 | 0.304 | 2.965 | 0.456 | 3.953 | 0.608 | 4.942 | 81 3/4   |
| 9°       | 0.988 | 0.156 | 1.975 | 0.313 | 2.963 | 0.469 | 3.951 | 0.626 | 4.938 | 81°      |
| 9 1/4    | 0.987 | 0.161 | 1.974 | 0.321 | 2.961 | 0.482 | 3.948 | 0.643 | 4.935 | 80 1/4   |
| 9 1/2    | 0.986 | 0.165 | 1.973 | 0.330 | 2.959 | 0.495 | 3.945 | 0.660 | 4.931 | 80 1/2   |
| 9 3/4    | 0.986 | 0.169 | 1.971 | 0.339 | 2.957 | 0.508 | 3.942 | 0.677 | 4.928 | 80 3/4   |
| 10°      | 0.985 | 0.174 | 1.970 | 0.347 | 2.954 | 0.521 | 3.939 | 0.695 | 4.924 | 80°      |
| 10 1/4   | 0.984 | 0.178 | 1.968 | 0.356 | 2.952 | 0.534 | 3.936 | 0.712 | 4.920 | 79 1/4   |
| 10 1/2   | 0.983 | 0.182 | 1.967 | 0.364 | 2.950 | 0.547 | 3.933 | 0.729 | 4.916 | 79 1/2   |
| 10 3/4   | 0.982 | 0.187 | 1.965 | 0.373 | 2.947 | 0.560 | 3.930 | 0.746 | 4.912 | 79 3/4   |
| 11°      | 0.982 | 0.191 | 1.963 | 0.382 | 2.945 | 0.572 | 3.927 | 0.763 | 4.908 | 79°      |
| 11 1/4   | 0.981 | 0.195 | 1.962 | 0.390 | 2.942 | 0.585 | 3.923 | 0.780 | 4.904 | 78 1/4   |
| 11 1/2   | 0.980 | 0.199 | 1.960 | 0.399 | 2.940 | 0.598 | 3.920 | 0.797 | 4.900 | 78 1/2   |
| 11 3/4   | 0.979 | 0.204 | 1.958 | 0.407 | 2.937 | 0.611 | 3.916 | 0.815 | 4.895 | 78 3/4   |
| 12°      | 0.978 | 0.208 | 1.956 | 0.416 | 2.934 | 0.624 | 3.913 | 0.832 | 4.891 | 78°      |
| 12 1/4   | 0.977 | 0.212 | 1.954 | 0.424 | 2.932 | 0.637 | 3.909 | 0.849 | 4.886 | 77 1/4   |
| 12 1/2   | 0.976 | 0.216 | 1.953 | 0.433 | 2.929 | 0.649 | 3.905 | 0.866 | 4.881 | 77 1/2   |
| 12 3/4   | 0.975 | 0.221 | 1.951 | 0.441 | 2.926 | 0.662 | 3.901 | 0.883 | 4.877 | 77 3/4   |
| 13°      | 0.974 | 0.225 | 1.949 | 0.450 | 2.923 | 0.675 | 3.897 | 0.900 | 4.872 | 77°      |
| 13 1/4   | 0.973 | 0.229 | 1.947 | 0.458 | 2.920 | 0.688 | 3.894 | 0.917 | 4.867 | 76 1/4   |
| 13 1/2   | 0.972 | 0.233 | 1.945 | 0.467 | 2.917 | 0.700 | 3.889 | 0.934 | 4.862 | 76 1/2   |
| 13 3/4   | 0.971 | 0.238 | 1.943 | 0.475 | 2.914 | 0.713 | 3.885 | 0.951 | 4.857 | 76 3/4   |
| 14°      | 0.970 | 0.242 | 1.941 | 0.484 | 2.911 | 0.726 | 3.881 | 0.968 | 4.851 | 76°      |
| 14 1/4   | 0.969 | 0.246 | 1.938 | 0.492 | 2.908 | 0.738 | 3.877 | 0.985 | 4.846 | 75 1/4   |
| 14 1/2   | 0.968 | 0.250 | 1.936 | 0.501 | 2.904 | 0.751 | 3.873 | 1.002 | 4.841 | 75 1/2   |
| 14 3/4   | 0.967 | 0.255 | 1.934 | 0.509 | 2.901 | 0.764 | 3.868 | 1.018 | 4.835 | 75 3/4   |
| 15°      | 0.966 | 0.259 | 1.932 | 0.518 | 2.898 | 0.776 | 3.864 | 1.035 | 4.830 | 75°      |
| Bearing. | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Bearing. |
|          | 1     |       | 2     |       | 3     |       | 4     |       | 5     |          |

# LATITUDES AND DEPARTURES.

| Bearing. | 5     |       | 6     |       | 7     |       | 8     |       | 9     |          | Bearing. |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|----------|
|          | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  |          |          |
| 0°       | 0.000 | 6.000 | 0.000 | 7.000 | 0.000 | 8.000 | 0.000 | 9.000 | 0.000 | 90°      |          |
| 0 1/2°   | 0.022 | 6.000 | 0.026 | 7.000 | 0.031 | 8.000 | 0.035 | 9.000 | 0.039 | 89 1/2°  |          |
| 0 1/4°   | 0.044 | 6.000 | 0.052 | 7.000 | 0.061 | 8.000 | 0.070 | 9.000 | 0.079 | 89 1/4°  |          |
| 0 3/4°   | 0.065 | 5.999 | 0.079 | 6.999 | 0.092 | 7.999 | 0.105 | 8.999 | 0.118 | 89 3/4°  |          |
| 1°       | 0.087 | 5.999 | 0.105 | 6.999 | 0.122 | 7.999 | 0.140 | 8.999 | 0.157 | 89°      |          |
| 1 1/2°   | 0.109 | 5.999 | 0.131 | 6.998 | 0.153 | 7.998 | 0.175 | 8.998 | 0.196 | 88 1/2°  |          |
| 1 1/4°   | 0.131 | 5.998 | 0.157 | 6.998 | 0.183 | 7.997 | 0.209 | 8.997 | 0.236 | 88 1/4°  |          |
| 1 3/4°   | 0.153 | 5.997 | 0.183 | 6.997 | 0.214 | 7.996 | 0.244 | 8.996 | 0.275 | 88 3/4°  |          |
| 2°       | 0.174 | 5.996 | 0.209 | 6.996 | 0.244 | 7.995 | 0.279 | 8.995 | 0.314 | 88°      |          |
| 2 1/2°   | 0.196 | 5.995 | 0.236 | 6.995 | 0.275 | 7.994 | 0.314 | 8.993 | 0.353 | 87 1/2°  |          |
| 2 1/4°   | 0.218 | 5.994 | 0.262 | 6.993 | 0.305 | 7.992 | 0.349 | 8.991 | 0.393 | 87 1/4°  |          |
| 2 3/4°   | 0.240 | 5.993 | 0.288 | 6.992 | 0.336 | 7.991 | 0.384 | 8.990 | 0.432 | 87 3/4°  |          |
| 3°       | 0.262 | 5.992 | 0.314 | 6.990 | 0.366 | 7.989 | 0.419 | 8.988 | 0.471 | 87°      |          |
| 3 1/2°   | 0.283 | 5.990 | 0.340 | 6.989 | 0.397 | 7.987 | 0.454 | 8.986 | 0.510 | 86 1/2°  |          |
| 3 1/4°   | 0.305 | 5.989 | 0.366 | 6.987 | 0.427 | 7.985 | 0.488 | 8.983 | 0.549 | 86 1/4°  |          |
| 3 3/4°   | 0.327 | 5.987 | 0.392 | 6.985 | 0.458 | 7.983 | 0.523 | 8.981 | 0.589 | 86 3/4°  |          |
| 4°       | 0.349 | 5.985 | 0.419 | 6.983 | 0.488 | 7.981 | 0.558 | 8.978 | 0.628 | 86°      |          |
| 4 1/2°   | 0.371 | 5.984 | 0.445 | 6.981 | 0.519 | 7.978 | 0.593 | 8.975 | 0.667 | 85 1/2°  |          |
| 4 1/4°   | 0.392 | 5.982 | 0.471 | 6.978 | 0.549 | 7.975 | 0.628 | 8.972 | 0.706 | 85 1/4°  |          |
| 4 3/4°   | 0.414 | 5.979 | 0.497 | 6.976 | 0.580 | 7.973 | 0.662 | 8.969 | 0.745 | 85 3/4°  |          |
| 5°       | 0.436 | 5.977 | 0.523 | 6.973 | 0.610 | 7.970 | 0.697 | 8.966 | 0.784 | 85°      |          |
| 5 1/2°   | 0.458 | 5.975 | 0.549 | 6.971 | 0.641 | 7.966 | 0.732 | 8.962 | 0.824 | 84 1/2°  |          |
| 5 1/4°   | 0.479 | 5.972 | 0.575 | 6.968 | 0.671 | 7.963 | 0.767 | 8.959 | 0.863 | 84 1/4°  |          |
| 5 3/4°   | 0.501 | 5.970 | 0.601 | 6.965 | 0.701 | 7.960 | 0.802 | 8.955 | 0.902 | 84 3/4°  |          |
| 6°       | 0.523 | 5.967 | 0.627 | 6.962 | 0.732 | 7.956 | 0.836 | 8.951 | 0.941 | 84°      |          |
| 6 1/2°   | 0.544 | 5.964 | 0.653 | 6.958 | 0.762 | 7.952 | 0.871 | 8.947 | 0.980 | 83 1/2°  |          |
| 6 1/4°   | 0.566 | 5.961 | 0.679 | 6.955 | 0.792 | 7.949 | 0.906 | 8.942 | 1.019 | 83 1/4°  |          |
| 6 3/4°   | 0.588 | 5.958 | 0.705 | 6.951 | 0.823 | 7.945 | 0.940 | 8.938 | 1.058 | 83 3/4°  |          |
| 7°       | 0.609 | 5.955 | 0.731 | 6.948 | 0.853 | 7.940 | 0.975 | 8.933 | 1.097 | 83°      |          |
| 7 1/2°   | 0.631 | 5.952 | 0.757 | 6.944 | 0.883 | 7.936 | 1.010 | 8.928 | 1.136 | 82 1/2°  |          |
| 7 1/4°   | 0.653 | 5.949 | 0.783 | 6.940 | 0.914 | 7.932 | 1.044 | 8.923 | 1.175 | 82 1/4°  |          |
| 7 3/4°   | 0.674 | 5.945 | 0.809 | 6.936 | 0.944 | 7.927 | 1.079 | 8.918 | 1.214 | 82 3/4°  |          |
| 8°       | 0.696 | 5.942 | 0.835 | 6.932 | 0.974 | 7.922 | 1.113 | 8.912 | 1.253 | 82°      |          |
| 8 1/2°   | 0.717 | 5.938 | 0.861 | 6.928 | 1.004 | 7.917 | 1.148 | 8.907 | 1.291 | 81 1/2°  |          |
| 8 1/4°   | 0.739 | 5.934 | 0.887 | 6.923 | 1.035 | 7.912 | 1.182 | 8.901 | 1.330 | 81 1/4°  |          |
| 8 3/4°   | 0.761 | 5.930 | 0.913 | 6.919 | 1.065 | 7.907 | 1.217 | 8.895 | 1.369 | 81 3/4°  |          |
| 9°       | 0.782 | 5.926 | 0.939 | 6.914 | 1.095 | 7.902 | 1.251 | 8.889 | 1.408 | 81°      |          |
| 9 1/2°   | 0.804 | 5.922 | 0.964 | 6.909 | 1.125 | 7.896 | 1.286 | 8.883 | 1.447 | 80 1/2°  |          |
| 9 1/4°   | 0.825 | 5.918 | 0.990 | 6.904 | 1.155 | 7.890 | 1.320 | 8.877 | 1.485 | 80 1/4°  |          |
| 9 3/4°   | 0.847 | 5.913 | 1.016 | 6.899 | 1.185 | 7.884 | 1.355 | 8.870 | 1.524 | 80 3/4°  |          |
| 10°      | 0.868 | 5.909 | 1.042 | 6.894 | 1.216 | 7.878 | 1.389 | 8.863 | 1.563 | 80°      |          |
| 10 1/2°  | 0.890 | 5.904 | 1.068 | 6.888 | 1.246 | 7.872 | 1.424 | 8.856 | 1.601 | 79 1/2°  |          |
| 10 1/4°  | 0.911 | 5.900 | 1.093 | 6.883 | 1.276 | 7.866 | 1.458 | 8.849 | 1.640 | 79 1/4°  |          |
| 10 3/4°  | 0.933 | 5.895 | 1.119 | 6.877 | 1.306 | 7.860 | 1.492 | 8.842 | 1.679 | 79 3/4°  |          |
| 11°      | 0.954 | 5.890 | 1.145 | 6.871 | 1.336 | 7.853 | 1.526 | 8.835 | 1.717 | 79°      |          |
| 11 1/2°  | 0.975 | 5.885 | 1.171 | 6.866 | 1.366 | 7.846 | 1.561 | 8.827 | 1.756 | 78 1/2°  |          |
| 11 1/4°  | 0.997 | 5.880 | 1.196 | 6.859 | 1.396 | 7.839 | 1.595 | 8.819 | 1.794 | 78 1/4°  |          |
| 11 3/4°  | 1.018 | 5.874 | 1.222 | 6.853 | 1.425 | 7.832 | 1.629 | 8.811 | 1.833 | 78 3/4°  |          |
| 12°      | 1.040 | 5.869 | 1.247 | 6.847 | 1.455 | 7.825 | 1.663 | 8.803 | 1.871 | 78°      |          |
| 12 1/2°  | 1.061 | 5.863 | 1.273 | 6.841 | 1.485 | 7.818 | 1.697 | 8.795 | 1.910 | 77 1/2°  |          |
| 12 1/4°  | 1.082 | 5.858 | 1.299 | 6.834 | 1.515 | 7.810 | 1.732 | 8.787 | 1.948 | 77 1/4°  |          |
| 12 3/4°  | 1.103 | 5.852 | 1.324 | 6.827 | 1.545 | 7.803 | 1.766 | 8.778 | 1.986 | 77 3/4°  |          |
| 13°      | 1.125 | 5.846 | 1.350 | 6.821 | 1.575 | 7.795 | 1.800 | 8.769 | 2.025 | 77°      |          |
| 13 1/2°  | 1.146 | 5.840 | 1.375 | 6.814 | 1.604 | 7.787 | 1.834 | 8.760 | 2.063 | 76 1/2°  |          |
| 13 1/4°  | 1.167 | 5.834 | 1.401 | 6.807 | 1.634 | 7.779 | 1.868 | 8.751 | 2.101 | 76 1/4°  |          |
| 13 3/4°  | 1.188 | 5.828 | 1.426 | 6.799 | 1.664 | 7.771 | 1.902 | 8.742 | 2.139 | 76 3/4°  |          |
| 14°      | 1.210 | 5.822 | 1.452 | 6.792 | 1.693 | 7.762 | 1.935 | 8.733 | 2.177 | 76°      |          |
| 14 1/2°  | 1.231 | 5.815 | 1.477 | 6.785 | 1.723 | 7.754 | 1.969 | 8.723 | 2.215 | 75 1/2°  |          |
| 14 1/4°  | 1.252 | 5.809 | 1.502 | 6.777 | 1.753 | 7.745 | 2.003 | 8.713 | 2.253 | 75 1/4°  |          |
| 14 3/4°  | 1.273 | 5.802 | 1.528 | 6.769 | 1.782 | 7.736 | 2.037 | 8.703 | 2.291 | 75 3/4°  |          |
| 15°      | 1.294 | 5.796 | 1.553 | 6.761 | 1.812 | 7.727 | 2.071 | 8.693 | 2.329 | 75°      |          |
| Bearing. | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Bearing. |          |
|          | 5     | 6     |       | 7     |       | 8     |       | 9     |       |          |          |

# LATITUDES AND DEPARTURES.

| Bearing. | 1     |       | 2     |       | 3     |       | 4     |       | 5     | Bearing. |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
|          | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  |          |
| 15°      | 0.966 | 0.259 | 1.932 | 0.518 | 2.898 | 0.776 | 3.864 | 1.035 | 4.830 | 75°      |
| 15½      | 0.965 | 0.263 | 1.930 | 0.526 | 2.894 | 0.789 | 3.859 | 1.052 | 4.824 | 74½      |
| 15½      | 0.964 | 0.267 | 1.927 | 0.534 | 2.891 | 0.802 | 3.855 | 1.069 | 4.818 | 74½      |
| 15½      | 0.962 | 0.271 | 1.925 | 0.543 | 2.887 | 0.814 | 3.850 | 1.086 | 4.812 | 74½      |
| 16°      | 0.961 | 0.276 | 1.923 | 0.551 | 2.884 | 0.827 | 3.845 | 1.103 | 4.806 | 74°      |
| 16½      | 0.960 | 0.280 | 1.920 | 0.560 | 2.880 | 0.839 | 3.840 | 1.119 | 4.800 | 73½      |
| 16½      | 0.959 | 0.284 | 1.918 | 0.568 | 2.876 | 0.852 | 3.835 | 1.136 | 4.794 | 73½      |
| 16½      | 0.958 | 0.288 | 1.915 | 0.576 | 2.873 | 0.865 | 3.830 | 1.153 | 4.788 | 73½      |
| 17°      | 0.956 | 0.292 | 1.913 | 0.585 | 2.869 | 0.877 | 3.825 | 1.169 | 4.782 | 73°      |
| 17½      | 0.955 | 0.297 | 1.910 | 0.593 | 2.865 | 0.890 | 3.820 | 1.186 | 4.775 | 72½      |
| 17½      | 0.954 | 0.301 | 1.907 | 0.601 | 2.861 | 0.902 | 3.815 | 1.203 | 4.769 | 72½      |
| 17½      | 0.952 | 0.305 | 1.905 | 0.610 | 2.857 | 0.915 | 3.810 | 1.220 | 4.762 | 72½      |
| 18°      | 0.951 | 0.309 | 1.902 | 0.618 | 2.853 | 0.927 | 3.804 | 1.236 | 4.755 | 72°      |
| 18½      | 0.950 | 0.313 | 1.899 | 0.626 | 2.849 | 0.939 | 3.799 | 1.253 | 4.748 | 71½      |
| 18½      | 0.948 | 0.317 | 1.897 | 0.635 | 2.845 | 0.952 | 3.793 | 1.269 | 4.742 | 71½      |
| 18½      | 0.947 | 0.321 | 1.894 | 0.643 | 2.841 | 0.964 | 3.788 | 1.286 | 4.735 | 71½      |
| 19°      | 0.946 | 0.326 | 1.891 | 0.651 | 2.837 | 0.977 | 3.782 | 1.302 | 4.728 | 71°      |
| 19½      | 0.944 | 0.330 | 1.888 | 0.659 | 2.832 | 0.989 | 3.776 | 1.319 | 4.720 | 70½      |
| 19½      | 0.943 | 0.334 | 1.885 | 0.666 | 2.828 | 1.001 | 3.771 | 1.335 | 4.713 | 70½      |
| 19½      | 0.941 | 0.338 | 1.882 | 0.676 | 2.824 | 1.014 | 3.765 | 1.352 | 4.706 | 70½      |
|          |       |       |       |       |       |       |       |       |       |          |
| 20°      | 0.940 | 0.342 | 1.879 | 0.684 | 2.819 | 1.026 | 3.759 | 1.368 | 4.698 | 70°      |
| 20½      | 0.938 | 0.346 | 1.876 | 0.692 | 2.815 | 1.038 | 3.753 | 1.384 | 4.691 | 69½      |
| 20½      | 0.937 | 0.350 | 1.873 | 0.700 | 2.810 | 1.051 | 3.747 | 1.401 | 4.683 | 69½      |
| 20½      | 0.935 | 0.354 | 1.870 | 0.709 | 2.805 | 1.063 | 3.741 | 1.417 | 4.676 | 69½      |
| 21°      | 0.934 | 0.358 | 1.867 | 0.717 | 2.801 | 1.075 | 3.734 | 1.433 | 4.668 | 69°      |
| 21½      | 0.932 | 0.362 | 1.864 | 0.725 | 2.796 | 1.087 | 3.728 | 1.450 | 4.660 | 68½      |
| 21½      | 0.930 | 0.367 | 1.861 | 0.733 | 2.791 | 1.100 | 3.722 | 1.466 | 4.652 | 68½      |
| 21½      | 0.929 | 0.371 | 1.858 | 0.741 | 2.786 | 1.112 | 3.715 | 1.482 | 4.644 | 68½      |
| 22°      | 0.927 | 0.375 | 1.854 | 0.749 | 2.782 | 1.124 | 3.709 | 1.498 | 4.636 | 68°      |
| 22½      | 0.926 | 0.379 | 1.851 | 0.757 | 2.777 | 1.136 | 3.702 | 1.515 | 4.628 | 67½      |
| 22½      | 0.924 | 0.383 | 1.848 | 0.765 | 2.772 | 1.148 | 3.696 | 1.531 | 4.619 | 67½      |
| 22½      | 0.922 | 0.387 | 1.844 | 0.773 | 2.767 | 1.160 | 3.689 | 1.547 | 4.611 | 67½      |
| 23°      | 0.921 | 0.391 | 1.841 | 0.781 | 2.762 | 1.172 | 3.682 | 1.563 | 4.603 | 67°      |
| 23½      | 0.919 | 0.395 | 1.838 | 0.789 | 2.756 | 1.184 | 3.675 | 1.579 | 4.594 | 66½      |
| 23½      | 0.917 | 0.399 | 1.834 | 0.797 | 2.751 | 1.196 | 3.668 | 1.595 | 4.585 | 66½      |
| 23½      | 0.915 | 0.403 | 1.831 | 0.805 | 2.746 | 1.208 | 3.661 | 1.611 | 4.577 | 66½      |
| 24°      | 0.914 | 0.407 | 1.827 | 0.813 | 2.741 | 1.220 | 3.654 | 1.627 | 4.568 | 66°      |
| 24½      | 0.912 | 0.411 | 1.824 | 0.821 | 2.735 | 1.232 | 3.647 | 1.643 | 4.559 | 65½      |
| 24½      | 0.910 | 0.415 | 1.820 | 0.829 | 2.730 | 1.244 | 3.640 | 1.659 | 4.550 | 65½      |
| 24½      | 0.908 | 0.419 | 1.816 | 0.837 | 2.724 | 1.256 | 3.633 | 1.675 | 4.541 | 65½      |
|          |       |       |       |       |       |       |       |       |       |          |
| 25°      | 0.906 | 0.423 | 1.813 | 0.845 | 2.719 | 1.268 | 3.625 | 1.690 | 4.532 | 65°      |
| 25½      | 0.904 | 0.427 | 1.809 | 0.853 | 2.713 | 1.280 | 3.618 | 1.706 | 4.522 | 64½      |
| 25½      | 0.903 | 0.431 | 1.805 | 0.861 | 2.708 | 1.292 | 3.610 | 1.722 | 4.513 | 64½      |
| 25½      | 0.901 | 0.434 | 1.801 | 0.869 | 2.702 | 1.303 | 3.603 | 1.738 | 4.503 | 64½      |
| 26°      | 0.899 | 0.438 | 1.798 | 0.877 | 2.696 | 1.315 | 3.595 | 1.753 | 4.494 | 64°      |
| 26½      | 0.897 | 0.442 | 1.794 | 0.885 | 2.691 | 1.327 | 3.587 | 1.769 | 4.484 | 63½      |
| 26½      | 0.895 | 0.446 | 1.790 | 0.892 | 2.685 | 1.339 | 3.580 | 1.785 | 4.475 | 63½      |
| 26½      | 0.893 | 0.450 | 1.786 | 0.900 | 2.679 | 1.350 | 3.572 | 1.800 | 4.465 | 63½      |
| 27°      | 0.891 | 0.454 | 1.782 | 0.908 | 2.673 | 1.362 | 3.564 | 1.816 | 4.455 | 63°      |
| 27½      | 0.889 | 0.458 | 1.778 | 0.916 | 2.667 | 1.374 | 3.556 | 1.831 | 4.445 | 62½      |
| 27½      | 0.887 | 0.462 | 1.774 | 0.923 | 2.661 | 1.385 | 3.548 | 1.847 | 4.435 | 62½      |
| 27½      | 0.885 | 0.466 | 1.770 | 0.931 | 2.655 | 1.397 | 3.540 | 1.862 | 4.425 | 62½      |
| 28°      | 0.883 | 0.469 | 1.766 | 0.939 | 2.649 | 1.408 | 3.532 | 1.878 | 4.415 | 62°      |
| 28½      | 0.881 | 0.473 | 1.762 | 0.947 | 2.643 | 1.420 | 3.524 | 1.893 | 4.404 | 61½      |
| 28½      | 0.879 | 0.477 | 1.758 | 0.954 | 2.636 | 1.431 | 3.515 | 1.909 | 4.394 | 61½      |
| 28½      | 0.877 | 0.481 | 1.753 | 0.962 | 2.630 | 1.443 | 3.507 | 1.924 | 4.384 | 61½      |
| 29°      | 0.875 | 0.485 | 1.749 | 0.970 | 2.624 | 1.454 | 3.498 | 1.939 | 4.373 | 61°      |
| 29½      | 0.872 | 0.489 | 1.745 | 0.977 | 2.617 | 1.466 | 3.490 | 1.954 | 4.362 | 60½      |
| 29½      | 0.870 | 0.492 | 1.741 | 0.985 | 2.611 | 1.477 | 3.481 | 1.970 | 4.352 | 60½      |
| 29½      | 0.868 | 0.496 | 1.736 | 0.992 | 2.605 | 1.489 | 3.473 | 1.985 | 4.341 | 60½      |
| 30°      | 0.866 | 0.500 | 1.732 | 1.000 | 2.598 | 1.500 | 3.464 | 2.000 | 4.330 | 60°      |
| Bearing. | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Bearing. |
| 1        |       | 2     |       | 3     |       | 4     |       | 5     |       |          |

# LATITUDES AND DEPARTURES.

| Bearing. | 5     |       | 6     |       | 7     |       | 8     |       | 9     |          | Bearing. |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|----------|
|          | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.     |          |
| 15°      | 1.294 | 5.796 | 1.553 | 6.761 | 1.812 | 7.727 | 2.071 | 8.693 | 2.329 | 75°      |          |
| 15½      | 1.315 | 5.789 | 1.578 | 6.754 | 1.841 | 7.718 | 2.104 | 8.683 | 2.367 | 74½      |          |
| 15¼      | 1.336 | 5.782 | 1.603 | 6.745 | 1.871 | 7.709 | 2.138 | 8.673 | 2.405 | 74¼      |          |
| 15½      | 1.357 | 5.775 | 1.629 | 6.737 | 1.900 | 7.700 | 2.172 | 8.662 | 2.443 | 74½      |          |
| 16°      | 1.378 | 5.768 | 1.654 | 6.729 | 1.929 | 7.690 | 2.205 | 8.651 | 2.481 | 74°      |          |
| 16¼      | 1.399 | 5.760 | 1.679 | 6.720 | 1.959 | 7.680 | 2.239 | 8.640 | 2.518 | 73¾      |          |
| 16½      | 1.420 | 5.753 | 1.704 | 6.712 | 1.988 | 7.671 | 2.272 | 8.629 | 2.556 | 73½      |          |
| 16¾      | 1.441 | 5.745 | 1.729 | 6.703 | 2.017 | 7.661 | 2.306 | 8.618 | 2.594 | 73¼      |          |
| 17°      | 1.462 | 5.738 | 1.754 | 6.694 | 2.047 | 7.650 | 2.339 | 8.607 | 2.631 | 73°      |          |
| 17¼      | 1.483 | 5.730 | 1.779 | 6.685 | 2.076 | 7.640 | 2.372 | 8.595 | 2.669 | 72¾      |          |
| 17½      | 1.504 | 5.722 | 1.804 | 6.676 | 2.105 | 7.630 | 2.406 | 8.583 | 2.706 | 72½      |          |
| 17¾      | 1.524 | 5.714 | 1.829 | 6.667 | 2.134 | 7.619 | 2.439 | 8.572 | 2.744 | 72¼      |          |
| 18°      | 1.545 | 5.706 | 1.854 | 6.657 | 2.163 | 7.608 | 2.472 | 8.560 | 2.781 | 72°      |          |
| 18¼      | 1.566 | 5.698 | 1.879 | 6.648 | 2.192 | 7.598 | 2.505 | 8.547 | 2.818 | 71¾      |          |
| 18½      | 1.587 | 5.690 | 1.904 | 6.638 | 2.221 | 7.587 | 2.538 | 8.535 | 2.856 | 71½      |          |
| 18¾      | 1.607 | 5.682 | 1.929 | 6.629 | 2.250 | 7.575 | 2.572 | 8.522 | 2.893 | 71¼      |          |
| 19°      | 1.628 | 5.673 | 1.953 | 6.619 | 2.279 | 7.564 | 2.605 | 8.510 | 2.930 | 71°      |          |
| 19¼      | 1.648 | 5.665 | 1.978 | 6.609 | 2.308 | 7.553 | 2.638 | 8.497 | 2.967 | 70¾      |          |
| 19½      | 1.669 | 5.656 | 2.003 | 6.598 | 2.337 | 7.541 | 2.670 | 8.484 | 3.004 | 70½      |          |
| 19¾      | 1.690 | 5.647 | 2.028 | 6.588 | 2.365 | 7.529 | 2.703 | 8.471 | 3.041 | 70¼      |          |
|          |       |       |       |       |       |       |       |       |       |          |          |
| 20°      | 1.710 | 5.638 | 2.052 | 6.578 | 2.394 | 7.518 | 2.736 | 8.457 | 3.078 | 70°      |          |
| 20¼      | 1.731 | 5.629 | 2.077 | 6.567 | 2.423 | 7.506 | 2.769 | 8.444 | 3.115 | 69¾      |          |
| 20½      | 1.751 | 5.620 | 2.101 | 6.557 | 2.451 | 7.493 | 2.802 | 8.430 | 3.152 | 69½      |          |
| 20¾      | 1.771 | 5.611 | 2.126 | 6.546 | 2.480 | 7.481 | 2.834 | 8.416 | 3.189 | 69¼      |          |
| 21°      | 1.792 | 5.601 | 2.150 | 6.535 | 2.509 | 7.469 | 2.867 | 8.402 | 3.225 | 69°      |          |
| 21¼      | 1.812 | 5.592 | 2.175 | 6.524 | 2.537 | 7.456 | 2.900 | 8.388 | 3.262 | 68¾      |          |
| 21½      | 1.833 | 5.582 | 2.199 | 6.513 | 2.566 | 7.443 | 2.932 | 8.374 | 3.299 | 68½      |          |
| 21¾      | 1.853 | 5.573 | 2.223 | 6.502 | 2.594 | 7.430 | 2.964 | 8.359 | 3.335 | 68¼      |          |
| 22°      | 1.873 | 5.563 | 2.248 | 6.490 | 2.622 | 7.417 | 2.997 | 8.345 | 3.371 | 68°      |          |
| 22¼      | 1.893 | 5.553 | 2.272 | 6.479 | 2.651 | 7.404 | 3.029 | 8.330 | 3.408 | 67¾      |          |
| 22½      | 1.913 | 5.543 | 2.296 | 6.467 | 2.679 | 7.391 | 3.061 | 8.315 | 3.444 | 67½      |          |
| 22¾      | 1.934 | 5.533 | 2.320 | 6.455 | 2.707 | 7.378 | 3.094 | 8.300 | 3.480 | 67¼      |          |
| 23°      | 1.954 | 5.523 | 2.344 | 6.444 | 2.735 | 7.364 | 3.126 | 8.285 | 3.517 | 67°      |          |
| 23¼      | 1.974 | 5.513 | 2.368 | 6.432 | 2.763 | 7.350 | 3.158 | 8.269 | 3.553 | 66¾      |          |
| 23½      | 1.994 | 5.502 | 2.392 | 6.419 | 2.791 | 7.336 | 3.190 | 8.254 | 3.589 | 66½      |          |
| 23¾      | 2.014 | 5.492 | 2.416 | 6.407 | 2.819 | 7.322 | 3.222 | 8.238 | 3.625 | 66¼      |          |
| 24°      | 2.034 | 5.481 | 2.440 | 6.395 | 2.847 | 7.308 | 3.254 | 8.222 | 3.661 | 66°      |          |
| 24¼      | 2.054 | 5.471 | 2.464 | 6.382 | 2.875 | 7.294 | 3.286 | 8.206 | 3.696 | 65¾      |          |
| 24½      | 2.073 | 5.460 | 2.488 | 6.370 | 2.903 | 7.280 | 3.318 | 8.190 | 3.732 | 65½      |          |
| 24¾      | 2.093 | 5.449 | 2.512 | 6.357 | 2.931 | 7.265 | 3.349 | 8.173 | 3.768 | 65¼      |          |
|          |       |       |       |       |       |       |       |       |       |          |          |
| 25°      | 2.113 | 5.438 | 2.536 | 6.344 | 2.958 | 7.250 | 3.381 | 8.157 | 3.804 | 65°      |          |
| 25¼      | 2.133 | 5.427 | 2.559 | 6.331 | 2.986 | 7.236 | 3.413 | 8.140 | 3.839 | 64¾      |          |
| 25½      | 2.153 | 5.416 | 2.583 | 6.318 | 3.014 | 7.221 | 3.444 | 8.123 | 3.875 | 64½      |          |
| 25¾      | 2.172 | 5.404 | 2.607 | 6.305 | 3.041 | 7.206 | 3.476 | 8.106 | 3.910 | 64¼      |          |
| 26°      | 2.192 | 5.393 | 2.630 | 6.292 | 3.069 | 7.190 | 3.507 | 8.089 | 3.945 | 64°      |          |
| 26¼      | 2.211 | 5.381 | 2.654 | 6.278 | 3.096 | 7.175 | 3.538 | 8.072 | 3.981 | 63¾      |          |
| 26½      | 2.231 | 5.370 | 2.677 | 6.265 | 3.123 | 7.160 | 3.570 | 8.054 | 4.016 | 63½      |          |
| 26¾      | 2.250 | 5.358 | 2.701 | 6.251 | 3.151 | 7.144 | 3.601 | 8.037 | 4.051 | 63¼      |          |
| 27°      | 2.270 | 5.346 | 2.724 | 6.237 | 3.178 | 7.128 | 3.632 | 8.019 | 4.086 | 63°      |          |
| 27¼      | 2.289 | 5.334 | 2.747 | 6.223 | 3.205 | 7.112 | 3.663 | 8.001 | 4.121 | 62¾      |          |
| 27½      | 2.309 | 5.322 | 2.770 | 6.209 | 3.232 | 7.096 | 3.694 | 7.983 | 4.156 | 62½      |          |
| 27¾      | 2.328 | 5.310 | 2.794 | 6.195 | 3.259 | 7.080 | 3.725 | 7.965 | 4.190 | 62¼      |          |
| 28°      | 2.347 | 5.298 | 2.817 | 6.181 | 3.286 | 7.064 | 3.756 | 7.947 | 4.225 | 62°      |          |
| 28¼      | 2.367 | 5.285 | 2.840 | 6.166 | 3.313 | 7.047 | 3.787 | 7.928 | 4.260 | 61¾      |          |
| 28½      | 2.386 | 5.273 | 2.863 | 6.152 | 3.340 | 7.031 | 3.817 | 7.909 | 4.294 | 61½      |          |
| 28¾      | 2.405 | 5.260 | 2.886 | 6.137 | 3.367 | 7.014 | 3.848 | 7.891 | 4.329 | 61¼      |          |
| 29°      | 2.424 | 5.248 | 2.909 | 6.122 | 3.394 | 6.997 | 3.878 | 7.872 | 4.363 | 61°      |          |
| 29¼      | 2.443 | 5.235 | 2.932 | 6.107 | 3.420 | 6.980 | 3.909 | 7.852 | 4.398 | 60¾      |          |
| 29½      | 2.462 | 5.222 | 2.955 | 6.093 | 3.447 | 6.963 | 3.939 | 7.833 | 4.432 | 60½      |          |
| 29¾      | 2.481 | 5.209 | 2.977 | 6.077 | 3.474 | 6.946 | 3.970 | 7.814 | 4.466 | 60¼      |          |
| 30°      | 2.500 | 5.196 | 3.000 | 6.062 | 3.501 | 6.928 | 4.000 | 7.794 | 4.500 | 60°      |          |
| Bearing. | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Bearing. |          |
|          | 5     | 6     | 7     | 8     | 9     |       |       |       |       |          |          |

# LATITUDES AND DEPARTURES.

| Bearing. | 1     |       | 2     |       | 3     |       | 4     |       | 5     | Bearing. |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
|          | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  |          |
| 30°      | 0.866 | 0.500 | 1.732 | 1.000 | 2.598 | 1.500 | 3.464 | 2.000 | 4.330 | 60°      |
| 30½      | 0.864 | 0.504 | 1.728 | 1.008 | 2.592 | 1.511 | 3.455 | 2.015 | 4.319 | 59½      |
| 30½      | 0.862 | 0.508 | 1.723 | 1.015 | 2.585 | 1.523 | 3.447 | 2.030 | 4.308 | 59½      |
| 30½      | 0.859 | 0.511 | 1.719 | 1.023 | 2.578 | 1.534 | 3.438 | 2.045 | 4.297 | 59½      |
| 31°      | 0.857 | 0.515 | 1.714 | 1.030 | 2.572 | 1.545 | 3.429 | 2.060 | 4.286 | 59°      |
| 31½      | 0.855 | 0.519 | 1.710 | 1.038 | 2.565 | 1.556 | 3.420 | 2.075 | 4.275 | 58½      |
| 31½      | 0.853 | 0.522 | 1.705 | 1.045 | 2.558 | 1.567 | 3.411 | 2.090 | 4.263 | 58½      |
| 31½      | 0.850 | 0.526 | 1.701 | 1.052 | 2.551 | 1.579 | 3.401 | 2.105 | 4.252 | 58½      |
| 32°      | 0.848 | 0.530 | 1.696 | 1.060 | 2.544 | 1.590 | 3.392 | 2.120 | 4.240 | 58°      |
| 32½      | 0.846 | 0.534 | 1.691 | 1.067 | 2.537 | 1.601 | 3.383 | 2.134 | 4.229 | 57½      |
| 32½      | 0.843 | 0.537 | 1.687 | 1.075 | 2.530 | 1.612 | 3.374 | 2.149 | 4.217 | 57½      |
| 32½      | 0.841 | 0.541 | 1.682 | 1.082 | 2.523 | 1.623 | 3.364 | 2.164 | 4.205 | 57½      |
| 33°      | 0.839 | 0.545 | 1.677 | 1.089 | 2.516 | 1.634 | 3.355 | 2.179 | 4.193 | 57°      |
| 33½      | 0.836 | 0.548 | 1.673 | 1.097 | 2.509 | 1.645 | 3.345 | 2.193 | 4.181 | 56½      |
| 33½      | 0.834 | 0.552 | 1.668 | 1.104 | 2.502 | 1.656 | 3.336 | 2.208 | 4.169 | 56½      |
| 33½      | 0.831 | 0.556 | 1.663 | 1.111 | 2.494 | 1.667 | 3.326 | 2.222 | 4.157 | 56½      |
| 34°      | 0.829 | 0.559 | 1.658 | 1.118 | 2.487 | 1.678 | 3.316 | 2.237 | 4.145 | 56°      |
| 34½      | 0.827 | 0.563 | 1.653 | 1.126 | 2.480 | 1.688 | 3.306 | 2.251 | 4.133 | 55½      |
| 34½      | 0.824 | 0.566 | 1.648 | 1.133 | 2.472 | 1.699 | 3.297 | 2.266 | 4.121 | 55½      |
| 34½      | 0.822 | 0.570 | 1.643 | 1.140 | 2.465 | 1.710 | 3.287 | 2.280 | 4.108 | 55½      |
|          |       |       |       |       |       |       |       |       |       |          |
| 35°      | 0.819 | 0.574 | 1.638 | 1.147 | 2.457 | 1.721 | 3.277 | 2.294 | 4.096 | 55°      |
| 35½      | 0.817 | 0.577 | 1.633 | 1.154 | 2.450 | 1.731 | 3.267 | 2.309 | 4.083 | 54½      |
| 35½      | 0.814 | 0.581 | 1.628 | 1.161 | 2.442 | 1.742 | 3.257 | 2.323 | 4.071 | 54½      |
| 35½      | 0.812 | 0.584 | 1.623 | 1.168 | 2.435 | 1.753 | 3.246 | 2.337 | 4.058 | 54½      |
| 36°      | 0.809 | 0.588 | 1.618 | 1.176 | 2.427 | 1.763 | 3.236 | 2.351 | 4.045 | 54°      |
| 36½      | 0.806 | 0.591 | 1.613 | 1.183 | 2.419 | 1.774 | 3.226 | 2.365 | 4.032 | 53½      |
| 36½      | 0.804 | 0.595 | 1.608 | 1.190 | 2.412 | 1.784 | 3.215 | 2.379 | 4.019 | 53½      |
| 36½      | 0.801 | 0.598 | 1.603 | 1.197 | 2.404 | 1.795 | 3.205 | 2.393 | 4.006 | 53½      |
| 37°      | 0.799 | 0.602 | 1.597 | 1.204 | 2.396 | 1.805 | 3.195 | 2.407 | 3.993 | 53°      |
| 37½      | 0.796 | 0.605 | 1.592 | 1.211 | 2.388 | 1.816 | 3.184 | 2.421 | 3.980 | 52½      |
| 37½      | 0.793 | 0.609 | 1.587 | 1.218 | 2.380 | 1.826 | 3.173 | 2.435 | 3.967 | 52½      |
| 37½      | 0.791 | 0.612 | 1.581 | 1.224 | 2.372 | 1.837 | 3.163 | 2.449 | 3.953 | 52½      |
| 38°      | 0.788 | 0.616 | 1.576 | 1.231 | 2.364 | 1.847 | 3.152 | 2.463 | 3.940 | 52°      |
| 38½      | 0.785 | 0.619 | 1.571 | 1.238 | 2.356 | 1.857 | 3.141 | 2.476 | 3.927 | 51½      |
| 38½      | 0.783 | 0.623 | 1.565 | 1.245 | 2.348 | 1.868 | 3.130 | 2.490 | 3.913 | 51½      |
| 38½      | 0.780 | 0.626 | 1.560 | 1.252 | 2.340 | 1.878 | 3.120 | 2.504 | 3.899 | 51½      |
| 39°      | 0.777 | 0.629 | 1.554 | 1.259 | 2.331 | 1.888 | 3.109 | 2.517 | 3.886 | 51°      |
| 39½      | 0.774 | 0.633 | 1.549 | 1.265 | 2.323 | 1.898 | 3.098 | 2.531 | 3.872 | 50½      |
| 39½      | 0.772 | 0.636 | 1.543 | 1.272 | 2.315 | 1.908 | 3.086 | 2.544 | 3.858 | 50½      |
| 39½      | 0.769 | 0.639 | 1.538 | 1.279 | 2.307 | 1.918 | 3.075 | 2.558 | 3.844 | 50½      |
|          |       |       |       |       |       |       |       |       |       |          |
| 40°      | 0.766 | 0.643 | 1.532 | 1.286 | 2.298 | 1.928 | 3.064 | 2.571 | 3.830 | 50°      |
| 40½      | 0.763 | 0.646 | 1.526 | 1.292 | 2.290 | 1.938 | 3.053 | 2.584 | 3.816 | 49½      |
| 40½      | 0.760 | 0.649 | 1.521 | 1.299 | 2.281 | 1.948 | 3.042 | 2.598 | 3.802 | 49½      |
| 40½      | 0.758 | 0.653 | 1.515 | 1.306 | 2.273 | 1.958 | 3.030 | 2.611 | 3.788 | 49½      |
| 41°      | 0.755 | 0.656 | 1.509 | 1.312 | 2.264 | 1.968 | 3.019 | 2.624 | 3.774 | 49°      |
| 41½      | 0.752 | 0.659 | 1.504 | 1.319 | 2.256 | 1.978 | 3.007 | 2.637 | 3.759 | 48½      |
| 41½      | 0.749 | 0.663 | 1.498 | 1.325 | 2.247 | 1.988 | 2.996 | 2.650 | 3.745 | 48½      |
| 41½      | 0.746 | 0.666 | 1.492 | 1.332 | 2.238 | 1.998 | 2.984 | 2.664 | 3.730 | 48½      |
| 42°      | 0.743 | 0.669 | 1.486 | 1.338 | 2.229 | 2.007 | 2.973 | 2.677 | 3.716 | 48°      |
| 42½      | 0.740 | 0.672 | 1.480 | 1.345 | 2.221 | 2.017 | 2.961 | 2.689 | 3.701 | 47½      |
| 42½      | 0.737 | 0.676 | 1.475 | 1.351 | 2.212 | 2.027 | 2.949 | 2.702 | 3.686 | 47½      |
| 42½      | 0.734 | 0.679 | 1.469 | 1.358 | 2.203 | 2.036 | 2.937 | 2.715 | 3.672 | 47½      |
| 43°      | 0.731 | 0.682 | 1.463 | 1.364 | 2.194 | 2.046 | 2.925 | 2.728 | 3.657 | 47°      |
| 43½      | 0.728 | 0.685 | 1.457 | 1.370 | 2.185 | 2.056 | 2.913 | 2.741 | 3.642 | 46½      |
| 43½      | 0.725 | 0.688 | 1.451 | 1.377 | 2.176 | 2.065 | 2.901 | 2.753 | 3.627 | 46½      |
| 43½      | 0.722 | 0.692 | 1.445 | 1.383 | 2.167 | 2.075 | 2.889 | 2.766 | 3.612 | 46½      |
| 44°      | 0.719 | 0.695 | 1.439 | 1.389 | 2.158 | 2.084 | 2.877 | 2.779 | 3.597 | 46°      |
| 44½      | 0.716 | 0.698 | 1.433 | 1.396 | 2.149 | 2.093 | 2.865 | 2.791 | 3.582 | 45½      |
| 44½      | 0.713 | 0.701 | 1.427 | 1.402 | 2.140 | 2.103 | 2.853 | 2.804 | 3.566 | 45½      |
| 44½      | 0.710 | 0.704 | 1.420 | 1.408 | 2.131 | 2.112 | 2.841 | 2.816 | 3.551 | 45½      |
| 45°      | 0.707 | 0.707 | 1.414 | 1.414 | 2.121 | 2.121 | 2.828 | 2.828 | 3.536 | 45°      |
| Bearing. | 1     |       | 2     |       | 3     |       | 4     |       | 5     | Bearing. |
|          | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  |          |

# LATITUDES AND DEPARTURES.

| Bearing. | 5     |       | 6     |       | 7     |       | 8     |       | 9     |          | Bearing. |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|----------|
|          | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  |          |          |
| 30°      | 2.500 | 5.196 | 3.000 | 6.062 | 3.500 | 6.928 | 4.000 | 7.794 | 4.500 | 60°      |          |
| 30½      | 2.519 | 5.183 | 3.023 | 6.047 | 3.526 | 6.911 | 4.030 | 7.775 | 4.534 | 59½      |          |
| 30½      | 2.538 | 5.170 | 3.045 | 6.031 | 3.553 | 6.893 | 4.060 | 7.755 | 4.568 | 59½      |          |
| 30½      | 2.556 | 5.156 | 3.068 | 6.016 | 3.579 | 6.875 | 4.090 | 7.735 | 4.602 | 59½      |          |
| 31°      | 2.575 | 5.143 | 3.090 | 6.000 | 3.605 | 6.857 | 4.120 | 7.715 | 4.635 | 59°      |          |
| 31½      | 2.594 | 5.129 | 3.113 | 5.984 | 3.631 | 6.839 | 4.150 | 7.694 | 4.669 | 58½      |          |
| 31½      | 2.612 | 5.116 | 3.135 | 5.968 | 3.657 | 6.821 | 4.180 | 7.674 | 4.702 | 58½      |          |
| 31½      | 2.631 | 5.102 | 3.157 | 5.952 | 3.683 | 6.803 | 4.210 | 7.653 | 4.736 | 58½      |          |
| 32°      | 2.650 | 5.088 | 3.180 | 5.936 | 3.709 | 6.784 | 4.239 | 7.632 | 4.769 | 58°      |          |
| 32½      | 2.668 | 5.074 | 3.202 | 5.920 | 3.735 | 6.766 | 4.269 | 7.612 | 4.802 | 57½      |          |
| 32½      | 2.686 | 5.060 | 3.224 | 5.904 | 3.761 | 6.747 | 4.298 | 7.591 | 4.836 | 57½      |          |
| 32½      | 2.705 | 5.046 | 3.246 | 5.887 | 3.787 | 6.728 | 4.328 | 7.569 | 4.869 | 57½      |          |
| 33°      | 2.723 | 5.032 | 3.268 | 5.871 | 3.812 | 6.709 | 4.357 | 7.548 | 4.902 | 57°      |          |
| 33½      | 2.741 | 5.018 | 3.290 | 5.854 | 3.838 | 6.690 | 4.386 | 7.527 | 4.935 | 56½      |          |
| 33½      | 2.760 | 5.003 | 3.312 | 5.837 | 3.864 | 6.671 | 4.416 | 7.505 | 4.967 | 56½      |          |
| 33½      | 2.778 | 4.989 | 3.333 | 5.820 | 3.889 | 6.652 | 4.445 | 7.483 | 5.000 | 56½      |          |
| 34°      | 2.796 | 4.974 | 3.355 | 5.803 | 3.914 | 6.632 | 4.474 | 7.461 | 5.033 | 56°      |          |
| 34½      | 2.814 | 4.960 | 3.377 | 5.786 | 3.940 | 6.613 | 4.502 | 7.439 | 5.065 | 55½      |          |
| 34½      | 2.832 | 4.945 | 3.398 | 5.769 | 3.965 | 6.593 | 4.531 | 7.417 | 5.098 | 55½      |          |
| 34½      | 2.850 | 4.930 | 3.420 | 5.752 | 3.990 | 6.573 | 4.560 | 7.395 | 5.130 | 55½      |          |
| 35°      | 2.868 | 4.915 | 3.441 | 5.734 | 4.015 | 6.553 | 4.589 | 7.372 | 5.162 | 55°      |          |
| 35½      | 2.886 | 4.900 | 3.463 | 5.716 | 4.040 | 6.533 | 4.617 | 7.350 | 5.194 | 54½      |          |
| 35½      | 2.904 | 4.885 | 3.484 | 5.699 | 4.065 | 6.513 | 4.646 | 7.327 | 5.226 | 54½      |          |
| 35½      | 2.921 | 4.869 | 3.505 | 5.681 | 4.090 | 6.493 | 4.674 | 7.304 | 5.258 | 54½      |          |
| 36°      | 2.939 | 4.854 | 3.527 | 5.663 | 4.115 | 6.472 | 4.702 | 7.281 | 5.290 | 54°      |          |
| 36½      | 2.957 | 4.839 | 3.548 | 5.645 | 4.139 | 6.452 | 4.730 | 7.258 | 5.322 | 53½      |          |
| 36½      | 2.974 | 4.823 | 3.569 | 5.627 | 4.164 | 6.431 | 4.759 | 7.235 | 5.353 | 53½      |          |
| 36½      | 2.992 | 4.808 | 3.590 | 5.609 | 4.188 | 6.410 | 4.787 | 7.211 | 5.385 | 53½      |          |
| 37°      | 3.009 | 4.792 | 3.611 | 5.590 | 4.213 | 6.389 | 4.815 | 7.188 | 5.416 | 53°      |          |
| 37½      | 3.026 | 4.776 | 3.632 | 5.572 | 4.237 | 6.368 | 4.842 | 7.164 | 5.448 | 52½      |          |
| 37½      | 3.044 | 4.760 | 3.653 | 5.554 | 4.261 | 6.347 | 4.870 | 7.140 | 5.479 | 52½      |          |
| 37½      | 3.061 | 4.744 | 3.673 | 5.535 | 4.286 | 6.326 | 4.898 | 7.116 | 5.510 | 52½      |          |
| 38°      | 3.078 | 4.728 | 3.694 | 5.516 | 4.310 | 6.304 | 4.925 | 7.092 | 5.541 | 52°      |          |
| 38½      | 3.095 | 4.712 | 3.715 | 5.497 | 4.334 | 6.283 | 4.953 | 7.068 | 5.572 | 51½      |          |
| 38½      | 3.113 | 4.696 | 3.735 | 5.478 | 4.358 | 6.261 | 4.980 | 7.043 | 5.603 | 51½      |          |
| 38½      | 3.130 | 4.679 | 3.756 | 5.459 | 4.381 | 6.239 | 5.007 | 7.019 | 5.633 | 51½      |          |
| 39°      | 3.147 | 4.663 | 3.776 | 5.440 | 4.405 | 6.217 | 5.035 | 6.994 | 5.664 | 51°      |          |
| 39½      | 3.164 | 4.646 | 3.796 | 5.421 | 4.429 | 6.195 | 5.062 | 6.970 | 5.694 | 50½      |          |
| 39½      | 3.180 | 4.630 | 3.816 | 5.401 | 4.453 | 6.173 | 5.089 | 6.945 | 5.725 | 50½      |          |
| 39½      | 3.197 | 4.613 | 3.837 | 5.382 | 4.476 | 6.151 | 5.116 | 6.920 | 5.755 | 50½      |          |
| 40°      | 3.214 | 4.596 | 3.857 | 5.362 | 4.500 | 6.128 | 5.142 | 6.894 | 5.785 | 50°      |          |
| 40½      | 3.231 | 4.579 | 3.877 | 5.343 | 4.523 | 6.106 | 5.169 | 6.869 | 5.815 | 49½      |          |
| 40½      | 3.247 | 4.562 | 3.897 | 5.323 | 4.546 | 6.083 | 5.196 | 6.844 | 5.845 | 49½      |          |
| 40½      | 3.264 | 4.545 | 3.917 | 5.303 | 4.569 | 6.061 | 5.222 | 6.818 | 5.875 | 49½      |          |
| 41°      | 3.280 | 4.528 | 3.936 | 5.283 | 4.592 | 6.038 | 5.248 | 6.792 | 5.905 | 49°      |          |
| 41½      | 3.297 | 4.511 | 3.956 | 5.263 | 4.615 | 6.015 | 5.275 | 6.767 | 5.934 | 48½      |          |
| 41½      | 3.313 | 4.494 | 3.976 | 5.243 | 4.638 | 5.992 | 5.301 | 6.741 | 5.964 | 48½      |          |
| 41½      | 3.329 | 4.476 | 3.995 | 5.222 | 4.661 | 5.968 | 5.327 | 6.715 | 5.993 | 48½      |          |
| 42°      | 3.346 | 4.459 | 4.015 | 5.202 | 4.684 | 5.945 | 5.353 | 6.688 | 6.022 | 48°      |          |
| 42½      | 3.362 | 4.441 | 4.034 | 5.182 | 4.707 | 5.922 | 5.379 | 6.662 | 6.051 | 47½      |          |
| 42½      | 3.378 | 4.424 | 4.054 | 5.161 | 4.729 | 5.898 | 5.405 | 6.635 | 6.080 | 47½      |          |
| 42½      | 3.394 | 4.406 | 4.073 | 5.140 | 4.752 | 5.875 | 5.430 | 6.609 | 6.109 | 47½      |          |
| 43°      | 3.410 | 4.388 | 4.092 | 5.119 | 4.774 | 5.851 | 5.456 | 6.582 | 6.138 | 47°      |          |
| 43½      | 3.426 | 4.370 | 4.111 | 5.099 | 4.796 | 5.827 | 5.481 | 6.555 | 6.167 | 46½      |          |
| 43½      | 3.442 | 4.352 | 4.130 | 5.078 | 4.818 | 5.803 | 5.507 | 6.528 | 6.195 | 46½      |          |
| 43½      | 3.458 | 4.334 | 4.149 | 5.057 | 4.841 | 5.779 | 5.532 | 6.501 | 6.224 | 46½      |          |
| 44°      | 3.473 | 4.316 | 4.168 | 5.035 | 4.863 | 5.755 | 5.557 | 6.474 | 6.252 | 46°      |          |
| 44½      | 3.489 | 4.298 | 4.187 | 5.014 | 4.885 | 5.730 | 5.582 | 6.447 | 6.280 | 45½      |          |
| 44½      | 3.505 | 4.280 | 4.206 | 4.993 | 4.906 | 5.706 | 5.607 | 6.419 | 6.308 | 45½      |          |
| 44½      | 3.520 | 4.261 | 4.224 | 4.971 | 4.928 | 5.681 | 5.632 | 6.392 | 6.336 | 45½      |          |
| 45°      | 3.536 | 4.243 | 4.243 | 4.950 | 4.950 | 5.657 | 5.657 | 6.364 | 6.364 | 45°      |          |
| Bearing. | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Dep.  | Lat.  | Bearing. |          |
| 5        | 6     | 7     | 8     | 9     |       |       |       |       |       |          |          |

TABLE OF CHORDS: [RADIUS = 1.0000].

| x  | 0°    | 1°    | 2°    | 3°    | 4°    | 5°    | 6°    | 7°    | 8°    | 9°    | 10°   | x  |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| 0' | .0000 | .0175 | .0349 | .0524 | .0698 | .0872 | .1047 | .1221 | .1395 | .1569 | .1743 | 0' |
| 1  | .0003 | .0177 | .0352 | .0526 | .0701 | .0875 | .1050 | .1224 | .1398 | .1572 | .1746 | 1  |
| 2  | .0006 | .0180 | .0355 | .0529 | .0704 | .0878 | .1053 | .1227 | .1401 | .1575 | .1749 | 2  |
| 3  | .0009 | .0183 | .0358 | .0532 | .0707 | .0881 | .1055 | .1230 | .1404 | .1578 | .1752 | 3  |
| 4  | .0012 | .0186 | .0361 | .0535 | .0710 | .0884 | .1058 | .1233 | .1407 | .1581 | .1755 | 4  |
| 5  | .0015 | .0189 | .0364 | .0538 | .0713 | .0887 | .1061 | .1235 | .1410 | .1584 | .1758 | 5  |
| 6  | .0017 | .0192 | .0366 | .0541 | .0715 | .0890 | .1064 | .1238 | .1413 | .1587 | .1761 | 6  |
| 7  | .0020 | .0195 | .0369 | .0544 | .0718 | .0893 | .1067 | .1241 | .1415 | .1589 | .1763 | 7  |
| 8  | .0023 | .0198 | .0372 | .0547 | .0721 | .0896 | .1070 | .1244 | .1418 | .1592 | .1766 | 8  |
| 9  | .0026 | .0201 | .0375 | .0550 | .0724 | .0899 | .1073 | .1247 | .1421 | .1595 | .1769 | 9  |
| 10 | .0029 | .0204 | .0378 | .0553 | .0727 | .0901 | .1076 | .1250 | .1424 | .1598 | .1772 | 10 |
| 11 | .0032 | .0207 | .0381 | .0556 | .0730 | .0904 | .1079 | .1253 | .1427 | .1601 | .1775 | 11 |
| 12 | .0035 | .0209 | .0384 | .0558 | .0733 | .0907 | .1082 | .1256 | .1430 | .1604 | .1778 | 12 |
| 13 | .0038 | .0212 | .0387 | .0561 | .0736 | .0910 | .1084 | .1259 | .1433 | .1607 | .1781 | 13 |
| 14 | .0041 | .0215 | .0390 | .0564 | .0739 | .0913 | .1087 | .1262 | .1436 | .1610 | .1784 | 14 |
| 15 | .0044 | .0218 | .0393 | .0567 | .0742 | .0916 | .1090 | .1265 | .1439 | .1613 | .1787 | 15 |
| 16 | .0047 | .0221 | .0396 | .0570 | .0745 | .0919 | .1093 | .1267 | .1442 | .1616 | .1789 | 16 |
| 17 | .0049 | .0224 | .0398 | .0573 | .0747 | .0922 | .1096 | .1270 | .1444 | .1618 | .1792 | 17 |
| 18 | .0052 | .0227 | .0401 | .0576 | .0750 | .0925 | .1099 | .1273 | .1447 | .1621 | .1795 | 18 |
| 19 | .0055 | .0230 | .0404 | .0579 | .0753 | .0928 | .1102 | .1276 | .1450 | .1624 | .1798 | 19 |
| 20 | .0058 | .0233 | .0407 | .0582 | .0756 | .0931 | .1105 | .1279 | .1453 | .1627 | .1801 | 20 |
| 21 | .0061 | .0236 | .0410 | .0585 | .0759 | .0933 | .1108 | .1282 | .1456 | .1630 | .1804 | 21 |
| 22 | .0064 | .0239 | .0413 | .0588 | .0762 | .0936 | .1111 | .1285 | .1459 | .1633 | .1807 | 22 |
| 23 | .0067 | .0241 | .0416 | .0590 | .0765 | .0939 | .1114 | .1288 | .1462 | .1636 | .1810 | 23 |
| 24 | .0070 | .0244 | .0419 | .0593 | .0768 | .0942 | .1116 | .1291 | .1465 | .1639 | .1813 | 24 |
| 25 | .0073 | .0247 | .0422 | .0596 | .0771 | .0945 | .1119 | .1294 | .1468 | .1642 | .1816 | 25 |
| 26 | .0076 | .0250 | .0425 | .0599 | .0774 | .0948 | .1122 | .1296 | .1471 | .1645 | .1818 | 26 |
| 27 | .0079 | .0253 | .0428 | .0602 | .0776 | .0951 | .1125 | .1299 | .1473 | .1647 | .1821 | 27 |
| 28 | .0081 | .0256 | .0430 | .0605 | .0779 | .0954 | .1128 | .1302 | .1476 | .1650 | .1824 | 28 |
| 29 | .0084 | .0259 | .0433 | .0608 | .0782 | .0957 | .1131 | .1305 | .1479 | .1653 | .1827 | 29 |
| 30 | .0087 | .0262 | .0436 | .0611 | .0785 | .0960 | .1134 | .1308 | .1482 | .1656 | .1830 | 30 |
| 31 | .0090 | .0265 | .0439 | .0614 | .0788 | .0962 | .1137 | .1311 | .1485 | .1659 | .1833 | 31 |
| 32 | .0093 | .0268 | .0442 | .0617 | .0791 | .0965 | .1140 | .1314 | .1488 | .1662 | .1836 | 32 |
| 33 | .0096 | .0271 | .0445 | .0619 | .0794 | .0968 | .1143 | .1317 | .1491 | .1665 | .1839 | 33 |
| 34 | .0099 | .0273 | .0448 | .0622 | .0797 | .0971 | .1145 | .1320 | .1494 | .1668 | .1842 | 34 |
| 35 | .0102 | .0276 | .0451 | .0625 | .0800 | .0974 | .1148 | .1323 | .1497 | .1671 | .1845 | 35 |
| 36 | .0105 | .0279 | .0454 | .0628 | .0803 | .0977 | .1151 | .1325 | .1500 | .1674 | .1847 | 36 |
| 37 | .0108 | .0282 | .0457 | .0631 | .0806 | .0980 | .1154 | .1328 | .1502 | .1676 | .1850 | 37 |
| 38 | .0111 | .0285 | .0460 | .0634 | .0808 | .0983 | .1157 | .1331 | .1505 | .1679 | .1853 | 38 |
| 39 | .0113 | .0288 | .0462 | .0637 | .0811 | .0986 | .1160 | .1334 | .1508 | .1682 | .1856 | 39 |
| 40 | .0116 | .0291 | .0465 | .0640 | .0814 | .0989 | .1163 | .1337 | .1511 | .1685 | .1859 | 40 |
| 41 | .0119 | .0294 | .0468 | .0643 | .0817 | .0992 | .1166 | .1340 | .1514 | .1688 | .1862 | 41 |
| 42 | .0122 | .0297 | .0471 | .0646 | .0820 | .0994 | .1169 | .1343 | .1517 | .1691 | .1865 | 42 |
| 43 | .0125 | .0300 | .0474 | .0649 | .0823 | .0997 | .1172 | .1346 | .1520 | .1694 | .1868 | 43 |
| 44 | .0128 | .0303 | .0477 | .0651 | .0826 | .1000 | .1175 | .1349 | .1523 | .1697 | .1871 | 44 |
| 45 | .0131 | .0305 | .0480 | .0654 | .0829 | .1003 | .1177 | .1352 | .1526 | .1700 | .1873 | 45 |
| 46 | .0134 | .0308 | .0483 | .0657 | .0832 | .1006 | .1180 | .1355 | .1529 | .1703 | .1876 | 46 |
| 47 | .0137 | .0311 | .0486 | .0660 | .0835 | .1009 | .1183 | .1357 | .1531 | .1705 | .1879 | 47 |
| 48 | .0140 | .0314 | .0489 | .0663 | .0838 | .1012 | .1186 | .1360 | .1534 | .1708 | .1882 | 48 |
| 49 | .0143 | .0317 | .0492 | .0666 | .0840 | .1015 | .1189 | .1363 | .1537 | .1711 | .1885 | 49 |
| 50 | .0145 | .0320 | .0494 | .0669 | .0843 | .1018 | .1192 | .1366 | .1540 | .1714 | .1888 | 50 |
| 51 | .0148 | .0323 | .0497 | .0672 | .0846 | .1021 | .1195 | .1369 | .1543 | .1717 | .1891 | 51 |
| 52 | .0151 | .0326 | .0500 | .0675 | .0849 | .1023 | .1198 | .1372 | .1546 | .1720 | .1894 | 52 |
| 53 | .0154 | .0329 | .0503 | .0678 | .0852 | .1026 | .1201 | .1375 | .1549 | .1723 | .1897 | 53 |
| 54 | .0157 | .0332 | .0506 | .0681 | .0855 | .1029 | .1204 | .1378 | .1552 | .1726 | .1900 | 54 |
| 55 | .0160 | .0335 | .0509 | .0683 | .0858 | .1032 | .1206 | .1381 | .1555 | .1729 | .1902 | 55 |
| 56 | .0163 | .0337 | .0512 | .0686 | .0861 | .1035 | .1209 | .1384 | .1558 | .1732 | .1905 | 56 |
| 57 | .0166 | .0340 | .0515 | .0689 | .0864 | .1038 | .1212 | .1386 | .1560 | .1734 | .1908 | 57 |
| 58 | .0169 | .0343 | .0518 | .0692 | .0867 | .1041 | .1215 | .1389 | .1563 | .1737 | .1911 | 58 |
| 59 | .0172 | .0346 | .0521 | .0695 | .0869 | .1044 | .1218 | .1392 | .1566 | .1740 | .1914 | 59 |
| 60 | .0175 | .0349 | .0524 | .0698 | .0872 | .1047 | .1221 | .1395 | .1569 | .1743 | .1917 | 60 |



TABLE OF CHORDS: [RADIUS = 1.0000].

| x. | 11°   | 12°   | 13°   | 14°   | 15°   | 16°   | 17°   | 18°   | 19°   | 20°   | 21°   | x. |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| 0' | .1917 | .2091 | .2264 | .2437 | .2611 | .2783 | .2956 | .3129 | .3301 | .3473 | .3645 | 0' |
| 1  | .1920 | .2093 | .2267 | .2440 | .2613 | .2786 | .2959 | .3132 | .3304 | .3476 | .3648 | 1  |
| 2  | .1923 | .2096 | .2270 | .2443 | .2616 | .2789 | .2962 | .3134 | .3307 | .3479 | .3650 | 2  |
| 3  | .1926 | .2099 | .2273 | .2446 | .2619 | .2792 | .2965 | .3137 | .3310 | .3482 | .3653 | 3  |
| 4  | .1928 | .2102 | .2276 | .2449 | .2622 | .2795 | .2968 | .3140 | .3312 | .3484 | .3656 | 4  |
| 5  | .1931 | .2105 | .2279 | .2452 | .2625 | .2798 | .2971 | .3143 | .3315 | .3487 | .3659 | 5  |
| 6  | .1934 | .2108 | .2281 | .2455 | .2628 | .2801 | .2973 | .3146 | .3318 | .3490 | .3662 | 6  |
| 7  | .1937 | .2111 | .2284 | .2458 | .2631 | .2804 | .2976 | .3149 | .3321 | .3493 | .3665 | 7  |
| 8  | .1940 | .2114 | .2287 | .2460 | .2634 | .2807 | .2979 | .3152 | .3324 | .3496 | .3668 | 8  |
| 9  | .1943 | .2117 | .2290 | .2463 | .2636 | .2809 | .2982 | .3155 | .3327 | .3499 | .3670 | 9  |
| 10 | .1946 | .2119 | .2293 | .2466 | .2639 | .2812 | .2985 | .3157 | .3330 | .3502 | .3673 | 10 |
| 11 | .1949 | .2122 | .2296 | .2469 | .2642 | .2815 | .2988 | .3160 | .3333 | .3504 | .3676 | 11 |
| 12 | .1952 | .2125 | .2299 | .2472 | .2645 | .2818 | .2991 | .3163 | .3335 | .3507 | .3679 | 12 |
| 13 | .1955 | .2128 | .2302 | .2475 | .2648 | .2821 | .2994 | .3166 | .3338 | .3510 | .3682 | 13 |
| 14 | .1957 | .2131 | .2305 | .2478 | .2651 | .2824 | .2996 | .3169 | .3341 | .3513 | .3685 | 14 |
| 15 | .1960 | .2134 | .2307 | .2481 | .2654 | .2827 | .2999 | .3172 | .3344 | .3516 | .3688 | 15 |
| 16 | .1963 | .2137 | .2310 | .2484 | .2657 | .2830 | .3002 | .3175 | .3347 | .3519 | .3690 | 16 |
| 17 | .1966 | .2140 | .2313 | .2486 | .2660 | .2832 | .3005 | .3178 | .3350 | .3522 | .3693 | 17 |
| 18 | .1969 | .2143 | .2316 | .2489 | .2662 | .2835 | .3008 | .3180 | .3353 | .3525 | .3696 | 18 |
| 19 | .1972 | .2146 | .2319 | .2492 | .2665 | .2838 | .3011 | .3183 | .3355 | .3527 | .3699 | 19 |
| 20 | .1975 | .2148 | .2322 | .2495 | .2668 | .2841 | .3014 | .3186 | .3358 | .3530 | .3702 | 20 |
| 21 | .1978 | .2151 | .2325 | .2498 | .2671 | .2844 | .3017 | .3189 | .3361 | .3533 | .3705 | 21 |
| 22 | .1981 | .2154 | .2328 | .2501 | .2674 | .2847 | .3019 | .3192 | .3364 | .3536 | .3708 | 22 |
| 23 | .1983 | .2157 | .2331 | .2504 | .2677 | .2850 | .3022 | .3195 | .3367 | .3539 | .3710 | 23 |
| 24 | .1986 | .2160 | .2333 | .2507 | .2680 | .2853 | .3025 | .3198 | .3370 | .3542 | .3713 | 24 |
| 25 | .1989 | .2163 | .2336 | .2510 | .2683 | .2855 | .3028 | .3200 | .3373 | .3545 | .3716 | 25 |
| 26 | .1992 | .2166 | .2339 | .2512 | .2685 | .2858 | .3031 | .3203 | .3376 | .3547 | .3719 | 26 |
| 27 | .1995 | .2169 | .2342 | .2515 | .2688 | .2861 | .3034 | .3206 | .3378 | .3550 | .3722 | 27 |
| 28 | .1998 | .2172 | .2345 | .2518 | .2691 | .2864 | .3037 | .3209 | .3381 | .3553 | .3725 | 28 |
| 29 | .2001 | .2174 | .2348 | .2521 | .2694 | .2867 | .3040 | .3212 | .3384 | .3556 | .3728 | 29 |
| 30 | .2004 | .2177 | .2351 | .2524 | .2697 | .2870 | .3042 | .3215 | .3387 | .3559 | .3730 | 30 |
| 31 | .2007 | .2180 | .2354 | .2527 | .2700 | .2873 | .3045 | .3218 | .3390 | .3562 | .3733 | 31 |
| 32 | .2010 | .2183 | .2357 | .2530 | .2703 | .2876 | .3048 | .3221 | .3393 | .3565 | .3736 | 32 |
| 33 | .2012 | .2186 | .2359 | .2533 | .2706 | .2878 | .3051 | .3223 | .3396 | .3567 | .3739 | 33 |
| 34 | .2015 | .2189 | .2362 | .2536 | .2709 | .2881 | .3054 | .3226 | .3398 | .3570 | .3742 | 34 |
| 35 | .2018 | .2192 | .2365 | .2538 | .2711 | .2884 | .3057 | .3229 | .3401 | .3573 | .3745 | 35 |
| 36 | .2021 | .2195 | .2368 | .2541 | .2714 | .2887 | .3060 | .3232 | .3404 | .3576 | .3748 | 36 |
| 37 | .2024 | .2198 | .2371 | .2544 | .2717 | .2890 | .3063 | .3235 | .3407 | .3579 | .3750 | 37 |
| 38 | .2027 | .2200 | .2374 | .2547 | .2720 | .2893 | .3065 | .3238 | .3410 | .3582 | .3753 | 38 |
| 39 | .2030 | .2203 | .2377 | .2550 | .2723 | .2896 | .3068 | .3241 | .3413 | .3585 | .3756 | 39 |
| 40 | .2033 | .2206 | .2380 | .2553 | .2726 | .2899 | .3071 | .3244 | .3416 | .3587 | .3759 | 40 |
| 41 | .2036 | .2209 | .2383 | .2556 | .2729 | .2902 | .3074 | .3246 | .3419 | .3590 | .3762 | 41 |
| 42 | .2038 | .2212 | .2385 | .2559 | .2732 | .2904 | .3077 | .3249 | .3421 | .3593 | .3765 | 42 |
| 43 | .2041 | .2215 | .2388 | .2561 | .2734 | .2907 | .3080 | .3252 | .3424 | .3596 | .3768 | 43 |
| 44 | .2044 | .2218 | .2391 | .2564 | .2737 | .2910 | .3083 | .3255 | .3427 | .3599 | .3770 | 44 |
| 45 | .2047 | .2221 | .2394 | .2567 | .2740 | .2913 | .3086 | .3258 | .3430 | .3602 | .3773 | 45 |
| 46 | .2050 | .2224 | .2397 | .2570 | .2743 | .2916 | .3088 | .3261 | .3433 | .3605 | .3776 | 46 |
| 47 | .2053 | .2226 | .2400 | .2573 | .2746 | .2919 | .3091 | .3264 | .3436 | .3608 | .3779 | 47 |
| 48 | .2056 | .2229 | .2403 | .2576 | .2749 | .2922 | .3094 | .3267 | .3439 | .3610 | .3782 | 48 |
| 49 | .2059 | .2232 | .2406 | .2579 | .2752 | .2925 | .3097 | .3269 | .3441 | .3613 | .3785 | 49 |
| 50 | .2062 | .2235 | .2409 | .2582 | .2755 | .2927 | .3100 | .3272 | .3444 | .3616 | .3788 | 50 |
| 51 | .2065 | .2238 | .2411 | .2585 | .2758 | .2930 | .3103 | .3275 | .3447 | .3619 | .3790 | 51 |
| 52 | .2067 | .2241 | .2414 | .2587 | .2760 | .2933 | .3106 | .3278 | .3450 | .3622 | .3793 | 52 |
| 53 | .2070 | .2244 | .2417 | .2590 | .2763 | .2936 | .3109 | .3281 | .3453 | .3625 | .3796 | 53 |
| 54 | .2073 | .2247 | .2420 | .2593 | .2766 | .2939 | .3111 | .3284 | .3456 | .3628 | .3799 | 54 |
| 55 | .2076 | .2250 | .2423 | .2596 | .2769 | .2942 | .3114 | .3287 | .3459 | .3630 | .3802 | 55 |
| 56 | .2079 | .2253 | .2426 | .2599 | .2772 | .2945 | .3117 | .3289 | .3462 | .3633 | .3805 | 56 |
| 57 | .2082 | .2255 | .2429 | .2602 | .2775 | .2948 | .3120 | .3292 | .3464 | .3636 | .3808 | 57 |
| 58 | .2085 | .2258 | .2432 | .2605 | .2778 | .2950 | .3123 | .3295 | .3467 | .3639 | .3810 | 58 |
| 59 | .2088 | .2261 | .2434 | .2608 | .2781 | .2953 | .3126 | .3298 | .3470 | .3642 | .3813 | 59 |
| 60 | .2091 | .2264 | .2437 | .2611 | .2783 | .2956 | .3129 | .3301 | .3473 | .3645 | .3816 | 60 |

TABLE OF CHORDS: [RADIUS = 1.0000].

| M  | 22°   | 23°   | 24°   | 25°   | 26°   | 27°   | 28°   | 29°   | 30°   | 31°   | 32°   | M  |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| 0  | .3816 | .3987 | .4158 | .4329 | .4499 | .4669 | .4838 | .5008 | .5176 | .5345 | .5513 | 0  |
| 1  | .3819 | .3990 | .4161 | .4332 | .4502 | .4672 | .4841 | .5010 | .5179 | .5348 | .5516 | 1  |
| 2  | .3822 | .3993 | .4164 | .4334 | .4505 | .4675 | .4844 | .5013 | .5182 | .5350 | .5518 | 2  |
| 3  | .3825 | .3996 | .4167 | .4337 | .4508 | .4677 | .4847 | .5016 | .5185 | .5353 | .5521 | 3  |
| 4  | .3828 | .3999 | .4170 | .4340 | .4510 | .4680 | .4850 | .5019 | .5188 | .5356 | .5524 | 4  |
| 5  | .3830 | .4002 | .4172 | .4343 | .4513 | .4683 | .4853 | .5022 | .5190 | .5359 | .5527 | 5  |
| 6  | .3833 | .4004 | .4175 | .4346 | .4516 | .4686 | .4855 | .5024 | .5193 | .5362 | .5530 | 6  |
| 7  | .3836 | .4007 | .4178 | .4349 | .4519 | .4689 | .4858 | .5027 | .5196 | .5364 | .5532 | 7  |
| 8  | .3839 | .4010 | .4181 | .4352 | .4522 | .4692 | .4861 | .5030 | .5199 | .5367 | .5535 | 8  |
| 9  | .3842 | .4013 | .4184 | .4354 | .4525 | .4694 | .4864 | .5033 | .5202 | .5370 | .5538 | 9  |
| 10 | .3845 | .4016 | .4187 | .4357 | .4527 | .4697 | .4867 | .5036 | .5204 | .5373 | .5541 | 10 |
| 11 | .3848 | .4019 | .4190 | .4360 | .4530 | .4700 | .4869 | .5039 | .5207 | .5376 | .5543 | 11 |
| 12 | .3850 | .4022 | .4192 | .4363 | .4533 | .4703 | .4872 | .5041 | .5210 | .5378 | .5546 | 12 |
| 13 | .3853 | .4024 | .4195 | .4366 | .4536 | .4706 | .4875 | .5044 | .5213 | .5381 | .5549 | 13 |
| 14 | .3856 | .4027 | .4198 | .4369 | .4539 | .4708 | .4878 | .5047 | .5216 | .5384 | .5552 | 14 |
| 15 | .3859 | .4030 | .4201 | .4371 | .4542 | .4711 | .4881 | .5050 | .5219 | .5387 | .5555 | 15 |
| 16 | .3862 | .4033 | .4204 | .4374 | .4544 | .4714 | .4884 | .5053 | .5221 | .5390 | .5557 | 16 |
| 17 | .3865 | .4036 | .4207 | .4377 | .4547 | .4717 | .4886 | .5055 | .5224 | .5392 | .5560 | 17 |
| 18 | .3868 | .4039 | .4209 | .4380 | .4550 | .4720 | .4889 | .5058 | .5227 | .5395 | .5563 | 18 |
| 19 | .3870 | .4042 | .4212 | .4383 | .4553 | .4723 | .4892 | .5061 | .5230 | .5398 | .5566 | 19 |
| 20 | .3873 | .4044 | .4215 | .4386 | .4556 | .4725 | .4895 | .5064 | .5233 | .5401 | .5569 | 20 |
| 21 | .3876 | .4047 | .4218 | .4388 | .4559 | .4728 | .4898 | .5067 | .5235 | .5404 | .5571 | 21 |
| 22 | .3879 | .4050 | .4221 | .4391 | .4561 | .4731 | .4901 | .5070 | .5238 | .5406 | .5574 | 22 |
| 23 | .3882 | .4053 | .4224 | .4394 | .4564 | .4734 | .4903 | .5072 | .5241 | .5409 | .5577 | 23 |
| 24 | .3885 | .4056 | .4226 | .4397 | .4567 | .4737 | .4906 | .5075 | .5244 | .5412 | .5580 | 24 |
| 25 | .3888 | .4059 | .4229 | .4400 | .4570 | .4740 | .4909 | .5078 | .5247 | .5415 | .5583 | 25 |
| 26 | .3890 | .4061 | .4232 | .4403 | .4573 | .4742 | .4912 | .5081 | .5249 | .5418 | .5585 | 26 |
| 27 | .3893 | .4064 | .4235 | .4405 | .4576 | .4745 | .4915 | .5084 | .5252 | .5420 | .5588 | 27 |
| 28 | .3896 | .4067 | .4238 | .4408 | .4578 | .4748 | .4917 | .5086 | .5255 | .5423 | .5591 | 28 |
| 29 | .3899 | .4070 | .4241 | .4411 | .4581 | .4751 | .4920 | .5089 | .5258 | .5426 | .5594 | 29 |
| 30 | .3902 | .4073 | .4244 | .4414 | .4584 | .4754 | .4923 | .5092 | .5261 | .5429 | .5597 | 30 |
| 31 | .3905 | .4076 | .4246 | .4417 | .4587 | .4757 | .4926 | .5095 | .5263 | .5432 | .5599 | 31 |
| 32 | .3908 | .4079 | .4249 | .4420 | .4590 | .4759 | .4929 | .5098 | .5266 | .5434 | .5602 | 32 |
| 33 | .3910 | .4081 | .4252 | .4422 | .4593 | .4762 | .4932 | .5100 | .5269 | .5437 | .5605 | 33 |
| 34 | .3913 | .4084 | .4255 | .4425 | .4595 | .4765 | .4934 | .5103 | .5272 | .5440 | .5608 | 34 |
| 35 | .3916 | .4087 | .4258 | .4428 | .4598 | .4768 | .4937 | .5106 | .5275 | .5443 | .5611 | 35 |
| 36 | .3919 | .4090 | .4261 | .4431 | .4601 | .4771 | .4940 | .5109 | .5277 | .5446 | .5613 | 36 |
| 37 | .3922 | .4093 | .4263 | .4434 | .4604 | .4773 | .4943 | .5112 | .5280 | .5448 | .5616 | 37 |
| 38 | .3925 | .4096 | .4266 | .4437 | .4607 | .4776 | .4946 | .5115 | .5283 | .5451 | .5619 | 38 |
| 39 | .3927 | .4098 | .4269 | .4439 | .4609 | .4779 | .4948 | .5117 | .5286 | .5454 | .5622 | 39 |
| 40 | .3930 | .4101 | .4272 | .4442 | .4612 | .4782 | .4951 | .5120 | .5289 | .5457 | .5625 | 40 |
| 41 | .3933 | .4104 | .4275 | .4445 | .4615 | .4785 | .4954 | .5123 | .5291 | .5460 | .5627 | 41 |
| 42 | .3936 | .4107 | .4278 | .4448 | .4618 | .4788 | .4957 | .5126 | .5294 | .5462 | .5630 | 42 |
| 43 | .3939 | .4110 | .4280 | .4451 | .4621 | .4790 | .4960 | .5129 | .5297 | .5465 | .5633 | 43 |
| 44 | .3942 | .4113 | .4283 | .4454 | .4624 | .4793 | .4963 | .5131 | .5300 | .5468 | .5636 | 44 |
| 45 | .3945 | .4116 | .4286 | .4456 | .4626 | .4796 | .4965 | .5134 | .5303 | .5471 | .5638 | 45 |
| 46 | .3947 | .4118 | .4289 | .4459 | .4629 | .4799 | .4968 | .5137 | .5306 | .5474 | .5641 | 46 |
| 47 | .3950 | .4121 | .4292 | .4462 | .4632 | .4802 | .4971 | .5140 | .5308 | .5476 | .5644 | 47 |
| 48 | .3953 | .4124 | .4295 | .4465 | .4635 | .4805 | .4974 | .5143 | .5311 | .5479 | .5647 | 48 |
| 49 | .3956 | .4127 | .4298 | .4468 | .4638 | .4807 | .4977 | .5145 | .5314 | .5482 | .5650 | 49 |
| 50 | .3959 | .4130 | .4300 | .4471 | .4641 | .4810 | .4979 | .5148 | .5317 | .5485 | .5652 | 50 |
| 51 | .3962 | .4133 | .4303 | .4474 | .4643 | .4813 | .4982 | .5151 | .5320 | .5488 | .5655 | 51 |
| 52 | .3965 | .4135 | .4306 | .4476 | .4646 | .4816 | .4985 | .5154 | .5322 | .5490 | .5658 | 52 |
| 53 | .3967 | .4138 | .4309 | .4479 | .4649 | .4819 | .4988 | .5157 | .5325 | .5493 | .5661 | 53 |
| 54 | .3970 | .4141 | .4312 | .4482 | .4652 | .4822 | .4991 | .5160 | .5328 | .5496 | .5664 | 54 |
| 55 | .3973 | .4144 | .4315 | .4485 | .4655 | .4824 | .4994 | .5162 | .5331 | .5499 | .5666 | 55 |
| 56 | .3976 | .4147 | .4317 | .4488 | .4658 | .4827 | .4996 | .5165 | .5334 | .5502 | .5669 | 56 |
| 57 | .3979 | .4150 | .4320 | .4491 | .4660 | .4830 | .4999 | .5168 | .5336 | .5504 | .5672 | 57 |
| 58 | .3982 | .4153 | .4323 | .4493 | .4663 | .4833 | .5002 | .5171 | .5339 | .5507 | .5675 | 58 |
| 59 | .3985 | .4155 | .4326 | .4496 | .4666 | .4836 | .5005 | .5174 | .5342 | .5510 | .5678 | 59 |
| 60 | .3987 | .4158 | .4329 | .4499 | .4669 | .4838 | .5008 | .5176 | .5345 | .5513 | .5680 | 60 |

TABLE OF CHORDS: [RADIUS = 1.0000].

| M. | 32°   | 34°   | 35°   | 36°   | 37°   | 38°   | 39°   | 40°   | 41°   | 42°   | 43°   | M. |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| 0  | .5680 | .5847 | .6014 | .6180 | .6346 | .6511 | .6676 | .6840 | .7004 | .7167 | .7330 | 0  |
| 1  | .5683 | .5850 | .6017 | .6183 | .6349 | .6514 | .6679 | .6843 | .7007 | .7170 | .7333 | 1  |
| 2  | .5686 | .5853 | .6020 | .6186 | .6352 | .6517 | .6682 | .6846 | .7010 | .7173 | .7335 | 2  |
| 3  | .5689 | .5856 | .6022 | .6189 | .6354 | .6520 | .6684 | .6849 | .7012 | .7176 | .7338 | 3  |
| 4  | .5691 | .5859 | .6025 | .6191 | .6357 | .6522 | .6687 | .6851 | .7015 | .7178 | .7341 | 4  |
| 5  | .5694 | .5861 | .6028 | .6194 | .6360 | .6525 | .6690 | .6854 | .7018 | .7181 | .7344 | 5  |
| 6  | .5697 | .5864 | .6031 | .6197 | .6363 | .6528 | .6693 | .6857 | .7020 | .7184 | .7346 | 6  |
| 7  | .5700 | .5867 | .6034 | .6200 | .6365 | .6531 | .6695 | .6860 | .7023 | .7186 | .7349 | 7  |
| 8  | .5703 | .5870 | .6036 | .6202 | .6368 | .6533 | .6698 | .6862 | .7026 | .7189 | .7352 | 8  |
| 9  | .5705 | .5872 | .6039 | .6205 | .6371 | .6536 | .6701 | .6865 | .7029 | .7192 | .7354 | 9  |
| 10 | .5708 | .5875 | .6042 | .6208 | .6374 | .6539 | .6704 | .6868 | .7031 | .7195 | .7357 | 10 |
| 11 | .5711 | .5878 | .6045 | .6211 | .6376 | .6542 | .6706 | .6870 | .7034 | .7197 | .7360 | 11 |
| 12 | .5714 | .5881 | .6047 | .6214 | .6379 | .6544 | .6709 | .6873 | .7037 | .7200 | .7362 | 12 |
| 13 | .5717 | .5884 | .6050 | .6216 | .6382 | .6547 | .6712 | .6876 | .7040 | .7203 | .7365 | 13 |
| 14 | .5719 | .5886 | .6053 | .6219 | .6385 | .6550 | .6715 | .6879 | .7042 | .7205 | .7368 | 14 |
| 15 | .5722 | .5889 | .6056 | .6222 | .6387 | .6553 | .6717 | .6881 | .7045 | .7208 | .7371 | 15 |
| 16 | .5725 | .5892 | .6058 | .6225 | .6390 | .6555 | .6720 | .6884 | .7048 | .7211 | .7373 | 16 |
| 17 | .5728 | .5895 | .6061 | .6227 | .6393 | .6558 | .6723 | .6887 | .7050 | .7214 | .7376 | 17 |
| 18 | .5730 | .5897 | .6064 | .6230 | .6396 | .6561 | .6725 | .6890 | .7053 | .7216 | .7379 | 18 |
| 19 | .5733 | .5900 | .6067 | .6233 | .6398 | .6564 | .6728 | .6892 | .7056 | .7219 | .7381 | 19 |
| 20 | .5736 | .5903 | .6070 | .6236 | .6401 | .6566 | .6731 | .6895 | .7059 | .7222 | .7384 | 20 |
| 21 | .5739 | .5906 | .6072 | .6238 | .6404 | .6569 | .6734 | .6898 | .7061 | .7224 | .7387 | 21 |
| 22 | .5742 | .5909 | .6075 | .6241 | .6407 | .6572 | .6736 | .6901 | .7064 | .7227 | .7390 | 22 |
| 23 | .5744 | .5911 | .6078 | .6244 | .6410 | .6575 | .6739 | .6903 | .7067 | .7230 | .7392 | 23 |
| 24 | .5747 | .5914 | .6081 | .6247 | .6412 | .6577 | .6742 | .6906 | .7069 | .7232 | .7395 | 24 |
| 25 | .5750 | .5917 | .6083 | .6249 | .6415 | .6580 | .6745 | .6909 | .7072 | .7235 | .7398 | 25 |
| 26 | .5753 | .5920 | .6086 | .6252 | .6418 | .6583 | .6747 | .6911 | .7075 | .7238 | .7400 | 26 |
| 27 | .5756 | .5922 | .6089 | .6255 | .6421 | .6586 | .6750 | .6914 | .7078 | .7241 | .7403 | 27 |
| 28 | .5758 | .5925 | .6092 | .6258 | .6423 | .6588 | .6753 | .6917 | .7080 | .7243 | .7406 | 28 |
| 29 | .5761 | .5928 | .6095 | .6260 | .6426 | .6591 | .6756 | .6920 | .7083 | .7246 | .7408 | 29 |
| 30 | .5764 | .5931 | .6097 | .6263 | .6429 | .6594 | .6758 | .6922 | .7086 | .7249 | .7411 | 30 |
| 31 | .5767 | .5934 | .6100 | .6266 | .6432 | .6597 | .6761 | .6925 | .7089 | .7251 | .7414 | 31 |
| 32 | .5769 | .5936 | .6103 | .6269 | .6434 | .6599 | .6764 | .6928 | .7091 | .7254 | .7417 | 32 |
| 33 | .5772 | .5939 | .6106 | .6272 | .6437 | .6602 | .6767 | .6931 | .7094 | .7257 | .7419 | 33 |
| 34 | .5775 | .5942 | .6108 | .6274 | .6440 | .6605 | .6769 | .6933 | .7097 | .7260 | .7422 | 34 |
| 35 | .5778 | .5945 | .6111 | .6277 | .6443 | .6608 | .6772 | .6936 | .7099 | .7262 | .7425 | 35 |
| 36 | .5781 | .5947 | .6114 | .6280 | .6445 | .6610 | .6775 | .6939 | .7102 | .7265 | .7427 | 36 |
| 37 | .5783 | .5950 | .6117 | .6283 | .6448 | .6613 | .6777 | .6941 | .7105 | .7268 | .7430 | 37 |
| 38 | .5786 | .5953 | .6119 | .6285 | .6451 | .6616 | .6780 | .6944 | .7108 | .7270 | .7433 | 38 |
| 39 | .5789 | .5956 | .6122 | .6288 | .6454 | .6619 | .6783 | .6947 | .7110 | .7273 | .7435 | 39 |
| 40 | .5792 | .5959 | .6125 | .6291 | .6456 | .6621 | .6786 | .6950 | .7113 | .7276 | .7438 | 40 |
| 41 | .5795 | .5961 | .6128 | .6294 | .6459 | .6624 | .6788 | .6952 | .7116 | .7279 | .7441 | 41 |
| 42 | .5797 | .5964 | .6130 | .6296 | .6462 | .6627 | .6791 | .6955 | .7118 | .7281 | .7443 | 42 |
| 43 | .5800 | .5967 | .6133 | .6299 | .6465 | .6630 | .6794 | .6958 | .7121 | .7284 | .7446 | 43 |
| 44 | .5803 | .5970 | .6136 | .6302 | .6467 | .6632 | .6797 | .6961 | .7124 | .7287 | .7449 | 44 |
| 45 | .5806 | .5972 | .6139 | .6305 | .6470 | .6635 | .6799 | .6963 | .7127 | .7289 | .7452 | 45 |
| 46 | .5808 | .5975 | .6142 | .6307 | .6473 | .6638 | .6802 | .6966 | .7129 | .7292 | .7454 | 46 |
| 47 | .5811 | .5978 | .6144 | .6310 | .6476 | .6640 | .6805 | .6969 | .7132 | .7295 | .7457 | 47 |
| 48 | .5814 | .5981 | .6147 | .6313 | .6478 | .6643 | .6808 | .6971 | .7135 | .7298 | .7460 | 48 |
| 49 | .5817 | .5984 | .6150 | .6316 | .6481 | .6646 | .6810 | .6974 | .7137 | .7300 | .7462 | 49 |
| 50 | .5820 | .5986 | .6153 | .6318 | .6484 | .6649 | .6813 | .6977 | .7140 | .7303 | .7465 | 50 |
| 51 | .5822 | .5989 | .6155 | .6321 | .6487 | .6651 | .6816 | .6980 | .7143 | .7306 | .7468 | 51 |
| 52 | .5825 | .5992 | .6158 | .6324 | .6489 | .6654 | .6819 | .6982 | .7146 | .7308 | .7471 | 52 |
| 53 | .5828 | .5995 | .6161 | .6327 | .6492 | .6657 | .6821 | .6985 | .7148 | .7311 | .7473 | 53 |
| 54 | .5831 | .5997 | .6164 | .6330 | .6495 | .6660 | .6824 | .6988 | .7151 | .7314 | .7476 | 54 |
| 55 | .5834 | .6000 | .6166 | .6332 | .6498 | .6662 | .6827 | .6991 | .7154 | .7316 | .7479 | 55 |
| 56 | .5836 | .6003 | .6169 | .6335 | .6500 | .6665 | .6829 | .6993 | .7156 | .7319 | .7481 | 56 |
| 57 | .5839 | .6006 | .6172 | .6338 | .6503 | .6668 | .6832 | .6996 | .7159 | .7322 | .7484 | 57 |
| 58 | .5842 | .6009 | .6175 | .6341 | .6506 | .6671 | .6835 | .6999 | .7162 | .7325 | .7487 | 58 |
| 59 | .5845 | .6011 | .6178 | .6343 | .6509 | .6673 | .6838 | .7001 | .7165 | .7327 | .7489 | 59 |
| 60 | .5847 | .6014 | .6180 | .6346 | .6511 | .6676 | .6840 | .7004 | .7167 | .7330 | .7492 | 60 |

TABLE OF CHORDS: [RADIUS = 1.0000].

| M. | 44°   | 45°   | 46°   | 47°   | 48°   | 49°   | 50°   | 51°   | 52°   | 53°   | 54°   | M. |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|
| 0' | .7492 | .7654 | .7815 | .7975 | .8135 | .8294 | .8452 | .8610 | .8767 | .8924 | .9080 | 0' |
| 1  | .7495 | .7656 | .7817 | .7978 | .8137 | .8297 | .8455 | .8613 | .8770 | .8927 | .9082 | 1  |
| 2  | .7498 | .7659 | .7820 | .7980 | .8140 | .8299 | .8458 | .8615 | .8773 | .8929 | .9085 | 2  |
| 3  | .7500 | .7662 | .7823 | .7983 | .8143 | .8302 | .8460 | .8618 | .8775 | .8932 | .9088 | 3  |
| 4  | .7503 | .7664 | .7825 | .7986 | .8145 | .8304 | .8463 | .8621 | .8778 | .8934 | .9090 | 4  |
| 5  | .7506 | .7667 | .7828 | .7988 | .8148 | .8307 | .8466 | .8623 | .8780 | .8937 | .9093 | 5  |
| 6  | .7508 | .7670 | .7831 | .7991 | .8151 | .8310 | .8468 | .8626 | .8783 | .8940 | .9095 | 6  |
| 7  | .7511 | .7672 | .7833 | .7994 | .8153 | .8312 | .8471 | .8629 | .8786 | .8942 | .9098 | 7  |
| 8  | .7514 | .7675 | .7836 | .7996 | .8156 | .8315 | .8473 | .8631 | .8788 | .8945 | .9101 | 8  |
| 9  | .7516 | .7678 | .7839 | .7999 | .8159 | .8318 | .8476 | .8634 | .8791 | .8947 | .9103 | 9  |
| 10 | .7519 | .7681 | .7841 | .8002 | .8161 | .8320 | .8479 | .8636 | .8794 | .8950 | .9106 | 10 |
| 11 | .7522 | .7683 | .7844 | .8004 | .8164 | .8323 | .8481 | .8639 | .8796 | .8953 | .9108 | 11 |
| 12 | .7524 | .7686 | .7847 | .8007 | .8167 | .8326 | .8484 | .8642 | .8799 | .8955 | .9111 | 12 |
| 13 | .7527 | .7689 | .7849 | .8010 | .8169 | .8328 | .8487 | .8644 | .8801 | .8958 | .9113 | 13 |
| 14 | .7530 | .7691 | .7852 | .8012 | .8172 | .8331 | .8490 | .8647 | .8804 | .8960 | .9116 | 14 |
| 15 | .7533 | .7694 | .7855 | .8015 | .8175 | .8334 | .8492 | .8650 | .8807 | .8963 | .9119 | 15 |
| 16 | .7535 | .7697 | .7857 | .8018 | .8177 | .8336 | .8495 | .8652 | .8809 | .8966 | .9121 | 16 |
| 17 | .7538 | .7699 | .7860 | .8020 | .8180 | .8339 | .8497 | .8655 | .8812 | .8968 | .9124 | 17 |
| 18 | .7541 | .7702 | .7863 | .8023 | .8183 | .8341 | .8500 | .8657 | .8814 | .8971 | .9126 | 18 |
| 19 | .7543 | .7705 | .7865 | .8026 | .8185 | .8344 | .8502 | .8660 | .8817 | .8973 | .9129 | 19 |
| 20 | .7546 | .7707 | .7868 | .8028 | .8188 | .8347 | .8505 | .8663 | .8820 | .8976 | .9132 | 20 |
| 21 | .7549 | .7710 | .7871 | .8031 | .8190 | .8349 | .8508 | .8665 | .8822 | .8979 | .9134 | 21 |
| 22 | .7551 | .7713 | .7873 | .8034 | .8193 | .8352 | .8510 | .8668 | .8825 | .8981 | .9137 | 22 |
| 23 | .7554 | .7715 | .7876 | .8036 | .8196 | .8355 | .8513 | .8671 | .8828 | .8984 | .9139 | 23 |
| 24 | .7557 | .7718 | .7879 | .8039 | .8198 | .8357 | .8516 | .8673 | .8830 | .8986 | .9142 | 24 |
| 25 | .7560 | .7721 | .7882 | .8042 | .8201 | .8360 | .8518 | .8676 | .8833 | .8989 | .9145 | 25 |
| 26 | .7562 | .7723 | .7884 | .8044 | .8204 | .8363 | .8521 | .8678 | .8835 | .8992 | .9147 | 26 |
| 27 | .7565 | .7726 | .7887 | .8047 | .8206 | .8365 | .8523 | .8681 | .8838 | .8994 | .9150 | 27 |
| 28 | .7568 | .7729 | .7890 | .8050 | .8209 | .8368 | .8526 | .8684 | .8841 | .8997 | .9152 | 28 |
| 29 | .7570 | .7731 | .7892 | .8052 | .8212 | .8371 | .8529 | .8686 | .8843 | .8999 | .9155 | 29 |
| 30 | .7573 | .7734 | .7895 | .8055 | .8214 | .8373 | .8531 | .8689 | .8846 | .9002 | .9157 | 30 |
| 31 | .7576 | .7737 | .7898 | .8058 | .8217 | .8376 | .8534 | .8692 | .8848 | .9005 | .9160 | 31 |
| 32 | .7578 | .7740 | .7900 | .8060 | .8220 | .8378 | .8537 | .8694 | .8851 | .9007 | .9163 | 32 |
| 33 | .7581 | .7742 | .7903 | .8063 | .8222 | .8381 | .8539 | .8697 | .8854 | .9010 | .9165 | 33 |
| 34 | .7584 | .7745 | .7906 | .8066 | .8225 | .8384 | .8542 | .8699 | .8856 | .9012 | .9168 | 34 |
| 35 | .7586 | .7748 | .7908 | .8068 | .8228 | .8386 | .8545 | .8702 | .8859 | .9015 | .9170 | 35 |
| 36 | .7589 | .7750 | .7911 | .8071 | .8230 | .8389 | .8547 | .8705 | .8861 | .9018 | .9173 | 36 |
| 37 | .7592 | .7753 | .7914 | .8074 | .8233 | .8392 | .8550 | .8707 | .8864 | .9020 | .9176 | 37 |
| 38 | .7595 | .7756 | .7916 | .8076 | .8236 | .8394 | .8552 | .8710 | .8867 | .9023 | .9178 | 38 |
| 39 | .7597 | .7758 | .7919 | .8079 | .8238 | .8397 | .8555 | .8712 | .8869 | .9025 | .9181 | 39 |
| 40 | .7600 | .7761 | .7922 | .8082 | .8241 | .8400 | .8558 | .8715 | .8872 | .9028 | .9183 | 40 |
| 41 | .7603 | .7764 | .7924 | .8084 | .8244 | .8402 | .8560 | .8718 | .8874 | .9031 | .9186 | 41 |
| 42 | .7605 | .7766 | .7927 | .8087 | .8246 | .8405 | .8563 | .8720 | .8877 | .9033 | .9188 | 42 |
| 43 | .7608 | .7769 | .7930 | .8090 | .8249 | .8408 | .8566 | .8723 | .8880 | .9036 | .9191 | 43 |
| 44 | .7611 | .7772 | .7932 | .8092 | .8251 | .8410 | .8568 | .8726 | .8882 | .9038 | .9194 | 44 |
| 45 | .7613 | .7774 | .7935 | .8095 | .8254 | .8413 | .8571 | .8728 | .8885 | .9041 | .9196 | 45 |
| 46 | .7616 | .7777 | .7938 | .8098 | .8257 | .8415 | .8573 | .8731 | .8887 | .9044 | .9199 | 46 |
| 47 | .7619 | .7780 | .7940 | .8100 | .8259 | .8418 | .8576 | .8734 | .8890 | .9046 | .9201 | 47 |
| 48 | .7621 | .7782 | .7943 | .8103 | .8262 | .8421 | .8579 | .8736 | .8893 | .9049 | .9204 | 48 |
| 49 | .7624 | .7785 | .7946 | .8105 | .8265 | .8423 | .8581 | .8739 | .8895 | .9051 | .9207 | 49 |
| 50 | .7627 | .7788 | .7948 | .8108 | .8267 | .8426 | .8584 | .8741 | .8898 | .9054 | .9209 | 50 |
| 51 | .7629 | .7791 | .7951 | .8111 | .8270 | .8429 | .8587 | .8744 | .8900 | .9056 | .9212 | 51 |
| 52 | .7632 | .7793 | .7954 | .8113 | .8273 | .8431 | .8589 | .8747 | .8903 | .9059 | .9214 | 52 |
| 53 | .7635 | .7796 | .7956 | .8116 | .8275 | .8434 | .8592 | .8749 | .8906 | .9062 | .9217 | 53 |
| 54 | .7638 | .7799 | .7959 | .8119 | .8278 | .8437 | .8594 | .8752 | .8908 | .9064 | .9219 | 54 |
| 55 | .7640 | .7801 | .7962 | .8121 | .8281 | .8439 | .8597 | .8754 | .8911 | .9067 | .9222 | 55 |
| 56 | .7643 | .7804 | .7964 | .8124 | .8283 | .8442 | .8600 | .8757 | .8914 | .9069 | .9225 | 56 |
| 57 | .7646 | .7807 | .7967 | .8127 | .8286 | .8444 | .8602 | .8760 | .8916 | .9072 | .9227 | 57 |
| 58 | .7648 | .7809 | .7970 | .8129 | .8289 | .8447 | .8605 | .8762 | .8919 | .9075 | .9230 | 58 |
| 59 | .7651 | .7812 | .7972 | .8132 | .8291 | .8450 | .8608 | .8765 | .8921 | .9077 | .9232 | 59 |
| 60 | .7654 | .7815 | .7975 | .8135 | .8294 | .8452 | .8610 | .8767 | .8924 | .9080 | .9235 | 60 |

TABLE OF CHORDS: [RADIUS = 1.0000].

| x. | 55°   | 56°   | 57°   | 58°   | 59°    | 60°    | 61°    | 62°    | 63°    | 64°    | x. |
|----|-------|-------|-------|-------|--------|--------|--------|--------|--------|--------|----|
| 0  | .9235 | .9389 | .9543 | .9696 | .9848  | 1.0000 | 1.0151 | 1.0301 | 1.0450 | 1.0598 | 0  |
| 1  | .9238 | .9392 | .9546 | .9699 | .9851  | 1.0003 | 1.0153 | 1.0303 | 1.0452 | 1.0601 | 1  |
| 2  | .9240 | .9395 | .9549 | .9701 | .9854  | 1.0005 | 1.0156 | 1.0306 | 1.0455 | 1.0603 | 2  |
| 3  | .9243 | .9397 | .9551 | .9704 | .9856  | 1.0008 | 1.0158 | 1.0308 | 1.0457 | 1.0606 | 3  |
| 4  | .9245 | .9400 | .9553 | .9706 | .9859  | 1.0010 | 1.0161 | 1.0311 | 1.0460 | 1.0608 | 4  |
| 5  | .9248 | .9402 | .9556 | .9709 | .9861  | 1.0013 | 1.0163 | 1.0313 | 1.0462 | 1.0611 | 5  |
| 6  | .9250 | .9405 | .9559 | .9711 | .9864  | 1.0015 | 1.0166 | 1.0316 | 1.0465 | 1.0613 | 6  |
| 7  | .9253 | .9407 | .9561 | .9714 | .9866  | 1.0018 | 1.0168 | 1.0318 | 1.0467 | 1.0616 | 7  |
| 8  | .9256 | .9410 | .9564 | .9717 | .9869  | 1.0020 | 1.0171 | 1.0321 | 1.0470 | 1.0618 | 8  |
| 9  | .9258 | .9413 | .9566 | .9719 | .9871  | 1.0023 | 1.0173 | 1.0323 | 1.0472 | 1.0621 | 9  |
| 10 | .9261 | .9415 | .9569 | .9722 | .9874  | 1.0025 | 1.0176 | 1.0326 | 1.0475 | 1.0623 | 10 |
| 11 | .9263 | .9418 | .9571 | .9724 | .9876  | 1.0028 | 1.0178 | 1.0328 | 1.0477 | 1.0626 | 11 |
| 12 | .9266 | .9420 | .9574 | .9727 | .9879  | 1.0030 | 1.0181 | 1.0331 | 1.0480 | 1.0628 | 12 |
| 13 | .9268 | .9423 | .9576 | .9729 | .9881  | 1.0033 | 1.0183 | 1.0333 | 1.0482 | 1.0630 | 13 |
| 14 | .9271 | .9425 | .9579 | .9732 | .9884  | 1.0035 | 1.0186 | 1.0336 | 1.0485 | 1.0633 | 14 |
| 15 | .9274 | .9428 | .9581 | .9734 | .9886  | 1.0038 | 1.0188 | 1.0338 | 1.0487 | 1.0635 | 15 |
| 16 | .9276 | .9430 | .9584 | .9737 | .9889  | 1.0040 | 1.0191 | 1.0341 | 1.0490 | 1.0638 | 16 |
| 17 | .9279 | .9433 | .9587 | .9739 | .9891  | 1.0043 | 1.0193 | 1.0343 | 1.0492 | 1.0640 | 17 |
| 18 | .9281 | .9436 | .9589 | .9742 | .9894  | 1.0045 | 1.0196 | 1.0346 | 1.0495 | 1.0643 | 18 |
| 19 | .9284 | .9438 | .9592 | .9744 | .9897  | 1.0048 | 1.0198 | 1.0348 | 1.0497 | 1.0645 | 19 |
| 20 | .9287 | .9441 | .9594 | .9747 | .9899  | 1.0050 | 1.0201 | 1.0351 | 1.0500 | 1.0648 | 20 |
| 21 | .9289 | .9443 | .9597 | .9750 | .9902  | 1.0053 | 1.0203 | 1.0353 | 1.0502 | 1.0650 | 21 |
| 22 | .9292 | .9446 | .9599 | .9752 | .9904  | 1.0055 | 1.0206 | 1.0356 | 1.0504 | 1.0653 | 22 |
| 23 | .9294 | .9448 | .9602 | .9755 | .9907  | 1.0058 | 1.0208 | 1.0358 | 1.0507 | 1.0655 | 23 |
| 24 | .9297 | .9451 | .9604 | .9757 | .9909  | 1.0060 | 1.0211 | 1.0361 | 1.0509 | 1.0658 | 24 |
| 25 | .9299 | .9454 | .9607 | .9760 | .9912  | 1.0063 | 1.0213 | 1.0363 | 1.0512 | 1.0660 | 25 |
| 26 | .9302 | .9456 | .9610 | .9762 | .9914  | 1.0065 | 1.0216 | 1.0366 | 1.0514 | 1.0662 | 26 |
| 27 | .9305 | .9459 | .9612 | .9765 | .9917  | 1.0068 | 1.0218 | 1.0368 | 1.0517 | 1.0665 | 27 |
| 28 | .9307 | .9461 | .9615 | .9767 | .9919  | 1.0070 | 1.0221 | 1.0370 | 1.0519 | 1.0667 | 28 |
| 29 | .9310 | .9464 | .9617 | .9770 | .9922  | 1.0073 | 1.0223 | 1.0373 | 1.0522 | 1.0670 | 29 |
| 30 | .9312 | .9466 | .9620 | .9772 | .9924  | 1.0075 | 1.0226 | 1.0375 | 1.0524 | 1.0672 | 30 |
| 31 | .9315 | .9469 | .9622 | .9775 | .9927  | 1.0078 | 1.0228 | 1.0378 | 1.0527 | 1.0675 | 31 |
| 32 | .9317 | .9472 | .9625 | .9778 | .9929  | 1.0080 | 1.0231 | 1.0380 | 1.0529 | 1.0677 | 32 |
| 33 | .9320 | .9474 | .9627 | .9780 | .9932  | 1.0083 | 1.0233 | 1.0383 | 1.0532 | 1.0680 | 33 |
| 34 | .9323 | .9477 | .9630 | .9783 | .9934  | 1.0086 | 1.0236 | 1.0385 | 1.0534 | 1.0682 | 34 |
| 35 | .9325 | .9479 | .9633 | .9785 | .9937  | 1.0088 | 1.0238 | 1.0388 | 1.0537 | 1.0685 | 35 |
| 36 | .9328 | .9482 | .9635 | .9788 | .9939  | 1.0091 | 1.0241 | 1.0390 | 1.0539 | 1.0687 | 36 |
| 37 | .9330 | .9484 | .9638 | .9790 | .9942  | 1.0093 | 1.0243 | 1.0393 | 1.0542 | 1.0690 | 37 |
| 38 | .9333 | .9487 | .9640 | .9793 | .9945  | 1.0096 | 1.0246 | 1.0395 | 1.0544 | 1.0692 | 38 |
| 39 | .9335 | .9489 | .9642 | .9795 | .9947  | 1.0098 | 1.0248 | 1.0398 | 1.0547 | 1.0694 | 39 |
| 40 | .9338 | .9492 | .9645 | .9798 | .9950  | 1.0101 | 1.0251 | 1.0400 | 1.0549 | 1.0697 | 40 |
| 41 | .9341 | .9495 | .9648 | .9800 | .9952  | 1.0103 | 1.0253 | 1.0403 | 1.0551 | 1.0699 | 41 |
| 42 | .9343 | .9497 | .9650 | .9803 | .9955  | 1.0106 | 1.0256 | 1.0405 | 1.0554 | 1.0702 | 42 |
| 43 | .9346 | .9500 | .9653 | .9805 | .9957  | 1.0108 | 1.0258 | 1.0408 | 1.0556 | 1.0704 | 43 |
| 44 | .9348 | .9502 | .9655 | .9808 | .9960  | 1.0111 | 1.0261 | 1.0410 | 1.0559 | 1.0707 | 44 |
| 45 | .9351 | .9505 | .9658 | .9810 | .9962  | 1.0113 | 1.0263 | 1.0413 | 1.0561 | 1.0709 | 45 |
| 46 | .9353 | .9507 | .9661 | .9813 | .9965  | 1.0116 | 1.0266 | 1.0415 | 1.0564 | 1.0712 | 46 |
| 47 | .9356 | .9510 | .9663 | .9816 | .9967  | 1.0118 | 1.0268 | 1.0418 | 1.0566 | 1.0714 | 47 |
| 48 | .9359 | .9512 | .9666 | .9818 | .9970  | 1.0121 | 1.0271 | 1.0420 | 1.0569 | 1.0717 | 48 |
| 49 | .9361 | .9515 | .9668 | .9821 | .9972  | 1.0123 | 1.0273 | 1.0423 | 1.0571 | 1.0719 | 49 |
| 50 | .9364 | .9518 | .9671 | .9823 | .9975  | 1.0126 | 1.0276 | 1.0425 | 1.0574 | 1.0721 | 50 |
| 51 | .9366 | .9520 | .9673 | .9826 | .9977  | 1.0128 | 1.0278 | 1.0428 | 1.0576 | 1.0724 | 51 |
| 52 | .9369 | .9523 | .9676 | .9828 | .9980  | 1.0131 | 1.0281 | 1.0430 | 1.0579 | 1.0726 | 52 |
| 53 | .9371 | .9525 | .9678 | .9831 | .9982  | 1.0133 | 1.0283 | 1.0433 | 1.0581 | 1.0729 | 53 |
| 54 | .9374 | .9528 | .9681 | .9833 | .9985  | 1.0136 | 1.0286 | 1.0435 | 1.0584 | 1.0731 | 54 |
| 55 | .9377 | .9530 | .9683 | .9836 | .9987  | 1.0138 | 1.0288 | 1.0438 | 1.0586 | 1.0734 | 55 |
| 56 | .9379 | .9533 | .9686 | .9838 | .9990  | 1.0141 | 1.0291 | 1.0440 | 1.0589 | 1.0736 | 56 |
| 57 | .9382 | .9536 | .9689 | .9841 | .9992  | 1.0143 | 1.0293 | 1.0443 | 1.0591 | 1.0739 | 57 |
| 58 | .9384 | .9538 | .9691 | .9843 | .9995  | 1.0146 | 1.0296 | 1.0445 | 1.0593 | 1.0741 | 58 |
| 59 | .9387 | .9541 | .9694 | .9846 | .9998  | 1.0148 | 1.0298 | 1.0447 | 1.0596 | 1.0744 | 59 |
| 60 | .9389 | .9543 | .9696 | .9848 | 1.0000 | 1.0151 | 1.0301 | 1.0450 | 1.0598 | 1.0746 | 60 |

TABLE OF CHORDS: [RADIUS = 1.0000].

| $\alpha$ | 65°    | 66°    | 67°    | 68°    | 69°    | 70°    | 71°    | 72°    | 73°    | $\alpha$ |
|----------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----------|
| 0'       | 1.0746 | 1.0893 | 1.1039 | 1.1184 | 1.1328 | 1.1472 | 1.1614 | 1.1756 | 1.1896 | 0        |
| 1        | 1.0748 | 1.0895 | 1.1041 | 1.1186 | 1.1331 | 1.1474 | 1.1616 | 1.1758 | 1.1899 | 1        |
| 2        | 1.0751 | 1.0898 | 1.1044 | 1.1189 | 1.1333 | 1.1476 | 1.1619 | 1.1760 | 1.1901 | 2        |
| 3        | 1.0753 | 1.0900 | 1.1046 | 1.1191 | 1.1335 | 1.1479 | 1.1621 | 1.1763 | 1.1903 | 3        |
| 4        | 1.0756 | 1.0903 | 1.1048 | 1.1194 | 1.1338 | 1.1481 | 1.1624 | 1.1765 | 1.1906 | 4        |
| 5        | 1.0758 | 1.0905 | 1.1051 | 1.1196 | 1.1340 | 1.1483 | 1.1626 | 1.1767 | 1.1908 | 5        |
| 6        | 1.0761 | 1.0907 | 1.1053 | 1.1198 | 1.1342 | 1.1486 | 1.1628 | 1.1770 | 1.1910 | 6        |
| 7        | 1.0763 | 1.0910 | 1.1056 | 1.1201 | 1.1345 | 1.1488 | 1.1631 | 1.1772 | 1.1913 | 7        |
| 8        | 1.0766 | 1.0912 | 1.1058 | 1.1203 | 1.1347 | 1.1491 | 1.1633 | 1.1775 | 1.1915 | 8        |
| 9        | 1.0768 | 1.0915 | 1.1061 | 1.1206 | 1.1350 | 1.1493 | 1.1635 | 1.1777 | 1.1917 | 9        |
| 10       | 1.0771 | 1.0917 | 1.1063 | 1.1208 | 1.1352 | 1.1495 | 1.1638 | 1.1779 | 1.1920 | 10       |
| 11       | 1.0773 | 1.0920 | 1.1065 | 1.1210 | 1.1354 | 1.1498 | 1.1640 | 1.1782 | 1.1922 | 11       |
| 12       | 1.0775 | 1.0922 | 1.1068 | 1.1213 | 1.1357 | 1.1500 | 1.1642 | 1.1784 | 1.1924 | 12       |
| 13       | 1.0778 | 1.0924 | 1.1070 | 1.1215 | 1.1359 | 1.1502 | 1.1645 | 1.1786 | 1.1927 | 13       |
| 14       | 1.0780 | 1.0927 | 1.1073 | 1.1218 | 1.1362 | 1.1505 | 1.1647 | 1.1789 | 1.1929 | 14       |
| 15       | 1.0783 | 1.0929 | 1.1075 | 1.1220 | 1.1364 | 1.1507 | 1.1650 | 1.1791 | 1.1931 | 15       |
| 16       | 1.0785 | 1.0932 | 1.1078 | 1.1222 | 1.1366 | 1.1510 | 1.1652 | 1.1793 | 1.1934 | 16       |
| 17       | 1.0788 | 1.0934 | 1.1080 | 1.1225 | 1.1369 | 1.1512 | 1.1654 | 1.1796 | 1.1936 | 17       |
| 18       | 1.0790 | 1.0937 | 1.1082 | 1.1227 | 1.1371 | 1.1514 | 1.1657 | 1.1798 | 1.1938 | 18       |
| 19       | 1.0793 | 1.0939 | 1.1085 | 1.1230 | 1.1374 | 1.1517 | 1.1659 | 1.1800 | 1.1941 | 19       |
| 20       | 1.0795 | 1.0942 | 1.1087 | 1.1232 | 1.1376 | 1.1519 | 1.1661 | 1.1803 | 1.1943 | 20       |
| 21       | 1.0797 | 1.0944 | 1.1090 | 1.1234 | 1.1378 | 1.1522 | 1.1664 | 1.1805 | 1.1946 | 21       |
| 22       | 1.0800 | 1.0946 | 1.1092 | 1.1237 | 1.1381 | 1.1524 | 1.1666 | 1.1807 | 1.1948 | 22       |
| 23       | 1.0802 | 1.0949 | 1.1094 | 1.1239 | 1.1383 | 1.1526 | 1.1668 | 1.1810 | 1.1950 | 23       |
| 24       | 1.0805 | 1.0951 | 1.1097 | 1.1242 | 1.1386 | 1.1529 | 1.1671 | 1.1812 | 1.1952 | 24       |
| 25       | 1.0807 | 1.0954 | 1.1099 | 1.1244 | 1.1388 | 1.1531 | 1.1673 | 1.1814 | 1.1955 | 25       |
| 26       | 1.0810 | 1.0956 | 1.1102 | 1.1246 | 1.1390 | 1.1533 | 1.1676 | 1.1817 | 1.1957 | 26       |
| 27       | 1.0812 | 1.0959 | 1.1104 | 1.1249 | 1.1393 | 1.1536 | 1.1678 | 1.1819 | 1.1959 | 27       |
| 28       | 1.0815 | 1.0961 | 1.1107 | 1.1251 | 1.1395 | 1.1538 | 1.1680 | 1.1821 | 1.1962 | 28       |
| 29       | 1.0817 | 1.0963 | 1.1109 | 1.1254 | 1.1398 | 1.1541 | 1.1683 | 1.1824 | 1.1964 | 29       |
| 30       | 1.0820 | 1.0966 | 1.1111 | 1.1256 | 1.1400 | 1.1543 | 1.1685 | 1.1826 | 1.1966 | 30       |
| 31       | 1.0822 | 1.0968 | 1.1114 | 1.1258 | 1.1402 | 1.1545 | 1.1687 | 1.1829 | 1.1969 | 31       |
| 32       | 1.0824 | 1.0971 | 1.1116 | 1.1261 | 1.1405 | 1.1548 | 1.1690 | 1.1831 | 1.1971 | 32       |
| 33       | 1.0827 | 1.0973 | 1.1119 | 1.1263 | 1.1407 | 1.1550 | 1.1692 | 1.1833 | 1.1973 | 33       |
| 34       | 1.0829 | 1.0976 | 1.1121 | 1.1266 | 1.1409 | 1.1552 | 1.1694 | 1.1836 | 1.1976 | 34       |
| 35       | 1.0832 | 1.0978 | 1.1123 | 1.1268 | 1.1412 | 1.1555 | 1.1697 | 1.1838 | 1.1978 | 35       |
| 36       | 1.0834 | 1.0980 | 1.1126 | 1.1271 | 1.1414 | 1.1557 | 1.1699 | 1.1840 | 1.1980 | 36       |
| 37       | 1.0837 | 1.0983 | 1.1128 | 1.1273 | 1.1417 | 1.1560 | 1.1702 | 1.1843 | 1.1983 | 37       |
| 38       | 1.0839 | 1.0985 | 1.1131 | 1.1275 | 1.1419 | 1.1562 | 1.1704 | 1.1845 | 1.1985 | 38       |
| 39       | 1.0841 | 1.0988 | 1.1133 | 1.1278 | 1.1421 | 1.1564 | 1.1706 | 1.1847 | 1.1987 | 39       |
| 40       | 1.0844 | 1.0990 | 1.1136 | 1.1280 | 1.1424 | 1.1567 | 1.1709 | 1.1850 | 1.1990 | 40       |
| 41       | 1.0846 | 1.0993 | 1.1138 | 1.1283 | 1.1426 | 1.1569 | 1.1711 | 1.1852 | 1.1992 | 41       |
| 42       | 1.0849 | 1.0995 | 1.1140 | 1.1285 | 1.1429 | 1.1571 | 1.1713 | 1.1854 | 1.1994 | 42       |
| 43       | 1.0851 | 1.0997 | 1.1143 | 1.1287 | 1.1431 | 1.1574 | 1.1716 | 1.1857 | 1.1997 | 43       |
| 44       | 1.0854 | 1.1000 | 1.1145 | 1.1290 | 1.1433 | 1.1576 | 1.1719 | 1.1859 | 1.1999 | 44       |
| 45       | 1.0856 | 1.1002 | 1.1148 | 1.1292 | 1.1436 | 1.1579 | 1.1720 | 1.1861 | 1.2001 | 45       |
| 46       | 1.0859 | 1.1005 | 1.1150 | 1.1295 | 1.1438 | 1.1581 | 1.1723 | 1.1864 | 1.2004 | 46       |
| 47       | 1.0861 | 1.1007 | 1.1152 | 1.1297 | 1.1441 | 1.1583 | 1.1725 | 1.1866 | 1.2006 | 47       |
| 48       | 1.0863 | 1.1010 | 1.1155 | 1.1299 | 1.1443 | 1.1586 | 1.1727 | 1.1868 | 1.2008 | 48       |
| 49       | 1.0866 | 1.1012 | 1.1157 | 1.1302 | 1.1445 | 1.1588 | 1.1730 | 1.1871 | 1.2011 | 49       |
| 50       | 1.0868 | 1.1014 | 1.1160 | 1.1304 | 1.1448 | 1.1590 | 1.1732 | 1.1873 | 1.2013 | 50       |
| 51       | 1.0871 | 1.1017 | 1.1162 | 1.1307 | 1.1450 | 1.1593 | 1.1735 | 1.1875 | 1.2015 | 51       |
| 52       | 1.0873 | 1.1019 | 1.1165 | 1.1309 | 1.1452 | 1.1595 | 1.1737 | 1.1878 | 1.2018 | 52       |
| 53       | 1.0876 | 1.1022 | 1.1167 | 1.1311 | 1.1455 | 1.1598 | 1.1739 | 1.1880 | 1.2020 | 53       |
| 54       | 1.0878 | 1.1024 | 1.1169 | 1.1314 | 1.1457 | 1.1600 | 1.1742 | 1.1882 | 1.2022 | 54       |
| 55       | 1.0881 | 1.1027 | 1.1172 | 1.1316 | 1.1460 | 1.1602 | 1.1744 | 1.1885 | 1.2025 | 55       |
| 56       | 1.0883 | 1.1029 | 1.1174 | 1.1319 | 1.1462 | 1.1605 | 1.1746 | 1.1887 | 1.2027 | 56       |
| 57       | 1.0885 | 1.1031 | 1.1177 | 1.1321 | 1.1464 | 1.1607 | 1.1749 | 1.1889 | 1.2029 | 57       |
| 58       | 1.0888 | 1.1034 | 1.1179 | 1.1323 | 1.1467 | 1.1609 | 1.1751 | 1.1892 | 1.2032 | 58       |
| 59       | 1.0890 | 1.1036 | 1.1181 | 1.1326 | 1.1469 | 1.1612 | 1.1753 | 1.1894 | 1.2034 | 59       |
| 60       | 1.0893 | 1.1039 | 1.1184 | 1.1328 | 1.1472 | 1.1614 | 1.1756 | 1.1896 | 1.2036 | 60       |

TABLE OF CHORDS: [RADIUS = 1.0000].

| M. | 74°    | 75°    | 76°    | 77°    | 78°    | 79°    | 80°    | 81°    | 82°    | M. |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0' | 1.2036 | 1.2175 | 1.2313 | 1.2450 | 1.2586 | 1.2722 | 1.2856 | 1.2989 | 1.3121 | 0' |
| 1  | 1.2039 | 1.2178 | 1.2316 | 1.2453 | 1.2589 | 1.2724 | 1.2858 | 1.2991 | 1.3123 | 1  |
| 2  | 1.2041 | 1.2180 | 1.2318 | 1.2455 | 1.2591 | 1.2726 | 1.2860 | 1.2993 | 1.3126 | 2  |
| 3  | 1.2043 | 1.2182 | 1.2320 | 1.2457 | 1.2593 | 1.2728 | 1.2862 | 1.2996 | 1.3128 | 3  |
| 4  | 1.2046 | 1.2184 | 1.2322 | 1.2459 | 1.2595 | 1.2731 | 1.2865 | 1.2998 | 1.3130 | 4  |
| 5  | 1.2048 | 1.2187 | 1.2325 | 1.2462 | 1.2598 | 1.2733 | 1.2867 | 1.3000 | 1.3132 | 5  |
| 6  | 1.2050 | 1.2189 | 1.2327 | 1.2464 | 1.2600 | 1.2735 | 1.2869 | 1.3002 | 1.3134 | 6  |
| 7  | 1.2053 | 1.2191 | 1.2329 | 1.2466 | 1.2602 | 1.2737 | 1.2871 | 1.3004 | 1.3137 | 7  |
| 8  | 1.2055 | 1.2194 | 1.2332 | 1.2468 | 1.2604 | 1.2740 | 1.2874 | 1.3007 | 1.3139 | 8  |
| 9  | 1.2057 | 1.2196 | 1.2334 | 1.2471 | 1.2607 | 1.2742 | 1.2876 | 1.3009 | 1.3141 | 9  |
| 10 | 1.2060 | 1.2198 | 1.2336 | 1.2473 | 1.2609 | 1.2744 | 1.2878 | 1.3011 | 1.3143 | 10 |
| 11 | 1.2062 | 1.2201 | 1.2338 | 1.2475 | 1.2611 | 1.2746 | 1.2880 | 1.3013 | 1.3145 | 11 |
| 12 | 1.2064 | 1.2203 | 1.2341 | 1.2478 | 1.2614 | 1.2748 | 1.2882 | 1.3015 | 1.3147 | 12 |
| 13 | 1.2066 | 1.2205 | 1.2343 | 1.2480 | 1.2616 | 1.2751 | 1.2885 | 1.3018 | 1.3150 | 13 |
| 14 | 1.2069 | 1.2208 | 1.2345 | 1.2482 | 1.2618 | 1.2753 | 1.2887 | 1.3020 | 1.3152 | 14 |
| 15 | 1.2071 | 1.2210 | 1.2348 | 1.2484 | 1.2620 | 1.2755 | 1.2889 | 1.3022 | 1.3154 | 15 |
| 16 | 1.2073 | 1.2212 | 1.2350 | 1.2487 | 1.2623 | 1.2757 | 1.2891 | 1.3024 | 1.3156 | 16 |
| 17 | 1.2076 | 1.2214 | 1.2352 | 1.2489 | 1.2625 | 1.2760 | 1.2894 | 1.3027 | 1.3158 | 17 |
| 18 | 1.2078 | 1.2217 | 1.2354 | 1.2491 | 1.2627 | 1.2762 | 1.2896 | 1.3029 | 1.3161 | 18 |
| 19 | 1.2080 | 1.2219 | 1.2357 | 1.2493 | 1.2629 | 1.2764 | 1.2898 | 1.3031 | 1.3163 | 19 |
| 20 | 1.2083 | 1.2221 | 1.2359 | 1.2496 | 1.2632 | 1.2766 | 1.2900 | 1.3033 | 1.3165 | 20 |
| 21 | 1.2085 | 1.2224 | 1.2361 | 1.2498 | 1.2634 | 1.2769 | 1.2903 | 1.3035 | 1.3167 | 21 |
| 22 | 1.2087 | 1.2226 | 1.2364 | 1.2500 | 1.2636 | 1.2771 | 1.2905 | 1.3038 | 1.3169 | 22 |
| 23 | 1.2090 | 1.2228 | 1.2366 | 1.2503 | 1.2638 | 1.2773 | 1.2907 | 1.3040 | 1.3172 | 23 |
| 24 | 1.2092 | 1.2231 | 1.2368 | 1.2505 | 1.2641 | 1.2775 | 1.2909 | 1.3042 | 1.3174 | 24 |
| 25 | 1.2094 | 1.2233 | 1.2370 | 1.2507 | 1.2643 | 1.2778 | 1.2911 | 1.3044 | 1.3176 | 25 |
| 26 | 1.2097 | 1.2235 | 1.2373 | 1.2509 | 1.2645 | 1.2780 | 1.2914 | 1.3046 | 1.3178 | 26 |
| 27 | 1.2099 | 1.2237 | 1.2375 | 1.2512 | 1.2648 | 1.2782 | 1.2916 | 1.3049 | 1.3180 | 27 |
| 28 | 1.2101 | 1.2240 | 1.2377 | 1.2514 | 1.2650 | 1.2784 | 1.2918 | 1.3051 | 1.3183 | 28 |
| 29 | 1.2104 | 1.2242 | 1.2380 | 1.2516 | 1.2652 | 1.2787 | 1.2920 | 1.3053 | 1.3185 | 29 |
| 30 | 1.2106 | 1.2244 | 1.2382 | 1.2518 | 1.2654 | 1.2789 | 1.2922 | 1.3055 | 1.3187 | 30 |
| 31 | 1.2108 | 1.2247 | 1.2384 | 1.2521 | 1.2656 | 1.2791 | 1.2925 | 1.3057 | 1.3189 | 31 |
| 32 | 1.2111 | 1.2249 | 1.2386 | 1.2523 | 1.2659 | 1.2793 | 1.2927 | 1.3060 | 1.3191 | 32 |
| 33 | 1.2113 | 1.2251 | 1.2389 | 1.2525 | 1.2661 | 1.2795 | 1.2929 | 1.3062 | 1.3193 | 33 |
| 34 | 1.2115 | 1.2254 | 1.2391 | 1.2528 | 1.2663 | 1.2798 | 1.2931 | 1.3064 | 1.3196 | 34 |
| 35 | 1.2117 | 1.2256 | 1.2393 | 1.2530 | 1.2665 | 1.2800 | 1.2934 | 1.3066 | 1.3198 | 35 |
| 36 | 1.2120 | 1.2258 | 1.2396 | 1.2532 | 1.2668 | 1.2802 | 1.2936 | 1.3068 | 1.3200 | 36 |
| 37 | 1.2122 | 1.2260 | 1.2398 | 1.2534 | 1.2670 | 1.2804 | 1.2938 | 1.3071 | 1.3202 | 37 |
| 38 | 1.2124 | 1.2263 | 1.2400 | 1.2537 | 1.2672 | 1.2807 | 1.2940 | 1.3073 | 1.3204 | 38 |
| 39 | 1.2127 | 1.2265 | 1.2402 | 1.2539 | 1.2674 | 1.2809 | 1.2942 | 1.3075 | 1.3207 | 39 |
| 40 | 1.2129 | 1.2267 | 1.2405 | 1.2541 | 1.2677 | 1.2811 | 1.2945 | 1.3077 | 1.3209 | 40 |
| 41 | 1.2131 | 1.2270 | 1.2407 | 1.2543 | 1.2679 | 1.2813 | 1.2947 | 1.3079 | 1.3211 | 41 |
| 42 | 1.2134 | 1.2272 | 1.2409 | 1.2546 | 1.2681 | 1.2816 | 1.2949 | 1.3082 | 1.3213 | 42 |
| 43 | 1.2136 | 1.2274 | 1.2412 | 1.2548 | 1.2683 | 1.2818 | 1.2951 | 1.3084 | 1.3215 | 43 |
| 44 | 1.2138 | 1.2277 | 1.2414 | 1.2550 | 1.2686 | 1.2820 | 1.2954 | 1.3086 | 1.3218 | 44 |
| 45 | 1.2141 | 1.2279 | 1.2416 | 1.2552 | 1.2688 | 1.2822 | 1.2956 | 1.3088 | 1.3220 | 45 |
| 46 | 1.2143 | 1.2281 | 1.2418 | 1.2555 | 1.2690 | 1.2825 | 1.2958 | 1.3090 | 1.3222 | 46 |
| 47 | 1.2145 | 1.2283 | 1.2421 | 1.2557 | 1.2692 | 1.2827 | 1.2960 | 1.3093 | 1.3224 | 47 |
| 48 | 1.2148 | 1.2286 | 1.2423 | 1.2559 | 1.2695 | 1.2829 | 1.2962 | 1.3095 | 1.3226 | 48 |
| 49 | 1.2150 | 1.2288 | 1.2425 | 1.2562 | 1.2697 | 1.2831 | 1.2965 | 1.3097 | 1.3228 | 49 |
| 50 | 1.2152 | 1.2290 | 1.2428 | 1.2564 | 1.2699 | 1.2833 | 1.2967 | 1.3099 | 1.3231 | 50 |
| 51 | 1.2154 | 1.2293 | 1.2430 | 1.2566 | 1.2701 | 1.2836 | 1.2969 | 1.3101 | 1.3233 | 51 |
| 52 | 1.2157 | 1.2295 | 1.2432 | 1.2568 | 1.2704 | 1.2838 | 1.2971 | 1.3104 | 1.3235 | 52 |
| 53 | 1.2159 | 1.2297 | 1.2434 | 1.2571 | 1.2706 | 1.2840 | 1.2973 | 1.3106 | 1.3237 | 53 |
| 54 | 1.2161 | 1.2299 | 1.2437 | 1.2573 | 1.2708 | 1.2842 | 1.2976 | 1.3108 | 1.3239 | 54 |
| 55 | 1.2164 | 1.2302 | 1.2439 | 1.2575 | 1.2710 | 1.2845 | 1.2978 | 1.3110 | 1.3242 | 55 |
| 56 | 1.2166 | 1.2304 | 1.2441 | 1.2577 | 1.2713 | 1.2847 | 1.2980 | 1.3112 | 1.3244 | 56 |
| 57 | 1.2168 | 1.2306 | 1.2443 | 1.2580 | 1.2715 | 1.2849 | 1.2982 | 1.3115 | 1.3246 | 57 |
| 58 | 1.2171 | 1.2309 | 1.2446 | 1.2582 | 1.2717 | 1.2851 | 1.2985 | 1.3117 | 1.3248 | 58 |
| 59 | 1.2173 | 1.2311 | 1.2448 | 1.2584 | 1.2719 | 1.2854 | 1.2987 | 1.3119 | 1.3250 | 59 |
| 60 | 1.2175 | 1.2313 | 1.2450 | 1.2586 | 1.2722 | 1.2856 | 1.2989 | 1.3121 | 1.3252 | 60 |

TABLE OF CHORDS: [RADIUS = 1.0000].

| $\alpha$ | $83^\circ$ | $84^\circ$ | $85^\circ$ | $86^\circ$ | $87^\circ$ | $88^\circ$ | $89^\circ$ | $\alpha$ |
|----------|------------|------------|------------|------------|------------|------------|------------|----------|
| 0        | 1.3252     | 1.3383     | 1.3512     | 1.3640     | 1.3767     | 1.3893     | 1.4018     | 0        |
| 1        | 1.3255     | 1.3385     | 1.3514     | 1.3642     | 1.3769     | 1.3895     | 1.4020     | 1        |
| 2        | 1.3257     | 1.3387     | 1.3516     | 1.3644     | 1.3771     | 1.3897     | 1.4022     | 2        |
| 3        | 1.3259     | 1.3389     | 1.3518     | 1.3646     | 1.3773     | 1.3899     | 1.4024     | 3        |
| 4        | 1.3261     | 1.3391     | 1.3520     | 1.3648     | 1.3776     | 1.3902     | 1.4026     | 4        |
| 5        | 1.3263     | 1.3393     | 1.3523     | 1.3651     | 1.3778     | 1.3904     | 1.4029     | 5        |
| 6        | 1.3265     | 1.3396     | 1.3525     | 1.3653     | 1.3780     | 1.3906     | 1.4031     | 6        |
| 7        | 1.3268     | 1.3398     | 1.3527     | 1.3655     | 1.3782     | 1.3908     | 1.4033     | 7        |
| 8        | 1.3270     | 1.3400     | 1.3529     | 1.3657     | 1.3784     | 1.3910     | 1.4035     | 8        |
| 9        | 1.3272     | 1.3402     | 1.3531     | 1.3659     | 1.3786     | 1.3912     | 1.4037     | 9        |
| 10       | 1.3274     | 1.3404     | 1.3533     | 1.3661     | 1.3788     | 1.3914     | 1.4039     | 10       |
| 11       | 1.3276     | 1.3406     | 1.3535     | 1.3663     | 1.3790     | 1.3916     | 1.4041     | 11       |
| 12       | 1.3279     | 1.3409     | 1.3538     | 1.3665     | 1.3792     | 1.3918     | 1.4043     | 12       |
| 13       | 1.3281     | 1.3411     | 1.3540     | 1.3668     | 1.3794     | 1.3920     | 1.4045     | 13       |
| 14       | 1.3283     | 1.3413     | 1.3542     | 1.3670     | 1.3797     | 1.3922     | 1.4047     | 14       |
| 15       | 1.3285     | 1.3415     | 1.3544     | 1.3672     | 1.3799     | 1.3925     | 1.4049     | 15       |
| 16       | 1.3287     | 1.3417     | 1.3546     | 1.3674     | 1.3801     | 1.3927     | 1.4051     | 16       |
| 17       | 1.3289     | 1.3419     | 1.3548     | 1.3676     | 1.3803     | 1.3929     | 1.4053     | 17       |
| 18       | 1.3292     | 1.3421     | 1.3550     | 1.3678     | 1.3805     | 1.3931     | 1.4055     | 18       |
| 19       | 1.3294     | 1.3424     | 1.3552     | 1.3680     | 1.3807     | 1.3933     | 1.4058     | 19       |
| 20       | 1.3296     | 1.3426     | 1.3555     | 1.3682     | 1.3809     | 1.3935     | 1.4060     | 20       |
| 21       | 1.3298     | 1.3428     | 1.3557     | 1.3685     | 1.3811     | 1.3937     | 1.4062     | 21       |
| 22       | 1.3300     | 1.3430     | 1.3559     | 1.3687     | 1.3813     | 1.3939     | 1.4064     | 22       |
| 23       | 1.3302     | 1.3432     | 1.3561     | 1.3689     | 1.3816     | 1.3941     | 1.4066     | 23       |
| 24       | 1.3305     | 1.3434     | 1.3563     | 1.3691     | 1.3818     | 1.3943     | 1.4068     | 24       |
| 25       | 1.3307     | 1.3437     | 1.3565     | 1.3693     | 1.3820     | 1.3945     | 1.4070     | 25       |
| 26       | 1.3309     | 1.3439     | 1.3567     | 1.3695     | 1.3822     | 1.3947     | 1.4072     | 26       |
| 27       | 1.3311     | 1.3441     | 1.3570     | 1.3697     | 1.3824     | 1.3950     | 1.4074     | 27       |
| 28       | 1.3313     | 1.3443     | 1.3572     | 1.3699     | 1.3826     | 1.3952     | 1.4076     | 28       |
| 29       | 1.3315     | 1.3445     | 1.3574     | 1.3702     | 1.3828     | 1.3954     | 1.4078     | 29       |
| 30       | 1.3318     | 1.3447     | 1.3576     | 1.3704     | 1.3830     | 1.3956     | 1.4080     | 30       |
| 31       | 1.3320     | 1.3449     | 1.3578     | 1.3706     | 1.3832     | 1.3958     | 1.4082     | 31       |
| 32       | 1.3322     | 1.3452     | 1.3580     | 1.3708     | 1.3834     | 1.3960     | 1.4084     | 32       |
| 33       | 1.3324     | 1.3454     | 1.3582     | 1.3710     | 1.3837     | 1.3962     | 1.4086     | 33       |
| 34       | 1.3326     | 1.3456     | 1.3585     | 1.3712     | 1.3839     | 1.3964     | 1.4089     | 34       |
| 35       | 1.3328     | 1.3458     | 1.3587     | 1.3714     | 1.3841     | 1.3966     | 1.4091     | 35       |
| 36       | 1.3331     | 1.3460     | 1.3589     | 1.3716     | 1.3843     | 1.3968     | 1.4093     | 36       |
| 37       | 1.3333     | 1.3462     | 1.3591     | 1.3718     | 1.3845     | 1.3970     | 1.4095     | 37       |
| 38       | 1.3335     | 1.3465     | 1.3593     | 1.3721     | 1.3847     | 1.3972     | 1.4097     | 38       |
| 39       | 1.3337     | 1.3467     | 1.3595     | 1.3723     | 1.3849     | 1.3975     | 1.4099     | 39       |
| 40       | 1.3339     | 1.3469     | 1.3597     | 1.3725     | 1.3851     | 1.3977     | 1.4101     | 40       |
| 41       | 1.3341     | 1.3471     | 1.3599     | 1.3727     | 1.3853     | 1.3979     | 1.4103     | 41       |
| 42       | 1.3344     | 1.3473     | 1.3602     | 1.3729     | 1.3855     | 1.3981     | 1.4105     | 42       |
| 43       | 1.3346     | 1.3475     | 1.3604     | 1.3731     | 1.3858     | 1.3983     | 1.4107     | 43       |
| 44       | 1.3348     | 1.3477     | 1.3606     | 1.3733     | 1.3860     | 1.3985     | 1.4109     | 44       |
| 45       | 1.3350     | 1.3480     | 1.3608     | 1.3735     | 1.3862     | 1.3987     | 1.4111     | 45       |
| 46       | 1.3352     | 1.3482     | 1.3610     | 1.3738     | 1.3864     | 1.3989     | 1.4113     | 46       |
| 47       | 1.3354     | 1.3484     | 1.3612     | 1.3740     | 1.3866     | 1.3991     | 1.4115     | 47       |
| 48       | 1.3357     | 1.3486     | 1.3614     | 1.3742     | 1.3868     | 1.3993     | 1.4117     | 48       |
| 49       | 1.3359     | 1.3488     | 1.3617     | 1.3744     | 1.3870     | 1.3995     | 1.4119     | 49       |
| 50       | 1.3361     | 1.3490     | 1.3619     | 1.3746     | 1.3872     | 1.3997     | 1.4122     | 50       |
| 51       | 1.3363     | 1.3492     | 1.3621     | 1.3748     | 1.3874     | 1.3999     | 1.4124     | 51       |
| 52       | 1.3365     | 1.3495     | 1.3623     | 1.3750     | 1.3876     | 1.4002     | 1.4126     | 52       |
| 53       | 1.3367     | 1.3497     | 1.3625     | 1.3752     | 1.3879     | 1.4004     | 1.4128     | 53       |
| 54       | 1.3370     | 1.3499     | 1.3627     | 1.3754     | 1.3881     | 1.4006     | 1.4130     | 54       |
| 55       | 1.3372     | 1.3501     | 1.3629     | 1.3757     | 1.3883     | 1.4008     | 1.4132     | 55       |
| 56       | 1.3374     | 1.3503     | 1.3631     | 1.3759     | 1.3885     | 1.4010     | 1.4134     | 56       |
| 57       | 1.3376     | 1.3505     | 1.3634     | 1.3761     | 1.3887     | 1.4012     | 1.4136     | 57       |
| 58       | 1.3378     | 1.3508     | 1.3636     | 1.3763     | 1.3889     | 1.4014     | 1.4138     | 58       |
| 59       | 1.3380     | 1.3510     | 1.3638     | 1.3765     | 1.3891     | 1.4016     | 1.4140     | 59       |
| 60       | 1.3383     | 1.3512     | 1.3640     | 1.3767     | 1.3893     | 1.4018     | 1.4142     | 60       |



# TABLE I..

OF

## LOGARITHMS OF NUMBERS

FROM

### 1 TO 10000.

---

| N. | Log.     | N. | Log.     | N. | Log.     | N.  | Log.     |
|----|----------|----|----------|----|----------|-----|----------|
| 1  | 0.000000 | 26 | 1.414973 | 51 | 1.707570 | 76  | 1.880814 |
| 2  | 0.301030 | 27 | 1.431364 | 52 | 1.716003 | 77  | 1.886491 |
| 3  | 0.477121 | 28 | 1.447158 | 53 | 1.724276 | 78  | 1.892095 |
| 4  | 0.602060 | 29 | 1.462398 | 54 | 1.732394 | 79  | 1.897627 |
| 5  | 0.698970 | 30 | 1.477121 | 55 | 1.740363 | 80  | 1.903090 |
| 6  | 0.778151 | 31 | 1.491362 | 56 | 1.748188 | 81  | 1.908485 |
| 7  | 0.845098 | 32 | 1.505150 | 57 | 1.755875 | 82  | 1.913814 |
| 8  | 0.903090 | 33 | 1.518514 | 58 | 1.763428 | 83  | 1.919078 |
| 9  | 0.954243 | 34 | 1.531479 | 59 | 1.770852 | 84  | 1.924279 |
| 10 | 1.000000 | 35 | 1.544068 | 60 | 1.778151 | 85  | 1.929419 |
| 11 | 1.041393 | 36 | 1.556303 | 61 | 1.785330 | 86  | 1.934498 |
| 12 | 1.079181 | 37 | 1.568202 | 62 | 1.792392 | 87  | 1.939519 |
| 13 | 1.113943 | 38 | 1.579784 | 63 | 1.799341 | 88  | 1.944483 |
| 14 | 1.146128 | 39 | 1.591065 | 64 | 1.806180 | 89  | 1.949390 |
| 15 | 1.176091 | 40 | 1.602060 | 65 | 1.812913 | 90  | 1.954243 |
| 16 | 1.204120 | 41 | 1.612784 | 66 | 1.819544 | 91  | 1.959041 |
| 17 | 1.230449 | 42 | 1.623249 | 67 | 1.826075 | 92  | 1.963788 |
| 18 | 1.255273 | 43 | 1.633468 | 68 | 1.832509 | 93  | 1.968483 |
| 19 | 1.278754 | 44 | 1.643453 | 69 | 1.838849 | 94  | 1.973128 |
| 20 | 1.301030 | 45 | 1.653213 | 70 | 1.845098 | 95  | 1.977724 |
| 21 | 1.322219 | 46 | 1.662758 | 71 | 1.851258 | 96  | 1.982271 |
| 22 | 1.342423 | 47 | 1.672098 | 72 | 1.857333 | 97  | 1.986772 |
| 23 | 1.361728 | 48 | 1.681241 | 73 | 1.863323 | 98  | 1.991226 |
| 24 | 1.380211 | 49 | 1.690196 | 74 | 1.869232 | 99  | 1.995635 |
| 25 | 1.397940 | 50 | 1.698970 | 75 | 1.875061 | 100 | 2.000000 |

N. B. In the following table, in the last nine columns of each page, where the first or leading figures change from 9's to 0's, the character + is introduced instead of the 0's, to catch the eye, and to indicate that from thence the annexed first two figures of the Logarithm in the second column stand in the next lower line, directly under the *asterisk*.

| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D.  |
|-----|---------|------|------|------|------|------|------|------|------|------|-----|
| 100 | 00 0000 | 0434 | 0868 | 1301 | 1734 | 2166 | 2598 | 3039 | 3461 | 3891 | 432 |
| 101 | 4321    | 4751 | 5181 | 5609 | 6038 | 6466 | 6894 | 7321 | 7748 | 8174 | 428 |
| 102 | * 8600  | 9026 | 9451 | 9876 | +300 | 0724 | 1147 | 1570 | 1993 | 2415 | 424 |
| 103 | 01 2837 | 3259 | 3680 | 4100 | 4521 | 4940 | 5360 | 5779 | 6197 | 6616 | 419 |
| 104 | * 7033  | 7451 | 7868 | 8284 | 8700 | 9116 | 9532 | 9947 | +361 | 0775 | 416 |
| 105 | 02 1189 | 1603 | 2016 | 2428 | 2841 | 3252 | 3664 | 4075 | 4486 | 4896 | 412 |
| 106 | 5306    | 5715 | 6125 | 6533 | 6942 | 7350 | 7757 | 8164 | 8571 | 8978 | 408 |
| 107 | * 9384  | 9789 | +195 | 0600 | 1004 | 1408 | 1812 | 2216 | 2619 | 3021 | 404 |
| 108 | 03 3424 | 3826 | 4227 | 4628 | 5029 | 5430 | 5830 | 6230 | 6629 | 7028 | 400 |
| 109 | * 7426  | 7825 | 8223 | 8620 | 9017 | 9414 | 9811 | +207 | 0602 | 0998 | 396 |
| 110 | 04 1393 | 1787 | 2182 | 2576 | 2969 | 3362 | 3755 | 4148 | 4540 | 4932 | 393 |
| 111 | 5323    | 5714 | 6105 | 6495 | 6885 | 7275 | 7664 | 8053 | 8442 | 8830 | 389 |
| 112 | * 9218  | 9606 | 9993 | +380 | 0766 | 1153 | 1538 | 1924 | 2309 | 2694 | 386 |
| 113 | 05 3078 | 3463 | 3846 | 4230 | 4613 | 4996 | 5378 | 5760 | 6142 | 6524 | 382 |
| 114 | * 6905  | 7286 | 7666 | 8046 | 8426 | 8805 | 9185 | 9563 | 9942 | +320 | 379 |
| 115 | 06 0698 | 1075 | 1452 | 1829 | 2206 | 2582 | 2958 | 3333 | 3709 | 4083 | 376 |
| 116 | 4458    | 4832 | 5206 | 5580 | 5953 | 6326 | 6699 | 7071 | 7443 | 7815 | 372 |
| 117 | * 8186  | 8557 | 8928 | 9298 | 9668 | +038 | 0407 | 0776 | 1145 | 1514 | 369 |
| 118 | 07 1882 | 2250 | 2617 | 2985 | 3352 | 3718 | 4085 | 4451 | 4816 | 5182 | 366 |
| 119 | 5547    | 5912 | 6276 | 6640 | 7004 | 7368 | 7731 | 8094 | 8457 | 8819 | 363 |
| 120 | * 9181  | 9543 | 9904 | +266 | 0626 | 0987 | 1347 | 1707 | 2067 | 2426 | 360 |
| 121 | 08 2785 | 3144 | 3503 | 3861 | 4219 | 4576 | 4934 | 5291 | 5647 | 6004 | 357 |
| 122 | 6360    | 6716 | 7071 | 7426 | 7781 | 8136 | 8490 | 8845 | 9198 | 9552 | 355 |
| 123 | * 9905  | +258 | 0611 | 0963 | 1315 | 1667 | 2018 | 2369 | 2721 | 3071 | 351 |
| 124 | 09 3422 | 3772 | 4122 | 4471 | 4820 | 5169 | 5518 | 5866 | 6215 | 6562 | 349 |
| 125 | * 6910  | 7257 | 7604 | 7951 | 8298 | 8644 | 8990 | 9335 | 9681 | +026 | 346 |
| 126 | 10 0371 | 0715 | 1059 | 1403 | 1747 | 2091 | 2434 | 2777 | 3119 | 3462 | 343 |
| 127 | 3804    | 4146 | 4487 | 4828 | 5169 | 5510 | 5851 | 6191 | 6531 | 6871 | 340 |
| 128 | * 7210  | 7549 | 7888 | 8227 | 8565 | 8903 | 9241 | 9579 | 9916 | +253 | 338 |
| 129 | 11 0590 | 0926 | 1263 | 1599 | 1934 | 2270 | 2605 | 2940 | 3275 | 3609 | 335 |
| 130 | 3943    | 4277 | 4611 | 4944 | 5278 | 5611 | 5943 | 6276 | 6608 | 6940 | 333 |
| 131 | * 7271  | 7603 | 7934 | 8265 | 8595 | 8926 | 9256 | 9586 | 9915 | +245 | 330 |
| 132 | 12 0574 | 0903 | 1231 | 1560 | 1888 | 2216 | 2544 | 2871 | 3198 | 3525 | 328 |
| 133 | 3852    | 4178 | 4504 | 4830 | 5156 | 5481 | 5806 | 6131 | 6456 | 6781 | 325 |
| 134 | * 7105  | 7429 | 7753 | 8076 | 8399 | 8722 | 9045 | 9368 | 9690 | +012 | 323 |
| 135 | 13 0334 | 0655 | 0977 | 1298 | 1619 | 1939 | 2260 | 2580 | 2900 | 3219 | 321 |
| 136 | 3539    | 3858 | 4177 | 4496 | 4814 | 5133 | 5451 | 5769 | 6086 | 6403 | 318 |
| 137 | 6721    | 7037 | 7354 | 7671 | 7987 | 8303 | 8618 | 8934 | 9249 | 9564 | 315 |
| 138 | * 9879  | +194 | 0508 | 0822 | 1136 | 1450 | 1763 | 2076 | 2389 | 2702 | 314 |
| 139 | 14 3015 | 3327 | 3639 | 3951 | 4263 | 4574 | 4885 | 5196 | 5507 | 5818 | 311 |
| 140 | 6128    | 6438 | 6748 | 7058 | 7367 | 7676 | 7985 | 8294 | 8603 | 8911 | 309 |
| 141 | * 9219  | 9527 | 9835 | +142 | 0449 | 0756 | 1063 | 1370 | 1676 | 1982 | 307 |
| 142 | 15 2286 | 2594 | 2900 | 3205 | 3510 | 3815 | 4120 | 4424 | 4728 | 5032 | 305 |
| 143 | 5336    | 5640 | 5943 | 6246 | 6549 | 6852 | 7154 | 7457 | 7759 | 8061 | 303 |
| 144 | * 8362  | 8664 | 8965 | 9266 | 9567 | 9868 | +168 | 0469 | 0769 | 1068 | 301 |
| 145 | 16 1368 | 1667 | 1967 | 2266 | 2564 | 2863 | 3161 | 3460 | 3758 | 4055 | 299 |
| 146 | 4353    | 4650 | 4947 | 5244 | 5541 | 5838 | 6134 | 6430 | 6726 | 7022 | 297 |
| 147 | 7317    | 7613 | 7908 | 8203 | 8497 | 8792 | 9086 | 9380 | 9674 | 9968 | 295 |
| 148 | 17 0262 | 0555 | 0848 | 1141 | 1434 | 1726 | 2019 | 2311 | 2603 | 2895 | 293 |
| 149 | 3186    | 3478 | 3769 | 4060 | 4351 | 4641 | 4932 | 5222 | 5512 | 5802 | 291 |
| 150 | 6091    | 6381 | 6670 | 6959 | 7248 | 7536 | 7825 | 8113 | 8401 | 8689 | 289 |
| 151 | * 8977  | 9264 | 9552 | 9839 | +126 | 0413 | 0699 | 0985 | 1272 | 1558 | 287 |
| 152 | 18 1844 | 2129 | 2415 | 2700 | 2985 | 3270 | 3555 | 3839 | 4123 | 4407 | 285 |
| 153 | 4691    | 4975 | 5259 | 5542 | 5825 | 6108 | 6391 | 6674 | 6956 | 7239 | 283 |
| 154 | * 7521  | 7803 | 8084 | 8366 | 8647 | 8928 | 9209 | 9490 | 9771 | +051 | 281 |
| 155 | 19 0332 | 0612 | 0892 | 1171 | 1451 | 1730 | 2010 | 2289 | 2567 | 2846 | 279 |
| 156 | 3125    | 3403 | 3681 | 3959 | 4237 | 4514 | 4792 | 5069 | 5346 | 5623 | 276 |
| 157 | 5900    | 6176 | 6453 | 6729 | 7005 | 7281 | 7556 | 7832 | 8107 | 8382 | 274 |
| 158 | * 8657  | 8932 | 9206 | 9481 | 9755 | +029 | 0303 | 0577 | 0850 | 1124 | 272 |
| 159 | 20 1397 | 1670 | 1943 | 2216 | 2488 | 2761 | 3033 | 3305 | 3577 | 3848 | 270 |
| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D.  |

TABLE I.

## LOGARITHMS OF NUMBERS.

3

| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D.  |
|-----|---------|------|------|------|------|------|------|------|------|------|-----|
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| 249 | 6199    | 6374 | 6548 | 6722 | 6896 | 7071 | 7245 | 7419 | 7592 | 7766 | 174 |
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| 254 | 4834    | 5005 | 5176 | 5346 | 5517 | 5688 | 5858 | 6029 | 6199 | 6370 | 171 |
| 255 | 6540    | 6710 | 6881 | 7051 | 7221 | 7391 | 7561 | 7731 | 7901 | 8070 | 170 |
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| 266 | 4882    | 5045 | 5208 | 5371 | 5534 | 5697 | 5860 | 6023 | 6186 | 6349 | 163 |
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| 278 | 4045    | 4201 | 4357 | 4513 | 4669 | 4825 | 4981 | 5137 | 5293 | 5449 | 156 |
| 279 | 5604    | 5760 | 5915 | 6071 | 6226 | 6382 | 6537 | 6692 | 6848 | 7003 | 155 |
| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D.  |

TABLE I.

## LOGARITHMS OF NUMBERS.

5

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| 285 | 4845    | 4997 | 5150 | 5302 | 5454 | 5606 | 5758 | 5910 | 6062 | 6214 | 152 |
| 286 | 6366    | 6518 | 6670 | 6821 | 6973 | 7125 | 7276 | 7428 | 7579 | 7731 | 152 |
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| 364 | 56 1101 | 1221 | 1340 | 1459 | 1578 | 1698 | 1817 | 1936 | 2055 | 2174 | 119 |
| 365 | 2293    | 2412 | 2531 | 2650 | 2769 | 2887 | 3006 | 3125 | 3244 | 3362 | 119 |
| 366 | 3481    | 3600 | 3718 | 3837 | 3955 | 4074 | 4192 | 4311 | 4429 | 4548 | 119 |
| 367 | 4666    | 4784 | 4903 | 5021 | 5139 | 5257 | 5376 | 5494 | 5612 | 5730 | 118 |
| 368 | 5848    | 5966 | 6084 | 6202 | 6320 | 6437 | 6555 | 6673 | 6791 | 6909 | 118 |
| 369 | 7026    | 7144 | 7262 | 7379 | 7497 | 7614 | 7732 | 7849 | 7967 | 8084 | 118 |
| 370 | 8202    | 8319 | 8436 | 8554 | 8671 | 8788 | 8905 | 9023 | 9140 | 9257 | 117 |
| 371 | * 9374  | 9491 | 9608 | 9725 | 9842 | 9959 | +076 | 0193 | 0309 | 0426 | 117 |
| 372 | 57 0543 | 0660 | 0776 | 0893 | 1010 | 1126 | 1243 | 1359 | 1476 | 1592 | 117 |
| 373 | 1709    | 1825 | 1942 | 2058 | 2174 | 2291 | 2407 | 2523 | 2639 | 2755 | 116 |
| 374 | 2872    | 2988 | 3104 | 3220 | 3336 | 3452 | 3568 | 3684 | 3800 | 3915 | 116 |
| 375 | 4031    | 4147 | 4263 | 4379 | 4494 | 4610 | 4726 | 4841 | 4957 | 5072 | 116 |
| 376 | 5188    | 5303 | 5419 | 5534 | 5650 | 5765 | 5880 | 5996 | 6111 | 6226 | 115 |
| 377 | 6341    | 6457 | 6572 | 6687 | 6802 | 6917 | 7032 | 7147 | 7262 | 7377 | 115 |
| 378 | 7492    | 7607 | 7722 | 7836 | 7951 | 8066 | 8181 | 8295 | 8410 | 8525 | 115 |
| 379 | 8639    | 8754 | 8868 | 8983 | 9097 | 9212 | 9326 | 9441 | 9555 | 9669 | 114 |
| 380 | * 9784  | 9898 | +012 | 0126 | 0241 | 0355 | 0469 | 0583 | 0697 | 0811 | 114 |
| 381 | 58 0925 | 1039 | 1153 | 1267 | 1381 | 1495 | 1608 | 1722 | 1836 | 1950 | 114 |
| 382 | 2063    | 2177 | 2291 | 2404 | 2518 | 2631 | 2745 | 2858 | 2972 | 3085 | 114 |
| 383 | 3199    | 3312 | 3426 | 3539 | 3652 | 3765 | 3879 | 3992 | 4105 | 4218 | 113 |
| 384 | 4331    | 4444 | 4557 | 4670 | 4783 | 4896 | 5009 | 5122 | 5235 | 5348 | 113 |
| 385 | 5461    | 5574 | 5686 | 5799 | 5912 | 6024 | 6137 | 6250 | 6362 | 6475 | 113 |
| 386 | 6587    | 6700 | 6812 | 6925 | 7037 | 7149 | 7262 | 7374 | 7486 | 7599 | 112 |
| 387 | 7711    | 7823 | 7935 | 8047 | 8160 | 8272 | 8384 | 8496 | 8608 | 8720 | 112 |
| 388 | 8832    | 8944 | 9056 | 9167 | 9279 | 9391 | 9503 | 9615 | 9726 | 9838 | 112 |
| 389 | * 9950  | +061 | 0173 | 0284 | 0396 | 0507 | 0619 | 0730 | 0842 | 0953 | 112 |
| 390 | 59 1065 | 1176 | 1287 | 1399 | 1510 | 1621 | 1732 | 1843 | 1955 | 2066 | 111 |
| 391 | 2177    | 2288 | 2399 | 2510 | 2621 | 2732 | 2843 | 2954 | 3064 | 3175 | 111 |
| 392 | 3286    | 3397 | 3508 | 3618 | 3729 | 3840 | 3950 | 4061 | 4171 | 4282 | 111 |
| 393 | 4393    | 4503 | 4614 | 4724 | 4834 | 4945 | 5055 | 5165 | 5276 | 5386 | 110 |
| 394 | 5496    | 5606 | 5717 | 5827 | 5937 | 6047 | 6157 | 6267 | 6377 | 6487 | 110 |
| 395 | 6597    | 6707 | 6817 | 6927 | 7037 | 7146 | 7256 | 7366 | 7476 | 7586 | 110 |
| 396 | 7695    | 7805 | 7914 | 8024 | 8134 | 8243 | 8353 | 8462 | 8572 | 8681 | 110 |
| 397 | 8791    | 8900 | 9009 | 9119 | 9228 | 9337 | 9446 | 9556 | 9665 | 9774 | 109 |
| 398 | * 9883  | 9992 | +101 | 0210 | 0319 | 0428 | 0537 | 0646 | 0755 | 0864 | 109 |
| 399 | 60 0973 | 1082 | 1191 | 1299 | 1408 | 1517 | 1625 | 1734 | 1843 | 1951 | 109 |
| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D.  |

TABLE I.

## LOGARITHMS OF NUMBERS.

7

| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D.  |
|-----|---------|------|------|------|------|------|------|------|------|------|-----|
| 400 | 60 2060 | 2160 | 2277 | 2386 | 2494 | 2603 | 2711 | 2819 | 2928 | 3036 | 108 |
| 401 | 3144    | 3253 | 3361 | 3469 | 3577 | 3686 | 3794 | 3902 | 4010 | 4118 | 108 |
| 402 | 4226    | 4334 | 4442 | 4550 | 4658 | 4766 | 4874 | 4982 | 5089 | 5197 | 108 |
| 403 | 5305    | 5413 | 5521 | 5628 | 5736 | 5844 | 5951 | 6059 | 6166 | 6274 | 108 |
| 404 | 6381    | 6489 | 6596 | 6704 | 6811 | 6919 | 7026 | 7133 | 7241 | 7348 | 107 |
| 405 | 7455    | 7562 | 7669 | 7777 | 7884 | 7991 | 8098 | 8205 | 8312 | 8419 | 107 |
| 406 | 8526    | 8633 | 8740 | 8847 | 8954 | 9061 | 9167 | 9274 | 9381 | 9488 | 107 |
| 407 | * 9594  | 9701 | 9808 | 9914 | +021 | 0128 | 0234 | 0341 | 0447 | 0554 | 107 |
| 408 | 61 0660 | 0767 | 0873 | 0979 | 1086 | 1192 | 1298 | 1405 | 1511 | 1617 | 106 |
| 409 | 1723    | 1829 | 1936 | 2042 | 2148 | 2254 | 2360 | 2466 | 2572 | 2678 | 106 |
| 410 | 2784    | 2890 | 2996 | 3102 | 3207 | 3313 | 3419 | 3525 | 3630 | 3736 | 106 |
| 411 | 3842    | 3947 | 4053 | 4159 | 4264 | 4370 | 4475 | 4581 | 4686 | 4792 | 106 |
| 412 | 4897    | 5003 | 5108 | 5213 | 5319 | 5424 | 5529 | 5634 | 5740 | 5845 | 105 |
| 413 | 5950    | 6055 | 6160 | 6265 | 6370 | 6476 | 6581 | 6686 | 6790 | 6895 | 105 |
| 414 | 7000    | 7105 | 7210 | 7315 | 7420 | 7525 | 7629 | 7734 | 7839 | 7943 | 105 |
| 415 | 8048    | 8153 | 8257 | 8362 | 8466 | 8571 | 8676 | 8780 | 8884 | 8989 | 105 |
| 416 | * 9093  | 9198 | 9302 | 9406 | 9511 | 9615 | 9719 | 9824 | 9928 | +032 | 104 |
| 417 | 62 0136 | 0240 | 0344 | 0448 | 0552 | 0656 | 0760 | 0864 | 0968 | 1072 | 104 |
| 418 | 1176    | 1280 | 1384 | 1488 | 1592 | 1695 | 1799 | 1903 | 2007 | 2110 | 104 |
| 419 | 2214    | 2318 | 2421 | 2525 | 2628 | 2732 | 2835 | 2939 | 3042 | 3146 | 104 |
| 420 | 3249    | 3353 | 3456 | 3559 | 3663 | 3766 | 3869 | 3973 | 4076 | 4179 | 103 |
| 421 | 4282    | 4385 | 4488 | 4591 | 4695 | 4798 | 4901 | 5004 | 5107 | 5210 | 103 |
| 422 | 5312    | 5415 | 5518 | 5621 | 5724 | 5827 | 5929 | 6032 | 6135 | 6238 | 103 |
| 423 | 6340    | 6443 | 6546 | 6648 | 6751 | 6853 | 6956 | 7058 | 7161 | 7263 | 103 |
| 424 | 7366    | 7468 | 7571 | 7673 | 7775 | 7878 | 7980 | 8082 | 8185 | 8287 | 102 |
| 425 | 8389    | 8491 | 8593 | 8695 | 8797 | 8900 | 9002 | 9104 | 9206 | 9308 | 102 |
| 426 | * 9410  | 9512 | 9613 | 9715 | 9817 | 9919 | +021 | 0123 | 0224 | 0326 | 102 |
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| 428 | 1444    | 1545 | 1647 | 1748 | 1849 | 1951 | 2052 | 2153 | 2255 | 2356 | 101 |
| 429 | 2457    | 2559 | 2660 | 2761 | 2862 | 2963 | 3064 | 3165 | 3266 | 3367 | 101 |
| 430 | 3468    | 3569 | 3670 | 3771 | 3872 | 3973 | 4074 | 4175 | 4276 | 4376 | 100 |
| 431 | 4477    | 4578 | 4679 | 4779 | 4880 | 4981 | 5081 | 5182 | 5283 | 5383 | 100 |
| 432 | 5484    | 5584 | 5685 | 5785 | 5886 | 5986 | 6087 | 6187 | 6287 | 6388 | 100 |
| 433 | 6488    | 6588 | 6688 | 6789 | 6889 | 6989 | 7089 | 7189 | 7290 | 7390 | 100 |
| 434 | 7490    | 7590 | 7690 | 7790 | 7890 | 7990 | 8090 | 8190 | 8290 | 8389 | 99  |
| 435 | 8489    | 8589 | 8689 | 8789 | 8888 | 8988 | 9088 | 9188 | 9287 | 9387 | 99  |
| 436 | * 9486  | 9586 | 9686 | 9785 | 9885 | 9984 | +084 | 0183 | 0283 | 0382 | 99  |
| 437 | 64 0481 | 0581 | 0680 | 0779 | 0879 | 0978 | 1077 | 1177 | 1276 | 1375 | 99  |
| 438 | 1474    | 1573 | 1672 | 1771 | 1871 | 1970 | 2069 | 2168 | 2267 | 2366 | 99  |
| 439 | 2465    | 2563 | 2662 | 2761 | 2860 | 2959 | 3058 | 3156 | 3255 | 3354 | 99  |
| 440 | 3453    | 3551 | 3650 | 3749 | 3847 | 3946 | 4044 | 4143 | 4242 | 4340 | 98  |
| 441 | 4439    | 4537 | 4636 | 4734 | 4832 | 4931 | 5029 | 5127 | 5226 | 5324 | 98  |
| 442 | 5422    | 5521 | 5619 | 5717 | 5815 | 5913 | 6011 | 6110 | 6208 | 6306 | 98  |
| 443 | 6404    | 6502 | 6600 | 6698 | 6796 | 6894 | 6992 | 7089 | 7187 | 7285 | 98  |
| 444 | 7383    | 7481 | 7579 | 7676 | 7774 | 7872 | 7969 | 8067 | 8165 | 8262 | 98  |
| 445 | 8360    | 8458 | 8555 | 8653 | 8750 | 8848 | 8945 | 9043 | 9140 | 9237 | 97  |
| 446 | * 9335  | 9432 | 9530 | 9627 | 9724 | 9821 | 9919 | +016 | 0113 | 0210 | 97  |
| 447 | 65 0308 | 0405 | 0502 | 0599 | 0696 | 0793 | 0890 | 0987 | 1084 | 1181 | 97  |
| 448 | 1278    | 1375 | 1472 | 1569 | 1666 | 1762 | 1859 | 1956 | 2053 | 2150 | 97  |
| 449 | 2246    | 2343 | 2440 | 2536 | 2633 | 2730 | 2826 | 2923 | 3019 | 3116 | 97  |
| 450 | 3213    | 3309 | 3405 | 3502 | 3598 | 3695 | 3791 | 3888 | 3984 | 4080 | 96  |
| 451 | 4177    | 4273 | 4369 | 4465 | 4562 | 4658 | 4754 | 4850 | 4946 | 5042 | 96  |
| 452 | 5138    | 5235 | 5331 | 5427 | 5523 | 5619 | 5715 | 5810 | 5906 | 6002 | 96  |
| 453 | 6098    | 6194 | 6290 | 6386 | 6482 | 6577 | 6673 | 6769 | 6864 | 6960 | 96  |
| 454 | 7056    | 7152 | 7247 | 7343 | 7438 | 7534 | 7629 | 7725 | 7820 | 7916 | 96  |
| 455 | 8011    | 8107 | 8202 | 8298 | 8393 | 8488 | 8584 | 8679 | 8774 | 8870 | 95  |
| 456 | 8965    | 9060 | 9155 | 9250 | 9346 | 9441 | 9536 | 9631 | 9726 | 9821 | 95  |
| 457 | * 9916  | +011 | 0106 | 0201 | 0296 | 0391 | 0486 | 0581 | 0676 | 0771 | 95  |
| 458 | 66 0865 | 0960 | 1055 | 1150 | 1245 | 1339 | 1434 | 1529 | 1623 | 1718 | 95  |
| 459 | 1813    | 1907 | 2002 | 2096 | 2191 | 2286 | 2380 | 2475 | 2569 | 2663 | 95  |
| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D.  |

| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D. |
|-----|---------|------|------|------|------|------|------|------|------|------|----|
| 460 | 66 2758 | 2852 | 2947 | 3041 | 3135 | 3230 | 3324 | 3418 | 3512 | 3607 | 94 |
| 461 | 3701    | 3795 | 3889 | 3983 | 4078 | 4172 | 4266 | 4360 | 4454 | 4548 | 94 |
| 462 | 4642    | 4736 | 4830 | 4924 | 5018 | 5112 | 5206 | 5299 | 5393 | 5487 | 94 |
| 463 | 5581    | 5675 | 5769 | 5862 | 5956 | 6050 | 6143 | 6237 | 6331 | 6424 | 94 |
| 464 | 6518    | 6612 | 6705 | 6799 | 6892 | 6986 | 7079 | 7173 | 7266 | 7360 | 94 |
| 465 | 7453    | 7546 | 7640 | 7733 | 7826 | 7920 | 8013 | 8106 | 8199 | 8293 | 93 |
| 466 | 8386    | 8479 | 8572 | 8665 | 8759 | 8852 | 8945 | 9038 | 9131 | 9224 | 93 |
| 467 | * 9317  | 9410 | 9503 | 9596 | 9689 | 9782 | 9875 | 9967 | +060 | 0153 | 93 |
| 468 | 67 0246 | 0339 | 0431 | 0524 | 0617 | 0710 | 0802 | 0895 | 0988 | 1080 | 93 |
| 469 | 1173    | 1265 | 1358 | 1451 | 1543 | 1636 | 1728 | 1821 | 1913 | 2005 | 93 |
| 470 | 2098    | 2190 | 2283 | 2375 | 2467 | 2560 | 2652 | 2744 | 2836 | 2929 | 92 |
| 471 | 3021    | 3113 | 3205 | 3297 | 3390 | 3482 | 3574 | 3666 | 3758 | 3850 | 92 |
| 472 | 3942    | 4034 | 4126 | 4218 | 4310 | 4402 | 4494 | 4586 | 4677 | 4769 | 92 |
| 473 | 4861    | 4953 | 5045 | 5137 | 5228 | 5320 | 5412 | 5503 | 5595 | 5687 | 92 |
| 474 | 5778    | 5870 | 5962 | 6053 | 6145 | 6236 | 6328 | 6419 | 6511 | 6602 | 92 |
| 475 | 6694    | 6785 | 6876 | 6968 | 7059 | 7151 | 7242 | 7333 | 7424 | 7516 | 91 |
| 476 | 7607    | 7698 | 7789 | 7881 | 7972 | 8063 | 8154 | 8245 | 8336 | 8427 | 91 |
| 477 | 8518    | 8609 | 8700 | 8791 | 8882 | 8973 | 9064 | 9155 | 9246 | 9337 | 91 |
| 478 | * 9428  | 9519 | 9610 | 9700 | 9791 | 9882 | 9973 | +063 | 0154 | 0245 | 91 |
| 479 | 68 0336 | 0426 | 0517 | 0607 | 0698 | 0789 | 0879 | 0970 | 1060 | 1151 | 91 |
| 480 | 1241    | 1332 | 1422 | 1513 | 1603 | 1693 | 1784 | 1874 | 1964 | 2055 | 90 |
| 481 | 2145    | 2235 | 2326 | 2416 | 2506 | 2596 | 2686 | 2777 | 2867 | 2957 | 90 |
| 482 | 3047    | 3137 | 3227 | 3317 | 3407 | 3497 | 3587 | 3677 | 3767 | 3857 | 90 |
| 483 | 3947    | 4037 | 4127 | 4217 | 4307 | 4396 | 4486 | 4576 | 4666 | 4756 | 90 |
| 484 | 4845    | 4935 | 5025 | 5114 | 5204 | 5294 | 5383 | 5473 | 5563 | 5652 | 90 |
| 485 | 5742    | 5831 | 5921 | 6010 | 6100 | 6189 | 6279 | 6368 | 6458 | 6547 | 89 |
| 486 | 6636    | 6726 | 6815 | 6904 | 6994 | 7083 | 7172 | 7261 | 7351 | 7440 | 89 |
| 487 | 7529    | 7618 | 7707 | 7796 | 7886 | 7975 | 8064 | 8153 | 8242 | 8331 | 89 |
| 488 | 8420    | 8509 | 8598 | 8687 | 8776 | 8865 | 8953 | 9042 | 9131 | 9220 | 89 |
| 489 | * 9309  | 9398 | 9486 | 9575 | 9664 | 9753 | 9841 | 9930 | +019 | 0107 | 89 |
| 490 | 69 0106 | 0195 | 0285 | 0373 | 0462 | 0550 | 0639 | 0728 | 0816 | 0905 | 89 |
| 491 | 1081    | 1170 | 1258 | 1347 | 1435 | 1524 | 1612 | 1700 | 1789 | 1877 | 88 |
| 492 | 1965    | 2053 | 2142 | 2230 | 2318 | 2406 | 2494 | 2583 | 2671 | 2759 | 88 |
| 493 | 2847    | 2935 | 3023 | 3111 | 3199 | 3287 | 3375 | 3463 | 3551 | 3639 | 88 |
| 494 | 3727    | 3815 | 3903 | 3991 | 4078 | 4166 | 4254 | 4342 | 4430 | 4517 | 88 |
| 495 | 4605    | 4693 | 4781 | 4868 | 4956 | 5044 | 5131 | 5219 | 5307 | 5394 | 88 |
| 496 | 5482    | 5569 | 5657 | 5744 | 5832 | 5919 | 6007 | 6094 | 6182 | 6269 | 87 |
| 497 | 6356    | 6444 | 6531 | 6618 | 6706 | 6793 | 6880 | 6968 | 7055 | 7142 | 87 |
| 498 | 7229    | 7317 | 7404 | 7491 | 7578 | 7665 | 7752 | 7839 | 7926 | 8014 | 87 |
| 499 | 8101    | 8188 | 8275 | 8362 | 8449 | 8535 | 8622 | 8709 | 8796 | 8883 | 87 |
| 500 | 8970    | 9057 | 9144 | 9231 | 9317 | 9404 | 9491 | 9578 | 9664 | 9751 | 87 |
| 501 | * 9838  | 9924 | +011 | 0098 | 0184 | 0271 | 0358 | 0444 | 0531 | 0617 | 87 |
| 502 | 70 0704 | 0790 | 0877 | 0963 | 1050 | 1136 | 1222 | 1309 | 1395 | 1482 | 86 |
| 503 | 1568    | 1654 | 1741 | 1827 | 1913 | 1999 | 2086 | 2172 | 2258 | 2344 | 86 |
| 504 | 2431    | 2517 | 2603 | 2689 | 2775 | 2861 | 2947 | 3033 | 3119 | 3205 | 86 |
| 505 | 3291    | 3377 | 3463 | 3549 | 3635 | 3721 | 3807 | 3893 | 3979 | 4065 | 86 |
| 506 | 4151    | 4236 | 4322 | 4408 | 4494 | 4579 | 4665 | 4751 | 4837 | 4922 | 86 |
| 507 | 5008    | 5094 | 5179 | 5265 | 5350 | 5436 | 5522 | 5607 | 5693 | 5778 | 86 |
| 508 | 5864    | 5949 | 6035 | 6120 | 6206 | 6291 | 6376 | 6462 | 6547 | 6632 | 85 |
| 509 | 6718    | 6803 | 6888 | 6974 | 7059 | 7144 | 7229 | 7315 | 7400 | 7485 | 85 |
| 510 | 7570    | 7655 | 7740 | 7826 | 7911 | 7996 | 8081 | 8166 | 8251 | 8336 | 85 |
| 511 | 8431    | 8506 | 8591 | 8676 | 8761 | 8846 | 8931 | 9015 | 9100 | 9185 | 85 |
| 512 | * 9270  | 9355 | 9440 | 9524 | 9609 | 9694 | 9779 | 9863 | 9948 | +033 | 85 |
| 513 | 71 0117 | 0202 | 0287 | 0371 | 0456 | 0540 | 0625 | 0710 | 0794 | 0879 | 85 |
| 514 | 0963    | 1048 | 1132 | 1217 | 1301 | 1385 | 1470 | 1554 | 1639 | 1723 | 84 |
| 515 | 1807    | 1892 | 1976 | 2060 | 2144 | 2229 | 2313 | 2397 | 2481 | 2566 | 84 |
| 516 | 2650    | 2734 | 2818 | 2902 | 2986 | 3070 | 3154 | 3238 | 3323 | 3407 | 84 |
| 517 | 3491    | 3575 | 3659 | 3742 | 3826 | 3910 | 3994 | 4078 | 4162 | 4246 | 84 |
| 518 | 4330    | 4414 | 4497 | 4581 | 4665 | 4749 | 4833 | 4916 | 5000 | 5084 | 84 |
| 519 | 5167    | 5251 | 5335 | 5418 | 5502 | 5586 | 5669 | 5753 | 5836 | 5920 | 84 |
| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D. |



TABLE I.

## LOGARITHMS OF NUMBERS.

9

| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D. |
|-----|---------|------|------|------|------|------|------|------|------|------|----|
| 520 | 71 6003 | 6087 | 6170 | 6254 | 6337 | 6421 | 6504 | 6588 | 6671 | 6754 | 83 |
| 521 | 6838    | 6921 | 7004 | 7088 | 7171 | 7254 | 7338 | 7421 | 7504 | 7587 | 83 |
| 522 | 7671    | 7754 | 7837 | 7920 | 8003 | 8086 | 8169 | 8252 | 8336 | 8419 | 83 |
| 523 | 8502    | 8585 | 8668 | 8751 | 8834 | 8917 | 9000 | 9083 | 9165 | 9248 | 83 |
| 524 | * 9331  | 9414 | 9497 | 9580 | 9663 | 9745 | 9828 | 9911 | 9994 | +077 | 83 |
| 525 | 72 0159 | 0242 | 0325 | 0407 | 0490 | 0573 | 0655 | 0738 | 0821 | 0903 | 83 |
| 526 | 0986    | 1068 | 1151 | 1233 | 1316 | 1398 | 1481 | 1563 | 1646 | 1728 | 82 |
| 527 | 1811    | 1893 | 1975 | 2058 | 2140 | 2222 | 2305 | 2387 | 2469 | 2552 | 82 |
| 528 | 2634    | 2716 | 2798 | 2881 | 2963 | 3045 | 3127 | 3209 | 3291 | 3374 | 82 |
| 529 | 3456    | 3538 | 3620 | 3702 | 3784 | 3866 | 3948 | 4030 | 4112 | 4194 | 82 |
| 530 | 4276    | 4358 | 4440 | 4522 | 4604 | 4685 | 4767 | 4849 | 4931 | 5013 | 82 |
| 531 | 5095    | 5176 | 5258 | 5340 | 5422 | 5503 | 5585 | 5667 | 5748 | 5830 | 82 |
| 532 | 5912    | 5993 | 6075 | 6156 | 6238 | 6320 | 6401 | 6483 | 6564 | 6646 | 82 |
| 533 | 6727    | 6809 | 6890 | 6972 | 7053 | 7134 | 7216 | 7297 | 7379 | 7460 | 81 |
| 534 | 7541    | 7623 | 7704 | 7785 | 7866 | 7948 | 8029 | 8110 | 8191 | 8273 | 81 |
| 535 | 8354    | 8435 | 8516 | 8597 | 8678 | 8759 | 8841 | 8922 | 9003 | 9084 | 81 |
| 536 | 9165    | 9246 | 9327 | 9408 | 9489 | 9570 | 9651 | 9732 | 9813 | 9893 | 81 |
| 537 | * 9974  | +055 | 0136 | 0217 | 0298 | 0378 | 0459 | 0540 | 0621 | 0702 | 81 |
| 538 | 73 0782 | 0863 | 0944 | 1024 | 1105 | 1186 | 1266 | 1347 | 1428 | 1508 | 81 |
| 539 | 1589    | 1669 | 1750 | 1830 | 1911 | 1991 | 2072 | 2152 | 2233 | 2313 | 81 |
| 540 | 2394    | 2474 | 2555 | 2635 | 2715 | 2796 | 2876 | 2956 | 3037 | 3117 | 80 |
| 541 | 3197    | 3278 | 3358 | 3438 | 3518 | 3598 | 3679 | 3759 | 3839 | 3919 | 80 |
| 542 | 3999    | 4079 | 4160 | 4240 | 4320 | 4400 | 4480 | 4560 | 4640 | 4720 | 80 |
| 543 | 4800    | 4880 | 4960 | 5040 | 5120 | 5200 | 5279 | 5359 | 5439 | 5519 | 80 |
| 544 | 5599    | 5679 | 5759 | 5838 | 5918 | 5998 | 6078 | 6157 | 6237 | 6317 | 80 |
| 545 | 6397    | 6476 | 6556 | 6635 | 6715 | 6795 | 6874 | 6954 | 7034 | 7113 | 80 |
| 546 | 7193    | 7272 | 7352 | 7431 | 7511 | 7590 | 7670 | 7749 | 7829 | 7908 | 79 |
| 547 | 7987    | 8067 | 8146 | 8225 | 8305 | 8384 | 8463 | 8543 | 8622 | 8701 | 79 |
| 548 | 8781    | 8860 | 8939 | 9018 | 9097 | 9177 | 9256 | 9335 | 9414 | 9493 | 79 |
| 549 | * 9572  | 9651 | 9731 | 9810 | 9889 | 9968 | +047 | 0126 | 0205 | 0284 | 79 |
| 550 | 74 0363 | 0442 | 0521 | 0600 | 0678 | 0757 | 0836 | 0915 | 0994 | 1073 | 79 |
| 551 | 1152    | 1230 | 1309 | 1388 | 1467 | 1546 | 1624 | 1703 | 1782 | 1860 | 79 |
| 552 | 1939    | 2018 | 2096 | 2175 | 2254 | 2332 | 2411 | 2490 | 2568 | 2646 | 79 |
| 553 | 2727    | 2804 | 2882 | 2961 | 3039 | 3118 | 3196 | 3275 | 3353 | 3431 | 78 |
| 554 | 3510    | 3588 | 3667 | 3745 | 3823 | 3902 | 3980 | 4058 | 4136 | 4215 | 78 |
| 555 | 4293    | 4371 | 4449 | 4528 | 4606 | 4684 | 4762 | 4840 | 4919 | 4997 | 78 |
| 556 | 5075    | 5153 | 5231 | 5309 | 5387 | 5465 | 5543 | 5621 | 5699 | 5777 | 78 |
| 557 | 5855    | 5933 | 6011 | 6089 | 6167 | 6245 | 6323 | 6401 | 6479 | 6556 | 78 |
| 558 | 6634    | 6712 | 6790 | 6868 | 6945 | 7023 | 7101 | 7179 | 7256 | 7334 | 78 |
| 559 | 7412    | 7489 | 7567 | 7645 | 7722 | 7800 | 7878 | 7955 | 8033 | 8110 | 78 |
| 560 | 8188    | 8266 | 8343 | 8421 | 8498 | 8576 | 8653 | 8731 | 8808 | 8885 | 77 |
| 561 | 8963    | 9040 | 9118 | 9195 | 9272 | 9350 | 9427 | 9504 | 9582 | 9659 | 77 |
| 562 | * 9736  | 9814 | 9891 | 9968 | +045 | 0123 | 0200 | 0277 | 0354 | 0431 | 77 |
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| 565 | 2048    | 2125 | 2202 | 2279 | 2356 | 2433 | 2509 | 2586 | 2663 | 2740 | 77 |
| 566 | 2816    | 2893 | 2970 | 3047 | 3123 | 3200 | 3277 | 3353 | 3430 | 3506 | 77 |
| 567 | 3583    | 3660 | 3736 | 3813 | 3889 | 3966 | 4042 | 4119 | 4195 | 4272 | 77 |
| 568 | 4348    | 4425 | 4501 | 4578 | 4654 | 4730 | 4807 | 4883 | 4960 | 5036 | 76 |
| 569 | 5112    | 5189 | 5265 | 5341 | 5417 | 5494 | 5570 | 5646 | 5722 | 5799 | 76 |
| 570 | 5875    | 5951 | 6027 | 6103 | 6180 | 6256 | 6332 | 6408 | 6484 | 6560 | 76 |
| 571 | 6636    | 6712 | 6788 | 6864 | 6940 | 7016 | 7092 | 7168 | 7244 | 7320 | 76 |
| 572 | 7396    | 7472 | 7548 | 7624 | 7700 | 7775 | 7851 | 7927 | 8003 | 8079 | 76 |
| 573 | 8155    | 8230 | 8306 | 8382 | 8458 | 8533 | 8609 | 8685 | 8761 | 8836 | 76 |
| 574 | 8912    | 8988 | 9063 | 9139 | 9214 | 9290 | 9366 | 9441 | 9517 | 9592 | 76 |
| 575 | * 9668  | 9743 | 9819 | 9894 | 9970 | +045 | 0121 | 0196 | 0272 | 0347 | 75 |
| 576 | 76 0422 | 0498 | 0573 | 0649 | 0724 | 0799 | 0875 | 0950 | 1025 | 1101 | 75 |
| 577 | 1176    | 1251 | 1326 | 1402 | 1477 | 1552 | 1627 | 1702 | 1778 | 1853 | 75 |
| 578 | 1928    | 2003 | 2078 | 2153 | 2228 | 2303 | 2378 | 2453 | 2529 | 2604 | 75 |
| 579 | 2679    | 2754 | 2829 | 2904 | 2978 | 3053 | 3128 | 3203 | 3278 | 3353 | 75 |
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| 580 | 76 3428 | 3503 | 3578 | 3653 | 3727 | 3802 | 3877   | 3952 | 4027 | 4101   | 75 |
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| 592 | 2322    | 2395 | 2468 | 2542 | 2615 | 2688 | 2762   | 2835 | 2908 | 2981   | 73 |
| 593 | 3055    | 3128 | 3201 | 3274 | 3348 | 3421 | 3494   | 3567 | 3640 | 3713   | 73 |
| 594 | 3786    | 3860 | 3933 | 4006 | 4079 | 4152 | 4225   | 4298 | 4371 | 4444   | 73 |
| 595 | 4517    | 4590 | 4663 | 4736 | 4809 | 4882 | 4955   | 5028 | 5100 | 5173   | 73 |
| 596 | 5246    | 5319 | 5392 | 5465 | 5538 | 5610 | 5683   | 5756 | 5829 | 5902   | 73 |
| 597 | 5974    | 6047 | 6120 | 6193 | 6265 | 6338 | 6411   | 6483 | 6556 | 6629   | 73 |
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| 600 | 8151    | 8224 | 8296 | 8368 | 8441 | 8513 | 8585   | 8658 | 8730 | 8802   | 72 |
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| 602 | * 9596  | 9669 | 9741 | 9813 | 9885 | 9957 | * 0029 | 0101 | 0173 | 0245   | 72 |
| 603 | 78 0317 | 0389 | 0461 | 0533 | 0605 | 0677 | 0749   | 0821 | 0893 | 0965   | 72 |
| 604 | 1037    | 1109 | 1181 | 1253 | 1324 | 1396 | 1468   | 1540 | 1612 | 1684   | 72 |
| 605 | 1755    | 1827 | 1899 | 1971 | 2042 | 2114 | 2186   | 2258 | 2329 | 2401   | 71 |
| 606 | 2473    | 2544 | 2616 | 2688 | 2759 | 2831 | 2902   | 2974 | 3046 | 3117   | 71 |
| 607 | 3189    | 3260 | 3332 | 3403 | 3475 | 3546 | 3618   | 3689 | 3761 | 3832   | 71 |
| 608 | 3904    | 3975 | 4046 | 4118 | 4189 | 4261 | 4332   | 4403 | 4475 | 4546   | 71 |
| 609 | 4617    | 4689 | 4760 | 4831 | 4902 | 4974 | 5045   | 5116 | 5187 | 5259   | 71 |
| 610 | 5330    | 5401 | 5472 | 5543 | 5615 | 5686 | 5757   | 5828 | 5899 | 5970   | 71 |
| 611 | 6041    | 6112 | 6183 | 6254 | 6325 | 6396 | 6467   | 6538 | 6609 | 6680   | 71 |
| 612 | 6751    | 6822 | 6893 | 6964 | 7035 | 7106 | 7177   | 7248 | 7319 | 7390   | 71 |
| 613 | 7460    | 7531 | 7602 | 7673 | 7744 | 7815 | 7885   | 7956 | 8027 | 8098   | 71 |
| 614 | 8168    | 8239 | 8310 | 8381 | 8451 | 8522 | 8593   | 8663 | 8734 | 8804   | 71 |
| 615 | 8875    | 8946 | 9016 | 9087 | 9157 | 9228 | 9299   | 9369 | 9440 | 9510   | 71 |
| 616 | * 9581  | 9651 | 9722 | 9792 | 9863 | 9933 | * 0004 | 0074 | 0144 | 0215   | 70 |
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| 619 | 1691    | 1761 | 1831 | 1901 | 1971 | 2041 | 2111   | 2181 | 2252 | 2322   | 70 |
| 620 | 2392    | 2462 | 2532 | 2602 | 2672 | 2742 | 2812   | 2882 | 2952 | 3022   | 70 |
| 621 | 3092    | 3162 | 3231 | 3301 | 3371 | 3441 | 3511   | 3581 | 3651 | 3721   | 70 |
| 622 | 3790    | 3860 | 3930 | 4000 | 4070 | 4139 | 4209   | 4279 | 4349 | 4418   | 70 |
| 623 | 4488    | 4558 | 4627 | 4697 | 4767 | 4836 | 4906   | 4976 | 5045 | 5115   | 70 |
| 624 | 5185    | 5254 | 5324 | 5393 | 5463 | 5532 | 5602   | 5672 | 5741 | 5811   | 70 |
| 625 | 5880    | 5949 | 6019 | 6088 | 6158 | 6227 | 6297   | 6366 | 6436 | 6505   | 69 |
| 626 | 6574    | 6644 | 6713 | 6782 | 6852 | 6921 | 6990   | 7060 | 7129 | 7198   | 69 |
| 627 | 7268    | 7337 | 7406 | 7475 | 7545 | 7614 | 7683   | 7752 | 7821 | 7890   | 69 |
| 628 | 7960    | 8029 | 8098 | 8167 | 8236 | 8305 | 8374   | 8443 | 8513 | 8582   | 69 |
| 629 | 8651    | 8720 | 8789 | 8858 | 8927 | 8996 | 9065   | 9134 | 9203 | 9272   | 69 |
| 630 | 9341    | 9409 | 9478 | 9547 | 9616 | 9685 | 9754   | 9823 | 9892 | 9961   | 69 |
| 631 | 80 0029 | 0098 | 0167 | 0236 | 0305 | 0373 | 0442   | 0511 | 0580 | 0648   | 69 |
| 632 | 0717    | 0786 | 0854 | 0923 | 0992 | 1061 | 1129   | 1198 | 1266 | 1335   | 69 |
| 633 | 1404    | 1472 | 1541 | 1609 | 1678 | 1747 | 1815   | 1884 | 1952 | 2021   | 69 |
| 634 | 2089    | 2158 | 2226 | 2295 | 2363 | 2432 | 2500   | 2568 | 2637 | 2705   | 69 |
| 635 | 2774    | 2842 | 2910 | 2979 | 3047 | 3116 | 3184   | 3252 | 3321 | 3389   | 68 |
| 636 | 3457    | 3525 | 3594 | 3662 | 3730 | 3798 | 3867   | 3935 | 4003 | 4071   | 68 |
| 637 | 4139    | 4208 | 4276 | 4344 | 4412 | 4480 | 4548   | 4616 | 4685 | 4753   | 68 |
| 638 | 4821    | 4889 | 4957 | 5025 | 5093 | 5161 | 5229   | 5297 | 5365 | 5433   | 68 |
| 639 | 5501    | 5569 | 5637 | 5705 | 5773 | 5841 | 5909   | 5976 | 6044 | 6112   | 68 |
| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6      | 7    | 8    | 9      | D. |

TABLE I.

## LOGARITHMS OF NUMBERS.

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| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D. |
|-----|---------|------|------|------|------|------|------|------|------|------|----|
| 640 | 80 6180 | 6248 | 6316 | 6384 | 6451 | 6519 | 6587 | 6655 | 6723 | 6790 | 68 |
| 641 | 6858    | 6926 | 6994 | 7061 | 7129 | 7197 | 7264 | 7332 | 7400 | 7467 | 68 |
| 642 | 7535    | 7603 | 7670 | 7738 | 7806 | 7873 | 7941 | 8008 | 8076 | 8143 | 68 |
| 643 | 8211    | 8279 | 8346 | 8414 | 8481 | 8549 | 8616 | 8684 | 8751 | 8818 | 67 |
| 644 | 8886    | 8953 | 9021 | 9088 | 9156 | 9223 | 9290 | 9358 | 9425 | 9492 | 67 |
| 645 | * 9560  | 9627 | 9694 | 9762 | 9829 | 9896 | 9964 | +031 | 0098 | 0165 | 67 |
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| 647 | 0904    | 0971 | 1039 | 1106 | 1173 | 1240 | 1307 | 1374 | 1441 | 1508 | 67 |
| 648 | 1575    | 1642 | 1709 | 1776 | 1843 | 1910 | 1977 | 2044 | 2111 | 2178 | 67 |
| 649 | 2245    | 2312 | 2379 | 2445 | 2512 | 2579 | 2646 | 2713 | 2780 | 2847 | 67 |
| 650 | 2913    | 2980 | 3047 | 3114 | 3181 | 3247 | 3314 | 3381 | 3448 | 3514 | 67 |
| 651 | 3581    | 3648 | 3714 | 3781 | 3848 | 3914 | 3981 | 4048 | 4114 | 4181 | 67 |
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| 654 | 5578    | 5644 | 5711 | 5777 | 5843 | 5910 | 5976 | 6042 | 6109 | 6175 | 66 |
| 655 | 6241    | 6308 | 6374 | 6440 | 6506 | 6573 | 6639 | 6705 | 6771 | 6838 | 66 |
| 656 | 6904    | 6970 | 7036 | 7102 | 7169 | 7235 | 7301 | 7367 | 7433 | 7499 | 66 |
| 657 | 7565    | 7631 | 7698 | 7764 | 7830 | 7896 | 7962 | 8028 | 8094 | 8160 | 66 |
| 658 | 8226    | 8292 | 8358 | 8424 | 8490 | 8556 | 8622 | 8688 | 8754 | 8820 | 66 |
| 659 | 8885    | 8951 | 9017 | 9083 | 9149 | 9215 | 9281 | 9346 | 9412 | 9478 | 66 |
| 660 | * 9544  | 9610 | 9676 | 9741 | 9807 | 9873 | 9939 | +004 | 0070 | 0136 | 66 |
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| 662 | 0858    | 0924 | 0989 | 1055 | 1120 | 1186 | 1251 | 1317 | 1382 | 1448 | 66 |
| 663 | 1514    | 1579 | 1645 | 1710 | 1775 | 1841 | 1906 | 1972 | 2037 | 2103 | 65 |
| 664 | 2168    | 2233 | 2299 | 2364 | 2430 | 2495 | 2560 | 2626 | 2691 | 2756 | 65 |
| 665 | 2822    | 2887 | 2952 | 3018 | 3083 | 3148 | 3213 | 3279 | 3344 | 3409 | 65 |
| 666 | 3474    | 3539 | 3605 | 3670 | 3735 | 3800 | 3865 | 3930 | 3996 | 4061 | 65 |
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| 670 | 6075    | 6140 | 6204 | 6269 | 6334 | 6399 | 6464 | 6528 | 6593 | 6658 | 65 |
| 671 | 6723    | 6787 | 6852 | 6917 | 6981 | 7046 | 7111 | 7175 | 7240 | 7305 | 65 |
| 672 | 7369    | 7434 | 7499 | 7563 | 7628 | 7692 | 7757 | 7821 | 7886 | 7951 | 65 |
| 673 | 8015    | 8080 | 8144 | 8209 | 8273 | 8338 | 8402 | 8467 | 8531 | 8595 | 64 |
| 674 | 8660    | 8724 | 8789 | 8853 | 8918 | 8982 | 9046 | 9111 | 9175 | 9239 | 64 |
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| 685 | 5691    | 5754 | 5817 | 5881 | 5944 | 6007 | 6071 | 6134 | 6197 | 6261 | 63 |
| 686 | 6324    | 6387 | 6451 | 6514 | 6577 | 6641 | 6704 | 6767 | 6830 | 6894 | 63 |
| 687 | 6957    | 7020 | 7083 | 7146 | 7210 | 7273 | 7336 | 7399 | 7462 | 7525 | 63 |
| 688 | 7588    | 7652 | 7715 | 7778 | 7841 | 7904 | 7967 | 8030 | 8093 | 8156 | 63 |
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| 694 | 1359    | 1422 | 1485 | 1547 | 1610 | 1672 | 1735 | 1797 | 1860 | 1922 | 63 |
| 695 | 1985    | 2047 | 2110 | 2172 | 2235 | 2297 | 2360 | 2422 | 2484 | 2547 | 62 |
| 696 | 2609    | 2672 | 2734 | 2796 | 2859 | 2921 | 2983 | 3046 | 3108 | 3170 | 62 |
| 697 | 3233    | 3295 | 3357 | 3420 | 3482 | 3544 | 3606 | 3669 | 3731 | 3793 | 62 |
| 698 | 3855    | 3918 | 3980 | 4042 | 4104 | 4166 | 4229 | 4291 | 4353 | 4415 | 62 |
| 699 | 4477    | 4539 | 4601 | 4664 | 4726 | 4788 | 4850 | 4912 | 4974 | 5036 | 62 |
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| 702 | 6337    | 5399 | 6461 | 6523 | 6585 | 6646 | 6708 | 6770 | 6832 | 6894 | 62 |
| 703 | 6655    | 7017 | 7079 | 7141 | 7202 | 7264 | 7326 | 7388 | 7449 | 7511 | 62 |
| 704 | 7573    | 7634 | 7696 | 7758 | 7819 | 7881 | 7943 | 8004 | 8066 | 8128 | 62 |
| 705 | 8189    | 8251 | 8312 | 8374 | 8435 | 8497 | 8559 | 8620 | 8682 | 8743 | 62 |
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| 721 | 7935    | 7995 | 8056 | 8116 | 8176 | 8236 | 8297 | 8357 | 8417 | 8477 | 60 |
| 722 | 8537    | 8597 | 8657 | 8718 | 8778 | 8838 | 8898 | 8958 | 9018 | 9078 | 60 |
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| 727 | 1534    | 1594 | 1654 | 1714 | 1773 | 1833 | 1893 | 1952 | 2012 | 2072 | 60 |
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| 729 | 2728    | 2787 | 2847 | 2906 | 2966 | 3025 | 3085 | 3144 | 3204 | 3263 | 60 |
| 730 | 3323    | 3382 | 3442 | 3501 | 3561 | 3620 | 3680 | 3739 | 3799 | 3858 | 59 |
| 731 | 3917    | 3977 | 4036 | 4096 | 4155 | 4214 | 4274 | 4333 | 4392 | 4452 | 59 |
| 732 | 4511    | 4570 | 4630 | 4689 | 4748 | 4808 | 4867 | 4926 | 4985 | 5045 | 59 |
| 733 | 5104    | 5163 | 5222 | 5282 | 5341 | 5400 | 5459 | 5519 | 5578 | 5637 | 59 |
| 734 | 5696    | 5755 | 5814 | 5874 | 5933 | 5992 | 6051 | 6110 | 6169 | 6228 | 59 |
| 735 | 6287    | 6346 | 6405 | 6465 | 6524 | 6583 | 6642 | 6701 | 6760 | 6819 | 59 |
| 736 | 6878    | 6937 | 6996 | 7055 | 7114 | 7173 | 7232 | 7291 | 7350 | 7409 | 59 |
| 737 | 7467    | 7526 | 7585 | 7644 | 7703 | 7762 | 7821 | 7880 | 7939 | 7998 | 59 |
| 738 | 8056    | 8115 | 8174 | 8233 | 8292 | 8350 | 8409 | 8468 | 8527 | 8586 | 59 |
| 739 | 8644    | 8703 | 8762 | 8821 | 8879 | 8938 | 8997 | 9056 | 9114 | 9173 | 59 |
| 740 | 9232    | 9290 | 9349 | 9408 | 9466 | 9525 | 9584 | 9642 | 9701 | 9760 | 59 |
| 741 | * 9818  | 9877 | 9935 | 9994 | +053 | 0111 | 0170 | 0228 | 0287 | 0345 | 59 |
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| 743 | 0989    | 1047 | 1106 | 1164 | 1223 | 1281 | 1339 | 1398 | 1456 | 1515 | 58 |
| 744 | 1573    | 1631 | 1690 | 1748 | 1806 | 1865 | 1923 | 1981 | 2040 | 2098 | 58 |
| 745 | 2156    | 2215 | 2273 | 2331 | 2389 | 2448 | 2506 | 2564 | 2622 | 2681 | 58 |
| 746 | 2739    | 2797 | 2855 | 2913 | 2972 | 3030 | 3088 | 3146 | 3204 | 3262 | 58 |
| 747 | 3321    | 3379 | 3437 | 3495 | 3553 | 3611 | 3669 | 3727 | 3785 | 3844 | 58 |
| 748 | 3902    | 3960 | 4018 | 4076 | 4134 | 4192 | 4250 | 4308 | 4366 | 4424 | 58 |
| 749 | 4482    | 4540 | 4598 | 4656 | 4714 | 4772 | 4830 | 4888 | 4945 | 5003 | 58 |
| 750 | 5061    | 5119 | 5177 | 5235 | 5293 | 5351 | 5409 | 5466 | 5524 | 5582 | 58 |
| 751 | 5640    | 5698 | 5756 | 5813 | 5871 | 5929 | 5987 | 6045 | 6102 | 6160 | 58 |
| 752 | 6218    | 6276 | 6333 | 6391 | 6449 | 6507 | 6564 | 6622 | 6680 | 6737 | 58 |
| 753 | 6795    | 6853 | 6910 | 6968 | 7026 | 7083 | 7141 | 7199 | 7256 | 7314 | 58 |
| 754 | 7371    | 7429 | 7487 | 7544 | 7602 | 7659 | 7717 | 7774 | 7832 | 7889 | 58 |
| 755 | 7947    | 8004 | 8062 | 8119 | 8177 | 8234 | 8292 | 8349 | 8407 | 8464 | 57 |
| 756 | 8522    | 8579 | 8637 | 8694 | 8752 | 8809 | 8866 | 8924 | 8981 | 9039 | 57 |
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| 758 | * 9669  | 9726 | 9784 | 9841 | 9898 | 9956 | +013 | 0070 | 0127 | 0185 | 57 |
| 759 | 88 0242 | 0299 | 0356 | 0413 | 0471 | 0528 | 0585 | 0642 | 0699 | 0756 | 57 |
| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D. |

TABLE I.

## LOGARITHMS OF NUMBERS.

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| N.  | 0       | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | D. |
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| 848 | 8396    | 8447 | 8498 | 8549 | 8601 | 8652 | 8703 | 8754 | 8805 | 8857 | 51 |
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| 856 | 2474    | 2524 | 2575 | 2626 | 2677 | 2727 | 2778 | 2829 | 2879 | 2930 | 51 |
| 857 | 2981    | 3031 | 3082 | 3133 | 3183 | 3234 | 3285 | 3335 | 3386 | 3437 | 51 |
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| 879 | 3989    | 4038 | 4088 | 4137 | 4186 | 4236 | 4285 | 4335 | 4384 | 4433 | 49 |
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TABLE I.

## LOGARITHMS OF NUMBERS.

15

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| 959 | 1819    | 1864 | 1909 | 1954  | 2000 | 2045 | 2090 | 2135 | 2181 | 2226 | 45 |
| 960 | 2271    | 2316 | 2362 | 2407  | 2452 | 2497 | 2543 | 2588 | 2633 | 2678 | 45 |
| 961 | 2723    | 2769 | 2814 | 2859  | 2904 | 2949 | 2994 | 3040 | 3085 | 3130 | 45 |
| 962 | 3175    | 3220 | 3265 | 3310  | 3356 | 3401 | 3446 | 3491 | 3536 | 3581 | 45 |
| 963 | 3626    | 3671 | 3716 | 3762  | 3807 | 3852 | 3897 | 3942 | 3987 | 4032 | 45 |
| 964 | 4077    | 4122 | 4167 | 4212  | 4257 | 4302 | 4347 | 4392 | 4437 | 4482 | 45 |
| 965 | 4527    | 4572 | 4617 | 4662  | 4707 | 4752 | 4797 | 4842 | 4887 | 4932 | 45 |
| 966 | 4977    | 5022 | 5067 | 5112  | 5157 | 5202 | 5247 | 5292 | 5337 | 5382 | 45 |
| 967 | 5426    | 5471 | 5516 | 5561  | 5606 | 5651 | 5696 | 5741 | 5786 | 5830 | 45 |
| 968 | 5875    | 5920 | 5965 | 6010  | 6055 | 6100 | 6144 | 6189 | 6234 | 6279 | 45 |
| 969 | 6324    | 6369 | 6413 | 6458  | 6503 | 6548 | 6593 | 6637 | 6682 | 6727 | 45 |
| 970 | 6772    | 6817 | 6861 | 6906  | 6951 | 6996 | 7040 | 7085 | 7130 | 7175 | 45 |
| 971 | 7219    | 7264 | 7309 | 7353  | 7398 | 7443 | 7488 | 7532 | 7577 | 7622 | 45 |
| 972 | 7666    | 7711 | 7756 | 7800  | 7845 | 7890 | 7934 | 7979 | 8024 | 8068 | 45 |
| 973 | 8113    | 8157 | 8202 | 8247  | 8291 | 8336 | 8381 | 8425 | 8470 | 8514 | 45 |
| 974 | 8559    | 8604 | 8648 | 8693  | 8737 | 8782 | 8826 | 8871 | 8916 | 8960 | 45 |
| 975 | 9005    | 9049 | 9094 | 9138  | 9183 | 9227 | 9272 | 9316 | 9361 | 9405 | 45 |
| 976 | 9450    | 9494 | 9539 | 9583  | 9628 | 9672 | 9717 | 9761 | 9806 | 9850 | 44 |
| 977 | * 9895  | 9939 | 9983 | 10028 | 0072 | 0117 | 0161 | 0206 | 0250 | 0294 | 44 |
| 978 | 99 0339 | 0383 | 0428 | 0472  | 0516 | 0561 | 0605 | 0650 | 0694 | 0738 | 44 |
| 979 | 0783    | 0827 | 0871 | 0916  | 0960 | 1004 | 1049 | 1093 | 1137 | 1182 | 44 |
| 980 | 1226    | 1270 | 1315 | 1359  | 1403 | 1448 | 1492 | 1536 | 1580 | 1625 | 44 |
| 981 | 1669    | 1713 | 1758 | 1802  | 1846 | 1890 | 1935 | 1979 | 2023 | 2067 | 44 |
| 982 | 2111    | 2156 | 2200 | 2244  | 2288 | 2333 | 2377 | 2421 | 2465 | 2509 | 44 |
| 983 | 2554    | 2598 | 2642 | 2686  | 2730 | 2774 | 2819 | 2863 | 2907 | 2951 | 44 |
| 984 | 2995    | 3039 | 3083 | 3127  | 3172 | 3216 | 3260 | 3304 | 3348 | 3392 | 44 |
| 985 | 3436    | 3480 | 3524 | 3568  | 3613 | 3657 | 3701 | 3745 | 3789 | 3833 | 44 |
| 986 | 3877    | 3921 | 3965 | 4009  | 4053 | 4097 | 4141 | 4185 | 4229 | 4273 | 44 |
| 987 | 4317    | 4361 | 4405 | 4449  | 4493 | 4537 | 4581 | 4625 | 4669 | 4713 | 44 |
| 988 | 4757    | 4801 | 4845 | 4889  | 4933 | 4977 | 5021 | 5065 | 5108 | 5152 | 44 |
| 989 | 5196    | 5240 | 5284 | 5328  | 5372 | 5416 | 5460 | 5504 | 5547 | 5591 | 44 |
| 990 | 5635    | 5679 | 5723 | 5767  | 5811 | 5854 | 5898 | 5942 | 5986 | 6030 | 44 |
| 991 | 6074    | 6117 | 6161 | 6205  | 6249 | 6293 | 6337 | 6380 | 6424 | 6468 | 44 |
| 992 | 6512    | 6555 | 6599 | 6643  | 6687 | 6731 | 6774 | 6818 | 6862 | 6906 | 44 |
| 993 | 6949    | 6993 | 7037 | 7080  | 7124 | 7168 | 7212 | 7255 | 7299 | 7343 | 44 |
| 994 | 7386    | 7430 | 7474 | 7517  | 7561 | 7605 | 7648 | 7692 | 7736 | 7779 | 44 |
| 995 | 7823    | 7867 | 7910 | 7954  | 7998 | 8041 | 8085 | 8129 | 8172 | 8216 | 44 |
| 996 | 8259    | 8303 | 8347 | 8390  | 8434 | 8477 | 8521 | 8564 | 8608 | 8652 | 44 |
| 997 | 8695    | 8739 | 8782 | 8826  | 8869 | 8913 | 8956 | 9000 | 9043 | 9087 | 44 |
| 998 | 9131    | 9174 | 9218 | 9261  | 9305 | 9348 | 9392 | 9435 | 9479 | 9522 | 44 |
| 999 | 9565    | 9609 | 9652 | 9696  | 9739 | 9783 | 9826 | 9870 | 9913 | 9957 | 43 |
| N.  | 0       | 1    | 2    | 3     | 4    | 5    | 6    | 7    | 8    | 9    | D. |



## TABLE II.

### LOGARITHMIC SINES AND TANGENTS.

FOR

EVERY DEGREE AND MINUTE OF THE QUADRANT.

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If the logarithms of the values in Table III. be each increased by 10, the results will be the values of this table.

The logarithmic Secants and Cosecants are not given. They may be readily obtained, as follows:—Subtract the logarithmic Cosine from 20, and the remainder will be the logarithmic Secant; subtract the logarithmic Sine from 20, and the remainder will be the logarithmic Cosecant.

0°

179°

| /  | Sine.     | D.     | Cosine.   | D. | Tang.     | D.     | Cotang.   | /  |
|----|-----------|--------|-----------|----|-----------|--------|-----------|----|
| 0  | Inf. Neg. |        | 10·000000 |    | Inf. Neg. |        | Infinita. | 60 |
| 1  | 6·463726  | 501717 | 000000    | 00 | 6·463726  | 501717 | 13·536274 | 59 |
| 2  | 764756    | 293485 | 000000    | 00 | 764756    | 293483 | 235244    | 58 |
| 3  | 940847    | 208231 | 000000    | 00 | 940847    | 208231 | 059153    | 57 |
| 4  | 7·065786  | 161517 | 000000    | 00 | 7·065786  | 161517 | 12·034214 | 56 |
| 5  | 162606    | 131968 | 000000    | 00 | 162606    | 131969 | 837304    | 55 |
| 6  | 241877    | 111575 | 9·999999  | 01 | 241878    | 111578 | 758122    | 54 |
| 7  | 308824    | 96653  | 999999    | 01 | 308825    | 96653  | 691175    | 53 |
| 8  | 366816    | 85254  | 999999    | 01 | 366817    | 85254  | 633183    | 52 |
| 9  | 417968    | 76263  | 999999    | 01 | 417970    | 76263  | 582030    | 51 |
| 10 | 463726    | 68988  | 999998    | 01 | 463727    | 68988  | 536273    | 50 |
| 11 | 7·505118  | 62981  | 9·999998  | 01 | 7·505120  | 62981  | 12·494880 | 49 |
| 12 | 542906    | 57936  | 999997    | 01 | 542909    | 57933  | 457091    | 48 |
| 13 | 577668    | 53641  | 999997    | 01 | 577672    | 53642  | 422328    | 47 |
| 14 | 609853    | 49938  | 999996    | 01 | 609857    | 49939  | 390143    | 46 |
| 15 | 639816    | 46714  | 999996    | 01 | 639820    | 46715  | 360180    | 45 |
| 16 | 667845    | 43881  | 999995    | 01 | 667849    | 43882  | 332151    | 44 |
| 17 | 694173    | 41372  | 999995    | 01 | 694179    | 41373  | 305821    | 43 |
| 18 | 718997    | 39135  | 999994    | 01 | 719003    | 39136  | 280997    | 42 |
| 19 | 742478    | 37127  | 999993    | 01 | 742484    | 37128  | 255161    | 41 |
| 20 | 764754    | 35315  | 999993    | 01 | 764761    | 35136  | 235239    | 40 |
| 21 | 7·785943  | 33672  | 9·999992  | 01 | 7·785951  | 33673  | 12·214049 | 39 |
| 22 | 806146    | 32175  | 999991    | 01 | 806155    | 32176  | 193845    | 38 |
| 23 | 825451    | 30805  | 999990    | 01 | 825460    | 30806  | 174540    | 37 |
| 24 | 843934    | 29547  | 999989    | 02 | 843944    | 29549  | 156056    | 36 |
| 25 | 861662    | 28388  | 999989    | 02 | 861674    | 28390  | 138326    | 35 |
| 26 | 878695    | 27317  | 999988    | 02 | 878708    | 27318  | 121292    | 34 |
| 27 | 895085    | 26323  | 999987    | 02 | 895099    | 26325  | 104901    | 33 |
| 28 | 910879    | 25399  | 999986    | 02 | 910894    | 25401  | 089106    | 32 |
| 29 | 926119    | 24538  | 999985    | 02 | 926134    | 24540  | 073866    | 31 |
| 30 | 940842    | 23733  | 999983    | 02 | 940858    | 23735  | 059142    | 30 |
| 31 | 7·955082  | 22980  | 9·999982  | 02 | 7·955100  | 22981  | 12·044900 | 29 |
| 32 | 968870    | 22273  | 999981    | 02 | 968880    | 22275  | 031111    | 28 |
| 33 | 982233    | 21608  | 999980    | 02 | 982253    | 21610  | 017747    | 27 |
| 34 | 995198    | 20981  | 999979    | 02 | 995219    | 20983  | 004781    | 26 |
| 35 | 8·007787  | 20390  | 999977    | 02 | 8·007809  | 20392  | 11·992191 | 25 |
| 36 | 020021    | 19831  | 999976    | 02 | 020044    | 19833  | 979936    | 24 |
| 37 | 031919    | 19302  | 999975    | 02 | 031945    | 19305  | 968055    | 23 |
| 38 | 043501    | 18801  | 999973    | 02 | 043527    | 18803  | 956473    | 22 |
| 39 | 054781    | 18325  | 999972    | 02 | 054809    | 18327  | 945191    | 21 |
| 40 | 065776    | 17872  | 999971    | 02 | 065806    | 17874  | 934194    | 20 |
| 41 | 8·076500  | 17441  | 9·999969  | 02 | 8·076531  | 17444  | 11·923469 | 19 |
| 42 | 086965    | 17031  | 999968    | 02 | 086997    | 17034  | 913003    | 18 |
| 43 | 097183    | 16639  | 999966    | 02 | 097217    | 16642  | 902783    | 17 |
| 44 | 107167    | 16265  | 999964    | 03 | 107203    | 16268  | 892797    | 16 |
| 45 | 116926    | 15908  | 999963    | 03 | 116963    | 15910  | 883037    | 15 |
| 46 | 126471    | 15566  | 999961    | 03 | 126510    | 15568  | 873490    | 14 |
| 47 | 135810    | 15238  | 999959    | 03 | 135851    | 15241  | 864149    | 13 |
| 48 | 144953    | 14924  | 999958    | 03 | 144996    | 14927  | 855004    | 12 |
| 49 | 153907    | 14622  | 999956    | 03 | 153952    | 14627  | 846048    | 11 |
| 50 | 162681    | 14333  | 999954    | 03 | 162727    | 14336  | 837273    | 10 |
| 51 | 8·171280  | 14054  | 9·999952  | 03 | 8·171328  | 14057  | 11·828672 | 9  |
| 52 | 179713    | 13786  | 999950    | 03 | 179763    | 13790  | 820237    | 8  |
| 53 | 187985    | 13529  | 999948    | 03 | 188036    | 13532  | 811964    | 7  |
| 54 | 196102    | 13280  | 999946    | 03 | 196156    | 13284  | 803844    | 6  |
| 55 | 204070    | 13041  | 999944    | 03 | 204126    | 13044  | 795874    | 5  |
| 56 | 211895    | 12810  | 999942    | 04 | 211953    | 12814  | 788047    | 4  |
| 57 | 219581    | 12587  | 999940    | 04 | 219641    | 12590  | 780359    | 3  |
| 58 | 227134    | 12372  | 999938    | 04 | 227195    | 12376  | 772805    | 2  |
| 59 | 234557    | 12164  | 999936    | 04 | 234621    | 12168  | 765379    | 1  |
| 60 | 241855    | 11963  | 999934    | 04 | 241921    | 11967  | 758079    | 0  |
| /  | Cosine.   | D.     | Sine.     | D. | Cotang.   | D.     | Tang.     | /  |

90°

89°

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 1° |          |       |          |    | 178°     |       |           |    |  |
|----|----------|-------|----------|----|----------|-------|-----------|----|--|
| /  | Sine.    | D.    | Cosine.  | D. | Tang.    | D.    | Cotang.   | /  |  |
| 0  | 8.241855 | 11963 | 9.999934 | 04 | 8.241921 | 11967 | 11.758079 | 60 |  |
| 1  | 249033   | 11768 | 999932   | 04 | 249102   | 11772 | 750898    | 59 |  |
| 2  | 256094   | 11580 | 999929   | 04 | 256165   | 11584 | 743835    | 58 |  |
| 3  | 263042   | 11398 | 999927   | 04 | 263115   | 11402 | 736885    | 57 |  |
| 4  | 269881   | 11221 | 999925   | 04 | 269956   | 11225 | 730044    | 56 |  |
| 5  | 276614   | 11050 | 999922   | 04 | 276691   | 11054 | 723309    | 55 |  |
| 6  | 283243   | 10883 | 999920   | 04 | 283323   | 10887 | 716677    | 54 |  |
| 7  | 289773   | 10721 | 999918   | 04 | 289856   | 10726 | 710144    | 53 |  |
| 8  | 296207   | 10565 | 999915   | 04 | 296292   | 10570 | 703708    | 52 |  |
| 9  | 302546   | 10413 | 999913   | 04 | 302634   | 10418 | 697366    | 51 |  |
| 10 | 308794   | 10266 | 999910   | 04 | 308884   | 10270 | 691116    | 50 |  |
| 11 | 8.314954 | 10122 | 9.999907 | 04 | 8.315046 | 10126 | 11.684954 | 49 |  |
| 12 | 321027   | 9982  | 999905   | 04 | 321122   | 9987  | 678878    | 48 |  |
| 13 | 327016   | 9847  | 999902   | 04 | 327114   | 9851  | 672886    | 47 |  |
| 14 | 332924   | 9714  | 999899   | 05 | 333025   | 9719  | 666975    | 46 |  |
| 15 | 338753   | 9586  | 999897   | 05 | 338856   | 9590  | 661144    | 45 |  |
| 16 | 344504   | 9460  | 999894   | 05 | 344610   | 9465  | 655390    | 44 |  |
| 17 | 350181   | 9338  | 999891   | 05 | 350289   | 9343  | 649711    | 43 |  |
| 18 | 355783   | 9219  | 999888   | 05 | 355895   | 9224  | 644105    | 42 |  |
| 19 | 361315   | 9103  | 999885   | 05 | 361430   | 9108  | 638576    | 41 |  |
| 20 | 366777   | 8990  | 999882   | 05 | 366895   | 8995  | 633105    | 40 |  |
| 21 | 8.372171 | 8880  | 9.999879 | 05 | 8.372292 | 8885  | 11.627708 | 39 |  |
| 22 | 377499   | 8772  | 999876   | 05 | 377622   | 8777  | 622378    | 38 |  |
| 23 | 382762   | 8667  | 999873   | 05 | 382889   | 8672  | 617111    | 37 |  |
| 24 | 387962   | 8564  | 999870   | 05 | 388092   | 8570  | 611908    | 36 |  |
| 25 | 393101   | 8464  | 999867   | 05 | 393234   | 8470  | 606766    | 35 |  |
| 26 | 398179   | 8366  | 999864   | 05 | 398315   | 8371  | 601685    | 34 |  |
| 27 | 403199   | 8271  | 999861   | 05 | 403338   | 8276  | 596662    | 33 |  |
| 28 | 408161   | 8177  | 999858   | 05 | 408304   | 8182  | 591696    | 32 |  |
| 29 | 413068   | 8086  | 999854   | 05 | 413213   | 8091  | 586787    | 31 |  |
| 30 | 417919   | 7996  | 999851   | 06 | 418068   | 8002  | 581932    | 30 |  |
| 31 | 8.422717 | 7909  | 9.999848 | 06 | 8.422869 | 7914  | 11.577131 | 29 |  |
| 32 | 427462   | 7823  | 999844   | 06 | 427618   | 7830  | 572382    | 28 |  |
| 33 | 432156   | 7740  | 999841   | 06 | 432315   | 7745  | 567685    | 27 |  |
| 34 | 436800   | 7657  | 999838   | 06 | 436962   | 7663  | 563038    | 26 |  |
| 35 | 441394   | 7577  | 999834   | 06 | 441560   | 7583  | 558440    | 25 |  |
| 36 | 445941   | 7499  | 999831   | 06 | 446110   | 7505  | 553890    | 24 |  |
| 37 | 450440   | 7422  | 999827   | 06 | 450613   | 7428  | 549387    | 23 |  |
| 38 | 454893   | 7346  | 999824   | 06 | 455070   | 7352  | 544930    | 22 |  |
| 39 | 459301   | 7273  | 999820   | 06 | 459481   | 7279  | 540519    | 21 |  |
| 40 | 463665   | 7200  | 999816   | 06 | 463849   | 7206  | 536151    | 20 |  |
| 41 | 8.467985 | 7129  | 9.999813 | 06 | 8.468172 | 7135  | 11.531828 | 19 |  |
| 42 | 472263   | 7060  | 999809   | 06 | 472454   | 7066  | 527546    | 18 |  |
| 43 | 476498   | 6991  | 999805   | 06 | 476693   | 6998  | 523307    | 17 |  |
| 44 | 480693   | 6924  | 999801   | 06 | 480892   | 6931  | 519108    | 16 |  |
| 45 | 484848   | 6859  | 999797   | 07 | 485050   | 6865  | 514950    | 15 |  |
| 46 | 488963   | 6794  | 999794   | 07 | 489170   | 6801  | 510830    | 14 |  |
| 47 | 493040   | 6731  | 999790   | 07 | 493250   | 6738  | 506750    | 13 |  |
| 48 | 497078   | 6669  | 999786   | 07 | 497293   | 6676  | 502707    | 12 |  |
| 49 | 501080   | 6608  | 999782   | 07 | 501298   | 6615  | 498702    | 11 |  |
| 50 | 505045   | 6548  | 999778   | 07 | 505267   | 6555  | 494733    | 10 |  |
| 51 | 8.508974 | 6489  | 9.999774 | 07 | 8.509200 | 6496  | 11.490800 | 9  |  |
| 52 | 512867   | 6431  | 999769   | 07 | 513098   | 6439  | 486902    | 8  |  |
| 53 | 516726   | 6375  | 999765   | 07 | 516961   | 6382  | 483039    | 7  |  |
| 54 | 520551   | 6319  | 999761   | 07 | 520790   | 6326  | 479210    | 6  |  |
| 55 | 524343   | 6264  | 999757   | 07 | 524586   | 6272  | 475414    | 5  |  |
| 56 | 528102   | 6211  | 999753   | 07 | 528349   | 6218  | 471651    | 4  |  |
| 57 | 531828   | 6158  | 999748   | 07 | 532080   | 6165  | 467920    | 3  |  |
| 58 | 535523   | 6106  | 999744   | 07 | 535779   | 6113  | 464221    | 2  |  |
| 59 | 539186   | 6055  | 999740   | 07 | 539447   | 6062  | 460553    | 1  |  |
| 60 | 542819   | 6004  | 999735   | 07 | 543084   | 6012  | 456916    | 0  |  |
| /  | Cosine.  | D.    | Sine.    | D. | Cotang.  | D.    | Tang.     | /  |  |

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|    | Sec.     | D.   | Cotang.  | D. | Tang.    | D.   | Cotang.   |    |
|----|----------|------|----------|----|----------|------|-----------|----|
| 0  | 8.562919 | 6004 | 9.999735 | 07 | 8.563084 | 6012 | 11.456916 | 60 |
| 1  | 564422   | 5993 | 999731   | 07 | 564601   | 5962 | 453309    | 59 |
| 2  | 565925   | 5982 | 999726   | 07 | 565768   | 5914 | 446732    | 58 |
| 3  | 567428   | 5971 | 999722   | 08 | 567317   | 5866 | 440183    | 57 |
| 4  | 568931   | 5961 | 999717   | 08 | 567336   | 5819 | 442664    | 56 |
| 5  | 570434   | 5951 | 999713   | 08 | 568228   | 5773 | 439172    | 55 |
| 6  | 571937   | 5941 | 999708   | 08 | 569291   | 5727 | 435709    | 54 |
| 7  | 573440   | 5931 | 999704   | 08 | 567727   | 5682 | 432273    | 53 |
| 8  | 574943   | 5920 | 999699   | 08 | 571137   | 5638 | 428863    | 52 |
| 9  | 576446   | 5910 | 999694   | 08 | 574520   | 5595 | 425480    | 51 |
| 10 | 577949   | 5900 | 999689   | 08 | 577877   | 5552 | 422123    | 50 |
| 11 | 8.584492 | 5890 | 9.999685 | 08 | 8.581208 | 5510 | 11.418792 | 49 |
| 12 | 584113   | 5880 | 999680   | 08 | 584514   | 5468 | 415486    | 48 |
| 13 | 585616   | 5870 | 999675   | 08 | 587795   | 5427 | 412205    | 47 |
| 14 | 587119   | 5860 | 999670   | 08 | 591051   | 5387 | 408949    | 46 |
| 15 | 588622   | 5850 | 999665   | 08 | 594283   | 5347 | 405717    | 45 |
| 16 | 590125   | 5840 | 999660   | 08 | 597492   | 5308 | 402508    | 44 |
| 17 | 591628   | 5830 | 999655   | 08 | 600677   | 5270 | 399323    | 43 |
| 18 | 593131   | 5820 | 999650   | 08 | 603839   | 5232 | 396161    | 42 |
| 19 | 594634   | 5810 | 999645   | 09 | 606978   | 5194 | 393022    | 41 |
| 20 | 596137   | 5800 | 999640   | 09 | 610094   | 5158 | 389909    | 40 |
| 21 | 8.612423 | 5790 | 9.999635 | 09 | 8.613189 | 5121 | 11.386811 | 39 |
| 22 | 612426   | 5780 | 999630   | 09 | 616262   | 5085 | 386738    | 38 |
| 23 | 613929   | 5770 | 999624   | 09 | 619313   | 5050 | 383687    | 37 |
| 24 | 615432   | 5760 | 999619   | 09 | 622343   | 5015 | 379657    | 36 |
| 25 | 616935   | 5750 | 999614   | 09 | 625352   | 4981 | 374648    | 35 |
| 26 | 618438   | 5740 | 999608   | 09 | 628340   | 4947 | 371660    | 34 |
| 27 | 619941   | 5730 | 999603   | 09 | 631308   | 4913 | 368692    | 33 |
| 28 | 621444   | 5720 | 999597   | 09 | 634256   | 4880 | 365744    | 32 |
| 29 | 622947   | 5710 | 999592   | 09 | 637184   | 4848 | 362816    | 31 |
| 30 | 624450   | 5700 | 999586   | 09 | 640093   | 4816 | 359907    | 30 |
| 31 | 8.642463 | 4775 | 9.999581 | 09 | 8.642982 | 4784 | 11.357018 | 29 |
| 32 | 642466   | 4765 | 999575   | 09 | 645953   | 4753 | 354147    | 28 |
| 33 | 643969   | 4755 | 999570   | 09 | 648904   | 4722 | 351296    | 27 |
| 34 | 645472   | 4745 | 999564   | 09 | 651837   | 4691 | 348463    | 26 |
| 35 | 646975   | 4735 | 999558   | 10 | 654752   | 4661 | 345648    | 25 |
| 36 | 648478   | 4725 | 999553   | 10 | 657649   | 4631 | 342851    | 24 |
| 37 | 649981   | 4715 | 999547   | 10 | 660528   | 4602 | 340072    | 23 |
| 38 | 651484   | 4705 | 999541   | 10 | 663400   | 4573 | 337311    | 22 |
| 39 | 652987   | 4695 | 999535   | 10 | 666263   | 4544 | 334567    | 21 |
| 40 | 654490   | 4685 | 999529   | 10 | 669116   | 4526 | 331840    | 20 |
| 41 | 8.672493 | 4670 | 9.999524 | 10 | 8.672970 | 4488 | 11.329130 | 19 |
| 42 | 672496   | 4660 | 999518   | 10 | 675953   | 4461 | 326437    | 18 |
| 43 | 673999   | 4650 | 999512   | 10 | 678900   | 4434 | 323761    | 17 |
| 44 | 675502   | 4640 | 999506   | 10 | 681844   | 4417 | 321100    | 16 |
| 45 | 677005   | 4630 | 999500   | 10 | 684772   | 4390 | 318456    | 15 |
| 46 | 678508   | 4620 | 999493   | 10 | 687691   | 4364 | 315828    | 14 |
| 47 | 680011   | 4610 | 999487   | 10 | 690604   | 4338 | 313216    | 13 |
| 48 | 681514   | 4600 | 999481   | 10 | 693511   | 4313 | 310619    | 12 |
| 49 | 683017   | 4590 | 999475   | 10 | 696413   | 4287 | 308037    | 11 |
| 50 | 684520   | 4580 | 999469   | 10 | 699319   | 4262 | 305471    | 10 |
| 51 | 8.692493 | 4575 | 9.999463 | 11 | 8.692981 | 4228 | 11.302919 | 9  |
| 52 | 692496   | 4565 | 999456   | 11 | 700017   | 4203 | 300383    | 8  |
| 53 | 693999   | 4555 | 999450   | 11 | 702939   | 4178 | 297861    | 7  |
| 54 | 695502   | 4545 | 999443   | 11 | 705860   | 4153 | 295354    | 6  |
| 55 | 697005   | 4535 | 999437   | 11 | 708772   | 4128 | 292860    | 5  |
| 56 | 698508   | 4525 | 999431   | 11 | 711691   | 4103 | 290382    | 4  |
| 57 | 699981   | 4515 | 999424   | 11 | 714603   | 4078 | 287917    | 3  |
| 58 | 701484   | 4505 | 999418   | 11 | 717514   | 4053 | 285466    | 2  |
| 59 | 702987   | 4495 | 999411   | 11 | 720426   | 4028 | 283028    | 1  |
| 60 | 704490   | 4485 | 999404   | 11 | 723339   | 4017 | 280604    | 0  |
|    | Cotang.  | D.   | Sec.     | D. | Cotang.  | D.   | Tang.     |    |

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 8° |          |      |          |    |          |      |           | 176° |  |  |  |  |  |  |  |
|----|----------|------|----------|----|----------|------|-----------|------|--|--|--|--|--|--|--|
| /  | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | /    |  |  |  |  |  |  |  |
| 0  | 8.718800 | 4006 | 9.999404 | 11 | 8.719396 | 4017 | 11.280604 | 60   |  |  |  |  |  |  |  |
| 1  | 721204   | 3984 | 999398   | 11 | 721806   | 3995 | 278194    | 59   |  |  |  |  |  |  |  |
| 2  | 723595   | 3962 | 999391   | 11 | 724204   | 3974 | 275796    | 58   |  |  |  |  |  |  |  |
| 3  | 725972   | 3941 | 999384   | 11 | 726588   | 3952 | 273412    | 57   |  |  |  |  |  |  |  |
| 4  | 728337   | 3919 | 999378   | 11 | 728959   | 3930 | 271041    | 56   |  |  |  |  |  |  |  |
| 5  | 730688   | 3898 | 999371   | 11 | 731317   | 3909 | 268683    | 55   |  |  |  |  |  |  |  |
| 6  | 733027   | 3877 | 999364   | 12 | 733663   | 3889 | 266337    | 54   |  |  |  |  |  |  |  |
| 7  | 735354   | 3857 | 999357   | 12 | 735996   | 3868 | 264004    | 53   |  |  |  |  |  |  |  |
| 8  | 737667   | 3836 | 999350   | 12 | 738317   | 3848 | 261683    | 52   |  |  |  |  |  |  |  |
| 9  | 739969   | 3816 | 999343   | 12 | 740626   | 3827 | 259374    | 51   |  |  |  |  |  |  |  |
| 10 | 742259   | 3796 | 999336   | 12 | 742922   | 3807 | 257078    | 50   |  |  |  |  |  |  |  |
| 11 | 8.744536 | 3776 | 9.999329 | 12 | 8.745207 | 3787 | 11.252793 | 49   |  |  |  |  |  |  |  |
| 12 | 746802   | 3756 | 999322   | 12 | 747479   | 3768 | 252321    | 48   |  |  |  |  |  |  |  |
| 13 | 749055   | 3737 | 999315   | 12 | 749740   | 3749 | 250260    | 47   |  |  |  |  |  |  |  |
| 14 | 751297   | 3717 | 999308   | 12 | 751989   | 3729 | 248011    | 46   |  |  |  |  |  |  |  |
| 15 | 753528   | 3698 | 999301   | 12 | 754227   | 3710 | 245773    | 45   |  |  |  |  |  |  |  |
| 16 | 755747   | 3679 | 999294   | 12 | 756453   | 3692 | 243547    | 44   |  |  |  |  |  |  |  |
| 17 | 757955   | 3661 | 999287   | 12 | 758668   | 3673 | 241332    | 43   |  |  |  |  |  |  |  |
| 18 | 760151   | 3642 | 999279   | 12 | 760872   | 3655 | 239128    | 42   |  |  |  |  |  |  |  |
| 19 | 762337   | 3624 | 999272   | 12 | 763065   | 3636 | 236935    | 41   |  |  |  |  |  |  |  |
| 20 | 764511   | 3606 | 999265   | 12 | 765246   | 3618 | 234754    | 40   |  |  |  |  |  |  |  |
| 21 | 8.766675 | 3588 | 9.999257 | 12 | 8.767417 | 3600 | 11.252583 | 39   |  |  |  |  |  |  |  |
| 22 | 768828   | 3570 | 999250   | 13 | 769578   | 3583 | 230422    | 38   |  |  |  |  |  |  |  |
| 23 | 770970   | 3553 | 999242   | 13 | 771727   | 3565 | 228273    | 37   |  |  |  |  |  |  |  |
| 24 | 773101   | 3535 | 999235   | 13 | 773866   | 3548 | 226134    | 36   |  |  |  |  |  |  |  |
| 25 | 775223   | 3518 | 999227   | 13 | 775995   | 3531 | 224005    | 35   |  |  |  |  |  |  |  |
| 26 | 777333   | 3501 | 999220   | 13 | 778114   | 3514 | 221886    | 34   |  |  |  |  |  |  |  |
| 27 | 779434   | 3484 | 999212   | 13 | 780222   | 3497 | 219778    | 33   |  |  |  |  |  |  |  |
| 28 | 781524   | 3467 | 999205   | 13 | 782320   | 3480 | 217680    | 32   |  |  |  |  |  |  |  |
| 29 | 783605   | 3451 | 999197   | 13 | 784408   | 3464 | 215592    | 31   |  |  |  |  |  |  |  |
| 30 | 785675   | 3431 | 999189   | 13 | 786486   | 3447 | 213514    | 30   |  |  |  |  |  |  |  |
| 31 | 8.787736 | 3418 | 9.999181 | 13 | 8.788554 | 3431 | 11.211446 | 29   |  |  |  |  |  |  |  |
| 32 | 789787   | 3402 | 999174   | 13 | 790613   | 3414 | 209387    | 28   |  |  |  |  |  |  |  |
| 33 | 791828   | 3386 | 999166   | 13 | 792662   | 3399 | 207338    | 27   |  |  |  |  |  |  |  |
| 34 | 793859   | 3370 | 999158   | 13 | 794701   | 3383 | 205299    | 26   |  |  |  |  |  |  |  |
| 35 | 795881   | 3354 | 999150   | 13 | 796731   | 3368 | 203269    | 25   |  |  |  |  |  |  |  |
| 36 | 797894   | 3339 | 999142   | 13 | 798752   | 3352 | 201248    | 24   |  |  |  |  |  |  |  |
| 37 | 799897   | 3323 | 999134   | 13 | 800763   | 3337 | 199237    | 23   |  |  |  |  |  |  |  |
| 38 | 801892   | 3308 | 999126   | 13 | 802765   | 3322 | 197235    | 22   |  |  |  |  |  |  |  |
| 39 | 803876   | 3293 | 999118   | 13 | 804758   | 3307 | 195242    | 21   |  |  |  |  |  |  |  |
| 40 | 805852   | 3278 | 999110   | 13 | 806742   | 3292 | 193258    | 20   |  |  |  |  |  |  |  |
| 41 | 8.807819 | 3263 | 9.999102 | 13 | 8.808717 | 3278 | 11.191283 | 19   |  |  |  |  |  |  |  |
| 42 | 809777   | 3249 | 999094   | 14 | 810683   | 3262 | 189317    | 18   |  |  |  |  |  |  |  |
| 43 | 811726   | 3234 | 999086   | 14 | 812641   | 3248 | 187359    | 17   |  |  |  |  |  |  |  |
| 44 | 813667   | 3219 | 999077   | 14 | 814589   | 3233 | 185411    | 16   |  |  |  |  |  |  |  |
| 45 | 815599   | 3205 | 999069   | 14 | 816529   | 3219 | 183471    | 15   |  |  |  |  |  |  |  |
| 46 | 817522   | 3191 | 999061   | 14 | 818461   | 3205 | 181539    | 14   |  |  |  |  |  |  |  |
| 47 | 819436   | 3177 | 999053   | 14 | 820384   | 3191 | 179616    | 13   |  |  |  |  |  |  |  |
| 48 | 821343   | 3163 | 999044   | 14 | 822298   | 3177 | 177702    | 12   |  |  |  |  |  |  |  |
| 49 | 823240   | 3149 | 999036   | 14 | 824205   | 3163 | 175795    | 11   |  |  |  |  |  |  |  |
| 50 | 825130   | 3135 | 999027   | 14 | 826103   | 3150 | 173897    | 10   |  |  |  |  |  |  |  |
| 51 | 8.827011 | 3122 | 9.999019 | 14 | 8.827992 | 3136 | 11.172008 | 9    |  |  |  |  |  |  |  |
| 52 | 828884   | 3108 | 999010   | 14 | 829874   | 3123 | 170126    | 8    |  |  |  |  |  |  |  |
| 53 | 830749   | 3095 | 999002   | 14 | 831748   | 3110 | 168252    | 7    |  |  |  |  |  |  |  |
| 54 | 832607   | 3082 | 998993   | 14 | 833613   | 3096 | 166387    | 6    |  |  |  |  |  |  |  |
| 55 | 834456   | 3069 | 998984   | 14 | 835471   | 3083 | 164529    | 5    |  |  |  |  |  |  |  |
| 56 | 836297   | 3056 | 998976   | 14 | 837321   | 3070 | 162679    | 4    |  |  |  |  |  |  |  |
| 57 | 838130   | 3043 | 998967   | 15 | 839163   | 3057 | 160837    | 3    |  |  |  |  |  |  |  |
| 58 | 839956   | 3030 | 998958   | 15 | 840998   | 3045 | 159002    | 2    |  |  |  |  |  |  |  |
| 59 | 841774   | 3017 | 998950   | 15 | 842825   | 3032 | 157175    | 1    |  |  |  |  |  |  |  |
| 60 | 843585   | 3000 | 998941   | 15 | 844644   | 3019 | 155356    | 0    |  |  |  |  |  |  |  |
| /  | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | /    |  |  |  |  |  |  |  |

98°

86°

4°

175°

| /  | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | /  |
|----|----------|------|----------|----|----------|------|-----------|----|
| 0  | 8.843585 | 3005 | 9.998941 | 15 | 8.844644 | 3019 | 11.155356 | 60 |
| 1  | 845387   | 2992 | 998932   | 15 | 846455   | 3007 | 153545    | 59 |
| 2  | 847183   | 2980 | 998923   | 15 | 848260   | 2995 | 151740    | 58 |
| 3  | 848971   | 2967 | 998914   | 15 | 850057   | 2982 | 149943    | 57 |
| 4  | 850751   | 2955 | 998905   | 15 | 851846   | 2970 | 148154    | 56 |
| 5  | 852525   | 2943 | 998896   | 15 | 853628   | 2958 | 146372    | 55 |
| 6  | 854291   | 2931 | 998887   | 15 | 855403   | 2946 | 144597    | 54 |
| 7  | 856049   | 2919 | 998878   | 15 | 857171   | 2935 | 142829    | 53 |
| 8  | 857801   | 2907 | 998869   | 15 | 858932   | 2923 | 141068    | 52 |
| 9  | 859546   | 2896 | 998860   | 15 | 860686   | 2911 | 139314    | 51 |
| 10 | 861283   | 2884 | 998851   | 15 | 862433   | 2900 | 137567    | 50 |
| 11 | 8.863014 | 2873 | 9.998841 | 15 | 8.864173 | 2888 | 11.135827 | 49 |
| 12 | 864738   | 2861 | 998832   | 15 | 865906   | 2877 | 134094    | 48 |
| 13 | 866455   | 2850 | 998823   | 16 | 867632   | 2866 | 132368    | 47 |
| 14 | 868165   | 2839 | 998813   | 16 | 869351   | 2854 | 130649    | 46 |
| 15 | 869868   | 2828 | 998804   | 16 | 871064   | 2843 | 128936    | 45 |
| 16 | 871565   | 2817 | 998795   | 16 | 872770   | 2832 | 127230    | 44 |
| 17 | 873255   | 2806 | 998785   | 16 | 874469   | 2821 | 125531    | 43 |
| 18 | 874938   | 2795 | 998776   | 16 | 876162   | 2811 | 123838    | 42 |
| 19 | 876615   | 2786 | 998766   | 16 | 877849   | 2800 | 122151    | 41 |
| 20 | 878285   | 2773 | 998757   | 16 | 879529   | 2789 | 120471    | 40 |
| 21 | 8.879949 | 2763 | 9.998747 | 16 | 8.881202 | 2779 | 11.118798 | 39 |
| 22 | 881607   | 2752 | 998738   | 16 | 882869   | 2768 | 117131    | 38 |
| 23 | 883258   | 2742 | 998728   | 16 | 884530   | 2758 | 115470    | 37 |
| 24 | 884903   | 2731 | 998718   | 16 | 886185   | 2747 | 113816    | 36 |
| 25 | 886542   | 2721 | 998708   | 16 | 887833   | 2737 | 112167    | 35 |
| 26 | 888174   | 2711 | 998699   | 16 | 889476   | 2727 | 110524    | 34 |
| 27 | 889801   | 2700 | 998689   | 16 | 891112   | 2717 | 108888    | 33 |
| 28 | 891421   | 2690 | 998679   | 16 | 892742   | 2707 | 107258    | 32 |
| 29 | 893035   | 2680 | 998669   | 17 | 894366   | 2697 | 105634    | 31 |
| 30 | 894643   | 2670 | 998659   | 17 | 895984   | 2687 | 104016    | 30 |
| 31 | 8.896246 | 2660 | 9.998649 | 17 | 8.897596 | 2677 | 11.102404 | 29 |
| 32 | 897842   | 2651 | 998639   | 17 | 899203   | 2667 | 100797    | 28 |
| 33 | 899432   | 2641 | 998629   | 17 | 900803   | 2658 | 999197    | 27 |
| 34 | 901017   | 2631 | 998619   | 17 | 902398   | 2648 | 997602    | 26 |
| 35 | 902596   | 2622 | 998609   | 17 | 903987   | 2638 | 996013    | 25 |
| 36 | 904169   | 2612 | 998599   | 17 | 905570   | 2629 | 994430    | 24 |
| 37 | 905736   | 2603 | 998589   | 17 | 907147   | 2620 | 992853    | 23 |
| 38 | 907297   | 2593 | 998578   | 17 | 908719   | 2610 | 991281    | 22 |
| 39 | 908853   | 2584 | 998568   | 17 | 910285   | 2601 | 989715    | 21 |
| 40 | 910404   | 2575 | 998558   | 17 | 911846   | 2592 | 988154    | 20 |
| 41 | 8.911949 | 2566 | 9.998548 | 17 | 8.913401 | 2583 | 11.086599 | 19 |
| 42 | 913488   | 2556 | 998537   | 17 | 914951   | 2574 | 985649    | 18 |
| 43 | 915022   | 2547 | 998527   | 17 | 916495   | 2565 | 983505    | 17 |
| 44 | 916550   | 2538 | 998516   | 18 | 918034   | 2556 | 981966    | 16 |
| 45 | 918073   | 2529 | 998506   | 18 | 919568   | 2547 | 980432    | 15 |
| 46 | 919591   | 2520 | 998495   | 18 | 921096   | 2538 | 978904    | 14 |
| 47 | 921103   | 2512 | 998485   | 18 | 922619   | 2530 | 977381    | 13 |
| 48 | 922610   | 2503 | 998474   | 18 | 924136   | 2521 | 975864    | 12 |
| 49 | 924112   | 2494 | 998464   | 18 | 925649   | 2512 | 974351    | 11 |
| 50 | 925609   | 2486 | 998453   | 18 | 927156   | 2503 | 972844    | 10 |
| 51 | 8.927100 | 2477 | 9.998442 | 18 | 8.928658 | 2495 | 11.071342 | 9  |
| 52 | 928587   | 2469 | 998431   | 18 | 930155   | 2486 | 969845    | 8  |
| 53 | 930068   | 2460 | 998421   | 18 | 931647   | 2478 | 968353    | 7  |
| 54 | 931544   | 2452 | 998410   | 18 | 933134   | 2470 | 966866    | 6  |
| 55 | 933015   | 2443 | 998399   | 18 | 934616   | 2461 | 965384    | 5  |
| 56 | 934481   | 2435 | 998388   | 18 | 936093   | 2453 | 963907    | 4  |
| 57 | 935942   | 2427 | 998377   | 18 | 937565   | 2445 | 962435    | 3  |
| 58 | 937398   | 2419 | 998366   | 18 | 939032   | 2437 | 960968    | 2  |
| 59 | 938850   | 2411 | 998355   | 18 | 940494   | 2430 | 959506    | 1  |
| 60 | 940296   | 2403 | 998344   | 18 | 941952   | 2421 | 958048    | 0  |
| /  | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | /  |

94°

85°

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 8° |          |      |          |    |          |      |           | 174° |  |  |  |  |  |  |   |
|----|----------|------|----------|----|----------|------|-----------|------|--|--|--|--|--|--|---|
| /  | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | /    |  |  |  |  |  |  | / |
| 0  | 8.940296 | 2403 | 9.998344 | 19 | 8.941952 | 2421 | 11.058048 | 60   |  |  |  |  |  |  |   |
| 1  | 941738   | 2394 | 998333   | 19 | 943404   | 2413 | 056596    | 59   |  |  |  |  |  |  |   |
| 2  | 943174   | 2387 | 998322   | 19 | 944852   | 2405 | 055148    | 58   |  |  |  |  |  |  |   |
| 3  | 944606   | 2379 | 998311   | 19 | 946295   | 2397 | 053705    | 57   |  |  |  |  |  |  |   |
| 4  | 946034   | 2371 | 998300   | 19 | 947734   | 2390 | 052266    | 56   |  |  |  |  |  |  |   |
| 5  | 947456   | 2363 | 998289   | 19 | 949168   | 2382 | 050832    | 55   |  |  |  |  |  |  |   |
| 6  | 948874   | 2355 | 998277   | 19 | 950597   | 2374 | 049403    | 54   |  |  |  |  |  |  |   |
| 7  | 950287   | 2348 | 998266   | 19 | 952021   | 2366 | 047979    | 53   |  |  |  |  |  |  |   |
| 8  | 951696   | 2340 | 998255   | 19 | 953441   | 2360 | 046559    | 52   |  |  |  |  |  |  |   |
| 9  | 953100   | 2332 | 998243   | 19 | 954856   | 2351 | 045144    | 51   |  |  |  |  |  |  |   |
| 10 | 954499   | 2325 | 998232   | 19 | 956267   | 2344 | 043733    | 50   |  |  |  |  |  |  |   |
| 11 | 8.955804 | 2317 | 9.998220 | 19 | 8.957674 | 2337 | 11.042326 | 49   |  |  |  |  |  |  |   |
| 12 | 957284   | 2310 | 998209   | 19 | 959075   | 2329 | 040925    | 48   |  |  |  |  |  |  |   |
| 13 | 958670   | 2302 | 998197   | 19 | 960473   | 2323 | 039527    | 47   |  |  |  |  |  |  |   |
| 14 | 960052   | 2295 | 998186   | 19 | 961866   | 2314 | 038134    | 46   |  |  |  |  |  |  |   |
| 15 | 961429   | 2288 | 998174   | 19 | 963255   | 2307 | 036745    | 45   |  |  |  |  |  |  |   |
| 16 | 962801   | 2280 | 998163   | 19 | 964639   | 2300 | 035361    | 44   |  |  |  |  |  |  |   |
| 17 | 964170   | 2273 | 998151   | 19 | 966019   | 2293 | 033981    | 43   |  |  |  |  |  |  |   |
| 18 | 965534   | 2266 | 998139   | 20 | 967394   | 2286 | 032606    | 42   |  |  |  |  |  |  |   |
| 19 | 966893   | 2259 | 998128   | 20 | 968766   | 2279 | 031234    | 41   |  |  |  |  |  |  |   |
| 20 | 968249   | 2252 | 998116   | 20 | 970133   | 2271 | 029867    | 40   |  |  |  |  |  |  |   |
| 21 | 8.969600 | 2244 | 9.998104 | 20 | 8.971496 | 2265 | 11.028504 | 39   |  |  |  |  |  |  |   |
| 22 | 970947   | 2238 | 998092   | 20 | 972855   | 2257 | 027145    | 38   |  |  |  |  |  |  |   |
| 23 | 972289   | 2231 | 998080   | 20 | 974209   | 2251 | 025791    | 37   |  |  |  |  |  |  |   |
| 24 | 973628   | 2224 | 998068   | 20 | 975560   | 2244 | 024440    | 36   |  |  |  |  |  |  |   |
| 25 | 974962   | 2217 | 998056   | 20 | 976906   | 2237 | 023094    | 35   |  |  |  |  |  |  |   |
| 26 | 976293   | 2210 | 998044   | 20 | 978248   | 2230 | 021752    | 34   |  |  |  |  |  |  |   |
| 27 | 977619   | 2203 | 998032   | 20 | 979586   | 2223 | 020414    | 33   |  |  |  |  |  |  |   |
| 28 | 978941   | 2197 | 998020   | 20 | 980921   | 2217 | 019079    | 32   |  |  |  |  |  |  |   |
| 29 | 980259   | 2190 | 998008   | 20 | 982251   | 2210 | 017749    | 31   |  |  |  |  |  |  |   |
| 30 | 981573   | 2183 | 997996   | 20 | 983577   | 2204 | 016423    | 30   |  |  |  |  |  |  |   |
| 31 | 8.982883 | 2177 | 9.997984 | 20 | 8.984899 | 2197 | 11.015101 | 29   |  |  |  |  |  |  |   |
| 32 | 984189   | 2170 | 997972   | 20 | 986217   | 2191 | 013783    | 28   |  |  |  |  |  |  |   |
| 33 | 985491   | 2163 | 997959   | 20 | 987532   | 2184 | 012468    | 27   |  |  |  |  |  |  |   |
| 34 | 986789   | 2157 | 997947   | 20 | 988842   | 2178 | 011158    | 26   |  |  |  |  |  |  |   |
| 35 | 988083   | 2150 | 997935   | 21 | 990149   | 2171 | 009851    | 25   |  |  |  |  |  |  |   |
| 36 | 989374   | 2144 | 997922   | 21 | 991451   | 2165 | 008549    | 24   |  |  |  |  |  |  |   |
| 37 | 990660   | 2138 | 997910   | 21 | 992750   | 2158 | 007250    | 23   |  |  |  |  |  |  |   |
| 38 | 991943   | 2131 | 997897   | 21 | 994045   | 2152 | 005955    | 22   |  |  |  |  |  |  |   |
| 39 | 993222   | 2125 | 997885   | 21 | 995337   | 2146 | 004663    | 21   |  |  |  |  |  |  |   |
| 40 | 994497   | 2119 | 997872   | 21 | 996624   | 2140 | 003376    | 20   |  |  |  |  |  |  |   |
| 41 | 8.995768 | 2112 | 9.997860 | 21 | 8.997908 | 2134 | 11.002092 | 19   |  |  |  |  |  |  |   |
| 42 | 997036   | 2106 | 997847   | 21 | 999188   | 2127 | 000812    | 18   |  |  |  |  |  |  |   |
| 43 | 998299   | 2100 | 997835   | 21 | 9.000464 | 2121 | 10.999535 | 17   |  |  |  |  |  |  |   |
| 44 | 999560   | 2094 | 997822   | 21 | 001738   | 2115 | 998262    | 16   |  |  |  |  |  |  |   |
| 45 | 9.000816 | 2087 | 997809   | 21 | 003007   | 2109 | 996993    | 15   |  |  |  |  |  |  |   |
| 46 | 002069   | 2082 | 997797   | 21 | 004272   | 2103 | 995728    | 14   |  |  |  |  |  |  |   |
| 47 | 003318   | 2076 | 997784   | 21 | 005534   | 2097 | 994466    | 13   |  |  |  |  |  |  |   |
| 48 | 004563   | 2070 | 997771   | 21 | 006792   | 2091 | 993208    | 12   |  |  |  |  |  |  |   |
| 49 | 005805   | 2064 | 997758   | 21 | 008047   | 2085 | 991953    | 11   |  |  |  |  |  |  |   |
| 50 | 007044   | 2058 | 997745   | 21 | 009298   | 2080 | 990702    | 10   |  |  |  |  |  |  |   |
| 51 | 9.008278 | 2052 | 9.997732 | 21 | 9.010546 | 2074 | 10.989454 | 9    |  |  |  |  |  |  |   |
| 52 | 009510   | 2046 | 997719   | 21 | 011790   | 2068 | 988210    | 8    |  |  |  |  |  |  |   |
| 53 | 010737   | 2040 | 997706   | 21 | 013031   | 2062 | 986969    | 7    |  |  |  |  |  |  |   |
| 54 | 011962   | 2034 | 997693   | 22 | 014268   | 2056 | 985732    | 6    |  |  |  |  |  |  |   |
| 55 | 013182   | 2029 | 997680   | 22 | 015502   | 2051 | 984498    | 5    |  |  |  |  |  |  |   |
| 56 | 014400   | 2023 | 997667   | 22 | 016732   | 2045 | 983268    | 4    |  |  |  |  |  |  |   |
| 57 | 015613   | 2017 | 997654   | 22 | 017959   | 2040 | 982041    | 3    |  |  |  |  |  |  |   |
| 58 | 016824   | 2012 | 997641   | 22 | 019183   | 2033 | 980817    | 2    |  |  |  |  |  |  |   |
| 59 | 018031   | 2006 | 997628   | 22 | 020403   | 2028 | 979597    | 1    |  |  |  |  |  |  |   |
| 60 | 019235   | 2000 | 997614   | 22 | 021620   | 2023 | 978380    | 0    |  |  |  |  |  |  |   |
| /  | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | /    |  |  |  |  |  |  | / |

95°

84°

| 8° |          |      |          |    |          |      |           | 173° |  |  |  |  |  |  |  |
|----|----------|------|----------|----|----------|------|-----------|------|--|--|--|--|--|--|--|
| /  | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | /    |  |  |  |  |  |  |  |
| 0  | 9.019235 | 2000 | 9.997614 | 22 | 9.021620 | 2023 | 10.978380 | 60   |  |  |  |  |  |  |  |
| 1  | 020435   | 1995 | 997601   | 22 | 022834   | 2017 | 977166    | 59   |  |  |  |  |  |  |  |
| 2  | 021632   | 1989 | 997588   | 22 | 024044   | 2011 | 975956    | 58   |  |  |  |  |  |  |  |
| 3  | 022825   | 1984 | 997574   | 22 | 025251   | 2006 | 974749    | 57   |  |  |  |  |  |  |  |
| 4  | 024016   | 1978 | 997561   | 22 | 026455   | 2000 | 973545    | 56   |  |  |  |  |  |  |  |
| 5  | 025203   | 1973 | 997547   | 22 | 027655   | 1995 | 972345    | 55   |  |  |  |  |  |  |  |
| 6  | 026386   | 1967 | 997534   | 23 | 028852   | 1990 | 971148    | 54   |  |  |  |  |  |  |  |
| 7  | 027567   | 1962 | 997520   | 23 | 030046   | 1985 | 969954    | 53   |  |  |  |  |  |  |  |
| 8  | 028744   | 1957 | 997507   | 23 | 031237   | 1979 | 968763    | 52   |  |  |  |  |  |  |  |
| 9  | 029918   | 1951 | 997493   | 23 | 032425   | 1974 | 967575    | 51   |  |  |  |  |  |  |  |
| 10 | 031089   | 1947 | 997480   | 23 | 033609   | 1969 | 966391    | 50   |  |  |  |  |  |  |  |
| 11 | 9.032257 | 1941 | 9.997466 | 23 | 9.034791 | 1964 | 10.965209 | 49   |  |  |  |  |  |  |  |
| 12 | 033421   | 1936 | 997452   | 23 | 035969   | 1958 | 964031    | 48   |  |  |  |  |  |  |  |
| 13 | 034582   | 1930 | 997439   | 23 | 037144   | 1953 | 962856    | 47   |  |  |  |  |  |  |  |
| 14 | 035741   | 1925 | 997425   | 23 | 038316   | 1948 | 961684    | 46   |  |  |  |  |  |  |  |
| 15 | 036866   | 1920 | 997411   | 23 | 039485   | 1943 | 960515    | 45   |  |  |  |  |  |  |  |
| 16 | 038048   | 1915 | 997397   | 23 | 040651   | 1938 | 959349    | 44   |  |  |  |  |  |  |  |
| 17 | 039197   | 1910 | 997383   | 23 | 041813   | 1933 | 958187    | 43   |  |  |  |  |  |  |  |
| 18 | 040342   | 1905 | 997369   | 23 | 042973   | 1928 | 957027    | 42   |  |  |  |  |  |  |  |
| 19 | 041485   | 1899 | 997355   | 23 | 044130   | 1923 | 955870    | 41   |  |  |  |  |  |  |  |
| 20 | 042625   | 1894 | 997341   | 23 | 045284   | 1918 | 954716    | 40   |  |  |  |  |  |  |  |
| 21 | 9.043762 | 1889 | 9.997327 | 24 | 9.046434 | 1913 | 10.953566 | 39   |  |  |  |  |  |  |  |
| 22 | 044895   | 1884 | 997313   | 24 | 047582   | 1908 | 952418    | 38   |  |  |  |  |  |  |  |
| 23 | 046026   | 1879 | 997299   | 24 | 048727   | 1903 | 951273    | 37   |  |  |  |  |  |  |  |
| 24 | 047154   | 1875 | 997285   | 24 | 049869   | 1898 | 950131    | 36   |  |  |  |  |  |  |  |
| 25 | 048279   | 1870 | 997271   | 24 | 051008   | 1893 | 948992    | 35   |  |  |  |  |  |  |  |
| 26 | 049400   | 1865 | 997257   | 24 | 052144   | 1889 | 947856    | 34   |  |  |  |  |  |  |  |
| 27 | 050519   | 1860 | 997242   | 24 | 053277   | 1884 | 946723    | 33   |  |  |  |  |  |  |  |
| 28 | 051635   | 1855 | 997228   | 24 | 054407   | 1879 | 945593    | 32   |  |  |  |  |  |  |  |
| 29 | 052749   | 1850 | 997214   | 24 | 055535   | 1874 | 944465    | 31   |  |  |  |  |  |  |  |
| 30 | 053859   | 1845 | 997199   | 24 | 056659   | 1870 | 943341    | 30   |  |  |  |  |  |  |  |
| 31 | 9.054966 | 1841 | 9.997185 | 24 | 9.057781 | 1865 | 10.942219 | 29   |  |  |  |  |  |  |  |
| 32 | 056071   | 1836 | 997170   | 24 | 058900   | 1860 | 941100    | 28   |  |  |  |  |  |  |  |
| 33 | 057172   | 1831 | 997156   | 24 | 060016   | 1855 | 939984    | 27   |  |  |  |  |  |  |  |
| 34 | 058271   | 1827 | 997141   | 24 | 061130   | 1851 | 938870    | 26   |  |  |  |  |  |  |  |
| 35 | 059367   | 1822 | 997127   | 24 | 062240   | 1846 | 937760    | 25   |  |  |  |  |  |  |  |
| 36 | 060460   | 1817 | 997112   | 24 | 063348   | 1842 | 936652    | 24   |  |  |  |  |  |  |  |
| 37 | 061551   | 1813 | 997098   | 24 | 064453   | 1837 | 935547    | 23   |  |  |  |  |  |  |  |
| 38 | 062639   | 1808 | 997083   | 25 | 065556   | 1833 | 934444    | 22   |  |  |  |  |  |  |  |
| 39 | 063724   | 1804 | 997068   | 25 | 066655   | 1828 | 933345    | 21   |  |  |  |  |  |  |  |
| 40 | 064806   | 1799 | 997053   | 25 | 067752   | 1824 | 932248    | 20   |  |  |  |  |  |  |  |
| 41 | 9.065885 | 1794 | 9.997039 | 25 | 9.068846 | 1819 | 10.931154 | 19   |  |  |  |  |  |  |  |
| 42 | 066962   | 1790 | 997024   | 25 | 069938   | 1815 | 930062    | 18   |  |  |  |  |  |  |  |
| 43 | 068036   | 1786 | 997009   | 25 | 071027   | 1810 | 928973    | 17   |  |  |  |  |  |  |  |
| 44 | 069107   | 1781 | 996994   | 25 | 072113   | 1806 | 927887    | 16   |  |  |  |  |  |  |  |
| 45 | 070176   | 1777 | 996979   | 25 | 073197   | 1802 | 926803    | 15   |  |  |  |  |  |  |  |
| 46 | 071242   | 1772 | 996964   | 25 | 074278   | 1797 | 925722    | 14   |  |  |  |  |  |  |  |
| 47 | 072306   | 1768 | 996949   | 25 | 075356   | 1793 | 924644    | 13   |  |  |  |  |  |  |  |
| 48 | 073366   | 1763 | 996934   | 25 | 076432   | 1789 | 923568    | 12   |  |  |  |  |  |  |  |
| 49 | 074424   | 1759 | 996919   | 25 | 077505   | 1784 | 922495    | 11   |  |  |  |  |  |  |  |
| 50 | 075480   | 1755 | 996904   | 25 | 078576   | 1780 | 921424    | 10   |  |  |  |  |  |  |  |
| 51 | 9.076533 | 1750 | 9.996889 | 25 | 9.079644 | 1776 | 10.920356 | 9    |  |  |  |  |  |  |  |
| 52 | 077583   | 1746 | 996874   | 25 | 080710   | 1772 | 919290    | 8    |  |  |  |  |  |  |  |
| 53 | 078631   | 1742 | 996858   | 25 | 081773   | 1767 | 918227    | 7    |  |  |  |  |  |  |  |
| 54 | 079676   | 1738 | 996843   | 25 | 082833   | 1763 | 917167    | 6    |  |  |  |  |  |  |  |
| 55 | 080719   | 1733 | 996828   | 25 | 083891   | 1759 | 916109    | 5    |  |  |  |  |  |  |  |
| 56 | 081759   | 1729 | 996812   | 26 | 084947   | 1755 | 915053    | 4    |  |  |  |  |  |  |  |
| 57 | 082797   | 1725 | 996797   | 26 | 086000   | 1751 | 914000    | 3    |  |  |  |  |  |  |  |
| 58 | 083832   | 1721 | 996782   | 26 | 087050   | 1747 | 912950    | 2    |  |  |  |  |  |  |  |
| 59 | 084864   | 1717 | 996766   | 26 | 088098   | 1743 | 911902    | 1    |  |  |  |  |  |  |  |
| 60 | 085894   | 1713 | 996751   | 26 | 089144   | 1738 | 910856    | 0    |  |  |  |  |  |  |  |
| /  | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | /    |  |  |  |  |  |  |  |



TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

25

| 70 |          |      |          |    |          |      |           |    |  | 172° |  |    |         |    |  |   |  |  |  |
|----|----------|------|----------|----|----------|------|-----------|----|--|------|--|----|---------|----|--|---|--|--|--|
| /  | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | /  |  | /    |  | D. | Cotang. | D. |  | / |  |  |  |
| 0  | 9.085894 | 1713 | 9.996751 | 26 | 9.089144 | 1738 | 10.910856 | 60 |  |      |  |    |         |    |  |   |  |  |  |
| 1  | 086922   | 1709 | 996735   | 26 | 090187   | 1734 | 909813    | 59 |  |      |  |    |         |    |  |   |  |  |  |
| 2  | 087947   | 1704 | 996720   | 26 | 091228   | 1730 | 908772    | 58 |  |      |  |    |         |    |  |   |  |  |  |
| 3  | 088970   | 1700 | 996704   | 26 | 092266   | 1727 | 907734    | 57 |  |      |  |    |         |    |  |   |  |  |  |
| 4  | 089990   | 1696 | 996688   | 26 | 093302   | 1722 | 906698    | 56 |  |      |  |    |         |    |  |   |  |  |  |
| 5  | 091008   | 1692 | 996673   | 26 | 094336   | 1719 | 905664    | 55 |  |      |  |    |         |    |  |   |  |  |  |
| 6  | 092024   | 1688 | 996657   | 26 | 095367   | 1715 | 904633    | 54 |  |      |  |    |         |    |  |   |  |  |  |
| 7  | 093037   | 1684 | 996641   | 26 | 096395   | 1711 | 903605    | 53 |  |      |  |    |         |    |  |   |  |  |  |
| 8  | 094047   | 1680 | 996625   | 26 | 097422   | 1707 | 902578    | 52 |  |      |  |    |         |    |  |   |  |  |  |
| 9  | 095056   | 1676 | 996610   | 26 | 098446   | 1703 | 901554    | 51 |  |      |  |    |         |    |  |   |  |  |  |
| 10 | 096062   | 1673 | 996594   | 26 | 099468   | 1699 | 900532    | 50 |  |      |  |    |         |    |  |   |  |  |  |
| 11 | 9.097065 | 1668 | 9.996578 | 27 | 9.100487 | 1695 | 10.899513 | 49 |  |      |  |    |         |    |  |   |  |  |  |
| 12 | 098066   | 1665 | 996562   | 27 | 101504   | 1691 | 898496    | 48 |  |      |  |    |         |    |  |   |  |  |  |
| 13 | 099065   | 1661 | 996546   | 27 | 102519   | 1687 | 897481    | 47 |  |      |  |    |         |    |  |   |  |  |  |
| 14 | 100062   | 1657 | 996530   | 27 | 103532   | 1684 | 896468    | 46 |  |      |  |    |         |    |  |   |  |  |  |
| 15 | 101056   | 1653 | 996514   | 27 | 104542   | 1680 | 895454    | 45 |  |      |  |    |         |    |  |   |  |  |  |
| 16 | 102048   | 1649 | 996498   | 27 | 105550   | 1676 | 894450    | 44 |  |      |  |    |         |    |  |   |  |  |  |
| 17 | 103037   | 1645 | 996482   | 27 | 106556   | 1672 | 893444    | 43 |  |      |  |    |         |    |  |   |  |  |  |
| 18 | 104025   | 1641 | 996465   | 27 | 107559   | 1669 | 892441    | 42 |  |      |  |    |         |    |  |   |  |  |  |
| 19 | 105010   | 1638 | 996449   | 27 | 108560   | 1665 | 891440    | 41 |  |      |  |    |         |    |  |   |  |  |  |
| 20 | 105992   | 1634 | 996433   | 27 | 109559   | 1661 | 890441    | 40 |  |      |  |    |         |    |  |   |  |  |  |
| 21 | 9.106973 | 1630 | 9.996417 | 27 | 9.110556 | 1658 | 10.889444 | 39 |  |      |  |    |         |    |  |   |  |  |  |
| 22 | 107951   | 1627 | 996400   | 27 | 111551   | 1654 | 888449    | 38 |  |      |  |    |         |    |  |   |  |  |  |
| 23 | 108927   | 1623 | 996384   | 27 | 112543   | 1650 | 887457    | 37 |  |      |  |    |         |    |  |   |  |  |  |
| 24 | 109901   | 1619 | 996368   | 27 | 113533   | 1646 | 886467    | 36 |  |      |  |    |         |    |  |   |  |  |  |
| 25 | 110873   | 1616 | 996351   | 27 | 114521   | 1643 | 885479    | 35 |  |      |  |    |         |    |  |   |  |  |  |
| 26 | 111842   | 1612 | 996335   | 27 | 115507   | 1639 | 884493    | 34 |  |      |  |    |         |    |  |   |  |  |  |
| 27 | 112809   | 1608 | 996318   | 27 | 116491   | 1636 | 883509    | 33 |  |      |  |    |         |    |  |   |  |  |  |
| 28 | 113774   | 1605 | 996302   | 28 | 117472   | 1632 | 882528    | 32 |  |      |  |    |         |    |  |   |  |  |  |
| 29 | 114737   | 1601 | 996285   | 28 | 118452   | 1629 | 881548    | 31 |  |      |  |    |         |    |  |   |  |  |  |
| 30 | 115698   | 1597 | 996269   | 28 | 119429   | 1625 | 880571    | 30 |  |      |  |    |         |    |  |   |  |  |  |
| 31 | 9.116656 | 1594 | 9.996252 | 28 | 9.120404 | 1622 | 10.879596 | 29 |  |      |  |    |         |    |  |   |  |  |  |
| 32 | 117613   | 1590 | 996235   | 28 | 121377   | 1618 | 878623    | 28 |  |      |  |    |         |    |  |   |  |  |  |
| 33 | 118567   | 1587 | 996219   | 28 | 122348   | 1615 | 877652    | 27 |  |      |  |    |         |    |  |   |  |  |  |
| 34 | 119519   | 1583 | 996202   | 28 | 123317   | 1611 | 876683    | 26 |  |      |  |    |         |    |  |   |  |  |  |
| 35 | 120469   | 1580 | 996185   | 28 | 124284   | 1607 | 875716    | 25 |  |      |  |    |         |    |  |   |  |  |  |
| 36 | 121417   | 1576 | 996168   | 28 | 125249   | 1604 | 874751    | 24 |  |      |  |    |         |    |  |   |  |  |  |
| 37 | 122362   | 1573 | 996151   | 28 | 126211   | 1601 | 873789    | 23 |  |      |  |    |         |    |  |   |  |  |  |
| 38 | 123306   | 1569 | 996134   | 28 | 127172   | 1597 | 872828    | 22 |  |      |  |    |         |    |  |   |  |  |  |
| 39 | 124248   | 1566 | 996117   | 28 | 128130   | 1594 | 871870    | 21 |  |      |  |    |         |    |  |   |  |  |  |
| 40 | 125187   | 1562 | 996100   | 28 | 129087   | 1591 | 870913    | 20 |  |      |  |    |         |    |  |   |  |  |  |
| 41 | 9.126125 | 1559 | 9.996083 | 29 | 9.130041 | 1587 | 10.869959 | 19 |  |      |  |    |         |    |  |   |  |  |  |
| 42 | 127060   | 1556 | 996066   | 29 | 130994   | 1584 | 869006    | 18 |  |      |  |    |         |    |  |   |  |  |  |
| 43 | 127993   | 1552 | 996049   | 29 | 131944   | 1581 | 868056    | 17 |  |      |  |    |         |    |  |   |  |  |  |
| 44 | 128925   | 1549 | 996032   | 29 | 132893   | 1577 | 867107    | 16 |  |      |  |    |         |    |  |   |  |  |  |
| 45 | 129854   | 1545 | 996015   | 29 | 133839   | 1574 | 866161    | 15 |  |      |  |    |         |    |  |   |  |  |  |
| 46 | 130781   | 1542 | 995998   | 29 | 134784   | 1571 | 865216    | 14 |  |      |  |    |         |    |  |   |  |  |  |
| 47 | 131706   | 1539 | 995980   | 29 | 135726   | 1567 | 864274    | 13 |  |      |  |    |         |    |  |   |  |  |  |
| 48 | 132630   | 1535 | 995963   | 29 | 136667   | 1564 | 863333    | 12 |  |      |  |    |         |    |  |   |  |  |  |
| 49 | 133551   | 1532 | 995946   | 29 | 137605   | 1561 | 862395    | 11 |  |      |  |    |         |    |  |   |  |  |  |
| 50 | 134470   | 1529 | 995928   | 29 | 138542   | 1558 | 861458    | 10 |  |      |  |    |         |    |  |   |  |  |  |
| 51 | 9.135387 | 1525 | 9.995911 | 29 | 9.139476 | 1555 | 10.860524 | 9  |  |      |  |    |         |    |  |   |  |  |  |
| 52 | 136303   | 1522 | 995894   | 29 | 140409   | 1551 | 859591    | 8  |  |      |  |    |         |    |  |   |  |  |  |
| 53 | 137216   | 1519 | 995876   | 29 | 141340   | 1548 | 858660    | 7  |  |      |  |    |         |    |  |   |  |  |  |
| 54 | 138128   | 1516 | 995859   | 29 | 142269   | 1545 | 857731    | 6  |  |      |  |    |         |    |  |   |  |  |  |
| 55 | 139037   | 1512 | 995841   | 29 | 143196   | 1542 | 856804    | 5  |  |      |  |    |         |    |  |   |  |  |  |
| 56 | 139944   | 1509 | 995823   | 29 | 144121   | 1539 | 855879    | 4  |  |      |  |    |         |    |  |   |  |  |  |
| 57 | 140850   | 1506 | 995806   | 29 | 145044   | 1535 | 854956    | 3  |  |      |  |    |         |    |  |   |  |  |  |
| 58 | 141754   | 1503 | 995788   | 29 | 145966   | 1532 | 854034    | 2  |  |      |  |    |         |    |  |   |  |  |  |
| 59 | 142655   | 1500 | 995771   | 29 | 146885   | 1529 | 853115    | 1  |  |      |  |    |         |    |  |   |  |  |  |
| 60 | 143555   | 1496 | 995753   | 29 | 147803   | 1526 | 852197    | 0  |  |      |  |    |         |    |  |   |  |  |  |
| /  | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | /  |  | /    |  | D. | Tang.   | D. |  | / |  |  |  |

97°

82°

80°

171°

| <i>r</i> | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | <i>r</i> |
|----------|----------|------|----------|----|----------|------|-----------|----------|
| 0        | 9.143555 | 1496 | 9.995753 | 30 | 9.147803 | 1526 | 10.852197 | 60       |
| 1        | 144453   | 1493 | 995735   | 30 | 148718   | 1523 | 851282    | 59       |
| 2        | 145349   | 1490 | 995717   | 30 | 149632   | 1520 | 850368    | 58       |
| 3        | 146243   | 1487 | 995699   | 30 | 150544   | 1517 | 849456    | 57       |
| 4        | 147136   | 1484 | 995681   | 30 | 151454   | 1514 | 848546    | 56       |
| 5        | 148026   | 1481 | 995664   | 30 | 152363   | 1511 | 847637    | 55       |
| 6        | 148915   | 1478 | 995646   | 30 | 153269   | 1508 | 846731    | 54       |
| 7        | 149802   | 1475 | 995628   | 30 | 154174   | 1505 | 845826    | 53       |
| 8        | 150686   | 1472 | 995610   | 30 | 155077   | 1502 | 844923    | 52       |
| 9        | 151569   | 1469 | 995591   | 30 | 155978   | 1499 | 844022    | 51       |
| 10       | 152451   | 1466 | 995573   | 30 | 156877   | 1496 | 843123    | 50       |
| 11       | 9.153330 | 1463 | 9.995555 | 30 | 9.157775 | 1493 | 10.842225 | 49       |
| 12       | 154208   | 1460 | 995537   | 30 | 158671   | 1490 | 841329    | 48       |
| 13       | 155083   | 1457 | 995519   | 30 | 159565   | 1487 | 840435    | 47       |
| 14       | 155957   | 1454 | 995501   | 31 | 160457   | 1484 | 839543    | 46       |
| 15       | 156830   | 1451 | 995482   | 31 | 161347   | 1481 | 838653    | 45       |
| 16       | 157700   | 1448 | 995464   | 31 | 162236   | 1479 | 837764    | 44       |
| 17       | 158569   | 1445 | 995446   | 31 | 163123   | 1476 | 836877    | 43       |
| 18       | 159435   | 1442 | 995427   | 31 | 164008   | 1473 | 835992    | 42       |
| 19       | 160301   | 1439 | 995409   | 31 | 164892   | 1470 | 835108    | 41       |
| 20       | 161164   | 1436 | 995390   | 31 | 165774   | 1467 | 834226    | 40       |
| 21       | 9.162925 | 1433 | 9.995372 | 31 | 9.166654 | 1464 | 10.833346 | 39       |
| 22       | 162885   | 1430 | 995353   | 31 | 167532   | 1461 | 832468    | 38       |
| 23       | 163743   | 1427 | 995334   | 31 | 168409   | 1458 | 831591    | 37       |
| 24       | 164600   | 1424 | 995316   | 31 | 169284   | 1455 | 830716    | 36       |
| 25       | 165454   | 1422 | 995297   | 31 | 170157   | 1453 | 829843    | 35       |
| 26       | 166307   | 1419 | 995278   | 31 | 171029   | 1450 | 828971    | 34       |
| 27       | 167159   | 1416 | 995260   | 31 | 171899   | 1447 | 828101    | 33       |
| 28       | 168008   | 1413 | 995241   | 32 | 172767   | 1444 | 827233    | 32       |
| 29       | 168856   | 1410 | 995222   | 32 | 173634   | 1442 | 826366    | 31       |
| 30       | 169702   | 1407 | 995203   | 32 | 174499   | 1439 | 825501    | 30       |
| 31       | 9.170547 | 1405 | 9.995184 | 32 | 9.175362 | 1436 | 10.824638 | 29       |
| 32       | 171389   | 1402 | 995165   | 32 | 176224   | 1433 | 823776    | 28       |
| 33       | 172230   | 1399 | 995146   | 32 | 177084   | 1431 | 822916    | 27       |
| 34       | 173070   | 1396 | 995127   | 32 | 177942   | 1428 | 822058    | 26       |
| 35       | 173908   | 1394 | 995108   | 32 | 178799   | 1425 | 821201    | 25       |
| 36       | 174744   | 1391 | 995089   | 32 | 179655   | 1423 | 820345    | 24       |
| 37       | 175578   | 1388 | 995070   | 32 | 180508   | 1420 | 819492    | 23       |
| 38       | 176411   | 1386 | 995051   | 32 | 181360   | 1417 | 818640    | 22       |
| 39       | 177242   | 1383 | 995032   | 32 | 182211   | 1415 | 817789    | 21       |
| 40       | 178072   | 1380 | 995013   | 32 | 183059   | 1412 | 816941    | 20       |
| 41       | 9.178900 | 1377 | 9.994993 | 32 | 9.183907 | 1409 | 10.816093 | 19       |
| 42       | 178926   | 1374 | 994974   | 32 | 184752   | 1407 | 815248    | 18       |
| 43       | 179751   | 1372 | 994955   | 32 | 185597   | 1404 | 814403    | 17       |
| 44       | 180574   | 1369 | 994935   | 32 | 186439   | 1402 | 813561    | 16       |
| 45       | 181396   | 1366 | 994916   | 33 | 187280   | 1399 | 812720    | 15       |
| 46       | 182216   | 1364 | 994896   | 33 | 188120   | 1396 | 811880    | 14       |
| 47       | 183034   | 1361 | 994877   | 33 | 188958   | 1393 | 811042    | 13       |
| 48       | 183851   | 1359 | 994857   | 33 | 189794   | 1391 | 810206    | 12       |
| 49       | 184666   | 1356 | 994838   | 33 | 190629   | 1389 | 809371    | 11       |
| 50       | 185479   | 1353 | 994818   | 33 | 191462   | 1386 | 808538    | 10       |
| 51       | 9.185902 | 1351 | 9.994798 | 33 | 9.192204 | 1384 | 10.807906 | 9        |
| 52       | 186293   | 1348 | 994779   | 33 | 193034   | 1381 | 806876    | 8        |
| 53       | 187092   | 1346 | 994759   | 33 | 193863   | 1379 | 806047    | 7        |
| 54       | 187889   | 1343 | 994739   | 33 | 194690   | 1376 | 805220    | 6        |
| 55       | 188684   | 1341 | 994719   | 33 | 195516   | 1374 | 804394    | 5        |
| 56       | 189477   | 1338 | 994699   | 33 | 196340   | 1371 | 803570    | 4        |
| 57       | 190268   | 1336 | 994679   | 33 | 197163   | 1369 | 802747    | 3        |
| 58       | 191057   | 1333 | 994659   | 33 | 197984   | 1366 | 801926    | 2        |
| 59       | 191844   | 1330 | 994639   | 33 | 198804   | 1364 | 801106    | 1        |
| 60       | 192629   | 1328 | 994619   | 33 | 199623   | 1362 | 800287    | 0        |
| <i>r</i> | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | <i>r</i> |

80°

81°

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

27

| 9°  |          |      |          |    |          |      |           | 170° |  |
|-----|----------|------|----------|----|----------|------|-----------|------|--|
| /   | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | /    |  |
| 0   | 9.194332 | 1328 | 9.994620 | 33 | 9.199713 | 1361 | 10.800287 | 60   |  |
| 1   | 195129   | 1326 | 994600   | 33 | 200529   | 1359 | 799471    | 59   |  |
| 2   | 195925   | 1323 | 994580   | 33 | 201345   | 1356 | 798655    | 58   |  |
| 3   | 196719   | 1321 | 994560   | 34 | 202159   | 1354 | 797841    | 57   |  |
| 4   | 197511   | 1318 | 994540   | 34 | 202971   | 1352 | 797029    | 56   |  |
| 5   | 198302   | 1316 | 994519   | 34 | 203782   | 1349 | 796218    | 55   |  |
| 6   | 199091   | 1313 | 994499   | 34 | 204592   | 1347 | 795408    | 54   |  |
| 7   | 199879   | 1311 | 994479   | 34 | 205400   | 1345 | 794600    | 53   |  |
| 8   | 200666   | 1308 | 994459   | 34 | 206207   | 1342 | 793793    | 52   |  |
| 9   | 201451   | 1306 | 994438   | 34 | 207013   | 1340 | 792987    | 51   |  |
| 10  | 202234   | 1304 | 994418   | 34 | 207817   | 1338 | 792183    | 50   |  |
| 11  | 9.203017 | 1301 | 9.994398 | 34 | 9.208619 | 1335 | 10.791381 | 49   |  |
| 12  | 203797   | 1299 | 994377   | 34 | 209420   | 1333 | 790580    | 48   |  |
| 13  | 204577   | 1296 | 994357   | 34 | 210220   | 1331 | 789780    | 47   |  |
| 14  | 205354   | 1294 | 994336   | 34 | 211018   | 1328 | 788982    | 46   |  |
| 15  | 206131   | 1292 | 994316   | 34 | 211815   | 1326 | 788185    | 45   |  |
| 16  | 206906   | 1289 | 994295   | 34 | 212611   | 1324 | 787389    | 44   |  |
| 17  | 207679   | 1287 | 994274   | 35 | 213405   | 1321 | 786595    | 43   |  |
| 18  | 208452   | 1285 | 994254   | 35 | 214198   | 1319 | 785802    | 42   |  |
| 19  | 209222   | 1282 | 994233   | 35 | 214989   | 1317 | 785011    | 41   |  |
| 20  | 209992   | 1280 | 994212   | 35 | 215780   | 1315 | 784220    | 40   |  |
| 21  | 9.210760 | 1278 | 9.994191 | 35 | 9.216568 | 1312 | 10.783432 | 39   |  |
| 22  | 211526   | 1275 | 994171   | 35 | 217356   | 1310 | 782644    | 38   |  |
| 23  | 212291   | 1273 | 994150   | 35 | 218142   | 1308 | 781858    | 37   |  |
| 24  | 213055   | 1271 | 994129   | 35 | 218926   | 1305 | 781074    | 36   |  |
| 25  | 213818   | 1268 | 994108   | 35 | 219710   | 1303 | 780290    | 35   |  |
| 26  | 214579   | 1266 | 994087   | 35 | 220492   | 1301 | 779508    | 34   |  |
| 27  | 215338   | 1264 | 994066   | 35 | 221272   | 1299 | 778728    | 33   |  |
| 28  | 216097   | 1261 | 994045   | 35 | 222052   | 1297 | 777948    | 32   |  |
| 29  | 216854   | 1259 | 994024   | 35 | 222830   | 1294 | 777170    | 31   |  |
| 30  | 217609   | 1257 | 994003   | 35 | 223607   | 1292 | 776393    | 30   |  |
| 31  | 9.218363 | 1255 | 9.993982 | 35 | 9.224382 | 1290 | 10.775618 | 29   |  |
| 32  | 219116   | 1253 | 993960   | 35 | 225156   | 1288 | 774844    | 28   |  |
| 33  | 219868   | 1250 | 993939   | 35 | 225929   | 1286 | 774071    | 27   |  |
| 34  | 220618   | 1248 | 993918   | 35 | 226700   | 1284 | 773300    | 26   |  |
| 35  | 221367   | 1246 | 993897   | 36 | 227471   | 1281 | 772529    | 25   |  |
| 36  | 222115   | 1244 | 993875   | 36 | 228239   | 1279 | 771761    | 24   |  |
| 37  | 222861   | 1242 | 993854   | 36 | 229007   | 1277 | 770993    | 23   |  |
| 38  | 223606   | 1239 | 993832   | 36 | 229773   | 1275 | 770227    | 22   |  |
| 39  | 224349   | 1237 | 993811   | 36 | 230539   | 1273 | 769461    | 21   |  |
| 40  | 225092   | 1235 | 993789   | 36 | 231302   | 1271 | 768698    | 20   |  |
| 41  | 9.225833 | 1233 | 9.993768 | 36 | 9.232065 | 1269 | 10.767935 | 19   |  |
| 42  | 226573   | 1231 | 993746   | 36 | 232826   | 1267 | 767174    | 18   |  |
| 43  | 227311   | 1228 | 993725   | 36 | 233586   | 1265 | 766414    | 17   |  |
| 44  | 228048   | 1226 | 993703   | 36 | 234345   | 1262 | 765655    | 16   |  |
| 45  | 228784   | 1224 | 993681   | 36 | 235103   | 1260 | 764897    | 15   |  |
| 46  | 229518   | 1222 | 993660   | 36 | 235859   | 1258 | 764141    | 14   |  |
| 47  | 230252   | 1220 | 993638   | 36 | 236614   | 1256 | 763386    | 13   |  |
| 48  | 230984   | 1218 | 993616   | 36 | 237368   | 1254 | 762632    | 12   |  |
| 49  | 231715   | 1216 | 993594   | 37 | 238120   | 1252 | 761880    | 11   |  |
| 50  | 232444   | 1214 | 993572   | 37 | 238872   | 1250 | 761128    | 10   |  |
| 51  | 9.233172 | 1212 | 9.993550 | 37 | 9.239622 | 1248 | 10.760378 | 9    |  |
| 52  | 233899   | 1209 | 993528   | 37 | 240371   | 1246 | 759629    | 8    |  |
| 53  | 234625   | 1207 | 993506   | 37 | 241118   | 1244 | 758882    | 7    |  |
| 54  | 235349   | 1205 | 993484   | 37 | 241865   | 1242 | 758135    | 6    |  |
| 55  | 236073   | 1203 | 993462   | 37 | 242610   | 1240 | 757390    | 5    |  |
| 56  | 236795   | 1201 | 993440   | 37 | 243354   | 1238 | 756646    | 4    |  |
| 57  | 237515   | 1199 | 993418   | 37 | 244097   | 1236 | 755903    | 3    |  |
| 58  | 238235   | 1197 | 993396   | 37 | 244839   | 1234 | 755161    | 2    |  |
| 59  | 238953   | 1195 | 993374   | 37 | 245579   | 1232 | 754421    | 1    |  |
| 60  | 239670   | 1193 | 993351   | 37 | 246319   | 1230 | 753681    | 0    |  |
| /   | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | /    |  |
| 99° |          |      |          |    |          |      |           | 80°  |  |

| No. | Name         | Age | Sex | Rank    | Pay    | Company         |
|-----|--------------|-----|-----|---------|--------|-----------------|
| 1   | Wm. A. Smith | 25  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 2   | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 3   | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 4   | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 5   | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 6   | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 7   | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 8   | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 9   | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 10  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 11  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 12  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 13  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 14  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 15  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 16  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 17  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 18  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 19  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 20  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 21  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 22  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 23  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 24  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 25  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 26  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 27  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 28  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 29  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 30  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 31  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 32  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 33  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 34  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 35  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 36  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 37  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 38  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 39  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 40  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 41  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 42  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 43  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 44  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 45  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 46  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 47  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 48  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |
| 49  | Wm. B. Brown | 22  | M   | 1st Lt. | \$1200 | 10th Regt. Inf. |
| 50  | J. H. Jones  | 28  | M   | 2nd Lt. | \$1000 | 10th Regt. Inf. |

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 11° |          |      |          |    |          |      |           | 168° |  |
|-----|----------|------|----------|----|----------|------|-----------|------|--|
| /   | Sine.    | D.   | Cosine.  | D. | Tang.    | D.   | Cotang.   | /    |  |
| 0   | 9.280599 | 1082 | 9.991947 | 41 | 9.288652 | 1123 | 10.711348 | 60   |  |
| 1   | 281248   | 1081 | 991922   | 41 | 289326   | 1122 | 710674    | 59   |  |
| 2   | 281897   | 1079 | 991897   | 41 | 289999   | 1120 | 710001    | 58   |  |
| 3   | 282544   | 1077 | 991873   | 41 | 290671   | 1118 | 709329    | 57   |  |
| 4   | 283190   | 1076 | 991848   | 41 | 291342   | 1117 | 708658    | 56   |  |
| 5   | 283836   | 1074 | 991823   | 41 | 292013   | 1115 | 707987    | 55   |  |
| 6   | 284480   | 1072 | 991799   | 41 | 292682   | 1114 | 707318    | 54   |  |
| 7   | 285124   | 1071 | 991774   | 42 | 293350   | 1112 | 706650    | 53   |  |
| 8   | 285766   | 1069 | 991749   | 42 | 294017   | 1111 | 705983    | 52   |  |
| 9   | 286408   | 1067 | 991724   | 42 | 294684   | 1109 | 705316    | 51   |  |
| 10  | 287048   | 1066 | 991699   | 42 | 295349   | 1107 | 704651    | 50   |  |
| 11  | 9.287688 | 1064 | 9.991674 | 42 | 9.296013 | 1106 | 10.703897 | 49   |  |
| 12  | 288326   | 1063 | 991649   | 42 | 296677   | 1104 | 703323    | 48   |  |
| 13  | 288964   | 1061 | 991624   | 42 | 297339   | 1103 | 702661    | 47   |  |
| 14  | 289600   | 1059 | 991599   | 42 | 298001   | 1101 | 701999    | 46   |  |
| 15  | 290236   | 1058 | 991574   | 42 | 298662   | 1100 | 701338    | 45   |  |
| 16  | 290870   | 1056 | 991549   | 42 | 299322   | 1098 | 700678    | 44   |  |
| 17  | 291504   | 1054 | 991524   | 42 | 299980   | 1096 | 700020    | 43   |  |
| 18  | 292137   | 1053 | 991498   | 42 | 300638   | 1095 | 699362    | 42   |  |
| 19  | 292768   | 1051 | 991473   | 42 | 301295   | 1093 | 698705    | 41   |  |
| 20  | 293399   | 1050 | 991448   | 42 | 301951   | 1092 | 698049    | 40   |  |
| 21  | 9.294029 | 1048 | 9.991422 | 42 | 9.302607 | 1090 | 10.697393 | 39   |  |
| 22  | 294658   | 1046 | 991397   | 42 | 303261   | 1089 | 696739    | 38   |  |
| 23  | 295286   | 1045 | 991372   | 43 | 303914   | 1087 | 696086    | 37   |  |
| 24  | 295913   | 1043 | 991346   | 43 | 304567   | 1086 | 695433    | 36   |  |
| 25  | 296539   | 1042 | 991321   | 43 | 305218   | 1084 | 694782    | 35   |  |
| 26  | 297164   | 1040 | 991295   | 43 | 305869   | 1083 | 694131    | 34   |  |
| 27  | 297788   | 1039 | 991270   | 43 | 306519   | 1081 | 693481    | 33   |  |
| 28  | 298412   | 1037 | 991244   | 43 | 307168   | 1080 | 692832    | 32   |  |
| 29  | 299034   | 1036 | 991218   | 43 | 307816   | 1078 | 692184    | 31   |  |
| 30  | 299655   | 1034 | 991193   | 43 | 308463   | 1077 | 691537    | 30   |  |
| 31  | 9.300276 | 1032 | 9.991167 | 43 | 9.309109 | 1075 | 10.690891 | 29   |  |
| 32  | 300895   | 1031 | 991141   | 43 | 309754   | 1074 | 690246    | 28   |  |
| 33  | 301514   | 1029 | 991115   | 43 | 310399   | 1073 | 689601    | 27   |  |
| 34  | 302132   | 1028 | 991090   | 43 | 311042   | 1071 | 688958    | 26   |  |
| 35  | 302748   | 1026 | 991064   | 43 | 311685   | 1070 | 688315    | 25   |  |
| 36  | 303364   | 1025 | 991038   | 43 | 312327   | 1068 | 687673    | 24   |  |
| 37  | 303979   | 1023 | 991012   | 43 | 312968   | 1067 | 687032    | 23   |  |
| 38  | 304593   | 1022 | 990986   | 43 | 313608   | 1065 | 686392    | 22   |  |
| 39  | 305207   | 1020 | 990960   | 43 | 314247   | 1064 | 685753    | 21   |  |
| 40  | 305819   | 1019 | 990934   | 44 | 314885   | 1062 | 685115    | 20   |  |
| 41  | 9.306430 | 1017 | 9.990908 | 44 | 9.315523 | 1061 | 10.684477 | 19   |  |
| 42  | 307041   | 1016 | 990882   | 44 | 316159   | 1060 | 683841    | 18   |  |
| 43  | 307650   | 1014 | 990855   | 44 | 316795   | 1058 | 683205    | 17   |  |
| 44  | 308259   | 1013 | 990829   | 44 | 317430   | 1057 | 682570    | 16   |  |
| 45  | 308867   | 1011 | 990803   | 44 | 318064   | 1055 | 681936    | 15   |  |
| 46  | 309474   | 1010 | 990777   | 44 | 318697   | 1054 | 681303    | 14   |  |
| 47  | 310080   | 1008 | 990750   | 44 | 319330   | 1053 | 680670    | 13   |  |
| 48  | 310685   | 1007 | 990724   | 44 | 319961   | 1051 | 680039    | 12   |  |
| 49  | 311289   | 1005 | 990697   | 44 | 320592   | 1050 | 679408    | 11   |  |
| 50  | 311893   | 1004 | 990671   | 44 | 321222   | 1048 | 678778    | 10   |  |
| 51  | 9.312495 | 1003 | 9.990645 | 44 | 9.321851 | 1047 | 10.678149 | 9    |  |
| 52  | 313097   | 1001 | 990618   | 44 | 322479   | 1045 | 677521    | 8    |  |
| 53  | 313698   | 1000 | 990591   | 44 | 323106   | 1044 | 676894    | 7    |  |
| 54  | 314297   | 998  | 990565   | 44 | 323733   | 1043 | 676267    | 6    |  |
| 55  | 314897   | 997  | 990538   | 44 | 324358   | 1041 | 675642    | 5    |  |
| 56  | 315495   | 996  | 990511   | 45 | 324983   | 1040 | 675017    | 4    |  |
| 57  | 316092   | 994  | 990485   | 45 | 325607   | 1039 | 674393    | 3    |  |
| 58  | 316689   | 993  | 990458   | 45 | 326231   | 1037 | 673769    | 2    |  |
| 59  | 317284   | 991  | 990431   | 45 | 326853   | 1036 | 673147    | 1    |  |
| 60  | 317879   | 990  | 990404   | 45 | 327475   | 1035 | 672525    | 0    |  |
| /   | Cosine.  | D.   | Sine.    | D. | Cotang.  | D.   | Tang.     | /    |  |

101°

78°

12°

167°

| /  | Sine.    | D.  | Cosine.  | D. | Tang.    | D.   | Cotang.   | /  |
|----|----------|-----|----------|----|----------|------|-----------|----|
| 0  | 9.317879 | 990 | 9.990404 | 45 | 9.327475 | 1035 | 10.672525 | 60 |
| 1  | 318473   | 888 | 990378   | 45 | 328095   | 1033 | 671905    | 59 |
| 2  | 319066   | 987 | 990351   | 45 | 328715   | 1032 | 671285    | 58 |
| 3  | 319658   | 986 | 990324   | 45 | 329334   | 1030 | 670666    | 57 |
| 4  | 320249   | 984 | 990297   | 45 | 329953   | 1029 | 670047    | 56 |
| 5  | 320840   | 983 | 990270   | 45 | 330570   | 1028 | 669430    | 55 |
| 6  | 321430   | 982 | 990243   | 45 | 331187   | 1026 | 668813    | 54 |
| 7  | 322019   | 980 | 990215   | 45 | 331803   | 1025 | 668197    | 53 |
| 8  | 322607   | 979 | 990188   | 45 | 332418   | 1024 | 667582    | 52 |
| 9  | 323194   | 977 | 990161   | 45 | 333033   | 1023 | 666967    | 51 |
| 10 | 323780   | 976 | 990134   | 45 | 333646   | 1021 | 666354    | 50 |
| 11 | 9.324366 | 975 | 9.990107 | 46 | 9.334259 | 1020 | 10.665741 | 49 |
| 12 | 324950   | 973 | 990079   | 46 | 334871   | 1019 | 665129    | 48 |
| 13 | 325534   | 972 | 990052   | 46 | 335482   | 1017 | 664518    | 47 |
| 14 | 326117   | 970 | 990025   | 46 | 336093   | 1016 | 663907    | 46 |
| 15 | 326700   | 969 | 989997   | 46 | 336702   | 1015 | 663298    | 45 |
| 16 | 327281   | 968 | 989970   | 46 | 337311   | 1013 | 662689    | 44 |
| 17 | 327862   | 966 | 989942   | 46 | 337919   | 1012 | 662081    | 43 |
| 18 | 328442   | 965 | 989915   | 46 | 338527   | 1011 | 661473    | 42 |
| 19 | 329021   | 964 | 989887   | 46 | 339133   | 1010 | 660867    | 41 |
| 20 | 329599   | 962 | 989860   | 46 | 339739   | 1008 | 660261    | 40 |
| 21 | 9.330176 | 961 | 9.989832 | 46 | 9.340344 | 1007 | 10.655656 | 39 |
| 22 | 330753   | 960 | 989804   | 46 | 340948   | 1006 | 655052    | 38 |
| 23 | 331329   | 958 | 989777   | 46 | 341552   | 1004 | 654448    | 37 |
| 24 | 331903   | 957 | 989749   | 47 | 342155   | 1003 | 653845    | 36 |
| 25 | 332478   | 956 | 989721   | 47 | 342757   | 1002 | 653243    | 35 |
| 26 | 333051   | 954 | 989693   | 47 | 343358   | 1000 | 652642    | 34 |
| 27 | 333624   | 953 | 989665   | 47 | 343958   | 999  | 652042    | 33 |
| 28 | 334195   | 952 | 989637   | 47 | 344558   | 998  | 651442    | 32 |
| 29 | 334767   | 950 | 989610   | 47 | 345157   | 997  | 650843    | 31 |
| 30 | 335337   | 949 | 989582   | 47 | 345755   | 996  | 650245    | 30 |
| 31 | 9.335906 | 948 | 9.989553 | 47 | 9.346353 | 994  | 10.653647 | 29 |
| 32 | 336475   | 946 | 989525   | 47 | 346949   | 993  | 653051    | 28 |
| 33 | 337043   | 945 | 989497   | 47 | 347545   | 992  | 652455    | 27 |
| 34 | 337610   | 944 | 989469   | 47 | 348141   | 991  | 651859    | 26 |
| 35 | 338176   | 943 | 989441   | 47 | 348735   | 990  | 651265    | 25 |
| 36 | 338742   | 941 | 989413   | 47 | 349329   | 988  | 650671    | 24 |
| 37 | 339307   | 940 | 989385   | 47 | 349922   | 987  | 650078    | 23 |
| 38 | 339871   | 939 | 989356   | 47 | 350514   | 986  | 649486    | 22 |
| 39 | 340434   | 937 | 989328   | 47 | 351106   | 985  | 648894    | 21 |
| 40 | 340996   | 936 | 989300   | 47 | 351697   | 983  | 648303    | 20 |
| 41 | 9.341558 | 935 | 9.989271 | 47 | 9.352287 | 982  | 10.647713 | 19 |
| 42 | 342119   | 934 | 989243   | 47 | 352876   | 981  | 647124    | 18 |
| 43 | 342679   | 932 | 989214   | 47 | 353465   | 980  | 646535    | 17 |
| 44 | 343239   | 931 | 989186   | 47 | 354053   | 979  | 645947    | 16 |
| 45 | 343797   | 930 | 989157   | 47 | 354640   | 977  | 645360    | 15 |
| 46 | 344355   | 929 | 989128   | 48 | 355227   | 976  | 644773    | 14 |
| 47 | 344912   | 927 | 989100   | 48 | 355813   | 975  | 644187    | 13 |
| 48 | 345469   | 926 | 989071   | 48 | 356398   | 974  | 643602    | 12 |
| 49 | 346024   | 925 | 989042   | 48 | 356982   | 973  | 643018    | 11 |
| 50 | 346579   | 924 | 989014   | 48 | 357566   | 971  | 642434    | 10 |
| 51 | 9.347134 | 922 | 9.988985 | 48 | 9.358149 | 970  | 10.641851 | 9  |
| 52 | 347687   | 921 | 988956   | 48 | 358731   | 969  | 641269    | 8  |
| 53 | 348240   | 920 | 988927   | 48 | 359313   | 968  | 640687    | 7  |
| 54 | 348792   | 919 | 988898   | 48 | 359893   | 967  | 640107    | 6  |
| 55 | 349343   | 917 | 988869   | 48 | 360474   | 966  | 639526    | 5  |
| 56 | 349893   | 916 | 988840   | 48 | 361053   | 965  | 638947    | 4  |
| 57 | 350443   | 915 | 988811   | 49 | 361632   | 963  | 638368    | 3  |
| 58 | 350992   | 914 | 988782   | 49 | 362210   | 962  | 637790    | 2  |
| 59 | 351540   | 913 | 988753   | 49 | 362787   | 961  | 637213    | 1  |
| 60 | 352088   | 911 | 988724   | 49 | 363364   | 960  | 636636    | 0  |
| /  | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.   | Tang.     | /  |

102°

77°

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

81

| 18° |          |     |          |    |          |     |           | 166° |  |  |  |  |  |  |   |
|-----|----------|-----|----------|----|----------|-----|-----------|------|--|--|--|--|--|--|---|
| /   | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  | / |
| 0   | 9.352088 | 911 | 9.988724 | 49 | 9.363364 | 960 | 10.636636 | 60   |  |  |  |  |  |  |   |
| 1   | 352635   | 910 | 988695   | 49 | 363940   | 959 | 636060    | 59   |  |  |  |  |  |  |   |
| 2   | 353181   | 909 | 988666   | 49 | 364515   | 958 | 635485    | 58   |  |  |  |  |  |  |   |
| 3   | 353726   | 908 | 988636   | 49 | 365090   | 957 | 634910    | 57   |  |  |  |  |  |  |   |
| 4   | 354271   | 907 | 988607   | 49 | 365664   | 955 | 634336    | 56   |  |  |  |  |  |  |   |
| 5   | 354815   | 905 | 988578   | 49 | 366237   | 954 | 633763    | 55   |  |  |  |  |  |  |   |
| 6   | 355358   | 904 | 988549   | 49 | 366810   | 953 | 633190    | 54   |  |  |  |  |  |  |   |
| 7   | 355901   | 903 | 988519   | 49 | 367382   | 952 | 632618    | 53   |  |  |  |  |  |  |   |
| 8   | 356443   | 902 | 988489   | 49 | 367953   | 951 | 632047    | 52   |  |  |  |  |  |  |   |
| 9   | 356984   | 901 | 988460   | 49 | 368524   | 950 | 631476    | 51   |  |  |  |  |  |  |   |
| 10  | 357524   | 899 | 988430   | 49 | 369094   | 949 | 630906    | 50   |  |  |  |  |  |  |   |
| 11  | 9.358064 | 898 | 9.988401 | 49 | 9.369663 | 948 | 10.630337 | 49   |  |  |  |  |  |  |   |
| 12  | 358603   | 897 | 988371   | 49 | 370232   | 946 | 629768    | 48   |  |  |  |  |  |  |   |
| 13  | 359141   | 896 | 988342   | 49 | 370799   | 945 | 629201    | 47   |  |  |  |  |  |  |   |
| 14  | 359678   | 895 | 988312   | 50 | 371367   | 944 | 628633    | 46   |  |  |  |  |  |  |   |
| 15  | 360215   | 893 | 988282   | 50 | 371933   | 943 | 628067    | 45   |  |  |  |  |  |  |   |
| 16  | 360752   | 892 | 988252   | 50 | 372499   | 942 | 627501    | 44   |  |  |  |  |  |  |   |
| 17  | 361287   | 891 | 988223   | 50 | 373064   | 941 | 626936    | 43   |  |  |  |  |  |  |   |
| 18  | 361822   | 890 | 988193   | 50 | 373629   | 940 | 626371    | 42   |  |  |  |  |  |  |   |
| 19  | 362356   | 889 | 988163   | 50 | 374193   | 939 | 625807    | 41   |  |  |  |  |  |  |   |
| 20  | 362889   | 888 | 988133   | 50 | 374756   | 938 | 625244    | 40   |  |  |  |  |  |  |   |
| 21  | 9.363422 | 887 | 9.988103 | 50 | 9.375319 | 937 | 10.624681 | 39   |  |  |  |  |  |  |   |
| 22  | 363954   | 885 | 988073   | 50 | 375881   | 935 | 624119    | 38   |  |  |  |  |  |  |   |
| 23  | 364485   | 884 | 988043   | 50 | 376442   | 934 | 623558    | 37   |  |  |  |  |  |  |   |
| 24  | 365016   | 883 | 988013   | 50 | 377003   | 933 | 622997    | 36   |  |  |  |  |  |  |   |
| 25  | 365546   | 882 | 987983   | 50 | 377563   | 932 | 622437    | 35   |  |  |  |  |  |  |   |
| 26  | 366075   | 881 | 987953   | 50 | 378122   | 931 | 621878    | 34   |  |  |  |  |  |  |   |
| 27  | 366604   | 880 | 987922   | 50 | 378681   | 930 | 621319    | 33   |  |  |  |  |  |  |   |
| 28  | 367131   | 879 | 987892   | 50 | 379239   | 929 | 620761    | 32   |  |  |  |  |  |  |   |
| 29  | 367659   | 877 | 987862   | 50 | 379797   | 928 | 620203    | 31   |  |  |  |  |  |  |   |
| 30  | 368185   | 876 | 987832   | 51 | 380354   | 927 | 619646    | 30   |  |  |  |  |  |  |   |
| 31  | 9.368711 | 875 | 9.987801 | 51 | 9.380910 | 926 | 10.619090 | 29   |  |  |  |  |  |  |   |
| 32  | 369236   | 874 | 987771   | 51 | 381466   | 925 | 618534    | 28   |  |  |  |  |  |  |   |
| 33  | 369761   | 873 | 987740   | 51 | 382020   | 924 | 617980    | 27   |  |  |  |  |  |  |   |
| 34  | 370285   | 872 | 987710   | 51 | 382575   | 923 | 617425    | 26   |  |  |  |  |  |  |   |
| 35  | 370808   | 871 | 987679   | 51 | 383129   | 922 | 616871    | 25   |  |  |  |  |  |  |   |
| 36  | 371330   | 870 | 987649   | 51 | 383682   | 921 | 616318    | 24   |  |  |  |  |  |  |   |
| 37  | 371852   | 869 | 987618   | 51 | 384234   | 920 | 615766    | 23   |  |  |  |  |  |  |   |
| 38  | 372373   | 867 | 987588   | 51 | 384786   | 919 | 615214    | 22   |  |  |  |  |  |  |   |
| 39  | 372894   | 866 | 987557   | 51 | 385337   | 918 | 614663    | 21   |  |  |  |  |  |  |   |
| 40  | 373414   | 865 | 987526   | 51 | 385888   | 917 | 614112    | 20   |  |  |  |  |  |  |   |
| 41  | 9.373933 | 864 | 9.987496 | 51 | 9.386438 | 915 | 10.613562 | 19   |  |  |  |  |  |  |   |
| 42  | 374452   | 863 | 987465   | 51 | 386987   | 914 | 613013    | 18   |  |  |  |  |  |  |   |
| 43  | 374970   | 862 | 987434   | 51 | 387536   | 913 | 612464    | 17   |  |  |  |  |  |  |   |
| 44  | 375487   | 861 | 987403   | 52 | 388084   | 912 | 611916    | 16   |  |  |  |  |  |  |   |
| 45  | 376003   | 860 | 987372   | 52 | 388631   | 911 | 611369    | 15   |  |  |  |  |  |  |   |
| 46  | 376519   | 859 | 987341   | 52 | 389178   | 910 | 610822    | 14   |  |  |  |  |  |  |   |
| 47  | 377035   | 858 | 987310   | 52 | 389724   | 909 | 610276    | 13   |  |  |  |  |  |  |   |
| 48  | 377549   | 857 | 987279   | 52 | 390270   | 908 | 609730    | 12   |  |  |  |  |  |  |   |
| 49  | 378063   | 856 | 987248   | 52 | 390815   | 907 | 609185    | 11   |  |  |  |  |  |  |   |
| 50  | 378577   | 854 | 987217   | 52 | 391360   | 906 | 608640    | 10   |  |  |  |  |  |  |   |
| 51  | 9.379089 | 853 | 9.987186 | 52 | 9.391903 | 905 | 10.608097 | 9    |  |  |  |  |  |  |   |
| 52  | 379601   | 852 | 987155   | 52 | 392447   | 904 | 607553    | 8    |  |  |  |  |  |  |   |
| 53  | 380113   | 851 | 987124   | 52 | 392989   | 903 | 607011    | 7    |  |  |  |  |  |  |   |
| 54  | 380624   | 850 | 987092   | 52 | 393531   | 902 | 606469    | 6    |  |  |  |  |  |  |   |
| 55  | 381134   | 849 | 987061   | 52 | 394073   | 901 | 605927    | 5    |  |  |  |  |  |  |   |
| 56  | 381643   | 848 | 987030   | 52 | 394614   | 900 | 605386    | 4    |  |  |  |  |  |  |   |
| 57  | 382152   | 847 | 986998   | 52 | 395154   | 899 | 604846    | 3    |  |  |  |  |  |  |   |
| 58  | 382661   | 846 | 986967   | 52 | 395694   | 898 | 604306    | 2    |  |  |  |  |  |  |   |
| 59  | 383168   | 845 | 986936   | 52 | 396233   | 897 | 603767    | 1    |  |  |  |  |  |  |   |
| 60  | 383675   | 844 | 986904   | 52 | 396771   | 896 | 603229    | 0    |  |  |  |  |  |  |   |
| /   | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  | / |

108°

76°

145°

185°

|    | Sine.     | D.  | Cotang.   | D. | Tang.     | D.  | Cotang.    |    |
|----|-----------|-----|-----------|----|-----------|-----|------------|----|
| 0  | 9. 454595 | 846 | 9. 986996 | 52 | 9. 367771 | 896 | 10. 633229 | 60 |
| 1  | 454632    | 845 | 986975    | 53 | 367789    | 896 | 633210     | 59 |
| 2  | 454669    | 845 | 986954    | 53 | 367806    | 895 | 633191     | 58 |
| 3  | 454706    | 845 | 986933    | 53 | 367823    | 894 | 633172     | 57 |
| 4  | 454743    | 845 | 986912    | 53 | 367840    | 893 | 633153     | 56 |
| 5  | 454780    | 845 | 986891    | 53 | 367857    | 892 | 633134     | 55 |
| 6  | 454817    | 845 | 986870    | 53 | 367874    | 891 | 633115     | 54 |
| 7  | 454854    | 845 | 986849    | 53 | 400524    | 890 | 599676     | 53 |
| 8  | 454891    | 845 | 986828    | 53 | 401058    | 889 | 599657     | 52 |
| 9  | 454928    | 845 | 986807    | 53 | 401592    | 888 | 599638     | 51 |
| 10 | 454965    | 844 | 986786    | 53 | 402126    | 887 | 599619     | 50 |
| 11 | 9. 389211 | 833 | 9. 986555 | 53 | 9. 402656 | 886 | 10. 597344 | 49 |
| 12 | 389248    | 832 | 986533    | 53 | 403189    | 885 | 596813     | 48 |
| 13 | 389285    | 831 | 986512    | 53 | 403718    | 884 | 596282     | 47 |
| 14 | 389322    | 830 | 986491    | 53 | 404246    | 883 | 595751     | 46 |
| 15 | 389359    | 828 | 986470    | 53 | 404775    | 882 | 595222     | 45 |
| 16 | 389396    | 827 | 986449    | 53 | 405308    | 881 | 594692     | 44 |
| 17 | 389433    | 826 | 986428    | 54 | 405836    | 880 | 594164     | 43 |
| 18 | 389470    | 825 | 986407    | 54 | 406364    | 879 | 593636     | 42 |
| 19 | 389507    | 824 | 986386    | 54 | 406892    | 878 | 593108     | 41 |
| 20 | 389544    | 823 | 986365    | 54 | 407419    | 877 | 592581     | 40 |
| 21 | 9. 389581 | 822 | 9. 986344 | 54 | 9. 407945 | 876 | 10. 592055 | 39 |
| 22 | 389618    | 821 | 986323    | 54 | 408471    | 875 | 591529     | 38 |
| 23 | 389655    | 820 | 986302    | 54 | 408996    | 874 | 591004     | 37 |
| 24 | 389692    | 819 | 986281    | 54 | 409521    | 873 | 590479     | 36 |
| 25 | 389729    | 818 | 986260    | 54 | 410045    | 872 | 589955     | 35 |
| 26 | 389766    | 817 | 986239    | 54 | 410569    | 871 | 589431     | 34 |
| 27 | 389803    | 817 | 986218    | 54 | 411092    | 870 | 588908     | 33 |
| 28 | 389840    | 816 | 986197    | 54 | 411615    | 869 | 588385     | 32 |
| 29 | 389877    | 815 | 986176    | 54 | 412137    | 868 | 587862     | 31 |
| 30 | 389914    | 814 | 986155    | 54 | 412658    | 867 | 587343     | 30 |
| 31 | 9. 389951 | 813 | 9. 986134 | 55 | 9. 413179 | 866 | 10. 586821 | 29 |
| 32 | 389988    | 812 | 986113    | 55 | 413699    | 865 | 586301     | 28 |
| 33 | 400025    | 811 | 986092    | 55 | 414219    | 864 | 585781     | 27 |
| 34 | 400062    | 810 | 986071    | 55 | 414738    | 863 | 585262     | 26 |
| 35 | 400099    | 809 | 986050    | 55 | 415257    | 862 | 584743     | 25 |
| 36 | 400136    | 808 | 986029    | 55 | 415775    | 861 | 584225     | 24 |
| 37 | 400173    | 807 | 986008    | 55 | 416293    | 860 | 583707     | 23 |
| 38 | 400210    | 806 | 985987    | 55 | 416810    | 859 | 583190     | 22 |
| 39 | 400247    | 805 | 985966    | 55 | 417326    | 858 | 582674     | 21 |
| 40 | 400284    | 804 | 985945    | 55 | 417842    | 857 | 582158     | 20 |
| 41 | 9. 400321 | 803 | 9. 985924 | 55 | 9. 418358 | 856 | 10. 581642 | 19 |
| 42 | 400358    | 802 | 985903    | 55 | 418873    | 855 | 581127     | 18 |
| 43 | 400395    | 801 | 985882    | 55 | 419387    | 854 | 580613     | 17 |
| 44 | 400432    | 800 | 985861    | 55 | 419901    | 853 | 580099     | 16 |
| 45 | 400469    | 799 | 985840    | 55 | 420415    | 852 | 579585     | 15 |
| 46 | 400506    | 798 | 985819    | 56 | 420927    | 851 | 579073     | 14 |
| 47 | 400543    | 797 | 985798    | 56 | 421440    | 850 | 578560     | 13 |
| 48 | 400580    | 796 | 985777    | 56 | 421952    | 849 | 578048     | 12 |
| 49 | 400617    | 795 | 985756    | 56 | 422463    | 848 | 577537     | 11 |
| 50 | 400654    | 794 | 985735    | 56 | 422974    | 847 | 577026     | 10 |
| 51 | 9. 400691 | 793 | 9. 985714 | 56 | 9. 423484 | 846 | 10. 576516 | 9  |
| 52 | 400728    | 792 | 985693    | 56 | 423993    | 845 | 576007     | 8  |
| 53 | 400765    | 791 | 985672    | 56 | 424503    | 844 | 575497     | 7  |
| 54 | 400802    | 790 | 985651    | 56 | 425011    | 843 | 574989     | 6  |
| 55 | 400839    | 789 | 985630    | 56 | 425519    | 842 | 574481     | 5  |
| 56 | 400876    | 788 | 985609    | 56 | 426027    | 841 | 573973     | 4  |
| 57 | 400913    | 787 | 985588    | 56 | 426534    | 840 | 573466     | 3  |
| 58 | 400950    | 786 | 985567    | 56 | 427041    | 839 | 572959     | 2  |
| 59 | 400987    | 785 | 985546    | 56 | 427547    | 838 | 572453     | 1  |
| 60 | 401024    | 784 | 985525    | 56 | 428052    | 837 | 571948     | 0  |
|    | Cotang.   | D.  | Sine.     | D. | Cotang.   | D.  | Tang.      |    |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 15° |          |     |          |    |          |     |           | 164° |  |  |  |  |  |  |   |
|-----|----------|-----|----------|----|----------|-----|-----------|------|--|--|--|--|--|--|---|
| /   | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  | / |
| 0   | 9.412006 | 785 | 9.984944 | 57 | 9.428052 | 842 | 10.571948 | 60   |  |  |  |  |  |  |   |
| 1   | 413467   | 784 | 984910   | 57 | 428558   | 841 | 571442    | 59   |  |  |  |  |  |  |   |
| 2   | 413938   | 783 | 984876   | 57 | 429062   | 840 | 570938    | 58   |  |  |  |  |  |  |   |
| 3   | 414408   | 783 | 984842   | 57 | 429566   | 839 | 570434    | 57   |  |  |  |  |  |  |   |
| 4   | 414878   | 782 | 984808   | 57 | 430070   | 838 | 569930    | 56   |  |  |  |  |  |  |   |
| 5   | 415347   | 781 | 984774   | 57 | 430573   | 838 | 569427    | 55   |  |  |  |  |  |  |   |
| 6   | 415815   | 780 | 984740   | 57 | 431075   | 837 | 568925    | 54   |  |  |  |  |  |  |   |
| 7   | 416283   | 779 | 984706   | 57 | 431577   | 836 | 568423    | 53   |  |  |  |  |  |  |   |
| 8   | 416751   | 778 | 984672   | 57 | 432079   | 835 | 567921    | 52   |  |  |  |  |  |  |   |
| 9   | 417217   | 777 | 984638   | 57 | 432580   | 834 | 567420    | 51   |  |  |  |  |  |  |   |
| 10  | 417684   | 776 | 984603   | 57 | 433080   | 833 | 566920    | 50   |  |  |  |  |  |  |   |
| 11  | 9.418150 | 775 | 9.984569 | 57 | 9.433580 | 832 | 10.566420 | 49   |  |  |  |  |  |  |   |
| 12  | 418615   | 774 | 984535   | 57 | 434080   | 832 | 565920    | 48   |  |  |  |  |  |  |   |
| 13  | 419079   | 773 | 984500   | 57 | 434579   | 831 | 565421    | 47   |  |  |  |  |  |  |   |
| 14  | 419544   | 773 | 984466   | 57 | 435078   | 830 | 564922    | 46   |  |  |  |  |  |  |   |
| 15  | 420007   | 772 | 984432   | 58 | 435576   | 829 | 564424    | 45   |  |  |  |  |  |  |   |
| 16  | 420470   | 771 | 984397   | 58 | 436073   | 828 | 563927    | 44   |  |  |  |  |  |  |   |
| 17  | 420933   | 770 | 984363   | 58 | 436570   | 828 | 563430    | 43   |  |  |  |  |  |  |   |
| 18  | 421395   | 769 | 984328   | 58 | 437067   | 827 | 562933    | 42   |  |  |  |  |  |  |   |
| 19  | 421857   | 768 | 984294   | 58 | 437563   | 826 | 562437    | 41   |  |  |  |  |  |  |   |
| 20  | 422318   | 767 | 984259   | 58 | 438059   | 825 | 561941    | 40   |  |  |  |  |  |  |   |
| 21  | 9.422778 | 767 | 9.984224 | 58 | 9.438554 | 824 | 10.561446 | 39   |  |  |  |  |  |  |   |
| 22  | 423238   | 766 | 984190   | 58 | 439048   | 823 | 560952    | 38   |  |  |  |  |  |  |   |
| 23  | 423697   | 765 | 984155   | 58 | 439543   | 823 | 560457    | 37   |  |  |  |  |  |  |   |
| 24  | 424156   | 764 | 984120   | 58 | 440036   | 822 | 559964    | 36   |  |  |  |  |  |  |   |
| 25  | 424615   | 763 | 984085   | 58 | 440529   | 821 | 559471    | 35   |  |  |  |  |  |  |   |
| 26  | 425073   | 762 | 984050   | 58 | 441022   | 820 | 558978    | 34   |  |  |  |  |  |  |   |
| 27  | 425530   | 761 | 984015   | 58 | 441514   | 819 | 558486    | 33   |  |  |  |  |  |  |   |
| 28  | 425987   | 760 | 983981   | 58 | 442006   | 819 | 557994    | 32   |  |  |  |  |  |  |   |
| 29  | 426443   | 760 | 983946   | 58 | 442497   | 818 | 557503    | 31   |  |  |  |  |  |  |   |
| 30  | 426899   | 759 | 983911   | 58 | 442988   | 817 | 557012    | 30   |  |  |  |  |  |  |   |
| 31  | 9.427354 | 758 | 9.983875 | 58 | 9.443479 | 816 | 10.556521 | 29   |  |  |  |  |  |  |   |
| 32  | 427809   | 757 | 983840   | 59 | 443968   | 816 | 556032    | 28   |  |  |  |  |  |  |   |
| 33  | 428263   | 756 | 983805   | 59 | 444458   | 815 | 555542    | 27   |  |  |  |  |  |  |   |
| 34  | 428717   | 755 | 983770   | 59 | 444947   | 814 | 555053    | 26   |  |  |  |  |  |  |   |
| 35  | 429170   | 754 | 983735   | 59 | 445435   | 813 | 554565    | 25   |  |  |  |  |  |  |   |
| 36  | 429623   | 753 | 983700   | 59 | 445923   | 812 | 554077    | 24   |  |  |  |  |  |  |   |
| 37  | 430075   | 752 | 983664   | 59 | 446411   | 812 | 553589    | 23   |  |  |  |  |  |  |   |
| 38  | 430527   | 752 | 983629   | 59 | 446898   | 811 | 553102    | 22   |  |  |  |  |  |  |   |
| 39  | 430978   | 751 | 983594   | 59 | 447384   | 810 | 552616    | 21   |  |  |  |  |  |  |   |
| 40  | 431429   | 750 | 983558   | 59 | 447870   | 809 | 552130    | 20   |  |  |  |  |  |  |   |
| 41  | 9.431879 | 749 | 9.983523 | 59 | 9.448356 | 809 | 10.551644 | 19   |  |  |  |  |  |  |   |
| 42  | 432329   | 749 | 983487   | 59 | 448841   | 808 | 551159    | 18   |  |  |  |  |  |  |   |
| 43  | 432778   | 748 | 983452   | 59 | 449326   | 807 | 550674    | 17   |  |  |  |  |  |  |   |
| 44  | 433226   | 747 | 983416   | 59 | 449810   | 806 | 550190    | 16   |  |  |  |  |  |  |   |
| 45  | 433675   | 746 | 983381   | 59 | 450294   | 806 | 549706    | 15   |  |  |  |  |  |  |   |
| 46  | 434122   | 745 | 983345   | 59 | 450777   | 805 | 549223    | 14   |  |  |  |  |  |  |   |
| 47  | 434569   | 744 | 983309   | 59 | 451260   | 804 | 548740    | 13   |  |  |  |  |  |  |   |
| 48  | 435016   | 744 | 983273   | 60 | 451743   | 803 | 548257    | 12   |  |  |  |  |  |  |   |
| 49  | 435462   | 743 | 983238   | 60 | 452225   | 802 | 547775    | 11   |  |  |  |  |  |  |   |
| 50  | 435908   | 742 | 983202   | 60 | 452706   | 802 | 547294    | 10   |  |  |  |  |  |  |   |
| 51  | 9.436353 | 741 | 9.983166 | 60 | 9.453187 | 801 | 10.546813 | 9    |  |  |  |  |  |  |   |
| 52  | 436798   | 740 | 983130   | 60 | 453668   | 800 | 546332    | 8    |  |  |  |  |  |  |   |
| 53  | 437242   | 740 | 983094   | 60 | 454148   | 799 | 545852    | 7    |  |  |  |  |  |  |   |
| 54  | 437686   | 739 | 983058   | 60 | 454628   | 799 | 545372    | 6    |  |  |  |  |  |  |   |
| 55  | 438129   | 738 | 983022   | 60 | 455107   | 798 | 544893    | 5    |  |  |  |  |  |  |   |
| 56  | 438572   | 737 | 982986   | 60 | 455586   | 797 | 544414    | 4    |  |  |  |  |  |  |   |
| 57  | 439014   | 736 | 982950   | 60 | 456064   | 796 | 543936    | 3    |  |  |  |  |  |  |   |
| 58  | 439456   | 736 | 982914   | 60 | 456542   | 796 | 543458    | 2    |  |  |  |  |  |  |   |
| 59  | 439897   | 735 | 982878   | 60 | 457019   | 795 | 542981    | 1    |  |  |  |  |  |  |   |
| 60  | 440338   | 734 | 982842   | 60 | 457496   | 794 | 542504    | 0    |  |  |  |  |  |  |   |
| /   | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  | / |

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|    | sin.     | D.  | Cont.    | D. | Tang.    | D.  | Contang.  |    |
|----|----------|-----|----------|----|----------|-----|-----------|----|
| 0  | 9.669134 | 714 | 9.978462 | 60 | 9.457496 | 794 | 10.542504 | 60 |
| 1  | 669778   | 715 | 9.978605 | 60 | 457973   | 793 | 542027    | 59 |
| 2  | 670422   | 716 | 9.978749 | 61 | 458449   | 793 | 541551    | 58 |
| 3  | 671066   | 717 | 9.978892 | 61 | 458925   | 792 | 541075    | 57 |
| 4  | 671710   | 718 | 9.979036 | 61 | 459400   | 791 | 540600    | 56 |
| 5  | 672354   | 719 | 9.979179 | 61 | 459875   | 790 | 540125    | 55 |
| 6  | 672998   | 720 | 9.979322 | 61 | 460349   | 789 | 539651    | 54 |
| 7  | 673642   | 721 | 9.979465 | 61 | 460823   | 789 | 539177    | 53 |
| 8  | 674286   | 722 | 9.979608 | 61 | 461297   | 788 | 538703    | 52 |
| 9  | 674930   | 723 | 9.979751 | 61 | 461770   | 788 | 538230    | 51 |
| 10 | 675574   | 724 | 9.979894 | 61 | 462243   | 787 | 537758    | 50 |
| 11 | 9.676218 | 725 | 9.980037 | 61 | 9.462715 | 786 | 10.537285 | 49 |
| 12 | 676862   | 726 | 9.980180 | 61 | 463186   | 785 | 536814    | 48 |
| 13 | 677506   | 727 | 9.980323 | 61 | 463658   | 785 | 536342    | 47 |
| 14 | 678150   | 728 | 9.980466 | 61 | 464128   | 784 | 535872    | 46 |
| 15 | 678794   | 729 | 9.980609 | 61 | 464599   | 783 | 535401    | 45 |
| 16 | 679438   | 730 | 9.980752 | 61 | 465069   | 783 | 534931    | 44 |
| 17 | 680082   | 731 | 9.980895 | 62 | 465539   | 782 | 534461    | 43 |
| 18 | 680726   | 732 | 9.981038 | 62 | 466008   | 781 | 533992    | 42 |
| 19 | 681370   | 733 | 9.981181 | 62 | 466477   | 780 | 533523    | 41 |
| 20 | 682014   | 734 | 9.981324 | 62 | 466945   | 780 | 533055    | 40 |
| 21 | 9.682658 | 735 | 9.981467 | 62 | 9.467413 | 779 | 10.532587 | 39 |
| 22 | 683302   | 736 | 9.981610 | 62 | 467880   | 778 | 532120    | 38 |
| 23 | 683946   | 737 | 9.981753 | 62 | 468347   | 778 | 531653    | 37 |
| 24 | 684590   | 738 | 9.981896 | 62 | 468814   | 777 | 531186    | 36 |
| 25 | 685234   | 739 | 9.982039 | 62 | 469280   | 776 | 530720    | 35 |
| 26 | 685878   | 740 | 9.982182 | 62 | 469746   | 775 | 530254    | 34 |
| 27 | 686522   | 741 | 9.982325 | 62 | 470211   | 775 | 529789    | 33 |
| 28 | 687166   | 742 | 9.982468 | 62 | 470676   | 774 | 529324    | 32 |
| 29 | 687810   | 743 | 9.982611 | 62 | 471141   | 773 | 528859    | 31 |
| 30 | 688454   | 744 | 9.982754 | 62 | 471605   | 773 | 528395    | 30 |
| 31 | 9.689098 | 745 | 9.982897 | 63 | 9.472069 | 772 | 10.527931 | 29 |
| 32 | 689742   | 746 | 9.983040 | 63 | 472532   | 771 | 527468    | 28 |
| 33 | 690386   | 747 | 9.983183 | 63 | 472995   | 771 | 527005    | 27 |
| 34 | 691030   | 748 | 9.983326 | 63 | 473457   | 770 | 526543    | 26 |
| 35 | 691674   | 749 | 9.983469 | 63 | 473919   | 769 | 526081    | 25 |
| 36 | 692318   | 750 | 9.983612 | 63 | 474381   | 769 | 525619    | 24 |
| 37 | 692962   | 751 | 9.983755 | 63 | 474842   | 768 | 525158    | 23 |
| 38 | 693606   | 752 | 9.983898 | 63 | 475303   | 767 | 524697    | 22 |
| 39 | 694250   | 753 | 9.984041 | 63 | 475763   | 767 | 524237    | 21 |
| 40 | 694894   | 754 | 9.984184 | 63 | 476223   | 766 | 523777    | 20 |
| 41 | 9.695538 | 755 | 9.984327 | 63 | 9.476683 | 765 | 10.523317 | 19 |
| 42 | 696182   | 756 | 9.984470 | 63 | 477142   | 765 | 522858    | 18 |
| 43 | 696826   | 757 | 9.984613 | 63 | 477601   | 764 | 522399    | 17 |
| 44 | 697470   | 758 | 9.984756 | 63 | 478059   | 763 | 521941    | 16 |
| 45 | 698114   | 759 | 9.984899 | 63 | 478517   | 763 | 521483    | 15 |
| 46 | 698758   | 760 | 9.985042 | 64 | 478975   | 762 | 521025    | 14 |
| 47 | 699402   | 761 | 9.985185 | 64 | 479432   | 761 | 520568    | 13 |
| 48 | 700046   | 762 | 9.985328 | 64 | 479889   | 761 | 520111    | 12 |
| 49 | 700690   | 763 | 9.985471 | 64 | 480345   | 760 | 519655    | 11 |
| 50 | 701334   | 764 | 9.985614 | 64 | 480801   | 759 | 519199    | 10 |
| 51 | 9.701978 | 765 | 9.985757 | 64 | 9.481257 | 759 | 10.518743 | 9  |
| 52 | 702622   | 766 | 9.985900 | 64 | 481712   | 758 | 518288    | 8  |
| 53 | 703266   | 767 | 9.986043 | 64 | 482167   | 757 | 517833    | 7  |
| 54 | 703910   | 768 | 9.986186 | 64 | 482621   | 757 | 517379    | 6  |
| 55 | 704554   | 769 | 9.986329 | 64 | 483075   | 756 | 516925    | 5  |
| 56 | 705198   | 770 | 9.986472 | 64 | 483529   | 755 | 516471    | 4  |
| 57 | 705842   | 771 | 9.986615 | 64 | 483982   | 755 | 516018    | 3  |
| 58 | 706486   | 772 | 9.986758 | 64 | 484435   | 754 | 515565    | 2  |
| 59 | 707130   | 773 | 9.986901 | 64 | 484887   | 753 | 515113    | 1  |
| 60 | 707774   | 774 | 9.987044 | 64 | 485339   | 753 | 514661    | 0  |
|    | Contang. | D.  | sin.     | D. | Contang. | D.  | Tang.     |    |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 17° |          |     |          |    |          |     |           | 163° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9.465935 | 688 | 9.980526 | 64 | 9.485339 | 755 | 10.514661 | 60   |  |  |  |  |  |  |  |
| 1   | 466348   | 688 | 980558   | 64 | 485791   | 752 | 514209    | 59   |  |  |  |  |  |  |  |
| 2   | 466761   | 687 | 980519   | 65 | 486242   | 751 | 513758    | 58   |  |  |  |  |  |  |  |
| 3   | 467173   | 686 | 980480   | 65 | 486693   | 751 | 513307    | 57   |  |  |  |  |  |  |  |
| 4   | 467585   | 685 | 980442   | 65 | 487143   | 750 | 512857    | 56   |  |  |  |  |  |  |  |
| 5   | 467996   | 685 | 980403   | 65 | 487593   | 749 | 512407    | 55   |  |  |  |  |  |  |  |
| 6   | 468407   | 684 | 980364   | 65 | 488043   | 749 | 511957    | 54   |  |  |  |  |  |  |  |
| 7   | 468817   | 683 | 980325   | 65 | 488492   | 748 | 511508    | 53   |  |  |  |  |  |  |  |
| 8   | 469227   | 683 | 980286   | 65 | 488941   | 747 | 511059    | 52   |  |  |  |  |  |  |  |
| 9   | 469637   | 682 | 980247   | 65 | 489390   | 747 | 510610    | 51   |  |  |  |  |  |  |  |
| 10  | 470046   | 681 | 980208   | 65 | 489838   | 746 | 510162    | 50   |  |  |  |  |  |  |  |
| 11  | 9.470455 | 680 | 9.980169 | 65 | 9.490286 | 746 | 10.509714 | 49   |  |  |  |  |  |  |  |
| 12  | 470863   | 680 | 980130   | 65 | 490733   | 745 | 509267    | 48   |  |  |  |  |  |  |  |
| 13  | 471271   | 679 | 980091   | 65 | 491180   | 744 | 508820    | 47   |  |  |  |  |  |  |  |
| 14  | 471679   | 678 | 980052   | 65 | 491627   | 744 | 508373    | 46   |  |  |  |  |  |  |  |
| 15  | 472086   | 678 | 980012   | 65 | 492073   | 743 | 507927    | 45   |  |  |  |  |  |  |  |
| 16  | 472492   | 677 | 979973   | 65 | 492519   | 743 | 507481    | 44   |  |  |  |  |  |  |  |
| 17  | 472898   | 676 | 979934   | 66 | 492965   | 742 | 507035    | 43   |  |  |  |  |  |  |  |
| 18  | 473304   | 676 | 979895   | 66 | 493410   | 741 | 506590    | 42   |  |  |  |  |  |  |  |
| 19  | 473710   | 675 | 979855   | 66 | 493854   | 740 | 506146    | 41   |  |  |  |  |  |  |  |
| 20  | 474115   | 674 | 979816   | 66 | 494299   | 740 | 505701    | 40   |  |  |  |  |  |  |  |
| 21  | 9.474519 | 674 | 9.979776 | 66 | 9.494743 | 740 | 10.505257 | 39   |  |  |  |  |  |  |  |
| 22  | 474923   | 673 | 979737   | 66 | 495186   | 739 | 504814    | 38   |  |  |  |  |  |  |  |
| 23  | 475327   | 672 | 979697   | 66 | 495630   | 738 | 504370    | 37   |  |  |  |  |  |  |  |
| 24  | 475730   | 672 | 979658   | 66 | 496073   | 737 | 503927    | 36   |  |  |  |  |  |  |  |
| 25  | 476133   | 671 | 979618   | 66 | 496515   | 737 | 503483    | 35   |  |  |  |  |  |  |  |
| 26  | 476536   | 670 | 979579   | 66 | 496957   | 736 | 503043    | 34   |  |  |  |  |  |  |  |
| 27  | 476938   | 669 | 979539   | 66 | 497399   | 736 | 502601    | 33   |  |  |  |  |  |  |  |
| 28  | 477340   | 669 | 979499   | 66 | 497841   | 735 | 502159    | 32   |  |  |  |  |  |  |  |
| 29  | 477741   | 668 | 979459   | 66 | 498282   | 734 | 501718    | 31   |  |  |  |  |  |  |  |
| 30  | 478142   | 667 | 979420   | 66 | 498722   | 734 | 501278    | 30   |  |  |  |  |  |  |  |
| 31  | 9.478542 | 667 | 9.979380 | 66 | 9.499163 | 733 | 10.500837 | 29   |  |  |  |  |  |  |  |
| 32  | 478942   | 666 | 979340   | 66 | 499603   | 733 | 500397    | 28   |  |  |  |  |  |  |  |
| 33  | 479342   | 665 | 979300   | 67 | 500042   | 732 | 499958    | 27   |  |  |  |  |  |  |  |
| 34  | 479741   | 665 | 979260   | 67 | 500481   | 731 | 499519    | 26   |  |  |  |  |  |  |  |
| 35  | 480140   | 664 | 979220   | 67 | 500920   | 731 | 499080    | 25   |  |  |  |  |  |  |  |
| 36  | 480539   | 663 | 979180   | 67 | 501359   | 730 | 498641    | 24   |  |  |  |  |  |  |  |
| 37  | 480937   | 663 | 979140   | 67 | 501797   | 730 | 498203    | 23   |  |  |  |  |  |  |  |
| 38  | 481334   | 662 | 979100   | 67 | 502235   | 729 | 497765    | 22   |  |  |  |  |  |  |  |
| 39  | 481731   | 661 | 979059   | 67 | 502672   | 728 | 497328    | 21   |  |  |  |  |  |  |  |
| 40  | 482128   | 661 | 979019   | 67 | 503109   | 728 | 496891    | 20   |  |  |  |  |  |  |  |
| 41  | 9.482525 | 660 | 9.978979 | 67 | 9.503546 | 727 | 10.496454 | 19   |  |  |  |  |  |  |  |
| 42  | 482921   | 659 | 978939   | 67 | 503982   | 727 | 496018    | 18   |  |  |  |  |  |  |  |
| 43  | 483316   | 659 | 978898   | 67 | 504418   | 726 | 495582    | 17   |  |  |  |  |  |  |  |
| 44  | 483712   | 658 | 978858   | 67 | 504854   | 725 | 495146    | 16   |  |  |  |  |  |  |  |
| 45  | 484107   | 657 | 978817   | 67 | 505289   | 725 | 494711    | 15   |  |  |  |  |  |  |  |
| 46  | 484501   | 657 | 978777   | 67 | 505724   | 724 | 494276    | 14   |  |  |  |  |  |  |  |
| 47  | 484895   | 656 | 978737   | 67 | 506159   | 724 | 493841    | 13   |  |  |  |  |  |  |  |
| 48  | 485289   | 655 | 978696   | 68 | 506593   | 723 | 493407    | 12   |  |  |  |  |  |  |  |
| 49  | 485682   | 655 | 978655   | 68 | 507027   | 722 | 492973    | 11   |  |  |  |  |  |  |  |
| 50  | 486075   | 654 | 978615   | 68 | 507460   | 722 | 492540    | 10   |  |  |  |  |  |  |  |
| 51  | 9.486467 | 653 | 9.978574 | 68 | 9.507803 | 721 | 10.492107 | 9    |  |  |  |  |  |  |  |
| 52  | 486860   | 653 | 978533   | 68 | 508236   | 721 | 491674    | 8    |  |  |  |  |  |  |  |
| 53  | 487251   | 652 | 978493   | 68 | 508679   | 720 | 491241    | 7    |  |  |  |  |  |  |  |
| 54  | 487643   | 651 | 978452   | 68 | 509119   | 719 | 490809    | 6    |  |  |  |  |  |  |  |
| 55  | 488034   | 651 | 978411   | 68 | 509562   | 719 | 490378    | 5    |  |  |  |  |  |  |  |
| 56  | 488424   | 650 | 978370   | 68 | 510004   | 718 | 489946    | 4    |  |  |  |  |  |  |  |
| 57  | 488814   | 650 | 978329   | 68 | 510445   | 718 | 489515    | 3    |  |  |  |  |  |  |  |
| 58  | 489204   | 649 | 978288   | 68 | 510886   | 717 | 489084    | 2    |  |  |  |  |  |  |  |
| 59  | 489593   | 648 | 978247   | 68 | 511326   | 716 | 488654    | 1    |  |  |  |  |  |  |  |
| 60  | 489982   | 648 | 978206   | 68 | 511766   | 716 | 488224    | 0    |  |  |  |  |  |  |  |
| /   | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

107°

72°

|    | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   |    |
|----|----------|-----|----------|----|----------|-----|-----------|----|
| 0  | 9.489982 | 648 | 9.978206 | 68 | 9.511776 | 716 | 10.488224 | 60 |
| 1  | 490371   | 648 | 978165   | 68 | 512206   | 716 | 487794    | 59 |
| 2  | 490759   | 647 | 978124   | 68 | 512635   | 715 | 487365    | 58 |
| 3  | 491147   | 646 | 978083   | 69 | 513064   | 714 | 486936    | 57 |
| 4  | 491535   | 646 | 978042   | 69 | 513493   | 714 | 486507    | 56 |
| 5  | 491922   | 645 | 978001   | 69 | 513921   | 713 | 486079    | 55 |
| 6  | 492308   | 644 | 977959   | 69 | 514349   | 713 | 485651    | 54 |
| 7  | 492695   | 644 | 977918   | 59 | 514777   | 712 | 485223    | 53 |
| 8  | 493081   | 643 | 977877   | 69 | 515204   | 712 | 484796    | 52 |
| 9  | 493466   | 642 | 977835   | 69 | 515631   | 711 | 484369    | 51 |
| 10 | 493851   | 642 | 977794   | 69 | 516057   | 710 | 483943    | 50 |
| 11 | 9.494236 | 641 | 9.977752 | 69 | 9.516484 | 710 | 10.483516 | 49 |
| 12 | 494621   | 641 | 977711   | 69 | 516910   | 709 | 483090    | 48 |
| 13 | 495005   | 640 | 977669   | 69 | 517335   | 709 | 482665    | 47 |
| 14 | 495388   | 639 | 977628   | 69 | 517761   | 708 | 482239    | 46 |
| 15 | 495772   | 639 | 977586   | 69 | 518186   | 708 | 481814    | 45 |
| 16 | 496154   | 638 | 977544   | 70 | 518610   | 707 | 481390    | 44 |
| 17 | 496537   | 637 | 977503   | 70 | 519034   | 706 | 480966    | 43 |
| 18 | 496919   | 637 | 977461   | 70 | 519458   | 706 | 480542    | 42 |
| 19 | 497301   | 636 | 977419   | 70 | 519882   | 705 | 480118    | 41 |
| 20 | 497682   | 636 | 977377   | 70 | 520305   | 705 | 479695    | 40 |
| 21 | 9.498064 | 635 | 9.977335 | 70 | 9.520728 | 704 | 10.479272 | 39 |
| 22 | 498444   | 634 | 977293   | 70 | 521151   | 703 | 478849    | 38 |
| 23 | 498825   | 634 | 977251   | 70 | 521573   | 703 | 478427    | 37 |
| 24 | 499204   | 633 | 977209   | 70 | 521995   | 703 | 478005    | 36 |
| 25 | 499584   | 632 | 977167   | 70 | 522417   | 702 | 477583    | 35 |
| 26 | 499963   | 632 | 977125   | 70 | 522838   | 702 | 477162    | 34 |
| 27 | 500342   | 631 | 977083   | 70 | 523259   | 701 | 476741    | 33 |
| 28 | 500721   | 631 | 977041   | 70 | 523680   | 701 | 476320    | 32 |
| 29 | 501099   | 630 | 976999   | 70 | 524100   | 700 | 475900    | 31 |
| 30 | 501476   | 629 | 976957   | 70 | 524520   | 699 | 475480    | 30 |
| 31 | 9.501854 | 629 | 9.976914 | 70 | 9.524940 | 699 | 10.475060 | 29 |
| 32 | 502231   | 628 | 976872   | 71 | 525359   | 698 | 474641    | 28 |
| 33 | 502607   | 628 | 976830   | 71 | 525778   | 698 | 474222    | 27 |
| 34 | 502984   | 627 | 976787   | 71 | 526197   | 697 | 473803    | 26 |
| 35 | 503360   | 626 | 976745   | 71 | 526615   | 697 | 473385    | 25 |
| 36 | 503735   | 626 | 976702   | 71 | 527033   | 696 | 472967    | 24 |
| 37 | 504110   | 625 | 976660   | 71 | 527451   | 696 | 472549    | 23 |
| 38 | 504485   | 625 | 976617   | 71 | 527868   | 695 | 472132    | 22 |
| 39 | 504860   | 624 | 976574   | 71 | 528285   | 695 | 471715    | 21 |
| 40 | 505234   | 623 | 976532   | 71 | 528702   | 694 | 471298    | 20 |
| 41 | 9.505608 | 623 | 9.976489 | 71 | 9.529119 | 693 | 10.470881 | 19 |
| 42 | 505981   | 622 | 976446   | 71 | 529535   | 693 | 470465    | 18 |
| 43 | 506354   | 622 | 976404   | 71 | 529951   | 693 | 470049    | 17 |
| 44 | 506727   | 621 | 976361   | 71 | 530366   | 692 | 469634    | 16 |
| 45 | 507099   | 620 | 976318   | 71 | 530781   | 691 | 469219    | 15 |
| 46 | 507471   | 620 | 976275   | 71 | 531196   | 691 | 468804    | 14 |
| 47 | 507843   | 619 | 976232   | 72 | 531611   | 690 | 468389    | 13 |
| 48 | 508214   | 619 | 976189   | 72 | 532025   | 690 | 467975    | 12 |
| 49 | 508585   | 618 | 976146   | 72 | 532439   | 689 | 467561    | 11 |
| 50 | 508956   | 618 | 976103   | 72 | 532853   | 689 | 467147    | 10 |
| 51 | 9.509326 | 617 | 9.976060 | 72 | 9.533266 | 688 | 10.466734 | 9  |
| 52 | 509696   | 616 | 976017   | 72 | 533679   | 688 | 466321    | 8  |
| 53 | 510065   | 616 | 975974   | 72 | 534092   | 687 | 465908    | 7  |
| 54 | 510434   | 615 | 975930   | 72 | 534504   | 687 | 465496    | 6  |
| 55 | 510803   | 615 | 975887   | 72 | 534916   | 686 | 465084    | 5  |
| 56 | 511172   | 614 | 975844   | 72 | 535328   | 686 | 464672    | 4  |
| 57 | 511540   | 613 | 975800   | 72 | 535739   | 685 | 464261    | 3  |
| 58 | 511907   | 613 | 975757   | 72 | 536150   | 685 | 463850    | 2  |
| 59 | 512275   | 612 | 975714   | 72 | 536561   | 684 | 463439    | 1  |
| 60 | 512642   | 612 | 975670   | 72 | 536972   | 684 | 463028    | 0  |
|    | Sine.    | D.  | Cosine.  | D. | Cotang.  | D.  | Tang.     |    |

| TABLE II. LOGARITHMIC SINES, TANGENTS, ETC. |          |     |          |    |          |     |           |      |  |
|---------------------------------------------|----------|-----|----------|----|----------|-----|-----------|------|--|
| 19°                                         |          |     |          |    |          |     |           | 180° |  |
| '                                           | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | '    |  |
| 0                                           | 9.512642 | 612 | 9.975670 | 73 | 9.536972 | 684 | 10.463028 | 60   |  |
| 1                                           | 513009   | 611 | 975627   | 72 | 537382   | 683 | 462618    | 59   |  |
| 2                                           | 513375   | 611 | 975583   | 73 | 537792   | 683 | 462208    | 58   |  |
| 3                                           | 513741   | 610 | 975539   | 73 | 538202   | 682 | 461798    | 57   |  |
| 4                                           | 514107   | 609 | 975496   | 73 | 538611   | 682 | 461389    | 56   |  |
| 5                                           | 514472   | 609 | 975452   | 73 | 539020   | 681 | 460980    | 55   |  |
| 6                                           | 514837   | 608 | 975408   | 73 | 539429   | 681 | 460571    | 54   |  |
| 7                                           | 515202   | 608 | 975365   | 73 | 539837   | 680 | 460163    | 53   |  |
| 8                                           | 515566   | 607 | 975321   | 73 | 540245   | 680 | 459755    | 52   |  |
| 9                                           | 515930   | 607 | 975277   | 73 | 540653   | 679 | 459347    | 51   |  |
| 10                                          | 516294   | 606 | 975233   | 73 | 541061   | 679 | 458939    | 50   |  |
| 11                                          | 9.516657 | 605 | 9.975189 | 73 | 9.541468 | 678 | 10.458532 | 49   |  |
| 12                                          | 517020   | 605 | 975145   | 73 | 541875   | 678 | 458125    | 48   |  |
| 13                                          | 517382   | 604 | 975101   | 73 | 542281   | 677 | 457719    | 47   |  |
| 14                                          | 517745   | 604 | 975057   | 73 | 542688   | 677 | 457312    | 46   |  |
| 15                                          | 518107   | 603 | 975013   | 73 | 543094   | 676 | 456906    | 45   |  |
| 16                                          | 518468   | 603 | 974969   | 74 | 543499   | 676 | 456501    | 44   |  |
| 17                                          | 518829   | 602 | 974925   | 74 | 543905   | 675 | 456095    | 43   |  |
| 18                                          | 519190   | 601 | 974880   | 74 | 544310   | 675 | 455690    | 42   |  |
| 19                                          | 519551   | 601 | 974836   | 74 | 544715   | 674 | 455285    | 41   |  |
| 20                                          | 519911   | 600 | 974792   | 74 | 545119   | 674 | 454881    | 40   |  |
| 21                                          | 9.520271 | 600 | 9.974748 | 74 | 9.545524 | 673 | 10.454476 | 39   |  |
| 22                                          | 520631   | 599 | 974703   | 74 | 545928   | 673 | 454072    | 38   |  |
| 23                                          | 520990   | 599 | 974659   | 74 | 546331   | 672 | 453669    | 37   |  |
| 24                                          | 521349   | 598 | 974614   | 74 | 546735   | 672 | 453265    | 36   |  |
| 25                                          | 521707   | 598 | 974570   | 74 | 547138   | 671 | 452862    | 35   |  |
| 26                                          | 522066   | 597 | 974525   | 74 | 547540   | 671 | 452460    | 34   |  |
| 27                                          | 522424   | 596 | 974481   | 74 | 547943   | 670 | 452057    | 33   |  |
| 28                                          | 522781   | 596 | 974436   | 74 | 548345   | 670 | 451655    | 32   |  |
| 29                                          | 523138   | 595 | 974391   | 74 | 548747   | 669 | 451253    | 31   |  |
| 30                                          | 523495   | 595 | 974347   | 75 | 549149   | 669 | 450851    | 30   |  |
| 31                                          | 9.523852 | 594 | 9.974302 | 75 | 9.549550 | 668 | 10.450450 | 29   |  |
| 32                                          | 524208   | 594 | 974257   | 75 | 549951   | 668 | 450049    | 28   |  |
| 33                                          | 524564   | 593 | 974212   | 75 | 550352   | 667 | 449648    | 27   |  |
| 34                                          | 524920   | 593 | 974167   | 75 | 550752   | 667 | 449248    | 26   |  |
| 35                                          | 525275   | 592 | 974122   | 75 | 551153   | 666 | 448847    | 25   |  |
| 36                                          | 525630   | 591 | 974077   | 75 | 551552   | 666 | 448448    | 24   |  |
| 37                                          | 525984   | 591 | 974032   | 75 | 551952   | 665 | 448048    | 23   |  |
| 38                                          | 526339   | 590 | 973987   | 75 | 552351   | 665 | 447649    | 22   |  |
| 39                                          | 526693   | 590 | 973942   | 75 | 552750   | 665 | 447250    | 21   |  |
| 40                                          | 527046   | 589 | 973897   | 75 | 553149   | 664 | 446851    | 20   |  |
| 41                                          | 9.527400 | 589 | 9.973852 | 75 | 9.553548 | 664 | 10.446452 | 19   |  |
| 42                                          | 527753   | 588 | 973807   | 75 | 553946   | 663 | 446054    | 18   |  |
| 43                                          | 528105   | 588 | 973761   | 75 | 554344   | 663 | 445656    | 17   |  |
| 44                                          | 528458   | 587 | 973716   | 76 | 554741   | 662 | 445259    | 16   |  |
| 45                                          | 528810   | 587 | 973671   | 76 | 555139   | 662 | 444861    | 15   |  |
| 46                                          | 529161   | 586 | 973625   | 76 | 555536   | 661 | 444464    | 14   |  |
| 47                                          | 529513   | 586 | 973580   | 76 | 555933   | 661 | 444067    | 13   |  |
| 48                                          | 529864   | 585 | 973535   | 76 | 556329   | 660 | 443671    | 12   |  |
| 49                                          | 530215   | 585 | 973489   | 76 | 556725   | 660 | 443275    | 11   |  |
| 50                                          | 530565   | 584 | 973444   | 76 | 557121   | 659 | 442879    | 10   |  |
| 51                                          | 9.530915 | 584 | 9.973398 | 76 | 9.557517 | 659 | 10.442483 | 9    |  |
| 52                                          | 531265   | 583 | 973352   | 76 | 557913   | 659 | 442087    | 8    |  |
| 53                                          | 531614   | 582 | 973307   | 76 | 558308   | 658 | 441692    | 7    |  |
| 54                                          | 531963   | 582 | 973261   | 76 | 558703   | 658 | 441297    | 6    |  |
| 55                                          | 532312   | 581 | 973215   | 76 | 559097   | 657 | 440903    | 5    |  |
| 56                                          | 532661   | 581 | 973169   | 76 | 559491   | 657 | 440509    | 4    |  |
| 57                                          | 533009   | 580 | 973124   | 76 | 559885   | 656 | 440115    | 3    |  |
| 58                                          | 533357   | 580 | 973078   | 76 | 560279   | 656 | 439721    | 2    |  |
| 59                                          | 533704   | 579 | 973032   | 77 | 560673   | 655 | 439327    | 1    |  |
| 60                                          | 534052   | 578 | 972986   | 77 | 561066   | 655 | 438934    | 0    |  |
| '                                           | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | '    |  |
| 109°                                        |          |     |          |    |          |     |           | 70°  |  |

| LOGARITHMIC SINES, TANGENTS, ETC. TABLE II. |          |     |          |    |          |     |           |    |  |
|---------------------------------------------|----------|-----|----------|----|----------|-----|-----------|----|--|
| 20°                                         |          |     |          |    | 180°     |     |           |    |  |
| /                                           | Sine.    | D.  | Cotang.  | D. | Tang.    | D.  | Cotang.   | /  |  |
| 0                                           | 9-534052 | 578 | 9-972986 | 77 | 9-561066 | 655 | 10-438934 | 60 |  |
| 1                                           | 534309   | 577 | 972940   | 77 | 561459   | 654 | 438541    | 59 |  |
| 2                                           | 534745   | 577 | 972894   | 77 | 561851   | 654 | 438149    | 58 |  |
| 3                                           | 535092   | 577 | 972848   | 77 | 562244   | 653 | 437756    | 57 |  |
| 4                                           | 535438   | 576 | 972802   | 77 | 562636   | 653 | 437364    | 56 |  |
| 5                                           | 535783   | 576 | 972755   | 77 | 563028   | 653 | 436972    | 55 |  |
| 6                                           | 536129   | 575 | 972709   | 77 | 563419   | 652 | 436581    | 54 |  |
| 7                                           | 536474   | 574 | 972663   | 77 | 563811   | 652 | 436189    | 53 |  |
| 8                                           | 536818   | 574 | 972617   | 77 | 564202   | 651 | 435798    | 52 |  |
| 9                                           | 537163   | 573 | 972570   | 77 | 564593   | 651 | 435407    | 51 |  |
| 10                                          | 537507   | 573 | 972524   | 77 | 564983   | 650 | 435017    | 50 |  |
| 11                                          | 9-537851 | 572 | 9-972478 | 77 | 9-565373 | 650 | 10-434627 | 49 |  |
| 12                                          | 538194   | 572 | 972431   | 76 | 565763   | 649 | 434237    | 48 |  |
| 13                                          | 538538   | 571 | 972385   | 76 | 566153   | 649 | 433847    | 47 |  |
| 14                                          | 538880   | 571 | 972338   | 76 | 566542   | 649 | 433458    | 46 |  |
| 15                                          | 539223   | 570 | 972291   | 76 | 566932   | 648 | 433068    | 45 |  |
| 16                                          | 539565   | 570 | 972245   | 76 | 567320   | 648 | 432680    | 44 |  |
| 17                                          | 539907   | 569 | 972198   | 76 | 567709   | 647 | 432291    | 43 |  |
| 18                                          | 540249   | 569 | 972151   | 76 | 568098   | 647 | 431902    | 42 |  |
| 19                                          | 540590   | 568 | 972105   | 76 | 568486   | 646 | 431514    | 41 |  |
| 20                                          | 540931   | 568 | 972058   | 76 | 568873   | 646 | 431127    | 40 |  |
| 21                                          | 9-541272 | 567 | 9-972011 | 76 | 9-569261 | 645 | 10-430739 | 39 |  |
| 22                                          | 541613   | 567 | 971964   | 76 | 569648   | 645 | 430352    | 38 |  |
| 23                                          | 541953   | 566 | 971917   | 76 | 570035   | 645 | 429965    | 37 |  |
| 24                                          | 542293   | 566 | 971870   | 76 | 570422   | 644 | 429578    | 36 |  |
| 25                                          | 542632   | 565 | 971823   | 76 | 570809   | 644 | 429191    | 35 |  |
| 26                                          | 542971   | 565 | 971776   | 76 | 571195   | 643 | 428805    | 34 |  |
| 27                                          | 543310   | 564 | 971729   | 75 | 571581   | 643 | 428419    | 33 |  |
| 28                                          | 543649   | 564 | 971682   | 75 | 571967   | 642 | 428033    | 32 |  |
| 29                                          | 543987   | 563 | 971635   | 75 | 572352   | 642 | 427648    | 31 |  |
| 30                                          | 544325   | 563 | 971588   | 75 | 572738   | 642 | 427262    | 30 |  |
| 31                                          | 9-544663 | 562 | 9-971540 | 75 | 9-573123 | 641 | 10-426877 | 29 |  |
| 32                                          | 545000   | 562 | 971493   | 75 | 573507   | 641 | 426493    | 28 |  |
| 33                                          | 545338   | 561 | 971446   | 75 | 573892   | 640 | 426108    | 27 |  |
| 34                                          | 545674   | 561 | 971398   | 75 | 574276   | 640 | 425724    | 26 |  |
| 35                                          | 546011   | 560 | 971351   | 75 | 574660   | 639 | 425340    | 25 |  |
| 36                                          | 546347   | 560 | 971303   | 75 | 575044   | 639 | 424956    | 24 |  |
| 37                                          | 546683   | 559 | 971256   | 75 | 575427   | 639 | 424573    | 23 |  |
| 38                                          | 547019   | 559 | 971208   | 75 | 575810   | 638 | 424190    | 22 |  |
| 39                                          | 547354   | 558 | 971161   | 75 | 576193   | 638 | 423807    | 21 |  |
| 40                                          | 547689   | 558 | 971113   | 75 | 576576   | 637 | 423424    | 20 |  |
| 41                                          | 9-548024 | 557 | 9-971066 | 80 | 9-576959 | 637 | 10-423041 | 19 |  |
| 42                                          | 548359   | 557 | 971018   | 80 | 577341   | 636 | 422659    | 18 |  |
| 43                                          | 548693   | 556 | 970970   | 80 | 577723   | 636 | 422277    | 17 |  |
| 44                                          | 549027   | 556 | 970922   | 80 | 578104   | 636 | 421890    | 16 |  |
| 45                                          | 549360   | 555 | 970874   | 80 | 578486   | 635 | 421514    | 15 |  |
| 46                                          | 549693   | 555 | 970827   | 80 | 578867   | 635 | 421133    | 14 |  |
| 47                                          | 550026   | 554 | 970779   | 80 | 579248   | 634 | 420752    | 13 |  |
| 48                                          | 550359   | 554 | 970731   | 80 | 579629   | 634 | 420371    | 12 |  |
| 49                                          | 550692   | 553 | 970683   | 80 | 580009   | 634 | 419991    | 11 |  |
| 50                                          | 551024   | 553 | 970635   | 80 | 580389   | 633 | 419611    | 10 |  |
| 51                                          | 9-551356 | 552 | 9-970586 | 80 | 9-580769 | 633 | 10-419231 | 9  |  |
| 52                                          | 551687   | 552 | 970538   | 80 | 581149   | 632 | 418851    | 8  |  |
| 53                                          | 552018   | 552 | 970490   | 80 | 581528   | 632 | 418472    | 7  |  |
| 54                                          | 552349   | 551 | 970442   | 80 | 581907   | 632 | 418093    | 6  |  |
| 55                                          | 552680   | 551 | 970394   | 80 | 582286   | 631 | 417714    | 5  |  |
| 56                                          | 553010   | 550 | 970345   | 81 | 582665   | 631 | 417335    | 4  |  |
| 57                                          | 553341   | 550 | 970297   | 81 | 583044   | 630 | 416956    | 3  |  |
| 58                                          | 553670   | 549 | 970249   | 81 | 583422   | 630 | 416578    | 2  |  |
| 59                                          | 554000   | 549 | 970200   | 81 | 583800   | 629 | 416200    | 1  |  |
| 60                                          | 554329   | 548 | 970152   | 81 | 584177   | 629 | 415823    | 0  |  |
| /                                           | Cotang.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /  |  |
| 110°                                        |          |     |          |    | 60°      |     |           |    |  |

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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21°

158°

| /  | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|----|----------|-----|-----------|----|
| 0  | 9.554329 | 548 | 9.970152 | 81 | 9.584177 | 629 | 10.415823 | 60 |
| 1  | 554658   | 548 | 970103   | 81 | 584555   | 629 | 415445    | 59 |
| 2  | 554987   | 547 | 970055   | 81 | 584932   | 628 | 415068    | 58 |
| 3  | 555315   | 547 | 970006   | 81 | 585309   | 628 | 414691    | 57 |
| 4  | 555643   | 546 | 969957   | 81 | 585686   | 627 | 414314    | 56 |
| 5  | 555971   | 546 | 969909   | 81 | 586062   | 627 | 413938    | 55 |
| 6  | 556299   | 545 | 969860   | 81 | 586439   | 627 | 413561    | 54 |
| 7  | 556626   | 545 | 969811   | 81 | 586815   | 626 | 413185    | 53 |
| 8  | 556953   | 544 | 969762   | 81 | 587190   | 626 | 412810    | 52 |
| 9  | 557280   | 544 | 969714   | 81 | 587566   | 625 | 412434    | 51 |
| 10 | 557606   | 543 | 969665   | 81 | 587941   | 625 | 412059    | 50 |
| 11 | 9.557932 | 543 | 9.969616 | 82 | 9.588316 | 625 | 10.411684 | 49 |
| 12 | 558258   | 543 | 969567   | 82 | 588691   | 624 | 411309    | 48 |
| 13 | 558583   | 542 | 969518   | 82 | 589066   | 624 | 410934    | 47 |
| 14 | 558909   | 542 | 969469   | 82 | 589440   | 623 | 410560    | 46 |
| 15 | 559234   | 541 | 969420   | 82 | 589814   | 623 | 410186    | 45 |
| 16 | 559558   | 541 | 969370   | 82 | 590188   | 623 | 409812    | 44 |
| 17 | 559883   | 540 | 969321   | 82 | 590562   | 622 | 409438    | 43 |
| 18 | 560207   | 540 | 969272   | 82 | 590935   | 622 | 409065    | 42 |
| 19 | 560531   | 539 | 969223   | 82 | 591308   | 622 | 408692    | 41 |
| 20 | 560855   | 539 | 969173   | 82 | 591681   | 621 | 408319    | 40 |
| 21 | 9.561178 | 538 | 9.969124 | 82 | 9.592054 | 621 | 10.407946 | 39 |
| 22 | 561501   | 538 | 969075   | 82 | 592426   | 620 | 407574    | 38 |
| 23 | 561824   | 537 | 969025   | 82 | 592799   | 620 | 407201    | 37 |
| 24 | 562146   | 537 | 968976   | 82 | 593171   | 619 | 406829    | 36 |
| 25 | 562468   | 536 | 968926   | 83 | 593542   | 619 | 406458    | 35 |
| 26 | 562790   | 536 | 968877   | 83 | 593914   | 618 | 406086    | 34 |
| 27 | 563112   | 536 | 968827   | 83 | 594285   | 618 | 405715    | 33 |
| 28 | 563433   | 535 | 968777   | 83 | 594656   | 618 | 405344    | 32 |
| 29 | 563755   | 535 | 968728   | 83 | 595027   | 617 | 404973    | 31 |
| 30 | 564075   | 534 | 968678   | 83 | 595398   | 617 | 404602    | 30 |
| 31 | 9.564396 | 534 | 9.968628 | 83 | 9.595768 | 617 | 10.404232 | 29 |
| 32 | 564716   | 533 | 968578   | 83 | 596138   | 616 | 403862    | 28 |
| 33 | 565036   | 533 | 968528   | 83 | 596508   | 616 | 403492    | 27 |
| 34 | 565356   | 532 | 968479   | 83 | 596878   | 616 | 403122    | 26 |
| 35 | 565676   | 532 | 968429   | 83 | 597247   | 615 | 402753    | 25 |
| 36 | 565995   | 531 | 968379   | 83 | 597616   | 615 | 402384    | 24 |
| 37 | 566314   | 531 | 968329   | 83 | 597985   | 615 | 402015    | 23 |
| 38 | 566632   | 531 | 968278   | 83 | 598354   | 614 | 401646    | 22 |
| 39 | 566951   | 530 | 968228   | 84 | 598722   | 614 | 401277    | 21 |
| 40 | 567269   | 530 | 968178   | 84 | 599091   | 613 | 400908    | 20 |
| 41 | 9.567587 | 529 | 9.968128 | 84 | 9.599459 | 613 | 10.400541 | 19 |
| 42 | 567904   | 529 | 968078   | 84 | 599827   | 613 | 400173    | 18 |
| 43 | 568222   | 528 | 968027   | 84 | 600194   | 612 | 399806    | 17 |
| 44 | 568539   | 528 | 967977   | 84 | 600562   | 612 | 399438    | 16 |
| 45 | 568856   | 528 | 967927   | 84 | 600929   | 611 | 399071    | 15 |
| 46 | 569172   | 527 | 967876   | 84 | 601296   | 611 | 398704    | 14 |
| 47 | 569488   | 527 | 967826   | 84 | 601663   | 611 | 398337    | 13 |
| 48 | 569804   | 526 | 967775   | 84 | 602029   | 610 | 397971    | 12 |
| 49 | 570120   | 526 | 967725   | 84 | 602395   | 610 | 397605    | 11 |
| 50 | 570435   | 525 | 967674   | 84 | 602761   | 610 | 397239    | 10 |
| 51 | 9.570751 | 525 | 9.967624 | 84 | 9.603127 | 609 | 10.396873 | 9  |
| 52 | 571066   | 524 | 967573   | 84 | 603493   | 609 | 396507    | 8  |
| 53 | 571380   | 524 | 967522   | 85 | 603858   | 609 | 396142    | 7  |
| 54 | 571695   | 523 | 967471   | 85 | 604223   | 608 | 395777    | 6  |
| 55 | 572009   | 523 | 967421   | 85 | 604588   | 608 | 395412    | 5  |
| 56 | 572323   | 523 | 967370   | 85 | 604953   | 607 | 395047    | 4  |
| 57 | 572636   | 522 | 967319   | 85 | 605317   | 607 | 394683    | 3  |
| 58 | 572950   | 522 | 967268   | 85 | 605682   | 607 | 394318    | 2  |
| 59 | 573263   | 521 | 967217   | 85 | 606046   | 606 | 393954    | 1  |
| 60 | 573575   | 521 | 967166   | 85 | 606410   | 606 | 393590    | 0  |
| /  | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /  |

111°

68°

22°

157°

| /  | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|----|----------|-----|-----------|----|
| 0  | 9.573575 | 521 | 9.967166 | 85 | 9.606410 | 606 | 10.393590 | 60 |
| 1  | 573888   | 520 | 967115   | 85 | 606773   | 606 | 393227    | 59 |
| 2  | 574200   | 520 | 967064   | 85 | 607137   | 605 | 392863    | 58 |
| 3  | 574512   | 519 | 967013   | 85 | 607500   | 605 | 392500    | 57 |
| 4  | 574824   | 519 | 966961   | 85 | 607863   | 604 | 392137    | 56 |
| 5  | 575136   | 519 | 966910   | 85 | 608225   | 604 | 391775    | 55 |
| 6  | 575447   | 518 | 966859   | 85 | 608588   | 604 | 391412    | 54 |
| 7  | 575758   | 518 | 966808   | 85 | 608950   | 603 | 391050    | 53 |
| 8  | 576069   | 517 | 966756   | 86 | 609312   | 603 | 390688    | 52 |
| 9  | 576379   | 517 | 966705   | 86 | 609674   | 603 | 390326    | 51 |
| 10 | 576689   | 516 | 966653   | 86 | 610036   | 602 | 389964    | 50 |
| 11 | 9.576999 | 516 | 9.966602 | 86 | 9.610397 | 602 | 10.389603 | 49 |
| 12 | 577309   | 516 | 966550   | 86 | 610759   | 602 | 389241    | 48 |
| 13 | 577618   | 515 | 966499   | 86 | 611120   | 601 | 388880    | 47 |
| 14 | 577927   | 515 | 966447   | 86 | 611480   | 601 | 388520    | 46 |
| 15 | 578236   | 514 | 966395   | 86 | 611841   | 601 | 388159    | 45 |
| 16 | 578545   | 514 | 966344   | 86 | 612201   | 600 | 387799    | 44 |
| 17 | 578853   | 513 | 966292   | 86 | 612561   | 600 | 387439    | 43 |
| 18 | 579162   | 513 | 966240   | 86 | 612921   | 600 | 387079    | 42 |
| 19 | 579470   | 513 | 966188   | 86 | 613281   | 599 | 386719    | 41 |
| 20 | 579777   | 512 | 966136   | 86 | 613641   | 599 | 386359    | 40 |
| 21 | 9.580085 | 512 | 9.966085 | 87 | 9.614000 | 598 | 10.386000 | 39 |
| 22 | 580392   | 511 | 966033   | 87 | 614359   | 598 | 385641    | 38 |
| 23 | 580699   | 511 | 965981   | 87 | 614718   | 598 | 385282    | 37 |
| 24 | 581005   | 511 | 965928   | 87 | 615077   | 597 | 384923    | 36 |
| 25 | 581312   | 510 | 965876   | 87 | 615435   | 597 | 384565    | 35 |
| 26 | 581618   | 510 | 965824   | 87 | 615793   | 597 | 384207    | 34 |
| 27 | 581924   | 509 | 965772   | 87 | 616151   | 596 | 383849    | 33 |
| 28 | 582229   | 509 | 965720   | 87 | 616509   | 596 | 383491    | 32 |
| 29 | 582535   | 509 | 965668   | 87 | 616867   | 596 | 383133    | 31 |
| 30 | 582840   | 508 | 965615   | 87 | 617224   | 595 | 382776    | 30 |
| 31 | 9.583145 | 508 | 9.965563 | 87 | 9.617582 | 595 | 10.382418 | 29 |
| 32 | 583449   | 507 | 965511   | 87 | 617939   | 595 | 382061    | 28 |
| 33 | 583754   | 507 | 965458   | 87 | 618295   | 594 | 381705    | 27 |
| 34 | 584058   | 506 | 965406   | 87 | 618652   | 594 | 381348    | 26 |
| 35 | 584361   | 506 | 965353   | 88 | 619008   | 594 | 380992    | 25 |
| 36 | 584665   | 506 | 965301   | 88 | 619364   | 593 | 380636    | 24 |
| 37 | 584968   | 505 | 965248   | 88 | 619720   | 593 | 380280    | 23 |
| 38 | 585272   | 505 | 965195   | 88 | 620076   | 593 | 379924    | 22 |
| 39 | 585574   | 504 | 965143   | 88 | 620432   | 592 | 379568    | 21 |
| 40 | 585877   | 504 | 965090   | 88 | 620787   | 592 | 379213    | 20 |
| 41 | 9.586179 | 503 | 9.965037 | 88 | 9.621142 | 592 | 10.378858 | 19 |
| 42 | 586482   | 503 | 964984   | 88 | 621497   | 591 | 378503    | 18 |
| 43 | 586783   | 503 | 964931   | 88 | 621852   | 591 | 378148    | 17 |
| 44 | 587085   | 502 | 964879   | 88 | 622207   | 590 | 377793    | 16 |
| 45 | 587386   | 502 | 964826   | 88 | 622561   | 590 | 377439    | 15 |
| 46 | 587688   | 501 | 964773   | 88 | 622915   | 590 | 377085    | 14 |
| 47 | 587989   | 501 | 964720   | 88 | 623269   | 589 | 376731    | 13 |
| 48 | 588289   | 501 | 964666   | 89 | 623623   | 589 | 376377    | 12 |
| 49 | 588590   | 500 | 964613   | 89 | 623976   | 589 | 376024    | 11 |
| 50 | 588890   | 500 | 964560   | 89 | 624330   | 588 | 375670    | 10 |
| 51 | 9.589190 | 499 | 9.964507 | 89 | 9.624683 | 588 | 10.375317 | 9  |
| 52 | 589489   | 499 | 964454   | 89 | 625036   | 588 | 374964    | 8  |
| 53 | 589789   | 499 | 964400   | 89 | 625388   | 587 | 374612    | 7  |
| 54 | 590088   | 498 | 964347   | 89 | 625741   | 587 | 374259    | 6  |
| 55 | 590387   | 498 | 964294   | 89 | 626093   | 587 | 373907    | 5  |
| 56 | 590686   | 497 | 964240   | 89 | 626445   | 586 | 373555    | 4  |
| 57 | 590984   | 497 | 964187   | 89 | 626797   | 586 | 373203    | 3  |
| 58 | 591282   | 497 | 964133   | 89 | 627149   | 586 | 372851    | 2  |
| 59 | 591580   | 496 | 964080   | 89 | 627501   | 585 | 372499    | 1  |
| 60 | 591878   | 496 | 964026   | 89 | 627852   | 585 | 372148    | 0  |
| /  | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /  |

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87°



TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 22° |          |     |          |    |          |     |           | 156° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9.591878 | 466 | 9.964026 | 89 | 9.627852 | 585 | 10.372148 | 60   |  |  |  |  |  |  |  |
| 1   | 592176   | 465 | 963972   | 89 | 628203   | 585 | 371797    | 59   |  |  |  |  |  |  |  |
| 2   | 592473   | 465 | 963919   | 89 | 628554   | 585 | 371446    | 58   |  |  |  |  |  |  |  |
| 3   | 592770   | 465 | 963865   | 90 | 628905   | 584 | 371095    | 57   |  |  |  |  |  |  |  |
| 4   | 593067   | 464 | 963811   | 90 | 629255   | 584 | 370745    | 56   |  |  |  |  |  |  |  |
| 5   | 593363   | 464 | 963757   | 90 | 629606   | 583 | 370394    | 55   |  |  |  |  |  |  |  |
| 6   | 593659   | 463 | 963704   | 90 | 629956   | 583 | 370044    | 54   |  |  |  |  |  |  |  |
| 7   | 593955   | 463 | 963650   | 90 | 630306   | 583 | 369694    | 53   |  |  |  |  |  |  |  |
| 8   | 594251   | 463 | 963596   | 90 | 630656   | 583 | 369344    | 52   |  |  |  |  |  |  |  |
| 9   | 594547   | 462 | 963542   | 90 | 631005   | 582 | 368993    | 51   |  |  |  |  |  |  |  |
| 10  | 594842   | 462 | 963488   | 90 | 631355   | 582 | 368643    | 50   |  |  |  |  |  |  |  |
| 11  | 9.595137 | 461 | 9.963434 | 90 | 9.631704 | 582 | 10.368296 | 49   |  |  |  |  |  |  |  |
| 12  | 595432   | 461 | 963379   | 90 | 632053   | 581 | 367947    | 48   |  |  |  |  |  |  |  |
| 13  | 595727   | 461 | 963325   | 90 | 632402   | 581 | 367598    | 47   |  |  |  |  |  |  |  |
| 14  | 596021   | 460 | 963271   | 90 | 632750   | 581 | 367248    | 46   |  |  |  |  |  |  |  |
| 15  | 596315   | 460 | 963217   | 90 | 633099   | 580 | 366901    | 45   |  |  |  |  |  |  |  |
| 16  | 596609   | 460 | 963163   | 90 | 633447   | 580 | 366553    | 44   |  |  |  |  |  |  |  |
| 17  | 596903   | 460 | 963108   | 91 | 633795   | 580 | 366205    | 43   |  |  |  |  |  |  |  |
| 18  | 597196   | 460 | 963054   | 91 | 634143   | 579 | 365857    | 42   |  |  |  |  |  |  |  |
| 19  | 597490   | 460 | 962999   | 91 | 634490   | 579 | 365510    | 41   |  |  |  |  |  |  |  |
| 20  | 597783   | 460 | 962945   | 91 | 634838   | 579 | 365162    | 40   |  |  |  |  |  |  |  |
| 21  | 9.598075 | 460 | 9.962890 | 91 | 9.635185 | 578 | 10.364815 | 39   |  |  |  |  |  |  |  |
| 22  | 598368   | 460 | 962836   | 91 | 635532   | 578 | 364468    | 38   |  |  |  |  |  |  |  |
| 23  | 598660   | 460 | 962781   | 91 | 635879   | 578 | 364121    | 37   |  |  |  |  |  |  |  |
| 24  | 598952   | 460 | 962727   | 91 | 636226   | 577 | 363774    | 36   |  |  |  |  |  |  |  |
| 25  | 599244   | 460 | 962672   | 91 | 636572   | 577 | 363428    | 35   |  |  |  |  |  |  |  |
| 26  | 599536   | 460 | 962617   | 91 | 636919   | 577 | 363081    | 34   |  |  |  |  |  |  |  |
| 27  | 599827   | 460 | 962562   | 91 | 637265   | 577 | 362735    | 33   |  |  |  |  |  |  |  |
| 28  | 600118   | 460 | 962508   | 91 | 637611   | 576 | 362389    | 32   |  |  |  |  |  |  |  |
| 29  | 600409   | 460 | 962453   | 91 | 637956   | 576 | 362044    | 31   |  |  |  |  |  |  |  |
| 30  | 600700   | 460 | 962398   | 92 | 638302   | 576 | 361698    | 30   |  |  |  |  |  |  |  |
| 31  | 9.600990 | 460 | 9.962343 | 92 | 9.638647 | 575 | 10.361353 | 29   |  |  |  |  |  |  |  |
| 32  | 601280   | 460 | 962288   | 92 | 638992   | 575 | 361008    | 28   |  |  |  |  |  |  |  |
| 33  | 601570   | 460 | 962233   | 92 | 639337   | 575 | 360663    | 27   |  |  |  |  |  |  |  |
| 34  | 601860   | 460 | 962178   | 92 | 639682   | 574 | 360318    | 26   |  |  |  |  |  |  |  |
| 35  | 602150   | 460 | 962123   | 92 | 640027   | 574 | 359973    | 25   |  |  |  |  |  |  |  |
| 36  | 602439   | 460 | 962067   | 92 | 640371   | 574 | 359629    | 24   |  |  |  |  |  |  |  |
| 37  | 602728   | 460 | 962012   | 92 | 640716   | 573 | 359284    | 23   |  |  |  |  |  |  |  |
| 38  | 603017   | 460 | 961957   | 92 | 641060   | 573 | 358940    | 22   |  |  |  |  |  |  |  |
| 39  | 603305   | 460 | 961902   | 92 | 641404   | 573 | 358596    | 21   |  |  |  |  |  |  |  |
| 40  | 603594   | 460 | 961846   | 92 | 641747   | 572 | 358253    | 20   |  |  |  |  |  |  |  |
| 41  | 9.603882 | 460 | 9.961791 | 92 | 9.642091 | 572 | 10.357909 | 19   |  |  |  |  |  |  |  |
| 42  | 604170   | 460 | 961735   | 92 | 642434   | 572 | 357566    | 18   |  |  |  |  |  |  |  |
| 43  | 604457   | 460 | 961680   | 92 | 642777   | 572 | 357223    | 17   |  |  |  |  |  |  |  |
| 44  | 604745   | 460 | 961624   | 93 | 643120   | 571 | 356880    | 16   |  |  |  |  |  |  |  |
| 45  | 605032   | 460 | 961569   | 93 | 643463   | 571 | 356537    | 15   |  |  |  |  |  |  |  |
| 46  | 605319   | 460 | 961513   | 93 | 643806   | 571 | 356194    | 14   |  |  |  |  |  |  |  |
| 47  | 605606   | 460 | 961458   | 93 | 644148   | 570 | 355852    | 13   |  |  |  |  |  |  |  |
| 48  | 605892   | 460 | 961402   | 93 | 644490   | 570 | 355510    | 12   |  |  |  |  |  |  |  |
| 49  | 606179   | 460 | 961346   | 93 | 644832   | 570 | 355168    | 11   |  |  |  |  |  |  |  |
| 50  | 606465   | 460 | 961290   | 93 | 645174   | 569 | 354826    | 10   |  |  |  |  |  |  |  |
| 51  | 9.606751 | 460 | 9.961235 | 93 | 9.645516 | 569 | 10.354484 | 9    |  |  |  |  |  |  |  |
| 52  | 607036   | 460 | 961179   | 93 | 645857   | 569 | 354143    | 8    |  |  |  |  |  |  |  |
| 53  | 607322   | 460 | 961123   | 93 | 646199   | 569 | 353801    | 7    |  |  |  |  |  |  |  |
| 54  | 607607   | 460 | 961067   | 93 | 646540   | 568 | 353460    | 6    |  |  |  |  |  |  |  |
| 55  | 607892   | 460 | 961011   | 93 | 646881   | 568 | 353119    | 5    |  |  |  |  |  |  |  |
| 56  | 608177   | 460 | 960955   | 93 | 647222   | 568 | 352778    | 4    |  |  |  |  |  |  |  |
| 57  | 608461   | 460 | 960899   | 93 | 647562   | 567 | 352438    | 3    |  |  |  |  |  |  |  |
| 58  | 608745   | 460 | 960843   | 94 | 647903   | 567 | 352097    | 2    |  |  |  |  |  |  |  |
| 59  | 609029   | 460 | 960786   | 94 | 648243   | 567 | 351757    | 1    |  |  |  |  |  |  |  |
| 60  | 609313   | 460 | 960730   | 94 | 648583   | 566 | 351417    | 0    |  |  |  |  |  |  |  |
| /   | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

113°

66°

24°

155°

| /  | Sine.    | D.  | Cosine.  | D. | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|----|----------|-----|-----------|----|
| 0  | 9-609313 | 473 | 9-960730 | 94 | 9-648583 | 566 | 10-351417 | 60 |
| 1  | 609597   | 472 | 960674   | 94 | 648923   | 566 | 351077    | 59 |
| 2  | 609880   | 472 | 960618   | 94 | 649263   | 566 | 350737    | 58 |
| 3  | 610164   | 472 | 960561   | 94 | 649602   | 566 | 350398    | 57 |
| 4  | 610447   | 471 | 960505   | 94 | 649942   | 565 | 350058    | 56 |
| 5  | 610729   | 471 | 960448   | 94 | 650281   | 565 | 349719    | 55 |
| 6  | 611012   | 470 | 960392   | 94 | 650620   | 565 | 349380    | 54 |
| 7  | 611294   | 470 | 960335   | 94 | 650959   | 564 | 349041    | 53 |
| 8  | 611576   | 470 | 960279   | 94 | 651297   | 564 | 348703    | 52 |
| 9  | 611858   | 469 | 960222   | 94 | 651636   | 564 | 348364    | 51 |
| 10 | 612140   | 469 | 960165   | 94 | 651974   | 563 | 348026    | 50 |
| 11 | 9-612421 | 469 | 9-960109 | 95 | 9-652312 | 563 | 10-347688 | 49 |
| 12 | 612702   | 468 | 960052   | 95 | 652650   | 563 | 347350    | 48 |
| 13 | 612983   | 468 | 959995   | 95 | 652988   | 563 | 347012    | 47 |
| 14 | 613264   | 467 | 959938   | 95 | 653326   | 562 | 346674    | 46 |
| 15 | 613545   | 467 | 959882   | 95 | 653663   | 562 | 346337    | 45 |
| 16 | 613825   | 467 | 959825   | 95 | 654000   | 562 | 346000    | 44 |
| 17 | 614105   | 466 | 959768   | 95 | 654337   | 561 | 345663    | 43 |
| 18 | 614385   | 466 | 959711   | 95 | 654674   | 561 | 345326    | 42 |
| 19 | 614665   | 466 | 959654   | 95 | 655011   | 561 | 344989    | 41 |
| 20 | 614944   | 465 | 959596   | 95 | 655348   | 561 | 344652    | 40 |
| 21 | 9-615223 | 465 | 9-959539 | 95 | 9-655684 | 560 | 10-344316 | 39 |
| 22 | 615502   | 465 | 959482   | 95 | 656020   | 560 | 343980    | 38 |
| 23 | 615781   | 464 | 959425   | 95 | 656356   | 560 | 343644    | 37 |
| 24 | 616060   | 464 | 959368   | 95 | 656692   | 559 | 343308    | 36 |
| 25 | 616338   | 464 | 959310   | 96 | 657028   | 559 | 342972    | 35 |
| 26 | 616616   | 463 | 959253   | 96 | 657364   | 559 | 342636    | 34 |
| 27 | 616894   | 463 | 959195   | 96 | 657699   | 559 | 342301    | 33 |
| 28 | 617172   | 462 | 959138   | 96 | 658034   | 558 | 341966    | 32 |
| 29 | 617450   | 462 | 959080   | 96 | 658369   | 558 | 341631    | 31 |
| 30 | 617727   | 462 | 959023   | 96 | 658704   | 558 | 341296    | 30 |
| 31 | 9-618004 | 461 | 9-958965 | 96 | 9-659039 | 558 | 10-340961 | 29 |
| 32 | 618281   | 461 | 958908   | 96 | 659373   | 557 | 340627    | 28 |
| 33 | 618558   | 461 | 958850   | 96 | 659708   | 557 | 340292    | 27 |
| 34 | 618834   | 460 | 958792   | 96 | 660042   | 557 | 339958    | 26 |
| 35 | 619111   | 460 | 958734   | 96 | 660376   | 557 | 339624    | 25 |
| 36 | 619386   | 460 | 958677   | 96 | 660710   | 556 | 339290    | 24 |
| 37 | 619662   | 459 | 958619   | 96 | 661043   | 556 | 338957    | 23 |
| 38 | 619938   | 459 | 958561   | 96 | 661377   | 556 | 338623    | 22 |
| 39 | 620213   | 458 | 958503   | 97 | 661710   | 555 | 338290    | 21 |
| 40 | 620488   | 458 | 958445   | 97 | 662043   | 555 | 337957    | 20 |
| 41 | 9-620763 | 458 | 9-958387 | 97 | 9-662376 | 555 | 10-337624 | 19 |
| 42 | 621038   | 457 | 958329   | 97 | 662709   | 554 | 337291    | 18 |
| 43 | 621313   | 457 | 958271   | 97 | 663042   | 554 | 336958    | 17 |
| 44 | 621587   | 457 | 958213   | 97 | 663375   | 554 | 336625    | 16 |
| 45 | 621861   | 456 | 958154   | 97 | 663707   | 554 | 336293    | 15 |
| 46 | 622135   | 456 | 958096   | 97 | 664039   | 553 | 335961    | 14 |
| 47 | 622409   | 456 | 958038   | 97 | 664371   | 553 | 335629    | 13 |
| 48 | 622682   | 455 | 957979   | 97 | 664703   | 553 | 335297    | 12 |
| 49 | 622956   | 455 | 957921   | 97 | 665035   | 553 | 334965    | 11 |
| 50 | 623229   | 455 | 957863   | 97 | 665366   | 552 | 334634    | 10 |
| 51 | 9-623502 | 454 | 9-957804 | 97 | 9-665698 | 552 | 10-334302 | 9  |
| 52 | 623774   | 454 | 957746   | 98 | 666029   | 552 | 333971    | 8  |
| 53 | 624047   | 454 | 957687   | 98 | 666360   | 551 | 333640    | 7  |
| 54 | 624319   | 453 | 957628   | 98 | 666691   | 551 | 333309    | 6  |
| 55 | 624591   | 453 | 957570   | 98 | 667021   | 551 | 332979    | 5  |
| 56 | 624863   | 453 | 957511   | 98 | 667352   | 551 | 332648    | 4  |
| 57 | 625135   | 452 | 957452   | 98 | 667682   | 550 | 332318    | 3  |
| 58 | 625406   | 452 | 957393   | 98 | 668013   | 550 | 331987    | 2  |
| 59 | 625677   | 452 | 957335   | 98 | 668343   | 550 | 331657    | 1  |
| 60 | 625948   | 451 | 957276   | 98 | 668673   | 550 | 331327    | 0  |
| /  | Cosine.  | D.  | Sine.    | D. | Cotang.  | D.  | Tang.     | /  |

114°

86°

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 25°  |          |     |          |     |          |     |           | 154° |  |
|------|----------|-----|----------|-----|----------|-----|-----------|------|--|
| /    | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |
| 0    | 9.625948 | 451 | 9.957276 | 98  | 9.668673 | 550 | 10.331327 | 60   |  |
| 1    | 626219   | 451 | 957217   | 98  | 669002   | 549 | 330998    | 59   |  |
| 2    | 626490   | 451 | 957158   | 98  | 669332   | 549 | 330668    | 58   |  |
| 3    | 626760   | 450 | 957099   | 98  | 669661   | 549 | 330339    | 57   |  |
| 4    | 627030   | 450 | 957040   | 98  | 669991   | 548 | 330009    | 56   |  |
| 5    | 627300   | 450 | 956981   | 98  | 670320   | 548 | 329680    | 55   |  |
| 6    | 627570   | 449 | 956921   | 99  | 670649   | 548 | 329351    | 54   |  |
| 7    | 627840   | 449 | 956862   | 99  | 670977   | 548 | 329023    | 53   |  |
| 8    | 628109   | 449 | 956803   | 99  | 671306   | 547 | 328694    | 52   |  |
| 9    | 628378   | 448 | 956744   | 99  | 671635   | 547 | 328365    | 51   |  |
| 10   | 628647   | 448 | 956684   | 99  | 671963   | 547 | 328037    | 50   |  |
| 11   | 9.628916 | 457 | 9.956625 | 99  | 9.672291 | 547 | 10.327709 | 49   |  |
| 12   | 629185   | 447 | 956566   | 99  | 672619   | 546 | 327381    | 48   |  |
| 13   | 629453   | 447 | 956506   | 99  | 672947   | 546 | 327053    | 47   |  |
| 14   | 629721   | 446 | 956447   | 99  | 673274   | 546 | 326726    | 46   |  |
| 15   | 629989   | 446 | 956387   | 99  | 673602   | 546 | 326398    | 45   |  |
| 16   | 630257   | 446 | 956327   | 99  | 673929   | 545 | 326071    | 44   |  |
| 17   | 630524   | 446 | 956268   | 99  | 674257   | 545 | 325743    | 43   |  |
| 18   | 630792   | 445 | 956208   | 100 | 674584   | 545 | 325416    | 42   |  |
| 19   | 631059   | 445 | 956148   | 100 | 674911   | 544 | 325089    | 41   |  |
| 20   | 631326   | 445 | 956089   | 100 | 675237   | 544 | 324763    | 40   |  |
| 21   | 9.631593 | 444 | 9.956029 | 100 | 9.675564 | 544 | 10.324436 | 39   |  |
| 22   | 631859   | 444 | 955969   | 100 | 675890   | 544 | 324410    | 38   |  |
| 23   | 632125   | 444 | 955909   | 100 | 676217   | 543 | 323783    | 37   |  |
| 24   | 632392   | 443 | 955849   | 100 | 676543   | 543 | 323457    | 36   |  |
| 25   | 632658   | 443 | 955789   | 100 | 676869   | 543 | 323131    | 35   |  |
| 26   | 632923   | 443 | 955729   | 100 | 677194   | 543 | 322806    | 34   |  |
| 27   | 633189   | 442 | 955669   | 100 | 677520   | 542 | 322480    | 33   |  |
| 28   | 633454   | 442 | 955609   | 100 | 677846   | 542 | 322154    | 32   |  |
| 29   | 633719   | 442 | 955548   | 100 | 678171   | 542 | 321829    | 31   |  |
| 30   | 633984   | 441 | 955488   | 100 | 678496   | 542 | 321504    | 30   |  |
| 31   | 9.634249 | 441 | 9.955428 | 101 | 9.678821 | 541 | 10.321179 | 29   |  |
| 32   | 634514   | 440 | 955368   | 101 | 679146   | 541 | 320854    | 28   |  |
| 33   | 634778   | 440 | 955307   | 101 | 679471   | 541 | 320529    | 27   |  |
| 34   | 635042   | 440 | 955247   | 101 | 679795   | 541 | 320205    | 26   |  |
| 35   | 635306   | 439 | 955186   | 101 | 680120   | 540 | 319880    | 25   |  |
| 36   | 635570   | 439 | 955126   | 101 | 680444   | 540 | 319556    | 24   |  |
| 37   | 635834   | 439 | 955065   | 101 | 680768   | 540 | 319232    | 23   |  |
| 38   | 636097   | 438 | 955005   | 101 | 681092   | 540 | 318908    | 22   |  |
| 39   | 636360   | 438 | 954944   | 101 | 681416   | 539 | 318584    | 21   |  |
| 40   | 636623   | 438 | 954883   | 101 | 681740   | 539 | 318260    | 20   |  |
| 41   | 9.636886 | 437 | 9.954823 | 101 | 9.682063 | 539 | 10.317937 | 19   |  |
| 42   | 637148   | 437 | 954762   | 101 | 682387   | 539 | 317613    | 18   |  |
| 43   | 637411   | 437 | 954701   | 101 | 682710   | 538 | 317290    | 17   |  |
| 44   | 637673   | 437 | 954640   | 101 | 683033   | 538 | 316967    | 16   |  |
| 45   | 637935   | 436 | 954579   | 101 | 683356   | 538 | 316644    | 15   |  |
| 46   | 638197   | 436 | 954518   | 102 | 683679   | 538 | 316321    | 14   |  |
| 47   | 638458   | 436 | 954457   | 102 | 684001   | 537 | 315999    | 13   |  |
| 48   | 638720   | 435 | 954396   | 102 | 684324   | 537 | 315676    | 12   |  |
| 49   | 638981   | 435 | 954335   | 102 | 684646   | 537 | 315354    | 11   |  |
| 50   | 639242   | 435 | 954274   | 102 | 684968   | 537 | 315032    | 10   |  |
| 51   | 9.639503 | 434 | 9.954213 | 102 | 9.685290 | 536 | 10.314710 | 9    |  |
| 52   | 639764   | 434 | 954152   | 102 | 685612   | 536 | 314388    | 8    |  |
| 53   | 640024   | 434 | 954090   | 102 | 685934   | 536 | 314066    | 7    |  |
| 54   | 640284   | 433 | 954029   | 102 | 686255   | 536 | 313745    | 6    |  |
| 55   | 640544   | 433 | 953968   | 102 | 686577   | 535 | 313423    | 5    |  |
| 56   | 640804   | 433 | 953906   | 102 | 686898   | 535 | 313102    | 4    |  |
| 57   | 641064   | 432 | 953845   | 102 | 687219   | 535 | 312781    | 3    |  |
| 58   | 641324   | 432 | 953783   | 102 | 687540   | 535 | 312460    | 2    |  |
| 59   | 641583   | 432 | 953722   | 103 | 687861   | 534 | 312139    | 1    |  |
| 60   | 641842   | 431 | 953660   | 103 | 688182   | 534 | 311818    | 0    |  |
| /    | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |
| 115° |          |     |          |     |          |     |           | 64°  |  |

| Table I |          |          |             |           |      |           |         |
|---------|----------|----------|-------------|-----------|------|-----------|---------|
| No.     | Location | Altitude | Temperature | Barometer | Wind | Direction | Remarks |
| 1       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 2       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 3       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 4       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 5       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 6       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 7       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 8       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 9       | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 10      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 11      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 12      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 13      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 14      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 15      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 16      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 17      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 18      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 19      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 20      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 21      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 22      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 23      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 24      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 25      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 26      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 27      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 28      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 29      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 30      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 31      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 32      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 33      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 34      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 35      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 36      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 37      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 38      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 39      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 40      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 41      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 42      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 43      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 44      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 45      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 46      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 47      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 48      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 49      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 50      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 51      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 52      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 53      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 54      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 55      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 56      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 57      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 58      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 59      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 60      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 61      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 62      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 63      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 64      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 65      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 66      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 67      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 68      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 69      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 70      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 71      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 72      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 73      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 74      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 75      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 76      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 77      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 78      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 79      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 80      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 81      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 82      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 83      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 84      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 85      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 86      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 87      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 88      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 89      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 90      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 91      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 92      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 93      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 94      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 95      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 96      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 97      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 98      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 99      | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| 100     | ...      | ...      | ...         | ...       | ...  | ...       | ...     |
| No.     | Location | Altitude | Temperature | Barometer | Wind | Direction | Remarks |

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 27° |          |     |          |     |          |     |           | 152° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9.657047 | 413 | 9.949881 | 107 | 0.707166 | 520 | 10.292834 | 60   |  |  |  |  |  |  |  |
| 1   | 657295   | 413 | 949816   | 107 | 707478   | 520 | 292522    | 59   |  |  |  |  |  |  |  |
| 2   | 657542   | 412 | 949752   | 107 | 707790   | 520 | 292210    | 58   |  |  |  |  |  |  |  |
| 3   | 657790   | 412 | 949688   | 108 | 708102   | 520 | 291898    | 57   |  |  |  |  |  |  |  |
| 4   | 658037   | 412 | 949623   | 108 | 708414   | 519 | 291586    | 56   |  |  |  |  |  |  |  |
| 5   | 658284   | 412 | 949558   | 108 | 708726   | 519 | 291274    | 55   |  |  |  |  |  |  |  |
| 6   | 658531   | 411 | 949494   | 108 | 709037   | 519 | 290963    | 54   |  |  |  |  |  |  |  |
| 7   | 658778   | 411 | 949429   | 108 | 709349   | 519 | 290651    | 53   |  |  |  |  |  |  |  |
| 8   | 659025   | 411 | 949364   | 108 | 709660   | 519 | 290340    | 52   |  |  |  |  |  |  |  |
| 9   | 659271   | 410 | 949300   | 108 | 709971   | 518 | 290029    | 51   |  |  |  |  |  |  |  |
| 10  | 659517   | 410 | 949235   | 108 | 710282   | 518 | 289718    | 50   |  |  |  |  |  |  |  |
| 11  | 9.659763 | 410 | 9.949170 | 108 | 9.710593 | 518 | 10.289407 | 49   |  |  |  |  |  |  |  |
| 12  | 660009   | 409 | 949105   | 108 | 710904   | 518 | 289096    | 48   |  |  |  |  |  |  |  |
| 13  | 660255   | 409 | 949040   | 108 | 711215   | 518 | 288785    | 47   |  |  |  |  |  |  |  |
| 14  | 660501   | 409 | 948975   | 108 | 711525   | 517 | 288475    | 46   |  |  |  |  |  |  |  |
| 15  | 660746   | 409 | 948910   | 108 | 711836   | 517 | 288164    | 45   |  |  |  |  |  |  |  |
| 16  | 660991   | 408 | 948845   | 108 | 712146   | 517 | 287854    | 44   |  |  |  |  |  |  |  |
| 17  | 661236   | 408 | 948780   | 109 | 712456   | 517 | 287544    | 43   |  |  |  |  |  |  |  |
| 18  | 661481   | 408 | 948715   | 109 | 712766   | 516 | 287234    | 42   |  |  |  |  |  |  |  |
| 19  | 661726   | 407 | 948650   | 109 | 713076   | 516 | 286924    | 41   |  |  |  |  |  |  |  |
| 20  | 661970   | 407 | 948584   | 109 | 713386   | 516 | 286614    | 40   |  |  |  |  |  |  |  |
| 21  | 9.662214 | 407 | 9.948519 | 109 | 9.713696 | 516 | 10.286304 | 39   |  |  |  |  |  |  |  |
| 22  | 662459   | 407 | 948454   | 109 | 714005   | 516 | 285995    | 38   |  |  |  |  |  |  |  |
| 23  | 662703   | 406 | 948388   | 109 | 714314   | 515 | 285686    | 37   |  |  |  |  |  |  |  |
| 24  | 662946   | 406 | 948323   | 109 | 714624   | 515 | 285376    | 36   |  |  |  |  |  |  |  |
| 25  | 663190   | 406 | 948257   | 109 | 714933   | 515 | 285067    | 35   |  |  |  |  |  |  |  |
| 26  | 663433   | 405 | 948192   | 109 | 715242   | 515 | 284758    | 34   |  |  |  |  |  |  |  |
| 27  | 663677   | 405 | 948126   | 109 | 715551   | 514 | 284449    | 33   |  |  |  |  |  |  |  |
| 28  | 663920   | 405 | 948060   | 109 | 715860   | 514 | 284140    | 32   |  |  |  |  |  |  |  |
| 29  | 664163   | 405 | 947995   | 110 | 716168   | 514 | 283832    | 31   |  |  |  |  |  |  |  |
| 30  | 664406   | 404 | 947929   | 110 | 716477   | 514 | 283523    | 30   |  |  |  |  |  |  |  |
| 31  | 9.664648 | 404 | 9.947863 | 110 | 9.716785 | 514 | 10.283215 | 29   |  |  |  |  |  |  |  |
| 32  | 664891   | 404 | 947797   | 110 | 717093   | 513 | 282907    | 28   |  |  |  |  |  |  |  |
| 33  | 665133   | 403 | 947731   | 110 | 717401   | 513 | 282599    | 27   |  |  |  |  |  |  |  |
| 34  | 665375   | 403 | 947665   | 110 | 717709   | 513 | 282291    | 26   |  |  |  |  |  |  |  |
| 35  | 665617   | 403 | 947600   | 110 | 718017   | 513 | 281983    | 25   |  |  |  |  |  |  |  |
| 36  | 665859   | 402 | 947533   | 110 | 718325   | 513 | 281675    | 24   |  |  |  |  |  |  |  |
| 37  | 666100   | 402 | 947467   | 110 | 718633   | 512 | 281367    | 23   |  |  |  |  |  |  |  |
| 38  | 666342   | 402 | 947401   | 110 | 718940   | 512 | 281060    | 22   |  |  |  |  |  |  |  |
| 39  | 666583   | 402 | 947335   | 110 | 719248   | 512 | 280752    | 21   |  |  |  |  |  |  |  |
| 40  | 666824   | 401 | 947269   | 110 | 719555   | 512 | 280445    | 20   |  |  |  |  |  |  |  |
| 41  | 9.667065 | 401 | 9.947203 | 110 | 9.719862 | 512 | 10.280138 | 19   |  |  |  |  |  |  |  |
| 42  | 667305   | 401 | 947136   | 111 | 720169   | 511 | 279831    | 18   |  |  |  |  |  |  |  |
| 43  | 667546   | 401 | 947070   | 111 | 720476   | 511 | 279524    | 17   |  |  |  |  |  |  |  |
| 44  | 667786   | 400 | 947004   | 111 | 720783   | 511 | 279217    | 16   |  |  |  |  |  |  |  |
| 45  | 668027   | 400 | 946937   | 111 | 721089   | 511 | 278911    | 15   |  |  |  |  |  |  |  |
| 46  | 668267   | 400 | 946871   | 111 | 721396   | 511 | 278604    | 14   |  |  |  |  |  |  |  |
| 47  | 668506   | 399 | 946804   | 111 | 721702   | 510 | 278298    | 13   |  |  |  |  |  |  |  |
| 48  | 668746   | 399 | 946738   | 111 | 722009   | 510 | 277991    | 12   |  |  |  |  |  |  |  |
| 49  | 668986   | 399 | 946671   | 111 | 722315   | 510 | 277685    | 11   |  |  |  |  |  |  |  |
| 50  | 669225   | 399 | 946604   | 111 | 722621   | 510 | 277379    | 10   |  |  |  |  |  |  |  |
| 51  | 9.669464 | 398 | 9.946538 | 111 | 9.722927 | 510 | 10.277073 | 9    |  |  |  |  |  |  |  |
| 52  | 669703   | 398 | 946471   | 111 | 723232   | 509 | 276768    | 8    |  |  |  |  |  |  |  |
| 53  | 669942   | 398 | 946404   | 111 | 723538   | 509 | 276462    | 7    |  |  |  |  |  |  |  |
| 54  | 670181   | 397 | 946337   | 111 | 723844   | 509 | 276156    | 6    |  |  |  |  |  |  |  |
| 55  | 670419   | 397 | 946270   | 112 | 724149   | 509 | 275851    | 5    |  |  |  |  |  |  |  |
| 56  | 670658   | 397 | 946203   | 112 | 724454   | 509 | 275545    | 4    |  |  |  |  |  |  |  |
| 57  | 670896   | 397 | 946136   | 112 | 724760   | 508 | 275240    | 3    |  |  |  |  |  |  |  |
| 58  | 671134   | 396 | 946069   | 112 | 725065   | 508 | 274935    | 2    |  |  |  |  |  |  |  |
| 59  | 671372   | 396 | 946002   | 112 | 725370   | 508 | 274630    | 1    |  |  |  |  |  |  |  |
| 60  | 671609   | 396 | 945935   | 112 | 725674   | 508 | 274326    | 0    |  |  |  |  |  |  |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

117°

63°

| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.671609 | 396 | 9.945935 | 112 | 9.725674 | 508 | 10.274326 | 60 |
| 1  | 671847   | 395 | 945868   | 112 | 725979   | 508 | 274021    | 59 |
| 2  | 672084   | 395 | 945800   | 112 | 726284   | 507 | 273716    | 58 |
| 3  | 672321   | 395 | 945733   | 112 | 726588   | 507 | 273412    | 57 |
| 4  | 672558   | 395 | 945666   | 112 | 726892   | 507 | 273108    | 56 |
| 5  | 672795   | 394 | 945598   | 112 | 727197   | 507 | 272803    | 55 |
| 6  | 673032   | 394 | 945531   | 112 | 727501   | 507 | 272499    | 54 |
| 7  | 673268   | 394 | 945464   | 113 | 727805   | 506 | 272195    | 53 |
| 8  | 673505   | 394 | 945396   | 113 | 728109   | 506 | 271891    | 52 |
| 9  | 673741   | 393 | 945328   | 113 | 728412   | 506 | 271588    | 51 |
| 10 | 673977   | 393 | 945261   | 113 | 728716   | 506 | 271284    | 50 |
| 11 | 9.674213 | 393 | 9.945193 | 113 | 9.729020 | 506 | 10.270980 | 49 |
| 12 | 674448   | 392 | 945125   | 113 | 729323   | 505 | 270677    | 48 |
| 13 | 674684   | 392 | 945058   | 113 | 729626   | 505 | 270374    | 47 |
| 14 | 674919   | 392 | 944990   | 113 | 729929   | 505 | 270071    | 46 |
| 15 | 675155   | 392 | 944922   | 113 | 730233   | 505 | 269767    | 45 |
| 16 | 675390   | 391 | 944854   | 113 | 730535   | 505 | 269465    | 44 |
| 17 | 675624   | 391 | 944786   | 113 | 730838   | 504 | 269162    | 43 |
| 18 | 675859   | 391 | 944718   | 113 | 731141   | 504 | 268859    | 42 |
| 19 | 676094   | 391 | 944650   | 113 | 731444   | 504 | 268556    | 41 |
| 20 | 676328   | 390 | 944582   | 114 | 731746   | 504 | 268254    | 40 |
| 21 | 9.676562 | 390 | 9.944514 | 114 | 9.732048 | 504 | 10.267952 | 39 |
| 22 | 676796   | 390 | 944446   | 114 | 732351   | 503 | 267649    | 38 |
| 23 | 677030   | 390 | 944377   | 114 | 732653   | 503 | 267347    | 37 |
| 24 | 677264   | 389 | 944309   | 114 | 732955   | 503 | 267045    | 36 |
| 25 | 677498   | 389 | 944241   | 114 | 733257   | 503 | 266743    | 35 |
| 26 | 677731   | 389 | 944172   | 114 | 733558   | 503 | 266442    | 34 |
| 27 | 677964   | 388 | 944104   | 114 | 733860   | 502 | 266140    | 33 |
| 28 | 678197   | 388 | 944036   | 114 | 734162   | 502 | 265838    | 32 |
| 29 | 678430   | 388 | 943967   | 114 | 734463   | 502 | 265537    | 31 |
| 30 | 678663   | 388 | 943899   | 114 | 734764   | 502 | 265236    | 30 |
| 31 | 9.678895 | 387 | 9.943830 | 114 | 9.735066 | 502 | 10.264934 | 29 |
| 32 | 679128   | 387 | 943761   | 114 | 735367   | 502 | 264633    | 28 |
| 33 | 679360   | 387 | 943693   | 115 | 735668   | 501 | 264332    | 27 |
| 34 | 679592   | 387 | 943624   | 115 | 735969   | 501 | 264031    | 26 |
| 35 | 679824   | 386 | 943555   | 115 | 736269   | 501 | 263731    | 25 |
| 36 | 680056   | 386 | 943486   | 115 | 736570   | 501 | 263430    | 24 |
| 37 | 680288   | 386 | 943417   | 115 | 736870   | 501 | 263130    | 23 |
| 38 | 680519   | 385 | 943348   | 115 | 737171   | 500 | 262829    | 22 |
| 39 | 680750   | 385 | 943279   | 115 | 737471   | 500 | 262529    | 21 |
| 40 | 680982   | 385 | 943210   | 115 | 737771   | 500 | 262229    | 20 |
| 41 | 9.681213 | 385 | 9.943141 | 115 | 9.738071 | 500 | 10.261929 | 19 |
| 42 | 681443   | 384 | 943072   | 115 | 738371   | 500 | 261629    | 18 |
| 43 | 681674   | 384 | 943003   | 115 | 738671   | 499 | 261329    | 17 |
| 44 | 681905   | 384 | 942934   | 115 | 738971   | 499 | 261029    | 16 |
| 45 | 682135   | 384 | 942864   | 115 | 739271   | 499 | 260729    | 15 |
| 46 | 682365   | 383 | 942795   | 116 | 739570   | 499 | 260430    | 14 |
| 47 | 682595   | 383 | 942726   | 116 | 739870   | 499 | 260130    | 13 |
| 48 | 682825   | 383 | 942656   | 116 | 740169   | 499 | 259831    | 12 |
| 49 | 683055   | 383 | 942587   | 116 | 740468   | 498 | 259532    | 11 |
| 50 | 683284   | 382 | 942517   | 116 | 740767   | 498 | 259233    | 10 |
| 51 | 9.683514 | 382 | 9.942448 | 116 | 9.741066 | 498 | 10.258934 | 9  |
| 52 | 683743   | 382 | 942378   | 116 | 741365   | 498 | 258635    | 8  |
| 53 | 683972   | 382 | 942308   | 116 | 741664   | 498 | 258336    | 7  |
| 54 | 684201   | 381 | 942239   | 116 | 741962   | 497 | 258038    | 6  |
| 55 | 684430   | 381 | 942169   | 116 | 742261   | 497 | 257739    | 5  |
| 56 | 684658   | 381 | 942099   | 116 | 742559   | 497 | 257441    | 4  |
| 57 | 684887   | 380 | 942029   | 116 | 742858   | 497 | 257142    | 3  |
| 58 | 685115   | 380 | 941959   | 116 | 743156   | 497 | 256844    | 2  |
| 59 | 685343   | 380 | 941889   | 117 | 743454   | 497 | 256546    | 1  |
| 60 | 685571   | 380 | 941819   | 117 | 743752   | 496 | 256248    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

47

| 29° |          |     |          |     |          |     | 150°      |    |
|-----|----------|-----|----------|-----|----------|-----|-----------|----|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
| 0   | 9.685571 | 380 | 9.941819 | 117 | 9.743752 | 496 | 10.256248 | 60 |
| 1   | 685799   | 379 | 941749   | 117 | 744050   | 496 | 255650    | 59 |
| 2   | 686027   | 379 | 941679   | 117 | 744348   | 496 | 255652    | 58 |
| 3   | 686254   | 379 | 941609   | 117 | 744645   | 496 | 255355    | 57 |
| 4   | 686482   | 379 | 941539   | 117 | 744943   | 496 | 255057    | 56 |
| 5   | 686709   | 378 | 941469   | 117 | 745240   | 496 | 254760    | 55 |
| 6   | 686936   | 378 | 941398   | 117 | 745538   | 495 | 254462    | 54 |
| 7   | 687163   | 378 | 941328   | 117 | 745835   | 495 | 254165    | 53 |
| 8   | 687389   | 378 | 941258   | 117 | 746132   | 495 | 253868    | 52 |
| 9   | 687616   | 377 | 941187   | 117 | 746429   | 495 | 253571    | 51 |
| 10  | 687843   | 377 | 941117   | 117 | 746726   | 495 | 253274    | 50 |
| 11  | 9.688069 | 377 | 9.941046 | 118 | 9.747023 | 494 | 10.252977 | 49 |
| 12  | 688295   | 377 | 940975   | 118 | 747319   | 494 | 252681    | 48 |
| 13  | 688521   | 376 | 940905   | 118 | 747616   | 494 | 252384    | 47 |
| 14  | 688747   | 376 | 940834   | 118 | 747913   | 494 | 252087    | 46 |
| 15  | 688972   | 376 | 940763   | 118 | 748209   | 494 | 251791    | 45 |
| 16  | 689198   | 376 | 940693   | 118 | 748505   | 493 | 251495    | 44 |
| 17  | 689423   | 375 | 940622   | 118 | 748801   | 493 | 251199    | 43 |
| 18  | 689648   | 375 | 940551   | 118 | 749097   | 493 | 250903    | 42 |
| 19  | 689873   | 375 | 940480   | 118 | 749393   | 493 | 250607    | 41 |
| 20  | 690098   | 375 | 940409   | 118 | 749689   | 493 | 250311    | 40 |
| 21  | 9.690323 | 374 | 9.940338 | 118 | 9.749985 | 493 | 10.250015 | 39 |
| 22  | 690548   | 374 | 940267   | 118 | 750281   | 492 | 249719    | 38 |
| 23  | 690772   | 374 | 940196   | 118 | 750576   | 492 | 249424    | 37 |
| 24  | 690996   | 374 | 940125   | 119 | 750872   | 492 | 249128    | 36 |
| 25  | 691220   | 373 | 940054   | 119 | 751167   | 492 | 248833    | 35 |
| 26  | 691444   | 373 | 939982   | 119 | 751462   | 492 | 248538    | 34 |
| 27  | 691668   | 373 | 939911   | 119 | 751757   | 492 | 248243    | 33 |
| 28  | 691892   | 373 | 939840   | 119 | 752052   | 491 | 247948    | 32 |
| 29  | 692115   | 372 | 939768   | 119 | 752347   | 491 | 247653    | 31 |
| 30  | 692339   | 372 | 939697   | 119 | 752642   | 491 | 247358    | 30 |
| 31  | 9.692562 | 372 | 9.939625 | 119 | 9.752937 | 491 | 10.247063 | 29 |
| 32  | 692785   | 371 | 939554   | 119 | 753231   | 491 | 246769    | 28 |
| 33  | 693008   | 371 | 939482   | 119 | 753526   | 491 | 246474    | 27 |
| 34  | 693231   | 371 | 939410   | 119 | 753820   | 490 | 246180    | 26 |
| 35  | 693453   | 371 | 939339   | 119 | 754115   | 490 | 245885    | 25 |
| 36  | 693676   | 370 | 939267   | 120 | 754409   | 490 | 245591    | 24 |
| 37  | 693898   | 370 | 939195   | 120 | 754703   | 490 | 245297    | 23 |
| 38  | 694120   | 370 | 939123   | 120 | 754997   | 490 | 245003    | 22 |
| 39  | 694342   | 370 | 939052   | 120 | 755291   | 490 | 244709    | 21 |
| 40  | 694564   | 369 | 938980   | 120 | 755585   | 489 | 244415    | 20 |
| 41  | 9.694786 | 369 | 9.938908 | 120 | 9.755878 | 489 | 10.244122 | 19 |
| 42  | 695007   | 369 | 938836   | 120 | 756172   | 489 | 243828    | 18 |
| 43  | 695229   | 369 | 938763   | 120 | 756465   | 489 | 243535    | 17 |
| 44  | 695450   | 368 | 938691   | 120 | 756759   | 489 | 243241    | 16 |
| 45  | 695671   | 368 | 938619   | 120 | 757052   | 489 | 242948    | 15 |
| 46  | 695892   | 368 | 938547   | 120 | 757345   | 488 | 242655    | 14 |
| 47  | 696113   | 368 | 938475   | 120 | 757638   | 488 | 242362    | 13 |
| 48  | 696334   | 367 | 938402   | 121 | 757931   | 488 | 242069    | 12 |
| 49  | 696554   | 367 | 938330   | 121 | 758224   | 488 | 241776    | 11 |
| 50  | 696775   | 367 | 938258   | 121 | 758517   | 488 | 241483    | 10 |
| 51  | 9.696995 | 367 | 9.938185 | 121 | 9.758810 | 488 | 10.241190 | 9  |
| 52  | 697215   | 366 | 938113   | 121 | 759102   | 487 | 240898    | 8  |
| 53  | 697435   | 366 | 938040   | 121 | 759395   | 487 | 240605    | 7  |
| 54  | 697654   | 366 | 937967   | 121 | 759687   | 487 | 240313    | 6  |
| 55  | 697874   | 366 | 937895   | 121 | 759979   | 487 | 240021    | 5  |
| 56  | 698094   | 365 | 937822   | 121 | 760272   | 487 | 239728    | 4  |
| 57  | 698313   | 365 | 937749   | 121 | 760564   | 487 | 239436    | 3  |
| 58  | 698532   | 365 | 937676   | 121 | 760856   | 486 | 239144    | 2  |
| 59  | 698751   | 365 | 937604   | 121 | 761148   | 486 | 238852    | 1  |
| 60  | 698970   | 364 | 937531   | 121 | 761439   | 486 | 238561    | 0  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

119°

60°

10°

100°

|    | Sec.    | D.   | Cotang. | D.  | Tang.   | D.  | Cotang.  |    |
|----|---------|------|---------|-----|---------|-----|----------|----|
| 1  | 9.99999 | 35.4 | 9.99999 | 121 | 9.99999 | 486 | 10.23856 | 60 |
| 2  | 9.99999 | 35.4 | 9.99999 | 122 | 9.99999 | 486 | 10.23856 | 59 |
| 3  | 9.99999 | 35.4 | 9.99999 | 123 | 9.99999 | 486 | 10.23856 | 58 |
| 4  | 9.99999 | 35.4 | 9.99999 | 124 | 9.99999 | 486 | 10.23856 | 57 |
| 5  | 9.99999 | 35.4 | 9.99999 | 125 | 9.99999 | 486 | 10.23856 | 56 |
| 6  | 9.99999 | 35.4 | 9.99999 | 126 | 9.99999 | 486 | 10.23856 | 55 |
| 7  | 9.99999 | 35.4 | 9.99999 | 127 | 9.99999 | 486 | 10.23856 | 54 |
| 8  | 9.99999 | 35.4 | 9.99999 | 128 | 9.99999 | 486 | 10.23856 | 53 |
| 9  | 9.99999 | 35.4 | 9.99999 | 129 | 9.99999 | 486 | 10.23856 | 52 |
| 10 | 9.99999 | 35.4 | 9.99999 | 130 | 9.99999 | 486 | 10.23856 | 51 |
| 11 | 9.99999 | 35.4 | 9.99999 | 131 | 9.99999 | 486 | 10.23856 | 50 |
| 12 | 9.99999 | 35.4 | 9.99999 | 132 | 9.99999 | 486 | 10.23856 | 49 |
| 13 | 9.99999 | 35.4 | 9.99999 | 133 | 9.99999 | 486 | 10.23856 | 48 |
| 14 | 9.99999 | 35.4 | 9.99999 | 134 | 9.99999 | 486 | 10.23856 | 47 |
| 15 | 9.99999 | 35.4 | 9.99999 | 135 | 9.99999 | 486 | 10.23856 | 46 |
| 16 | 9.99999 | 35.4 | 9.99999 | 136 | 9.99999 | 486 | 10.23856 | 45 |
| 17 | 9.99999 | 35.4 | 9.99999 | 137 | 9.99999 | 486 | 10.23856 | 44 |
| 18 | 9.99999 | 35.4 | 9.99999 | 138 | 9.99999 | 486 | 10.23856 | 43 |
| 19 | 9.99999 | 35.4 | 9.99999 | 139 | 9.99999 | 486 | 10.23856 | 42 |
| 20 | 9.99999 | 35.4 | 9.99999 | 140 | 9.99999 | 486 | 10.23856 | 41 |
| 21 | 9.99999 | 35.4 | 9.99999 | 141 | 9.99999 | 486 | 10.23856 | 40 |
| 22 | 9.99999 | 35.4 | 9.99999 | 142 | 9.99999 | 486 | 10.23856 | 39 |
| 23 | 9.99999 | 35.4 | 9.99999 | 143 | 9.99999 | 486 | 10.23856 | 38 |
| 24 | 9.99999 | 35.4 | 9.99999 | 144 | 9.99999 | 486 | 10.23856 | 37 |
| 25 | 9.99999 | 35.4 | 9.99999 | 145 | 9.99999 | 486 | 10.23856 | 36 |
| 26 | 9.99999 | 35.4 | 9.99999 | 146 | 9.99999 | 486 | 10.23856 | 35 |
| 27 | 9.99999 | 35.4 | 9.99999 | 147 | 9.99999 | 486 | 10.23856 | 34 |
| 28 | 9.99999 | 35.4 | 9.99999 | 148 | 9.99999 | 486 | 10.23856 | 33 |
| 29 | 9.99999 | 35.4 | 9.99999 | 149 | 9.99999 | 486 | 10.23856 | 32 |
| 30 | 9.99999 | 35.4 | 9.99999 | 150 | 9.99999 | 486 | 10.23856 | 31 |
| 31 | 9.99999 | 35.4 | 9.99999 | 151 | 9.99999 | 486 | 10.23856 | 30 |
| 32 | 9.99999 | 35.4 | 9.99999 | 152 | 9.99999 | 486 | 10.23856 | 29 |
| 33 | 9.99999 | 35.4 | 9.99999 | 153 | 9.99999 | 486 | 10.23856 | 28 |
| 34 | 9.99999 | 35.4 | 9.99999 | 154 | 9.99999 | 486 | 10.23856 | 27 |
| 35 | 9.99999 | 35.4 | 9.99999 | 155 | 9.99999 | 486 | 10.23856 | 26 |
| 36 | 9.99999 | 35.4 | 9.99999 | 156 | 9.99999 | 486 | 10.23856 | 25 |
| 37 | 9.99999 | 35.4 | 9.99999 | 157 | 9.99999 | 486 | 10.23856 | 24 |
| 38 | 9.99999 | 35.4 | 9.99999 | 158 | 9.99999 | 486 | 10.23856 | 23 |
| 39 | 9.99999 | 35.4 | 9.99999 | 159 | 9.99999 | 486 | 10.23856 | 22 |
| 40 | 9.99999 | 35.4 | 9.99999 | 160 | 9.99999 | 486 | 10.23856 | 21 |
| 41 | 9.99999 | 35.4 | 9.99999 | 161 | 9.99999 | 486 | 10.23856 | 20 |
| 42 | 9.99999 | 35.4 | 9.99999 | 162 | 9.99999 | 486 | 10.23856 | 19 |
| 43 | 9.99999 | 35.4 | 9.99999 | 163 | 9.99999 | 486 | 10.23856 | 18 |
| 44 | 9.99999 | 35.4 | 9.99999 | 164 | 9.99999 | 486 | 10.23856 | 17 |
| 45 | 9.99999 | 35.4 | 9.99999 | 165 | 9.99999 | 486 | 10.23856 | 16 |
| 46 | 9.99999 | 35.4 | 9.99999 | 166 | 9.99999 | 486 | 10.23856 | 15 |
| 47 | 9.99999 | 35.4 | 9.99999 | 167 | 9.99999 | 486 | 10.23856 | 14 |
| 48 | 9.99999 | 35.4 | 9.99999 | 168 | 9.99999 | 486 | 10.23856 | 13 |
| 49 | 9.99999 | 35.4 | 9.99999 | 169 | 9.99999 | 486 | 10.23856 | 12 |
| 50 | 9.99999 | 35.4 | 9.99999 | 170 | 9.99999 | 486 | 10.23856 | 11 |
| 51 | 9.99999 | 35.4 | 9.99999 | 171 | 9.99999 | 486 | 10.23856 | 10 |
| 52 | 9.99999 | 35.4 | 9.99999 | 172 | 9.99999 | 486 | 10.23856 | 9  |
| 53 | 9.99999 | 35.4 | 9.99999 | 173 | 9.99999 | 486 | 10.23856 | 8  |
| 54 | 9.99999 | 35.4 | 9.99999 | 174 | 9.99999 | 486 | 10.23856 | 7  |
| 55 | 9.99999 | 35.4 | 9.99999 | 175 | 9.99999 | 486 | 10.23856 | 6  |
| 56 | 9.99999 | 35.4 | 9.99999 | 176 | 9.99999 | 486 | 10.23856 | 5  |
| 57 | 9.99999 | 35.4 | 9.99999 | 177 | 9.99999 | 486 | 10.23856 | 4  |
| 58 | 9.99999 | 35.4 | 9.99999 | 178 | 9.99999 | 486 | 10.23856 | 3  |
| 59 | 9.99999 | 35.4 | 9.99999 | 179 | 9.99999 | 486 | 10.23856 | 2  |
| 60 | 9.99999 | 35.4 | 9.99999 | 180 | 9.99999 | 486 | 10.23856 | 1  |
|    | 9.99999 | 35.4 | 9.99999 | 181 | 9.99999 | 486 | 10.23856 | 0  |
|    | Cotang. | D.   | Sine.   | D.  | Cotang. | D.  | Tang.    |    |

120°

59°



TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 81°  |          |     |          |     |          |     |           | 149° |  |
|------|----------|-----|----------|-----|----------|-----|-----------|------|--|
| /    | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |
| 0    | 9.711839 | 350 | 9.933066 | 126 | 9.778774 | 477 | 10.221226 | 60   |  |
| 1    | 712050   | 350 | 932990   | 127 | 779060   | 477 | 220940    | 59   |  |
| 2    | 712260   | 350 | 932914   | 127 | 779346   | 476 | 220654    | 58   |  |
| 3    | 712469   | 349 | 932838   | 127 | 779632   | 476 | 220368    | 57   |  |
| 4    | 712679   | 349 | 932762   | 127 | 779918   | 476 | 220082    | 56   |  |
| 5    | 712889   | 349 | 932685   | 127 | 780203   | 476 | 219797    | 55   |  |
| 6    | 713098   | 349 | 932609   | 127 | 780489   | 476 | 219511    | 54   |  |
| 7    | 713308   | 349 | 932533   | 127 | 780775   | 476 | 219225    | 53   |  |
| 8    | 713517   | 348 | 932457   | 127 | 781060   | 476 | 218940    | 52   |  |
| 9    | 713726   | 348 | 932380   | 127 | 781346   | 475 | 218654    | 51   |  |
| 10   | 713935   | 348 | 932304   | 127 | 781631   | 475 | 218369    | 50   |  |
| 11   | 9.714144 | 348 | 9.932228 | 127 | 9.781916 | 475 | 10.218084 | 49   |  |
| 12   | 714352   | 347 | 932151   | 127 | 782201   | 475 | 217799    | 48   |  |
| 13   | 714561   | 347 | 932075   | 128 | 782486   | 475 | 217514    | 47   |  |
| 14   | 714769   | 347 | 931998   | 128 | 782771   | 475 | 217229    | 46   |  |
| 15   | 714978   | 347 | 931921   | 128 | 783056   | 475 | 216944    | 45   |  |
| 16   | 715186   | 347 | 931845   | 128 | 783341   | 475 | 216659    | 44   |  |
| 17   | 715394   | 346 | 931768   | 128 | 783626   | 474 | 216374    | 43   |  |
| 18   | 715602   | 346 | 931691   | 128 | 783910   | 474 | 216090    | 42   |  |
| 19   | 715809   | 346 | 931614   | 128 | 784195   | 474 | 215805    | 41   |  |
| 20   | 716017   | 346 | 931537   | 128 | 784479   | 474 | 215521    | 40   |  |
| 21   | 9.716224 | 345 | 9.931460 | 128 | 9.784764 | 474 | 10.215236 | 39   |  |
| 22   | 716432   | 345 | 931383   | 128 | 785048   | 474 | 214952    | 38   |  |
| 23   | 716639   | 345 | 931306   | 128 | 785332   | 473 | 214668    | 37   |  |
| 24   | 716846   | 345 | 931229   | 129 | 785616   | 473 | 214384    | 36   |  |
| 25   | 717053   | 345 | 931152   | 129 | 785900   | 473 | 214100    | 35   |  |
| 26   | 717259   | 344 | 931075   | 129 | 786184   | 473 | 213816    | 34   |  |
| 27   | 717466   | 344 | 930998   | 129 | 786468   | 473 | 213532    | 33   |  |
| 28   | 717673   | 344 | 930921   | 129 | 786752   | 473 | 213248    | 32   |  |
| 29   | 717879   | 344 | 930843   | 129 | 787036   | 473 | 212964    | 31   |  |
| 30   | 718085   | 343 | 930766   | 129 | 787319   | 472 | 212681    | 30   |  |
| 31   | 9.718291 | 343 | 9.930688 | 129 | 9.787603 | 472 | 10.212397 | 29   |  |
| 32   | 718497   | 343 | 930611   | 129 | 787886   | 472 | 212114    | 28   |  |
| 33   | 718703   | 343 | 930533   | 129 | 788170   | 472 | 211830    | 27   |  |
| 34   | 718909   | 343 | 930456   | 129 | 788453   | 472 | 211547    | 26   |  |
| 35   | 719114   | 342 | 930378   | 129 | 788736   | 472 | 211264    | 25   |  |
| 36   | 719320   | 342 | 930300   | 130 | 789019   | 472 | 210981    | 24   |  |
| 37   | 719525   | 342 | 930223   | 130 | 789302   | 471 | 210698    | 23   |  |
| 38   | 719730   | 342 | 930145   | 130 | 789585   | 471 | 210415    | 22   |  |
| 39   | 719935   | 341 | 930067   | 130 | 789868   | 471 | 210132    | 21   |  |
| 40   | 720140   | 341 | 929989   | 130 | 790151   | 471 | 209849    | 20   |  |
| 41   | 9.720345 | 341 | 9.929911 | 130 | 9.790434 | 471 | 10.209566 | 19   |  |
| 42   | 720549   | 341 | 929833   | 130 | 790716   | 471 | 209284    | 18   |  |
| 43   | 720754   | 340 | 929755   | 130 | 790999   | 471 | 209001    | 17   |  |
| 44   | 720958   | 340 | 929677   | 130 | 791281   | 471 | 208719    | 16   |  |
| 45   | 721162   | 340 | 929599   | 130 | 791563   | 470 | 208437    | 15   |  |
| 46   | 721366   | 340 | 929521   | 130 | 791846   | 470 | 208154    | 14   |  |
| 47   | 721570   | 340 | 929442   | 130 | 792128   | 470 | 207872    | 13   |  |
| 48   | 721774   | 339 | 929364   | 131 | 792410   | 470 | 207590    | 12   |  |
| 49   | 721978   | 339 | 929286   | 131 | 792692   | 470 | 207308    | 11   |  |
| 50   | 722181   | 339 | 929207   | 131 | 792974   | 470 | 207026    | 10   |  |
| 51   | 9.722385 | 339 | 9.929129 | 131 | 9.793256 | 470 | 10.206744 | 9    |  |
| 52   | 722588   | 339 | 929050   | 131 | 793538   | 469 | 206462    | 8    |  |
| 53   | 722791   | 338 | 928972   | 131 | 793819   | 469 | 206181    | 7    |  |
| 54   | 722994   | 338 | 928893   | 131 | 794101   | 469 | 205899    | 6    |  |
| 55   | 723197   | 338 | 928815   | 131 | 794383   | 469 | 205617    | 5    |  |
| 56   | 723400   | 338 | 928736   | 131 | 794664   | 469 | 205336    | 4    |  |
| 57   | 723603   | 337 | 928657   | 131 | 794946   | 469 | 205054    | 3    |  |
| 58   | 723805   | 337 | 928578   | 131 | 795227   | 469 | 204773    | 2    |  |
| 59   | 724007   | 337 | 928499   | 131 | 795508   | 468 | 204492    | 1    |  |
| 60   | 724210   | 337 | 928420   | 131 | 795789   | 468 | 204211    | 0    |  |
| /    | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |
| 121° |          |     |          |     |          |     |           |      |  |
| 58°  |          |     |          |     |          |     |           |      |  |

| 50   |          | LOGARITHMIC SINES, TANGENTS, ETC. |          |     |          |     |           | TABLE II. |  |
|------|----------|-----------------------------------|----------|-----|----------|-----|-----------|-----------|--|
| 32°  |          |                                   |          |     |          |     |           | 147°      |  |
| /    | Sine.    | D.                                | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /         |  |
| 0    | 9.724210 | 337                               | 9.928420 | 132 | 9.795789 | 468 | 10.204211 | 60        |  |
| 1    | 724412   | 337                               | 928342   | 132 | 796070   | 468 | 203930    | 59        |  |
| 2    | 724614   | 336                               | 928263   | 132 | 796351   | 468 | 203649    | 58        |  |
| 3    | 724816   | 336                               | 928183   | 132 | 796632   | 468 | 203368    | 57        |  |
| 4    | 725017   | 336                               | 928104   | 132 | 796913   | 468 | 203087    | 56        |  |
| 5    | 725219   | 336                               | 928025   | 132 | 797194   | 468 | 202806    | 55        |  |
| 6    | 725420   | 335                               | 927946   | 132 | 797474   | 468 | 202526    | 54        |  |
| 7    | 725622   | 335                               | 927867   | 132 | 797755   | 468 | 202245    | 53        |  |
| 8    | 725823   | 335                               | 927787   | 132 | 798036   | 467 | 201964    | 52        |  |
| 9    | 726024   | 335                               | 927708   | 132 | 798316   | 467 | 201684    | 51        |  |
| 10   | 726225   | 335                               | 927629   | 132 | 798596   | 467 | 201404    | 50        |  |
| 11   | 9.726426 | 334                               | 9.927549 | 132 | 9.798877 | 467 | 10.201123 | 49        |  |
| 12   | 726626   | 334                               | 927470   | 133 | 799157   | 467 | 200843    | 48        |  |
| 13   | 726827   | 334                               | 927390   | 133 | 799437   | 467 | 200563    | 47        |  |
| 14   | 727027   | 334                               | 927310   | 133 | 799717   | 467 | 200283    | 46        |  |
| 15   | 727228   | 334                               | 927231   | 133 | 799997   | 466 | 200003    | 45        |  |
| 16   | 727428   | 333                               | 927151   | 133 | 800277   | 466 | 199723    | 44        |  |
| 17   | 727628   | 333                               | 927071   | 133 | 800557   | 466 | 199443    | 43        |  |
| 18   | 727828   | 333                               | 926991   | 133 | 800836   | 466 | 199164    | 42        |  |
| 19   | 728027   | 333                               | 926911   | 133 | 801116   | 466 | 198884    | 41        |  |
| 20   | 728227   | 333                               | 926831   | 133 | 801396   | 466 | 198604    | 40        |  |
| 21   | 9.728427 | 332                               | 9.926751 | 133 | 9.801675 | 466 | 10.198325 | 39        |  |
| 22   | 728626   | 332                               | 926671   | 133 | 801955   | 466 | 198045    | 38        |  |
| 23   | 728825   | 332                               | 926591   | 133 | 802234   | 465 | 197766    | 37        |  |
| 24   | 729024   | 332                               | 926511   | 134 | 802513   | 465 | 197487    | 36        |  |
| 25   | 729223   | 331                               | 926431   | 134 | 802792   | 465 | 197208    | 35        |  |
| 26   | 729422   | 331                               | 926351   | 134 | 803072   | 465 | 196928    | 34        |  |
| 27   | 729621   | 331                               | 926270   | 134 | 803351   | 465 | 196649    | 33        |  |
| 28   | 729820   | 331                               | 926190   | 134 | 803630   | 465 | 196370    | 32        |  |
| 29   | 730018   | 330                               | 926110   | 134 | 803909   | 465 | 196091    | 31        |  |
| 30   | 730217   | 330                               | 926029   | 134 | 804187   | 465 | 195813    | 30        |  |
| 31   | 9.730415 | 330                               | 9.925949 | 134 | 9.804466 | 464 | 10.195534 | 29        |  |
| 32   | 730613   | 330                               | 925868   | 134 | 804745   | 464 | 195255    | 28        |  |
| 33   | 730811   | 330                               | 925788   | 134 | 805023   | 464 | 194977    | 27        |  |
| 34   | 731009   | 329                               | 925707   | 134 | 805302   | 464 | 194698    | 26        |  |
| 35   | 731206   | 329                               | 925626   | 134 | 805580   | 464 | 194420    | 25        |  |
| 36   | 731404   | 329                               | 925545   | 135 | 805859   | 464 | 194141    | 24        |  |
| 37   | 731602   | 329                               | 925465   | 135 | 806137   | 464 | 193863    | 23        |  |
| 38   | 731799   | 329                               | 925384   | 135 | 806415   | 463 | 193585    | 22        |  |
| 39   | 731996   | 328                               | 925303   | 135 | 806693   | 463 | 193307    | 21        |  |
| 40   | 732193   | 328                               | 925222   | 135 | 806971   | 463 | 193029    | 20        |  |
| 41   | 9.732390 | 328                               | 9.925141 | 135 | 9.807249 | 463 | 10.192751 | 19        |  |
| 42   | 732587   | 328                               | 925060   | 135 | 807527   | 463 | 192473    | 18        |  |
| 43   | 732784   | 328                               | 924979   | 135 | 807805   | 463 | 192195    | 17        |  |
| 44   | 732980   | 327                               | 924897   | 135 | 808083   | 463 | 191917    | 16        |  |
| 45   | 733177   | 327                               | 924816   | 135 | 808361   | 463 | 191639    | 15        |  |
| 46   | 733373   | 327                               | 924735   | 136 | 808638   | 462 | 191362    | 14        |  |
| 47   | 733569   | 327                               | 924654   | 136 | 808916   | 462 | 191084    | 13        |  |
| 48   | 733765   | 327                               | 924572   | 136 | 809193   | 462 | 190807    | 12        |  |
| 49   | 733961   | 326                               | 924491   | 136 | 809471   | 462 | 190529    | 11        |  |
| 50   | 734157   | 326                               | 924409   | 136 | 809748   | 462 | 190252    | 10        |  |
| 51   | 9.734353 | 326                               | 9.924328 | 136 | 9.810025 | 462 | 10.189975 | 9         |  |
| 52   | 734549   | 326                               | 924246   | 136 | 810302   | 462 | 189698    | 8         |  |
| 53   | 734744   | 325                               | 924164   | 136 | 810580   | 462 | 189420    | 7         |  |
| 54   | 734939   | 325                               | 924083   | 136 | 810857   | 462 | 189143    | 6         |  |
| 55   | 735135   | 325                               | 924001   | 136 | 811134   | 461 | 188866    | 5         |  |
| 56   | 735330   | 325                               | 923919   | 136 | 811410   | 461 | 188589    | 4         |  |
| 57   | 735525   | 325                               | 923837   | 136 | 811687   | 461 | 188313    | 3         |  |
| 58   | 735719   | 324                               | 923755   | 137 | 811964   | 461 | 188036    | 2         |  |
| 59   | 735914   | 324                               | 923673   | 137 | 812241   | 461 | 187759    | 1         |  |
| 60   | 736109   | 324                               | 923591   | 137 | 812517   | 461 | 187483    | 0         |  |
| /    | Cosine.  | D.                                | Sine.    | D.  | Cotang.  | D.  | Tang.     | /         |  |
| 122° |          |                                   |          |     |          |     |           | 57°       |  |

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 33° |          |     |          |     |          |     |           | 146° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9.736109 | 324 | 9.923591 | 137 | 9.812517 | 461 | 10.187483 | 60   |  |  |  |  |  |  |  |
| 1   | 736303   | 324 | 923509   | 137 | 812794   | 461 | 187206    | 59   |  |  |  |  |  |  |  |
| 2   | 736498   | 324 | 923427   | 137 | 813070   | 461 | 186930    | 58   |  |  |  |  |  |  |  |
| 3   | 736692   | 323 | 923345   | 137 | 813347   | 460 | 186653    | 57   |  |  |  |  |  |  |  |
| 4   | 736886   | 323 | 923263   | 137 | 813623   | 460 | 186377    | 56   |  |  |  |  |  |  |  |
| 5   | 737080   | 323 | 923181   | 137 | 813899   | 460 | 186101    | 55   |  |  |  |  |  |  |  |
| 6   | 737274   | 323 | 923098   | 137 | 814176   | 460 | 185824    | 54   |  |  |  |  |  |  |  |
| 7   | 737467   | 323 | 923016   | 137 | 814452   | 460 | 185548    | 53   |  |  |  |  |  |  |  |
| 8   | 737661   | 322 | 922933   | 137 | 814728   | 460 | 185272    | 52   |  |  |  |  |  |  |  |
| 9   | 737855   | 322 | 922851   | 137 | 815004   | 460 | 184996    | 51   |  |  |  |  |  |  |  |
| 10  | 738048   | 322 | 922768   | 138 | 815280   | 460 | 184720    | 50   |  |  |  |  |  |  |  |
| 11  | 9.738241 | 322 | 9.922686 | 138 | 9.815555 | 459 | 10.184445 | 49   |  |  |  |  |  |  |  |
| 12  | 738434   | 322 | 922603   | 138 | 815831   | 459 | 184169    | 48   |  |  |  |  |  |  |  |
| 13  | 738627   | 321 | 922520   | 138 | 816107   | 459 | 183893    | 47   |  |  |  |  |  |  |  |
| 14  | 738820   | 321 | 922438   | 138 | 816382   | 459 | 183618    | 46   |  |  |  |  |  |  |  |
| 15  | 739013   | 321 | 922355   | 138 | 816658   | 459 | 183342    | 45   |  |  |  |  |  |  |  |
| 16  | 739206   | 321 | 922272   | 138 | 816933   | 459 | 183067    | 44   |  |  |  |  |  |  |  |
| 17  | 739398   | 321 | 922189   | 138 | 817209   | 459 | 182791    | 43   |  |  |  |  |  |  |  |
| 18  | 739590   | 320 | 922106   | 138 | 817484   | 459 | 182516    | 42   |  |  |  |  |  |  |  |
| 19  | 739783   | 320 | 922023   | 138 | 817759   | 459 | 182241    | 41   |  |  |  |  |  |  |  |
| 20  | 739975   | 320 | 921940   | 138 | 818035   | 458 | 181965    | 40   |  |  |  |  |  |  |  |
| 21  | 9.740167 | 320 | 9.921857 | 139 | 9.818310 | 458 | 10.181690 | 39   |  |  |  |  |  |  |  |
| 22  | 740359   | 320 | 921774   | 139 | 818585   | 458 | 181415    | 38   |  |  |  |  |  |  |  |
| 23  | 740550   | 319 | 921691   | 139 | 818860   | 458 | 181140    | 37   |  |  |  |  |  |  |  |
| 24  | 740742   | 319 | 921607   | 139 | 819135   | 458 | 180865    | 36   |  |  |  |  |  |  |  |
| 25  | 740934   | 319 | 921524   | 139 | 819410   | 458 | 180590    | 35   |  |  |  |  |  |  |  |
| 26  | 741125   | 319 | 921441   | 139 | 819684   | 458 | 180316    | 34   |  |  |  |  |  |  |  |
| 27  | 741316   | 319 | 921357   | 139 | 819959   | 458 | 180041    | 33   |  |  |  |  |  |  |  |
| 28  | 741508   | 318 | 921274   | 139 | 820234   | 458 | 179766    | 32   |  |  |  |  |  |  |  |
| 29  | 741699   | 318 | 921190   | 139 | 820508   | 457 | 179492    | 31   |  |  |  |  |  |  |  |
| 30  | 741889   | 318 | 921107   | 139 | 820783   | 457 | 179217    | 30   |  |  |  |  |  |  |  |
| 31  | 9.742080 | 318 | 9.921023 | 139 | 9.821057 | 457 | 10.178943 | 29   |  |  |  |  |  |  |  |
| 32  | 742271   | 318 | 920939   | 140 | 821332   | 457 | 178668    | 28   |  |  |  |  |  |  |  |
| 33  | 742462   | 317 | 920856   | 140 | 821606   | 457 | 178394    | 27   |  |  |  |  |  |  |  |
| 34  | 742652   | 317 | 920772   | 140 | 821880   | 457 | 178120    | 26   |  |  |  |  |  |  |  |
| 35  | 742842   | 317 | 920688   | 140 | 822154   | 457 | 177846    | 25   |  |  |  |  |  |  |  |
| 36  | 743033   | 317 | 920604   | 140 | 822429   | 457 | 177571    | 24   |  |  |  |  |  |  |  |
| 37  | 743223   | 317 | 920520   | 140 | 822703   | 457 | 177297    | 23   |  |  |  |  |  |  |  |
| 38  | 743413   | 316 | 920436   | 140 | 822977   | 456 | 177023    | 22   |  |  |  |  |  |  |  |
| 39  | 743602   | 316 | 920352   | 140 | 823251   | 456 | 176749    | 21   |  |  |  |  |  |  |  |
| 40  | 743792   | 316 | 920268   | 140 | 823524   | 456 | 176476    | 20   |  |  |  |  |  |  |  |
| 41  | 9.743982 | 316 | 9.920184 | 140 | 9.823798 | 456 | 10.176202 | 19   |  |  |  |  |  |  |  |
| 42  | 744171   | 316 | 920099   | 140 | 824072   | 456 | 175928    | 18   |  |  |  |  |  |  |  |
| 43  | 744361   | 315 | 920015   | 140 | 824345   | 456 | 175655    | 17   |  |  |  |  |  |  |  |
| 44  | 744550   | 315 | 919931   | 141 | 824619   | 456 | 175381    | 16   |  |  |  |  |  |  |  |
| 45  | 744739   | 315 | 919846   | 141 | 824893   | 456 | 175107    | 15   |  |  |  |  |  |  |  |
| 46  | 744928   | 315 | 919762   | 141 | 825166   | 456 | 174834    | 14   |  |  |  |  |  |  |  |
| 47  | 745117   | 315 | 919677   | 141 | 825439   | 455 | 174561    | 13   |  |  |  |  |  |  |  |
| 48  | 745306   | 314 | 919593   | 141 | 825713   | 455 | 174287    | 12   |  |  |  |  |  |  |  |
| 49  | 745494   | 314 | 919508   | 141 | 825986   | 455 | 174014    | 11   |  |  |  |  |  |  |  |
| 50  | 745683   | 314 | 919424   | 141 | 826259   | 455 | 173741    | 10   |  |  |  |  |  |  |  |
| 51  | 9.745871 | 314 | 9.919339 | 141 | 9.826532 | 455 | 10.173468 | 9    |  |  |  |  |  |  |  |
| 52  | 746060   | 314 | 919254   | 141 | 826805   | 455 | 173195    | 8    |  |  |  |  |  |  |  |
| 53  | 746248   | 313 | 919169   | 141 | 827078   | 455 | 172922    | 7    |  |  |  |  |  |  |  |
| 54  | 746436   | 313 | 919085   | 141 | 827351   | 455 | 172649    | 6    |  |  |  |  |  |  |  |
| 55  | 746624   | 313 | 919000   | 141 | 827624   | 455 | 172376    | 5    |  |  |  |  |  |  |  |
| 56  | 746812   | 313 | 918915   | 142 | 827897   | 454 | 172103    | 4    |  |  |  |  |  |  |  |
| 57  | 746999   | 313 | 918830   | 142 | 828170   | 454 | 171830    | 3    |  |  |  |  |  |  |  |
| 58  | 747187   | 312 | 918745   | 142 | 828442   | 454 | 171558    | 2    |  |  |  |  |  |  |  |
| 59  | 747374   | 312 | 918659   | 142 | 828715   | 454 | 171285    | 1    |  |  |  |  |  |  |  |
| 60  | 747562   | 312 | 918574   | 142 | 828987   | 454 | 171013    | 0    |  |  |  |  |  |  |  |
| /   | Sine.    | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

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24°

145°

| /  | Sine.    | D.  | Co. no.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.747562 | 212 | 9.918574 | 142 | 9.828987 | 454 | 10.171013 | 60 |
| 1  | 747749   | 212 | 918489   | 142 | 829260   | 454 | 170740    | 59 |
| 2  | 747936   | 212 | 918404   | 142 | 829532   | 454 | 170468    | 58 |
| 3  | 748123   | 211 | 918318   | 142 | 829805   | 454 | 170195    | 57 |
| 4  | 748310   | 211 | 918233   | 142 | 830077   | 454 | 169923    | 56 |
| 5  | 748497   | 211 | 918147   | 142 | 830349   | 453 | 169651    | 55 |
| 6  | 748683   | 211 | 918062   | 142 | 830621   | 453 | 169379    | 54 |
| 7  | 748870   | 211 | 917976   | 143 | 830893   | 453 | 169107    | 53 |
| 8  | 749056   | 210 | 917891   | 143 | 831165   | 453 | 168835    | 52 |
| 9  | 749243   | 210 | 917805   | 143 | 831437   | 453 | 168563    | 51 |
| 10 | 749429   | 210 | 917719   | 143 | 831709   | 453 | 168291    | 50 |
| 11 | 9.749615 | 210 | 9.917634 | 143 | 9.831981 | 453 | 10.168019 | 49 |
| 12 | 749801   | 210 | 917548   | 143 | 832253   | 453 | 167747    | 48 |
| 13 | 749987   | 209 | 917462   | 143 | 832525   | 453 | 167475    | 47 |
| 14 | 750172   | 209 | 917376   | 143 | 832796   | 453 | 167204    | 46 |
| 15 | 750358   | 209 | 917290   | 143 | 833068   | 452 | 166932    | 45 |
| 16 | 750543   | 209 | 917204   | 143 | 833339   | 452 | 166661    | 44 |
| 17 | 750729   | 209 | 917118   | 144 | 833611   | 452 | 166389    | 43 |
| 18 | 750914   | 208 | 917032   | 144 | 833882   | 452 | 166118    | 42 |
| 19 | 751099   | 208 | 916946   | 144 | 834154   | 452 | 165846    | 41 |
| 20 | 751284   | 208 | 916859   | 144 | 834425   | 452 | 165575    | 40 |
| 21 | 9.751469 | 208 | 9.916773 | 144 | 9.834696 | 452 | 10.165304 | 39 |
| 22 | 751654   | 208 | 916687   | 144 | 834967   | 452 | 165033    | 38 |
| 23 | 751839   | 208 | 916600   | 144 | 835238   | 452 | 164762    | 37 |
| 24 | 752023   | 207 | 916514   | 144 | 835509   | 452 | 164491    | 36 |
| 25 | 752208   | 207 | 916427   | 144 | 835780   | 451 | 164220    | 35 |
| 26 | 752392   | 207 | 916341   | 144 | 836051   | 451 | 163949    | 34 |
| 27 | 752576   | 207 | 916254   | 144 | 836322   | 451 | 163678    | 33 |
| 28 | 752760   | 207 | 916167   | 145 | 836593   | 451 | 163407    | 32 |
| 29 | 752944   | 206 | 916081   | 145 | 836864   | 451 | 163136    | 31 |
| 30 | 753128   | 206 | 915994   | 145 | 837134   | 451 | 162866    | 30 |
| 31 | 9.753312 | 206 | 9.915907 | 145 | 9.837405 | 451 | 10.162595 | 29 |
| 32 | 753495   | 206 | 915820   | 145 | 837675   | 451 | 162325    | 28 |
| 33 | 753679   | 206 | 915733   | 145 | 837946   | 451 | 162054    | 27 |
| 34 | 753862   | 205 | 915646   | 145 | 838216   | 451 | 161784    | 26 |
| 35 | 754046   | 205 | 915559   | 145 | 838487   | 450 | 161513    | 25 |
| 36 | 754229   | 205 | 915472   | 145 | 838757   | 450 | 161243    | 24 |
| 37 | 754412   | 205 | 915385   | 145 | 839027   | 450 | 160973    | 23 |
| 38 | 754595   | 205 | 915297   | 145 | 839297   | 450 | 160703    | 22 |
| 39 | 754778   | 204 | 915210   | 145 | 839568   | 450 | 160432    | 21 |
| 40 | 754960   | 204 | 915123   | 146 | 839838   | 450 | 160162    | 20 |
| 41 | 9.755143 | 204 | 9.915035 | 146 | 9.840108 | 450 | 10.159892 | 19 |
| 42 | 755326   | 204 | 914948   | 146 | 840378   | 450 | 159622    | 18 |
| 43 | 755508   | 204 | 914860   | 146 | 840648   | 450 | 159352    | 17 |
| 44 | 755690   | 204 | 914773   | 146 | 840917   | 449 | 159083    | 16 |
| 45 | 755872   | 203 | 914685   | 146 | 841187   | 449 | 158813    | 15 |
| 46 | 756054   | 203 | 914598   | 146 | 841457   | 449 | 158543    | 14 |
| 47 | 756236   | 203 | 914510   | 146 | 841727   | 449 | 158273    | 13 |
| 48 | 756418   | 203 | 914422   | 146 | 841996   | 449 | 158004    | 12 |
| 49 | 756600   | 203 | 914334   | 146 | 842266   | 449 | 157734    | 11 |
| 50 | 756782   | 202 | 914246   | 147 | 842535   | 449 | 157465    | 10 |
| 51 | 9.756963 | 202 | 9.914158 | 147 | 9.842805 | 449 | 10.157195 | 9  |
| 52 | 757144   | 202 | 914070   | 147 | 843074   | 449 | 156926    | 8  |
| 53 | 757326   | 202 | 913982   | 147 | 843343   | 449 | 156657    | 7  |
| 54 | 757507   | 202 | 913894   | 147 | 843612   | 449 | 156388    | 6  |
| 55 | 757688   | 201 | 913806   | 147 | 843882   | 448 | 156118    | 5  |
| 56 | 757869   | 201 | 913718   | 147 | 844151   | 448 | 155849    | 4  |
| 57 | 758050   | 201 | 913630   | 147 | 844420   | 448 | 155580    | 3  |
| 58 | 758230   | 201 | 913541   | 147 | 844689   | 448 | 155311    | 2  |
| 59 | 758411   | 201 | 913453   | 147 | 844958   | 448 | 155042    | 1  |
| 60 | 758591   | 201 | 913365   | 147 | 845227   | 448 | 154773    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.758591 | 301 | 9.913365 | 147 | 9.845227 | 448 | 10.154773 | 60 |
| 1  | 758772   | 300 | 913276   | 147 | 845496   | 448 | 154504    | 59 |
| 2  | 758952   | 300 | 913187   | 148 | 845764   | 448 | 154236    | 58 |
| 3  | 759132   | 300 | 913099   | 148 | 846033   | 448 | 153967    | 57 |
| 4  | 759312   | 300 | 913010   | 148 | 846302   | 448 | 153698    | 56 |
| 5  | 759492   | 300 | 912922   | 148 | 846570   | 447 | 153430    | 55 |
| 6  | 759672   | 299 | 912833   | 148 | 846839   | 447 | 153161    | 54 |
| 7  | 759852   | 299 | 912744   | 148 | 847108   | 447 | 152892    | 53 |
| 8  | 760031   | 299 | 912655   | 148 | 847376   | 447 | 152624    | 52 |
| 9  | 760211   | 299 | 912566   | 148 | 847644   | 447 | 152356    | 51 |
| 10 | 760390   | 299 | 912477   | 148 | 847913   | 447 | 152087    | 50 |
| 11 | 9.760569 | 298 | 9.912388 | 148 | 9.848181 | 447 | 10.151819 | 49 |
| 12 | 760748   | 298 | 912299   | 149 | 848449   | 447 | 151551    | 48 |
| 13 | 760927   | 298 | 912210   | 149 | 848717   | 447 | 151283    | 47 |
| 14 | 761106   | 298 | 912121   | 149 | 848986   | 447 | 151014    | 46 |
| 15 | 761285   | 298 | 912031   | 149 | 849254   | 447 | 150746    | 45 |
| 16 | 761464   | 298 | 911942   | 149 | 849522   | 447 | 150478    | 44 |
| 17 | 761642   | 297 | 911853   | 149 | 849790   | 446 | 150210    | 43 |
| 18 | 761821   | 297 | 911763   | 149 | 850057   | 446 | 149943    | 42 |
| 19 | 761999   | 297 | 911674   | 149 | 850325   | 446 | 149675    | 41 |
| 20 | 762177   | 297 | 911584   | 149 | 850593   | 446 | 149407    | 40 |
| 21 | 9.762356 | 297 | 9.911495 | 149 | 9.850861 | 446 | 10.149139 | 39 |
| 22 | 762534   | 296 | 911405   | 149 | 851129   | 446 | 148871    | 38 |
| 23 | 762712   | 296 | 911315   | 150 | 851396   | 446 | 148604    | 37 |
| 24 | 762890   | 296 | 911226   | 150 | 851664   | 446 | 148336    | 36 |
| 25 | 763067   | 296 | 911136   | 150 | 851931   | 446 | 148069    | 35 |
| 26 | 763245   | 296 | 911046   | 150 | 852199   | 446 | 147801    | 34 |
| 27 | 763422   | 296 | 910956   | 150 | 852466   | 446 | 147534    | 33 |
| 28 | 763600   | 295 | 910866   | 150 | 852733   | 445 | 147267    | 32 |
| 29 | 763777   | 295 | 910776   | 150 | 853001   | 445 | 146999    | 31 |
| 30 | 763954   | 295 | 910686   | 150 | 853268   | 445 | 146732    | 30 |
| 31 | 9.764131 | 295 | 9.910596 | 150 | 9.853535 | 445 | 10.146465 | 29 |
| 32 | 764308   | 295 | 910506   | 150 | 853802   | 445 | 146198    | 28 |
| 33 | 764485   | 294 | 910415   | 150 | 854069   | 445 | 145931    | 27 |
| 34 | 764662   | 294 | 910325   | 151 | 854336   | 445 | 145664    | 26 |
| 35 | 764838   | 294 | 910235   | 151 | 854603   | 445 | 145397    | 25 |
| 36 | 765015   | 294 | 910144   | 151 | 854870   | 445 | 145130    | 24 |
| 37 | 765191   | 294 | 910054   | 151 | 855137   | 445 | 144863    | 23 |
| 38 | 765367   | 294 | 909963   | 151 | 855404   | 445 | 144596    | 22 |
| 39 | 765544   | 293 | 909873   | 151 | 855671   | 444 | 144329    | 21 |
| 40 | 765720   | 293 | 909782   | 151 | 855938   | 444 | 144062    | 20 |
| 41 | 9.765896 | 293 | 9.909691 | 151 | 9.856204 | 444 | 10.143796 | 19 |
| 42 | 766072   | 293 | 909601   | 151 | 856471   | 444 | 143529    | 18 |
| 43 | 766247   | 293 | 909510   | 151 | 856737   | 444 | 143263    | 17 |
| 44 | 766423   | 293 | 909419   | 151 | 857004   | 444 | 142996    | 16 |
| 45 | 766598   | 292 | 909328   | 152 | 857270   | 444 | 142730    | 15 |
| 46 | 766774   | 292 | 909237   | 152 | 857537   | 444 | 142463    | 14 |
| 47 | 766949   | 292 | 909146   | 152 | 857803   | 444 | 142197    | 13 |
| 48 | 767124   | 292 | 909055   | 152 | 858069   | 444 | 141931    | 12 |
| 49 | 767300   | 292 | 908964   | 152 | 858336   | 444 | 141664    | 11 |
| 50 | 767475   | 291 | 908873   | 152 | 858602   | 443 | 141398    | 10 |
| 51 | 9.767649 | 291 | 9.908781 | 152 | 9.858868 | 443 | 10.141132 | 9  |
| 52 | 767824   | 291 | 908690   | 152 | 859134   | 443 | 140866    | 8  |
| 53 | 767999   | 291 | 908599   | 152 | 859400   | 443 | 140600    | 7  |
| 54 | 768173   | 291 | 908507   | 152 | 859666   | 443 | 140334    | 6  |
| 55 | 768348   | 290 | 908416   | 153 | 859932   | 443 | 140068    | 5  |
| 56 | 768522   | 290 | 908324   | 153 | 860198   | 443 | 139802    | 4  |
| 57 | 768697   | 290 | 908233   | 153 | 860464   | 443 | 139536    | 3  |
| 58 | 768871   | 290 | 908141   | 153 | 860730   | 443 | 139270    | 2  |
| 59 | 769045   | 290 | 908049   | 153 | 860995   | 443 | 139005    | 1  |
| 60 | 769219   | 290 | 907958   | 153 | 861261   | 443 | 138739    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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|    | Area.    | D.  | Contn.  | D.  | Tang.    | D.  | Contn.    |    |
|----|----------|-----|---------|-----|----------|-----|-----------|----|
| 0  | 9-769219 | 288 | 9-90958 | 153 | 9-861251 | 443 | 10-138739 | 68 |
| 1  | 769219   | 289 | 9-90958 | 153 | 861257   | 443 | 138739    | 59 |
| 2  | 769219   | 289 | 9-90958 | 153 | 861257   | 443 | 138739    | 58 |
| 3  | 769219   | 289 | 9-90958 | 153 | 862058   | 442 | 137422    | 57 |
| 4  | 769219   | 289 | 9-90958 | 153 | 862323   | 442 | 137077    | 56 |
| 5  | 769219   | 289 | 9-90958 | 153 | 862589   | 442 | 137411    | 55 |
| 6  | 769219   | 288 | 9-90958 | 153 | 862854   | 442 | 137146    | 54 |
| 7  | 769219   | 288 | 9-90958 | 154 | 863119   | 442 | 136881    | 53 |
| 8  | 769219   | 288 | 9-90958 | 154 | 863385   | 442 | 136615    | 52 |
| 9  | 769219   | 288 | 9-90958 | 154 | 863650   | 442 | 136350    | 51 |
| 10 | 769219   | 288 | 9-90958 | 154 | 863915   | 442 | 136085    | 50 |
| 11 | 9-771125 | 288 | 9-90958 | 154 | 9-864180 | 442 | 10-135820 | 46 |
| 12 | 771125   | 289 | 9-90958 | 154 | 864445   | 442 | 135555    | 47 |
| 13 | 771125   | 289 | 9-90958 | 154 | 864710   | 442 | 135290    | 48 |
| 14 | 771125   | 289 | 9-90958 | 154 | 864975   | 441 | 135025    | 49 |
| 15 | 771125   | 289 | 9-90958 | 154 | 865240   | 441 | 134760    | 45 |
| 16 | 771125   | 289 | 9-90958 | 154 | 865505   | 441 | 134495    | 44 |
| 17 | 771125   | 289 | 9-90958 | 155 | 865770   | 441 | 134230    | 43 |
| 18 | 771125   | 289 | 9-90958 | 155 | 866035   | 441 | 133965    | 42 |
| 19 | 771125   | 289 | 9-90958 | 155 | 866300   | 441 | 133700    | 41 |
| 20 | 771125   | 289 | 9-90958 | 155 | 866565   | 441 | 133435    | 40 |
| 21 | 9-772847 | 286 | 9-90958 | 155 | 9-866829 | 441 | 10-133171 | 39 |
| 22 | 772847   | 286 | 9-90958 | 155 | 867094   | 441 | 132906    | 38 |
| 23 | 772847   | 286 | 9-90958 | 155 | 867358   | 441 | 132642    | 37 |
| 24 | 772847   | 285 | 9-90958 | 155 | 867623   | 441 | 132377    | 36 |
| 25 | 772847   | 285 | 9-90958 | 155 | 867887   | 441 | 132113    | 35 |
| 26 | 772847   | 285 | 9-90958 | 155 | 868152   | 440 | 131848    | 34 |
| 27 | 772847   | 285 | 9-90958 | 155 | 868416   | 440 | 131584    | 33 |
| 28 | 772847   | 285 | 9-90958 | 156 | 868680   | 440 | 131320    | 32 |
| 29 | 772847   | 285 | 9-90958 | 156 | 868945   | 440 | 131055    | 31 |
| 30 | 772847   | 284 | 9-90958 | 156 | 869209   | 440 | 130791    | 30 |
| 31 | 9-774558 | 284 | 9-90958 | 156 | 9-869473 | 440 | 10-130527 | 29 |
| 32 | 774558   | 284 | 9-90958 | 156 | 869737   | 440 | 130263    | 28 |
| 33 | 774558   | 284 | 9-90958 | 156 | 870001   | 440 | 129999    | 27 |
| 34 | 774558   | 284 | 9-90958 | 156 | 870265   | 440 | 129735    | 26 |
| 35 | 774558   | 284 | 9-90958 | 156 | 870529   | 440 | 129471    | 25 |
| 36 | 774558   | 283 | 9-90958 | 156 | 870793   | 440 | 129207    | 24 |
| 37 | 774558   | 283 | 9-90958 | 156 | 871057   | 440 | 128943    | 23 |
| 38 | 774558   | 283 | 9-90958 | 157 | 871321   | 440 | 128679    | 22 |
| 39 | 774558   | 283 | 9-90958 | 157 | 871585   | 440 | 128415    | 21 |
| 40 | 774558   | 283 | 9-90958 | 157 | 871849   | 439 | 128151    | 20 |
| 41 | 9-776270 | 283 | 9-90958 | 157 | 9-872112 | 439 | 10-127858 | 19 |
| 42 | 776270   | 282 | 9-90958 | 157 | 872376   | 439 | 127624    | 18 |
| 43 | 776270   | 282 | 9-90958 | 157 | 872640   | 439 | 127360    | 17 |
| 44 | 776270   | 282 | 9-90958 | 157 | 872904   | 439 | 127097    | 16 |
| 45 | 776270   | 281 | 9-90958 | 157 | 873167   | 439 | 126833    | 15 |
| 46 | 776270   | 281 | 9-90958 | 157 | 873430   | 439 | 126570    | 14 |
| 47 | 776270   | 281 | 9-90958 | 160 | 873694   | 439 | 126306    | 13 |
| 48 | 776270   | 281 | 9-90958 | 157 | 873957   | 439 | 126043    | 12 |
| 49 | 776270   | 281 | 9-90958 | 158 | 874220   | 439 | 125780    | 11 |
| 50 | 776270   | 281 | 9-90958 | 158 | 874484   | 439 | 125516    | 10 |
| 51 | 9-777970 | 281 | 9-90958 | 158 | 9-874747 | 439 | 10-125253 | 9  |
| 52 | 777970   | 281 | 9-90958 | 158 | 875010   | 439 | 124990    | 8  |
| 53 | 777970   | 280 | 9-90958 | 158 | 875273   | 438 | 124727    | 7  |
| 54 | 777970   | 280 | 9-90958 | 158 | 875537   | 438 | 124463    | 6  |
| 55 | 777970   | 280 | 9-90958 | 158 | 875800   | 438 | 124200    | 5  |
| 56 | 777970   | 280 | 9-90958 | 158 | 876063   | 438 | 123937    | 4  |
| 57 | 777970   | 280 | 9-90958 | 158 | 876326   | 438 | 123674    | 3  |
| 58 | 777970   | 280 | 9-90958 | 159 | 876589   | 438 | 123411    | 2  |
| 59 | 777970   | 279 | 9-90958 | 159 | 876852   | 438 | 123148    | 1  |
| 60 | 777970   | 279 | 9-90958 | 159 | 877114   | 438 | 122886    | 0  |
| 1  | Contn.   | D.  | Contn.  | D.  | Contn.   | D.  | Tang.     | 1  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 87° |          |     |          |     |          |     |           | 142° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9.779463 | 279 | 9.902349 | 159 | 9.877114 | 438 | 10.122886 | 60   |  |  |  |  |  |  |  |
| 1   | 779631   | 279 | 902253   | 159 | 877377   | 438 | 122623    | 59   |  |  |  |  |  |  |  |
| 2   | 779798   | 279 | 902158   | 159 | 877640   | 438 | 122360    | 58   |  |  |  |  |  |  |  |
| 3   | 779966   | 279 | 902063   | 159 | 877903   | 438 | 122097    | 57   |  |  |  |  |  |  |  |
| 4   | 780133   | 279 | 901967   | 159 | 878165   | 438 | 121835    | 56   |  |  |  |  |  |  |  |
| 5   | 780300   | 278 | 901872   | 159 | 878428   | 438 | 121572    | 55   |  |  |  |  |  |  |  |
| 6   | 780467   | 278 | 901776   | 159 | 878691   | 438 | 121309    | 54   |  |  |  |  |  |  |  |
| 7   | 780634   | 278 | 901681   | 159 | 878953   | 437 | 121047    | 53   |  |  |  |  |  |  |  |
| 8   | 780801   | 278 | 901585   | 159 | 879216   | 437 | 120784    | 52   |  |  |  |  |  |  |  |
| 9   | 780968   | 278 | 901490   | 159 | 879478   | 437 | 120522    | 51   |  |  |  |  |  |  |  |
| 10  | 781134   | 278 | 901394   | 160 | 879741   | 437 | 120259    | 50   |  |  |  |  |  |  |  |
| 11  | 9.781301 | 277 | 9.901298 | 160 | 9.880003 | 437 | 10.119997 | 49   |  |  |  |  |  |  |  |
| 12  | 781468   | 277 | 901202   | 160 | 880265   | 437 | 119735    | 48   |  |  |  |  |  |  |  |
| 13  | 781634   | 277 | 901106   | 160 | 880528   | 437 | 119472    | 47   |  |  |  |  |  |  |  |
| 14  | 781800   | 277 | 901010   | 160 | 880790   | 437 | 119210    | 46   |  |  |  |  |  |  |  |
| 15  | 781966   | 277 | 900914   | 160 | 881052   | 437 | 118948    | 45   |  |  |  |  |  |  |  |
| 16  | 782132   | 277 | 900818   | 160 | 881314   | 437 | 118686    | 44   |  |  |  |  |  |  |  |
| 17  | 782298   | 276 | 900722   | 160 | 881577   | 437 | 118423    | 43   |  |  |  |  |  |  |  |
| 18  | 782464   | 276 | 900626   | 160 | 881839   | 437 | 118161    | 42   |  |  |  |  |  |  |  |
| 19  | 782630   | 276 | 900529   | 160 | 882101   | 437 | 117899    | 41   |  |  |  |  |  |  |  |
| 20  | 782796   | 276 | 900433   | 161 | 882363   | 436 | 117637    | 40   |  |  |  |  |  |  |  |
| 21  | 9.782961 | 276 | 9.900337 | 161 | 9.882625 | 436 | 10.117375 | 39   |  |  |  |  |  |  |  |
| 22  | 783127   | 276 | 900240   | 161 | 882887   | 436 | 117113    | 38   |  |  |  |  |  |  |  |
| 23  | 783292   | 275 | 900144   | 161 | 883148   | 436 | 116852    | 37   |  |  |  |  |  |  |  |
| 24  | 783458   | 275 | 900047   | 161 | 883410   | 436 | 116590    | 36   |  |  |  |  |  |  |  |
| 25  | 783623   | 275 | 899951   | 161 | 883672   | 436 | 116328    | 35   |  |  |  |  |  |  |  |
| 26  | 783788   | 275 | 899854   | 161 | 883934   | 436 | 116066    | 34   |  |  |  |  |  |  |  |
| 27  | 783953   | 275 | 899757   | 161 | 884196   | 436 | 115804    | 33   |  |  |  |  |  |  |  |
| 28  | 784118   | 275 | 899660   | 161 | 884457   | 436 | 115543    | 32   |  |  |  |  |  |  |  |
| 29  | 784282   | 274 | 899564   | 161 | 884719   | 436 | 115281    | 31   |  |  |  |  |  |  |  |
| 30  | 784447   | 274 | 899467   | 162 | 884980   | 436 | 115020    | 30   |  |  |  |  |  |  |  |
| 31  | 9.784612 | 274 | 9.899370 | 162 | 9.885242 | 436 | 10.114758 | 29   |  |  |  |  |  |  |  |
| 32  | 784776   | 274 | 899273   | 162 | 885504   | 436 | 114496    | 28   |  |  |  |  |  |  |  |
| 33  | 784941   | 274 | 899176   | 162 | 885765   | 436 | 114235    | 27   |  |  |  |  |  |  |  |
| 34  | 785105   | 274 | 899078   | 162 | 886026   | 436 | 113974    | 26   |  |  |  |  |  |  |  |
| 35  | 785269   | 273 | 898981   | 162 | 886288   | 436 | 113712    | 25   |  |  |  |  |  |  |  |
| 36  | 785433   | 273 | 898884   | 162 | 886549   | 435 | 113451    | 24   |  |  |  |  |  |  |  |
| 37  | 785597   | 273 | 898787   | 162 | 886811   | 435 | 113189    | 23   |  |  |  |  |  |  |  |
| 38  | 785761   | 273 | 898689   | 162 | 887072   | 435 | 112928    | 22   |  |  |  |  |  |  |  |
| 39  | 785925   | 273 | 898592   | 162 | 887333   | 435 | 112667    | 21   |  |  |  |  |  |  |  |
| 40  | 786089   | 273 | 898494   | 163 | 887594   | 435 | 112406    | 20   |  |  |  |  |  |  |  |
| 41  | 9.786252 | 272 | 9.898397 | 163 | 9.887855 | 435 | 10.112145 | 19   |  |  |  |  |  |  |  |
| 42  | 786416   | 272 | 898299   | 163 | 888116   | 435 | 111884    | 18   |  |  |  |  |  |  |  |
| 43  | 786579   | 272 | 898202   | 163 | 888378   | 435 | 111622    | 17   |  |  |  |  |  |  |  |
| 44  | 786742   | 272 | 898104   | 163 | 888639   | 435 | 111361    | 16   |  |  |  |  |  |  |  |
| 45  | 786906   | 272 | 898006   | 163 | 888900   | 435 | 111100    | 15   |  |  |  |  |  |  |  |
| 46  | 787069   | 272 | 897908   | 163 | 889161   | 435 | 110839    | 14   |  |  |  |  |  |  |  |
| 47  | 787232   | 271 | 897810   | 163 | 889421   | 435 | 110579    | 13   |  |  |  |  |  |  |  |
| 48  | 787395   | 271 | 897712   | 163 | 889682   | 435 | 110318    | 12   |  |  |  |  |  |  |  |
| 49  | 787557   | 271 | 897614   | 163 | 889943   | 435 | 110057    | 11   |  |  |  |  |  |  |  |
| 50  | 787720   | 271 | 897516   | 163 | 890204   | 434 | 109796    | 10   |  |  |  |  |  |  |  |
| 51  | 9.787883 | 271 | 9.897418 | 164 | 9.890465 | 434 | 10.109535 | 9    |  |  |  |  |  |  |  |
| 52  | 788045   | 271 | 897320   | 164 | 890725   | 434 | 109275    | 8    |  |  |  |  |  |  |  |
| 53  | 788208   | 271 | 897222   | 164 | 890986   | 434 | 109014    | 7    |  |  |  |  |  |  |  |
| 54  | 788370   | 270 | 897123   | 164 | 891247   | 434 | 108753    | 6    |  |  |  |  |  |  |  |
| 55  | 788532   | 270 | 897025   | 164 | 891507   | 434 | 108493    | 5    |  |  |  |  |  |  |  |
| 56  | 788694   | 270 | 896926   | 164 | 891768   | 434 | 108232    | 4    |  |  |  |  |  |  |  |
| 57  | 788856   | 270 | 896828   | 164 | 892028   | 434 | 107972    | 3    |  |  |  |  |  |  |  |
| 58  | 789018   | 270 | 896729   | 164 | 892289   | 434 | 107711    | 2    |  |  |  |  |  |  |  |
| 59  | 789180   | 270 | 896631   | 164 | 892549   | 434 | 107451    | 1    |  |  |  |  |  |  |  |
| 60  | 789342   | 269 | 896532   | 164 | 892810   | 434 | 107190    | 0    |  |  |  |  |  |  |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

127°

52°

88°

141°

| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.789342 | 269 | 9.896532 | 164 | 9.892810 | 434 | 10.107190 | 60 |
| 1  | 789504   | 269 | 896433   | 165 | 893070   | 434 | 106930    | 59 |
| 2  | 789665   | 269 | 896335   | 165 | 893331   | 434 | 106609    | 58 |
| 3  | 789827   | 269 | 896236   | 165 | 893591   | 434 | 106409    | 57 |
| 4  | 789988   | 269 | 896137   | 165 | 893851   | 434 | 106149    | 56 |
| 5  | 790149   | 269 | 896038   | 165 | 894111   | 434 | 105889    | 55 |
| 6  | 790310   | 268 | 895939   | 165 | 894372   | 434 | 105628    | 54 |
| 7  | 790471   | 268 | 895840   | 165 | 894632   | 433 | 105368    | 53 |
| 8  | 790632   | 268 | 895741   | 165 | 894892   | 433 | 105108    | 52 |
| 9  | 790793   | 268 | 895641   | 165 | 895152   | 433 | 104848    | 51 |
| 10 | 790954   | 268 | 895542   | 165 | 895412   | 433 | 104588    | 50 |
| 11 | 9.791115 | 268 | 9.895443 | 166 | 9.895672 | 433 | 10.104328 | 49 |
| 12 | 791275   | 267 | 895343   | 166 | 895932   | 433 | 104068    | 48 |
| 13 | 791436   | 267 | 895244   | 166 | 896192   | 433 | 103808    | 47 |
| 14 | 791596   | 267 | 895145   | 166 | 896452   | 433 | 103548    | 46 |
| 15 | 791757   | 267 | 895045   | 166 | 896712   | 433 | 103288    | 45 |
| 16 | 791917   | 267 | 894945   | 166 | 896971   | 433 | 103029    | 44 |
| 17 | 792077   | 267 | 894846   | 166 | 897231   | 433 | 102769    | 43 |
| 18 | 792237   | 266 | 894746   | 166 | 897491   | 433 | 102509    | 42 |
| 19 | 792397   | 266 | 894646   | 166 | 897751   | 433 | 102249    | 41 |
| 20 | 792557   | 266 | 894546   | 166 | 898010   | 433 | 101990    | 40 |
| 21 | 9.792716 | 266 | 9.894446 | 167 | 9.898270 | 433 | 10.101730 | 39 |
| 22 | 792876   | 266 | 894346   | 167 | 898530   | 433 | 101470    | 38 |
| 23 | 793035   | 266 | 894246   | 167 | 898789   | 433 | 101211    | 37 |
| 24 | 793195   | 265 | 894146   | 167 | 899049   | 432 | 100951    | 36 |
| 25 | 793354   | 265 | 894046   | 167 | 899308   | 432 | 100692    | 35 |
| 26 | 793514   | 265 | 893946   | 167 | 899568   | 432 | 100432    | 34 |
| 27 | 793673   | 265 | 893846   | 167 | 899827   | 432 | 100173    | 33 |
| 28 | 793832   | 265 | 893745   | 167 | 900087   | 432 | 999913    | 32 |
| 29 | 793991   | 265 | 893645   | 167 | 900346   | 432 | 999654    | 31 |
| 30 | 794150   | 264 | 893544   | 167 | 900605   | 432 | 999395    | 30 |
| 31 | 9.794308 | 264 | 9.893444 | 168 | 9.900864 | 432 | 10.999136 | 29 |
| 32 | 794467   | 264 | 893343   | 168 | 901124   | 432 | 998876    | 28 |
| 33 | 794626   | 264 | 893243   | 168 | 901383   | 432 | 998617    | 27 |
| 34 | 794784   | 264 | 893142   | 168 | 901642   | 432 | 998358    | 26 |
| 35 | 794942   | 264 | 893041   | 168 | 901901   | 432 | 998099    | 25 |
| 36 | 795101   | 264 | 892940   | 168 | 902160   | 432 | 997840    | 24 |
| 37 | 795259   | 263 | 892839   | 168 | 902420   | 432 | 997580    | 23 |
| 38 | 795417   | 263 | 892739   | 168 | 902679   | 432 | 997321    | 22 |
| 39 | 795575   | 263 | 892638   | 168 | 902938   | 432 | 997062    | 21 |
| 40 | 795733   | 263 | 892536   | 168 | 903197   | 431 | 996803    | 20 |
| 41 | 9.795891 | 263 | 9.892435 | 169 | 9.903456 | 431 | 10.996544 | 19 |
| 42 | 796049   | 263 | 892334   | 169 | 903714   | 431 | 996286    | 18 |
| 43 | 796206   | 263 | 892233   | 169 | 903973   | 431 | 996027    | 17 |
| 44 | 796364   | 262 | 892132   | 169 | 904232   | 431 | 995768    | 16 |
| 45 | 796521   | 262 | 892030   | 169 | 904491   | 431 | 995509    | 15 |
| 46 | 796679   | 262 | 891929   | 169 | 904750   | 431 | 995250    | 14 |
| 47 | 796836   | 262 | 891827   | 169 | 905008   | 431 | 994992    | 13 |
| 48 | 796993   | 262 | 891726   | 169 | 905267   | 431 | 994733    | 12 |
| 49 | 797150   | 261 | 891624   | 169 | 905526   | 431 | 994474    | 11 |
| 50 | 797307   | 261 | 891523   | 170 | 905785   | 431 | 994215    | 10 |
| 51 | 9.797464 | 261 | 9.891421 | 170 | 9.906043 | 431 | 10.993957 | 9  |
| 52 | 797621   | 261 | 891319   | 170 | 906302   | 431 | 993698    | 8  |
| 53 | 797777   | 261 | 891217   | 170 | 906560   | 431 | 993440    | 7  |
| 54 | 797934   | 261 | 891115   | 170 | 906819   | 431 | 993181    | 6  |
| 55 | 798091   | 261 | 891013   | 170 | 907077   | 431 | 992923    | 5  |
| 56 | 798247   | 261 | 890911   | 170 | 907336   | 431 | 992664    | 4  |
| 57 | 798403   | 260 | 890809   | 170 | 907594   | 431 | 992406    | 3  |
| 58 | 798560   | 260 | 890707   | 170 | 907853   | 431 | 992147    | 2  |
| 59 | 798716   | 260 | 890605   | 170 | 908111   | 430 | 991889    | 1  |
| 60 | 798872   | 260 | 890503   | 170 | 908369   | 430 | 991631    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

128°

61°



TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

87

89°

140°

| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.798872 | 260 | 9.890503 | 170 | 9.908369 | 430 | 10.091631 | 60 |
| 1  | 799028   | 260 | 890400   | 171 | 908628   | 430 | 091372    | 59 |
| 2  | 799184   | 260 | 890298   | 171 | 908886   | 430 | 091114    | 58 |
| 3  | 799339   | 259 | 890195   | 171 | 909144   | 430 | 090856    | 57 |
| 4  | 799495   | 259 | 890093   | 171 | 909402   | 430 | 090598    | 56 |
| 5  | 799651   | 259 | 889990   | 171 | 909660   | 430 | 090340    | 55 |
| 6  | 799806   | 259 | 889888   | 171 | 909918   | 430 | 090082    | 54 |
| 7  | 799962   | 259 | 889785   | 171 | 910177   | 430 | 089823    | 53 |
| 8  | 800117   | 259 | 889682   | 171 | 910435   | 430 | 089565    | 52 |
| 9  | 800272   | 258 | 889579   | 171 | 910693   | 430 | 089307    | 51 |
| 10 | 800427   | 258 | 889477   | 171 | 910951   | 430 | 089049    | 50 |
| 11 | 9.800582 | 258 | 9.889374 | 172 | 9.911209 | 430 | 10.088791 | 49 |
| 12 | 800737   | 258 | 889271   | 172 | 911467   | 430 | 088533    | 48 |
| 13 | 800892   | 258 | 889168   | 172 | 911725   | 430 | 088275    | 47 |
| 14 | 801047   | 258 | 889064   | 172 | 911982   | 430 | 088018    | 46 |
| 15 | 801201   | 258 | 888961   | 172 | 912240   | 430 | 087760    | 45 |
| 16 | 801356   | 257 | 888858   | 172 | 912498   | 430 | 087502    | 44 |
| 17 | 801511   | 257 | 888755   | 172 | 912756   | 430 | 087244    | 43 |
| 18 | 801665   | 257 | 888651   | 172 | 913014   | 429 | 086986    | 42 |
| 19 | 801819   | 257 | 888548   | 172 | 913271   | 429 | 086729    | 41 |
| 20 | 801973   | 257 | 888444   | 173 | 913529   | 429 | 086471    | 40 |
| 21 | 9.802128 | 257 | 9.888341 | 173 | 9.913787 | 429 | 10.086213 | 39 |
| 22 | 802282   | 256 | 888237   | 173 | 914044   | 429 | 085956    | 38 |
| 23 | 802436   | 256 | 888134   | 173 | 914302   | 429 | 085698    | 37 |
| 24 | 802589   | 256 | 888030   | 173 | 914560   | 429 | 085440    | 36 |
| 25 | 802743   | 256 | 887926   | 173 | 914817   | 429 | 085183    | 35 |
| 26 | 802897   | 256 | 887822   | 173 | 915075   | 429 | 084925    | 34 |
| 27 | 803050   | 256 | 887718   | 173 | 915332   | 429 | 084668    | 33 |
| 28 | 803204   | 256 | 887614   | 173 | 915590   | 429 | 084410    | 32 |
| 29 | 803357   | 255 | 887510   | 173 | 915847   | 429 | 084153    | 31 |
| 30 | 803511   | 255 | 887406   | 174 | 916104   | 429 | 083896    | 30 |
| 31 | 9.803664 | 255 | 9.887302 | 174 | 9.916362 | 429 | 10.083638 | 29 |
| 32 | 803817   | 255 | 887198   | 174 | 916619   | 429 | 083381    | 28 |
| 33 | 803970   | 255 | 887093   | 174 | 916877   | 429 | 083123    | 27 |
| 34 | 804123   | 255 | 886989   | 174 | 917134   | 429 | 082866    | 26 |
| 35 | 804276   | 254 | 886885   | 174 | 917391   | 429 | 082609    | 25 |
| 36 | 804428   | 254 | 886780   | 174 | 917648   | 429 | 082352    | 24 |
| 37 | 804581   | 254 | 886676   | 174 | 917906   | 429 | 082094    | 23 |
| 38 | 804734   | 254 | 886571   | 174 | 918163   | 428 | 081837    | 22 |
| 39 | 804886   | 254 | 886466   | 174 | 918420   | 428 | 081580    | 21 |
| 40 | 805039   | 254 | 886362   | 175 | 918677   | 428 | 081323    | 20 |
| 41 | 9.805191 | 254 | 9.886257 | 175 | 9.918934 | 428 | 10.081066 | 19 |
| 42 | 805343   | 253 | 886152   | 175 | 919191   | 428 | 080809    | 18 |
| 43 | 805495   | 253 | 886047   | 175 | 919448   | 428 | 080552    | 17 |
| 44 | 805647   | 253 | 885942   | 175 | 919705   | 428 | 080295    | 16 |
| 45 | 805799   | 253 | 885837   | 175 | 919962   | 428 | 080038    | 15 |
| 46 | 805951   | 253 | 885732   | 175 | 920219   | 428 | 079781    | 14 |
| 47 | 806103   | 253 | 885627   | 175 | 920476   | 428 | 079524    | 13 |
| 48 | 806254   | 253 | 885522   | 175 | 920733   | 428 | 079267    | 12 |
| 49 | 806406   | 252 | 885416   | 175 | 920990   | 428 | 079010    | 11 |
| 50 | 806557   | 252 | 885311   | 176 | 921247   | 428 | 078753    | 10 |
| 51 | 9.806709 | 252 | 9.885205 | 176 | 9.921503 | 428 | 10.078497 | 9  |
| 52 | 806860   | 252 | 885100   | 176 | 921760   | 428 | 078240    | 8  |
| 53 | 807011   | 252 | 884994   | 176 | 922017   | 428 | 077983    | 7  |
| 54 | 807163   | 252 | 884889   | 176 | 922274   | 428 | 077726    | 6  |
| 55 | 807314   | 252 | 884783   | 176 | 922530   | 428 | 077470    | 5  |
| 56 | 807465   | 251 | 884677   | 176 | 922787   | 428 | 077213    | 4  |
| 57 | 807615   | 251 | 884572   | 176 | 923044   | 428 | 076956    | 3  |
| 58 | 807766   | 251 | 884466   | 176 | 923300   | 428 | 076700    | 2  |
| 59 | 807917   | 251 | 884360   | 176 | 923557   | 427 | 076443    | 1  |
| 60 | 808067   | 251 | 884254   | 177 | 923814   | 427 | 076186    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

129°

50°

88°

141°

| /  | Sz.      | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.789342 | 269 | 9.896532 | 164 | 9.892810 | 434 | 10.107190 | 60 |
| 1  | 789504   | 269 | 896433   | 165 | 893070   | 434 | 100930    | 59 |
| 2  | 789665   | 269 | 896335   | 165 | 893331   | 434 | 106669    | 58 |
| 3  | 789827   | 269 | 896236   | 165 | 893591   | 434 | 106409    | 57 |
| 4  | 789988   | 269 | 896137   | 165 | 893851   | 434 | 106149    | 56 |
| 5  | 790149   | 269 | 896038   | 165 | 894111   | 434 | 105889    | 55 |
| 6  | 790310   | 268 | 895939   | 165 | 894372   | 434 | 105628    | 54 |
| 7  | 790471   | 268 | 895840   | 165 | 894632   | 433 | 105368    | 53 |
| 8  | 790632   | 268 | 895741   | 165 | 894892   | 433 | 105108    | 52 |
| 9  | 790793   | 268 | 895641   | 165 | 895152   | 433 | 104848    | 51 |
| 10 | 790954   | 268 | 895542   | 165 | 895412   | 433 | 104588    | 50 |
| 11 | 9.791115 | 268 | 9.895443 | 166 | 9.895672 | 433 | 10.104328 | 49 |
| 12 | 791275   | 267 | 895343   | 166 | 895932   | 433 | 104068    | 48 |
| 13 | 791436   | 267 | 895244   | 166 | 896192   | 433 | 103808    | 47 |
| 14 | 791596   | 267 | 895145   | 166 | 896452   | 433 | 103548    | 46 |
| 15 | 791757   | 267 | 895045   | 166 | 896712   | 433 | 103288    | 45 |
| 16 | 791917   | 267 | 894945   | 166 | 896971   | 433 | 103029    | 44 |
| 17 | 792077   | 267 | 894846   | 166 | 897231   | 433 | 102769    | 43 |
| 18 | 792237   | 266 | 894746   | 166 | 897491   | 433 | 102509    | 42 |
| 19 | 792397   | 266 | 894646   | 166 | 897751   | 433 | 102249    | 41 |
| 20 | 792557   | 266 | 894546   | 166 | 898010   | 433 | 101990    | 40 |
| 21 | 9.792716 | 266 | 9.894446 | 167 | 9.898270 | 433 | 10.101730 | 39 |
| 22 | 792876   | 266 | 894346   | 167 | 898530   | 433 | 101470    | 38 |
| 23 | 793035   | 266 | 894246   | 167 | 898789   | 433 | 101211    | 37 |
| 24 | 793195   | 265 | 894146   | 167 | 899049   | 432 | 100951    | 36 |
| 25 | 793354   | 265 | 894046   | 167 | 899308   | 432 | 100692    | 35 |
| 26 | 793514   | 265 | 893946   | 167 | 899568   | 432 | 100432    | 34 |
| 27 | 793673   | 265 | 893846   | 167 | 899827   | 432 | 100173    | 33 |
| 28 | 793832   | 265 | 893745   | 167 | 900087   | 432 | 999913    | 32 |
| 29 | 793991   | 265 | 893645   | 167 | 900346   | 432 | 999654    | 31 |
| 30 | 794150   | 264 | 893544   | 167 | 900605   | 432 | 999395    | 30 |
| 31 | 9.794308 | 264 | 9.893444 | 168 | 9.900864 | 432 | 10.999136 | 29 |
| 32 | 794467   | 264 | 893343   | 168 | 901124   | 432 | 998876    | 28 |
| 33 | 794626   | 264 | 893243   | 168 | 901383   | 432 | 998617    | 27 |
| 34 | 794784   | 264 | 893142   | 168 | 901642   | 432 | 998358    | 26 |
| 35 | 794942   | 264 | 893041   | 168 | 901901   | 432 | 998099    | 25 |
| 36 | 795101   | 264 | 892940   | 168 | 902160   | 432 | 997840    | 24 |
| 37 | 795259   | 263 | 892839   | 168 | 902420   | 432 | 997580    | 23 |
| 38 | 795417   | 263 | 892739   | 168 | 902679   | 432 | 997321    | 22 |
| 39 | 795575   | 263 | 892638   | 168 | 902938   | 432 | 997062    | 21 |
| 40 | 795733   | 263 | 892536   | 168 | 903197   | 431 | 996803    | 20 |
| 41 | 9.795891 | 263 | 9.892435 | 169 | 9.903456 | 431 | 10.996544 | 19 |
| 42 | 796049   | 263 | 892334   | 169 | 903714   | 431 | 996286    | 18 |
| 43 | 796206   | 263 | 892233   | 169 | 903973   | 431 | 996027    | 17 |
| 44 | 796364   | 262 | 892132   | 169 | 904232   | 431 | 995768    | 16 |
| 45 | 796521   | 262 | 892030   | 169 | 904491   | 431 | 995509    | 15 |
| 46 | 796679   | 262 | 891929   | 169 | 904750   | 431 | 995250    | 14 |
| 47 | 796836   | 262 | 891827   | 169 | 905008   | 431 | 994992    | 13 |
| 48 | 796993   | 262 | 891726   | 169 | 905267   | 431 | 994733    | 12 |
| 49 | 797150   | 261 | 891624   | 169 | 905526   | 431 | 994474    | 11 |
| 50 | 797307   | 261 | 891523   | 170 | 905785   | 431 | 994215    | 10 |
| 51 | 9.797464 | 261 | 9.891421 | 170 | 9.906043 | 431 | 10.993957 | 9  |
| 52 | 797621   | 261 | 891319   | 170 | 906302   | 431 | 993698    | 8  |
| 53 | 797777   | 261 | 891217   | 170 | 906560   | 431 | 993440    | 7  |
| 54 | 797934   | 261 | 891115   | 170 | 906819   | 431 | 993181    | 6  |
| 55 | 798091   | 261 | 891013   | 170 | 907077   | 431 | 992923    | 5  |
| 56 | 798247   | 261 | 890911   | 170 | 907336   | 431 | 992664    | 4  |
| 57 | 798403   | 260 | 890809   | 170 | 907594   | 431 | 992406    | 3  |
| 58 | 798560   | 260 | 890707   | 170 | 907853   | 431 | 992147    | 2  |
| 59 | 798716   | 260 | 890605   | 170 | 908111   | 430 | 991889    | 1  |
| 60 | 798872   | 260 | 890503   | 170 | 908369   | 430 | 991631    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 89° |          |     |          |     |          |     | 140°      |    |
|-----|----------|-----|----------|-----|----------|-----|-----------|----|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
| 0   | 9.798872 | 260 | 9.890503 | 170 | 9.908369 | 430 | 10.091631 | 60 |
| 1   | 799028   | 260 | 890400   | 171 | 908628   | 430 | 091372    | 59 |
| 2   | 799184   | 260 | 890298   | 171 | 908886   | 430 | 091114    | 58 |
| 3   | 799339   | 259 | 890195   | 171 | 909144   | 430 | 090856    | 57 |
| 4   | 799495   | 259 | 890093   | 171 | 909402   | 430 | 090598    | 56 |
| 5   | 799651   | 259 | 889990   | 171 | 909660   | 430 | 090340    | 55 |
| 6   | 799806   | 259 | 889888   | 171 | 909918   | 430 | 090082    | 54 |
| 7   | 799962   | 259 | 889785   | 171 | 910177   | 430 | 089823    | 53 |
| 8   | 800117   | 259 | 889682   | 171 | 910435   | 430 | 089565    | 52 |
| 9   | 800272   | 258 | 889579   | 171 | 910693   | 430 | 089307    | 51 |
| 10  | 800427   | 258 | 889477   | 171 | 910951   | 430 | 089049    | 50 |
| 11  | 9.800582 | 258 | 9.889374 | 172 | 9.911209 | 430 | 10.088791 | 49 |
| 12  | 800737   | 258 | 889271   | 172 | 911467   | 430 | 088533    | 48 |
| 13  | 800892   | 258 | 889168   | 172 | 911725   | 430 | 088275    | 47 |
| 14  | 801047   | 258 | 889064   | 172 | 911982   | 430 | 088018    | 46 |
| 15  | 801201   | 258 | 888961   | 172 | 912240   | 430 | 087760    | 45 |
| 16  | 801356   | 257 | 888858   | 172 | 912498   | 430 | 087502    | 44 |
| 17  | 801511   | 257 | 888755   | 172 | 912756   | 430 | 087244    | 43 |
| 18  | 801665   | 257 | 888651   | 172 | 913014   | 429 | 086986    | 42 |
| 19  | 801819   | 257 | 888548   | 172 | 913271   | 429 | 086729    | 41 |
| 20  | 801973   | 257 | 888444   | 173 | 913529   | 429 | 086471    | 40 |
| 21  | 9.802128 | 257 | 9.888341 | 173 | 9.913787 | 429 | 10.086213 | 39 |
| 22  | 802282   | 256 | 888237   | 173 | 914044   | 429 | 085956    | 38 |
| 23  | 802436   | 256 | 888134   | 173 | 914302   | 429 | 085698    | 37 |
| 24  | 802589   | 256 | 888030   | 173 | 914560   | 429 | 085440    | 36 |
| 25  | 802743   | 256 | 887926   | 173 | 914817   | 429 | 085183    | 35 |
| 26  | 802897   | 256 | 887822   | 173 | 915075   | 429 | 084925    | 34 |
| 27  | 803050   | 256 | 887718   | 173 | 915332   | 429 | 084668    | 33 |
| 28  | 803204   | 256 | 887614   | 173 | 915590   | 429 | 084410    | 32 |
| 29  | 803357   | 255 | 887510   | 173 | 915847   | 429 | 084153    | 31 |
| 30  | 803511   | 255 | 887406   | 174 | 916104   | 429 | 083896    | 30 |
| 31  | 9.803664 | 255 | 9.887302 | 174 | 9.916362 | 429 | 10.083638 | 29 |
| 32  | 803817   | 255 | 887198   | 174 | 916619   | 429 | 083381    | 28 |
| 33  | 803970   | 255 | 887093   | 174 | 916877   | 429 | 083123    | 27 |
| 34  | 804123   | 255 | 886989   | 174 | 917134   | 429 | 082866    | 26 |
| 35  | 804276   | 254 | 886885   | 174 | 917391   | 429 | 082609    | 25 |
| 36  | 804428   | 254 | 886780   | 174 | 917648   | 429 | 082352    | 24 |
| 37  | 804581   | 254 | 886676   | 174 | 917906   | 429 | 082094    | 23 |
| 38  | 804734   | 254 | 886571   | 174 | 918163   | 428 | 081837    | 22 |
| 39  | 804886   | 254 | 886466   | 174 | 918420   | 428 | 081580    | 21 |
| 40  | 805039   | 254 | 886362   | 175 | 918677   | 428 | 081323    | 20 |
| 41  | 9.805191 | 254 | 9.886257 | 175 | 9.918934 | 428 | 10.081066 | 19 |
| 42  | 805343   | 253 | 886152   | 175 | 919191   | 428 | 080809    | 18 |
| 43  | 805495   | 253 | 886047   | 175 | 919448   | 428 | 080552    | 17 |
| 44  | 805647   | 253 | 885942   | 175 | 919705   | 428 | 080295    | 16 |
| 45  | 805799   | 253 | 885837   | 175 | 919962   | 428 | 080038    | 15 |
| 46  | 805951   | 253 | 885732   | 175 | 920219   | 428 | 079781    | 14 |
| 47  | 806103   | 253 | 885627   | 175 | 920476   | 428 | 079524    | 13 |
| 48  | 806254   | 253 | 885522   | 175 | 920733   | 428 | 079267    | 12 |
| 49  | 806406   | 252 | 885416   | 175 | 920990   | 428 | 079010    | 11 |
| 50  | 806557   | 252 | 885311   | 176 | 921247   | 428 | 078753    | 10 |
| 51  | 9.806709 | 252 | 9.885205 | 176 | 9.921503 | 428 | 10.078497 | 9  |
| 52  | 806860   | 252 | 885100   | 176 | 921760   | 428 | 078240    | 8  |
| 53  | 807011   | 252 | 884994   | 176 | 922017   | 428 | 077983    | 7  |
| 54  | 807163   | 252 | 884889   | 176 | 922274   | 428 | 077726    | 6  |
| 55  | 807314   | 252 | 884783   | 176 | 922530   | 428 | 077470    | 5  |
| 56  | 807465   | 251 | 884677   | 176 | 922787   | 428 | 077213    | 4  |
| 57  | 807615   | 251 | 884572   | 176 | 923044   | 428 | 076956    | 3  |
| 58  | 807766   | 251 | 884466   | 176 | 923300   | 428 | 076700    | 2  |
| 59  | 807917   | 251 | 884360   | 176 | 923557   | 427 | 076443    | 1  |
| 60  | 808067   | 251 | 884254   | 177 | 923814   | 427 | 076186    | 0  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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|    | Base.    | D.   | Contn.   | D.  | Tang.    | D.  | Contn.   |    |
|----|----------|------|----------|-----|----------|-----|----------|----|
| 0  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 10.07356 | 60 |
| 1  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 59 |
| 2  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 58 |
| 3  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 57 |
| 4  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 56 |
| 5  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 55 |
| 6  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 54 |
| 7  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 53 |
| 8  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 52 |
| 9  | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 51 |
| 10 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 50 |
| 11 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 10.07356 | 49 |
| 12 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 48 |
| 13 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 47 |
| 14 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 46 |
| 15 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 45 |
| 16 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 44 |
| 17 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 43 |
| 18 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 42 |
| 19 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 41 |
| 20 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 40 |
| 21 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 10.07356 | 39 |
| 22 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 38 |
| 23 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 427 | 07.356   | 37 |
| 24 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 36 |
| 25 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 35 |
| 26 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 34 |
| 27 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 33 |
| 28 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 32 |
| 29 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 31 |
| 30 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 30 |
| 31 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 10.07356 | 29 |
| 32 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 28 |
| 33 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 27 |
| 34 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 26 |
| 35 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 25 |
| 36 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 24 |
| 37 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 23 |
| 38 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 22 |
| 39 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 21 |
| 40 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 20 |
| 41 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 10.07356 | 19 |
| 42 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 18 |
| 43 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 17 |
| 44 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 16 |
| 45 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 15 |
| 46 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 14 |
| 47 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 13 |
| 48 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 12 |
| 49 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 11 |
| 50 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 426 | 07.356   | 10 |
| 51 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 10.07356 | 9  |
| 52 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 8  |
| 53 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 7  |
| 54 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 6  |
| 55 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 5  |
| 56 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 4  |
| 57 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 3  |
| 58 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 2  |
| 59 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 1  |
| 60 | 9.246000 | 24.1 | 9.246000 | 179 | 9.246000 | 425 | 07.356   | 0  |
|    | Contn.   | D.   | Contn.   | D.  | Contn.   | D.  | Tang.    |    |



| LOGARITHMIC SINES, TANGENTS, ETC. TABLE II. |          |     |          |     |          |     |           |    |  |
|---------------------------------------------|----------|-----|----------|-----|----------|-----|-----------|----|--|
| 32°                                         |          |     |          |     | 147°     |     |           |    |  |
| /                                           | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |  |
| 0                                           | 9.724210 | 337 | 9.928420 | 132 | 9.795789 | 468 | 10.204211 | 60 |  |
| 1                                           | 724412   | 337 | 928342   | 132 | 796070   | 468 | 203930    | 59 |  |
| 2                                           | 724614   | 336 | 928263   | 132 | 796351   | 468 | 203649    | 58 |  |
| 3                                           | 724816   | 336 | 928183   | 132 | 796632   | 468 | 203368    | 57 |  |
| 4                                           | 725017   | 336 | 928104   | 132 | 796913   | 468 | 203087    | 56 |  |
| 5                                           | 725219   | 336 | 928025   | 132 | 797194   | 468 | 202806    | 55 |  |
| 6                                           | 725420   | 335 | 927946   | 132 | 797474   | 468 | 202526    | 54 |  |
| 7                                           | 725622   | 335 | 927867   | 132 | 797755   | 468 | 202245    | 53 |  |
| 8                                           | 725823   | 335 | 927787   | 132 | 798036   | 467 | 201964    | 52 |  |
| 9                                           | 726024   | 335 | 927708   | 132 | 798316   | 467 | 201684    | 51 |  |
| 10                                          | 726225   | 335 | 927629   | 132 | 798596   | 467 | 201404    | 50 |  |
| 11                                          | 9.726426 | 334 | 9.927549 | 132 | 9.798877 | 467 | 10.201123 | 49 |  |
| 12                                          | 726626   | 334 | 927470   | 133 | 799157   | 467 | 200843    | 48 |  |
| 13                                          | 726827   | 334 | 927390   | 133 | 799437   | 467 | 200563    | 47 |  |
| 14                                          | 727027   | 334 | 927310   | 133 | 799717   | 467 | 200283    | 46 |  |
| 15                                          | 727228   | 334 | 927231   | 133 | 799997   | 466 | 200003    | 45 |  |
| 16                                          | 727428   | 333 | 927151   | 133 | 800277   | 466 | 199723    | 44 |  |
| 17                                          | 727628   | 333 | 927071   | 133 | 800557   | 466 | 199443    | 43 |  |
| 18                                          | 727828   | 333 | 926991   | 133 | 800836   | 466 | 199164    | 42 |  |
| 19                                          | 728027   | 333 | 926911   | 133 | 801116   | 466 | 198884    | 41 |  |
| 20                                          | 728227   | 333 | 926831   | 133 | 801396   | 466 | 198604    | 40 |  |
| 21                                          | 9.728427 | 332 | 9.926751 | 133 | 9.801675 | 466 | 10.198325 | 39 |  |
| 22                                          | 728626   | 332 | 926671   | 133 | 801955   | 466 | 198045    | 38 |  |
| 23                                          | 728825   | 332 | 926591   | 133 | 802234   | 465 | 197766    | 37 |  |
| 24                                          | 729024   | 332 | 926511   | 134 | 802513   | 465 | 197487    | 36 |  |
| 25                                          | 729223   | 331 | 926431   | 134 | 802792   | 465 | 197208    | 35 |  |
| 26                                          | 729422   | 331 | 926351   | 134 | 803072   | 465 | 196928    | 34 |  |
| 27                                          | 729621   | 331 | 926270   | 134 | 803351   | 465 | 196649    | 33 |  |
| 28                                          | 729820   | 331 | 926190   | 134 | 803630   | 465 | 196370    | 32 |  |
| 29                                          | 730018   | 330 | 926110   | 134 | 803909   | 465 | 196091    | 31 |  |
| 30                                          | 730217   | 330 | 926029   | 134 | 804187   | 465 | 195813    | 30 |  |
| 31                                          | 9.730415 | 330 | 9.925949 | 134 | 9.804466 | 464 | 10.195534 | 29 |  |
| 32                                          | 730613   | 330 | 925868   | 134 | 804745   | 464 | 195255    | 28 |  |
| 33                                          | 730811   | 330 | 925788   | 134 | 805023   | 464 | 194977    | 27 |  |
| 34                                          | 731009   | 329 | 925707   | 134 | 805302   | 464 | 194698    | 26 |  |
| 35                                          | 731206   | 329 | 925626   | 134 | 805580   | 464 | 194420    | 25 |  |
| 36                                          | 731404   | 329 | 925545   | 135 | 805859   | 464 | 194141    | 24 |  |
| 37                                          | 731602   | 329 | 925465   | 135 | 806137   | 464 | 193863    | 23 |  |
| 38                                          | 731799   | 329 | 925384   | 135 | 806415   | 463 | 193585    | 22 |  |
| 39                                          | 731996   | 328 | 925303   | 135 | 806693   | 463 | 193307    | 21 |  |
| 40                                          | 732193   | 328 | 925222   | 135 | 806971   | 463 | 193029    | 20 |  |
| 41                                          | 9.732390 | 328 | 9.925141 | 135 | 9.807249 | 463 | 10.192751 | 19 |  |
| 42                                          | 732587   | 328 | 925060   | 135 | 807527   | 463 | 192473    | 18 |  |
| 43                                          | 732784   | 328 | 924979   | 135 | 807805   | 463 | 192195    | 17 |  |
| 44                                          | 732980   | 327 | 924897   | 135 | 808083   | 463 | 191917    | 16 |  |
| 45                                          | 733177   | 327 | 924816   | 135 | 808361   | 463 | 191639    | 15 |  |
| 46                                          | 733373   | 327 | 924735   | 136 | 808638   | 462 | 191362    | 14 |  |
| 47                                          | 733569   | 327 | 924654   | 136 | 808916   | 462 | 191084    | 13 |  |
| 48                                          | 733765   | 327 | 924572   | 136 | 809193   | 462 | 190807    | 12 |  |
| 49                                          | 733961   | 326 | 924491   | 136 | 809471   | 462 | 190529    | 11 |  |
| 50                                          | 734157   | 326 | 924409   | 136 | 809748   | 462 | 190252    | 10 |  |
| 51                                          | 9.734353 | 326 | 9.924328 | 136 | 9.810025 | 462 | 10.189975 | 9  |  |
| 52                                          | 734549   | 326 | 924246   | 136 | 810302   | 462 | 189698    | 8  |  |
| 53                                          | 734744   | 325 | 924164   | 136 | 810580   | 462 | 189420    | 7  |  |
| 54                                          | 734939   | 325 | 924083   | 136 | 810857   | 462 | 189143    | 6  |  |
| 55                                          | 735135   | 325 | 924001   | 136 | 811134   | 461 | 188866    | 5  |  |
| 56                                          | 735330   | 325 | 923919   | 136 | 811410   | 461 | 188590    | 4  |  |
| 57                                          | 735525   | 325 | 923837   | 136 | 811687   | 461 | 188313    | 3  |  |
| 58                                          | 735719   | 324 | 923755   | 137 | 811964   | 461 | 188036    | 2  |  |
| 59                                          | 735914   | 324 | 923673   | 137 | 812241   | 461 | 187759    | 1  |  |
| 60                                          | 736109   | 324 | 923591   | 137 | 812517   | 461 | 187483    | 0  |  |
| /                                           | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |  |
| 133°                                        |          |     |          |     | 57°      |     |           |    |  |

TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 38° |          |     |          |     |          |     |           | 146° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9.736109 | 324 | 9.923591 | 137 | 9.812517 | 461 | 10.187483 | 60   |  |  |  |  |  |  |  |
| 1   | 736303   | 324 | 923509   | 137 | 812794   | 461 | 187206    | 59   |  |  |  |  |  |  |  |
| 2   | 736498   | 324 | 923427   | 137 | 813070   | 461 | 186930    | 58   |  |  |  |  |  |  |  |
| 3   | 736692   | 323 | 923345   | 137 | 813347   | 460 | 186653    | 57   |  |  |  |  |  |  |  |
| 4   | 736886   | 323 | 923263   | 137 | 813623   | 460 | 186377    | 56   |  |  |  |  |  |  |  |
| 5   | 737080   | 323 | 923181   | 137 | 813899   | 460 | 186101    | 55   |  |  |  |  |  |  |  |
| 6   | 737274   | 323 | 923098   | 137 | 814176   | 460 | 185824    | 54   |  |  |  |  |  |  |  |
| 7   | 737467   | 323 | 923016   | 137 | 814452   | 460 | 185548    | 53   |  |  |  |  |  |  |  |
| 8   | 737661   | 322 | 922933   | 137 | 814728   | 460 | 185272    | 52   |  |  |  |  |  |  |  |
| 9   | 737855   | 322 | 922851   | 137 | 815004   | 460 | 184996    | 51   |  |  |  |  |  |  |  |
| 10  | 738048   | 322 | 922768   | 138 | 815280   | 460 | 184720    | 50   |  |  |  |  |  |  |  |
| 11  | 9.738241 | 322 | 9.922686 | 138 | 9.815555 | 459 | 10.184445 | 49   |  |  |  |  |  |  |  |
| 12  | 738434   | 322 | 922603   | 138 | 815831   | 459 | 184169    | 48   |  |  |  |  |  |  |  |
| 13  | 738627   | 321 | 922520   | 138 | 816107   | 459 | 183893    | 47   |  |  |  |  |  |  |  |
| 14  | 738820   | 321 | 922438   | 138 | 816382   | 459 | 183618    | 46   |  |  |  |  |  |  |  |
| 15  | 739013   | 321 | 922355   | 138 | 816658   | 459 | 183342    | 45   |  |  |  |  |  |  |  |
| 16  | 739206   | 321 | 922272   | 138 | 816933   | 459 | 183067    | 44   |  |  |  |  |  |  |  |
| 17  | 739398   | 321 | 922189   | 138 | 817209   | 459 | 182791    | 43   |  |  |  |  |  |  |  |
| 18  | 739590   | 320 | 922106   | 138 | 817484   | 459 | 182516    | 42   |  |  |  |  |  |  |  |
| 19  | 739783   | 320 | 922023   | 138 | 817759   | 459 | 182241    | 41   |  |  |  |  |  |  |  |
| 20  | 739975   | 320 | 921940   | 138 | 818035   | 458 | 181965    | 40   |  |  |  |  |  |  |  |
| 21  | 9.740167 | 320 | 9.921857 | 139 | 9.818310 | 458 | 10.181690 | 39   |  |  |  |  |  |  |  |
| 22  | 740359   | 320 | 921774   | 139 | 818585   | 458 | 181415    | 38   |  |  |  |  |  |  |  |
| 23  | 740550   | 319 | 921691   | 139 | 818860   | 458 | 181140    | 37   |  |  |  |  |  |  |  |
| 24  | 740742   | 319 | 921607   | 139 | 819135   | 458 | 180865    | 36   |  |  |  |  |  |  |  |
| 25  | 740934   | 319 | 921524   | 139 | 819410   | 458 | 180590    | 35   |  |  |  |  |  |  |  |
| 26  | 741125   | 319 | 921441   | 139 | 819684   | 458 | 180316    | 34   |  |  |  |  |  |  |  |
| 27  | 741316   | 319 | 921357   | 139 | 819959   | 458 | 180041    | 33   |  |  |  |  |  |  |  |
| 28  | 741508   | 318 | 921274   | 139 | 820234   | 458 | 179766    | 32   |  |  |  |  |  |  |  |
| 29  | 741699   | 318 | 921190   | 139 | 820508   | 457 | 179492    | 31   |  |  |  |  |  |  |  |
| 30  | 741889   | 318 | 921107   | 139 | 820783   | 457 | 179217    | 30   |  |  |  |  |  |  |  |
| 31  | 9.742080 | 318 | 9.921023 | 139 | 9.821057 | 457 | 10.178943 | 29   |  |  |  |  |  |  |  |
| 32  | 742271   | 318 | 920939   | 140 | 821332   | 457 | 178668    | 28   |  |  |  |  |  |  |  |
| 33  | 742462   | 317 | 920856   | 140 | 821606   | 457 | 178394    | 27   |  |  |  |  |  |  |  |
| 34  | 742652   | 317 | 920772   | 140 | 821880   | 457 | 178120    | 26   |  |  |  |  |  |  |  |
| 35  | 742842   | 317 | 920688   | 140 | 822154   | 457 | 177846    | 25   |  |  |  |  |  |  |  |
| 36  | 743033   | 317 | 920604   | 140 | 822429   | 457 | 177571    | 24   |  |  |  |  |  |  |  |
| 37  | 743223   | 317 | 920520   | 140 | 822703   | 457 | 177297    | 23   |  |  |  |  |  |  |  |
| 38  | 743413   | 316 | 920436   | 140 | 822977   | 456 | 177023    | 22   |  |  |  |  |  |  |  |
| 39  | 743602   | 316 | 920352   | 140 | 823251   | 456 | 176749    | 21   |  |  |  |  |  |  |  |
| 40  | 743792   | 316 | 920268   | 140 | 823524   | 456 | 176476    | 20   |  |  |  |  |  |  |  |
| 41  | 9.743982 | 316 | 9.920184 | 140 | 9.823798 | 456 | 10.176202 | 19   |  |  |  |  |  |  |  |
| 42  | 744171   | 316 | 920099   | 140 | 824072   | 456 | 175928    | 18   |  |  |  |  |  |  |  |
| 43  | 744361   | 315 | 920015   | 140 | 824345   | 456 | 175655    | 17   |  |  |  |  |  |  |  |
| 44  | 744550   | 315 | 919931   | 141 | 824619   | 456 | 175381    | 16   |  |  |  |  |  |  |  |
| 45  | 744739   | 315 | 919846   | 141 | 824893   | 456 | 175107    | 15   |  |  |  |  |  |  |  |
| 46  | 744928   | 315 | 919762   | 141 | 825166   | 456 | 174834    | 14   |  |  |  |  |  |  |  |
| 47  | 745117   | 315 | 919677   | 141 | 825439   | 455 | 174561    | 13   |  |  |  |  |  |  |  |
| 48  | 745306   | 314 | 919593   | 141 | 825713   | 455 | 174287    | 12   |  |  |  |  |  |  |  |
| 49  | 745494   | 314 | 919508   | 141 | 825986   | 455 | 174014    | 11   |  |  |  |  |  |  |  |
| 50  | 745683   | 314 | 919424   | 141 | 826259   | 455 | 173741    | 10   |  |  |  |  |  |  |  |
| 51  | 9.745871 | 314 | 9.919339 | 141 | 9.826532 | 455 | 10.173468 | 9    |  |  |  |  |  |  |  |
| 52  | 746060   | 314 | 919254   | 141 | 826805   | 455 | 173195    | 8    |  |  |  |  |  |  |  |
| 53  | 746248   | 313 | 919169   | 141 | 827078   | 455 | 172922    | 7    |  |  |  |  |  |  |  |
| 54  | 746436   | 313 | 919085   | 141 | 827351   | 455 | 172649    | 6    |  |  |  |  |  |  |  |
| 55  | 746624   | 313 | 919000   | 141 | 827624   | 455 | 172376    | 5    |  |  |  |  |  |  |  |
| 56  | 746812   | 313 | 918915   | 142 | 827897   | 454 | 172103    | 4    |  |  |  |  |  |  |  |
| 57  | 746999   | 313 | 918830   | 142 | 828170   | 454 | 171830    | 3    |  |  |  |  |  |  |  |
| 58  | 747187   | 312 | 918745   | 142 | 828442   | 454 | 171558    | 2    |  |  |  |  |  |  |  |
| 59  | 747374   | 312 | 918659   | 142 | 828715   | 454 | 171285    | 1    |  |  |  |  |  |  |  |
| 60  | 747562   | 312 | 918574   | 142 | 828987   | 454 | 171013    | 0    |  |  |  |  |  |  |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

138°

56°

34°

146°

| /  | Sine.     | D.  | Co. no.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|-----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.747562  | 312 | 9.918574 | 142 | 9.828987 | 454 | 10.171013 | 60 |
| 1  | 747749    | 312 | 918489   | 142 | 829260   | 454 | 170740    | 59 |
| 2  | 747936    | 312 | 918404   | 142 | 829532   | 454 | 170468    | 58 |
| 3  | 748123    | 311 | 918318   | 142 | 829805   | 454 | 170195    | 57 |
| 4  | 748310    | 311 | 918233   | 142 | 830077   | 454 | 169923    | 56 |
| 5  | 748497    | 311 | 918147   | 142 | 830349   | 453 | 169651    | 55 |
| 6  | 748683    | 311 | 918062   | 142 | 830621   | 453 | 169379    | 54 |
| 7  | 748870    | 311 | 917976   | 143 | 830893   | 453 | 169107    | 53 |
| 8  | 749056    | 310 | 917891   | 143 | 831165   | 453 | 168835    | 52 |
| 9  | 749243    | 310 | 917805   | 143 | 831437   | 453 | 168563    | 51 |
| 10 | 749429    | 310 | 917719   | 143 | 831709   | 453 | 168291    | 50 |
| 11 | 9.749615  | 310 | 9.917634 | 143 | 9.831981 | 453 | 10.168019 | 49 |
| 12 | 749801    | 310 | 917548   | 143 | 832253   | 453 | 167747    | 48 |
| 13 | 749987    | 309 | 917462   | 143 | 832525   | 453 | 167475    | 47 |
| 14 | 750172    | 309 | 917376   | 143 | 832796   | 453 | 167204    | 46 |
| 15 | 750358    | 309 | 917290   | 143 | 833068   | 452 | 166932    | 45 |
| 16 | 750543    | 309 | 917204   | 143 | 833339   | 452 | 166661    | 44 |
| 17 | 750729    | 309 | 917118   | 144 | 833611   | 452 | 166389    | 43 |
| 18 | 750914    | 308 | 917032   | 144 | 833882   | 452 | 166118    | 42 |
| 19 | 751099    | 308 | 916946   | 144 | 834154   | 452 | 165846    | 41 |
| 20 | 751284    | 308 | 916859   | 144 | 834425   | 452 | 165575    | 40 |
| 21 | 9.751469  | 308 | 9.916773 | 144 | 9.834696 | 452 | 10.165304 | 39 |
| 22 | 751654    | 308 | 916687   | 144 | 834967   | 452 | 165033    | 38 |
| 23 | 751839    | 308 | 916600   | 144 | 835238   | 452 | 164762    | 37 |
| 24 | 752023    | 307 | 916514   | 144 | 835509   | 452 | 164491    | 36 |
| 25 | 752208    | 307 | 916427   | 144 | 835780   | 451 | 164220    | 35 |
| 26 | 752392    | 307 | 916341   | 144 | 836051   | 451 | 163949    | 34 |
| 27 | 752576    | 307 | 916254   | 144 | 836322   | 451 | 163678    | 33 |
| 28 | 752760    | 307 | 916167   | 145 | 836593   | 451 | 163407    | 32 |
| 29 | 752944    | 306 | 916081   | 145 | 836864   | 451 | 163136    | 31 |
| 30 | 753128    | 306 | 915994   | 145 | 837134   | 451 | 162866    | 30 |
| 31 | 9.753312  | 306 | 9.915907 | 145 | 9.837405 | 451 | 10.162595 | 29 |
| 32 | 753495    | 306 | 915820   | 145 | 837675   | 451 | 162325    | 28 |
| 33 | 753679    | 306 | 915733   | 145 | 837946   | 451 | 162054    | 27 |
| 34 | 753862    | 305 | 915646   | 145 | 838216   | 451 | 161784    | 26 |
| 35 | 754046    | 305 | 915559   | 145 | 838487   | 450 | 161513    | 25 |
| 36 | 754229    | 305 | 915472   | 145 | 838757   | 450 | 161243    | 24 |
| 37 | 754412    | 305 | 915385   | 145 | 839027   | 450 | 160973    | 23 |
| 38 | 754595    | 305 | 915297   | 145 | 839297   | 450 | 160703    | 22 |
| 39 | 754778    | 304 | 915210   | 145 | 839568   | 450 | 160432    | 21 |
| 40 | 754960    | 304 | 915123   | 146 | 839838   | 450 | 160162    | 20 |
| 41 | 9.755143  | 304 | 9.915035 | 146 | 9.840108 | 450 | 10.159892 | 19 |
| 42 | 755326    | 304 | 914948   | 146 | 840378   | 450 | 159622    | 18 |
| 43 | 755508    | 304 | 914860   | 146 | 840648   | 450 | 159352    | 17 |
| 44 | 755690    | 304 | 914773   | 146 | 840917   | 449 | 159083    | 16 |
| 45 | 755872    | 303 | 914685   | 146 | 841187   | 449 | 158813    | 15 |
| 46 | 756054    | 303 | 914598   | 146 | 841457   | 449 | 158543    | 14 |
| 47 | 756236    | 303 | 914510   | 146 | 841727   | 449 | 158273    | 13 |
| 48 | 756418    | 303 | 914422   | 146 | 841996   | 449 | 158004    | 12 |
| 49 | 756600    | 303 | 914334   | 146 | 842266   | 449 | 157734    | 11 |
| 50 | 756782    | 302 | 914246   | 147 | 842535   | 449 | 157465    | 10 |
| 51 | 9.756963  | 302 | 9.914158 | 147 | 9.842805 | 449 | 10.157195 | 9  |
| 52 | 757144    | 302 | 914070   | 147 | 843074   | 449 | 156926    | 8  |
| 53 | 757326    | 302 | 913982   | 147 | 843343   | 449 | 156657    | 7  |
| 54 | 757507    | 302 | 913894   | 147 | 843612   | 449 | 156388    | 6  |
| 55 | 757688    | 301 | 913806   | 147 | 843882   | 448 | 156118    | 5  |
| 56 | 757869    | 301 | 913718   | 147 | 844151   | 448 | 155849    | 4  |
| 57 | 758050    | 301 | 913630   | 147 | 844420   | 448 | 155580    | 3  |
| 58 | 758230    | 301 | 913541   | 147 | 844689   | 448 | 155311    | 2  |
| 59 | 758411    | 301 | 913453   | 147 | 844958   | 448 | 155042    | 1  |
| 60 | 758591    | 301 | 913365   | 147 | 845227   | 448 | 154773    | 0  |
| /  | Co. sine. | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

124°

66°



TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

58

| 38° |          |     |          |     |          |     |           | 144° |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |
| 0   | 9.758591 | 301 | 9.913365 | 147 | 9.845227 | 448 | 10.154773 | 60   |  |
| 1   | 758772   | 300 | 913276   | 147 | 845496   | 448 | 154504    | 59   |  |
| 2   | 758952   | 300 | 913187   | 148 | 845764   | 448 | 154236    | 58   |  |
| 3   | 759132   | 300 | 913099   | 148 | 846033   | 448 | 153967    | 57   |  |
| 4   | 759312   | 300 | 913010   | 148 | 846302   | 448 | 153698    | 56   |  |
| 5   | 759492   | 300 | 912922   | 148 | 846570   | 447 | 153430    | 55   |  |
| 6   | 759672   | 299 | 912833   | 148 | 846839   | 447 | 153161    | 54   |  |
| 7   | 759852   | 299 | 912744   | 148 | 847108   | 447 | 152892    | 53   |  |
| 8   | 760031   | 299 | 912655   | 148 | 847376   | 447 | 152624    | 52   |  |
| 9   | 760211   | 299 | 912566   | 148 | 847644   | 447 | 152356    | 51   |  |
| 10  | 760390   | 299 | 912477   | 148 | 847913   | 447 | 152087    | 50   |  |
| 11  | 9.760569 | 298 | 9.912388 | 148 | 9.848181 | 447 | 10.151819 | 49   |  |
| 12  | 760748   | 298 | 912299   | 149 | 848449   | 447 | 151551    | 48   |  |
| 13  | 760927   | 298 | 912210   | 149 | 848717   | 447 | 151283    | 47   |  |
| 14  | 761106   | 298 | 912121   | 149 | 848986   | 447 | 151014    | 46   |  |
| 15  | 761285   | 298 | 912031   | 149 | 849254   | 447 | 150746    | 45   |  |
| 16  | 761464   | 298 | 911942   | 149 | 849522   | 447 | 150478    | 44   |  |
| 17  | 761642   | 297 | 911853   | 149 | 849790   | 446 | 150210    | 43   |  |
| 18  | 761821   | 297 | 911763   | 149 | 850057   | 446 | 149943    | 42   |  |
| 19  | 761999   | 297 | 911674   | 149 | 850325   | 446 | 149675    | 41   |  |
| 20  | 762177   | 297 | 911584   | 149 | 850593   | 446 | 149407    | 40   |  |
| 21  | 9.762356 | 297 | 9.911495 | 149 | 9.850861 | 446 | 10.149139 | 39   |  |
| 22  | 762534   | 296 | 911405   | 149 | 851129   | 446 | 148871    | 38   |  |
| 23  | 762712   | 296 | 911315   | 150 | 851396   | 446 | 148604    | 37   |  |
| 24  | 762890   | 296 | 911226   | 150 | 851664   | 446 | 148336    | 36   |  |
| 25  | 763067   | 296 | 911136   | 150 | 851931   | 446 | 148069    | 35   |  |
| 26  | 763245   | 296 | 911046   | 150 | 852199   | 446 | 147801    | 34   |  |
| 27  | 763422   | 296 | 910956   | 150 | 852466   | 446 | 147534    | 33   |  |
| 28  | 763600   | 295 | 910866   | 150 | 852733   | 445 | 147267    | 32   |  |
| 29  | 763777   | 295 | 910776   | 150 | 853001   | 445 | 146999    | 31   |  |
| 30  | 763954   | 295 | 910686   | 150 | 853268   | 445 | 146732    | 30   |  |
| 31  | 9.764131 | 295 | 9.910596 | 150 | 9.853535 | 445 | 10.146465 | 29   |  |
| 32  | 764308   | 295 | 910506   | 150 | 853802   | 445 | 146198    | 28   |  |
| 33  | 764485   | 294 | 910415   | 150 | 854069   | 445 | 145931    | 27   |  |
| 34  | 764662   | 294 | 910325   | 151 | 854336   | 445 | 145664    | 26   |  |
| 35  | 764838   | 294 | 910235   | 151 | 854603   | 445 | 145397    | 25   |  |
| 36  | 765015   | 294 | 910144   | 151 | 854870   | 445 | 145130    | 24   |  |
| 37  | 765191   | 294 | 910054   | 151 | 855137   | 445 | 144863    | 23   |  |
| 38  | 765367   | 294 | 909963   | 151 | 855404   | 445 | 144596    | 22   |  |
| 39  | 765544   | 293 | 909873   | 151 | 855671   | 444 | 144329    | 21   |  |
| 40  | 765720   | 293 | 909782   | 151 | 855938   | 444 | 144062    | 20   |  |
| 41  | 9.765896 | 293 | 9.909691 | 151 | 9.856204 | 444 | 10.143796 | 19   |  |
| 42  | 766072   | 293 | 909601   | 151 | 856471   | 444 | 143529    | 18   |  |
| 43  | 766247   | 293 | 909510   | 151 | 856737   | 444 | 143263    | 17   |  |
| 44  | 766423   | 293 | 909419   | 151 | 857004   | 444 | 142996    | 16   |  |
| 45  | 766598   | 292 | 909328   | 152 | 857270   | 444 | 142730    | 15   |  |
| 46  | 766774   | 292 | 909237   | 152 | 857537   | 444 | 142463    | 14   |  |
| 47  | 766949   | 292 | 909146   | 152 | 857803   | 444 | 142197    | 13   |  |
| 48  | 767124   | 292 | 909055   | 152 | 858069   | 444 | 141931    | 12   |  |
| 49  | 767300   | 292 | 908964   | 152 | 858336   | 444 | 141664    | 11   |  |
| 50  | 767475   | 291 | 908873   | 152 | 858602   | 443 | 141398    | 10   |  |
| 51  | 9.767649 | 291 | 9.908781 | 152 | 9.858868 | 443 | 10.141132 | 9    |  |
| 52  | 767824   | 291 | 908690   | 152 | 859134   | 443 | 140866    | 8    |  |
| 53  | 767999   | 291 | 908599   | 152 | 859400   | 443 | 140600    | 7    |  |
| 54  | 768173   | 291 | 908507   | 152 | 859666   | 443 | 140334    | 6    |  |
| 55  | 768348   | 290 | 908416   | 153 | 859932   | 443 | 140068    | 5    |  |
| 56  | 768522   | 290 | 908324   | 153 | 860198   | 443 | 139802    | 4    |  |
| 57  | 768697   | 290 | 908233   | 153 | 860464   | 443 | 139536    | 3    |  |
| 58  | 768871   | 290 | 908141   | 153 | 860730   | 443 | 139270    | 2    |  |
| 59  | 769045   | 290 | 908049   | 153 | 860995   | 443 | 139005    | 1    |  |
| 60  | 769219   | 290 | 907958   | 153 | 861261   | 443 | 138739    | 0    |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |

125°

54°

86°

148°

| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.769219 | 290 | 9.907958 | 153 | 9.861251 | 443 | 10.138739 | 60 |
| 1  | 769393   | 289 | 907866   | 153 | 861527   | 443 | 138473    | 59 |
| 2  | 769566   | 289 | 907774   | 153 | 861792   | 442 | 138208    | 58 |
| 3  | 769740   | 289 | 907682   | 153 | 862058   | 442 | 137942    | 57 |
| 4  | 769913   | 289 | 907590   | 153 | 862323   | 442 | 137677    | 56 |
| 5  | 770087   | 289 | 907498   | 153 | 862589   | 442 | 137411    | 55 |
| 6  | 770260   | 288 | 907406   | 153 | 862854   | 442 | 137146    | 54 |
| 7  | 770433   | 288 | 907314   | 154 | 363119   | 442 | 136881    | 53 |
| 8  | 770606   | 288 | 907222   | 154 | 863385   | 442 | 136615    | 52 |
| 9  | 770779   | 288 | 907139   | 154 | 863650   | 442 | 136350    | 51 |
| 10 | 770952   | 288 | 907037   | 154 | 863915   | 442 | 136085    | 50 |
| 11 | 9.771125 | 288 | 9.906945 | 154 | 9.864180 | 442 | 10.135820 | 49 |
| 12 | 771298   | 287 | 906852   | 154 | 864445   | 442 | 135555    | 48 |
| 13 | 771470   | 287 | 906760   | 154 | 864710   | 442 | 135290    | 47 |
| 14 | 771643   | 287 | 906667   | 154 | 864975   | 441 | 135025    | 46 |
| 15 | 771815   | 287 | 906575   | 154 | 865240   | 441 | 134760    | 45 |
| 16 | 771987   | 287 | 906482   | 154 | 865505   | 441 | 134495    | 44 |
| 17 | 772159   | 287 | 906389   | 155 | 865770   | 441 | 134230    | 43 |
| 18 | 772331   | 286 | 906296   | 155 | 866035   | 441 | 133965    | 42 |
| 19 | 772503   | 286 | 906204   | 155 | 866300   | 441 | 133700    | 41 |
| 20 | 772675   | 286 | 906111   | 155 | 866564   | 441 | 133436    | 40 |
| 21 | 9.772847 | 286 | 9.906018 | 155 | 9.866829 | 441 | 10.133171 | 39 |
| 22 | 773018   | 286 | 905925   | 155 | 867094   | 441 | 132906    | 38 |
| 23 | 773190   | 286 | 905832   | 155 | 867358   | 441 | 132642    | 37 |
| 24 | 773361   | 285 | 905739   | 155 | 867623   | 441 | 132377    | 36 |
| 25 | 773533   | 285 | 905645   | 155 | 867887   | 441 | 132113    | 35 |
| 26 | 773704   | 285 | 905552   | 155 | 868152   | 440 | 131848    | 34 |
| 27 | 773875   | 285 | 905459   | 155 | 868416   | 440 | 131584    | 33 |
| 28 | 774046   | 285 | 905366   | 156 | 868680   | 440 | 131320    | 32 |
| 29 | 774217   | 285 | 905272   | 156 | 868945   | 440 | 131055    | 31 |
| 30 | 774388   | 284 | 905179   | 156 | 869209   | 440 | 130791    | 30 |
| 31 | 9.774558 | 284 | 9.905085 | 156 | 9.869473 | 440 | 10.130527 | 29 |
| 32 | 774729   | 284 | 904992   | 156 | 869737   | 440 | 130263    | 28 |
| 33 | 774899   | 284 | 904898   | 156 | 870001   | 440 | 129999    | 27 |
| 34 | 775070   | 284 | 904804   | 156 | 870265   | 440 | 129735    | 26 |
| 35 | 775240   | 284 | 904711   | 156 | 870529   | 440 | 129471    | 25 |
| 36 | 775410   | 283 | 904617   | 156 | 870793   | 440 | 129207    | 24 |
| 37 | 775580   | 283 | 904523   | 156 | 871057   | 440 | 128943    | 23 |
| 38 | 775750   | 283 | 904429   | 157 | 871321   | 440 | 128679    | 22 |
| 39 | 775920   | 283 | 904335   | 157 | 871585   | 440 | 128415    | 21 |
| 40 | 776090   | 283 | 904241   | 157 | 871849   | 439 | 128151    | 20 |
| 41 | 9.776259 | 283 | 9.904147 | 157 | 9.872112 | 439 | 10.127888 | 19 |
| 42 | 776429   | 282 | 904053   | 157 | 872376   | 439 | 127624    | 18 |
| 43 | 776598   | 282 | 903959   | 157 | 872640   | 439 | 127360    | 17 |
| 44 | 776768   | 282 | 903864   | 157 | 872903   | 439 | 127097    | 16 |
| 45 | 776937   | 282 | 903770   | 157 | 873167   | 439 | 126833    | 15 |
| 46 | 777106   | 282 | 903676   | 157 | 873430   | 439 | 126570    | 14 |
| 47 | 777275   | 281 | 903581   | 157 | 873694   | 439 | 126306    | 13 |
| 48 | 777444   | 281 | 903487   | 157 | 873957   | 439 | 126043    | 12 |
| 49 | 777613   | 281 | 903392   | 158 | 874220   | 439 | 125780    | 11 |
| 50 | 777781   | 281 | 903298   | 158 | 874484   | 439 | 125516    | 10 |
| 51 | 9.777950 | 281 | 9.903203 | 158 | 9.874747 | 439 | 10.125253 | 9  |
| 52 | 778119   | 281 | 903108   | 158 | 875010   | 439 | 124990    | 8  |
| 53 | 778287   | 280 | 903014   | 158 | 875273   | 438 | 124727    | 7  |
| 54 | 778455   | 280 | 902919   | 158 | 875537   | 438 | 124463    | 6  |
| 55 | 778624   | 280 | 902824   | 158 | 875800   | 438 | 124200    | 5  |
| 56 | 778792   | 280 | 902729   | 158 | 876063   | 438 | 123937    | 4  |
| 57 | 778960   | 280 | 902634   | 158 | 876326   | 438 | 123674    | 3  |
| 58 | 779128   | 280 | 902539   | 159 | 876589   | 438 | 123411    | 2  |
| 59 | 779295   | 279 | 902444   | 159 | 876852   | 438 | 123148    | 1  |
| 60 | 779463   | 279 | 902349   | 159 | 877114   | 438 | 122886    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| '  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | '  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.779463 | 279 | 9.902349 | 159 | 9.877114 | 438 | 10.122886 | 60 |
| 1  | 779631   | 279 | 902253   | 159 | 877377   | 438 | 122623    | 59 |
| 2  | 779798   | 279 | 902158   | 159 | 877640   | 438 | 122360    | 58 |
| 3  | 779966   | 279 | 902063   | 159 | 877903   | 438 | 122097    | 57 |
| 4  | 780133   | 279 | 901967   | 159 | 878165   | 438 | 121835    | 56 |
| 5  | 780300   | 278 | 901872   | 159 | 878428   | 438 | 121572    | 55 |
| 6  | 780467   | 278 | 901776   | 159 | 878691   | 438 | 121309    | 54 |
| 7  | 780634   | 278 | 901681   | 159 | 878953   | 437 | 121047    | 53 |
| 8  | 780801   | 278 | 901585   | 159 | 879216   | 437 | 120784    | 52 |
| 9  | 780968   | 278 | 901490   | 159 | 879478   | 437 | 120522    | 51 |
| 10 | 781134   | 278 | 901394   | 160 | 879741   | 437 | 120259    | 50 |
| 11 | 9.781301 | 277 | 9.901298 | 160 | 9.880003 | 437 | 10.119997 | 49 |
| 12 | 781468   | 277 | 901202   | 160 | 880265   | 437 | 119735    | 48 |
| 13 | 781634   | 277 | 901106   | 160 | 880528   | 437 | 119472    | 47 |
| 14 | 781800   | 277 | 901010   | 160 | 880790   | 437 | 119210    | 46 |
| 15 | 781966   | 277 | 900914   | 160 | 881052   | 437 | 118948    | 45 |
| 16 | 782132   | 277 | 900818   | 160 | 881314   | 437 | 118686    | 44 |
| 17 | 782298   | 276 | 900722   | 160 | 881577   | 437 | 118423    | 43 |
| 18 | 782464   | 276 | 900626   | 160 | 881839   | 437 | 118161    | 42 |
| 19 | 782630   | 276 | 900529   | 160 | 882101   | 437 | 117899    | 41 |
| 20 | 782796   | 276 | 900433   | 161 | 882363   | 436 | 117637    | 40 |
| 21 | 9.782961 | 276 | 9.900337 | 161 | 9.882625 | 436 | 10.117375 | 39 |
| 22 | 783127   | 276 | 900240   | 161 | 882887   | 436 | 117113    | 38 |
| 23 | 783292   | 275 | 900144   | 161 | 883148   | 436 | 116852    | 37 |
| 24 | 783458   | 275 | 900047   | 161 | 883410   | 436 | 116590    | 36 |
| 25 | 783623   | 275 | 899951   | 161 | 883672   | 436 | 116328    | 35 |
| 26 | 783788   | 275 | 899854   | 161 | 883934   | 436 | 116066    | 34 |
| 27 | 783953   | 275 | 899757   | 161 | 884196   | 436 | 115804    | 33 |
| 28 | 784118   | 275 | 899660   | 161 | 884457   | 436 | 115543    | 32 |
| 29 | 784282   | 274 | 899564   | 161 | 884719   | 436 | 115281    | 31 |
| 30 | 784447   | 274 | 899467   | 162 | 884980   | 436 | 115020    | 30 |
| 31 | 9.784612 | 274 | 9.899370 | 162 | 9.885242 | 436 | 10.114758 | 29 |
| 32 | 784776   | 274 | 899273   | 162 | 885504   | 436 | 114496    | 28 |
| 33 | 784941   | 274 | 899176   | 162 | 885765   | 436 | 114235    | 27 |
| 34 | 785105   | 274 | 899078   | 162 | 886026   | 436 | 113974    | 26 |
| 35 | 785269   | 273 | 898981   | 162 | 886288   | 436 | 113712    | 25 |
| 36 | 785433   | 273 | 898884   | 162 | 886549   | 435 | 113451    | 24 |
| 37 | 785597   | 273 | 898787   | 162 | 886811   | 435 | 113189    | 23 |
| 38 | 785761   | 273 | 898689   | 162 | 887072   | 435 | 112928    | 22 |
| 39 | 785925   | 273 | 898592   | 162 | 887333   | 435 | 112667    | 21 |
| 40 | 786089   | 273 | 898494   | 163 | 887594   | 435 | 112406    | 20 |
| 41 | 9.786252 | 272 | 9.898397 | 163 | 9.887855 | 435 | 10.112145 | 19 |
| 42 | 786416   | 272 | 898299   | 163 | 888116   | 435 | 111884    | 18 |
| 43 | 786579   | 272 | 898202   | 163 | 888378   | 435 | 111622    | 17 |
| 44 | 786742   | 272 | 898104   | 163 | 888639   | 435 | 111361    | 16 |
| 45 | 786906   | 272 | 898006   | 163 | 888900   | 435 | 111100    | 15 |
| 46 | 787069   | 272 | 897908   | 163 | 889161   | 435 | 110839    | 14 |
| 47 | 787232   | 271 | 897810   | 163 | 889421   | 435 | 110579    | 13 |
| 48 | 787395   | 271 | 897712   | 163 | 889682   | 435 | 110318    | 12 |
| 49 | 787557   | 271 | 897614   | 163 | 889943   | 435 | 110057    | 11 |
| 50 | 787720   | 271 | 897516   | 163 | 890204   | 434 | 109796    | 10 |
| 51 | 9.787883 | 271 | 9.897418 | 164 | 9.890465 | 434 | 10.109535 | 9  |
| 52 | 788045   | 271 | 897320   | 164 | 890725   | 434 | 109275    | 8  |
| 53 | 788208   | 271 | 897222   | 164 | 890986   | 434 | 109014    | 7  |
| 54 | 788370   | 270 | 897123   | 164 | 891247   | 434 | 108753    | 6  |
| 55 | 788532   | 270 | 897025   | 164 | 891507   | 434 | 108493    | 5  |
| 56 | 788694   | 270 | 896926   | 164 | 891768   | 434 | 108232    | 4  |
| 57 | 788856   | 270 | 896828   | 164 | 892028   | 434 | 107972    | 3  |
| 58 | 789018   | 270 | 896729   | 164 | 892289   | 434 | 107711    | 2  |
| 59 | 789180   | 270 | 896631   | 164 | 892549   | 434 | 107451    | 1  |
| 60 | 789342   | 269 | 896532   | 164 | 892810   | 434 | 107190    | 0  |
| '  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | '  |

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| /  | Srs.     | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9-789342 | 269 | 9-896532 | 164 | 9-892810 | 434 | 10-107190 | 60 |
| 1  | 789304   | 269 | 896433   | 165 | 893070   | 434 | 106930    | 59 |
| 2  | 789665   | 269 | 896335   | 165 | 893331   | 434 | 106669    | 58 |
| 3  | 789827   | 269 | 896236   | 165 | 893591   | 434 | 106409    | 57 |
| 4  | 789988   | 269 | 896137   | 165 | 893851   | 434 | 106149    | 56 |
| 5  | 790149   | 269 | 896038   | 165 | 894111   | 434 | 105889    | 55 |
| 6  | 790310   | 268 | 895939   | 165 | 894372   | 434 | 105628    | 54 |
| 7  | 790471   | 268 | 895840   | 165 | 894632   | 433 | 105368    | 53 |
| 8  | 790632   | 268 | 895741   | 165 | 894892   | 433 | 105108    | 52 |
| 9  | 790793   | 268 | 895641   | 165 | 895152   | 433 | 104848    | 51 |
| 10 | 790954   | 268 | 895542   | 165 | 895412   | 433 | 104588    | 50 |
| 11 | 9-791115 | 268 | 9-895443 | 166 | 9-895672 | 433 | 10-104328 | 49 |
| 12 | 791275   | 267 | 895343   | 166 | 895932   | 433 | 104068    | 48 |
| 13 | 791436   | 267 | 895244   | 166 | 896192   | 433 | 103808    | 47 |
| 14 | 791596   | 267 | 895145   | 166 | 896452   | 433 | 103548    | 46 |
| 15 | 791757   | 267 | 895045   | 166 | 896712   | 433 | 103288    | 45 |
| 16 | 791917   | 267 | 894945   | 166 | 896971   | 433 | 103029    | 44 |
| 17 | 792077   | 267 | 894846   | 166 | 897231   | 433 | 102769    | 43 |
| 18 | 792237   | 266 | 894746   | 166 | 897491   | 433 | 102509    | 42 |
| 19 | 792397   | 266 | 894646   | 166 | 897751   | 433 | 102249    | 41 |
| 20 | 792557   | 266 | 894546   | 166 | 898010   | 433 | 101990    | 40 |
| 21 | 9-792716 | 266 | 9-894446 | 167 | 9-898270 | 433 | 10-101730 | 39 |
| 22 | 792876   | 266 | 894346   | 167 | 898530   | 433 | 101470    | 38 |
| 23 | 793035   | 266 | 894246   | 167 | 898789   | 433 | 101211    | 37 |
| 24 | 793195   | 265 | 894146   | 167 | 899049   | 432 | 100951    | 36 |
| 25 | 793354   | 265 | 894046   | 167 | 899308   | 432 | 100692    | 35 |
| 26 | 793514   | 265 | 893946   | 167 | 899568   | 432 | 100432    | 34 |
| 27 | 793673   | 265 | 893846   | 167 | 899827   | 432 | 100173    | 33 |
| 28 | 793832   | 265 | 893745   | 167 | 900087   | 432 | 999913    | 32 |
| 29 | 793991   | 265 | 893645   | 167 | 900346   | 432 | 999654    | 31 |
| 30 | 794150   | 264 | 893544   | 167 | 900605   | 432 | 999395    | 30 |
| 31 | 9-794308 | 264 | 9-893444 | 168 | 9-900864 | 432 | 10-999136 | 29 |
| 32 | 794467   | 264 | 893343   | 168 | 901124   | 432 | 998876    | 28 |
| 33 | 794626   | 264 | 893243   | 168 | 901383   | 432 | 998617    | 27 |
| 34 | 794784   | 264 | 893142   | 168 | 901642   | 432 | 998358    | 26 |
| 35 | 794942   | 264 | 893041   | 168 | 901901   | 432 | 998099    | 25 |
| 36 | 795101   | 264 | 892940   | 168 | 902160   | 432 | 997840    | 24 |
| 37 | 795259   | 263 | 892839   | 168 | 902420   | 432 | 997580    | 23 |
| 38 | 795417   | 263 | 892739   | 168 | 902679   | 432 | 997321    | 22 |
| 39 | 795575   | 263 | 892638   | 168 | 902938   | 432 | 997062    | 21 |
| 40 | 795733   | 263 | 892536   | 168 | 903197   | 431 | 996803    | 20 |
| 41 | 9-795891 | 263 | 9-892435 | 169 | 9-903456 | 431 | 10-996544 | 19 |
| 42 | 796049   | 263 | 892334   | 169 | 903714   | 431 | 996286    | 18 |
| 43 | 796206   | 263 | 892233   | 169 | 903973   | 431 | 996027    | 17 |
| 44 | 796364   | 262 | 892132   | 169 | 904232   | 431 | 995768    | 16 |
| 45 | 796521   | 262 | 892030   | 169 | 904491   | 431 | 995509    | 15 |
| 46 | 796679   | 262 | 891929   | 169 | 904750   | 431 | 995250    | 14 |
| 47 | 796836   | 262 | 891827   | 169 | 905008   | 431 | 994992    | 13 |
| 48 | 796993   | 262 | 891726   | 169 | 905267   | 431 | 994733    | 12 |
| 49 | 797150   | 261 | 891624   | 169 | 905526   | 431 | 994474    | 11 |
| 50 | 797307   | 261 | 891523   | 170 | 905785   | 431 | 994215    | 10 |
| 51 | 9-797464 | 261 | 9-891421 | 170 | 9-906043 | 431 | 10-993957 | 9  |
| 52 | 797621   | 261 | 891319   | 170 | 906302   | 431 | 993698    | 8  |
| 53 | 797777   | 261 | 891217   | 170 | 906560   | 431 | 993440    | 7  |
| 54 | 797934   | 261 | 891115   | 170 | 906819   | 431 | 993181    | 6  |
| 55 | 798091   | 261 | 891013   | 170 | 907077   | 431 | 992923    | 5  |
| 56 | 798247   | 261 | 890911   | 170 | 907336   | 431 | 992664    | 4  |
| 57 | 798403   | 260 | 890809   | 170 | 907594   | 431 | 992406    | 3  |
| 58 | 798560   | 260 | 890707   | 170 | 907853   | 431 | 992147    | 2  |
| 59 | 798716   | 260 | 890605   | 170 | 908111   | 430 | 991889    | 1  |
| 60 | 798872   | 260 | 890503   | 170 | 908369   | 430 | 991631    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.798872 | 260 | 9.890503 | 170 | 9.908369 | 430 | 10.091631 | 60 |
| 1  | 799028   | 260 | 890400   | 171 | 908628   | 430 | 091372    | 59 |
| 2  | 799184   | 260 | 890298   | 171 | 908886   | 430 | 091114    | 58 |
| 3  | 799339   | 259 | 890195   | 171 | 909144   | 430 | 090856    | 57 |
| 4  | 799495   | 259 | 890093   | 171 | 909402   | 430 | 090598    | 56 |
| 5  | 799651   | 259 | 889990   | 171 | 909660   | 430 | 090340    | 55 |
| 6  | 799806   | 259 | 889888   | 171 | 909918   | 430 | 090082    | 54 |
| 7  | 799962   | 259 | 889785   | 171 | 910177   | 430 | 089823    | 53 |
| 8  | 800117   | 259 | 889682   | 171 | 910435   | 430 | 089565    | 52 |
| 9  | 800272   | 258 | 889579   | 171 | 910693   | 430 | 089307    | 51 |
| 10 | 800427   | 258 | 889477   | 171 | 910951   | 430 | 089049    | 50 |
| 11 | 9.800582 | 258 | 9.889374 | 172 | 9.911209 | 430 | 10.088791 | 49 |
| 12 | 800737   | 258 | 889271   | 172 | 911467   | 430 | 088533    | 48 |
| 13 | 800892   | 258 | 889168   | 172 | 911725   | 430 | 088275    | 47 |
| 14 | 801047   | 258 | 889064   | 172 | 911982   | 430 | 088018    | 46 |
| 15 | 801201   | 258 | 888961   | 172 | 912240   | 430 | 087760    | 45 |
| 16 | 801356   | 257 | 888858   | 172 | 912498   | 430 | 087502    | 44 |
| 17 | 801511   | 257 | 888755   | 172 | 912756   | 430 | 087244    | 43 |
| 18 | 801665   | 257 | 888651   | 172 | 913014   | 429 | 086986    | 42 |
| 19 | 801819   | 257 | 888548   | 172 | 913271   | 429 | 086729    | 41 |
| 20 | 801973   | 257 | 888444   | 173 | 913529   | 429 | 086471    | 40 |
| 21 | 9.802128 | 257 | 9.888341 | 173 | 9.913787 | 429 | 10.086213 | 39 |
| 22 | 802282   | 256 | 888237   | 173 | 914044   | 429 | 085956    | 38 |
| 23 | 802436   | 256 | 888134   | 173 | 914302   | 429 | 085698    | 37 |
| 24 | 802589   | 256 | 888030   | 173 | 914560   | 429 | 085440    | 36 |
| 25 | 802743   | 256 | 887926   | 173 | 914817   | 429 | 085183    | 35 |
| 26 | 802897   | 256 | 887822   | 173 | 915075   | 429 | 084925    | 34 |
| 27 | 803050   | 256 | 887718   | 173 | 915332   | 429 | 084668    | 33 |
| 28 | 803204   | 256 | 887614   | 173 | 915590   | 429 | 084410    | 32 |
| 29 | 803357   | 255 | 887510   | 173 | 915847   | 429 | 084153    | 31 |
| 30 | 803511   | 255 | 887406   | 174 | 916104   | 429 | 083896    | 30 |
| 31 | 9.803664 | 255 | 9.887302 | 174 | 9.916362 | 429 | 10.083638 | 29 |
| 32 | 803817   | 255 | 887198   | 174 | 916619   | 429 | 083381    | 28 |
| 33 | 803970   | 255 | 887093   | 174 | 916877   | 429 | 083123    | 27 |
| 34 | 804123   | 255 | 886989   | 174 | 917134   | 429 | 082866    | 26 |
| 35 | 804276   | 254 | 886885   | 174 | 917391   | 429 | 082609    | 25 |
| 36 | 804428   | 254 | 886780   | 174 | 917648   | 429 | 082352    | 24 |
| 37 | 804581   | 254 | 886676   | 174 | 917906   | 429 | 082094    | 23 |
| 38 | 804734   | 254 | 886571   | 174 | 918163   | 428 | 081837    | 22 |
| 39 | 804886   | 254 | 886466   | 174 | 918420   | 428 | 081580    | 21 |
| 40 | 805039   | 254 | 886362   | 175 | 918677   | 428 | 081323    | 20 |
| 41 | 9.805191 | 254 | 9.886257 | 175 | 9.918934 | 428 | 10.081066 | 19 |
| 42 | 805343   | 253 | 886152   | 175 | 919191   | 428 | 080809    | 18 |
| 43 | 805495   | 253 | 886047   | 175 | 919448   | 428 | 080552    | 17 |
| 44 | 805647   | 253 | 885942   | 175 | 919705   | 428 | 080295    | 16 |
| 45 | 805799   | 253 | 885837   | 175 | 919962   | 428 | 080038    | 15 |
| 46 | 805951   | 253 | 885732   | 175 | 920219   | 428 | 079781    | 14 |
| 47 | 806103   | 253 | 885627   | 175 | 920476   | 428 | 079524    | 13 |
| 48 | 806254   | 253 | 885522   | 175 | 920733   | 428 | 079267    | 12 |
| 49 | 806406   | 252 | 885416   | 175 | 920990   | 428 | 079010    | 11 |
| 50 | 806557   | 252 | 885311   | 176 | 921247   | 428 | 078753    | 10 |
| 51 | 9.806709 | 252 | 9.885205 | 176 | 9.921503 | 428 | 10.078497 | 9  |
| 52 | 806860   | 252 | 885100   | 176 | 921760   | 428 | 078240    | 8  |
| 53 | 807011   | 252 | 884994   | 176 | 922017   | 428 | 077983    | 7  |
| 54 | 807163   | 252 | 884889   | 176 | 922274   | 428 | 077726    | 6  |
| 55 | 807314   | 252 | 884783   | 176 | 922530   | 428 | 077470    | 5  |
| 56 | 807465   | 251 | 884677   | 176 | 922787   | 428 | 077213    | 4  |
| 57 | 807615   | 251 | 884572   | 176 | 923044   | 428 | 076956    | 3  |
| 58 | 807766   | 251 | 884466   | 176 | 923300   | 428 | 076700    | 2  |
| 59 | 807917   | 251 | 884360   | 176 | 923557   | 427 | 076443    | 1  |
| 60 | 808067   | 251 | 884254   | 177 | 923814   | 427 | 076186    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9-808067 | 251 | 9-884254 | 177 | 9-923814 | 427 | 10-076186 | 60 |
| 1  | 808218   | 251 | 884148   | 177 | 924070   | 427 | 075930    | 59 |
| 2  | 808368   | 251 | 884042   | 177 | 924327   | 427 | 075673    | 58 |
| 3  | 808519   | 250 | 883936   | 177 | 924583   | 427 | 075417    | 57 |
| 4  | 808669   | 250 | 883829   | 177 | 924840   | 427 | 075160    | 56 |
| 5  | 808819   | 250 | 883723   | 177 | 925096   | 427 | 074904    | 55 |
| 6  | 808969   | 250 | 883617   | 177 | 925352   | 427 | 074648    | 54 |
| 7  | 809119   | 250 | 883510   | 177 | 925609   | 427 | 074391    | 53 |
| 8  | 809269   | 250 | 883404   | 177 | 925865   | 427 | 074135    | 52 |
| 9  | 809419   | 249 | 883297   | 178 | 926122   | 427 | 073878    | 51 |
| 10 | 809569   | 249 | 883191   | 178 | 926378   | 427 | 073622    | 50 |
| 11 | 9-809718 | 249 | 9-883084 | 178 | 9-926634 | 427 | 10-073366 | 49 |
| 12 | 809868   | 249 | 882977   | 178 | 926890   | 427 | 073110    | 48 |
| 13 | 810017   | 249 | 882871   | 178 | 927147   | 427 | 072853    | 47 |
| 14 | 810167   | 249 | 882764   | 178 | 927403   | 427 | 072597    | 46 |
| 15 | 810316   | 248 | 882657   | 178 | 927659   | 427 | 072341    | 45 |
| 16 | 810465   | 248 | 882550   | 178 | 927915   | 427 | 072085    | 44 |
| 17 | 810614   | 248 | 882443   | 178 | 928171   | 427 | 071829    | 43 |
| 18 | 810763   | 248 | 882336   | 179 | 928427   | 427 | 071573    | 42 |
| 19 | 810912   | 248 | 882229   | 179 | 928684   | 427 | 071316    | 41 |
| 20 | 811061   | 248 | 882121   | 179 | 928940   | 427 | 071060    | 40 |
| 21 | 9-811210 | 248 | 9-882014 | 179 | 9-929196 | 427 | 10-070804 | 39 |
| 22 | 811358   | 247 | 881907   | 179 | 929452   | 427 | 070548    | 38 |
| 23 | 811507   | 247 | 881799   | 179 | 929708   | 427 | 070292    | 37 |
| 24 | 811655   | 247 | 881692   | 179 | 929964   | 426 | 070036    | 36 |
| 25 | 811804   | 247 | 881584   | 179 | 930220   | 426 | 069780    | 35 |
| 26 | 811952   | 247 | 881477   | 179 | 930475   | 426 | 069525    | 34 |
| 27 | 812100   | 247 | 881369   | 179 | 930731   | 426 | 069269    | 33 |
| 28 | 812248   | 247 | 881261   | 180 | 930987   | 426 | 069013    | 32 |
| 29 | 812396   | 246 | 881153   | 180 | 931243   | 426 | 068757    | 31 |
| 30 | 812544   | 246 | 881046   | 180 | 931499   | 426 | 068501    | 30 |
| 31 | 9-812692 | 246 | 9-880938 | 180 | 9-931755 | 426 | 10-068245 | 29 |
| 32 | 812840   | 246 | 880830   | 180 | 932010   | 426 | 067990    | 28 |
| 33 | 812988   | 246 | 880722   | 180 | 932266   | 426 | 067734    | 27 |
| 34 | 813135   | 246 | 880613   | 180 | 932522   | 426 | 067478    | 26 |
| 35 | 813283   | 246 | 880505   | 180 | 932778   | 426 | 067222    | 25 |
| 36 | 813430   | 245 | 880397   | 180 | 933033   | 426 | 066967    | 24 |
| 37 | 813578   | 245 | 880289   | 181 | 933289   | 426 | 066711    | 23 |
| 38 | 813725   | 245 | 880180   | 181 | 933545   | 426 | 066455    | 22 |
| 39 | 813872   | 245 | 880072   | 181 | 933800   | 426 | 066200    | 21 |
| 40 | 814019   | 245 | 879963   | 181 | 934056   | 426 | 065944    | 20 |
| 41 | 9-814166 | 245 | 9-879855 | 181 | 9-934311 | 426 | 10-065689 | 19 |
| 42 | 814313   | 245 | 879746   | 181 | 934567   | 426 | 065433    | 18 |
| 43 | 814460   | 244 | 879637   | 181 | 934822   | 426 | 065178    | 17 |
| 44 | 814607   | 244 | 879529   | 181 | 935078   | 426 | 064922    | 16 |
| 45 | 814753   | 244 | 879420   | 181 | 935333   | 426 | 064667    | 15 |
| 46 | 814900   | 244 | 879311   | 181 | 935589   | 426 | 064411    | 14 |
| 47 | 815046   | 244 | 879202   | 182 | 935844   | 426 | 064156    | 13 |
| 48 | 815193   | 244 | 879093   | 182 | 936100   | 426 | 063900    | 12 |
| 49 | 815339   | 244 | 878984   | 182 | 936355   | 426 | 063645    | 11 |
| 50 | 815485   | 243 | 878875   | 182 | 936611   | 426 | 063389    | 10 |
| 51 | 9-815631 | 243 | 9-878766 | 182 | 9-936866 | 425 | 10-063134 | 9  |
| 52 | 815778   | 243 | 878656   | 182 | 937121   | 425 | 062879    | 8  |
| 53 | 815924   | 243 | 878547   | 182 | 937377   | 425 | 062623    | 7  |
| 54 | 816069   | 243 | 878438   | 182 | 937632   | 425 | 062368    | 6  |
| 55 | 816215   | 243 | 878328   | 182 | 937887   | 425 | 062113    | 5  |
| 56 | 816361   | 243 | 878219   | 183 | 938142   | 425 | 061858    | 4  |
| 57 | 816507   | 242 | 878109   | 183 | 938398   | 425 | 061602    | 3  |
| 58 | 816652   | 242 | 877999   | 183 | 938653   | 425 | 061347    | 2  |
| 59 | 816798   | 242 | 877890   | 183 | 938908   | 425 | 061092    | 1  |
| 60 | 816943   | 242 | 877780   | 183 | 939163   | 425 | 060837    | 0  |
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| SIN-ARTHEMIO OLIVER TANGENTE ETC. TABLE II |  |  |  |  |  |  |  |  |  |
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|                                            |  |  |  |  |  |  |  |  |  |





44°

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| /  | Sine.   | D.  | Cosine. | D.  | Tang.   | D.  | Cotang.  | /  |
|----|---------|-----|---------|-----|---------|-----|----------|----|
| 0  | 9.84371 | 2.8 | 9.84371 | 2.8 | 9.84371 | 421 | 10.05628 | 20 |
| 1  | 84372   | 2.8 | 84372   | 2.8 | 84372   | 421 | 05.628   | 19 |
| 2  | 84373   | 2.8 | 84373   | 2.8 | 84373   | 421 | 05.629   | 18 |
| 3  | 84374   | 2.8 | 84374   | 2.8 | 84374   | 421 | 05.630   | 17 |
| 4  | 84375   | 2.8 | 84375   | 2.8 | 84375   | 421 | 05.631   | 16 |
| 5  | 84376   | 2.8 | 84376   | 2.8 | 84376   | 421 | 05.632   | 15 |
| 6  | 84377   | 2.8 | 84377   | 2.8 | 84377   | 421 | 05.633   | 14 |
| 7  | 84378   | 2.8 | 84378   | 2.8 | 84378   | 421 | 05.634   | 13 |
| 8  | 84379   | 2.8 | 84379   | 2.8 | 84379   | 421 | 05.635   | 12 |
| 9  | 84380   | 2.8 | 84380   | 2.8 | 84380   | 421 | 05.636   | 11 |
| 10 | 84381   | 2.8 | 84381   | 2.8 | 84381   | 421 | 05.637   | 10 |
| 11 | 9.84382 | 2.8 | 9.84382 | 2.8 | 9.84382 | 421 | 10.05638 | 9  |
| 12 | 84383   | 2.8 | 84383   | 2.8 | 84383   | 421 | 05.638   | 8  |
| 13 | 84384   | 2.8 | 84384   | 2.8 | 84384   | 421 | 05.639   | 7  |
| 14 | 84385   | 2.8 | 84385   | 2.8 | 84385   | 421 | 05.640   | 6  |
| 15 | 84386   | 2.8 | 84386   | 2.8 | 84386   | 421 | 05.641   | 5  |
| 16 | 84387   | 2.8 | 84387   | 2.8 | 84387   | 421 | 05.642   | 4  |
| 17 | 84388   | 2.8 | 84388   | 2.8 | 84388   | 421 | 05.643   | 3  |
| 18 | 84389   | 2.8 | 84389   | 2.8 | 84389   | 421 | 05.644   | 2  |
| 19 | 84390   | 2.8 | 84390   | 2.8 | 84390   | 421 | 05.645   | 1  |
| 20 | 84391   | 2.8 | 84391   | 2.8 | 84391   | 421 | 05.646   | 0  |
| 21 | 9.84392 | 2.8 | 9.84392 | 2.8 | 9.84392 | 421 | 10.05647 | 20 |
| 22 | 84393   | 2.8 | 84393   | 2.8 | 84393   | 421 | 05.647   | 19 |
| 23 | 84394   | 2.8 | 84394   | 2.8 | 84394   | 421 | 05.648   | 18 |
| 24 | 84395   | 2.8 | 84395   | 2.8 | 84395   | 421 | 05.649   | 17 |
| 25 | 84396   | 2.8 | 84396   | 2.8 | 84396   | 421 | 05.650   | 16 |
| 26 | 84397   | 2.8 | 84397   | 2.8 | 84397   | 421 | 05.651   | 15 |
| 27 | 84398   | 2.8 | 84398   | 2.8 | 84398   | 421 | 05.652   | 14 |
| 28 | 84399   | 2.8 | 84399   | 2.8 | 84399   | 421 | 05.653   | 13 |
| 29 | 84400   | 2.8 | 84400   | 2.8 | 84400   | 421 | 05.654   | 12 |
| 30 | 84401   | 2.8 | 84401   | 2.8 | 84401   | 421 | 05.655   | 11 |
| 31 | 84402   | 2.8 | 84402   | 2.8 | 84402   | 421 | 05.656   | 10 |
| 32 | 84403   | 2.8 | 84403   | 2.8 | 84403   | 421 | 05.657   | 9  |
| 33 | 84404   | 2.8 | 84404   | 2.8 | 84404   | 421 | 05.658   | 8  |
| 34 | 84405   | 2.8 | 84405   | 2.8 | 84405   | 421 | 05.659   | 7  |
| 35 | 84406   | 2.8 | 84406   | 2.8 | 84406   | 421 | 05.660   | 6  |
| 36 | 84407   | 2.8 | 84407   | 2.8 | 84407   | 421 | 05.661   | 5  |
| 37 | 84408   | 2.8 | 84408   | 2.8 | 84408   | 421 | 05.662   | 4  |
| 38 | 84409   | 2.8 | 84409   | 2.8 | 84409   | 421 | 05.663   | 3  |
| 39 | 84410   | 2.8 | 84410   | 2.8 | 84410   | 421 | 05.664   | 2  |
| 40 | 84411   | 2.8 | 84411   | 2.8 | 84411   | 421 | 05.665   | 1  |
| 41 | 9.84412 | 2.8 | 9.84412 | 2.8 | 9.84412 | 421 | 10.05666 | 0  |
| 42 | 84413   | 2.8 | 84413   | 2.8 | 84413   | 421 | 05.666   | 20 |
| 43 | 84414   | 2.8 | 84414   | 2.8 | 84414   | 421 | 05.667   | 19 |
| 44 | 84415   | 2.8 | 84415   | 2.8 | 84415   | 421 | 05.668   | 18 |
| 45 | 84416   | 2.8 | 84416   | 2.8 | 84416   | 421 | 05.669   | 17 |
| 46 | 84417   | 2.8 | 84417   | 2.8 | 84417   | 421 | 05.670   | 16 |
| 47 | 84418   | 2.8 | 84418   | 2.8 | 84418   | 421 | 05.671   | 15 |
| 48 | 84419   | 2.8 | 84419   | 2.8 | 84419   | 421 | 05.672   | 14 |
| 49 | 84420   | 2.8 | 84420   | 2.8 | 84420   | 421 | 05.673   | 13 |
| 50 | 84421   | 2.8 | 84421   | 2.8 | 84421   | 421 | 05.674   | 12 |
| 51 | 84422   | 2.8 | 84422   | 2.8 | 84422   | 421 | 05.675   | 11 |
| 52 | 84423   | 2.8 | 84423   | 2.8 | 84423   | 421 | 05.676   | 10 |
| 53 | 84424   | 2.8 | 84424   | 2.8 | 84424   | 421 | 05.677   | 9  |
| 54 | 84425   | 2.8 | 84425   | 2.8 | 84425   | 421 | 05.678   | 8  |
| 55 | 84426   | 2.8 | 84426   | 2.8 | 84426   | 421 | 05.679   | 7  |
| 56 | 84427   | 2.8 | 84427   | 2.8 | 84427   | 421 | 05.680   | 6  |
| 57 | 84428   | 2.8 | 84428   | 2.8 | 84428   | 421 | 05.681   | 5  |
| 58 | 84429   | 2.8 | 84429   | 2.8 | 84429   | 421 | 05.682   | 4  |
| 59 | 84430   | 2.8 | 84430   | 2.8 | 84430   | 421 | 05.683   | 3  |
| 60 | 84431   | 2.8 | 84431   | 2.8 | 84431   | 421 | 05.684   | 2  |
| 61 | 84432   | 2.8 | 84432   | 2.8 | 84432   | 421 | 05.685   | 1  |
| 62 | 84433   | 2.8 | 84433   | 2.8 | 84433   | 421 | 05.686   | 0  |

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45°

TABLE III.,  
OF  
NATURAL SINES AND TANGENTS;  
TO  
•  
EVERY DEGREE AND MINUTE OF THE QUADRANT.

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If the given angle is less than  $45^\circ$ , look for the degrees and the title of the column, at the *top* of the page; and for the minutes on the *left*. But if the angle is between  $45^\circ$  and  $90^\circ$ , look for the degrees and the title of the column, at the *bottom*; and for the minutes on the *right*.

The *Secants* and *Cosecants*, which are not inserted in this table, may be easily supplied. If 1 be divided by the cosine of an arc, the quotient will be the secant of that arc. And if 1 be divided by the sine, the quotient will be the cosecant.

The values of the Sines and Cosines are less than a unit, and are given in decimals, although the decimal point is not printed. So also, the tangents of arcs less than  $45^\circ$ , and cotangents of arcs greater than  $45^\circ$ , are less than a unit and are expressed in decimals with the decimal point omitted.

| °  | 0°      |         | 1°      |         | 2°      |         | 3°      |         | 4°      |         | °  |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 00000   | Unit.   | 01745   | 99985   | 03490   | 99939   | 05234   | 99863   | 06976   | 99756   | 60 |
| 1  | 00029   | Unit.   | 01774   | 99984   | 03519   | 99938   | 05263   | 99861   | 07005   | 99754   | 59 |
| 2  | 00058   | Unit.   | 01803   | 99984   | 03548   | 99937   | 05292   | 99860   | 07034   | 99752   | 58 |
| 3  | 00087   | Unit.   | 01832   | 99983   | 03577   | 99936   | 05321   | 99858   | 07063   | 99750   | 57 |
| 4  | 00116   | Unit.   | 01862   | 99983   | 03606   | 99935   | 05350   | 99857   | 07092   | 99748   | 56 |
| 5  | 00145   | Unit.   | 01891   | 99982   | 03635   | 99934   | 05379   | 99855   | 07121   | 99746   | 55 |
| 6  | 00175   | Unit.   | 01920   | 99982   | 03664   | 99933   | 05408   | 99854   | 07150   | 99744   | 54 |
| 7  | 00204   | Unit.   | 01949   | 99981   | 03693   | 99932   | 05437   | 99852   | 07179   | 99742   | 53 |
| 8  | 00233   | Unit.   | 01978   | 99980   | 03723   | 99931   | 05466   | 99851   | 07208   | 99740   | 52 |
| 9  | 00262   | Unit.   | 02007   | 99980   | 03752   | 99930   | 05495   | 99849   | 07237   | 99738   | 51 |
| 10 | 00291   | Unit.   | 02036   | 99979   | 03781   | 99929   | 05524   | 99847   | 07266   | 99736   | 50 |
| 11 | 00320   | 99999   | 02065   | 99979   | 03810   | 99927   | 05553   | 99846   | 07295   | 99734   | 49 |
| 12 | 00349   | 99999   | 02094   | 99978   | 03839   | 99926   | 05582   | 99844   | 07324   | 99731   | 48 |
| 13 | 00378   | 99999   | 02123   | 99977   | 03868   | 99925   | 05611   | 99842   | 07353   | 99729   | 47 |
| 14 | 00407   | 99999   | 02152   | 99977   | 03897   | 99924   | 05640   | 99841   | 07382   | 99727   | 46 |
| 15 | 00436   | 99999   | 02181   | 99976   | 03926   | 99923   | 05669   | 99839   | 07411   | 99725   | 45 |
| 16 | 00465   | 99999   | 02211   | 99976   | 03955   | 99922   | 05698   | 99838   | 07440   | 99723   | 44 |
| 17 | 00494   | 99999   | 02240   | 99975   | 03984   | 99921   | 05727   | 99836   | 07469   | 99721   | 43 |
| 18 | 00524   | 99999   | 02269   | 99974   | 04013   | 99919   | 05756   | 99834   | 07498   | 99719   | 42 |
| 19 | 00553   | 99998   | 02298   | 99974   | 04042   | 99918   | 05785   | 99833   | 07527   | 99716   | 41 |
| 20 | 00582   | 99998   | 02327   | 99973   | 04071   | 99917   | 05814   | 99831   | 07556   | 99714   | 40 |
| 21 | 00611   | 99998   | 02356   | 99972   | 04100   | 99916   | 05844   | 99829   | 07585   | 99712   | 39 |
| 22 | 00640   | 99998   | 02385   | 99972   | 04129   | 99915   | 05873   | 99827   | 07614   | 99710   | 38 |
| 23 | 00669   | 99998   | 02414   | 99971   | 04159   | 99913   | 05902   | 99826   | 07643   | 99708   | 37 |
| 24 | 00698   | 99998   | 02443   | 99970   | 04188   | 99912   | 05931   | 99824   | 07672   | 99705   | 36 |
| 25 | 00727   | 99997   | 02472   | 99969   | 04217   | 99911   | 05960   | 99822   | 07701   | 99703   | 35 |
| 26 | 00756   | 99997   | 02501   | 99969   | 04246   | 99910   | 05989   | 99821   | 07730   | 99701   | 34 |
| 27 | 00785   | 99997   | 02530   | 99968   | 04275   | 99909   | 06018   | 99819   | 07759   | 99699   | 33 |
| 28 | 00814   | 99997   | 02560   | 99967   | 04304   | 99907   | 06047   | 99817   | 07788   | 99696   | 32 |
| 29 | 00844   | 99996   | 02589   | 99966   | 04333   | 99906   | 06076   | 99815   | 07817   | 99694   | 31 |
| 30 | 00873   | 99996   | 02618   | 99966   | 04362   | 99905   | 06105   | 99813   | 07846   | 99692   | 30 |
| 31 | 00902   | 99996   | 02647   | 99965   | 04391   | 99904   | 06134   | 99812   | 07875   | 99689   | 29 |
| 32 | 00931   | 99996   | 02676   | 99964   | 04420   | 99902   | 06163   | 99810   | 07904   | 99687   | 28 |
| 33 | 00960   | 99995   | 02705   | 99963   | 04449   | 99901   | 06192   | 99808   | 07933   | 99685   | 27 |
| 34 | 00989   | 99995   | 02734   | 99963   | 04478   | 99900   | 06221   | 99806   | 07962   | 99683   | 26 |
| 35 | 01018   | 99995   | 02763   | 99962   | 04507   | 99898   | 06250   | 99804   | 07991   | 99680   | 25 |
| 36 | 01047   | 99995   | 02792   | 99961   | 04536   | 99897   | 06279   | 99803   | 08020   | 99678   | 24 |
| 37 | 01076   | 99994   | 02821   | 99960   | 04565   | 99896   | 06308   | 99801   | 08049   | 99676   | 23 |
| 38 | 01105   | 99994   | 02850   | 99959   | 04594   | 99894   | 06337   | 99799   | 08078   | 99673   | 22 |
| 39 | 01134   | 99994   | 02879   | 99959   | 04623   | 99893   | 06366   | 99797   | 08107   | 99671   | 21 |
| 40 | 01164   | 99993   | 02908   | 99958   | 04653   | 99892   | 06395   | 99795   | 08136   | 99668   | 20 |
| 41 | 01193   | 99993   | 02938   | 99957   | 04682   | 99890   | 06424   | 99793   | 08165   | 99666   | 19 |
| 42 | 01222   | 99993   | 02967   | 99956   | 04711   | 99889   | 06453   | 99792   | 08194   | 99664   | 18 |
| 43 | 01251   | 99992   | 02996   | 99955   | 04740   | 99888   | 06482   | 99790   | 08223   | 99661   | 17 |
| 44 | 01280   | 99992   | 03025   | 99954   | 04769   | 99886   | 06511   | 99788   | 08252   | 99659   | 16 |
| 45 | 01309   | 99991   | 03054   | 99953   | 04798   | 99885   | 06540   | 99786   | 08281   | 99657   | 15 |
| 46 | 01338   | 99991   | 03083   | 99952   | 04827   | 99883   | 06569   | 99784   | 08310   | 99654   | 14 |
| 47 | 01367   | 99991   | 03112   | 99952   | 04856   | 99882   | 06598   | 99782   | 08339   | 99652   | 13 |
| 48 | 01396   | 99990   | 03141   | 99951   | 04885   | 99881   | 06627   | 99780   | 08368   | 99649   | 12 |
| 49 | 01425   | 99990   | 03170   | 99950   | 04914   | 99879   | 06656   | 99778   | 08397   | 99647   | 11 |
| 50 | 01454   | 99989   | 03199   | 99949   | 04943   | 99878   | 06685   | 99776   | 08426   | 99644   | 10 |
| 51 | 01483   | 99989   | 03228   | 99948   | 04972   | 99876   | 06714   | 99774   | 08455   | 99642   | 9  |
| 52 | 01513   | 99989   | 03257   | 99947   | 05001   | 99875   | 06743   | 99772   | 08484   | 99639   | 8  |
| 53 | 01542   | 99988   | 03286   | 99946   | 05030   | 99873   | 06773   | 99770   | 08513   | 99637   | 7  |
| 54 | 01571   | 99988   | 03316   | 99945   | 05059   | 99872   | 06802   | 99768   | 08542   | 99635   | 6  |
| 55 | 01600   | 99987   | 03345   | 99944   | 05088   | 99870   | 06831   | 99766   | 08571   | 99632   | 5  |
| 56 | 01629   | 99987   | 03374   | 99943   | 05117   | 99869   | 06860   | 99764   | 08600   | 99630   | 4  |
| 57 | 01658   | 99986   | 03403   | 99942   | 05146   | 99867   | 06889   | 99762   | 08629   | 99627   | 3  |
| 58 | 01687   | 99986   | 03432   | 99941   | 05175   | 99866   | 06918   | 99760   | 08658   | 99625   | 2  |
| 59 | 01716   | 99985   | 03461   | 99940   | 05205   | 99864   | 06947   | 99758   | 08687   | 99622   | 1  |
| 60 | 01745   | 99985   | 03490   | 99939   | 05234   | 99863   | 06976   | 99756   | 08716   | 99619   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 89°     |         | 88°     |         | 87°     |         | 86°     |         | 85°     |         |    |

TABLE III. NATURAL SINES AND COSINES.

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| °  | 5°      |        | 6°      |        | 7°      |        | 8°      |        | 9°      |        | °  |
|----|---------|--------|---------|--------|---------|--------|---------|--------|---------|--------|----|
|    | Sine    | Cosine | Sine    | Cosine | Sine    | Cosine | Sine    | Cosine | Sine    | Cosine |    |
| 0  | 08716   | 99619  | 10453   | 99452  | 12187   | 99255  | 13917   | 99027  | 15643   | 98769  | 60 |
| 1  | 08745   | 99617  | 10482   | 99449  | 12216   | 99251  | 13946   | 99023  | 15672   | 98764  | 59 |
| 2  | 08774   | 99614  | 10511   | 99446  | 12245   | 99248  | 13975   | 99019  | 15701   | 98760  | 58 |
| 3  | 08803   | 99612  | 10540   | 99443  | 12274   | 99244  | 14004   | 99015  | 15730   | 98755  | 57 |
| 4  | 08831   | 99609  | 10569   | 99440  | 12302   | 99240  | 14033   | 99011  | 15758   | 98751  | 56 |
| 5  | 08860   | 99607  | 10597   | 99437  | 12331   | 99237  | 14061   | 99006  | 15787   | 98746  | 55 |
| 6  | 08889   | 99604  | 10626   | 99434  | 12360   | 99233  | 14090   | 99002  | 15816   | 98741  | 54 |
| 7  | 08918   | 99602  | 10655   | 99431  | 12389   | 99230  | 14119   | 98998  | 15845   | 98737  | 53 |
| 8  | 08947   | 99599  | 10684   | 99428  | 12418   | 99226  | 14148   | 98994  | 15873   | 98732  | 52 |
| 9  | 08976   | 99596  | 10713   | 99424  | 12447   | 99222  | 14177   | 98990  | 15902   | 98728  | 51 |
| 10 | 09005   | 99594  | 10742   | 99421  | 12476   | 99219  | 14205   | 98986  | 15931   | 98723  | 50 |
| 11 | 09034   | 99591  | 10771   | 99418  | 12504   | 99215  | 14234   | 98982  | 15960   | 98718  | 49 |
| 12 | 09063   | 99588  | 10800   | 99415  | 12533   | 99211  | 14263   | 98978  | 15988   | 98714  | 48 |
| 13 | 09092   | 99586  | 10829   | 99412  | 12562   | 99208  | 14292   | 98973  | 16017   | 98709  | 47 |
| 14 | 09121   | 99583  | 10858   | 99409  | 12591   | 99204  | 14320   | 98969  | 16046   | 98704  | 46 |
| 15 | 09150   | 99580  | 10887   | 99406  | 12620   | 99200  | 14349   | 98965  | 16074   | 98700  | 45 |
| 16 | 09179   | 99578  | 10916   | 99402  | 12649   | 99197  | 14378   | 98961  | 16103   | 98695  | 44 |
| 17 | 09208   | 99575  | 10945   | 99399  | 12678   | 99193  | 14407   | 98957  | 16132   | 98690  | 43 |
| 18 | 09237   | 99572  | 10973   | 99396  | 12706   | 99189  | 14436   | 98953  | 16160   | 98686  | 42 |
| 19 | 09266   | 99570  | 11002   | 99393  | 12735   | 99186  | 14464   | 98948  | 16189   | 98681  | 41 |
| 20 | 09295   | 99567  | 11031   | 99390  | 12764   | 99182  | 14493   | 98944  | 16218   | 98676  | 40 |
| 21 | 09324   | 99564  | 11060   | 99386  | 12793   | 99178  | 14522   | 98940  | 16246   | 98671  | 39 |
| 22 | 09353   | 99562  | 11089   | 99383  | 12822   | 99175  | 14551   | 98936  | 16275   | 98667  | 38 |
| 23 | 09382   | 99559  | 11118   | 99380  | 12851   | 99171  | 14580   | 98931  | 16304   | 98662  | 37 |
| 24 | 09411   | 99556  | 11147   | 99377  | 12880   | 99167  | 14608   | 98927  | 16333   | 98657  | 36 |
| 25 | 09440   | 99553  | 11176   | 99374  | 12908   | 99163  | 14637   | 98923  | 16361   | 98652  | 35 |
| 26 | 09469   | 99551  | 11205   | 99370  | 12937   | 99160  | 14666   | 98919  | 16390   | 98648  | 34 |
| 27 | 09498   | 99548  | 11234   | 99367  | 12966   | 99156  | 14695   | 98914  | 16419   | 98643  | 33 |
| 28 | 09527   | 99545  | 11263   | 99364  | 12995   | 99152  | 14723   | 98910  | 16447   | 98638  | 32 |
| 29 | 09556   | 99542  | 11291   | 99360  | 13024   | 99148  | 14752   | 98906  | 16476   | 98633  | 31 |
| 30 | 09585   | 99540  | 11320   | 99357  | 13053   | 99144  | 14781   | 98902  | 16505   | 98629  | 30 |
| 31 | 09614   | 99537  | 11349   | 99354  | 13081   | 99141  | 14810   | 98897  | 16533   | 98624  | 29 |
| 32 | 09642   | 99534  | 11378   | 99351  | 13110   | 99137  | 14838   | 98893  | 16562   | 98619  | 28 |
| 33 | 09671   | 99531  | 11407   | 99347  | 13139   | 99133  | 14867   | 98889  | 16591   | 98614  | 27 |
| 34 | 09700   | 99528  | 11436   | 99344  | 13168   | 99129  | 14896   | 98884  | 16620   | 98609  | 26 |
| 35 | 09729   | 99526  | 11465   | 99341  | 13197   | 99125  | 14925   | 98880  | 16648   | 98604  | 25 |
| 36 | 09758   | 99523  | 11494   | 99337  | 13226   | 99122  | 14954   | 98876  | 16677   | 98600  | 24 |
| 37 | 09787   | 99520  | 11523   | 99334  | 13254   | 99118  | 14982   | 98871  | 16706   | 98595  | 23 |
| 38 | 09816   | 99517  | 11552   | 99331  | 13283   | 99114  | 15011   | 98867  | 16734   | 98590  | 22 |
| 39 | 09845   | 99514  | 11580   | 99327  | 13312   | 99110  | 15040   | 98863  | 16763   | 98585  | 21 |
| 40 | 09874   | 99511  | 11609   | 99324  | 13341   | 99106  | 15069   | 98858  | 16792   | 98580  | 20 |
| 41 | 09903   | 99508  | 11638   | 99320  | 13370   | 99102  | 15097   | 98854  | 16820   | 98575  | 19 |
| 42 | 09932   | 99506  | 11667   | 99317  | 13399   | 99098  | 15126   | 98849  | 16849   | 98570  | 18 |
| 43 | 09961   | 99503  | 11696   | 99314  | 13427   | 99094  | 15155   | 98845  | 16878   | 98565  | 17 |
| 44 | 09990   | 99500  | 11725   | 99310  | 13456   | 99091  | 15184   | 98841  | 16906   | 98561  | 16 |
| 45 | 10019   | 99497  | 11754   | 99307  | 13485   | 99087  | 15212   | 98836  | 16935   | 98556  | 15 |
| 46 | 10048   | 99494  | 11783   | 99303  | 13514   | 99083  | 15241   | 98832  | 16964   | 98551  | 14 |
| 47 | 10077   | 99491  | 11812   | 99300  | 13543   | 99079  | 15270   | 98827  | 16992   | 98546  | 13 |
| 48 | 10106   | 99488  | 11840   | 99297  | 13572   | 99075  | 15299   | 98823  | 17021   | 98541  | 12 |
| 49 | 10135   | 99485  | 11869   | 99293  | 13600   | 99071  | 15327   | 98818  | 17050   | 98536  | 11 |
| 50 | 10164   | 99482  | 11898   | 99290  | 13629   | 99067  | 15356   | 98814  | 17078   | 98531  | 10 |
| 51 | 10192   | 99479  | 11927   | 99286  | 13658   | 99063  | 15385   | 98809  | 17107   | 98526  | 9  |
| 52 | 10221   | 99476  | 11956   | 99283  | 13687   | 99059  | 15414   | 98805  | 17136   | 98521  | 8  |
| 53 | 10250   | 99473  | 11985   | 99279  | 13716   | 99055  | 15442   | 98800  | 17164   | 98516  | 7  |
| 54 | 10279   | 99470  | 12014   | 99276  | 13744   | 99051  | 15471   | 98796  | 17193   | 98511  | 6  |
| 55 | 10308   | 99467  | 12043   | 99272  | 13773   | 99047  | 15500   | 98791  | 17222   | 98506  | 5  |
| 56 | 10337   | 99464  | 12071   | 99269  | 13802   | 99043  | 15529   | 98787  | 17250   | 98501  | 4  |
| 57 | 10366   | 99461  | 12100   | 99265  | 13831   | 99039  | 15557   | 98782  | 17279   | 98496  | 3  |
| 58 | 10395   | 99458  | 12129   | 99262  | 13860   | 99035  | 15586   | 98778  | 17308   | 98491  | 2  |
| 59 | 10424   | 99455  | 12158   | 99258  | 13889   | 99031  | 15615   | 98773  | 17336   | 98486  | 1  |
| 60 | 10453   | 99452  | 12187   | 99255  | 13917   | 99027  | 15643   | 98769  | 17365   | 98481  | 0  |
|    | Cosine. | Sine.  | Cosine. | Sine.  | Cosine. | Sine.  | Cosine. | Sine.  | Cosine. | Sine.  |    |
|    | 84°     |        | 88°     |        | 82°     |        | 81°     |        | 80°     |        |    |

| °  | 0°      |         | 1°      |         | 2°      |         | 3°      |         | 4°      |         | °  |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 00000   | Unit.   | 01745   | 99985   | 03490   | 99939   | 05234   | 99863   | 06976   | 99756   | 60 |
| 1  | 00029   | Unit.   | 01774   | 99984   | 03519   | 99938   | 05263   | 99861   | 07005   | 99754   | 59 |
| 2  | 00058   | Unit.   | 01803   | 99984   | 03548   | 99937   | 05292   | 99860   | 07034   | 99752   | 58 |
| 3  | 00087   | Unit.   | 01832   | 99983   | 03577   | 99936   | 05321   | 99858   | 07063   | 99750   | 57 |
| 4  | 00116   | Unit.   | 01862   | 99983   | 03606   | 99935   | 05350   | 99857   | 07092   | 99748   | 56 |
| 5  | 00145   | Unit.   | 01891   | 99982   | 03635   | 99934   | 05379   | 99855   | 07121   | 99746   | 55 |
| 6  | 00175   | Unit.   | 01920   | 99982   | 03664   | 99933   | 05408   | 99854   | 07150   | 99744   | 54 |
| 7  | 00204   | Unit.   | 01949   | 99981   | 03693   | 99932   | 05437   | 99852   | 07179   | 99742   | 53 |
| 8  | 00233   | Unit.   | 01978   | 99980   | 03723   | 99931   | 05466   | 99851   | 07208   | 99740   | 52 |
| 9  | 00262   | Unit.   | 02007   | 99980   | 03752   | 99930   | 05495   | 99849   | 07237   | 99738   | 51 |
| 10 | 00291   | Unit.   | 02036   | 99979   | 03781   | 99929   | 05524   | 99847   | 07266   | 99736   | 50 |
| 11 | 00320   | 99999   | 02065   | 99979   | 03810   | 99927   | 05553   | 99846   | 07295   | 99734   | 49 |
| 12 | 00349   | 99999   | 02094   | 99978   | 03839   | 99926   | 05582   | 99844   | 07324   | 99731   | 48 |
| 13 | 00378   | 99999   | 02123   | 99977   | 03868   | 99925   | 05611   | 99842   | 07353   | 99729   | 47 |
| 14 | 00407   | 99999   | 02152   | 99977   | 03897   | 99924   | 05640   | 99841   | 07382   | 99727   | 46 |
| 15 | 00436   | 99999   | 02181   | 99976   | 03926   | 99923   | 05669   | 99839   | 07411   | 99725   | 45 |
| 16 | 00465   | 99999   | 02211   | 99976   | 03955   | 99922   | 05698   | 99838   | 07440   | 99723   | 44 |
| 17 | 00495   | 99999   | 02240   | 99975   | 03984   | 99921   | 05727   | 99836   | 07469   | 99721   | 43 |
| 18 | 00524   | 99999   | 02269   | 99974   | 04013   | 99919   | 05756   | 99834   | 07498   | 99719   | 42 |
| 19 | 00553   | 99998   | 02298   | 99974   | 04042   | 99918   | 05785   | 99833   | 07527   | 99716   | 41 |
| 20 | 00582   | 99998   | 02327   | 99973   | 04071   | 99917   | 05814   | 99831   | 07556   | 99714   | 40 |
| 21 | 00611   | 99998   | 02356   | 99972   | 04100   | 99916   | 05844   | 99829   | 07585   | 99712   | 39 |
| 22 | 00640   | 99998   | 02385   | 99972   | 04129   | 99915   | 05873   | 99827   | 07614   | 99710   | 38 |
| 23 | 00669   | 99998   | 02414   | 99971   | 04159   | 99913   | 05902   | 99826   | 07643   | 99708   | 37 |
| 24 | 00698   | 99998   | 02443   | 99970   | 04188   | 99912   | 05931   | 99824   | 07672   | 99705   | 36 |
| 25 | 00727   | 99997   | 02472   | 99969   | 04217   | 99911   | 05960   | 99822   | 07701   | 99703   | 35 |
| 26 | 00756   | 99997   | 02501   | 99969   | 04246   | 99910   | 05989   | 99821   | 07730   | 99701   | 34 |
| 27 | 00785   | 99997   | 02530   | 99968   | 04275   | 99909   | 06018   | 99819   | 07759   | 99699   | 33 |
| 28 | 00814   | 99997   | 02560   | 99967   | 04304   | 99907   | 06047   | 99817   | 07788   | 99696   | 32 |
| 29 | 00844   | 99996   | 02589   | 99966   | 04333   | 99906   | 06076   | 99815   | 07817   | 99694   | 31 |
| 30 | 00873   | 99996   | 02618   | 99966   | 04362   | 99905   | 06105   | 99813   | 07846   | 99692   | 30 |
| 31 | 00902   | 99996   | 02647   | 99965   | 04391   | 99904   | 06134   | 99812   | 07875   | 99689   | 29 |
| 32 | 00931   | 99995   | 02676   | 99964   | 04420   | 99902   | 06163   | 99810   | 07904   | 99687   | 28 |
| 33 | 00960   | 99995   | 02705   | 99963   | 04449   | 99901   | 06192   | 99808   | 07933   | 99685   | 27 |
| 34 | 00989   | 99995   | 02734   | 99963   | 04478   | 99900   | 06221   | 99806   | 07962   | 99683   | 26 |
| 35 | 01018   | 99995   | 02763   | 99962   | 04507   | 99898   | 06250   | 99804   | 07991   | 99680   | 25 |
| 36 | 01047   | 99995   | 02792   | 99961   | 04536   | 99897   | 06279   | 99803   | 08020   | 99678   | 24 |
| 37 | 01076   | 99994   | 02821   | 99960   | 04565   | 99896   | 06308   | 99801   | 08049   | 99676   | 23 |
| 38 | 01105   | 99994   | 02850   | 99959   | 04594   | 99894   | 06337   | 99799   | 08078   | 99673   | 22 |
| 39 | 01134   | 99994   | 02879   | 99959   | 04623   | 99893   | 06366   | 99797   | 08107   | 99671   | 21 |
| 40 | 01164   | 99993   | 02908   | 99958   | 04653   | 99892   | 06395   | 99795   | 08136   | 99668   | 20 |
| 41 | 01193   | 99993   | 02938   | 99957   | 04682   | 99890   | 06424   | 99793   | 08165   | 99666   | 19 |
| 42 | 01222   | 99993   | 02967   | 99956   | 04711   | 99889   | 06453   | 99792   | 08194   | 99664   | 18 |
| 43 | 01251   | 99992   | 02996   | 99955   | 04740   | 99888   | 06482   | 99790   | 08223   | 99661   | 17 |
| 44 | 01280   | 99992   | 03025   | 99954   | 04769   | 99886   | 06511   | 99788   | 08252   | 99659   | 16 |
| 45 | 01309   | 99991   | 03054   | 99953   | 04798   | 99885   | 06540   | 99786   | 08281   | 99657   | 15 |
| 46 | 01338   | 99991   | 03083   | 99952   | 04827   | 99883   | 06569   | 99784   | 08310   | 99654   | 14 |
| 47 | 01367   | 99991   | 03112   | 99952   | 04856   | 99882   | 06598   | 99782   | 08339   | 99652   | 13 |
| 48 | 01396   | 99990   | 03141   | 99951   | 04885   | 99881   | 06627   | 99780   | 08368   | 99649   | 12 |
| 49 | 01425   | 99990   | 03170   | 99950   | 04914   | 99879   | 06656   | 99778   | 08397   | 99647   | 11 |
| 50 | 01454   | 99989   | 03199   | 99949   | 04943   | 99878   | 06685   | 99776   | 08426   | 99644   | 10 |
| 51 | 01483   | 99989   | 03228   | 99948   | 04972   | 99876   | 06714   | 99774   | 08455   | 99642   | 9  |
| 52 | 01513   | 99989   | 03257   | 99947   | 05001   | 99875   | 06743   | 99772   | 08484   | 99639   | 8  |
| 53 | 01542   | 99988   | 03286   | 99946   | 05030   | 99873   | 06773   | 99770   | 08513   | 99637   | 7  |
| 54 | 01571   | 99988   | 03316   | 99945   | 05059   | 99872   | 06802   | 99768   | 08542   | 99635   | 6  |
| 55 | 01600   | 99987   | 03345   | 99944   | 05088   | 99870   | 06831   | 99766   | 08571   | 99632   | 5  |
| 56 | 01629   | 99987   | 03374   | 99943   | 05117   | 99869   | 06860   | 99764   | 08600   | 99630   | 4  |
| 57 | 01658   | 99986   | 03403   | 99942   | 05146   | 99867   | 06889   | 99762   | 08629   | 99627   | 3  |
| 58 | 01687   | 99986   | 03432   | 99941   | 05175   | 99866   | 06918   | 99760   | 08658   | 99625   | 2  |
| 59 | 01716   | 99985   | 03461   | 99940   | 05205   | 99864   | 06947   | 99758   | 08687   | 99622   | 1  |
| 60 | 01745   | 99985   | 03490   | 99939   | 05234   | 99863   | 06976   | 99756   | 08716   | 99619   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 89°     |         | 88°     |         | 87°     |         | 86°     |         | 85°     |         |    |

TABLE III. NATURAL SINES AND COSINES.

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| °  | 5°      |        | 6°      |        | 7°      |        | 8°      |        | 9°      |        | °  |
|----|---------|--------|---------|--------|---------|--------|---------|--------|---------|--------|----|
|    | Sine    | Cosine | Sine    | Cosine | Sine    | Cosine | Sine    | Cosine | Sine    | Cosine |    |
| 0  | 08716   | 99619  | 10453   | 99452  | 12187   | 99255  | 13917   | 99027  | 15643   | 98796  | 60 |
| 1  | 08745   | 99617  | 10482   | 99449  | 12216   | 99251  | 13946   | 99023  | 15672   | 98764  | 59 |
| 2  | 08774   | 99614  | 10511   | 99446  | 12245   | 99248  | 13975   | 99019  | 15701   | 98760  | 58 |
| 3  | 08803   | 99612  | 10540   | 99443  | 12274   | 99244  | 14004   | 99015  | 15730   | 98755  | 57 |
| 4  | 08831   | 99609  | 10569   | 99440  | 12302   | 99240  | 14033   | 99011  | 15758   | 98751  | 56 |
| 5  | 08860   | 99607  | 10597   | 99437  | 12331   | 99237  | 14061   | 99006  | 15787   | 98746  | 55 |
| 6  | 08889   | 99604  | 10626   | 99434  | 12360   | 99233  | 14090   | 99002  | 15816   | 98741  | 54 |
| 7  | 08918   | 99602  | 10655   | 99431  | 12389   | 99230  | 14119   | 98998  | 15845   | 98737  | 53 |
| 8  | 08947   | 99599  | 10684   | 99428  | 12418   | 99226  | 14148   | 98994  | 15873   | 98732  | 52 |
| 9  | 08976   | 99596  | 10713   | 99424  | 12447   | 99222  | 14177   | 98990  | 15902   | 98728  | 51 |
| 10 | 09005   | 99594  | 10742   | 99421  | 12476   | 99219  | 14205   | 98986  | 15931   | 98723  | 50 |
| 11 | 09034   | 99591  | 10771   | 99418  | 12504   | 99215  | 14234   | 98982  | 15959   | 98718  | 49 |
| 12 | 09063   | 99588  | 10800   | 99415  | 12533   | 99211  | 14263   | 98978  | 15988   | 98714  | 48 |
| 13 | 09092   | 99586  | 10829   | 99412  | 12562   | 99208  | 14292   | 98973  | 16017   | 98709  | 47 |
| 14 | 09121   | 99583  | 10858   | 99409  | 12591   | 99204  | 14320   | 98969  | 16046   | 98704  | 46 |
| 15 | 09150   | 99580  | 10887   | 99406  | 12620   | 99200  | 14349   | 98965  | 16074   | 98700  | 45 |
| 16 | 09179   | 99578  | 10916   | 99402  | 12649   | 99197  | 14378   | 98961  | 16103   | 98695  | 44 |
| 17 | 09208   | 99575  | 10945   | 99399  | 12678   | 99193  | 14407   | 98957  | 16132   | 98690  | 43 |
| 18 | 09237   | 99572  | 10973   | 99396  | 12706   | 99189  | 14436   | 98953  | 16160   | 98686  | 42 |
| 19 | 09266   | 99570  | 11002   | 99393  | 12735   | 99186  | 14464   | 98948  | 16189   | 98681  | 41 |
| 20 | 09295   | 99567  | 11031   | 99390  | 12764   | 99182  | 14493   | 98944  | 16218   | 98676  | 40 |
| 21 | 09324   | 99564  | 11060   | 99386  | 12793   | 99178  | 14522   | 98940  | 16246   | 98671  | 39 |
| 22 | 09353   | 99562  | 11089   | 99383  | 12822   | 99175  | 14551   | 98936  | 16275   | 98667  | 38 |
| 23 | 09382   | 99559  | 11118   | 99380  | 12851   | 99171  | 14580   | 98931  | 16304   | 98662  | 37 |
| 24 | 09411   | 99556  | 11147   | 99377  | 12880   | 99167  | 14608   | 98927  | 16333   | 98657  | 36 |
| 25 | 09440   | 99553  | 11176   | 99374  | 12908   | 99163  | 14637   | 98923  | 16361   | 98652  | 35 |
| 26 | 09469   | 99551  | 11205   | 99370  | 12937   | 99160  | 14666   | 98919  | 16390   | 98648  | 34 |
| 27 | 09498   | 99548  | 11234   | 99367  | 12966   | 99156  | 14695   | 98914  | 16419   | 98643  | 33 |
| 28 | 09527   | 99545  | 11263   | 99364  | 12995   | 99152  | 14723   | 98910  | 16447   | 98638  | 32 |
| 29 | 09556   | 99542  | 11291   | 99360  | 13024   | 99148  | 14752   | 98906  | 16476   | 98633  | 31 |
| 30 | 09585   | 99540  | 11320   | 99357  | 13053   | 99144  | 14781   | 98902  | 16505   | 98629  | 30 |
| 31 | 09614   | 99537  | 11349   | 99354  | 13081   | 99141  | 14810   | 98897  | 16533   | 98624  | 29 |
| 32 | 09642   | 99534  | 11378   | 99351  | 13110   | 99137  | 14838   | 98893  | 16562   | 98619  | 28 |
| 33 | 09671   | 99531  | 11407   | 99347  | 13139   | 99133  | 14867   | 98889  | 16591   | 98614  | 27 |
| 34 | 09700   | 99528  | 11436   | 99344  | 13168   | 99129  | 14896   | 98884  | 16620   | 98609  | 26 |
| 35 | 09729   | 99526  | 11465   | 99341  | 13197   | 99125  | 14925   | 98880  | 16648   | 98604  | 25 |
| 36 | 09758   | 99523  | 11494   | 99337  | 13226   | 99122  | 14954   | 98876  | 16677   | 98600  | 24 |
| 37 | 09787   | 99520  | 11523   | 99334  | 13254   | 99118  | 14982   | 98871  | 16706   | 98595  | 23 |
| 38 | 09816   | 99517  | 11552   | 99331  | 13283   | 99114  | 15011   | 98867  | 16734   | 98590  | 22 |
| 39 | 09845   | 99514  | 11580   | 99327  | 13312   | 99110  | 15040   | 98863  | 16763   | 98585  | 21 |
| 40 | 09874   | 99511  | 11609   | 99324  | 13341   | 99106  | 15069   | 98858  | 16792   | 98580  | 20 |
| 41 | 09903   | 99508  | 11638   | 99320  | 13370   | 99102  | 15097   | 98854  | 16820   | 98575  | 19 |
| 42 | 09932   | 99506  | 11667   | 99317  | 13399   | 99098  | 15126   | 98849  | 16849   | 98570  | 18 |
| 43 | 09961   | 99503  | 11696   | 99314  | 13427   | 99094  | 15155   | 98845  | 16878   | 98565  | 17 |
| 44 | 09990   | 99500  | 11725   | 99310  | 13456   | 99091  | 15184   | 98841  | 16906   | 98561  | 16 |
| 45 | 10019   | 99497  | 11754   | 99307  | 13485   | 99087  | 15212   | 98836  | 16935   | 98556  | 15 |
| 46 | 10048   | 99494  | 11783   | 99303  | 13514   | 99083  | 15241   | 98832  | 16964   | 98551  | 14 |
| 47 | 10077   | 99491  | 11812   | 99300  | 13543   | 99079  | 15270   | 98827  | 16992   | 98546  | 13 |
| 48 | 10106   | 99488  | 11840   | 99297  | 13572   | 99075  | 15299   | 98823  | 17021   | 98541  | 12 |
| 49 | 10135   | 99485  | 11869   | 99293  | 13600   | 99071  | 15327   | 98818  | 17050   | 98536  | 11 |
| 50 | 10164   | 99482  | 11898   | 99290  | 13629   | 99067  | 15356   | 98814  | 17078   | 98531  | 10 |
| 51 | 10192   | 99479  | 11927   | 99286  | 13658   | 99063  | 15385   | 98809  | 17107   | 98526  | 9  |
| 52 | 10221   | 99476  | 11956   | 99283  | 13687   | 99059  | 15414   | 98805  | 17136   | 98521  | 8  |
| 53 | 10250   | 99473  | 11985   | 99279  | 13716   | 99055  | 15442   | 98800  | 17164   | 98516  | 7  |
| 54 | 10279   | 99470  | 12014   | 99276  | 13744   | 99051  | 15471   | 98796  | 17193   | 98511  | 6  |
| 55 | 10308   | 99467  | 12043   | 99272  | 13773   | 99047  | 15500   | 98791  | 17222   | 98506  | 5  |
| 56 | 10337   | 99464  | 12071   | 99269  | 13802   | 99043  | 15529   | 98787  | 17250   | 98501  | 4  |
| 57 | 10366   | 99461  | 12100   | 99265  | 13831   | 99039  | 15557   | 98782  | 17279   | 98496  | 3  |
| 58 | 10395   | 99458  | 12129   | 99262  | 13860   | 99035  | 15586   | 98778  | 17308   | 98491  | 2  |
| 59 | 10424   | 99455  | 12158   | 99258  | 13889   | 99031  | 15615   | 98773  | 17336   | 98486  | 1  |
| 60 | 10453   | 99452  | 12187   | 99255  | 13917   | 99027  | 15643   | 98769  | 17365   | 98481  | 0  |
|    | Cosine. | Sine.  | Cosine. | Sine.  | Cosine. | Sine.  | Cosine. | Sine.  | Cosine. | Sine.  |    |
|    | 84°     |        | 88°     |        | 82°     |        | 81°     |        | 80°     |        |    |

|    | 10°     |         | 11°     |         | 12°     |         | 13°     |         | 14°     |         |    |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 17365   | 98481   | 19081   | 98163   | 20791   | 97815   | 22495   | 97437   | 24192   | 97030   | 60 |
| 1  | 17393   | 98476   | 19109   | 98157   | 20820   | 97809   | 22523   | 97430   | 24220   | 97023   | 59 |
| 2  | 17422   | 98471   | 19136   | 98152   | 20848   | 97803   | 22552   | 97424   | 24249   | 97015   | 58 |
| 3  | 17451   | 98466   | 19167   | 98146   | 20877   | 97797   | 22580   | 97417   | 24277   | 97008   | 57 |
| 4  | 17479   | 98461   | 19195   | 98140   | 20905   | 97791   | 22608   | 97411   | 24305   | 97001   | 56 |
| 5  | 17508   | 98455   | 19224   | 98135   | 20933   | 97784   | 22637   | 97404   | 24333   | 96994   | 55 |
| 6  | 17537   | 98450   | 19252   | 98129   | 20962   | 97778   | 22665   | 97398   | 24362   | 96987   | 54 |
| 7  | 17565   | 98445   | 19281   | 98124   | 20990   | 97772   | 22693   | 97391   | 24390   | 96980   | 53 |
| 8  | 17594   | 98440   | 19309   | 98118   | 21019   | 97766   | 22722   | 97384   | 24418   | 96973   | 52 |
| 9  | 17623   | 98435   | 19338   | 98112   | 21047   | 97760   | 22750   | 97378   | 24446   | 96966   | 51 |
| 10 | 17651   | 98430   | 19366   | 98107   | 21076   | 97754   | 22778   | 97371   | 24474   | 96959   | 50 |
| 11 | 17680   | 98425   | 19395   | 98101   | 21104   | 97748   | 22807   | 97365   | 24503   | 96952   | 49 |
| 12 | 17708   | 98420   | 19423   | 98096   | 21132   | 97742   | 22835   | 97358   | 24531   | 96945   | 48 |
| 13 | 17737   | 98414   | 19452   | 98090   | 21161   | 97735   | 22863   | 97351   | 24559   | 96937   | 47 |
| 14 | 17766   | 98409   | 19481   | 98084   | 21189   | 97729   | 22892   | 97345   | 24587   | 96930   | 46 |
| 15 | 17794   | 98404   | 19509   | 98079   | 21218   | 97723   | 22920   | 97338   | 24615   | 96923   | 45 |
| 16 | 17823   | 98399   | 19538   | 98073   | 21246   | 97717   | 22948   | 97331   | 24644   | 96916   | 44 |
| 17 | 17852   | 98394   | 19566   | 98067   | 21275   | 97711   | 22977   | 97325   | 24672   | 96909   | 43 |
| 18 | 17880   | 98389   | 19595   | 98061   | 21303   | 97705   | 23005   | 97318   | 24700   | 96902   | 42 |
| 19 | 17909   | 98383   | 19623   | 98056   | 21331   | 97698   | 23033   | 97311   | 24728   | 96894   | 41 |
| 20 | 17937   | 98378   | 19652   | 98050   | 21360   | 97692   | 23062   | 97304   | 24756   | 96887   | 40 |
| 21 | 17966   | 98373   | 19680   | 98044   | 21388   | 97686   | 23090   | 97298   | 24784   | 96880   | 39 |
| 22 | 17995   | 98368   | 19709   | 98039   | 21417   | 97680   | 23118   | 97291   | 24813   | 96873   | 38 |
| 23 | 18023   | 98362   | 19737   | 98033   | 21445   | 97673   | 23146   | 97284   | 24841   | 96866   | 37 |
| 24 | 18052   | 98357   | 19766   | 98027   | 21474   | 97667   | 23175   | 97278   | 24869   | 96858   | 36 |
| 25 | 18081   | 98352   | 19794   | 98021   | 21502   | 97661   | 23203   | 97271   | 24897   | 96851   | 35 |
| 26 | 18109   | 98347   | 19823   | 98016   | 21530   | 97655   | 23231   | 97264   | 24925   | 96844   | 34 |
| 27 | 18138   | 98341   | 19851   | 98010   | 21559   | 97648   | 23260   | 97257   | 24954   | 96837   | 33 |
| 28 | 18166   | 98336   | 19880   | 98004   | 21587   | 97642   | 23288   | 97251   | 24982   | 96829   | 32 |
| 29 | 18195   | 98331   | 19908   | 97998   | 21616   | 97636   | 23316   | 97244   | 25010   | 96822   | 31 |
| 30 | 18224   | 98325   | 19937   | 97992   | 21644   | 97630   | 23345   | 97237   | 25038   | 96815   | 30 |
| 31 | 18252   | 98320   | 19965   | 97987   | 21672   | 97623   | 23373   | 97230   | 25066   | 96807   | 29 |
| 32 | 18281   | 98315   | 19994   | 97981   | 21701   | 97617   | 23401   | 97223   | 25094   | 96800   | 28 |
| 33 | 18309   | 98310   | 20022   | 97975   | 21729   | 97611   | 23429   | 97217   | 25122   | 96793   | 27 |
| 34 | 18338   | 98304   | 20051   | 97969   | 21758   | 97604   | 23458   | 97210   | 25151   | 96786   | 26 |
| 35 | 18367   | 98299   | 20079   | 97963   | 21786   | 97598   | 23486   | 97203   | 25179   | 96778   | 25 |
| 36 | 18395   | 98294   | 20108   | 97958   | 21814   | 97592   | 23514   | 97196   | 25207   | 96771   | 24 |
| 37 | 18424   | 98288   | 20136   | 97952   | 21843   | 97585   | 23542   | 97189   | 25235   | 96764   | 23 |
| 38 | 18452   | 98283   | 20165   | 97946   | 21871   | 97579   | 23571   | 97182   | 25263   | 96756   | 22 |
| 39 | 18481   | 98277   | 20193   | 97940   | 21899   | 97573   | 23599   | 97176   | 25291   | 96749   | 21 |
| 40 | 18509   | 98272   | 20222   | 97934   | 21928   | 97566   | 23627   | 97169   | 25320   | 96742   | 20 |
| 41 | 18538   | 98267   | 20250   | 97928   | 21956   | 97560   | 23656   | 97162   | 25348   | 96734   | 19 |
| 42 | 18567   | 98261   | 20279   | 97922   | 21985   | 97553   | 23684   | 97155   | 25376   | 96727   | 18 |
| 43 | 18595   | 98255   | 20307   | 97916   | 22013   | 97547   | 23712   | 97148   | 25404   | 96719   | 17 |
| 44 | 18624   | 98250   | 20336   | 97910   | 22041   | 97541   | 23740   | 97141   | 25432   | 96712   | 16 |
| 45 | 18652   | 98245   | 20364   | 97905   | 22070   | 97534   | 23769   | 97134   | 25460   | 96705   | 15 |
| 46 | 18681   | 98240   | 20393   | 97899   | 22098   | 97528   | 23797   | 97127   | 25488   | 96697   | 14 |
| 47 | 18710   | 98234   | 20421   | 97893   | 22126   | 97521   | 23825   | 97120   | 25516   | 96690   | 13 |
| 48 | 18738   | 98229   | 20450   | 97887   | 22155   | 97515   | 23853   | 97113   | 25545   | 96682   | 12 |
| 49 | 18767   | 98223   | 20478   | 97881   | 22183   | 97508   | 23882   | 97106   | 25573   | 96675   | 11 |
| 50 | 18795   | 98218   | 20507   | 97875   | 22212   | 97502   | 23910   | 97100   | 25601   | 96667   | 10 |
| 51 | 18824   | 98212   | 20535   | 97869   | 22240   | 97496   | 23938   | 97093   | 25629   | 96660   | 9  |
| 52 | 18852   | 98207   | 20563   | 97863   | 22268   | 97489   | 23966   | 97086   | 25657   | 96653   | 8  |
| 53 | 18881   | 98201   | 20592   | 97857   | 22297   | 97483   | 23995   | 97079   | 25685   | 96645   | 7  |
| 54 | 18910   | 98196   | 20620   | 97851   | 22325   | 97476   | 24023   | 97072   | 25713   | 96638   | 6  |
| 55 | 18938   | 98190   | 20649   | 97845   | 22353   | 97470   | 24051   | 97065   | 25741   | 96630   | 5  |
| 56 | 18967   | 98185   | 20677   | 97839   | 22382   | 97463   | 24079   | 97058   | 25769   | 96623   | 4  |
| 57 | 18995   | 98179   | 20706   | 97833   | 22410   | 97457   | 24108   | 97051   | 25798   | 96615   | 3  |
| 58 | 19024   | 98174   | 20734   | 97827   | 22438   | 97450   | 24136   | 97044   | 25826   | 96608   | 2  |
| 59 | 19052   | 98168   | 20763   | 97821   | 22467   | 97444   | 24164   | 97037   | 25854   | 96600   | 1  |
| 60 | 19081   | 98163   | 20791   | 97815   | 22495   | 97437   | 24192   | 97030   | 25882   | 96593   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 79°     |         | 78°     |         | 77°     |         | 76°     |         | 75°     |         |    |



TABLE III. NATURAL SINES AND COSINES.

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| °   | 15°     |         | 16°     |         | 17°     |         | 18°     |         | 19°     |         | °  |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|     | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0   | 25882   | 96593   | 27564   | 96126   | 29237   | 95630   | 30902   | 95106   | 32557   | 94552   | 60 |
| 1   | 25910   | 96585   | 27592   | 96118   | 29265   | 95622   | 30929   | 95097   | 32584   | 94542   | 59 |
| 2   | 25938   | 96578   | 27620   | 96110   | 29293   | 95613   | 30957   | 95088   | 32612   | 94533   | 58 |
| 3   | 25966   | 96570   | 27648   | 96102   | 29321   | 95605   | 30985   | 95079   | 32639   | 94523   | 57 |
| 4   | 25994   | 96562   | 27676   | 96094   | 29348   | 95596   | 31012   | 95070   | 32667   | 94514   | 56 |
| 5   | 26022   | 96555   | 27704   | 96086   | 29376   | 95588   | 31040   | 95061   | 32694   | 94504   | 55 |
| 6   | 26050   | 96547   | 27731   | 96078   | 29404   | 95579   | 31068   | 95052   | 32722   | 94495   | 54 |
| 7   | 26079   | 96540   | 27759   | 96070   | 29432   | 95571   | 31095   | 95043   | 32749   | 94485   | 53 |
| 8   | 26107   | 96532   | 27787   | 96062   | 29460   | 95562   | 31123   | 95033   | 32777   | 94476   | 52 |
| 9   | 26135   | 96524   | 27815   | 96054   | 29487   | 95554   | 31151   | 95024   | 32804   | 94466   | 51 |
| 10  | 26163   | 96517   | 27843   | 96046   | 29515   | 95545   | 31178   | 95015   | 32832   | 94457   | 50 |
| 11  | 26191   | 96509   | 27871   | 96037   | 29543   | 95536   | 31206   | 95006   | 32859   | 94447   | 49 |
| 12  | 26219   | 96502   | 27899   | 96029   | 29571   | 95528   | 31233   | 94997   | 32887   | 94438   | 48 |
| 13  | 26247   | 96494   | 27927   | 96021   | 29599   | 95519   | 31261   | 94988   | 32914   | 94428   | 47 |
| 14  | 26275   | 96486   | 27955   | 96013   | 29626   | 95511   | 31289   | 94979   | 32942   | 94418   | 46 |
| 15  | 26303   | 96479   | 27983   | 96005   | 29654   | 95502   | 31316   | 94970   | 32969   | 94409   | 45 |
| 16  | 26331   | 96471   | 28011   | 95997   | 29682   | 95493   | 31344   | 94961   | 32997   | 94399   | 44 |
| 17  | 26359   | 96463   | 28039   | 95989   | 29710   | 95485   | 31372   | 94952   | 33024   | 94390   | 43 |
| 18  | 26387   | 96456   | 28067   | 95981   | 29737   | 95476   | 31399   | 94943   | 33051   | 94380   | 42 |
| 19  | 26415   | 96448   | 28095   | 95972   | 29765   | 95467   | 31427   | 94933   | 33079   | 94370   | 41 |
| 20  | 26443   | 96440   | 28123   | 95964   | 29793   | 95459   | 31454   | 94924   | 33106   | 94361   | 40 |
| 21  | 26471   | 96433   | 28150   | 95956   | 29821   | 95450   | 31482   | 94915   | 33134   | 94351   | 39 |
| 22  | 26500   | 96425   | 28178   | 95948   | 29849   | 95441   | 31510   | 94906   | 33161   | 94342   | 38 |
| 23  | 26528   | 96417   | 28206   | 95940   | 29876   | 95433   | 31537   | 94897   | 33189   | 94332   | 37 |
| 24  | 26556   | 96410   | 28234   | 95931   | 29904   | 95424   | 31565   | 94888   | 33216   | 94322   | 36 |
| 25  | 26584   | 96402   | 28262   | 95923   | 29932   | 95415   | 31593   | 94878   | 33244   | 94313   | 35 |
| 26  | 26612   | 96394   | 28290   | 95915   | 29960   | 95407   | 31620   | 94869   | 33271   | 94303   | 34 |
| 27  | 26640   | 96386   | 28318   | 95907   | 29987   | 95398   | 31648   | 94860   | 33298   | 94293   | 33 |
| 28  | 26668   | 96379   | 28346   | 95898   | 30015   | 95389   | 31675   | 94851   | 33326   | 94284   | 32 |
| 29  | 26696   | 96371   | 28374   | 95890   | 30043   | 95380   | 31703   | 94842   | 33353   | 94274   | 31 |
| 30  | 26724   | 96363   | 28402   | 95882   | 30071   | 95372   | 31730   | 94832   | 33381   | 94264   | 30 |
| 31  | 26752   | 96355   | 28429   | 95874   | 30098   | 95363   | 31758   | 94823   | 33408   | 94254   | 29 |
| 32  | 26780   | 96347   | 28457   | 95865   | 30126   | 95354   | 31786   | 94814   | 33436   | 94245   | 28 |
| 33  | 26808   | 96340   | 28485   | 95857   | 30154   | 95345   | 31813   | 94805   | 33463   | 94235   | 27 |
| 34  | 26836   | 96332   | 28513   | 95849   | 30182   | 95337   | 31841   | 94795   | 33490   | 94225   | 26 |
| 35  | 26864   | 96324   | 28541   | 95841   | 30209   | 95328   | 31868   | 94786   | 33518   | 94215   | 25 |
| 36  | 26892   | 96316   | 28569   | 95832   | 30237   | 95319   | 31896   | 94777   | 33545   | 94206   | 24 |
| 37  | 26920   | 96308   | 28597   | 95824   | 30265   | 95310   | 31923   | 94768   | 33573   | 94196   | 23 |
| 38  | 26948   | 96301   | 28625   | 95816   | 30292   | 95301   | 31951   | 94758   | 33600   | 94186   | 22 |
| 39  | 26976   | 96293   | 28652   | 95807   | 30320   | 95293   | 31979   | 94749   | 33627   | 94176   | 21 |
| 40  | 27004   | 96285   | 28680   | 95799   | 30348   | 95284   | 32006   | 94740   | 33655   | 94167   | 20 |
| 41  | 27032   | 96277   | 28708   | 95791   | 30376   | 95275   | 32034   | 94730   | 33682   | 94157   | 19 |
| 42  | 27060   | 96269   | 28736   | 95782   | 30403   | 95266   | 32061   | 94721   | 33710   | 94147   | 18 |
| 43  | 27088   | 96261   | 28764   | 95774   | 30431   | 95257   | 32089   | 94712   | 33737   | 94137   | 17 |
| 44  | 27116   | 96253   | 28792   | 95766   | 30459   | 95248   | 32116   | 94702   | 33764   | 94127   | 16 |
| 45  | 27144   | 96246   | 28820   | 95757   | 30486   | 95240   | 32144   | 94693   | 33792   | 94118   | 15 |
| 46  | 27172   | 96238   | 28847   | 95749   | 30514   | 95231   | 32171   | 94684   | 33819   | 94108   | 14 |
| 47  | 27200   | 96230   | 28875   | 95740   | 30542   | 95222   | 32199   | 94674   | 33846   | 94098   | 13 |
| 48  | 27228   | 96222   | 28903   | 95732   | 30570   | 95213   | 32227   | 94665   | 33874   | 94088   | 12 |
| 49  | 27256   | 96214   | 28931   | 95724   | 30597   | 95204   | 32254   | 94656   | 33901   | 94078   | 11 |
| 50  | 27284   | 96206   | 28959   | 95715   | 30625   | 95195   | 32282   | 94646   | 33929   | 94068   | 10 |
| 51  | 27312   | 96198   | 28987   | 95707   | 30653   | 95186   | 32309   | 94637   | 33956   | 94058   | 9  |
| 52  | 27340   | 96190   | 29015   | 95698   | 30680   | 95177   | 32337   | 94627   | 33983   | 94048   | 8  |
| 53  | 27368   | 96182   | 29042   | 95690   | 30708   | 95168   | 32364   | 94618   | 34011   | 94039   | 7  |
| 54  | 27396   | 96174   | 29070   | 95681   | 30736   | 95159   | 32392   | 94609   | 34038   | 94029   | 6  |
| 55  | 27424   | 96166   | 29098   | 95673   | 30763   | 95150   | 32419   | 94599   | 34065   | 94019   | 5  |
| 56  | 27452   | 96158   | 29126   | 95664   | 30791   | 95142   | 32447   | 94590   | 34093   | 94009   | 4  |
| 57  | 27480   | 96150   | 29154   | 95656   | 30819   | 95133   | 32474   | 94580   | 34120   | 93999   | 3  |
| 58  | 27508   | 96142   | 29182   | 95647   | 30846   | 95124   | 32502   | 94571   | 34147   | 93989   | 2  |
| 59  | 27536   | 96134   | 29209   | 95639   | 30874   | 95115   | 32529   | 94561   | 34175   | 93979   | 1  |
| 60  | 27564   | 96126   | 29237   | 95630   | 30902   | 95106   | 32557   | 94552   | 34202   | 93969   | 0  |
| °   | 15°     |         | 16°     |         | 17°     |         | 18°     |         | 19°     |         | °  |
|     | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
| 74° |         |         | 78°     |         | 72°     |         | 71°     |         | 70°     |         |    |

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| /  | Sze.     | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.789342 | 269 | 9.896532 | 164 | 9.892810 | 434 | 10.107190 | 60 |
| 1  | 789504   | 269 | 896433   | 165 | 893070   | 434 | 106930    | 59 |
| 2  | 789665   | 269 | 896335   | 165 | 893331   | 434 | 106669    | 58 |
| 3  | 789827   | 269 | 896236   | 165 | 893591   | 434 | 106409    | 57 |
| 4  | 789988   | 269 | 896137   | 165 | 893851   | 434 | 106149    | 56 |
| 5  | 790149   | 269 | 896038   | 165 | 894111   | 434 | 105889    | 55 |
| 6  | 790310   | 268 | 895939   | 165 | 894372   | 434 | 105628    | 54 |
| 7  | 790471   | 268 | 895840   | 165 | 894632   | 433 | 105368    | 53 |
| 8  | 790632   | 268 | 895741   | 165 | 894892   | 433 | 105108    | 52 |
| 9  | 790793   | 268 | 895642   | 165 | 895152   | 433 | 104848    | 51 |
| 10 | 790954   | 268 | 895542   | 165 | 895412   | 433 | 104588    | 50 |
| 11 | 9.791115 | 268 | 9.895443 | 166 | 9.895672 | 433 | 10.104328 | 49 |
| 12 | 791275   | 267 | 895343   | 166 | 895932   | 433 | 104068    | 48 |
| 13 | 791436   | 267 | 895244   | 166 | 896192   | 433 | 103808    | 47 |
| 14 | 791596   | 267 | 895145   | 166 | 896452   | 433 | 103548    | 46 |
| 15 | 791757   | 267 | 895045   | 166 | 896712   | 433 | 103288    | 45 |
| 16 | 791917   | 267 | 894945   | 166 | 896971   | 433 | 103029    | 44 |
| 17 | 792077   | 267 | 894846   | 166 | 897231   | 433 | 102769    | 43 |
| 18 | 792237   | 266 | 894746   | 166 | 897491   | 433 | 102509    | 42 |
| 19 | 792397   | 266 | 894646   | 166 | 897751   | 433 | 102249    | 41 |
| 20 | 792557   | 266 | 894546   | 166 | 898010   | 433 | 101990    | 40 |
| 21 | 9.792716 | 266 | 9.894446 | 167 | 9.898270 | 432 | 10.101730 | 39 |
| 22 | 792876   | 266 | 894346   | 167 | 898530   | 432 | 101470    | 38 |
| 23 | 793035   | 266 | 894246   | 167 | 898790   | 432 | 101211    | 37 |
| 24 | 793195   | 265 | 894146   | 167 | 899049   | 432 | 100951    | 36 |
| 25 | 793354   | 265 | 894046   | 167 | 899308   | 432 | 100692    | 35 |
| 26 | 793514   | 265 | 893946   | 167 | 899568   | 432 | 100432    | 34 |
| 27 | 793673   | 265 | 893846   | 167 | 899827   | 432 | 100173    | 33 |
| 28 | 793832   | 265 | 893745   | 167 | 900087   | 432 | 999913    | 32 |
| 29 | 793991   | 265 | 893645   | 167 | 900346   | 432 | 999654    | 31 |
| 30 | 794150   | 264 | 893544   | 167 | 900605   | 432 | 999395    | 30 |
| 31 | 9.794308 | 264 | 9.893444 | 168 | 9.900864 | 432 | 10.099136 | 29 |
| 32 | 794467   | 264 | 893343   | 168 | 901124   | 432 | 998876    | 28 |
| 33 | 794626   | 264 | 893243   | 168 | 901383   | 432 | 998617    | 27 |
| 34 | 794784   | 264 | 893142   | 168 | 901642   | 432 | 998358    | 26 |
| 35 | 794942   | 264 | 893041   | 168 | 901901   | 432 | 998099    | 25 |
| 36 | 795101   | 264 | 892940   | 168 | 902160   | 432 | 997840    | 24 |
| 37 | 795259   | 263 | 892839   | 168 | 902420   | 432 | 997580    | 23 |
| 38 | 795417   | 263 | 892739   | 168 | 902679   | 432 | 997321    | 22 |
| 39 | 795575   | 263 | 892638   | 168 | 902938   | 432 | 997062    | 21 |
| 40 | 795733   | 263 | 892536   | 168 | 903197   | 431 | 996803    | 20 |
| 41 | 9.795891 | 263 | 9.892435 | 169 | 9.903456 | 431 | 10.096544 | 19 |
| 42 | 796049   | 263 | 892334   | 169 | 903714   | 431 | 996286    | 18 |
| 43 | 796206   | 263 | 892233   | 169 | 903973   | 431 | 996027    | 17 |
| 44 | 796364   | 262 | 892132   | 169 | 904232   | 431 | 995768    | 16 |
| 45 | 796521   | 262 | 892030   | 169 | 904491   | 431 | 995509    | 15 |
| 46 | 796679   | 262 | 891929   | 169 | 904750   | 431 | 995250    | 14 |
| 47 | 796836   | 262 | 891827   | 169 | 905008   | 431 | 994992    | 13 |
| 48 | 796993   | 262 | 891726   | 169 | 905267   | 431 | 994733    | 12 |
| 49 | 797150   | 261 | 891624   | 169 | 905526   | 431 | 994474    | 11 |
| 50 | 797307   | 261 | 891523   | 170 | 905785   | 431 | 994215    | 10 |
| 51 | 9.797464 | 261 | 9.891421 | 170 | 9.906043 | 431 | 10.093957 | 9  |
| 52 | 797621   | 261 | 891319   | 170 | 906302   | 431 | 993698    | 8  |
| 53 | 797777   | 261 | 891217   | 170 | 906560   | 431 | 993440    | 7  |
| 54 | 797934   | 261 | 891115   | 170 | 906819   | 431 | 993181    | 6  |
| 55 | 798091   | 261 | 891013   | 170 | 907077   | 431 | 992923    | 5  |
| 56 | 798247   | 261 | 890911   | 170 | 907336   | 431 | 992664    | 4  |
| 57 | 798403   | 260 | 890809   | 170 | 907594   | 431 | 992406    | 3  |
| 58 | 798559   | 260 | 890707   | 170 | 907853   | 431 | 992147    | 2  |
| 59 | 798716   | 260 | 890605   | 170 | 908111   | 430 | 991889    | 1  |
| 60 | 798872   | 260 | 890503   | 170 | 908369   | 430 | 991631    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 89° |          |     |          |     |          |     |           | 140° |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |
| 0   | 9.798872 | 260 | 9.890503 | 170 | 9.908369 | 430 | 10.091631 | 60   |  |
| 1   | 799028   | 260 | 890400   | 171 | 908628   | 430 | 091372    | 59   |  |
| 2   | 799184   | 260 | 890298   | 171 | 908886   | 430 | 091114    | 58   |  |
| 3   | 799339   | 259 | 890195   | 171 | 909144   | 430 | 090856    | 57   |  |
| 4   | 799495   | 259 | 890093   | 171 | 909402   | 430 | 090598    | 56   |  |
| 5   | 799651   | 259 | 889990   | 171 | 909660   | 430 | 090340    | 55   |  |
| 6   | 799806   | 259 | 889888   | 171 | 909918   | 430 | 090082    | 54   |  |
| 7   | 799962   | 259 | 889785   | 171 | 910177   | 430 | 089823    | 53   |  |
| 8   | 800117   | 259 | 889682   | 171 | 910435   | 430 | 089565    | 52   |  |
| 9   | 800272   | 258 | 889579   | 171 | 910693   | 430 | 089307    | 51   |  |
| 10  | 800427   | 258 | 889477   | 171 | 910951   | 430 | 089049    | 50   |  |
| 11  | 9.800582 | 258 | 9.889374 | 172 | 9.911209 | 430 | 10.088791 | 49   |  |
| 12  | 800737   | 258 | 889271   | 172 | 911467   | 430 | 088533    | 48   |  |
| 13  | 800892   | 258 | 889168   | 172 | 911725   | 430 | 088275    | 47   |  |
| 14  | 801047   | 258 | 889064   | 172 | 911982   | 430 | 088018    | 46   |  |
| 15  | 801201   | 258 | 888961   | 172 | 912240   | 430 | 087760    | 45   |  |
| 16  | 801356   | 257 | 888858   | 172 | 912498   | 430 | 087502    | 44   |  |
| 17  | 801511   | 257 | 888755   | 172 | 912756   | 430 | 087244    | 43   |  |
| 18  | 801665   | 257 | 888651   | 172 | 913014   | 429 | 086986    | 42   |  |
| 19  | 801819   | 257 | 888548   | 172 | 913271   | 429 | 086729    | 41   |  |
| 20  | 801973   | 257 | 888444   | 173 | 913529   | 429 | 086471    | 40   |  |
| 21  | 9.802128 | 257 | 9.888341 | 173 | 9.913787 | 429 | 10.086213 | 39   |  |
| 22  | 802282   | 256 | 888237   | 173 | 914044   | 429 | 085956    | 38   |  |
| 23  | 802436   | 256 | 888134   | 173 | 914302   | 429 | 085698    | 37   |  |
| 24  | 802589   | 256 | 888030   | 173 | 914560   | 429 | 085440    | 36   |  |
| 25  | 802743   | 256 | 887926   | 173 | 914817   | 429 | 085183    | 35   |  |
| 26  | 802897   | 256 | 887822   | 173 | 915075   | 429 | 084925    | 34   |  |
| 27  | 803050   | 256 | 887718   | 173 | 915332   | 429 | 084668    | 33   |  |
| 28  | 803204   | 256 | 887614   | 173 | 915590   | 429 | 084410    | 32   |  |
| 29  | 803357   | 255 | 887510   | 173 | 915847   | 429 | 084153    | 31   |  |
| 30  | 803511   | 255 | 887406   | 174 | 916104   | 429 | 083896    | 30   |  |
| 31  | 9.803664 | 255 | 9.887302 | 174 | 9.916362 | 429 | 10.083638 | 29   |  |
| 32  | 803817   | 255 | 887198   | 174 | 916619   | 429 | 083381    | 28   |  |
| 33  | 803970   | 255 | 887093   | 174 | 916877   | 429 | 083123    | 27   |  |
| 34  | 804123   | 255 | 886989   | 174 | 917134   | 429 | 082866    | 26   |  |
| 35  | 804276   | 254 | 886885   | 174 | 917391   | 429 | 082609    | 25   |  |
| 36  | 804428   | 254 | 886780   | 174 | 917648   | 429 | 082352    | 24   |  |
| 37  | 804581   | 254 | 886676   | 174 | 917906   | 429 | 082094    | 23   |  |
| 38  | 804734   | 254 | 886571   | 174 | 918163   | 428 | 081837    | 22   |  |
| 39  | 804886   | 254 | 886466   | 174 | 918420   | 428 | 081580    | 21   |  |
| 40  | 805039   | 254 | 886362   | 175 | 918677   | 428 | 081323    | 20   |  |
| 41  | 9.805191 | 254 | 9.886257 | 175 | 9.918934 | 428 | 10.081066 | 19   |  |
| 42  | 805343   | 253 | 886152   | 175 | 919191   | 428 | 080809    | 18   |  |
| 43  | 805495   | 253 | 886047   | 175 | 919448   | 428 | 080552    | 17   |  |
| 44  | 805647   | 253 | 885942   | 175 | 919705   | 428 | 080295    | 16   |  |
| 45  | 805799   | 253 | 885837   | 175 | 919962   | 428 | 080038    | 15   |  |
| 46  | 805951   | 253 | 885732   | 175 | 920219   | 428 | 079781    | 14   |  |
| 47  | 806103   | 253 | 885627   | 175 | 920476   | 428 | 079524    | 13   |  |
| 48  | 806254   | 253 | 885522   | 175 | 920733   | 428 | 079267    | 12   |  |
| 49  | 806406   | 252 | 885416   | 175 | 920990   | 428 | 079010    | 11   |  |
| 50  | 806557   | 252 | 885311   | 176 | 921247   | 428 | 078753    | 10   |  |
| 51  | 9.806709 | 252 | 9.885205 | 176 | 9.921503 | 428 | 10.078497 | 9    |  |
| 52  | 806860   | 252 | 885100   | 176 | 921760   | 428 | 078240    | 8    |  |
| 53  | 807011   | 252 | 884994   | 176 | 922017   | 428 | 077983    | 7    |  |
| 54  | 807163   | 252 | 884889   | 176 | 922274   | 428 | 077726    | 6    |  |
| 55  | 807314   | 252 | 884783   | 176 | 922530   | 428 | 077470    | 5    |  |
| 56  | 807465   | 251 | 884677   | 176 | 922787   | 428 | 077213    | 4    |  |
| 57  | 807615   | 251 | 884572   | 176 | 923044   | 428 | 076956    | 3    |  |
| 58  | 807766   | 251 | 884466   | 176 | 923300   | 428 | 076700    | 2    |  |
| 59  | 807917   | 251 | 884360   | 176 | 923557   | 427 | 076443    | 1    |  |
| 60  | 808067   | 251 | 884254   | 177 | 923814   | 427 | 076186    | 0    |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |

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50°

88°

141°

| /  | Sz.      | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.789342 | 269 | 9.896532 | 164 | 9.892810 | 434 | 10.107190 | 60 |
| 1  | 789304   | 269 | 896433   | 165 | 893070   | 434 | 106930    | 59 |
| 2  | 789665   | 269 | 896335   | 165 | 893331   | 434 | 106669    | 58 |
| 3  | 789827   | 269 | 896236   | 165 | 893591   | 434 | 106409    | 57 |
| 4  | 789988   | 269 | 896137   | 165 | 893851   | 434 | 106149    | 56 |
| 5  | 790149   | 269 | 896038   | 165 | 894111   | 434 | 105889    | 55 |
| 6  | 790310   | 268 | 895939   | 165 | 894372   | 434 | 105628    | 54 |
| 7  | 790471   | 268 | 895840   | 165 | 894632   | 433 | 105368    | 53 |
| 8  | 790632   | 268 | 895741   | 165 | 894892   | 433 | 105108    | 52 |
| 9  | 790793   | 268 | 895641   | 165 | 895152   | 433 | 104848    | 51 |
| 10 | 790954   | 268 | 895542   | 165 | 895412   | 433 | 104588    | 50 |
| 11 | 9.791115 | 268 | 9.895443 | 166 | 9.895672 | 433 | 10.104328 | 49 |
| 12 | 791275   | 267 | 895343   | 166 | 895932   | 433 | 104068    | 48 |
| 13 | 791436   | 267 | 895244   | 166 | 896192   | 433 | 103808    | 47 |
| 14 | 791596   | 267 | 895145   | 166 | 896452   | 433 | 103548    | 46 |
| 15 | 791757   | 267 | 895045   | 166 | 896712   | 433 | 103288    | 45 |
| 16 | 791917   | 267 | 894945   | 166 | 896971   | 433 | 103029    | 44 |
| 17 | 792077   | 267 | 894846   | 166 | 897231   | 433 | 102769    | 43 |
| 18 | 792237   | 266 | 894746   | 166 | 897491   | 433 | 102509    | 42 |
| 19 | 792397   | 266 | 894646   | 166 | 897751   | 433 | 102249    | 41 |
| 20 | 792557   | 266 | 894546   | 166 | 898010   | 433 | 101990    | 40 |
| 21 | 9.792716 | 266 | 9.894446 | 167 | 9.898270 | 433 | 10.101730 | 39 |
| 22 | 792876   | 266 | 894346   | 167 | 898530   | 433 | 101470    | 38 |
| 23 | 793035   | 266 | 894246   | 167 | 898789   | 433 | 101211    | 37 |
| 24 | 793195   | 265 | 894146   | 167 | 899049   | 432 | 100951    | 36 |
| 25 | 793354   | 265 | 894046   | 167 | 899308   | 432 | 100692    | 35 |
| 26 | 793514   | 265 | 893946   | 167 | 899568   | 432 | 100432    | 34 |
| 27 | 793673   | 265 | 893846   | 167 | 899827   | 432 | 100173    | 33 |
| 28 | 793832   | 265 | 893745   | 167 | 900087   | 432 | 999913    | 32 |
| 29 | 793991   | 265 | 893645   | 167 | 900346   | 432 | 999654    | 31 |
| 30 | 794150   | 264 | 893544   | 167 | 900605   | 432 | 999395    | 30 |
| 31 | 9.794308 | 264 | 9.893444 | 168 | 9.900864 | 432 | 10.099136 | 29 |
| 32 | 794467   | 264 | 893343   | 168 | 901124   | 432 | 998876    | 28 |
| 33 | 794626   | 264 | 893243   | 168 | 901383   | 432 | 998617    | 27 |
| 34 | 794784   | 264 | 893142   | 168 | 901642   | 432 | 998358    | 26 |
| 35 | 794942   | 264 | 893041   | 168 | 901901   | 432 | 998099    | 25 |
| 36 | 795101   | 264 | 892940   | 168 | 902160   | 432 | 997840    | 24 |
| 37 | 795259   | 263 | 892839   | 168 | 902420   | 432 | 997580    | 23 |
| 38 | 795417   | 263 | 892739   | 168 | 902679   | 432 | 997321    | 22 |
| 39 | 795575   | 263 | 892638   | 168 | 902938   | 432 | 997062    | 21 |
| 40 | 795733   | 263 | 892536   | 168 | 903197   | 431 | 996803    | 20 |
| 41 | 9.795891 | 263 | 9.892435 | 169 | 9.903456 | 431 | 10.096544 | 19 |
| 42 | 796049   | 263 | 892334   | 169 | 903714   | 431 | 996286    | 18 |
| 43 | 796206   | 263 | 892233   | 169 | 903973   | 431 | 996027    | 17 |
| 44 | 796364   | 262 | 892132   | 169 | 904232   | 431 | 995768    | 16 |
| 45 | 796521   | 262 | 892030   | 169 | 904491   | 431 | 995509    | 15 |
| 46 | 796679   | 262 | 891929   | 169 | 904750   | 431 | 995250    | 14 |
| 47 | 796836   | 262 | 891827   | 169 | 905008   | 431 | 994992    | 13 |
| 48 | 796993   | 262 | 891726   | 169 | 905267   | 431 | 994733    | 12 |
| 49 | 797150   | 261 | 891624   | 169 | 905526   | 431 | 994474    | 11 |
| 50 | 797307   | 261 | 891523   | 170 | 905785   | 431 | 994215    | 10 |
| 51 | 9.797464 | 261 | 9.891421 | 170 | 9.906043 | 431 | 10.096397 | 9  |
| 52 | 797621   | 261 | 891319   | 170 | 906302   | 431 | 993698    | 8  |
| 53 | 797777   | 261 | 891217   | 170 | 906560   | 431 | 993440    | 7  |
| 54 | 797934   | 261 | 891115   | 170 | 906819   | 431 | 993181    | 6  |
| 55 | 798091   | 261 | 891013   | 170 | 907077   | 431 | 992923    | 5  |
| 56 | 798247   | 261 | 890911   | 170 | 907336   | 431 | 992664    | 4  |
| 57 | 798403   | 260 | 890809   | 170 | 907594   | 431 | 992406    | 3  |
| 58 | 798560   | 260 | 890707   | 170 | 907853   | 431 | 992147    | 2  |
| 59 | 798716   | 260 | 890605   | 170 | 908111   | 430 | 991889    | 1  |
| 60 | 798872   | 260 | 890503   | 170 | 908369   | 430 | 991631    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 39° |          |     |          |     |          |     |           | 140° |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |
| 0   | 9.798872 | 260 | 9.890503 | 170 | 9.908369 | 430 | 10.091631 | 60   |  |
| 1   | 799028   | 260 | 890400   | 171 | 908628   | 430 | 091372    | 59   |  |
| 2   | 799184   | 260 | 890298   | 171 | 908886   | 430 | 091114    | 58   |  |
| 3   | 799339   | 259 | 890195   | 171 | 909144   | 430 | 090856    | 57   |  |
| 4   | 799495   | 259 | 890093   | 171 | 909402   | 430 | 090598    | 56   |  |
| 5   | 799651   | 259 | 889990   | 171 | 909660   | 430 | 090340    | 55   |  |
| 6   | 799806   | 259 | 889888   | 171 | 909918   | 430 | 090082    | 54   |  |
| 7   | 799962   | 259 | 889785   | 171 | 910177   | 430 | 089823    | 53   |  |
| 8   | 800117   | 259 | 889682   | 171 | 910435   | 430 | 089565    | 52   |  |
| 9   | 800272   | 258 | 889579   | 171 | 910693   | 430 | 089307    | 51   |  |
| 10  | 800427   | 258 | 889477   | 171 | 910951   | 430 | 089049    | 50   |  |
| 11  | 9.800582 | 258 | 9.889374 | 172 | 9.911209 | 430 | 10.088791 | 49   |  |
| 12  | 800737   | 258 | 889271   | 172 | 911467   | 430 | 088533    | 48   |  |
| 13  | 800892   | 258 | 889168   | 172 | 911725   | 430 | 088275    | 47   |  |
| 14  | 801047   | 258 | 889064   | 172 | 911982   | 430 | 088018    | 46   |  |
| 15  | 801201   | 258 | 888961   | 172 | 912240   | 430 | 087760    | 45   |  |
| 16  | 801356   | 257 | 888858   | 172 | 912498   | 430 | 087502    | 44   |  |
| 17  | 801511   | 257 | 888755   | 172 | 912756   | 430 | 087244    | 43   |  |
| 18  | 801665   | 257 | 888651   | 172 | 913014   | 429 | 086986    | 42   |  |
| 19  | 801819   | 257 | 888548   | 172 | 913271   | 429 | 086729    | 41   |  |
| 20  | 801973   | 257 | 888444   | 173 | 913529   | 429 | 086471    | 40   |  |
| 21  | 9.802128 | 257 | 9.888341 | 173 | 9.913787 | 429 | 10.086213 | 39   |  |
| 22  | 802282   | 256 | 888237   | 173 | 914044   | 429 | 085956    | 38   |  |
| 23  | 802436   | 256 | 888134   | 173 | 914302   | 429 | 085698    | 37   |  |
| 24  | 802589   | 256 | 888030   | 173 | 914560   | 429 | 085440    | 36   |  |
| 25  | 802743   | 256 | 887926   | 173 | 914817   | 429 | 085183    | 35   |  |
| 26  | 802897   | 256 | 887822   | 173 | 915075   | 429 | 084925    | 34   |  |
| 27  | 803050   | 256 | 887718   | 173 | 915332   | 429 | 084668    | 33   |  |
| 28  | 803204   | 256 | 887614   | 173 | 915590   | 429 | 084410    | 32   |  |
| 29  | 803357   | 255 | 887510   | 173 | 915847   | 429 | 084153    | 31   |  |
| 30  | 803511   | 255 | 887406   | 174 | 916104   | 429 | 083896    | 30   |  |
| 31  | 9.803664 | 255 | 9.887302 | 174 | 9.916362 | 429 | 10.083638 | 29   |  |
| 32  | 803817   | 255 | 887198   | 174 | 916619   | 429 | 083381    | 28   |  |
| 33  | 803970   | 255 | 887093   | 174 | 916877   | 429 | 083123    | 27   |  |
| 34  | 804123   | 255 | 886989   | 174 | 917134   | 429 | 082866    | 26   |  |
| 35  | 804276   | 254 | 886885   | 174 | 917391   | 429 | 082609    | 25   |  |
| 36  | 804428   | 254 | 886780   | 174 | 917648   | 429 | 082352    | 24   |  |
| 37  | 804581   | 254 | 886676   | 174 | 917906   | 429 | 082094    | 23   |  |
| 38  | 804734   | 254 | 886571   | 174 | 918163   | 428 | 081837    | 22   |  |
| 39  | 804886   | 254 | 886466   | 174 | 918420   | 428 | 081580    | 21   |  |
| 40  | 805039   | 254 | 886362   | 175 | 918677   | 428 | 081323    | 20   |  |
| 41  | 9.805191 | 254 | 9.886257 | 175 | 9.918934 | 428 | 10.081066 | 19   |  |
| 42  | 805343   | 253 | 886152   | 175 | 919191   | 428 | 080809    | 18   |  |
| 43  | 805495   | 253 | 886047   | 175 | 919448   | 428 | 080552    | 17   |  |
| 44  | 805647   | 253 | 885942   | 175 | 919705   | 428 | 080295    | 16   |  |
| 45  | 805799   | 253 | 885837   | 175 | 919962   | 428 | 080038    | 15   |  |
| 46  | 805951   | 253 | 885732   | 175 | 920219   | 428 | 079781    | 14   |  |
| 47  | 806103   | 253 | 885627   | 175 | 920476   | 428 | 079524    | 13   |  |
| 48  | 806254   | 253 | 885522   | 175 | 920733   | 428 | 079267    | 12   |  |
| 49  | 806406   | 252 | 885416   | 175 | 920990   | 428 | 079010    | 11   |  |
| 50  | 806557   | 252 | 885311   | 176 | 921247   | 428 | 078753    | 10   |  |
| 51  | 9.806709 | 252 | 9.885205 | 176 | 9.921503 | 428 | 10.078497 | 9    |  |
| 52  | 806860   | 252 | 885100   | 176 | 921760   | 428 | 078240    | 8    |  |
| 53  | 807011   | 252 | 884994   | 176 | 922017   | 428 | 077983    | 7    |  |
| 54  | 807163   | 252 | 884889   | 176 | 922274   | 428 | 077726    | 6    |  |
| 55  | 807314   | 252 | 884783   | 176 | 922530   | 428 | 077470    | 5    |  |
| 56  | 807465   | 251 | 884677   | 176 | 922787   | 428 | 077213    | 4    |  |
| 57  | 807615   | 251 | 884572   | 176 | 923044   | 428 | 076956    | 3    |  |
| 58  | 807766   | 251 | 884466   | 176 | 923300   | 428 | 076700    | 2    |  |
| 59  | 807917   | 251 | 884360   | 176 | 923557   | 427 | 076443    | 1    |  |
| 60  | 808067   | 251 | 884254   | 177 | 923814   | 427 | 076186    | 0    |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |

129°

50°

40°

139°

| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9.808067 | 251 | 9.884254 | 177 | 9.923814 | 427 | 10.076186 | 60 |
| 1  | 808218   | 251 | 884148   | 177 | 924070   | 427 | 075930    | 59 |
| 2  | 808368   | 251 | 884042   | 177 | 924327   | 427 | 075673    | 58 |
| 3  | 808519   | 250 | 883936   | 177 | 924583   | 427 | 075417    | 57 |
| 4  | 808669   | 250 | 883829   | 177 | 924840   | 427 | 075160    | 56 |
| 5  | 808819   | 250 | 883723   | 177 | 925096   | 427 | 074904    | 55 |
| 6  | 808969   | 250 | 883617   | 177 | 925352   | 427 | 074648    | 54 |
| 7  | 809119   | 250 | 883510   | 177 | 925609   | 427 | 074391    | 53 |
| 8  | 809269   | 250 | 883404   | 177 | 925865   | 427 | 074135    | 52 |
| 9  | 809419   | 249 | 883297   | 178 | 926122   | 427 | 073878    | 51 |
| 10 | 809569   | 249 | 883191   | 178 | 926378   | 427 | 073622    | 50 |
| 11 | 9.809718 | 249 | 9.883084 | 178 | 9.926634 | 427 | 10.073366 | 49 |
| 12 | 809868   | 249 | 882977   | 178 | 926890   | 427 | 073110    | 48 |
| 13 | 810017   | 249 | 882871   | 178 | 927147   | 427 | 072853    | 47 |
| 14 | 810167   | 249 | 882764   | 178 | 927403   | 427 | 072597    | 46 |
| 15 | 810316   | 248 | 882657   | 178 | 927659   | 427 | 072341    | 45 |
| 16 | 810465   | 248 | 882550   | 178 | 927915   | 427 | 072085    | 44 |
| 17 | 810614   | 248 | 882443   | 178 | 928171   | 427 | 071829    | 43 |
| 18 | 810763   | 248 | 882336   | 179 | 928427   | 427 | 071573    | 42 |
| 19 | 810912   | 248 | 882229   | 179 | 928684   | 427 | 071316    | 41 |
| 20 | 811061   | 248 | 882121   | 179 | 928940   | 427 | 071060    | 40 |
| 21 | 9.811210 | 248 | 9.882014 | 179 | 9.929196 | 427 | 10.070804 | 39 |
| 22 | 811358   | 247 | 881907   | 179 | 929452   | 427 | 070548    | 38 |
| 23 | 811507   | 247 | 881799   | 179 | 929708   | 427 | 070292    | 37 |
| 24 | 811655   | 247 | 881692   | 179 | 929964   | 426 | 070036    | 36 |
| 25 | 811804   | 247 | 881584   | 179 | 930220   | 426 | 069780    | 35 |
| 26 | 811952   | 247 | 881477   | 179 | 930475   | 426 | 069525    | 34 |
| 27 | 812100   | 247 | 881369   | 179 | 930731   | 426 | 069269    | 33 |
| 28 | 812248   | 247 | 881261   | 180 | 930987   | 426 | 069013    | 32 |
| 29 | 812396   | 246 | 881153   | 180 | 931243   | 426 | 068757    | 31 |
| 30 | 812544   | 246 | 881046   | 180 | 931499   | 426 | 068501    | 30 |
| 31 | 9.812692 | 246 | 9.880938 | 180 | 9.931755 | 426 | 10.068245 | 29 |
| 32 | 812840   | 246 | 880830   | 180 | 932010   | 426 | 067990    | 28 |
| 33 | 812988   | 246 | 880722   | 180 | 932266   | 426 | 067734    | 27 |
| 34 | 813135   | 246 | 880613   | 180 | 932522   | 426 | 067478    | 26 |
| 35 | 813283   | 246 | 880505   | 180 | 932778   | 426 | 067222    | 25 |
| 36 | 813430   | 245 | 880397   | 180 | 933033   | 426 | 066967    | 24 |
| 37 | 813578   | 245 | 880289   | 181 | 933289   | 426 | 066711    | 23 |
| 38 | 813725   | 245 | 880180   | 181 | 933545   | 426 | 066455    | 22 |
| 39 | 813873   | 245 | 880072   | 181 | 933800   | 426 | 066200    | 21 |
| 40 | 814019   | 245 | 879963   | 181 | 934056   | 426 | 065944    | 20 |
| 41 | 9.814166 | 245 | 9.879855 | 181 | 9.934311 | 426 | 10.065689 | 19 |
| 42 | 814313   | 245 | 879746   | 181 | 934567   | 426 | 065433    | 18 |
| 43 | 814460   | 244 | 879637   | 181 | 934822   | 426 | 065178    | 17 |
| 44 | 814607   | 244 | 879529   | 181 | 935078   | 426 | 064922    | 16 |
| 45 | 814753   | 244 | 879420   | 181 | 935333   | 426 | 064667    | 15 |
| 46 | 814900   | 244 | 879311   | 181 | 935589   | 426 | 064411    | 14 |
| 47 | 815046   | 244 | 879202   | 182 | 935844   | 426 | 064156    | 13 |
| 48 | 815193   | 244 | 879093   | 182 | 936100   | 426 | 063900    | 12 |
| 49 | 815339   | 244 | 878984   | 182 | 936355   | 426 | 063645    | 11 |
| 50 | 815485   | 243 | 878875   | 182 | 936611   | 426 | 063389    | 10 |
| 51 | 9.815631 | 243 | 9.878766 | 182 | 9.936866 | 425 | 10.063134 | 9  |
| 52 | 815778   | 243 | 878656   | 182 | 937121   | 425 | 062879    | 8  |
| 53 | 815924   | 243 | 878547   | 182 | 937377   | 425 | 062623    | 7  |
| 54 | 816069   | 243 | 878438   | 182 | 937632   | 425 | 062368    | 6  |
| 55 | 816215   | 243 | 878328   | 182 | 937887   | 425 | 062113    | 5  |
| 56 | 816361   | 243 | 878219   | 183 | 938142   | 425 | 061858    | 4  |
| 57 | 816507   | 242 | 878109   | 183 | 938398   | 425 | 061602    | 3  |
| 58 | 816652   | 242 | 877999   | 183 | 938653   | 425 | 061347    | 2  |
| 59 | 816798   | 242 | 877890   | 183 | 938908   | 425 | 061092    | 1  |
| 60 | 816943   | 242 | 877780   | 183 | 939163   | 425 | 060837    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 41° |          |     |          |     |          |     |           | 138° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9-816943 | 242 | 9-877780 | 183 | 9-939163 | 425 | 10-060843 | 60   |  |  |  |  |  |  |  |
| 1   | 817088   | 242 | 877670   | 183 | 939418   | 425 | 060582    | 59   |  |  |  |  |  |  |  |
| 2   | 817233   | 242 | 877560   | 183 | 939673   | 425 | 060327    | 58   |  |  |  |  |  |  |  |
| 3   | 817379   | 242 | 877450   | 183 | 939928   | 425 | 060072    | 57   |  |  |  |  |  |  |  |
| 4   | 817524   | 241 | 877340   | 183 | 940183   | 425 | 059817    | 56   |  |  |  |  |  |  |  |
| 5   | 817668   | 241 | 877230   | 184 | 940439   | 425 | 059561    | 55   |  |  |  |  |  |  |  |
| 6   | 817813   | 241 | 877120   | 184 | 940694   | 425 | 059306    | 54   |  |  |  |  |  |  |  |
| 7   | 817958   | 241 | 877010   | 184 | 940949   | 425 | 059051    | 53   |  |  |  |  |  |  |  |
| 8   | 818103   | 241 | 876899   | 184 | 941204   | 425 | 058796    | 52   |  |  |  |  |  |  |  |
| 9   | 818247   | 241 | 876789   | 184 | 941459   | 425 | 058541    | 51   |  |  |  |  |  |  |  |
| 10  | 818392   | 241 | 876678   | 184 | 941713   | 425 | 058287    | 50   |  |  |  |  |  |  |  |
| 11  | 9-818536 | 240 | 9-876568 | 184 | 9-941968 | 425 | 10-058032 | 49   |  |  |  |  |  |  |  |
| 12  | 818681   | 240 | 876457   | 184 | 942223   | 425 | 057777    | 48   |  |  |  |  |  |  |  |
| 13  | 818825   | 240 | 876347   | 184 | 942478   | 425 | 057522    | 47   |  |  |  |  |  |  |  |
| 14  | 818969   | 240 | 876236   | 185 | 942733   | 425 | 057267    | 46   |  |  |  |  |  |  |  |
| 15  | 819113   | 240 | 876125   | 185 | 942988   | 425 | 057012    | 45   |  |  |  |  |  |  |  |
| 16  | 819257   | 240 | 876014   | 185 | 943243   | 425 | 056757    | 44   |  |  |  |  |  |  |  |
| 17  | 819401   | 240 | 875904   | 185 | 943498   | 425 | 056502    | 43   |  |  |  |  |  |  |  |
| 18  | 819545   | 239 | 875793   | 185 | 943752   | 425 | 056248    | 42   |  |  |  |  |  |  |  |
| 19  | 819689   | 239 | 875682   | 185 | 944007   | 425 | 055993    | 41   |  |  |  |  |  |  |  |
| 20  | 819832   | 239 | 875571   | 185 | 944262   | 425 | 055738    | 40   |  |  |  |  |  |  |  |
| 21  | 9-819976 | 239 | 9-875459 | 185 | 9-944517 | 425 | 10-055483 | 39   |  |  |  |  |  |  |  |
| 22  | 820120   | 239 | 875348   | 185 | 944771   | 424 | 055229    | 38   |  |  |  |  |  |  |  |
| 23  | 820263   | 239 | 875237   | 185 | 945026   | 424 | 054974    | 37   |  |  |  |  |  |  |  |
| 24  | 820406   | 239 | 875126   | 186 | 945281   | 424 | 054719    | 36   |  |  |  |  |  |  |  |
| 25  | 820550   | 238 | 875014   | 186 | 945535   | 424 | 054465    | 35   |  |  |  |  |  |  |  |
| 26  | 820693   | 238 | 874903   | 186 | 945790   | 424 | 054210    | 34   |  |  |  |  |  |  |  |
| 27  | 820836   | 238 | 874791   | 186 | 946045   | 424 | 053955    | 33   |  |  |  |  |  |  |  |
| 28  | 820979   | 238 | 874680   | 186 | 946299   | 424 | 053701    | 32   |  |  |  |  |  |  |  |
| 29  | 821122   | 238 | 874568   | 186 | 946554   | 424 | 053446    | 31   |  |  |  |  |  |  |  |
| 30  | 821265   | 238 | 874456   | 186 | 946808   | 424 | 053192    | 30   |  |  |  |  |  |  |  |
| 31  | 9-821407 | 238 | 9-874344 | 186 | 9-947063 | 424 | 10-052937 | 29   |  |  |  |  |  |  |  |
| 32  | 821550   | 238 | 874232   | 187 | 947318   | 424 | 052682    | 28   |  |  |  |  |  |  |  |
| 33  | 821693   | 237 | 874121   | 187 | 947572   | 424 | 052428    | 27   |  |  |  |  |  |  |  |
| 34  | 821835   | 237 | 874009   | 187 | 947827   | 424 | 052173    | 26   |  |  |  |  |  |  |  |
| 35  | 821977   | 237 | 873896   | 187 | 948081   | 424 | 051919    | 25   |  |  |  |  |  |  |  |
| 36  | 822120   | 237 | 873784   | 187 | 948335   | 424 | 051665    | 24   |  |  |  |  |  |  |  |
| 37  | 822262   | 237 | 873672   | 187 | 948590   | 424 | 051410    | 23   |  |  |  |  |  |  |  |
| 38  | 822404   | 237 | 873560   | 187 | 948844   | 424 | 051156    | 22   |  |  |  |  |  |  |  |
| 39  | 822546   | 237 | 873448   | 187 | 949099   | 424 | 050901    | 21   |  |  |  |  |  |  |  |
| 40  | 822688   | 236 | 873335   | 187 | 949353   | 424 | 050647    | 20   |  |  |  |  |  |  |  |
| 41  | 9-822830 | 236 | 9-873223 | 187 | 9-949608 | 424 | 10-050392 | 19   |  |  |  |  |  |  |  |
| 42  | 822972   | 236 | 873110   | 188 | 949862   | 424 | 050138    | 18   |  |  |  |  |  |  |  |
| 43  | 823114   | 236 | 872998   | 188 | 950116   | 424 | 049884    | 17   |  |  |  |  |  |  |  |
| 44  | 823255   | 236 | 872885   | 188 | 950371   | 424 | 049629    | 16   |  |  |  |  |  |  |  |
| 45  | 823397   | 236 | 872772   | 188 | 950625   | 424 | 049375    | 15   |  |  |  |  |  |  |  |
| 46  | 823539   | 236 | 872659   | 188 | 950879   | 424 | 049121    | 14   |  |  |  |  |  |  |  |
| 47  | 823680   | 235 | 872547   | 188 | 951133   | 424 | 048867    | 13   |  |  |  |  |  |  |  |
| 48  | 823821   | 235 | 872434   | 188 | 951388   | 424 | 048612    | 12   |  |  |  |  |  |  |  |
| 49  | 823963   | 235 | 872321   | 188 | 951642   | 424 | 048358    | 11   |  |  |  |  |  |  |  |
| 50  | 824104   | 235 | 872208   | 188 | 951896   | 424 | 048104    | 10   |  |  |  |  |  |  |  |
| 51  | 9-824245 | 235 | 9-872095 | 189 | 9-952150 | 424 | 10-047850 | 9    |  |  |  |  |  |  |  |
| 52  | 824386   | 235 | 871981   | 189 | 952405   | 424 | 047595    | 8    |  |  |  |  |  |  |  |
| 53  | 824527   | 235 | 871868   | 189 | 952659   | 424 | 047341    | 7    |  |  |  |  |  |  |  |
| 54  | 824668   | 234 | 871755   | 189 | 952913   | 424 | 047087    | 6    |  |  |  |  |  |  |  |
| 55  | 824808   | 234 | 871641   | 189 | 953167   | 423 | 046833    | 5    |  |  |  |  |  |  |  |
| 56  | 824949   | 234 | 871528   | 189 | 953421   | 423 | 046579    | 4    |  |  |  |  |  |  |  |
| 57  | 825090   | 234 | 871414   | 189 | 953675   | 423 | 046325    | 3    |  |  |  |  |  |  |  |
| 58  | 825230   | 234 | 871301   | 189 | 953929   | 423 | 046071    | 2    |  |  |  |  |  |  |  |
| 59  | 825371   | 234 | 871187   | 189 | 954183   | 423 | 045817    | 1    |  |  |  |  |  |  |  |
| 60  | 825511   | 234 | 871073   | 190 | 954437   | 423 | 045563    | 0    |  |  |  |  |  |  |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

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139°

| /  | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
|----|----------|-----|----------|-----|----------|-----|-----------|----|
| 0  | 9-808067 | 251 | 9-884254 | 177 | 9-923814 | 427 | 10-076186 | 60 |
| 1  | 808218   | 251 | 884148   | 177 | 924070   | 427 | 075930    | 59 |
| 2  | 808368   | 251 | 884042   | 177 | 924327   | 427 | 075673    | 58 |
| 3  | 808519   | 250 | 883936   | 177 | 924583   | 427 | 075417    | 57 |
| 4  | 808669   | 250 | 883829   | 177 | 924840   | 427 | 075160    | 56 |
| 5  | 808819   | 250 | 883723   | 177 | 925096   | 427 | 074904    | 55 |
| 6  | 808969   | 250 | 883617   | 177 | 925352   | 427 | 074648    | 54 |
| 7  | 809119   | 250 | 883510   | 177 | 925609   | 427 | 074391    | 53 |
| 8  | 809269   | 250 | 883404   | 177 | 925865   | 427 | 074135    | 52 |
| 9  | 809419   | 249 | 883297   | 178 | 926122   | 427 | 073878    | 51 |
| 10 | 809569   | 249 | 883191   | 178 | 926378   | 427 | 073622    | 50 |
| 11 | 9-809718 | 249 | 9-883084 | 178 | 9-926634 | 427 | 10-073366 | 49 |
| 12 | 809868   | 249 | 882977   | 178 | 926890   | 427 | 073110    | 48 |
| 13 | 810017   | 249 | 882871   | 178 | 927147   | 427 | 072853    | 47 |
| 14 | 810167   | 249 | 882764   | 178 | 927403   | 427 | 072597    | 46 |
| 15 | 810316   | 248 | 882657   | 178 | 927659   | 427 | 072341    | 45 |
| 16 | 810465   | 248 | 882550   | 178 | 927915   | 427 | 072085    | 44 |
| 17 | 810614   | 248 | 882443   | 178 | 928171   | 427 | 071829    | 43 |
| 18 | 810763   | 248 | 882336   | 179 | 928427   | 427 | 071573    | 42 |
| 19 | 810912   | 248 | 882229   | 179 | 928684   | 427 | 071316    | 41 |
| 20 | 811061   | 248 | 882121   | 179 | 928940   | 427 | 071060    | 40 |
| 21 | 9-811210 | 248 | 9-882014 | 179 | 9-929196 | 427 | 10-070804 | 39 |
| 22 | 811358   | 247 | 881907   | 179 | 929452   | 427 | 070548    | 38 |
| 23 | 811507   | 247 | 881799   | 179 | 929708   | 427 | 070292    | 37 |
| 24 | 811655   | 247 | 881692   | 179 | 929964   | 426 | 070036    | 36 |
| 25 | 811804   | 247 | 881584   | 179 | 930220   | 426 | 069780    | 35 |
| 26 | 811952   | 247 | 881477   | 179 | 930475   | 426 | 069525    | 34 |
| 27 | 812100   | 247 | 881369   | 179 | 930731   | 426 | 069269    | 33 |
| 28 | 812248   | 247 | 881261   | 180 | 930987   | 426 | 069013    | 32 |
| 29 | 812396   | 246 | 881153   | 180 | 931243   | 426 | 068757    | 31 |
| 30 | 812544   | 246 | 881046   | 180 | 931499   | 426 | 068501    | 30 |
| 31 | 9-812692 | 246 | 9-880938 | 180 | 9-931755 | 426 | 10-068245 | 29 |
| 32 | 812840   | 246 | 880830   | 180 | 932010   | 426 | 067990    | 28 |
| 33 | 812988   | 246 | 880722   | 180 | 932266   | 426 | 067734    | 27 |
| 34 | 813135   | 246 | 880613   | 180 | 932522   | 426 | 067478    | 26 |
| 35 | 813283   | 246 | 880505   | 180 | 932778   | 426 | 067222    | 25 |
| 36 | 813430   | 245 | 880397   | 180 | 933033   | 426 | 066967    | 24 |
| 37 | 813578   | 245 | 880289   | 181 | 933289   | 426 | 066711    | 23 |
| 38 | 813725   | 245 | 880180   | 181 | 933545   | 426 | 066455    | 22 |
| 39 | 813872   | 245 | 880072   | 181 | 933800   | 426 | 066200    | 21 |
| 40 | 814019   | 245 | 879963   | 181 | 934056   | 426 | 065944    | 20 |
| 41 | 9-814166 | 245 | 9-879855 | 181 | 9-934311 | 426 | 10-065689 | 19 |
| 42 | 814313   | 245 | 879746   | 181 | 934567   | 426 | 065433    | 18 |
| 43 | 814460   | 244 | 879637   | 181 | 934822   | 426 | 065178    | 17 |
| 44 | 814607   | 244 | 879529   | 181 | 935078   | 426 | 064922    | 16 |
| 45 | 814753   | 244 | 879420   | 181 | 935333   | 426 | 064667    | 15 |
| 46 | 814900   | 244 | 879311   | 181 | 935589   | 426 | 064411    | 14 |
| 47 | 815046   | 244 | 879202   | 182 | 935844   | 426 | 064156    | 13 |
| 48 | 815193   | 244 | 879093   | 182 | 936100   | 426 | 063900    | 12 |
| 49 | 815339   | 244 | 878984   | 182 | 936355   | 426 | 063645    | 11 |
| 50 | 815485   | 243 | 878875   | 182 | 936611   | 426 | 063389    | 10 |
| 51 | 9-815631 | 243 | 9-878766 | 182 | 9-936866 | 425 | 10-063134 | 9  |
| 52 | 815778   | 243 | 878656   | 182 | 937121   | 425 | 062879    | 8  |
| 53 | 815924   | 243 | 878547   | 182 | 937377   | 425 | 062623    | 7  |
| 54 | 816069   | 243 | 878438   | 182 | 937632   | 425 | 062368    | 6  |
| 55 | 816215   | 243 | 878328   | 182 | 937887   | 425 | 062113    | 5  |
| 56 | 816361   | 243 | 878219   | 183 | 938142   | 425 | 061858    | 4  |
| 57 | 816507   | 242 | 878109   | 183 | 938398   | 425 | 061602    | 3  |
| 58 | 816652   | 242 | 877999   | 183 | 938653   | 425 | 061347    | 2  |
| 59 | 816798   | 242 | 877890   | 183 | 938908   | 425 | 061092    | 1  |
| 60 | 816943   | 242 | 877780   | 183 | 939163   | 425 | 060837    | 0  |
| /  | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 41° |          |     |          |     |          |     |           | 138° |  |  |  |  |  |  |  |
|-----|----------|-----|----------|-----|----------|-----|-----------|------|--|--|--|--|--|--|--|
| /   | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /    |  |  |  |  |  |  |  |
| 0   | 9-816943 | 242 | 9-877780 | 183 | 9-939163 | 425 | 10-060837 | 60   |  |  |  |  |  |  |  |
| 1   | 817088   | 242 | 877670   | 183 | 939418   | 425 | 060582    | 59   |  |  |  |  |  |  |  |
| 2   | 817233   | 242 | 877560   | 183 | 939673   | 425 | 060327    | 58   |  |  |  |  |  |  |  |
| 3   | 817379   | 242 | 877450   | 183 | 939928   | 425 | 060072    | 57   |  |  |  |  |  |  |  |
| 4   | 817524   | 241 | 877340   | 183 | 940183   | 425 | 059817    | 56   |  |  |  |  |  |  |  |
| 5   | 817668   | 241 | 877230   | 184 | 940439   | 425 | 059561    | 55   |  |  |  |  |  |  |  |
| 6   | 817813   | 241 | 877120   | 184 | 940694   | 425 | 059306    | 54   |  |  |  |  |  |  |  |
| 7   | 817958   | 241 | 877010   | 184 | 940949   | 425 | 059051    | 53   |  |  |  |  |  |  |  |
| 8   | 818103   | 241 | 876899   | 184 | 941204   | 425 | 058796    | 52   |  |  |  |  |  |  |  |
| 9   | 818247   | 241 | 876789   | 184 | 941459   | 425 | 058541    | 51   |  |  |  |  |  |  |  |
| 10  | 818392   | 241 | 876678   | 184 | 941713   | 425 | 058287    | 50   |  |  |  |  |  |  |  |
| 11  | 9-818536 | 240 | 9-876568 | 184 | 9-941968 | 425 | 10-058032 | 49   |  |  |  |  |  |  |  |
| 12  | 818681   | 240 | 876457   | 184 | 942223   | 425 | 057777    | 48   |  |  |  |  |  |  |  |
| 13  | 818825   | 240 | 876347   | 184 | 942478   | 425 | 057522    | 47   |  |  |  |  |  |  |  |
| 14  | 818969   | 240 | 876236   | 185 | 942733   | 425 | 057267    | 46   |  |  |  |  |  |  |  |
| 15  | 819113   | 240 | 876125   | 185 | 942988   | 425 | 057012    | 45   |  |  |  |  |  |  |  |
| 16  | 819257   | 240 | 876014   | 185 | 943243   | 425 | 056757    | 44   |  |  |  |  |  |  |  |
| 17  | 819401   | 240 | 875904   | 185 | 943498   | 425 | 056502    | 43   |  |  |  |  |  |  |  |
| 18  | 819545   | 239 | 875793   | 185 | 943752   | 425 | 056248    | 42   |  |  |  |  |  |  |  |
| 19  | 819689   | 239 | 875682   | 185 | 944007   | 425 | 055993    | 41   |  |  |  |  |  |  |  |
| 20  | 819832   | 239 | 875571   | 185 | 944262   | 425 | 055738    | 40   |  |  |  |  |  |  |  |
| 21  | 9-819976 | 239 | 9-875459 | 185 | 9-944517 | 425 | 10-055483 | 39   |  |  |  |  |  |  |  |
| 22  | 820120   | 239 | 875348   | 185 | 944771   | 424 | 055229    | 38   |  |  |  |  |  |  |  |
| 23  | 820263   | 239 | 875237   | 185 | 945026   | 424 | 054974    | 37   |  |  |  |  |  |  |  |
| 24  | 820406   | 239 | 875126   | 186 | 945281   | 424 | 054719    | 36   |  |  |  |  |  |  |  |
| 25  | 820550   | 238 | 875014   | 186 | 945535   | 424 | 054465    | 35   |  |  |  |  |  |  |  |
| 26  | 820693   | 238 | 874903   | 186 | 945790   | 424 | 054210    | 34   |  |  |  |  |  |  |  |
| 27  | 820836   | 238 | 874791   | 186 | 946045   | 424 | 053955    | 33   |  |  |  |  |  |  |  |
| 28  | 820979   | 238 | 874680   | 186 | 946300   | 424 | 053701    | 32   |  |  |  |  |  |  |  |
| 29  | 821122   | 238 | 874568   | 186 | 946554   | 424 | 053446    | 31   |  |  |  |  |  |  |  |
| 30  | 821265   | 238 | 874456   | 186 | 946808   | 424 | 053192    | 30   |  |  |  |  |  |  |  |
| 31  | 9-821407 | 238 | 9-874344 | 186 | 9-947063 | 424 | 10-052937 | 29   |  |  |  |  |  |  |  |
| 32  | 821550   | 238 | 874232   | 187 | 947318   | 424 | 052682    | 28   |  |  |  |  |  |  |  |
| 33  | 821693   | 237 | 874121   | 187 | 947572   | 424 | 052428    | 27   |  |  |  |  |  |  |  |
| 34  | 821835   | 237 | 874009   | 187 | 947827   | 424 | 052173    | 26   |  |  |  |  |  |  |  |
| 35  | 821977   | 237 | 873896   | 187 | 948081   | 424 | 051919    | 25   |  |  |  |  |  |  |  |
| 36  | 822120   | 237 | 873784   | 187 | 948335   | 424 | 051665    | 24   |  |  |  |  |  |  |  |
| 37  | 822262   | 237 | 873672   | 187 | 948590   | 424 | 051410    | 23   |  |  |  |  |  |  |  |
| 38  | 822404   | 237 | 873560   | 187 | 948844   | 424 | 051156    | 22   |  |  |  |  |  |  |  |
| 39  | 822546   | 237 | 873448   | 187 | 949099   | 424 | 050901    | 21   |  |  |  |  |  |  |  |
| 40  | 822688   | 236 | 873335   | 187 | 949353   | 424 | 050647    | 20   |  |  |  |  |  |  |  |
| 41  | 9-822830 | 236 | 9-873223 | 187 | 9-949608 | 424 | 10-050392 | 19   |  |  |  |  |  |  |  |
| 42  | 822972   | 236 | 873110   | 188 | 949862   | 424 | 050138    | 18   |  |  |  |  |  |  |  |
| 43  | 823114   | 236 | 872998   | 188 | 950116   | 424 | 049884    | 17   |  |  |  |  |  |  |  |
| 44  | 823255   | 236 | 872885   | 188 | 950371   | 424 | 049629    | 16   |  |  |  |  |  |  |  |
| 45  | 823397   | 236 | 872772   | 188 | 950625   | 424 | 049375    | 15   |  |  |  |  |  |  |  |
| 46  | 823539   | 236 | 872659   | 188 | 950879   | 424 | 049121    | 14   |  |  |  |  |  |  |  |
| 47  | 823680   | 235 | 872547   | 188 | 951133   | 424 | 048867    | 13   |  |  |  |  |  |  |  |
| 48  | 823821   | 235 | 872434   | 188 | 951388   | 424 | 048612    | 12   |  |  |  |  |  |  |  |
| 49  | 823963   | 235 | 872321   | 188 | 951642   | 424 | 048358    | 11   |  |  |  |  |  |  |  |
| 50  | 824104   | 235 | 872208   | 188 | 951896   | 424 | 048104    | 10   |  |  |  |  |  |  |  |
| 51  | 9-824245 | 235 | 9-872095 | 189 | 9-952150 | 424 | 10-047850 | 9    |  |  |  |  |  |  |  |
| 52  | 824386   | 235 | 871981   | 189 | 952405   | 424 | 047595    | 8    |  |  |  |  |  |  |  |
| 53  | 824527   | 235 | 871868   | 189 | 952659   | 424 | 047341    | 7    |  |  |  |  |  |  |  |
| 54  | 824668   | 234 | 871755   | 189 | 952913   | 424 | 047087    | 6    |  |  |  |  |  |  |  |
| 55  | 824808   | 234 | 871641   | 189 | 953167   | 423 | 046833    | 5    |  |  |  |  |  |  |  |
| 56  | 824949   | 234 | 871528   | 189 | 953421   | 423 | 046579    | 4    |  |  |  |  |  |  |  |
| 57  | 825090   | 234 | 871414   | 189 | 953675   | 423 | 046325    | 3    |  |  |  |  |  |  |  |
| 58  | 825230   | 234 | 871301   | 189 | 953929   | 423 | 046071    | 2    |  |  |  |  |  |  |  |
| 59  | 825371   | 234 | 871187   | 189 | 954183   | 423 | 045817    | 1    |  |  |  |  |  |  |  |
| 60  | 825511   | 234 | 871073   | 190 | 954437   | 423 | 045563    | 0    |  |  |  |  |  |  |  |
| /   | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /    |  |  |  |  |  |  |  |

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TABLE II. LOGARITHMIC SINES, TANGENTS, ETC.

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| 48°  |          |     |          |     |          |     | 186°      |    |
|------|----------|-----|----------|-----|----------|-----|-----------|----|
| /    | Sine.    | D.  | Cosine.  | D.  | Tang.    | D.  | Cotang.   | /  |
| 0    | 9.833783 | 226 | 9.864127 | 196 | 9.969656 | 422 | 10.030344 | 60 |
| 1    | 833919   | 225 | 864010   | 196 | 969909   | 422 | 030091    | 59 |
| 2    | 834054   | 225 | 863892   | 197 | 970162   | 422 | 029838    | 58 |
| 3    | 834189   | 225 | 863774   | 197 | 970416   | 422 | 029584    | 57 |
| 4    | 834325   | 225 | 863656   | 197 | 970669   | 422 | 029331    | 56 |
| 5    | 834460   | 225 | 863538   | 197 | 970922   | 422 | 029078    | 55 |
| 6    | 834595   | 225 | 863419   | 197 | 971175   | 422 | 028825    | 54 |
| 7    | 834730   | 225 | 863301   | 197 | 971429   | 422 | 028571    | 53 |
| 8    | 834865   | 225 | 863183   | 197 | 971682   | 422 | 028318    | 52 |
| 9    | 834999   | 224 | 863064   | 197 | 971935   | 422 | 028065    | 51 |
| 10   | 835134   | 224 | 862946   | 198 | 972188   | 422 | 027812    | 50 |
| 11   | 9.835269 | 224 | 9.862827 | 198 | 9.972441 | 422 | 10.027559 | 49 |
| 12   | 835403   | 224 | 862709   | 198 | 972695   | 422 | 027305    | 48 |
| 13   | 835538   | 224 | 862590   | 198 | 972948   | 422 | 027052    | 47 |
| 14   | 835672   | 224 | 862471   | 198 | 973201   | 422 | 026799    | 46 |
| 15   | 835807   | 224 | 862353   | 198 | 973454   | 422 | 026546    | 45 |
| 16   | 835941   | 224 | 862234   | 198 | 973707   | 422 | 026293    | 44 |
| 17   | 836075   | 223 | 862115   | 198 | 973960   | 422 | 026040    | 43 |
| 18   | 836209   | 223 | 861996   | 198 | 974213   | 422 | 025787    | 42 |
| 19   | 836343   | 223 | 861877   | 198 | 974466   | 422 | 025534    | 41 |
| 20   | 836477   | 223 | 861758   | 199 | 974720   | 422 | 025280    | 40 |
| 21   | 9.836611 | 223 | 9.861638 | 199 | 9.974973 | 422 | 10.025027 | 39 |
| 22   | 836745   | 223 | 861519   | 199 | 975226   | 422 | 024774    | 38 |
| 23   | 836878   | 223 | 861400   | 199 | 975479   | 422 | 024521    | 37 |
| 24   | 837012   | 222 | 861280   | 199 | 975732   | 422 | 024268    | 36 |
| 25   | 837146   | 222 | 861161   | 199 | 975985   | 422 | 024015    | 35 |
| 26   | 837279   | 222 | 861041   | 199 | 976238   | 422 | 023762    | 34 |
| 27   | 837412   | 222 | 860922   | 199 | 976491   | 422 | 023509    | 33 |
| 28   | 837546   | 222 | 860802   | 199 | 976744   | 422 | 023256    | 32 |
| 29   | 837679   | 222 | 860682   | 200 | 976997   | 422 | 023003    | 31 |
| 30   | 837812   | 222 | 860562   | 200 | 977250   | 422 | 022750    | 30 |
| 31   | 9.837945 | 222 | 9.860442 | 200 | 9.977503 | 422 | 10.022497 | 29 |
| 32   | 838078   | 221 | 860322   | 200 | 977756   | 422 | 022244    | 28 |
| 33   | 838211   | 221 | 860202   | 200 | 978009   | 422 | 021991    | 27 |
| 34   | 838344   | 221 | 860082   | 200 | 978262   | 422 | 021738    | 26 |
| 35   | 838477   | 221 | 859962   | 200 | 978515   | 422 | 021485    | 25 |
| 36   | 838610   | 221 | 859842   | 200 | 978768   | 422 | 021232    | 24 |
| 37   | 838742   | 221 | 859721   | 201 | 979021   | 422 | 020979    | 23 |
| 38   | 838875   | 221 | 859601   | 201 | 979274   | 422 | 020726    | 22 |
| 39   | 839007   | 221 | 859480   | 201 | 979527   | 422 | 020473    | 21 |
| 40   | 839140   | 220 | 859360   | 201 | 979780   | 422 | 020220    | 20 |
| 41   | 9.839272 | 220 | 9.859239 | 201 | 9.980033 | 422 | 10.019967 | 19 |
| 42   | 839404   | 220 | 859119   | 201 | 980286   | 422 | 019714    | 18 |
| 43   | 839536   | 220 | 858998   | 201 | 980538   | 422 | 019462    | 17 |
| 44   | 839668   | 220 | 858877   | 201 | 980791   | 421 | 019209    | 16 |
| 45   | 839800   | 220 | 858756   | 202 | 981044   | 421 | 018956    | 15 |
| 46   | 839932   | 220 | 858635   | 202 | 981297   | 421 | 018703    | 14 |
| 47   | 840064   | 219 | 858514   | 202 | 981550   | 421 | 018450    | 13 |
| 48   | 840196   | 219 | 858393   | 202 | 981803   | 421 | 018197    | 12 |
| 49   | 840328   | 219 | 858272   | 202 | 982056   | 421 | 017944    | 11 |
| 50   | 840459   | 219 | 858151   | 202 | 982309   | 421 | 017691    | 10 |
| 51   | 9.840591 | 219 | 9.858029 | 202 | 9.982562 | 421 | 10.017438 | 9  |
| 52   | 840722   | 219 | 857908   | 202 | 982814   | 421 | 017186    | 8  |
| 53   | 840854   | 219 | 857786   | 202 | 983067   | 421 | 016933    | 7  |
| 54   | 840985   | 219 | 857665   | 203 | 983320   | 421 | 016680    | 6  |
| 55   | 841116   | 218 | 857543   | 203 | 983573   | 421 | 016427    | 5  |
| 56   | 841247   | 218 | 857422   | 203 | 983826   | 421 | 016174    | 4  |
| 57   | 841378   | 218 | 857300   | 203 | 984079   | 421 | 015921    | 3  |
| 58   | 841509   | 218 | 857178   | 203 | 984332   | 421 | 015668    | 2  |
| 59   | 841640   | 218 | 857056   | 203 | 984584   | 421 | 015416    | 1  |
| 60   | 841771   | 218 | 856934   | 203 | 984837   | 421 | 015163    | 0  |
| /    | Cosine.  | D.  | Sine.    | D.  | Cotang.  | D.  | Tang.     | /  |
| 188° |          |     |          |     |          |     | 46°       |    |

| °  | 20°      |          | 21°      |          | 22°      |          | 23°      |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 36397    | 2.74748  | 38386    | 2.60509  | 40403    | 2.47509  | 42447    | 2.35585  | 60 |
| 1  | 36430    | 2.74499  | 38420    | 2.60283  | 40436    | 2.47302  | 42482    | 2.35395  | 59 |
| 2  | 36463    | 2.74251  | 38453    | 2.60057  | 40470    | 2.47095  | 42516    | 2.35205  | 58 |
| 3  | 36496    | 2.74004  | 38487    | 2.59831  | 40504    | 2.46888  | 42551    | 2.35015  | 57 |
| 4  | 36529    | 2.73756  | 38520    | 2.59606  | 40538    | 2.46682  | 42585    | 2.34825  | 56 |
| 5  | 36562    | 2.73509  | 38553    | 2.59381  | 40572    | 2.46476  | 42619    | 2.34636  | 55 |
| 6  | 36595    | 2.73263  | 38587    | 2.59156  | 40606    | 2.46270  | 42654    | 2.34447  | 54 |
| 7  | 36628    | 2.73017  | 38620    | 2.58932  | 40640    | 2.46065  | 42688    | 2.34258  | 53 |
| 8  | 36661    | 2.72771  | 38654    | 2.58708  | 40674    | 2.45860  | 42722    | 2.34069  | 52 |
| 9  | 36694    | 2.72526  | 38687    | 2.58484  | 40707    | 2.45655  | 42757    | 2.33881  | 51 |
| 10 | 36727    | 2.72281  | 38721    | 2.58261  | 40741    | 2.45451  | 42791    | 2.33693  | 50 |
| 11 | 36760    | 2.72036  | 38754    | 2.58038  | 40775    | 2.45246  | 42826    | 2.33505  | 49 |
| 12 | 36793    | 2.71792  | 38787    | 2.57815  | 40809    | 2.45043  | 42860    | 2.33317  | 48 |
| 13 | 36826    | 2.71548  | 38821    | 2.57593  | 40843    | 2.44839  | 42894    | 2.33130  | 47 |
| 14 | 36859    | 2.71305  | 38854    | 2.57371  | 40877    | 2.44636  | 42929    | 2.32943  | 46 |
| 15 | 36892    | 2.71062  | 38888    | 2.57150  | 40911    | 2.44433  | 42963    | 2.32756  | 45 |
| 16 | 36925    | 2.70819  | 38921    | 2.56928  | 40945    | 2.44230  | 42998    | 2.32570  | 44 |
| 17 | 36958    | 2.70577  | 38955    | 2.56707  | 40979    | 2.44027  | 43032    | 2.32383  | 43 |
| 18 | 36991    | 2.70335  | 38988    | 2.56487  | 41013    | 2.43825  | 43067    | 2.32197  | 42 |
| 19 | 37024    | 2.70094  | 39022    | 2.56266  | 41047    | 2.43623  | 43101    | 2.32012  | 41 |
| 20 | 37057    | 2.69853  | 39055    | 2.56046  | 41081    | 2.43422  | 43136    | 2.31826  | 40 |
| 21 | 37090    | 2.69612  | 39089    | 2.55827  | 41115    | 2.43220  | 43170    | 2.31641  | 39 |
| 22 | 37124    | 2.69371  | 39122    | 2.55608  | 41149    | 2.43019  | 43205    | 2.31456  | 38 |
| 23 | 37157    | 2.69131  | 39156    | 2.55389  | 41183    | 2.42819  | 43239    | 2.31271  | 37 |
| 24 | 37190    | 2.68892  | 39190    | 2.55170  | 41217    | 2.42618  | 43274    | 2.31086  | 36 |
| 25 | 37223    | 2.68653  | 39223    | 2.54952  | 41251    | 2.42418  | 43308    | 2.30902  | 35 |
| 26 | 37256    | 2.68414  | 39257    | 2.54734  | 41285    | 2.42218  | 43343    | 2.30718  | 34 |
| 27 | 37289    | 2.68175  | 39290    | 2.54516  | 41319    | 2.42019  | 43378    | 2.30534  | 33 |
| 28 | 37322    | 2.67937  | 39324    | 2.54299  | 41353    | 2.41819  | 43412    | 2.30351  | 32 |
| 29 | 37355    | 2.67700  | 39357    | 2.54082  | 41387    | 2.41620  | 43447    | 2.30167  | 31 |
| 30 | 37388    | 2.67462  | 39391    | 2.53865  | 41421    | 2.41421  | 43481    | 2.29984  | 30 |
| 31 | 37422    | 2.67225  | 39425    | 2.53648  | 41455    | 2.41223  | 43516    | 2.29801  | 29 |
| 32 | 37455    | 2.66989  | 39458    | 2.53432  | 41490    | 2.41025  | 43550    | 2.29619  | 28 |
| 33 | 37488    | 2.66752  | 39492    | 2.53217  | 41524    | 2.40827  | 43585    | 2.29437  | 27 |
| 34 | 37521    | 2.66516  | 39526    | 2.53001  | 41558    | 2.40629  | 43620    | 2.29254  | 26 |
| 35 | 37554    | 2.66281  | 39559    | 2.52786  | 41592    | 2.40432  | 43654    | 2.29073  | 25 |
| 36 | 37588    | 2.66046  | 39593    | 2.52571  | 41626    | 2.40235  | 43689    | 2.28891  | 24 |
| 37 | 37621    | 2.65811  | 39626    | 2.52357  | 41660    | 2.40038  | 43724    | 2.28710  | 23 |
| 38 | 37654    | 2.65576  | 39660    | 2.52142  | 41694    | 2.39841  | 43758    | 2.28528  | 22 |
| 39 | 37687    | 2.65342  | 39694    | 2.51929  | 41728    | 2.39645  | 43793    | 2.28348  | 21 |
| 40 | 37720    | 2.65109  | 39727    | 2.51715  | 41763    | 2.39449  | 43828    | 2.28167  | 20 |
| 41 | 37754    | 2.64875  | 39761    | 2.51502  | 41797    | 2.39253  | 43862    | 2.27987  | 19 |
| 42 | 37787    | 2.64642  | 39795    | 2.51289  | 41831    | 2.39058  | 43897    | 2.27806  | 18 |
| 43 | 37820    | 2.64410  | 39829    | 2.51076  | 41865    | 2.38862  | 43932    | 2.27626  | 17 |
| 44 | 37853    | 2.64177  | 39862    | 2.50864  | 41899    | 2.38668  | 43966    | 2.27447  | 16 |
| 45 | 37887    | 2.63945  | 39896    | 2.50652  | 41933    | 2.38473  | 44001    | 2.27267  | 15 |
| 46 | 37920    | 2.63714  | 39930    | 2.50440  | 41968    | 2.38279  | 44036    | 2.27088  | 14 |
| 47 | 37953    | 2.63483  | 39963    | 2.50229  | 42002    | 2.38084  | 44071    | 2.26909  | 13 |
| 48 | 37986    | 2.63252  | 39997    | 2.50018  | 42036    | 2.37891  | 44105    | 2.26730  | 12 |
| 49 | 38020    | 2.63021  | 40031    | 2.49807  | 42070    | 2.37697  | 44140    | 2.26552  | 11 |
| 50 | 38053    | 2.62791  | 40065    | 2.49597  | 42105    | 2.37504  | 44175    | 2.26374  | 10 |
| 51 | 38086    | 2.62561  | 40099    | 2.49386  | 42139    | 2.37311  | 44210    | 2.26196  | 9  |
| 52 | 38120    | 2.62332  | 40132    | 2.49177  | 42173    | 2.37118  | 44244    | 2.26018  | 8  |
| 53 | 38153    | 2.62103  | 40166    | 2.48967  | 42207    | 2.36925  | 44279    | 2.25840  | 7  |
| 54 | 38186    | 2.61874  | 40200    | 2.48758  | 42242    | 2.36733  | 44314    | 2.25663  | 6  |
| 55 | 38220    | 2.61646  | 40234    | 2.48549  | 42276    | 2.36541  | 44349    | 2.25486  | 5  |
| 56 | 38253    | 2.61418  | 40267    | 2.48340  | 42310    | 2.36349  | 44384    | 2.25309  | 4  |
| 57 | 38286    | 2.61190  | 40301    | 2.48132  | 42345    | 2.36158  | 44418    | 2.25132  | 3  |
| 58 | 38320    | 2.60963  | 40335    | 2.47924  | 42379    | 2.35967  | 44453    | 2.24956  | 2  |
| 59 | 38353    | 2.60736  | 40369    | 2.47716  | 42413    | 2.35776  | 44488    | 2.24780  | 1  |
| 60 | 38386    | 2.60509  | 40403    | 2.47509  | 42447    | 2.35585  | 44523    | 2.24604  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 69°      |          | 68°      |          | 67°      |          | 66°      |          |    |

TABLE III. NATURAL TANGENTS AND COTANGENTS.

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| °  | 24°      |          | 25°      |          | 26°      |          | 27°      |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 44523    | 2.24604  | 46631    | 2.14451  | 48773    | 2.05230  | 50953    | 1.96261  | 60 |
| 1  | 44558    | 2.24428  | 46666    | 2.14288  | 48809    | 2.04879  | 50989    | 1.96120  | 59 |
| 2  | 44593    | 2.24252  | 46702    | 2.14125  | 48845    | 2.04728  | 51026    | 1.95979  | 58 |
| 3  | 44627    | 2.24077  | 46737    | 2.13963  | 48881    | 2.04577  | 51063    | 1.95838  | 57 |
| 4  | 44662    | 2.23902  | 46772    | 2.13801  | 48917    | 2.04426  | 51099    | 1.95698  | 56 |
| 5  | 44697    | 2.23727  | 46808    | 2.13639  | 48953    | 2.04276  | 51136    | 1.95557  | 55 |
| 6  | 44732    | 2.23553  | 46843    | 2.13477  | 48989    | 2.04125  | 51173    | 1.95417  | 54 |
| 7  | 44767    | 2.23378  | 46879    | 2.13316  | 49026    | 2.03975  | 51209    | 1.95277  | 53 |
| 8  | 44802    | 2.23204  | 46914    | 2.13154  | 49062    | 2.03825  | 51246    | 1.95137  | 52 |
| 9  | 44837    | 2.23030  | 46950    | 2.12993  | 49098    | 2.03675  | 51283    | 1.94997  | 51 |
| 10 | 44872    | 2.22857  | 46985    | 2.12832  | 49134    | 2.03526  | 51319    | 1.94858  | 50 |
| 11 | 44907    | 2.22683  | 47021    | 2.12671  | 49170    | 2.03376  | 51356    | 1.94718  | 49 |
| 12 | 44942    | 2.22510  | 47056    | 2.12511  | 49206    | 2.03227  | 51393    | 1.94579  | 48 |
| 13 | 44977    | 2.22337  | 47092    | 2.12350  | 49242    | 2.03078  | 51430    | 1.94440  | 47 |
| 14 | 45012    | 2.22164  | 47128    | 2.12190  | 49278    | 2.02929  | 51467    | 1.94301  | 46 |
| 15 | 45047    | 2.21992  | 47163    | 2.12030  | 49315    | 2.02780  | 51503    | 1.94162  | 45 |
| 16 | 45082    | 2.21819  | 47199    | 2.11871  | 49351    | 2.02631  | 51540    | 1.94023  | 44 |
| 17 | 45117    | 2.21647  | 47234    | 2.11711  | 49387    | 2.02483  | 51577    | 1.93885  | 43 |
| 18 | 45152    | 2.21475  | 47270    | 2.11552  | 49423    | 2.02335  | 51614    | 1.93746  | 42 |
| 19 | 45187    | 2.21304  | 47305    | 2.11392  | 49459    | 2.02187  | 51651    | 1.93608  | 41 |
| 20 | 45222    | 2.21132  | 47341    | 2.11233  | 49495    | 2.02039  | 51688    | 1.93470  | 40 |
| 21 | 45257    | 2.20961  | 47377    | 2.11075  | 49532    | 2.01891  | 51724    | 1.93332  | 39 |
| 22 | 45292    | 2.20790  | 47412    | 2.10916  | 49568    | 2.01743  | 51761    | 1.93195  | 38 |
| 23 | 45327    | 2.20619  | 47448    | 2.10758  | 49604    | 2.01596  | 51798    | 1.93057  | 37 |
| 24 | 45362    | 2.20449  | 47483    | 2.10600  | 49640    | 2.01449  | 51835    | 1.92920  | 36 |
| 25 | 45397    | 2.20278  | 47519    | 2.10442  | 49677    | 2.01302  | 51872    | 1.92782  | 35 |
| 26 | 45432    | 2.20108  | 47555    | 2.10284  | 49713    | 2.01155  | 51909    | 1.92645  | 34 |
| 27 | 45467    | 2.19938  | 47590    | 2.10126  | 49749    | 2.01008  | 51946    | 1.92508  | 33 |
| 28 | 45502    | 2.19769  | 47626    | 2.09969  | 49786    | 2.00862  | 51983    | 1.92371  | 32 |
| 29 | 45537    | 2.19599  | 47662    | 2.09811  | 49822    | 2.00715  | 52020    | 1.92235  | 31 |
| 30 | 45573    | 2.19430  | 47698    | 2.09654  | 49858    | 2.00569  | 52057    | 1.92098  | 30 |
| 31 | 45608    | 2.19261  | 47733    | 2.09498  | 49894    | 2.00423  | 52094    | 1.91962  | 29 |
| 32 | 45643    | 2.19092  | 47769    | 2.09341  | 49931    | 2.00277  | 52131    | 1.91826  | 28 |
| 33 | 45678    | 2.18923  | 47805    | 2.09184  | 49967    | 2.00131  | 52168    | 1.91690  | 27 |
| 34 | 45713    | 2.18755  | 47840    | 2.09028  | 50004    | 1.99986  | 52205    | 1.91554  | 26 |
| 35 | 45748    | 2.18587  | 47876    | 2.08872  | 50040    | 1.99841  | 52242    | 1.91418  | 25 |
| 36 | 45784    | 2.18419  | 47912    | 2.08716  | 50076    | 1.99695  | 52279    | 1.91282  | 24 |
| 37 | 45819    | 2.18251  | 47948    | 2.08560  | 50113    | 1.99550  | 52316    | 1.91147  | 23 |
| 38 | 45854    | 2.18084  | 47984    | 2.08405  | 50149    | 1.99406  | 52353    | 1.91012  | 22 |
| 39 | 45889    | 2.17916  | 48019    | 2.08250  | 50185    | 1.99261  | 52390    | 1.90876  | 21 |
| 40 | 45924    | 2.17749  | 48055    | 2.08094  | 50222    | 1.99116  | 52427    | 1.90741  | 20 |
| 41 | 45960    | 2.17582  | 48091    | 2.07939  | 50258    | 1.98972  | 52464    | 1.90607  | 19 |
| 42 | 45995    | 2.17416  | 48127    | 2.07785  | 50295    | 1.98828  | 52501    | 1.90472  | 18 |
| 43 | 46030    | 2.17249  | 48163    | 2.07630  | 50331    | 1.98684  | 52538    | 1.90337  | 17 |
| 44 | 46065    | 2.17083  | 48198    | 2.07476  | 50368    | 1.98540  | 52575    | 1.90203  | 16 |
| 45 | 46101    | 2.16917  | 48234    | 2.07321  | 50404    | 1.98396  | 52613    | 1.90069  | 15 |
| 46 | 46136    | 2.16751  | 48270    | 2.07167  | 50441    | 1.98253  | 52650    | 1.89935  | 14 |
| 47 | 46171    | 2.16585  | 48306    | 2.07014  | 50477    | 1.98110  | 52687    | 1.89801  | 13 |
| 48 | 46206    | 2.16420  | 48342    | 2.06860  | 50514    | 1.97966  | 52724    | 1.89667  | 12 |
| 49 | 46242    | 2.16255  | 48378    | 2.06706  | 50550    | 1.97823  | 52761    | 1.89533  | 11 |
| 50 | 46277    | 2.16090  | 48414    | 2.06553  | 50587    | 1.97680  | 52798    | 1.89400  | 10 |
| 51 | 46312    | 2.15925  | 48450    | 2.06400  | 50623    | 1.97538  | 52836    | 1.89266  | 9  |
| 52 | 46348    | 2.15760  | 48486    | 2.06247  | 50660    | 1.97395  | 52873    | 1.89133  | 8  |
| 53 | 46383    | 2.15596  | 48521    | 2.06094  | 50696    | 1.97253  | 52910    | 1.89000  | 7  |
| 54 | 46418    | 2.15432  | 48557    | 2.05942  | 50733    | 1.97111  | 52947    | 1.88867  | 6  |
| 55 | 46454    | 2.15268  | 48593    | 2.05790  | 50769    | 1.96969  | 52984    | 1.88734  | 5  |
| 56 | 46489    | 2.15104  | 48629    | 2.05637  | 50806    | 1.96827  | 53022    | 1.88602  | 4  |
| 57 | 46525    | 2.14940  | 48665    | 2.05485  | 50843    | 1.96685  | 53059    | 1.88469  | 3  |
| 58 | 46560    | 2.14777  | 48701    | 2.05333  | 50879    | 1.96544  | 53096    | 1.88337  | 2  |
| 59 | 46595    | 2.14614  | 48737    | 2.05182  | 50916    | 1.96402  | 53134    | 1.88205  | 1  |
| 60 | 46631    | 2.14451  | 48773    | 2.05030  | 50953    | 1.96261  | 53171    | 1.88073  | 0  |
| °  | 65°      |          | 64°      |          | 63°      |          | 62°      |          | °  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |

|    | 80°     |         | 81°     |         | 82°     |         | 83°     |         | 84°     |         |    |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 50000   | 86603   | 51504   | 85717   | 52992   | 84805   | 54464   | 83867   | 55919   | 82904   | 60 |
| 1  | 50025   | 86588   | 51529   | 85702   | 53017   | 84789   | 54488   | 83851   | 55943   | 82887   | 59 |
| 2  | 50050   | 86573   | 51554   | 85687   | 53041   | 84774   | 54513   | 83835   | 55968   | 82871   | 58 |
| 3  | 50076   | 86559   | 51579   | 85672   | 53066   | 84759   | 54537   | 83819   | 55992   | 82855   | 57 |
| 4  | 50101   | 86544   | 51604   | 85657   | 53091   | 84743   | 54561   | 83804   | 56016   | 82839   | 56 |
| 5  | 50126   | 86530   | 51628   | 85642   | 53115   | 84728   | 54586   | 83788   | 56040   | 82822   | 55 |
| 6  | 50151   | 86515   | 51653   | 85627   | 53140   | 84712   | 54610   | 83772   | 56064   | 82806   | 54 |
| 7  | 50176   | 86501   | 51678   | 85612   | 53164   | 84697   | 54635   | 83756   | 56088   | 82790   | 53 |
| 8  | 50201   | 86486   | 51703   | 85597   | 53189   | 84681   | 54659   | 83740   | 56112   | 82773   | 52 |
| 9  | 50227   | 86471   | 51728   | 85582   | 53214   | 84666   | 54683   | 83724   | 56136   | 82757   | 51 |
| 10 | 50252   | 86457   | 51753   | 85567   | 53238   | 84650   | 54708   | 83708   | 56160   | 82741   | 50 |
| 11 | 50277   | 86442   | 51778   | 85551   | 53263   | 84635   | 54732   | 83692   | 56184   | 82724   | 49 |
| 12 | 50302   | 86427   | 51803   | 85536   | 53288   | 84619   | 54756   | 83676   | 56208   | 82708   | 48 |
| 13 | 50327   | 86413   | 51828   | 85521   | 53312   | 84604   | 54781   | 83660   | 56232   | 82692   | 47 |
| 14 | 50352   | 86398   | 51852   | 85506   | 53337   | 84588   | 54805   | 83645   | 56256   | 82675   | 46 |
| 15 | 50377   | 86384   | 51877   | 85491   | 53361   | 84573   | 54829   | 83629   | 56280   | 82659   | 45 |
| 16 | 50403   | 86369   | 51902   | 85476   | 53386   | 84557   | 54854   | 83613   | 56305   | 82643   | 44 |
| 17 | 50428   | 86354   | 51927   | 85461   | 53411   | 84542   | 54878   | 83597   | 56329   | 82626   | 43 |
| 18 | 50453   | 86340   | 51952   | 85446   | 53435   | 84526   | 54902   | 83581   | 56353   | 82610   | 42 |
| 19 | 50478   | 86325   | 51977   | 85431   | 53460   | 84511   | 54927   | 83565   | 56377   | 82593   | 41 |
| 20 | 50503   | 86310   | 52002   | 85416   | 53484   | 84495   | 54951   | 83549   | 56401   | 82577   | 40 |
| 21 | 50528   | 86295   | 52026   | 85401   | 53509   | 84480   | 54975   | 83533   | 56425   | 82561   | 39 |
| 22 | 50553   | 86281   | 52051   | 85385   | 53534   | 84464   | 54999   | 83517   | 56449   | 82544   | 38 |
| 23 | 50578   | 86266   | 52076   | 85370   | 53558   | 84448   | 55024   | 83501   | 56473   | 82528   | 37 |
| 24 | 50603   | 86251   | 52101   | 85355   | 53583   | 84433   | 55048   | 83485   | 56497   | 82511   | 36 |
| 25 | 50628   | 86237   | 52126   | 85340   | 53607   | 84417   | 55072   | 83469   | 56521   | 82495   | 35 |
| 26 | 50654   | 86222   | 52151   | 85325   | 53632   | 84402   | 55097   | 83453   | 56545   | 82478   | 34 |
| 27 | 50679   | 86207   | 52175   | 85310   | 53656   | 84386   | 55121   | 83437   | 56569   | 82462   | 33 |
| 28 | 50704   | 86192   | 52200   | 85294   | 53681   | 84370   | 55145   | 83421   | 56593   | 82446   | 32 |
| 29 | 50729   | 86178   | 52225   | 85279   | 53705   | 84355   | 55169   | 83405   | 56617   | 82429   | 31 |
| 30 | 50754   | 86163   | 52250   | 85264   | 53730   | 84339   | 55194   | 83389   | 56641   | 82413   | 30 |
| 31 | 50779   | 86148   | 52275   | 85249   | 53754   | 84324   | 55218   | 83373   | 56665   | 82396   | 29 |
| 32 | 50804   | 86133   | 52299   | 85234   | 53779   | 84308   | 55242   | 83356   | 56689   | 82380   | 28 |
| 33 | 50829   | 86119   | 52324   | 85218   | 53804   | 84292   | 55266   | 83340   | 56713   | 82363   | 27 |
| 34 | 50854   | 86104   | 52349   | 85203   | 53828   | 84277   | 55291   | 83324   | 56736   | 82347   | 26 |
| 35 | 50879   | 86089   | 52374   | 85188   | 53853   | 84261   | 55315   | 83308   | 56760   | 82330   | 25 |
| 36 | 50904   | 86074   | 52399   | 85173   | 53877   | 84245   | 55339   | 83292   | 56784   | 82314   | 24 |
| 37 | 50929   | 86059   | 52423   | 85157   | 53902   | 84230   | 55363   | 83276   | 56808   | 82297   | 23 |
| 38 | 50954   | 86045   | 52448   | 85142   | 53926   | 84214   | 55388   | 83260   | 56832   | 82281   | 22 |
| 39 | 50979   | 86030   | 52473   | 85127   | 53951   | 84198   | 55412   | 83244   | 56856   | 82264   | 21 |
| 40 | 51004   | 86015   | 52498   | 85112   | 53975   | 84182   | 55436   | 83228   | 56880   | 82248   | 20 |
| 41 | 51029   | 86000   | 52522   | 85096   | 54000   | 84167   | 55460   | 83212   | 56904   | 82231   | 19 |
| 42 | 51054   | 85985   | 52547   | 85081   | 54024   | 84151   | 55484   | 83195   | 56928   | 82214   | 18 |
| 43 | 51079   | 85970   | 52572   | 85066   | 54049   | 84135   | 55509   | 83179   | 56952   | 82198   | 17 |
| 44 | 51104   | 85956   | 52597   | 85051   | 54073   | 84120   | 55533   | 83163   | 56976   | 82181   | 16 |
| 45 | 51129   | 85941   | 52621   | 85035   | 54097   | 84104   | 55557   | 83147   | 57000   | 82165   | 15 |
| 46 | 51154   | 85926   | 52646   | 85020   | 54122   | 84088   | 55581   | 83131   | 57024   | 82148   | 14 |
| 47 | 51179   | 85911   | 52671   | 85005   | 54146   | 84072   | 55605   | 83115   | 57047   | 82132   | 13 |
| 48 | 51204   | 85896   | 52696   | 84989   | 54171   | 84057   | 55630   | 83098   | 57071   | 82115   | 12 |
| 49 | 51229   | 85881   | 52720   | 84974   | 54195   | 84041   | 55654   | 83082   | 57095   | 82098   | 11 |
| 50 | 51254   | 85866   | 52745   | 84959   | 54220   | 84025   | 55678   | 83066   | 57119   | 82082   | 10 |
| 51 | 51279   | 85851   | 52770   | 84943   | 54244   | 84009   | 55702   | 83050   | 57143   | 82065   | 9  |
| 52 | 51304   | 85836   | 52794   | 84928   | 54269   | 83994   | 55726   | 83034   | 57167   | 82048   | 8  |
| 53 | 51329   | 85821   | 52819   | 84913   | 54293   | 83978   | 55750   | 83017   | 57191   | 82032   | 7  |
| 54 | 51354   | 85806   | 52844   | 84897   | 54317   | 83962   | 55775   | 83001   | 57215   | 82015   | 6  |
| 55 | 51379   | 85792   | 52869   | 84882   | 54342   | 83946   | 55799   | 82985   | 57238   | 81999   | 5  |
| 56 | 51404   | 85777   | 52893   | 84866   | 54366   | 83930   | 55823   | 82969   | 57262   | 81982   | 4  |
| 57 | 51429   | 85762   | 52918   | 84851   | 54391   | 83915   | 55847   | 82953   | 57286   | 81965   | 3  |
| 58 | 51454   | 85747   | 52943   | 84836   | 54415   | 83899   | 55871   | 82936   | 57310   | 81949   | 2  |
| 59 | 51479   | 85732   | 52967   | 84820   | 54440   | 83883   | 55895   | 82920   | 57334   | 81932   | 1  |
| 60 | 51504   | 85717   | 52992   | 84805   | 54464   | 83867   | 55919   | 82904   | 57358   | 81915   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 59°     |         | 58°     |         | 57°     |         | 56°     |         | 55°     |         |    |

TABLE III.

## NATURAL SINES AND COSINES.

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|    | 85°    |         | 86°     |         | 87°     |         | 88°     |         | 89°     |         |    |
|----|--------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.  | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 57358  | 81915   | 58779   | 80902   | 60182   | 79864   | 61566   | 78801   | 62932   | 77715   | 60 |
| 1  | 57381  | 81899   | 58802   | 80885   | 60205   | 79846   | 61589   | 78783   | 62955   | 77696   | 59 |
| 2  | 57405  | 81882   | 58826   | 80867   | 60228   | 79829   | 61612   | 78765   | 62977   | 77678   | 58 |
| 3  | 57429  | 81865   | 58849   | 80850   | 60251   | 79811   | 61635   | 78747   | 63000   | 77660   | 57 |
| 4  | 57453  | 81848   | 58873   | 80833   | 60274   | 79793   | 61658   | 78729   | 63022   | 77641   | 56 |
| 5  | 57477  | 81832   | 58896   | 80816   | 60298   | 79776   | 61681   | 78711   | 63045   | 77623   | 55 |
| 6  | 57501  | 81815   | 58920   | 80799   | 60321   | 79758   | 61704   | 78694   | 63068   | 77605   | 54 |
| 7  | 57524  | 81798   | 58943   | 80782   | 60344   | 79741   | 61726   | 78676   | 63090   | 77586   | 53 |
| 8  | 57548  | 81782   | 58967   | 80765   | 60367   | 79723   | 61749   | 78658   | 63113   | 77568   | 52 |
| 9  | 57572  | 81765   | 58990   | 80748   | 60390   | 79706   | 61772   | 78640   | 63135   | 77550   | 51 |
| 10 | 57596  | 81748   | 59014   | 80730   | 60414   | 79688   | 61795   | 78622   | 63158   | 77531   | 50 |
| 11 | 57619  | 81731   | 59037   | 80713   | 60437   | 79671   | 61818   | 78604   | 63180   | 77513   | 49 |
| 12 | 57643  | 81714   | 59061   | 80696   | 60460   | 79653   | 61841   | 78586   | 63203   | 77494   | 48 |
| 13 | 57667  | 81698   | 59084   | 80679   | 60483   | 79635   | 61864   | 78568   | 63225   | 77476   | 47 |
| 14 | 57691  | 81681   | 59108   | 80662   | 60506   | 79618   | 61887   | 78550   | 63248   | 77458   | 46 |
| 15 | 57715  | 81664   | 59131   | 80644   | 60529   | 79600   | 61909   | 78532   | 63271   | 77439   | 45 |
| 16 | 57738  | 81647   | 59154   | 80627   | 60553   | 79583   | 61932   | 78514   | 63293   | 77421   | 44 |
| 17 | 57762  | 81631   | 59178   | 80610   | 60576   | 79565   | 61955   | 78496   | 63316   | 77402   | 43 |
| 18 | 57786  | 81614   | 59201   | 80593   | 60599   | 79547   | 61978   | 78478   | 63338   | 77384   | 42 |
| 19 | 57810  | 81597   | 59225   | 80576   | 60622   | 79530   | 62001   | 78460   | 63361   | 77366   | 41 |
| 20 | 57833  | 81580   | 59248   | 80558   | 60645   | 79512   | 62024   | 78442   | 63383   | 77347   | 40 |
| 21 | 57857  | 81563   | 59272   | 80541   | 60668   | 79494   | 62046   | 78424   | 63406   | 77329   | 39 |
| 22 | 57881  | 81546   | 59295   | 80524   | 60691   | 79477   | 62069   | 78405   | 63428   | 77310   | 38 |
| 23 | 57904  | 81530   | 59318   | 80507   | 60714   | 79459   | 62092   | 78387   | 63451   | 77292   | 37 |
| 24 | 57928  | 81513   | 59342   | 80489   | 60738   | 79441   | 62115   | 78369   | 63473   | 77273   | 36 |
| 25 | 57952  | 81496   | 59365   | 80472   | 60761   | 79424   | 62138   | 78351   | 63496   | 77255   | 35 |
| 26 | 57976  | 81479   | 59389   | 80455   | 60784   | 79406   | 62160   | 78333   | 63518   | 77236   | 34 |
| 27 | 57999  | 81462   | 59412   | 80438   | 60807   | 79388   | 62183   | 78315   | 63540   | 77218   | 33 |
| 28 | 58023  | 81445   | 59436   | 80420   | 60830   | 79371   | 62206   | 78297   | 63563   | 77199   | 32 |
| 29 | 58047  | 81428   | 59459   | 80403   | 60853   | 79353   | 62229   | 78279   | 63585   | 77181   | 31 |
| 30 | 58070  | 81412   | 59482   | 80386   | 60876   | 79335   | 62251   | 78261   | 63608   | 77162   | 30 |
| 31 | 58094  | 81395   | 59506   | 80368   | 60899   | 79318   | 62274   | 78243   | 63630   | 77144   | 29 |
| 32 | 58118  | 81378   | 59529   | 80351   | 60922   | 79300   | 62297   | 78225   | 63653   | 77125   | 28 |
| 33 | 58141  | 81361   | 59552   | 80334   | 60945   | 79282   | 62320   | 78206   | 63675   | 77107   | 27 |
| 34 | 58165  | 81344   | 59576   | 80316   | 60968   | 79264   | 62342   | 78188   | 63698   | 77088   | 26 |
| 35 | 58189  | 81327   | 59599   | 80299   | 60991   | 79247   | 62365   | 78170   | 63720   | 77070   | 25 |
| 36 | 58212  | 81310   | 59622   | 80282   | 61015   | 79229   | 62388   | 78152   | 63742   | 77051   | 24 |
| 37 | 58236  | 81293   | 59646   | 80264   | 61038   | 79211   | 62411   | 78134   | 63765   | 77033   | 23 |
| 38 | 58260  | 81276   | 59669   | 80247   | 61061   | 79193   | 62433   | 78116   | 63787   | 77014   | 22 |
| 39 | 58283  | 81259   | 59693   | 80230   | 61084   | 79176   | 62456   | 78098   | 63810   | 76996   | 21 |
| 40 | 58307  | 81242   | 59716   | 80212   | 61107   | 79158   | 62479   | 78079   | 63832   | 76977   | 20 |
| 41 | 58330  | 81225   | 59739   | 80195   | 61130   | 79140   | 62502   | 78061   | 63854   | 76959   | 19 |
| 42 | 58354  | 81208   | 59763   | 80178   | 61153   | 79122   | 62524   | 78043   | 63877   | 76940   | 18 |
| 43 | 58378  | 81191   | 59786   | 80160   | 61176   | 79105   | 62547   | 78025   | 63899   | 76921   | 17 |
| 44 | 58401  | 81174   | 59809   | 80143   | 61199   | 79087   | 62570   | 78007   | 63922   | 76903   | 16 |
| 45 | 58425  | 81157   | 59832   | 80125   | 61222   | 79069   | 62592   | 77988   | 63944   | 76884   | 15 |
| 46 | 58449  | 81140   | 59856   | 80108   | 61245   | 79051   | 62615   | 77970   | 63966   | 76866   | 14 |
| 47 | 58472  | 81123   | 59879   | 80091   | 61268   | 79033   | 62638   | 77952   | 63989   | 76847   | 13 |
| 48 | 58496  | 81106   | 59902   | 80073   | 61291   | 79016   | 62660   | 77934   | 64011   | 76828   | 12 |
| 49 | 58519  | 81089   | 59926   | 80056   | 61314   | 78998   | 62683   | 77916   | 64033   | 76810   | 11 |
| 50 | 58543  | 81072   | 59949   | 80038   | 61337   | 78980   | 62706   | 77897   | 64056   | 76791   | 10 |
| 51 | 58567  | 81055   | 59972   | 80021   | 61360   | 78962   | 62728   | 77879   | 64078   | 76772   | 9  |
| 52 | 58590  | 81038   | 59995   | 80003   | 61383   | 78944   | 62751   | 77861   | 64100   | 76754   | 8  |
| 53 | 58614  | 81021   | 60019   | 79986   | 61406   | 78926   | 62774   | 77843   | 64123   | 76735   | 7  |
| 54 | 58637  | 81004   | 60042   | 79968   | 61429   | 78908   | 62796   | 77824   | 64145   | 76717   | 6  |
| 55 | 58661  | 80987   | 60065   | 79951   | 61451   | 78891   | 62819   | 77806   | 64167   | 76698   | 5  |
| 56 | 58684  | 80970   | 60089   | 79934   | 61474   | 78873   | 62842   | 77788   | 64190   | 76679   | 4  |
| 57 | 58708  | 80953   | 60112   | 79916   | 61497   | 78855   | 62864   | 77769   | 64212   | 76661   | 3  |
| 58 | 58731  | 80936   | 60135   | 79899   | 61520   | 78837   | 62887   | 77751   | 64234   | 76642   | 2  |
| 59 | 58755  | 80919   | 60158   | 79881   | 61543   | 78819   | 62909   | 77733   | 64256   | 76623   | 1  |
| 60 | 58779  | 80902   | 60182   | 79864   | 61566   | 78801   | 62932   | 77715   | 64279   | 76604   | 0  |
|    | Cosine | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 54°    |         | 53°     |         | 52°     |         | 51°     |         | 50°     |         |    |

|    | 40°     |         | 41°     |         | 42°     |         | 43°     |         | 44°     |         |    |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 64279   | 76604   | 65606   | 75471   | 66913   | 74314   | 68200   | 73135   | 69466   | 71934   | 60 |
| 1  | 64301   | 76586   | 65628   | 75452   | 66935   | 74295   | 68221   | 73116   | 69487   | 71914   | 59 |
| 2  | 64323   | 76567   | 65650   | 75433   | 66956   | 74276   | 68242   | 73096   | 69508   | 71894   | 58 |
| 3  | 64346   | 76548   | 65672   | 75414   | 66978   | 74256   | 68264   | 73075   | 69529   | 71873   | 57 |
| 4  | 64368   | 76530   | 65694   | 75395   | 66999   | 74237   | 68285   | 73056   | 69549   | 71853   | 56 |
| 5  | 64390   | 76511   | 65716   | 75375   | 67021   | 74217   | 68306   | 73036   | 69570   | 71833   | 55 |
| 6  | 64412   | 76492   | 65738   | 75356   | 67043   | 74198   | 68327   | 73016   | 69591   | 71813   | 54 |
| 7  | 64435   | 76473   | 65759   | 75337   | 67064   | 74178   | 68349   | 72996   | 69612   | 71792   | 53 |
| 8  | 64457   | 76455   | 65781   | 75318   | 67086   | 74159   | 68370   | 72976   | 69633   | 71772   | 52 |
| 9  | 64479   | 76436   | 65803   | 75299   | 67107   | 74139   | 68391   | 72957   | 69654   | 71752   | 51 |
| 10 | 64501   | 76417   | 65825   | 75280   | 67129   | 74120   | 68412   | 72937   | 69675   | 71732   | 50 |
| 11 | 64524   | 76398   | 65847   | 75261   | 67151   | 74100   | 68434   | 72917   | 69696   | 71711   | 49 |
| 12 | 64546   | 76380   | 65869   | 75241   | 67172   | 74080   | 68455   | 72897   | 69717   | 71691   | 48 |
| 13 | 64568   | 76361   | 65891   | 75222   | 67194   | 74061   | 68476   | 72877   | 69737   | 71671   | 47 |
| 14 | 64590   | 76342   | 65913   | 75203   | 67215   | 74041   | 68497   | 72857   | 69758   | 71650   | 46 |
| 15 | 64612   | 76323   | 65935   | 75184   | 67237   | 74022   | 68518   | 72837   | 69779   | 71630   | 45 |
| 16 | 64635   | 76304   | 65956   | 75165   | 67258   | 74002   | 68539   | 72817   | 69800   | 71610   | 44 |
| 17 | 64657   | 76286   | 65978   | 75146   | 67280   | 73983   | 68561   | 72797   | 69821   | 71590   | 43 |
| 18 | 64679   | 76267   | 66000   | 75126   | 67301   | 73963   | 68582   | 72777   | 69842   | 71569   | 42 |
| 19 | 64701   | 76248   | 66022   | 75107   | 67323   | 73944   | 68603   | 72757   | 69862   | 71549   | 41 |
| 20 | 64723   | 76229   | 66044   | 75088   | 67344   | 73924   | 68624   | 72737   | 69883   | 71529   | 40 |
| 21 | 64746   | 76210   | 66066   | 75069   | 67366   | 73904   | 68645   | 72717   | 69904   | 71508   | 39 |
| 22 | 64768   | 76192   | 66088   | 75050   | 67387   | 73885   | 68666   | 72697   | 69925   | 71488   | 38 |
| 23 | 64790   | 76173   | 66109   | 75030   | 67409   | 73865   | 68688   | 72677   | 69946   | 71468   | 37 |
| 24 | 64812   | 76154   | 66131   | 75011   | 67430   | 73846   | 68709   | 72657   | 69966   | 71447   | 36 |
| 25 | 64834   | 76135   | 66153   | 74992   | 67452   | 73826   | 68730   | 72637   | 69987   | 71427   | 35 |
| 26 | 64856   | 76116   | 66175   | 74973   | 67473   | 73806   | 68751   | 72617   | 70008   | 71407   | 34 |
| 27 | 64878   | 76097   | 66197   | 74953   | 67495   | 73787   | 68772   | 72597   | 70029   | 71386   | 33 |
| 28 | 64901   | 76078   | 66218   | 74934   | 67516   | 73767   | 68793   | 72577   | 70049   | 71366   | 32 |
| 29 | 64923   | 76059   | 66240   | 74915   | 67538   | 73747   | 68814   | 72557   | 70070   | 71345   | 31 |
| 30 | 64945   | 76041   | 66262   | 74896   | 67559   | 73728   | 68835   | 72537   | 70091   | 71325   | 30 |
| 31 | 64967   | 76022   | 66284   | 74876   | 67580   | 73708   | 68857   | 72517   | 70112   | 71305   | 29 |
| 32 | 64989   | 76003   | 66305   | 74857   | 67602   | 73688   | 68878   | 72497   | 70132   | 71284   | 28 |
| 33 | 65011   | 75984   | 66327   | 74838   | 67623   | 73669   | 68899   | 72477   | 70153   | 71264   | 27 |
| 34 | 65033   | 75965   | 66349   | 74818   | 67645   | 73649   | 68920   | 72457   | 70174   | 71243   | 26 |
| 35 | 65055   | 75946   | 66371   | 74799   | 67666   | 73629   | 68941   | 72437   | 70195   | 71223   | 25 |
| 36 | 65077   | 75927   | 66393   | 74780   | 67688   | 73610   | 68962   | 72417   | 70215   | 71203   | 24 |
| 37 | 65100   | 75908   | 66414   | 74760   | 67709   | 73590   | 68983   | 72397   | 70236   | 71182   | 23 |
| 38 | 65122   | 75889   | 66436   | 74741   | 67730   | 73570   | 69004   | 72377   | 70257   | 71162   | 22 |
| 39 | 65144   | 75870   | 66458   | 74722   | 67752   | 73551   | 69025   | 72357   | 70277   | 71141   | 21 |
| 40 | 65166   | 75851   | 66480   | 74703   | 67773   | 73531   | 69046   | 72337   | 70298   | 71121   | 20 |
| 41 | 65188   | 75832   | 66501   | 74683   | 67795   | 73511   | 69067   | 72317   | 70319   | 71100   | 19 |
| 42 | 65210   | 75813   | 66523   | 74664   | 67816   | 73491   | 69088   | 72297   | 70339   | 71080   | 18 |
| 43 | 65232   | 75794   | 66545   | 74644   | 67837   | 73472   | 69109   | 72277   | 70360   | 71059   | 17 |
| 44 | 65254   | 75775   | 66566   | 74625   | 67859   | 73452   | 69130   | 72257   | 70381   | 71039   | 16 |
| 45 | 65276   | 75756   | 66588   | 74606   | 67880   | 73432   | 69151   | 72236   | 70401   | 71019   | 15 |
| 46 | 65298   | 75738   | 66610   | 74586   | 67901   | 73413   | 69172   | 72216   | 70422   | 70998   | 14 |
| 47 | 65320   | 75719   | 66632   | 74567   | 67923   | 73393   | 69193   | 72196   | 70443   | 70978   | 13 |
| 48 | 65342   | 75700   | 66653   | 74548   | 67944   | 73373   | 69214   | 72176   | 70463   | 70957   | 12 |
| 49 | 65364   | 75680   | 66675   | 74528   | 67965   | 73353   | 69235   | 72156   | 70484   | 70937   | 11 |
| 50 | 65386   | 75661   | 66697   | 74509   | 67987   | 73333   | 69256   | 72136   | 70505   | 70916   | 10 |
| 51 | 65408   | 75642   | 66718   | 74489   | 68008   | 73314   | 69277   | 72116   | 70525   | 70896   | 9  |
| 52 | 65430   | 75623   | 66740   | 74470   | 68029   | 73294   | 69298   | 72095   | 70546   | 70875   | 8  |
| 53 | 65452   | 75604   | 66762   | 74451   | 68051   | 73274   | 69319   | 72075   | 70567   | 70855   | 7  |
| 54 | 65474   | 75585   | 66783   | 74431   | 68072   | 73254   | 69340   | 72055   | 70587   | 70834   | 6  |
| 55 | 65496   | 75566   | 66805   | 74412   | 68093   | 73234   | 69361   | 72035   | 70608   | 70813   | 5  |
| 56 | 65518   | 75547   | 66827   | 74392   | 68115   | 73215   | 69382   | 72015   | 70628   | 70793   | 4  |
| 57 | 65540   | 75528   | 66848   | 74373   | 68136   | 73195   | 69403   | 71995   | 70649   | 70772   | 3  |
| 58 | 65562   | 75509   | 66870   | 74353   | 68157   | 73175   | 69424   | 71974   | 70670   | 70752   | 2  |
| 59 | 65584   | 75490   | 66891   | 74334   | 68179   | 73155   | 69445   | 71954   | 70690   | 70731   | 1  |
| 60 | 65606   | 75471   | 66913   | 74314   | 68200   | 73135   | 69466   | 71934   | 70711   | 70711   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 49°     |         | 48°     |         | 47°     |         | 46°     |         | 45°     |         |    |



TABLE III. NATURAL TANGENTS AND COTANGENTS. 78

| °  | 0°       |           | 1°       |          | 2°       |          | 3°       |          | °  |
|----|----------|-----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.   | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 00000    | Infinite. | 01746    | 57.2900  | 03492    | 28.6363  | 05241    | 19.0811  | 60 |
| 1  | 00029    | 3437.75   | 01775    | 56.3506  | 03521    | 28.3994  | 05270    | 18.9755  | 59 |
| 2  | 00058    | 1718.87   | 01804    | 55.4415  | 03550    | 28.1664  | 05299    | 18.8711  | 58 |
| 3  | 00087    | 1145.92   | 01833    | 54.5613  | 03579    | 27.9372  | 05328    | 18.7678  | 57 |
| 4  | 00116    | 859.436   | 01862    | 53.7086  | 03609    | 27.7117  | 05357    | 18.6656  | 56 |
| 5  | 00145    | 687.549   | 01891    | 52.8821  | 03638    | 27.4899  | 05387    | 18.5645  | 55 |
| 6  | 00175    | 572.957   | 01920    | 52.0807  | 03667    | 27.2715  | 05416    | 18.4645  | 54 |
| 7  | 00204    | 491.106   | 01949    | 51.3032  | 03696    | 27.0566  | 05445    | 18.3655  | 53 |
| 8  | 00233    | 429.718   | 01978    | 50.5485  | 03725    | 26.8450  | 05474    | 18.2677  | 52 |
| 9  | 00262    | 381.971   | 02007    | 49.8157  | 03754    | 26.6367  | 05503    | 18.1708  | 51 |
| 10 | 00291    | 343.774   | 02036    | 49.1039  | 03783    | 26.4315  | 05533    | 18.0750  | 50 |
| 11 | 00320    | 312.521   | 02066    | 48.4121  | 03812    | 26.2296  | 05562    | 17.9802  | 49 |
| 12 | 00349    | 286.478   | 02095    | 47.7395  | 03842    | 26.0307  | 05591    | 17.8863  | 48 |
| 13 | 00378    | 264.441   | 02124    | 47.0853  | 03871    | 25.8348  | 05620    | 17.7934  | 47 |
| 14 | 00407    | 245.552   | 02153    | 46.4489  | 03900    | 25.6418  | 05649    | 17.7015  | 46 |
| 15 | 00436    | 229.182   | 02182    | 45.8294  | 03929    | 25.4517  | 05678    | 17.6106  | 45 |
| 16 | 00465    | 214.858   | 02211    | 45.2261  | 03958    | 25.2644  | 05708    | 17.5205  | 44 |
| 17 | 00495    | 202.219   | 02240    | 44.6386  | 03987    | 25.0798  | 05737    | 17.4314  | 43 |
| 18 | 00524    | 190.984   | 02269    | 44.0661  | 04016    | 24.8978  | 05766    | 17.3432  | 42 |
| 19 | 00553    | 180.032   | 02298    | 43.5081  | 04046    | 24.7185  | 05795    | 17.2558  | 41 |
| 20 | 00582    | 171.885   | 02328    | 42.9641  | 04075    | 24.5418  | 05824    | 17.1693  | 40 |
| 21 | 00611    | 163.700   | 02357    | 42.4335  | 04104    | 24.3675  | 05854    | 17.0837  | 39 |
| 22 | 00640    | 156.259   | 02386    | 41.9158  | 04133    | 24.1957  | 05883    | 16.9990  | 38 |
| 23 | 00669    | 149.465   | 02415    | 41.4106  | 04162    | 24.0263  | 05912    | 16.9150  | 37 |
| 24 | 00698    | 143.537   | 02444    | 40.9174  | 04191    | 23.8593  | 05941    | 16.8319  | 36 |
| 25 | 00727    | 137.507   | 02473    | 40.4358  | 04220    | 23.6945  | 05970    | 16.7490  | 35 |
| 26 | 00756    | 132.219   | 02502    | 39.9655  | 04250    | 23.5321  | 05999    | 16.6681  | 34 |
| 27 | 00785    | 127.321   | 02531    | 39.5059  | 04279    | 23.3718  | 06029    | 16.5874  | 33 |
| 28 | 00814    | 122.774   | 02560    | 39.0568  | 04308    | 23.2137  | 06058    | 16.5075  | 32 |
| 29 | 00844    | 118.540   | 02589    | 38.6177  | 04337    | 23.0577  | 06087    | 16.4283  | 31 |
| 30 | 00873    | 114.589   | 02619    | 38.1885  | 04366    | 22.9038  | 06116    | 16.3499  | 30 |
| 31 | 00902    | 110.892   | 02648    | 37.7686  | 04395    | 22.7519  | 06145    | 16.2722  | 29 |
| 32 | 00931    | 107.426   | 02677    | 37.3579  | 04424    | 22.6020  | 06175    | 16.1952  | 28 |
| 33 | 00960    | 104.171   | 02706    | 36.9560  | 04454    | 22.4541  | 06204    | 16.1190  | 27 |
| 34 | 00989    | 101.107   | 02735    | 36.5627  | 04483    | 22.3081  | 06233    | 16.0435  | 26 |
| 35 | 01018    | 98.2179   | 02764    | 36.1776  | 04512    | 22.1640  | 06262    | 15.9687  | 25 |
| 36 | 01047    | 95.4895   | 02793    | 35.8006  | 04541    | 22.0217  | 06291    | 15.8945  | 24 |
| 37 | 01076    | 92.9085   | 02822    | 35.4313  | 04570    | 21.8813  | 06321    | 15.8211  | 23 |
| 38 | 01105    | 90.4633   | 02851    | 35.0695  | 04599    | 21.7426  | 06350    | 15.7483  | 22 |
| 39 | 01135    | 88.1436   | 02881    | 34.7151  | 04628    | 21.6056  | 06379    | 15.6762  | 21 |
| 40 | 01164    | 85.9398   | 02910    | 34.3678  | 04658    | 21.4704  | 06408    | 15.6048  | 20 |
| 41 | 01193    | 83.8435   | 02939    | 34.0273  | 04687    | 21.3369  | 06437    | 15.5340  | 19 |
| 42 | 01222    | 81.8470   | 02968    | 33.6935  | 04716    | 21.2049  | 06467    | 15.4638  | 18 |
| 43 | 01251    | 79.9434   | 02997    | 33.3662  | 04745    | 21.0747  | 06496    | 15.3943  | 17 |
| 44 | 01280    | 78.1263   | 03026    | 33.0452  | 04774    | 20.9460  | 06525    | 15.3254  | 16 |
| 45 | 01309    | 76.3900   | 03055    | 32.7303  | 04803    | 20.8188  | 06554    | 15.2571  | 15 |
| 46 | 01338    | 74.7292   | 03084    | 32.4213  | 04832    | 20.6932  | 06584    | 15.1893  | 14 |
| 47 | 01367    | 73.1390   | 03113    | 32.1181  | 04862    | 20.5691  | 06613    | 15.1222  | 13 |
| 48 | 01396    | 71.6151   | 03143    | 31.8205  | 04891    | 20.4465  | 06642    | 15.0557  | 12 |
| 49 | 01425    | 70.1533   | 03172    | 31.5284  | 04920    | 20.3253  | 06671    | 14.9898  | 11 |
| 50 | 01455    | 68.7501   | 03201    | 31.2416  | 04949    | 20.2056  | 06700    | 14.9244  | 10 |
| 51 | 01484    | 67.4019   | 03230    | 30.9599  | 04978    | 20.0872  | 06730    | 14.8596  | 9  |
| 52 | 01513    | 66.1055   | 03259    | 30.6833  | 05007    | 19.9702  | 06759    | 14.7954  | 8  |
| 53 | 01542    | 64.8580   | 03288    | 30.4116  | 05037    | 19.8546  | 06788    | 14.7317  | 7  |
| 54 | 01571    | 63.6567   | 03317    | 30.1446  | 05066    | 19.7403  | 06817    | 14.6685  | 6  |
| 55 | 01600    | 62.4992   | 03346    | 29.8823  | 05095    | 19.6273  | 06847    | 14.6059  | 5  |
| 56 | 01629    | 61.3829   | 03376    | 29.6245  | 05124    | 19.5156  | 06876    | 14.5438  | 4  |
| 57 | 01658    | 60.3058   | 03405    | 29.3711  | 05153    | 19.4051  | 06905    | 14.4823  | 3  |
| 58 | 01687    | 59.2659   | 03434    | 29.1220  | 05182    | 19.2959  | 06934    | 14.4212  | 2  |
| 59 | 01716    | 58.2612   | 03463    | 28.8771  | 05212    | 19.1879  | 06963    | 14.3607  | 1  |
| 60 | 01746    | 57.2900   | 03492    | 28.6363  | 05241    | 19.0811  | 06993    | 14.3007  | 0  |
| °  | Cotang.  | Tangent.  | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | °  |
|    | 89°      |           | 88°      |          | 87°      |          | 86°      |          |    |

| °  | 0°      |         | 1°      |         | 2°      |         | 3°      |         | 4°      |         | °  |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 00000   | Unit.   | 01745   | 99985   | 03490   | 99939   | 05234   | 99863   | 06976   | 99756   | 60 |
| 1  | 00029   | Unit.   | 01774   | 99984   | 03519   | 99938   | 05263   | 99861   | 07005   | 99754   | 59 |
| 2  | 00058   | Unit.   | 01803   | 99984   | 03548   | 99937   | 05292   | 99860   | 07034   | 99752   | 58 |
| 3  | 00087   | Unit.   | 01832   | 99983   | 03577   | 99936   | 05321   | 99858   | 07063   | 99750   | 57 |
| 4  | 00116   | Unit.   | 01862   | 99983   | 03606   | 99935   | 05350   | 99857   | 07092   | 99748   | 56 |
| 5  | 00145   | Unit.   | 01891   | 99982   | 03635   | 99934   | 05379   | 99855   | 07121   | 99746   | 55 |
| 6  | 00175   | Unit.   | 01920   | 99982   | 03664   | 99933   | 05408   | 99854   | 07150   | 99744   | 54 |
| 7  | 00204   | Unit.   | 01949   | 99981   | 03693   | 99932   | 05437   | 99852   | 07179   | 99742   | 53 |
| 8  | 00233   | Unit.   | 01978   | 99980   | 03723   | 99931   | 05466   | 99851   | 07208   | 99740   | 52 |
| 9  | 00262   | Unit.   | 02007   | 99980   | 03752   | 99930   | 05495   | 99849   | 07237   | 99738   | 51 |
| 10 | 00291   | Unit.   | 02036   | 99979   | 03781   | 99929   | 05524   | 99847   | 07266   | 99736   | 50 |
| 11 | 00320   | 99999   | 02065   | 99979   | 03810   | 99927   | 05553   | 99846   | 07295   | 99734   | 49 |
| 12 | 00349   | 99999   | 02094   | 99978   | 03839   | 99926   | 05582   | 99844   | 07324   | 99731   | 48 |
| 13 | 00378   | 99999   | 02123   | 99977   | 03868   | 99925   | 05611   | 99842   | 07353   | 99729   | 47 |
| 14 | 00407   | 99999   | 02152   | 99977   | 03897   | 99924   | 05640   | 99841   | 07382   | 99727   | 46 |
| 15 | 00436   | 99999   | 02181   | 99976   | 03926   | 99923   | 05669   | 99839   | 07411   | 99725   | 45 |
| 16 | 00465   | 99999   | 02211   | 99976   | 03955   | 99922   | 05698   | 99838   | 07440   | 99723   | 44 |
| 17 | 00495   | 99999   | 02240   | 99975   | 03984   | 99921   | 05727   | 99836   | 07469   | 99721   | 43 |
| 18 | 00524   | 99999   | 02269   | 99974   | 04013   | 99919   | 05756   | 99834   | 07498   | 99719   | 42 |
| 19 | 00553   | 99998   | 02298   | 99974   | 04042   | 99918   | 05785   | 99833   | 07527   | 99717   | 41 |
| 20 | 00582   | 99998   | 02327   | 99973   | 04071   | 99917   | 05814   | 99831   | 07556   | 99714   | 40 |
| 21 | 00611   | 99998   | 02356   | 99972   | 04100   | 99916   | 05844   | 99829   | 07585   | 99712   | 39 |
| 22 | 00640   | 99998   | 02385   | 99972   | 04129   | 99915   | 05873   | 99827   | 07614   | 99710   | 38 |
| 23 | 00669   | 99998   | 02414   | 99971   | 04159   | 99913   | 05902   | 99826   | 07643   | 99708   | 37 |
| 24 | 00698   | 99998   | 02443   | 99970   | 04188   | 99912   | 05931   | 99824   | 07672   | 99705   | 36 |
| 25 | 00727   | 99997   | 02472   | 99969   | 04217   | 99911   | 05960   | 99822   | 07701   | 99703   | 35 |
| 26 | 00756   | 99997   | 02501   | 99969   | 04246   | 99910   | 05989   | 99821   | 07730   | 99701   | 34 |
| 27 | 00785   | 99997   | 02530   | 99968   | 04275   | 99909   | 06018   | 99819   | 07759   | 99699   | 33 |
| 28 | 00814   | 99997   | 02560   | 99967   | 04304   | 99907   | 06047   | 99817   | 07788   | 99696   | 32 |
| 29 | 00844   | 99996   | 02589   | 99966   | 04333   | 99906   | 06076   | 99815   | 07817   | 99694   | 31 |
| 30 | 00873   | 99996   | 02618   | 99966   | 04362   | 99905   | 06105   | 99813   | 07846   | 99692   | 30 |
| 31 | 00902   | 99996   | 02647   | 99965   | 04391   | 99904   | 06134   | 99812   | 07875   | 99689   | 29 |
| 32 | 00931   | 99996   | 02676   | 99964   | 04420   | 99902   | 06163   | 99810   | 07904   | 99687   | 28 |
| 33 | 00960   | 99995   | 02705   | 99963   | 04449   | 99901   | 06192   | 99808   | 07933   | 99685   | 27 |
| 34 | 00989   | 99995   | 02734   | 99963   | 04478   | 99900   | 06221   | 99806   | 07962   | 99683   | 26 |
| 35 | 01018   | 99995   | 02763   | 99962   | 04507   | 99898   | 06250   | 99804   | 07991   | 99680   | 25 |
| 36 | 01047   | 99995   | 02792   | 99961   | 04536   | 99897   | 06279   | 99803   | 08020   | 99678   | 24 |
| 37 | 01076   | 99994   | 02821   | 99960   | 04565   | 99896   | 06308   | 99801   | 08049   | 99676   | 23 |
| 38 | 01105   | 99994   | 02850   | 99959   | 04594   | 99894   | 06337   | 99799   | 08078   | 99673   | 22 |
| 39 | 01134   | 99994   | 02879   | 99959   | 04623   | 99893   | 06366   | 99797   | 08107   | 99671   | 21 |
| 40 | 01164   | 99993   | 02908   | 99958   | 04653   | 99892   | 06395   | 99795   | 08136   | 99668   | 20 |
| 41 | 01193   | 99993   | 02938   | 99957   | 04682   | 99890   | 06424   | 99793   | 08165   | 99666   | 19 |
| 42 | 01222   | 99993   | 02967   | 99956   | 04711   | 99889   | 06453   | 99792   | 08194   | 99664   | 18 |
| 43 | 01251   | 99992   | 02996   | 99955   | 04740   | 99888   | 06482   | 99790   | 08223   | 99661   | 17 |
| 44 | 01280   | 99992   | 03025   | 99954   | 04769   | 99886   | 06511   | 99788   | 08252   | 99659   | 16 |
| 45 | 01309   | 99991   | 03054   | 99953   | 04798   | 99885   | 06540   | 99786   | 08281   | 99657   | 15 |
| 46 | 01338   | 99991   | 03083   | 99952   | 04827   | 99883   | 06569   | 99784   | 08310   | 99654   | 14 |
| 47 | 01367   | 99991   | 03112   | 99952   | 04856   | 99882   | 06598   | 99782   | 08339   | 99652   | 13 |
| 48 | 01396   | 99990   | 03141   | 99951   | 04885   | 99881   | 06627   | 99780   | 08368   | 99649   | 12 |
| 49 | 01425   | 99990   | 03170   | 99950   | 04914   | 99879   | 06656   | 99778   | 08397   | 99647   | 11 |
| 50 | 01454   | 99989   | 03199   | 99949   | 04943   | 99878   | 06685   | 99776   | 08426   | 99644   | 10 |
| 51 | 01483   | 99989   | 03228   | 99948   | 04972   | 99876   | 06714   | 99774   | 08455   | 99642   | 9  |
| 52 | 01513   | 99989   | 03257   | 99947   | 05001   | 99875   | 06743   | 99772   | 08484   | 99639   | 8  |
| 53 | 01542   | 99988   | 03286   | 99946   | 05030   | 99873   | 06773   | 99770   | 08513   | 99637   | 7  |
| 54 | 01571   | 99988   | 03316   | 99945   | 05059   | 99872   | 06802   | 99768   | 08542   | 99635   | 6  |
| 55 | 01600   | 99987   | 03345   | 99944   | 05088   | 99870   | 06831   | 99766   | 08571   | 99632   | 5  |
| 56 | 01629   | 99987   | 03374   | 99943   | 05117   | 99869   | 06860   | 99764   | 08600   | 99630   | 4  |
| 57 | 01658   | 99986   | 03403   | 99942   | 05146   | 99867   | 06889   | 99762   | 08629   | 99627   | 3  |
| 58 | 01687   | 99986   | 03432   | 99941   | 05175   | 99866   | 06918   | 99760   | 08658   | 99625   | 2  |
| 59 | 01716   | 99985   | 03461   | 99940   | 05205   | 99864   | 06947   | 99758   | 08687   | 99622   | 1  |
| 60 | 01745   | 99985   | 03490   | 99939   | 05234   | 99863   | 06976   | 99756   | 08716   | 99619   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 89°     |         | 88°     |         | 87°     |         | 86°     |         | 85°     |         |    |

TABLE III.

NATURAL SINES AND COSINES.

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| °  | 5°     |        | 6°     |        | 7°     |        | 8°     |        | 9°     |        | °  |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
|    | Sine   | Cosine | Sine   | Cosine | Sine   | Cosine | Sine   | Cosine | Sine   | Cosine |    |
| 0  | 08716  | 99619  | 10453  | 99452  | 12187  | 99255  | 13917  | 99027  | 15643  | 98769  | 60 |
| 1  | 08745  | 99617  | 10482  | 99449  | 12216  | 99251  | 13946  | 99023  | 15672  | 98764  | 59 |
| 2  | 08774  | 99614  | 10511  | 99446  | 12245  | 99248  | 13975  | 99019  | 15701  | 98760  | 58 |
| 3  | 08803  | 99612  | 10540  | 99443  | 12274  | 99244  | 14004  | 99015  | 15730  | 98755  | 57 |
| 4  | 08831  | 99609  | 10569  | 99440  | 12302  | 99240  | 14033  | 99011  | 15758  | 98751  | 56 |
| 5  | 08860  | 99607  | 10597  | 99437  | 12331  | 99237  | 14061  | 99006  | 15787  | 98746  | 55 |
| 6  | 08889  | 99604  | 10626  | 99434  | 12360  | 99233  | 14090  | 99002  | 15816  | 98741  | 54 |
| 7  | 08918  | 99602  | 10655  | 99431  | 12389  | 99230  | 14119  | 98998  | 15845  | 98737  | 53 |
| 8  | 08947  | 99599  | 10684  | 99428  | 12418  | 99226  | 14148  | 98994  | 15873  | 98732  | 52 |
| 9  | 08976  | 99596  | 10713  | 99424  | 12447  | 99222  | 14177  | 98990  | 15902  | 98728  | 51 |
| 10 | 09005  | 99594  | 10742  | 99421  | 12476  | 99219  | 14205  | 98986  | 15931  | 98723  | 50 |
| 11 | 09034  | 99591  | 10771  | 99418  | 12504  | 99215  | 14234  | 98982  | 15959  | 98718  | 49 |
| 12 | 09063  | 99588  | 10800  | 99415  | 12533  | 99211  | 14263  | 98978  | 15988  | 98714  | 48 |
| 13 | 09092  | 99586  | 10829  | 99412  | 12562  | 99208  | 14292  | 98973  | 16017  | 98709  | 47 |
| 14 | 09121  | 99583  | 10858  | 99409  | 12591  | 99204  | 14320  | 98969  | 16046  | 98704  | 46 |
| 15 | 09150  | 99580  | 10887  | 99406  | 12620  | 99200  | 14349  | 98965  | 16074  | 98700  | 45 |
| 16 | 09179  | 99578  | 10916  | 99402  | 12649  | 99197  | 14378  | 98961  | 16103  | 98695  | 44 |
| 17 | 09208  | 99575  | 10945  | 99399  | 12678  | 99193  | 14407  | 98957  | 16132  | 98690  | 43 |
| 18 | 09237  | 99572  | 10973  | 99396  | 12706  | 99189  | 14436  | 98953  | 16160  | 98686  | 42 |
| 19 | 09266  | 99570  | 11002  | 99393  | 12735  | 99186  | 14464  | 98948  | 16189  | 98681  | 41 |
| 20 | 09295  | 99567  | 11031  | 99390  | 12764  | 99182  | 14493  | 98944  | 16218  | 98676  | 40 |
| 21 | 09324  | 99564  | 11060  | 99386  | 12793  | 99178  | 14522  | 98940  | 16246  | 98671  | 39 |
| 22 | 09353  | 99562  | 11089  | 99383  | 12822  | 99175  | 14551  | 98936  | 16275  | 98667  | 38 |
| 23 | 09382  | 99559  | 11118  | 99380  | 12851  | 99171  | 14580  | 98931  | 16304  | 98662  | 37 |
| 24 | 09411  | 99556  | 11147  | 99377  | 12880  | 99167  | 14608  | 98927  | 16333  | 98657  | 36 |
| 25 | 09440  | 99553  | 11176  | 99374  | 12908  | 99163  | 14637  | 98923  | 16361  | 98652  | 35 |
| 26 | 09469  | 99551  | 11205  | 99370  | 12937  | 99160  | 14666  | 98919  | 16390  | 98648  | 34 |
| 27 | 09498  | 99548  | 11234  | 99367  | 12966  | 99156  | 14695  | 98914  | 16419  | 98643  | 33 |
| 28 | 09527  | 99545  | 11263  | 99364  | 12995  | 99152  | 14723  | 98910  | 16447  | 98638  | 32 |
| 29 | 09556  | 99542  | 11291  | 99360  | 13024  | 99148  | 14752  | 98906  | 16476  | 98633  | 31 |
| 30 | 09585  | 99540  | 11320  | 99357  | 13053  | 99144  | 14781  | 98902  | 16505  | 98629  | 30 |
| 31 | 09614  | 99537  | 11349  | 99354  | 13081  | 99141  | 14810  | 98897  | 16533  | 98624  | 29 |
| 32 | 09642  | 99534  | 11378  | 99351  | 13110  | 99137  | 14838  | 98893  | 16562  | 98619  | 28 |
| 33 | 09671  | 99531  | 11407  | 99347  | 13139  | 99133  | 14867  | 98889  | 16591  | 98614  | 27 |
| 34 | 09700  | 99528  | 11436  | 99344  | 13168  | 99129  | 14896  | 98884  | 16620  | 98609  | 26 |
| 35 | 09729  | 99526  | 11465  | 99341  | 13197  | 99125  | 14925  | 98880  | 16648  | 98604  | 25 |
| 36 | 09758  | 99523  | 11494  | 99337  | 13226  | 99122  | 14954  | 98876  | 16677  | 98600  | 24 |
| 37 | 09787  | 99520  | 11523  | 99334  | 13254  | 99118  | 14982  | 98871  | 16706  | 98595  | 23 |
| 38 | 09816  | 99517  | 11552  | 99331  | 13283  | 99114  | 15011  | 98867  | 16734  | 98590  | 22 |
| 39 | 09845  | 99514  | 11580  | 99327  | 13312  | 99110  | 15040  | 98863  | 16763  | 98585  | 21 |
| 40 | 09874  | 99511  | 11609  | 99324  | 13341  | 99106  | 15069  | 98858  | 16792  | 98580  | 20 |
| 41 | 09903  | 99508  | 11638  | 99320  | 13370  | 99102  | 15097  | 98854  | 16820  | 98575  | 19 |
| 42 | 09932  | 99506  | 11667  | 99317  | 13399  | 99098  | 15126  | 98849  | 16849  | 98570  | 18 |
| 43 | 09961  | 99503  | 11696  | 99314  | 13427  | 99094  | 15155  | 98845  | 16878  | 98565  | 17 |
| 44 | 09990  | 99500  | 11725  | 99310  | 13456  | 99091  | 15184  | 98841  | 16906  | 98561  | 16 |
| 45 | 10019  | 99497  | 11754  | 99307  | 13485  | 99087  | 15212  | 98836  | 16935  | 98556  | 15 |
| 46 | 10048  | 99494  | 11783  | 99303  | 13514  | 99083  | 15241  | 98832  | 16964  | 98551  | 14 |
| 47 | 10077  | 99491  | 11812  | 99300  | 13543  | 99079  | 15270  | 98827  | 16992  | 98546  | 13 |
| 48 | 10106  | 99488  | 11840  | 99297  | 13572  | 99075  | 15299  | 98823  | 17021  | 98541  | 12 |
| 49 | 10135  | 99485  | 11869  | 99293  | 13600  | 99071  | 15327  | 98818  | 17050  | 98536  | 11 |
| 50 | 10164  | 99482  | 11898  | 99290  | 13629  | 99067  | 15356  | 98814  | 17078  | 98531  | 10 |
| 51 | 10192  | 99479  | 11927  | 99286  | 13658  | 99063  | 15385  | 98809  | 17107  | 98526  | 9  |
| 52 | 10221  | 99476  | 11956  | 99283  | 13687  | 99059  | 15414  | 98805  | 17136  | 98521  | 8  |
| 53 | 10250  | 99473  | 11985  | 99279  | 13716  | 99055  | 15442  | 98800  | 17164  | 98516  | 7  |
| 54 | 10279  | 99470  | 12014  | 99276  | 13744  | 99051  | 15471  | 98796  | 17193  | 98511  | 6  |
| 55 | 10308  | 99467  | 12043  | 99272  | 13773  | 99047  | 15500  | 98791  | 17222  | 98506  | 5  |
| 56 | 10337  | 99464  | 12071  | 99269  | 13802  | 99043  | 15529  | 98787  | 17250  | 98501  | 4  |
| 57 | 10366  | 99461  | 12100  | 99265  | 13831  | 99039  | 15557  | 98782  | 17279  | 98496  | 3  |
| 58 | 10395  | 99458  | 12129  | 99262  | 13860  | 99035  | 15586  | 98778  | 17308  | 98491  | 2  |
| 59 | 10424  | 99455  | 12158  | 99258  | 13889  | 99031  | 15615  | 98773  | 17336  | 98486  | 1  |
| 60 | 10453  | 99452  | 12187  | 99255  | 13917  | 99027  | 15643  | 98769  | 17365  | 98481  | 0  |
|    | Cosine | Sine   | Cosine | Sine   | Cosine | Sine   | Cosine | Sine   | Cosine | Sine   |    |
|    | 84°    |        | 88°    |        | 82°    |        | 81°    |        | 80°    |        |    |

|    | 10°     |         | 11°     |         | 12°     |         | 13°     |         | 14°     |         |    |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 17365   | 98481   | 19081   | 98163   | 20791   | 97815   | 22495   | 97437   | 24192   | 97030   | 60 |
| 1  | 17393   | 98476   | 19109   | 98157   | 20820   | 97809   | 22523   | 97430   | 24220   | 97023   | 59 |
| 2  | 17422   | 98471   | 19136   | 98152   | 20848   | 97803   | 22552   | 97424   | 24249   | 97015   | 58 |
| 3  | 17451   | 98466   | 19167   | 98146   | 20877   | 97797   | 22580   | 97417   | 24277   | 97008   | 57 |
| 4  | 17479   | 98461   | 19195   | 98140   | 20905   | 97791   | 22608   | 97411   | 24305   | 97001   | 56 |
| 5  | 17508   | 98455   | 19224   | 98135   | 20933   | 97784   | 22637   | 97404   | 24333   | 96994   | 55 |
| 6  | 17537   | 98450   | 19252   | 98129   | 20962   | 97778   | 22665   | 97398   | 24362   | 96987   | 54 |
| 7  | 17565   | 98445   | 19281   | 98124   | 20990   | 97772   | 22693   | 97391   | 24390   | 96980   | 53 |
| 8  | 17594   | 98440   | 19309   | 98118   | 21019   | 97766   | 22722   | 97384   | 24418   | 96973   | 52 |
| 9  | 17623   | 98435   | 19338   | 98112   | 21047   | 97760   | 22750   | 97378   | 24446   | 96966   | 51 |
| 10 | 17651   | 98430   | 19366   | 98107   | 21076   | 97754   | 22778   | 97371   | 24474   | 96959   | 50 |
| 11 | 17680   | 98425   | 19395   | 98101   | 21104   | 97748   | 22807   | 97365   | 24503   | 96952   | 49 |
| 12 | 17708   | 98420   | 19423   | 98096   | 21132   | 97742   | 22835   | 97358   | 24531   | 96945   | 48 |
| 13 | 17737   | 98414   | 19452   | 98090   | 21161   | 97735   | 22863   | 97351   | 24559   | 96937   | 47 |
| 14 | 17766   | 98409   | 19481   | 98084   | 21189   | 97729   | 22892   | 97345   | 24587   | 96930   | 46 |
| 15 | 17794   | 98404   | 19509   | 98079   | 21218   | 97723   | 22920   | 97338   | 24615   | 96923   | 45 |
| 16 | 17823   | 98399   | 19538   | 98073   | 21246   | 97717   | 22948   | 97331   | 24644   | 96916   | 44 |
| 17 | 17852   | 98394   | 19566   | 98067   | 21275   | 97711   | 22977   | 97325   | 24672   | 96909   | 43 |
| 18 | 17880   | 98389   | 19595   | 98061   | 21303   | 97705   | 23005   | 97318   | 24700   | 96902   | 42 |
| 19 | 17909   | 98383   | 19623   | 98056   | 21331   | 97699   | 23033   | 97311   | 24728   | 96894   | 41 |
| 20 | 17937   | 98378   | 19652   | 98050   | 21360   | 97692   | 23062   | 97304   | 24756   | 96887   | 40 |
| 21 | 17966   | 98373   | 19680   | 98044   | 21388   | 97686   | 23090   | 97298   | 24784   | 96880   | 39 |
| 22 | 17995   | 98368   | 19709   | 98039   | 21417   | 97680   | 23118   | 97291   | 24813   | 96873   | 38 |
| 23 | 18023   | 98362   | 19737   | 98033   | 21445   | 97673   | 23146   | 97284   | 24841   | 96866   | 37 |
| 24 | 18052   | 98357   | 19766   | 98027   | 21474   | 97667   | 23175   | 97278   | 24869   | 96858   | 36 |
| 25 | 18081   | 98352   | 19794   | 98021   | 21502   | 97661   | 23203   | 97271   | 24897   | 96851   | 35 |
| 26 | 18109   | 98347   | 19823   | 98016   | 21530   | 97655   | 23231   | 97264   | 24925   | 96844   | 34 |
| 27 | 18138   | 98341   | 19851   | 98010   | 21559   | 97648   | 23260   | 97257   | 24954   | 96837   | 33 |
| 28 | 18166   | 98336   | 19880   | 98004   | 21587   | 97642   | 23288   | 97251   | 24982   | 96829   | 32 |
| 29 | 18195   | 98331   | 19908   | 97998   | 21616   | 97636   | 23316   | 97244   | 25010   | 96822   | 31 |
| 30 | 18224   | 98325   | 19937   | 97992   | 21644   | 97630   | 23345   | 97237   | 25038   | 96815   | 30 |
| 31 | 18252   | 98320   | 19965   | 97987   | 21672   | 97623   | 23373   | 97230   | 25066   | 96807   | 29 |
| 32 | 18281   | 98315   | 19994   | 97981   | 21701   | 97617   | 23401   | 97223   | 25094   | 96800   | 28 |
| 33 | 18309   | 98310   | 20022   | 97975   | 21729   | 97611   | 23429   | 97217   | 25122   | 96793   | 27 |
| 34 | 18338   | 98304   | 20051   | 97969   | 21758   | 97604   | 23458   | 97210   | 25151   | 96786   | 26 |
| 35 | 18367   | 98299   | 20079   | 97963   | 21786   | 97598   | 23486   | 97203   | 25179   | 96778   | 25 |
| 36 | 18395   | 98294   | 20108   | 97958   | 21814   | 97592   | 23514   | 97196   | 25207   | 96771   | 24 |
| 37 | 18424   | 98288   | 20136   | 97952   | 21843   | 97585   | 23542   | 97189   | 25235   | 96764   | 23 |
| 38 | 18452   | 98283   | 20165   | 97946   | 21871   | 97579   | 23571   | 97182   | 25263   | 96756   | 22 |
| 39 | 18481   | 98277   | 20193   | 97940   | 21899   | 97573   | 23599   | 97176   | 25291   | 96749   | 21 |
| 40 | 18509   | 98272   | 20222   | 97934   | 21928   | 97566   | 23627   | 97169   | 25320   | 96742   | 20 |
| 41 | 18538   | 98267   | 20250   | 97928   | 21956   | 97560   | 23656   | 97162   | 25348   | 96734   | 19 |
| 42 | 18567   | 98261   | 20279   | 97922   | 21985   | 97553   | 23684   | 97155   | 25376   | 96727   | 18 |
| 43 | 18595   | 98256   | 20307   | 97916   | 22013   | 97547   | 23712   | 97148   | 25404   | 96719   | 17 |
| 44 | 18624   | 98250   | 20336   | 97910   | 22041   | 97541   | 23740   | 97141   | 25432   | 96712   | 16 |
| 45 | 18652   | 98245   | 20364   | 97905   | 22070   | 97534   | 23769   | 97134   | 25460   | 96705   | 15 |
| 46 | 18681   | 98240   | 20393   | 97899   | 22098   | 97528   | 23797   | 97127   | 25488   | 96697   | 14 |
| 47 | 18710   | 98234   | 20421   | 97893   | 22126   | 97521   | 23825   | 97120   | 25516   | 96690   | 13 |
| 48 | 18738   | 98229   | 20450   | 97887   | 22155   | 97515   | 23853   | 97113   | 25545   | 96682   | 12 |
| 49 | 18767   | 98223   | 20478   | 97881   | 22183   | 97508   | 23882   | 97106   | 25573   | 96675   | 11 |
| 50 | 18795   | 98218   | 20507   | 97875   | 22212   | 97502   | 23910   | 97100   | 25601   | 96667   | 10 |
| 51 | 18824   | 98212   | 20535   | 97869   | 22240   | 97496   | 23938   | 97093   | 25629   | 96660   | 9  |
| 52 | 18852   | 98207   | 20563   | 97863   | 22268   | 97489   | 23966   | 97086   | 25657   | 96653   | 8  |
| 53 | 18881   | 98201   | 20592   | 97857   | 22297   | 97483   | 23995   | 97079   | 25685   | 96645   | 7  |
| 54 | 18910   | 98196   | 20620   | 97851   | 22325   | 97476   | 24023   | 97072   | 25713   | 96638   | 6  |
| 55 | 18938   | 98190   | 20649   | 97845   | 22353   | 97470   | 24051   | 97065   | 25741   | 96630   | 5  |
| 56 | 18967   | 98185   | 20677   | 97839   | 22382   | 97463   | 24079   | 97058   | 25769   | 96623   | 4  |
| 57 | 18995   | 98179   | 20706   | 97833   | 22410   | 97457   | 24108   | 97051   | 25796   | 96615   | 3  |
| 58 | 19024   | 98174   | 20734   | 97827   | 22438   | 97450   | 24136   | 97044   | 25826   | 96608   | 2  |
| 59 | 19052   | 98168   | 20763   | 97821   | 22467   | 97444   | 24164   | 97037   | 25854   | 96600   | 1  |
| 60 | 19081   | 98163   | 20791   | 97815   | 22495   | 97437   | 24192   | 97030   | 25882   | 96593   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 79°     |         | 78°     |         | 77°     |         | 76°     |         | 75°     |         |    |

TABLE III.

## NATURAL SINES AND COSINES.

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| °  | 15°     |         | 16°     |         | 17°     |         | 18°     |         | 19°     |         | °  |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 25882   | 96593   | 27564   | 96126   | 29237   | 95630   | 30902   | 95106   | 32557   | 94552   | 60 |
| 1  | 25910   | 96585   | 27592   | 96118   | 29265   | 95622   | 30929   | 95097   | 32584   | 94542   | 59 |
| 2  | 25938   | 96578   | 27620   | 96110   | 29293   | 95613   | 30957   | 95088   | 32612   | 94533   | 58 |
| 3  | 25966   | 96570   | 27648   | 96102   | 29321   | 95605   | 30985   | 95079   | 32639   | 94523   | 57 |
| 4  | 25994   | 96562   | 27676   | 96094   | 29348   | 95596   | 31012   | 95070   | 32667   | 94514   | 56 |
| 5  | 26022   | 96555   | 27704   | 96086   | 29376   | 95588   | 31040   | 95061   | 32694   | 94504   | 55 |
| 6  | 26050   | 96547   | 27731   | 96078   | 29404   | 95579   | 31068   | 95052   | 32722   | 94495   | 54 |
| 7  | 26079   | 96540   | 27759   | 96070   | 29432   | 95571   | 31095   | 95043   | 32749   | 94485   | 53 |
| 8  | 26107   | 96532   | 27787   | 96062   | 29460   | 95562   | 31123   | 95033   | 32777   | 94476   | 52 |
| 9  | 26135   | 96524   | 27815   | 96054   | 29487   | 95554   | 31151   | 95024   | 32804   | 94466   | 51 |
| 10 | 26163   | 96517   | 27843   | 96046   | 29515   | 95545   | 31178   | 95015   | 32832   | 94457   | 50 |
| 11 | 26191   | 96509   | 27871   | 96037   | 29543   | 95536   | 31206   | 95006   | 32859   | 94447   | 49 |
| 12 | 26219   | 96502   | 27899   | 96029   | 29571   | 95528   | 31233   | 94997   | 32887   | 94438   | 48 |
| 13 | 26247   | 96494   | 27927   | 96021   | 29599   | 95519   | 31261   | 94988   | 32914   | 94428   | 47 |
| 14 | 26275   | 96486   | 27955   | 96013   | 29626   | 95511   | 31289   | 94979   | 32942   | 94418   | 46 |
| 15 | 26303   | 96479   | 27983   | 96005   | 29654   | 95502   | 31316   | 94970   | 32969   | 94409   | 45 |
| 16 | 26331   | 96471   | 28011   | 95997   | 29682   | 95493   | 31344   | 94961   | 32997   | 94399   | 44 |
| 17 | 26359   | 96463   | 28039   | 95989   | 29710   | 95485   | 31372   | 94952   | 33024   | 94390   | 43 |
| 18 | 26387   | 96456   | 28067   | 95981   | 29737   | 95476   | 31399   | 94943   | 33051   | 94380   | 42 |
| 19 | 26415   | 96448   | 28095   | 95972   | 29765   | 95467   | 31427   | 94934   | 33079   | 94370   | 41 |
| 20 | 26443   | 96440   | 28123   | 95964   | 29793   | 95459   | 31454   | 94924   | 33106   | 94361   | 40 |
| 21 | 26471   | 96433   | 28150   | 95956   | 29821   | 95450   | 31482   | 94915   | 33134   | 94351   | 39 |
| 22 | 26500   | 96425   | 28178   | 95948   | 29849   | 95441   | 31510   | 94906   | 33161   | 94342   | 38 |
| 23 | 26528   | 96417   | 28206   | 95940   | 29876   | 95433   | 31537   | 94897   | 33189   | 94332   | 37 |
| 24 | 26556   | 96410   | 28234   | 95931   | 29904   | 95424   | 31565   | 94888   | 33216   | 94322   | 36 |
| 25 | 26584   | 96402   | 28262   | 95923   | 29932   | 95415   | 31593   | 94878   | 33244   | 94313   | 35 |
| 26 | 26612   | 96394   | 28290   | 95915   | 29960   | 95407   | 31620   | 94869   | 33271   | 94303   | 34 |
| 27 | 26640   | 96386   | 28318   | 95907   | 29987   | 95398   | 31648   | 94860   | 33298   | 94293   | 33 |
| 28 | 26668   | 96379   | 28346   | 95898   | 30015   | 95389   | 31675   | 94851   | 33326   | 94284   | 32 |
| 29 | 26696   | 96371   | 28374   | 95890   | 30043   | 95380   | 31703   | 94842   | 33353   | 94274   | 31 |
| 30 | 26724   | 96363   | 28402   | 95882   | 30071   | 95372   | 31730   | 94832   | 33381   | 94264   | 30 |
| 31 | 26752   | 96355   | 28429   | 95874   | 30098   | 95363   | 31758   | 94823   | 33408   | 94254   | 29 |
| 32 | 26780   | 96347   | 28457   | 95865   | 30126   | 95354   | 31786   | 94814   | 33436   | 94245   | 28 |
| 33 | 26808   | 96340   | 28485   | 95857   | 30154   | 95345   | 31813   | 94805   | 33463   | 94235   | 27 |
| 34 | 26836   | 96332   | 28513   | 95849   | 30182   | 95337   | 31841   | 94795   | 33490   | 94225   | 26 |
| 35 | 26864   | 96324   | 28541   | 95841   | 30209   | 95328   | 31868   | 94786   | 33518   | 94215   | 25 |
| 36 | 26892   | 96316   | 28569   | 95832   | 30237   | 95319   | 31896   | 94777   | 33545   | 94206   | 24 |
| 37 | 26920   | 96308   | 28597   | 95824   | 30265   | 95310   | 31923   | 94768   | 33573   | 94196   | 23 |
| 38 | 26948   | 96301   | 28625   | 95816   | 30292   | 95301   | 31951   | 94758   | 33600   | 94186   | 22 |
| 39 | 26976   | 96293   | 28652   | 95807   | 30320   | 95293   | 31979   | 94749   | 33627   | 94176   | 21 |
| 40 | 27004   | 96285   | 28680   | 95799   | 30348   | 95284   | 32006   | 94740   | 33655   | 94167   | 20 |
| 41 | 27032   | 96277   | 28708   | 95791   | 30376   | 95275   | 32034   | 94730   | 33682   | 94157   | 19 |
| 42 | 27060   | 96269   | 28736   | 95782   | 30403   | 95266   | 32061   | 94721   | 33710   | 94147   | 18 |
| 43 | 27088   | 96261   | 28764   | 95774   | 30431   | 95257   | 32089   | 94712   | 33737   | 94137   | 17 |
| 44 | 27116   | 96253   | 28792   | 95766   | 30459   | 95248   | 32116   | 94702   | 33764   | 94127   | 16 |
| 45 | 27144   | 96246   | 28820   | 95757   | 30486   | 95240   | 32144   | 94693   | 33792   | 94118   | 15 |
| 46 | 27172   | 96238   | 28847   | 95749   | 30514   | 95231   | 32171   | 94684   | 33819   | 94108   | 14 |
| 47 | 27200   | 96230   | 28875   | 95740   | 30542   | 95222   | 32199   | 94674   | 33846   | 94098   | 13 |
| 48 | 27228   | 96222   | 28903   | 95732   | 30570   | 95213   | 32227   | 94665   | 33874   | 94088   | 12 |
| 49 | 27256   | 96214   | 28931   | 95724   | 30597   | 95204   | 32254   | 94656   | 33901   | 94078   | 11 |
| 50 | 27284   | 96206   | 28959   | 95715   | 30625   | 95195   | 32282   | 94646   | 33929   | 94068   | 10 |
| 51 | 27312   | 96198   | 28987   | 95707   | 30653   | 95186   | 32309   | 94637   | 33956   | 94058   | 9  |
| 52 | 27340   | 96190   | 29015   | 95698   | 30680   | 95177   | 32337   | 94627   | 33983   | 94049   | 8  |
| 53 | 27368   | 96182   | 29042   | 95690   | 30708   | 95168   | 32364   | 94618   | 34011   | 94039   | 7  |
| 54 | 27396   | 96174   | 29070   | 95681   | 30736   | 95159   | 32392   | 94609   | 34038   | 94029   | 6  |
| 55 | 27424   | 96166   | 29098   | 95673   | 30763   | 95150   | 32419   | 94599   | 34065   | 94019   | 5  |
| 56 | 27452   | 96158   | 29126   | 95664   | 30791   | 95142   | 32447   | 94590   | 34093   | 94009   | 4  |
| 57 | 27480   | 96150   | 29154   | 95656   | 30819   | 95133   | 32474   | 94580   | 34120   | 93999   | 3  |
| 58 | 27508   | 96142   | 29182   | 95647   | 30846   | 95124   | 32502   | 94571   | 34147   | 93989   | 2  |
| 59 | 27536   | 96134   | 29209   | 95639   | 30874   | 95115   | 32529   | 94561   | 34175   | 93979   | 1  |
| 60 | 27564   | 96126   | 29237   | 95630   | 30902   | 95106   | 32557   | 94552   | 34202   | 93969   | 0  |
|    | Cosine. | Sine    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 74°     |         | 78°     |         | 72°     |         | 71°     |         | 70°     |         |    |

| °  | 20°     |         | 21°     |         | 22°     |         | 23°     |         | 24°     |         | °  |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 34202   | 93969   | 35837   | 93358   | 37461   | 92718   | 39073   | 92050   | 40674   | 91355   | 60 |
| 1  | 34229   | 93959   | 35864   | 93348   | 37488   | 92707   | 39100   | 92039   | 40700   | 91343   | 59 |
| 2  | 34257   | 93949   | 35891   | 93337   | 37515   | 92697   | 39127   | 92028   | 40727   | 91331   | 58 |
| 3  | 34284   | 93939   | 35918   | 93327   | 37542   | 92686   | 39153   | 92016   | 40753   | 91319   | 57 |
| 4  | 34311   | 93929   | 35945   | 93316   | 37569   | 92675   | 39180   | 92005   | 40780   | 91307   | 56 |
| 5  | 34339   | 93919   | 35973   | 93306   | 37595   | 92664   | 39207   | 91994   | 40806   | 91295   | 55 |
| 6  | 34366   | 93909   | 36000   | 93295   | 37622   | 92653   | 39234   | 91982   | 40833   | 91283   | 54 |
| 7  | 34393   | 93899   | 36027   | 93285   | 37649   | 92642   | 39260   | 91971   | 40860   | 91272   | 53 |
| 8  | 34421   | 93889   | 36054   | 93274   | 37676   | 92631   | 39287   | 91959   | 40886   | 91260   | 52 |
| 9  | 34448   | 93879   | 36081   | 93264   | 37703   | 92620   | 39314   | 91948   | 40913   | 91248   | 51 |
| 10 | 34475   | 93869   | 36108   | 93253   | 37730   | 92609   | 39341   | 91936   | 40939   | 91236   | 50 |
| 11 | 34503   | 93859   | 36135   | 93243   | 37757   | 92598   | 39367   | 91925   | 40966   | 91224   | 49 |
| 12 | 34530   | 93849   | 36162   | 93232   | 37784   | 92587   | 39394   | 91914   | 40992   | 91212   | 48 |
| 13 | 34557   | 93839   | 36190   | 93222   | 37811   | 92576   | 39421   | 91902   | 41019   | 91200   | 47 |
| 14 | 34584   | 93829   | 36217   | 93211   | 37838   | 92565   | 39448   | 91891   | 41045   | 91188   | 46 |
| 15 | 34612   | 93819   | 36244   | 93201   | 37865   | 92554   | 39474   | 91879   | 41072   | 91176   | 45 |
| 16 | 34639   | 93809   | 36271   | 93190   | 37892   | 92543   | 39501   | 91868   | 41098   | 91164   | 44 |
| 17 | 34666   | 93799   | 36298   | 93180   | 37919   | 92532   | 39528   | 91856   | 41125   | 91152   | 43 |
| 18 | 34694   | 93789   | 36325   | 93169   | 37946   | 92521   | 39555   | 91845   | 41151   | 91140   | 42 |
| 19 | 34721   | 93779   | 36352   | 93159   | 37973   | 92510   | 39581   | 91833   | 41178   | 91128   | 41 |
| 20 | 34748   | 93769   | 36379   | 93148   | 37999   | 92499   | 39608   | 91822   | 41204   | 91116   | 40 |
| 21 | 34775   | 93759   | 36406   | 93137   | 38026   | 92488   | 39635   | 91810   | 41231   | 91104   | 39 |
| 22 | 34803   | 93748   | 36434   | 93127   | 38053   | 92477   | 39661   | 91799   | 41257   | 91092   | 38 |
| 23 | 34830   | 93738   | 36461   | 93116   | 38080   | 92466   | 39688   | 91787   | 41284   | 91080   | 37 |
| 24 | 34857   | 93728   | 36488   | 93106   | 38107   | 92455   | 39715   | 91775   | 41310   | 91068   | 36 |
| 25 | 34884   | 93718   | 36515   | 93095   | 38134   | 92444   | 39741   | 91764   | 41337   | 91056   | 35 |
| 26 | 34912   | 93708   | 36542   | 93084   | 38161   | 92432   | 39768   | 91752   | 41363   | 91044   | 34 |
| 27 | 34939   | 93698   | 36569   | 93074   | 38188   | 92421   | 39795   | 91741   | 41390   | 91032   | 33 |
| 28 | 34966   | 93688   | 36596   | 93063   | 38215   | 92410   | 39822   | 91729   | 41416   | 91020   | 32 |
| 29 | 34993   | 93677   | 36623   | 93052   | 38241   | 92399   | 39848   | 91718   | 41443   | 91008   | 31 |
| 30 | 35021   | 93667   | 36650   | 93042   | 38268   | 92388   | 39875   | 91706   | 41469   | 90996   | 30 |
| 31 | 35048   | 93657   | 36677   | 93031   | 38295   | 92377   | 39902   | 91694   | 41496   | 90984   | 29 |
| 32 | 35075   | 93647   | 36704   | 93020   | 38322   | 92366   | 39928   | 91683   | 41522   | 90972   | 28 |
| 33 | 35102   | 93637   | 36731   | 93010   | 38349   | 92355   | 39955   | 91671   | 41549   | 90960   | 27 |
| 34 | 35130   | 93626   | 36758   | 92999   | 38376   | 92343   | 39982   | 91660   | 41575   | 90948   | 26 |
| 35 | 35157   | 93616   | 36785   | 92988   | 38403   | 92332   | 40008   | 91648   | 41602   | 90936   | 25 |
| 36 | 35184   | 93606   | 36812   | 92978   | 38430   | 92321   | 40035   | 91636   | 41628   | 90924   | 24 |
| 37 | 35211   | 93596   | 36839   | 92967   | 38456   | 92310   | 40062   | 91625   | 41655   | 90911   | 23 |
| 38 | 35239   | 93585   | 36867   | 92956   | 38483   | 92299   | 40088   | 91613   | 41681   | 90899   | 22 |
| 39 | 35266   | 93575   | 36894   | 92945   | 38510   | 92287   | 40115   | 91601   | 41707   | 90887   | 21 |
| 40 | 35293   | 93565   | 36921   | 92935   | 38537   | 92276   | 40141   | 91590   | 41734   | 90875   | 20 |
| 41 | 35320   | 93555   | 36948   | 92924   | 38564   | 92265   | 40168   | 91578   | 41760   | 90863   | 19 |
| 42 | 35347   | 93544   | 36975   | 92913   | 38591   | 92254   | 40195   | 91566   | 41787   | 90851   | 18 |
| 43 | 35375   | 93534   | 37002   | 92902   | 38617   | 92243   | 40221   | 91555   | 41813   | 90839   | 17 |
| 44 | 35402   | 93524   | 37029   | 92892   | 38644   | 92231   | 40248   | 91543   | 41840   | 90826   | 16 |
| 45 | 35429   | 93514   | 37056   | 92881   | 38671   | 92220   | 40275   | 91531   | 41866   | 90814   | 15 |
| 46 | 35456   | 93503   | 37083   | 92870   | 38698   | 92209   | 40301   | 91519   | 41892   | 90802   | 14 |
| 47 | 35484   | 93493   | 37110   | 92859   | 38725   | 92198   | 40328   | 91508   | 41919   | 90790   | 13 |
| 48 | 35511   | 93483   | 37137   | 92849   | 38752   | 92186   | 40355   | 91496   | 41945   | 90778   | 12 |
| 49 | 35538   | 93472   | 37164   | 92838   | 38778   | 92175   | 40381   | 91484   | 41972   | 90766   | 11 |
| 50 | 35565   | 93462   | 37191   | 92827   | 38805   | 92164   | 40408   | 91472   | 41998   | 90753   | 10 |
| 51 | 35592   | 93452   | 37218   | 92816   | 38832   | 92152   | 40434   | 91461   | 42024   | 90741   | 9  |
| 52 | 35619   | 93441   | 37245   | 92805   | 38859   | 92141   | 40461   | 91449   | 42051   | 90729   | 8  |
| 53 | 35647   | 93431   | 37272   | 92794   | 38886   | 92130   | 40488   | 91437   | 42077   | 90717   | 7  |
| 54 | 35674   | 93420   | 37299   | 92784   | 38912   | 92119   | 40514   | 91425   | 42104   | 90704   | 6  |
| 55 | 35701   | 93410   | 37326   | 92773   | 38939   | 92107   | 40541   | 91414   | 42130   | 90692   | 5  |
| 56 | 35728   | 93400   | 37353   | 92762   | 38966   | 92096   | 40567   | 91402   | 42156   | 90680   | 4  |
| 57 | 35755   | 93389   | 37380   | 92751   | 38993   | 92085   | 40594   | 91390   | 42183   | 90668   | 3  |
| 58 | 35782   | 93379   | 37407   | 92740   | 39020   | 92073   | 40621   | 91378   | 42209   | 90655   | 2  |
| 59 | 35810   | 93368   | 37434   | 92729   | 39046   | 92062   | 40647   | 91366   | 42235   | 90643   | 1  |
| 60 | 35837   | 93358   | 37461   | 92718   | 39073   | 92050   | 40674   | 91355   | 42262   | 90631   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 69°     |         | 68°     |         | 67°     |         | 66°     |         | 65°     |         |    |

TABLE III.

## NATURAL SINES AND COSINES.

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| °  | 25°     |         | 26°     |         | 27°     |         | 28°     |         | 29°     |         | °  |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 42262   | 90631   | 43837   | 89879   | 45399   | 89101   | 46947   | 88295   | 48481   | 87462   | 60 |
| 1  | 42288   | 90618   | 43863   | 89867   | 45425   | 89087   | 46973   | 88281   | 48506   | 87448   | 59 |
| 2  | 42315   | 90606   | 43889   | 89854   | 45451   | 89074   | 46999   | 88267   | 48532   | 87434   | 58 |
| 3  | 42341   | 90594   | 43916   | 89841   | 45477   | 89061   | 47024   | 88254   | 48557   | 87420   | 57 |
| 4  | 42367   | 90582   | 43942   | 89828   | 45503   | 89048   | 47050   | 88240   | 48583   | 87406   | 56 |
| 5  | 42394   | 90569   | 43968   | 89816   | 45529   | 89035   | 47076   | 88226   | 48608   | 87391   | 55 |
| 6  | 42420   | 90557   | 43994   | 89803   | 45554   | 89021   | 47101   | 88213   | 48634   | 87377   | 54 |
| 7  | 42446   | 90545   | 44020   | 89790   | 45580   | 89008   | 47127   | 88199   | 48659   | 87363   | 53 |
| 8  | 42473   | 90532   | 44046   | 89777   | 45606   | 88995   | 47153   | 88185   | 48684   | 87349   | 52 |
| 9  | 42499   | 90520   | 44072   | 89764   | 45632   | 88981   | 47178   | 88172   | 48710   | 87335   | 51 |
| 10 | 42525   | 90507   | 44098   | 89752   | 45658   | 88968   | 47204   | 88158   | 48735   | 87321   | 50 |
| 11 | 42552   | 90495   | 44124   | 89739   | 45684   | 88955   | 47229   | 88144   | 48761   | 87306   | 49 |
| 12 | 42578   | 90483   | 44151   | 89726   | 45710   | 88942   | 47255   | 88130   | 48786   | 87292   | 48 |
| 13 | 42604   | 90470   | 44177   | 89713   | 45736   | 88928   | 47281   | 88117   | 48811   | 87278   | 47 |
| 14 | 42631   | 90458   | 44203   | 89700   | 45762   | 88915   | 47306   | 88103   | 48837   | 87264   | 46 |
| 15 | 42657   | 90446   | 44229   | 89687   | 45787   | 88902   | 47332   | 88089   | 48862   | 87250   | 45 |
| 16 | 42683   | 90433   | 44255   | 89674   | 45813   | 88888   | 47358   | 88075   | 48888   | 87235   | 44 |
| 17 | 42709   | 90421   | 44281   | 89662   | 45839   | 88875   | 47383   | 88062   | 48913   | 87221   | 43 |
| 18 | 42736   | 90408   | 44307   | 89649   | 45865   | 88862   | 47409   | 88048   | 48938   | 87207   | 42 |
| 19 | 42762   | 90396   | 44333   | 89636   | 45891   | 88848   | 47434   | 88034   | 48964   | 87193   | 41 |
| 20 | 42788   | 90383   | 44359   | 89623   | 45917   | 88835   | 47460   | 88020   | 48989   | 87178   | 40 |
| 21 | 42815   | 90371   | 44385   | 89610   | 45942   | 88822   | 47486   | 88006   | 49014   | 87164   | 39 |
| 22 | 42841   | 90358   | 44411   | 89597   | 45968   | 88808   | 47511   | 87993   | 49040   | 87150   | 38 |
| 23 | 42867   | 90346   | 44437   | 89584   | 45994   | 88795   | 47537   | 87979   | 49065   | 87136   | 37 |
| 24 | 42894   | 90334   | 44464   | 89571   | 46020   | 88782   | 47562   | 87965   | 49090   | 87121   | 36 |
| 25 | 42920   | 90321   | 44490   | 89558   | 46046   | 88768   | 47588   | 87951   | 49116   | 87107   | 35 |
| 26 | 42946   | 90309   | 44516   | 89545   | 46072   | 88755   | 47614   | 87937   | 49141   | 87093   | 34 |
| 27 | 42972   | 90296   | 44542   | 89532   | 46097   | 88741   | 47639   | 87923   | 49166   | 87079   | 33 |
| 28 | 42999   | 90284   | 44568   | 89519   | 46123   | 88728   | 47665   | 87909   | 49192   | 87064   | 32 |
| 29 | 43025   | 90271   | 44594   | 89506   | 46149   | 88715   | 47690   | 87896   | 49217   | 87050   | 31 |
| 30 | 43051   | 90259   | 44620   | 89493   | 46175   | 88701   | 47716   | 87882   | 49242   | 87036   | 30 |
| 31 | 43077   | 90246   | 44646   | 89480   | 46201   | 88688   | 47741   | 87868   | 49268   | 87021   | 29 |
| 32 | 43104   | 90233   | 44672   | 89467   | 46226   | 88674   | 47767   | 87854   | 49293   | 87007   | 28 |
| 33 | 43130   | 90221   | 44698   | 89454   | 46252   | 88661   | 47793   | 87840   | 49318   | 86993   | 27 |
| 34 | 43156   | 90208   | 44724   | 89441   | 46278   | 88647   | 47818   | 87826   | 49344   | 86978   | 26 |
| 35 | 43182   | 90196   | 44750   | 89428   | 46304   | 88634   | 47844   | 87812   | 49369   | 86964   | 25 |
| 36 | 43209   | 90183   | 44776   | 89415   | 46330   | 88620   | 47869   | 87798   | 49394   | 86949   | 24 |
| 37 | 43235   | 90171   | 44802   | 89402   | 46355   | 88607   | 47895   | 87784   | 49419   | 86935   | 23 |
| 38 | 43261   | 90158   | 44828   | 89389   | 46381   | 88593   | 47920   | 87770   | 49445   | 86921   | 22 |
| 39 | 43287   | 90146   | 44854   | 89376   | 46407   | 88580   | 47946   | 87756   | 49470   | 86906   | 21 |
| 40 | 43313   | 90133   | 44880   | 89363   | 46433   | 88566   | 47971   | 87743   | 49495   | 86892   | 20 |
| 41 | 43340   | 90120   | 44906   | 89350   | 46458   | 88553   | 47997   | 87729   | 49521   | 86878   | 19 |
| 42 | 43366   | 90108   | 44932   | 89337   | 46484   | 88539   | 48022   | 87715   | 49546   | 86863   | 18 |
| 43 | 43392   | 90095   | 44958   | 89324   | 46510   | 88526   | 48048   | 87701   | 49571   | 86849   | 17 |
| 44 | 43418   | 90082   | 44984   | 89311   | 46536   | 88512   | 48073   | 87687   | 49596   | 86834   | 16 |
| 45 | 43445   | 90070   | 45010   | 89298   | 46561   | 88499   | 48099   | 87673   | 49622   | 86820   | 15 |
| 46 | 43471   | 90057   | 45036   | 89285   | 46587   | 88485   | 48124   | 87659   | 49647   | 86805   | 14 |
| 47 | 43497   | 90045   | 45062   | 89272   | 46613   | 88472   | 48150   | 87645   | 49672   | 86791   | 13 |
| 48 | 43523   | 90032   | 45088   | 89259   | 46639   | 88458   | 48175   | 87631   | 49697   | 86777   | 12 |
| 49 | 43549   | 90019   | 45114   | 89245   | 46664   | 88445   | 48201   | 87617   | 49723   | 86762   | 11 |
| 50 | 43575   | 90007   | 45140   | 89232   | 46690   | 88431   | 48226   | 87603   | 49748   | 86748   | 10 |
| 51 | 43602   | 89994   | 45166   | 89219   | 46716   | 88417   | 48252   | 87589   | 49773   | 86733   | 9  |
| 52 | 43628   | 89981   | 45192   | 89206   | 46742   | 88404   | 48277   | 87575   | 49798   | 86719   | 8  |
| 53 | 43654   | 89968   | 45218   | 89193   | 46767   | 88390   | 48303   | 87561   | 49824   | 86704   | 7  |
| 54 | 43680   | 89956   | 45243   | 89180   | 46793   | 88377   | 48328   | 87546   | 49849   | 86690   | 6  |
| 55 | 43706   | 89943   | 45269   | 89167   | 46819   | 88363   | 48354   | 87532   | 49874   | 86675   | 5  |
| 56 | 43733   | 89930   | 45295   | 89153   | 46844   | 88349   | 48379   | 87518   | 49899   | 86661   | 4  |
| 57 | 43759   | 89918   | 45321   | 89140   | 46870   | 88336   | 48405   | 87504   | 49924   | 86646   | 3  |
| 58 | 43785   | 89905   | 45347   | 89127   | 46896   | 88322   | 48430   | 87490   | 49950   | 86632   | 2  |
| 59 | 43811   | 89892   | 45373   | 89114   | 46921   | 88308   | 48456   | 87476   | 49975   | 86617   | 1  |
| 60 | 43837   | 89879   | 45399   | 89101   | 46947   | 88295   | 48481   | 87462   | 50000   | 86603   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 64°     |         | 63°     |         | 62°     |         | 61°     |         | 60°     |         |    |

|    | 80°     |         | 81°     |         | 82°     |         | 83°     |         | 84°     |         |    |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 50000   | 86603   | 51504   | 85717   | 52992   | 84805   | 54464   | 83867   | 55919   | 82904   | 60 |
| 1  | 50025   | 86588   | 51529   | 85702   | 53017   | 84789   | 54488   | 83851   | 55943   | 82887   | 59 |
| 2  | 50050   | 86573   | 51554   | 85687   | 53041   | 84774   | 54513   | 83835   | 55968   | 82871   | 58 |
| 3  | 50076   | 86559   | 51579   | 85672   | 53066   | 84759   | 54537   | 83819   | 55992   | 82855   | 57 |
| 4  | 50101   | 86544   | 51604   | 85657   | 53091   | 84743   | 54561   | 83804   | 56016   | 82839   | 56 |
| 5  | 50126   | 86530   | 51628   | 85642   | 53115   | 84728   | 54586   | 83788   | 56040   | 82822   | 55 |
| 6  | 50151   | 86515   | 51653   | 85627   | 53140   | 84712   | 54610   | 83772   | 56064   | 82806   | 54 |
| 7  | 50176   | 86501   | 51678   | 85612   | 53164   | 84697   | 54635   | 83756   | 56088   | 82790   | 53 |
| 8  | 50201   | 86486   | 51703   | 85597   | 53189   | 84681   | 54659   | 83740   | 56112   | 82773   | 52 |
| 9  | 50227   | 86471   | 51728   | 85582   | 53214   | 84666   | 54683   | 83724   | 56136   | 82757   | 51 |
| 10 | 50252   | 86457   | 51753   | 85567   | 53238   | 84650   | 54708   | 83708   | 56160   | 82741   | 50 |
| 11 | 50277   | 86442   | 51778   | 85551   | 53263   | 84635   | 54732   | 83692   | 56184   | 82724   | 49 |
| 12 | 50302   | 86427   | 51803   | 85536   | 53288   | 84619   | 54756   | 83676   | 56208   | 82708   | 48 |
| 13 | 50327   | 86413   | 51828   | 85521   | 53312   | 84604   | 54781   | 83660   | 56232   | 82692   | 47 |
| 14 | 50352   | 86398   | 51852   | 85506   | 53337   | 84588   | 54805   | 83645   | 56256   | 82675   | 46 |
| 15 | 50377   | 86384   | 51877   | 85491   | 53361   | 84573   | 54829   | 83629   | 56280   | 82659   | 45 |
| 16 | 50403   | 86369   | 51902   | 85476   | 53386   | 84557   | 54854   | 83613   | 56305   | 82643   | 44 |
| 17 | 50428   | 86354   | 51927   | 85461   | 53411   | 84542   | 54878   | 83597   | 56329   | 82626   | 43 |
| 18 | 50453   | 86340   | 51952   | 85446   | 53435   | 84526   | 54902   | 83581   | 56353   | 82610   | 42 |
| 19 | 50478   | 86325   | 51977   | 85431   | 53460   | 84511   | 54927   | 83565   | 56377   | 82593   | 41 |
| 20 | 50503   | 86310   | 52002   | 85416   | 53484   | 84495   | 54951   | 83549   | 56401   | 82577   | 40 |
| 21 | 50528   | 86295   | 52026   | 85401   | 53509   | 84480   | 54975   | 83533   | 56425   | 82561   | 39 |
| 22 | 50553   | 86281   | 52051   | 85385   | 53534   | 84464   | 54999   | 83517   | 56449   | 82544   | 38 |
| 23 | 50578   | 86266   | 52076   | 85370   | 53558   | 84448   | 55024   | 83501   | 56473   | 82528   | 37 |
| 24 | 50603   | 86251   | 52101   | 85355   | 53583   | 84433   | 55048   | 83485   | 56497   | 82511   | 36 |
| 25 | 50628   | 86237   | 52126   | 85340   | 53607   | 84417   | 55072   | 83469   | 56521   | 82495   | 35 |
| 26 | 50654   | 86222   | 52151   | 85325   | 53632   | 84402   | 55097   | 83453   | 56545   | 82478   | 34 |
| 27 | 50679   | 86207   | 52175   | 85310   | 53656   | 84386   | 55121   | 83437   | 56569   | 82462   | 33 |
| 28 | 50704   | 86192   | 52200   | 85294   | 53681   | 84370   | 55145   | 83421   | 56593   | 82446   | 32 |
| 29 | 50729   | 86178   | 52225   | 85279   | 53705   | 84355   | 55169   | 83405   | 56617   | 82429   | 31 |
| 30 | 50754   | 86163   | 52250   | 85264   | 53730   | 84339   | 55194   | 83389   | 56641   | 82413   | 30 |
| 31 | 50779   | 86148   | 52275   | 85249   | 53754   | 84324   | 55218   | 83373   | 56665   | 82396   | 29 |
| 32 | 50804   | 86133   | 52299   | 85234   | 53779   | 84308   | 55242   | 83356   | 56689   | 82380   | 28 |
| 33 | 50829   | 86119   | 52324   | 85218   | 53804   | 84292   | 55266   | 83340   | 56713   | 82363   | 27 |
| 34 | 50854   | 86104   | 52349   | 85203   | 53828   | 84277   | 55291   | 83324   | 56736   | 82347   | 26 |
| 35 | 50879   | 86089   | 52374   | 85188   | 53853   | 84261   | 55315   | 83308   | 56760   | 82330   | 25 |
| 36 | 50904   | 86074   | 52399   | 85173   | 53877   | 84245   | 55339   | 83292   | 56784   | 82314   | 24 |
| 37 | 50929   | 86059   | 52423   | 85157   | 53902   | 84230   | 55363   | 83276   | 56808   | 82297   | 23 |
| 38 | 50954   | 86045   | 52448   | 85142   | 53926   | 84214   | 55388   | 83260   | 56832   | 82281   | 22 |
| 39 | 50979   | 86030   | 52473   | 85127   | 53951   | 84198   | 55412   | 83244   | 56856   | 82264   | 21 |
| 40 | 51004   | 86015   | 52498   | 85112   | 53975   | 84182   | 55436   | 83228   | 56880   | 82248   | 20 |
| 41 | 51029   | 86000   | 52522   | 85096   | 54000   | 84167   | 55460   | 83212   | 56904   | 82231   | 19 |
| 42 | 51054   | 85985   | 52547   | 85081   | 54024   | 84151   | 55484   | 83195   | 56928   | 82214   | 18 |
| 43 | 51079   | 85970   | 52572   | 85066   | 54049   | 84135   | 55509   | 83179   | 56952   | 82198   | 17 |
| 44 | 51104   | 85956   | 52597   | 85051   | 54073   | 84120   | 55533   | 83163   | 56976   | 82181   | 16 |
| 45 | 51129   | 85941   | 52621   | 85035   | 54097   | 84104   | 55557   | 83147   | 57000   | 82165   | 15 |
| 46 | 51154   | 85926   | 52646   | 85020   | 54122   | 84088   | 55581   | 83131   | 57024   | 82148   | 14 |
| 47 | 51179   | 85911   | 52671   | 85005   | 54146   | 84072   | 55605   | 83115   | 57047   | 82132   | 13 |
| 48 | 51204   | 85896   | 52696   | 84989   | 54171   | 84057   | 55630   | 83098   | 57071   | 82115   | 12 |
| 49 | 51229   | 85881   | 52720   | 84974   | 54195   | 84041   | 55654   | 83082   | 57095   | 82098   | 11 |
| 50 | 51254   | 85866   | 52745   | 84959   | 54220   | 84025   | 55678   | 83066   | 57119   | 82082   | 10 |
| 51 | 51279   | 85851   | 52770   | 84943   | 54244   | 84009   | 55702   | 83050   | 57143   | 82065   | 9  |
| 52 | 51304   | 85836   | 52794   | 84928   | 54269   | 83994   | 55726   | 83034   | 57167   | 82048   | 8  |
| 53 | 51329   | 85821   | 52819   | 84913   | 54293   | 83978   | 55750   | 83017   | 57191   | 82032   | 7  |
| 54 | 51354   | 85806   | 52844   | 84897   | 54317   | 83962   | 55775   | 83001   | 57215   | 82015   | 6  |
| 55 | 51379   | 85792   | 52869   | 84882   | 54342   | 83946   | 55799   | 82985   | 57238   | 81999   | 5  |
| 56 | 51404   | 85777   | 52893   | 84866   | 54366   | 83930   | 55823   | 82969   | 57262   | 81982   | 4  |
| 57 | 51429   | 85762   | 52918   | 84851   | 54391   | 83915   | 55847   | 82953   | 57286   | 81965   | 3  |
| 58 | 51454   | 85747   | 52943   | 84836   | 54415   | 83899   | 55871   | 82936   | 57310   | 81949   | 2  |
| 59 | 51479   | 85732   | 52967   | 84820   | 54440   | 83883   | 55895   | 82920   | 57334   | 81932   | 1  |
| 60 | 51504   | 85717   | 52992   | 84805   | 54464   | 83867   | 55919   | 82904   | 57358   | 81915   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 59°     |         | 58°     |         | 57°     |         | 56°     |         | 55°     |         |    |



TABLE III. NATURAL SINES AND COSINES.

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| °       | 85°   |         | 86°     |         | 87°     |         | 88°     |         | 89°     |         | °  |
|---------|-------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|         | Sine. | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0       | 57358 | 81915   | 58779   | 80902   | 60182   | 79864   | 61566   | 78801   | 62932   | 77715   | 50 |
| 1       | 57381 | 81899   | 58802   | 80885   | 60205   | 79846   | 61589   | 78783   | 62955   | 77696   | 59 |
| 2       | 57405 | 81882   | 58826   | 80867   | 60228   | 79829   | 61612   | 78765   | 62977   | 77678   | 58 |
| 3       | 57429 | 81865   | 58849   | 80850   | 60251   | 79811   | 61635   | 78747   | 63000   | 77660   | 57 |
| 4       | 57453 | 81848   | 58873   | 80833   | 60274   | 79793   | 61658   | 78729   | 63022   | 77641   | 56 |
| 5       | 57477 | 81832   | 58896   | 80816   | 60298   | 79776   | 61681   | 78711   | 63045   | 77623   | 55 |
| 6       | 57501 | 81815   | 58920   | 80799   | 60321   | 79758   | 61704   | 78694   | 63068   | 77605   | 54 |
| 7       | 57524 | 81798   | 58943   | 80782   | 60344   | 79741   | 61726   | 78676   | 63090   | 77586   | 53 |
| 8       | 57548 | 81782   | 58967   | 80765   | 60367   | 79723   | 61749   | 78658   | 63113   | 77568   | 52 |
| 9       | 57572 | 81765   | 58990   | 80748   | 60390   | 79706   | 61772   | 78640   | 63135   | 77550   | 51 |
| 10      | 57596 | 81748   | 59014   | 80730   | 60414   | 79688   | 61795   | 78622   | 63158   | 77531   | 50 |
| 11      | 57619 | 81731   | 59037   | 80713   | 60437   | 79671   | 61818   | 78604   | 63180   | 77513   | 49 |
| 12      | 57643 | 81714   | 59061   | 80696   | 60460   | 79653   | 61841   | 78586   | 63203   | 77494   | 48 |
| 13      | 57667 | 81698   | 59084   | 80679   | 60483   | 79635   | 61864   | 78568   | 63225   | 77476   | 47 |
| 14      | 57691 | 81681   | 59108   | 80662   | 60506   | 79618   | 61887   | 78550   | 63248   | 77458   | 46 |
| 15      | 57715 | 81664   | 59131   | 80644   | 60529   | 79600   | 61909   | 78532   | 63271   | 77439   | 45 |
| 16      | 57738 | 81647   | 59154   | 80627   | 60553   | 79583   | 61932   | 78514   | 63293   | 77421   | 44 |
| 17      | 57762 | 81631   | 59178   | 80610   | 60576   | 79565   | 61955   | 78496   | 63316   | 77402   | 43 |
| 18      | 57786 | 81614   | 59201   | 80593   | 60599   | 79547   | 61978   | 78478   | 63338   | 77384   | 42 |
| 19      | 57810 | 81597   | 59225   | 80576   | 60622   | 79530   | 62001   | 78460   | 63361   | 77366   | 41 |
| 20      | 57833 | 81580   | 59248   | 80558   | 60645   | 79512   | 62024   | 78442   | 63383   | 77347   | 40 |
| 21      | 57857 | 81563   | 59272   | 80541   | 60668   | 79494   | 62046   | 78424   | 63406   | 77329   | 39 |
| 22      | 57881 | 81546   | 59295   | 80524   | 60691   | 79477   | 62069   | 78405   | 63428   | 77310   | 38 |
| 23      | 57904 | 81530   | 59318   | 80507   | 60714   | 79459   | 62092   | 78387   | 63451   | 77292   | 37 |
| 24      | 57928 | 81513   | 59342   | 80490   | 60738   | 79441   | 62115   | 78369   | 63473   | 77273   | 36 |
| 25      | 57952 | 81496   | 59365   | 80472   | 60761   | 79424   | 62138   | 78351   | 63496   | 77255   | 35 |
| 26      | 57976 | 81479   | 59389   | 80455   | 60784   | 79406   | 62160   | 78333   | 63518   | 77236   | 34 |
| 27      | 57999 | 81462   | 59412   | 80438   | 60807   | 79388   | 62183   | 78315   | 63540   | 77218   | 33 |
| 28      | 58023 | 81445   | 59436   | 80420   | 60830   | 79371   | 62206   | 78297   | 63563   | 77199   | 32 |
| 29      | 58047 | 81428   | 59459   | 80403   | 60853   | 79353   | 62229   | 78279   | 63585   | 77181   | 31 |
| 30      | 58070 | 81412   | 59482   | 80386   | 60876   | 79335   | 62251   | 78261   | 63608   | 77162   | 30 |
| 31      | 58094 | 81395   | 59506   | 80368   | 60899   | 79318   | 62274   | 78243   | 63630   | 77144   | 29 |
| 32      | 58118 | 81378   | 59529   | 80351   | 60922   | 79300   | 62297   | 78225   | 63653   | 77125   | 28 |
| 33      | 58141 | 81361   | 59552   | 80334   | 60945   | 79282   | 62320   | 78206   | 63675   | 77107   | 27 |
| 34      | 58165 | 81344   | 59576   | 80316   | 60968   | 79264   | 62342   | 78188   | 63698   | 77088   | 26 |
| 35      | 58189 | 81327   | 59599   | 80299   | 60991   | 79247   | 62365   | 78170   | 63720   | 77070   | 25 |
| 36      | 58212 | 81310   | 59622   | 80282   | 61015   | 79229   | 62388   | 78152   | 63742   | 77051   | 24 |
| 37      | 58236 | 81293   | 59646   | 80264   | 61038   | 79211   | 62411   | 78134   | 63765   | 77033   | 23 |
| 38      | 58260 | 81276   | 59669   | 80247   | 61061   | 79193   | 62433   | 78116   | 63787   | 77014   | 22 |
| 39      | 58283 | 81259   | 59693   | 80230   | 61084   | 79176   | 62456   | 78098   | 63810   | 76996   | 21 |
| 40      | 58307 | 81242   | 59716   | 80212   | 61107   | 79158   | 62479   | 78079   | 63832   | 76977   | 20 |
| 41      | 58330 | 81225   | 59739   | 80195   | 61130   | 79140   | 62502   | 78061   | 63854   | 76959   | 19 |
| 42      | 58354 | 81208   | 59763   | 80178   | 61153   | 79122   | 62524   | 78043   | 63877   | 76940   | 18 |
| 43      | 58378 | 81191   | 59786   | 80160   | 61176   | 79105   | 62547   | 78025   | 63899   | 76921   | 17 |
| 44      | 58401 | 81174   | 59809   | 80143   | 61199   | 79087   | 62570   | 78007   | 63922   | 76903   | 16 |
| 45      | 58425 | 81157   | 59832   | 80125   | 61222   | 79069   | 62592   | 77988   | 63944   | 76884   | 15 |
| 46      | 58449 | 81140   | 59856   | 80108   | 61245   | 79051   | 62615   | 77970   | 63966   | 76866   | 14 |
| 47      | 58472 | 81123   | 59879   | 80091   | 61268   | 79033   | 62638   | 77952   | 63989   | 76847   | 13 |
| 48      | 58496 | 81106   | 59902   | 80073   | 61291   | 79016   | 62660   | 77934   | 64011   | 76828   | 12 |
| 49      | 58519 | 81089   | 59926   | 80056   | 61314   | 78998   | 62683   | 77916   | 64033   | 76810   | 11 |
| 50      | 58543 | 81072   | 59949   | 80038   | 61337   | 78980   | 62706   | 77897   | 64056   | 76791   | 10 |
| 51      | 58567 | 81055   | 59972   | 80021   | 61360   | 78962   | 62728   | 77879   | 64078   | 76772   | 9  |
| 52      | 58590 | 81038   | 59995   | 80003   | 61383   | 78944   | 62751   | 77861   | 64100   | 76754   | 8  |
| 53      | 58614 | 81021   | 60018   | 79986   | 61406   | 78926   | 62774   | 77843   | 64123   | 76735   | 7  |
| 54      | 58637 | 81004   | 60042   | 79968   | 61429   | 78908   | 62796   | 77824   | 64145   | 76717   | 6  |
| 55      | 58661 | 80987   | 60065   | 79951   | 61451   | 78891   | 62819   | 77806   | 64167   | 76698   | 5  |
| 56      | 58684 | 80970   | 60089   | 79934   | 61474   | 78873   | 62842   | 77788   | 64190   | 76679   | 4  |
| 57      | 58708 | 80953   | 60112   | 79916   | 61497   | 78855   | 62864   | 77769   | 64212   | 76661   | 3  |
| 58      | 58731 | 80936   | 60135   | 79899   | 61520   | 78837   | 62887   | 77751   | 64234   | 76642   | 2  |
| 59      | 58755 | 80919   | 60158   | 79881   | 61543   | 78819   | 62909   | 77733   | 64256   | 76623   | 1  |
| 60      | 58779 | 80902   | 60182   | 79864   | 61566   | 78801   | 62932   | 77715   | 64279   | 76604   | 0  |
| Cosine. |       | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
| 54°     |       | 53°     |         | 52°     |         | 51°     |         | 50°     |         |         |    |

| °  | 40°     |         | 41°     |         | 42°     |         | 43°     |         | 44°     |         | °  |
|----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----|
|    | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. |    |
| 0  | 64279   | 76604   | 65606   | 75471   | 66913   | 74314   | 68200   | 73135   | 69466   | 71934   | 60 |
| 1  | 64301   | 76586   | 65628   | 75452   | 66935   | 74295   | 68221   | 73116   | 69487   | 71914   | 59 |
| 2  | 64323   | 76567   | 65650   | 75433   | 66956   | 74276   | 68242   | 73096   | 69508   | 71894   | 58 |
| 3  | 64346   | 76548   | 65672   | 75414   | 66978   | 74256   | 68264   | 73075   | 69529   | 71873   | 57 |
| 4  | 64368   | 76530   | 65694   | 75395   | 66999   | 74237   | 68285   | 73056   | 69549   | 71853   | 56 |
| 5  | 64390   | 76511   | 65716   | 75375   | 67021   | 74217   | 68306   | 73036   | 69570   | 71833   | 55 |
| 6  | 64412   | 76492   | 65738   | 75356   | 67043   | 74198   | 68327   | 73016   | 69591   | 71813   | 54 |
| 7  | 64435   | 76473   | 65759   | 75337   | 67064   | 74178   | 68349   | 72996   | 69612   | 71792   | 53 |
| 8  | 64457   | 76455   | 65781   | 75318   | 67086   | 74159   | 68370   | 72976   | 69633   | 71772   | 52 |
| 9  | 64479   | 76436   | 65803   | 75299   | 67107   | 74139   | 68391   | 72957   | 69654   | 71752   | 51 |
| 10 | 64501   | 76417   | 65825   | 75280   | 67129   | 74120   | 68412   | 72937   | 69675   | 71732   | 50 |
| 11 | 64524   | 76398   | 65847   | 75261   | 67151   | 74100   | 68434   | 72917   | 69696   | 71711   | 49 |
| 12 | 64546   | 76380   | 65869   | 75241   | 67172   | 74080   | 68455   | 72897   | 69717   | 71691   | 48 |
| 13 | 64568   | 76361   | 65891   | 75222   | 67194   | 74061   | 68476   | 72877   | 69737   | 71671   | 47 |
| 14 | 64590   | 76342   | 65913   | 75203   | 67215   | 74041   | 68497   | 72857   | 69758   | 71650   | 46 |
| 15 | 64612   | 76323   | 65935   | 75184   | 67237   | 74022   | 68518   | 72837   | 69779   | 71630   | 45 |
| 16 | 64635   | 76304   | 65956   | 75165   | 67258   | 74002   | 68539   | 72817   | 69800   | 71610   | 44 |
| 17 | 64657   | 76286   | 65978   | 75146   | 67280   | 73983   | 68561   | 72797   | 69821   | 71590   | 43 |
| 18 | 64679   | 76267   | 66000   | 75126   | 67301   | 73963   | 68582   | 72777   | 69842   | 71569   | 42 |
| 19 | 64701   | 76248   | 66022   | 75107   | 67323   | 73944   | 68603   | 72757   | 69862   | 71549   | 41 |
| 20 | 64723   | 76229   | 66044   | 75088   | 67344   | 73924   | 68624   | 72737   | 69883   | 71529   | 40 |
| 21 | 64746   | 76210   | 66066   | 75069   | 67366   | 73904   | 68645   | 72717   | 69904   | 71508   | 39 |
| 22 | 64768   | 76192   | 66088   | 75050   | 67387   | 73885   | 68666   | 72697   | 69925   | 71488   | 38 |
| 23 | 64790   | 76173   | 66109   | 75030   | 67409   | 73865   | 68688   | 72677   | 69946   | 71468   | 37 |
| 24 | 64812   | 76154   | 66131   | 75011   | 67430   | 73846   | 68709   | 72657   | 69966   | 71447   | 36 |
| 25 | 64834   | 76135   | 66153   | 74992   | 67452   | 73826   | 68730   | 72637   | 69987   | 71427   | 35 |
| 26 | 64856   | 76116   | 66175   | 74973   | 67473   | 73806   | 68751   | 72617   | 70008   | 71407   | 34 |
| 27 | 64878   | 76097   | 66197   | 74953   | 67495   | 73787   | 68772   | 72597   | 70029   | 71386   | 33 |
| 28 | 64901   | 76078   | 66218   | 74934   | 67516   | 73767   | 68793   | 72577   | 70049   | 71366   | 32 |
| 29 | 64923   | 76059   | 66240   | 74915   | 67538   | 73747   | 68814   | 72557   | 70070   | 71345   | 31 |
| 30 | 64945   | 76041   | 66262   | 74896   | 67559   | 73728   | 68835   | 72537   | 70091   | 71325   | 30 |
| 31 | 64967   | 76022   | 66284   | 74876   | 67580   | 73708   | 68855   | 72517   | 70112   | 71305   | 29 |
| 32 | 64989   | 76003   | 66305   | 74857   | 67602   | 73688   | 68878   | 72497   | 70132   | 71284   | 28 |
| 33 | 65011   | 75984   | 66327   | 74838   | 67623   | 73669   | 68899   | 72477   | 70153   | 71264   | 27 |
| 34 | 65033   | 75965   | 66349   | 74818   | 67645   | 73649   | 68920   | 72457   | 70174   | 71243   | 26 |
| 35 | 65055   | 75946   | 66371   | 74799   | 67666   | 73629   | 68941   | 72437   | 70195   | 71223   | 25 |
| 36 | 65077   | 75927   | 66393   | 74780   | 67688   | 73610   | 68962   | 72417   | 70215   | 71203   | 24 |
| 37 | 65100   | 75908   | 66414   | 74760   | 67709   | 73590   | 68983   | 72397   | 70236   | 71182   | 23 |
| 38 | 65122   | 75889   | 66436   | 74741   | 67730   | 73570   | 69004   | 72377   | 70257   | 71162   | 22 |
| 39 | 65144   | 75870   | 66458   | 74722   | 67752   | 73551   | 69025   | 72357   | 70277   | 71141   | 21 |
| 40 | 65166   | 75851   | 66480   | 74703   | 67773   | 73531   | 69046   | 72337   | 70298   | 71121   | 20 |
| 41 | 65188   | 75832   | 66501   | 74683   | 67795   | 73511   | 69067   | 72317   | 70319   | 71100   | 19 |
| 42 | 65210   | 75813   | 66523   | 74664   | 67816   | 73491   | 69088   | 72297   | 70339   | 71080   | 18 |
| 43 | 65232   | 75794   | 66545   | 74644   | 67837   | 73472   | 69109   | 72277   | 70360   | 71059   | 17 |
| 44 | 65254   | 75775   | 66566   | 74625   | 67859   | 73452   | 69130   | 72257   | 70381   | 71039   | 16 |
| 45 | 65276   | 75756   | 66588   | 74606   | 67880   | 73432   | 69151   | 72236   | 70401   | 71019   | 15 |
| 46 | 65298   | 75738   | 66610   | 74586   | 67901   | 73413   | 69172   | 72216   | 70422   | 70998   | 14 |
| 47 | 65320   | 75719   | 66632   | 74567   | 67923   | 73393   | 69193   | 72196   | 70443   | 70978   | 13 |
| 48 | 65342   | 75700   | 66653   | 74548   | 67944   | 73373   | 69214   | 72176   | 70463   | 70957   | 12 |
| 49 | 65364   | 75680   | 66675   | 74528   | 67965   | 73353   | 69235   | 72156   | 70484   | 70937   | 11 |
| 50 | 65386   | 75661   | 66697   | 74509   | 67987   | 73333   | 69256   | 72136   | 70505   | 70916   | 10 |
| 51 | 65408   | 75642   | 66718   | 74489   | 68008   | 73314   | 69277   | 72116   | 70525   | 70896   | 9  |
| 52 | 65430   | 75623   | 66740   | 74470   | 68029   | 73294   | 69298   | 72095   | 70546   | 70875   | 8  |
| 53 | 65452   | 75604   | 66762   | 74451   | 68051   | 73274   | 69319   | 72075   | 70567   | 70855   | 7  |
| 54 | 65474   | 75585   | 66783   | 74431   | 68072   | 73254   | 69340   | 72055   | 70587   | 70834   | 6  |
| 55 | 65496   | 75566   | 66805   | 74412   | 68093   | 73234   | 69361   | 72035   | 70608   | 70813   | 5  |
| 56 | 65518   | 75547   | 66827   | 74392   | 68115   | 73215   | 69382   | 72015   | 70628   | 70793   | 4  |
| 57 | 65540   | 75528   | 66848   | 74373   | 68136   | 73195   | 69403   | 71995   | 70649   | 70772   | 3  |
| 58 | 65562   | 75509   | 66870   | 74353   | 68157   | 73175   | 69424   | 71974   | 70670   | 70752   | 2  |
| 59 | 65584   | 75490   | 66891   | 74334   | 68179   | 73155   | 69445   | 71954   | 70690   | 70731   | 1  |
| 60 | 65606   | 75471   | 66913   | 74314   | 68200   | 73135   | 69466   | 71934   | 70711   | 70711   | 0  |
|    | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   | Cosine. | Sine.   |    |
|    | 49°     |         | 48°     |         | 47°     |         | 46°     |         | 45°     |         |    |

TABLE III. NATURAL TANGENTS AND COTANGENTS.

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| °  | 0°       |          | 1°       |          | 2°       |          | 3°       |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 00000    | Infinit. | 01746    | 57.2900  | 03492    | 28.6363  | 05241    | 19.0811  | 60 |
| 1  | 00029    | 3437.75  | 01775    | 56.3506  | 03521    | 28.3994  | 05270    | 18.9755  | 59 |
| 2  | 00058    | 1718.87  | 01804    | 55.4415  | 03550    | 28.1664  | 05299    | 18.8711  | 58 |
| 3  | 00087    | 1145.92  | 01833    | 54.5613  | 03579    | 27.9372  | 05328    | 18.7678  | 57 |
| 4  | 00116    | 859.436  | 01862    | 53.7086  | 03609    | 27.7117  | 05357    | 18.6656  | 56 |
| 5  | 00145    | 687.549  | 01891    | 52.8821  | 03638    | 27.4899  | 05387    | 18.5645  | 55 |
| 6  | 00175    | 572.957  | 01920    | 52.0807  | 03667    | 27.2715  | 05416    | 18.4645  | 54 |
| 7  | 00204    | 491.106  | 01949    | 51.3032  | 03696    | 27.0566  | 05445    | 18.3655  | 53 |
| 8  | 00233    | 429.718  | 01978    | 50.5485  | 03725    | 26.8450  | 05474    | 18.2677  | 52 |
| 9  | 00262    | 381.971  | 02007    | 49.8157  | 03754    | 26.6367  | 05503    | 18.1708  | 51 |
| 10 | 00291    | 343.774  | 02036    | 49.1039  | 03783    | 26.4315  | 05533    | 18.0750  | 50 |
| 11 | 00320    | 312.521  | 02066    | 48.4121  | 03812    | 26.2296  | 05562    | 17.9802  | 49 |
| 12 | 00349    | 286.478  | 02095    | 47.7395  | 03842    | 26.0307  | 05591    | 17.8863  | 48 |
| 13 | 00378    | 264.441  | 02124    | 47.0853  | 03871    | 25.8348  | 05620    | 17.7934  | 47 |
| 14 | 00407    | 245.552  | 02153    | 46.4489  | 03900    | 25.6418  | 05649    | 17.7015  | 46 |
| 15 | 00436    | 229.182  | 02182    | 45.8294  | 03929    | 25.4517  | 05678    | 17.6106  | 45 |
| 16 | 00465    | 214.858  | 02211    | 45.2261  | 03958    | 25.2644  | 05708    | 17.5205  | 44 |
| 17 | 00495    | 202.219  | 02240    | 44.6386  | 03987    | 25.0798  | 05737    | 17.4314  | 43 |
| 18 | 00524    | 190.984  | 02269    | 44.0661  | 04016    | 24.8978  | 05766    | 17.3432  | 42 |
| 19 | 00553    | 180.932  | 02298    | 43.5081  | 04046    | 24.7185  | 05795    | 17.2558  | 41 |
| 20 | 00582    | 171.885  | 02328    | 42.9641  | 04075    | 24.5418  | 05824    | 17.1693  | 40 |
| 21 | 00611    | 163.700  | 02357    | 42.4335  | 04104    | 24.3675  | 05854    | 17.0837  | 39 |
| 22 | 00640    | 156.259  | 02386    | 41.9158  | 04133    | 24.1957  | 05883    | 16.9990  | 38 |
| 23 | 00669    | 149.465  | 02415    | 41.4106  | 04162    | 24.0263  | 05912    | 16.9150  | 37 |
| 24 | 00698    | 143.237  | 02444    | 40.9174  | 04191    | 23.8593  | 05941    | 16.8319  | 36 |
| 25 | 00727    | 137.507  | 02473    | 40.4358  | 04220    | 23.6945  | 05970    | 16.7490  | 35 |
| 26 | 00756    | 132.219  | 02502    | 39.9655  | 04250    | 23.5321  | 05999    | 16.6661  | 34 |
| 27 | 00785    | 127.321  | 02531    | 39.5059  | 04279    | 23.3718  | 06029    | 16.5874  | 33 |
| 28 | 00814    | 122.774  | 02560    | 39.0568  | 04308    | 23.2137  | 06058    | 16.5075  | 32 |
| 29 | 00844    | 118.540  | 02589    | 38.6177  | 04337    | 23.0577  | 06087    | 16.4283  | 31 |
| 30 | 00873    | 114.589  | 02619    | 38.1885  | 04366    | 22.9038  | 06116    | 16.3499  | 30 |
| 31 | 00902    | 110.892  | 02648    | 37.7686  | 04395    | 22.7519  | 06145    | 16.2722  | 29 |
| 32 | 00931    | 107.426  | 02677    | 37.3579  | 04424    | 22.6020  | 06175    | 16.1952  | 28 |
| 33 | 00960    | 104.171  | 02706    | 36.9560  | 04454    | 22.4541  | 06204    | 16.1190  | 27 |
| 34 | 00989    | 101.107  | 02735    | 36.5627  | 04483    | 22.3081  | 06233    | 16.0435  | 26 |
| 35 | 01018    | 98.2179  | 02764    | 36.1776  | 04512    | 22.1640  | 06262    | 15.9687  | 25 |
| 36 | 01047    | 95.4895  | 02793    | 35.8006  | 04541    | 22.0217  | 06291    | 15.8945  | 24 |
| 37 | 01076    | 92.9085  | 02822    | 35.4313  | 04570    | 21.8813  | 06321    | 15.8211  | 23 |
| 38 | 01105    | 90.4633  | 02851    | 35.0695  | 04599    | 21.7426  | 06350    | 15.7483  | 22 |
| 39 | 01135    | 88.1436  | 02881    | 34.7151  | 04628    | 21.6056  | 06379    | 15.6762  | 21 |
| 40 | 01164    | 85.9398  | 02910    | 34.3678  | 04658    | 21.4704  | 06408    | 15.6048  | 20 |
| 41 | 01193    | 83.8435  | 02939    | 34.0273  | 04687    | 21.3369  | 06437    | 15.5340  | 19 |
| 42 | 01222    | 81.8470  | 02968    | 33.6935  | 04716    | 21.2049  | 06467    | 15.4638  | 18 |
| 43 | 01251    | 79.9434  | 02997    | 33.3662  | 04745    | 21.0747  | 06496    | 15.3943  | 17 |
| 44 | 01280    | 78.1263  | 03026    | 33.0452  | 04774    | 20.9460  | 06525    | 15.3254  | 16 |
| 45 | 01309    | 76.3900  | 03055    | 32.7303  | 04803    | 20.8188  | 06554    | 15.2571  | 15 |
| 46 | 01338    | 74.7292  | 03084    | 32.4213  | 04832    | 20.6932  | 06584    | 15.1893  | 14 |
| 47 | 01367    | 73.1390  | 03114    | 32.1181  | 04862    | 20.5691  | 06613    | 15.1222  | 13 |
| 48 | 01396    | 71.6151  | 03143    | 31.8205  | 04891    | 20.4465  | 06642    | 15.0557  | 12 |
| 49 | 01425    | 70.1533  | 03172    | 31.5284  | 04920    | 20.3253  | 06671    | 14.9898  | 11 |
| 50 | 01455    | 68.7501  | 03201    | 31.2416  | 04949    | 20.2056  | 06700    | 14.9244  | 10 |
| 51 | 01484    | 67.4019  | 03230    | 30.9599  | 04978    | 20.0872  | 06730    | 14.8596  | 9  |
| 52 | 01513    | 66.1055  | 03259    | 30.6833  | 05007    | 19.9702  | 06759    | 14.7954  | 8  |
| 53 | 01542    | 64.8580  | 03288    | 30.4116  | 05037    | 19.8546  | 06788    | 14.7317  | 7  |
| 54 | 01571    | 63.6567  | 03317    | 30.1446  | 05066    | 19.7403  | 06817    | 14.6685  | 6  |
| 55 | 01600    | 62.4992  | 03346    | 29.8823  | 05095    | 19.6273  | 06847    | 14.6059  | 5  |
| 56 | 01629    | 61.3829  | 03376    | 29.6245  | 05124    | 19.5156  | 06876    | 14.5438  | 4  |
| 57 | 01658    | 60.3058  | 03405    | 29.3711  | 05153    | 19.4051  | 06905    | 14.4823  | 3  |
| 58 | 01687    | 59.2659  | 03434    | 29.1220  | 05182    | 19.2959  | 06934    | 14.4212  | 2  |
| 59 | 01716    | 58.2612  | 03463    | 28.8771  | 05212    | 19.1879  | 06963    | 14.3607  | 1  |
| 60 | 01746    | 57.2900  | 03492    | 28.6363  | 05241    | 19.0811  | 06993    | 14.3007  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 89°      |          | 88°      |          | 87°      |          | 86°      |          |    |

| °  | 4°       |          | 5°       |          | 6°       |          | 7°       |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 06993    | 14.3007  | 08749    | 11.4301  | 10510    | 9.51436  | 12278    | 8.14435  | 60 |
| 1  | 07022    | 14.2411  | 08778    | 11.3919  | 10540    | 9.48781  | 12308    | 8.12481  | 59 |
| 2  | 07051    | 14.1821  | 08807    | 11.3540  | 10569    | 9.46141  | 12338    | 8.10536  | 58 |
| 3  | 07080    | 14.1235  | 08837    | 11.3163  | 10599    | 9.43515  | 12367    | 8.08600  | 57 |
| 4  | 07110    | 14.0655  | 08866    | 11.2789  | 10628    | 9.40904  | 12397    | 8.06674  | 56 |
| 5  | 07139    | 14.0079  | 08895    | 11.2417  | 10657    | 9.38307  | 12426    | 8.04756  | 55 |
| 6  | 07168    | 13.9507  | 08925    | 11.2048  | 10687    | 9.35724  | 12456    | 8.02848  | 54 |
| 7  | 07197    | 13.8940  | 08954    | 11.1681  | 10716    | 9.33154  | 12485    | 8.00948  | 53 |
| 8  | 07227    | 13.8378  | 08983    | 11.1316  | 10746    | 9.30599  | 12515    | 7.99058  | 52 |
| 9  | 07256    | 13.7821  | 09013    | 11.0954  | 10775    | 9.28058  | 12544    | 7.97176  | 51 |
| 10 | 07285    | 13.7267  | 09042    | 11.0594  | 10805    | 9.25530  | 12574    | 7.95302  | 50 |
| 11 | 07314    | 13.6719  | 09071    | 11.0237  | 10834    | 9.23016  | 12603    | 7.93438  | 49 |
| 12 | 07344    | 13.6174  | 09101    | 10.9882  | 10863    | 9.20516  | 12633    | 7.91582  | 48 |
| 13 | 07373    | 13.5634  | 09130    | 10.9529  | 10893    | 9.18028  | 12662    | 7.89734  | 47 |
| 14 | 07402    | 13.5098  | 09159    | 10.9178  | 10922    | 9.15554  | 12692    | 7.87895  | 46 |
| 15 | 07431    | 13.4566  | 09189    | 10.8829  | 10952    | 9.13093  | 12722    | 7.86064  | 45 |
| 16 | 07461    | 13.4039  | 09218    | 10.8483  | 10981    | 9.10646  | 12751    | 7.84242  | 44 |
| 17 | 07490    | 13.3515  | 09247    | 10.8139  | 11011    | 9.08211  | 12781    | 7.82428  | 43 |
| 18 | 07519    | 13.2996  | 09277    | 10.7797  | 11040    | 9.05789  | 12810    | 7.80622  | 42 |
| 19 | 07548    | 13.2480  | 09306    | 10.7457  | 11070    | 9.03379  | 12840    | 7.78825  | 41 |
| 20 | 07578    | 13.1969  | 09335    | 10.7119  | 11099    | 9.00983  | 12869    | 7.77035  | 40 |
| 21 | 07607    | 13.1461  | 09365    | 10.6783  | 11128    | 8.98598  | 12899    | 7.75254  | 39 |
| 22 | 07636    | 13.0958  | 09394    | 10.6450  | 11158    | 8.96227  | 12929    | 7.73480  | 38 |
| 23 | 07665    | 13.0458  | 09423    | 10.6118  | 11187    | 8.93867  | 12958    | 7.71715  | 37 |
| 24 | 07695    | 12.9962  | 09453    | 10.5789  | 11217    | 8.91520  | 12988    | 7.69957  | 36 |
| 25 | 07724    | 12.9469  | 09482    | 10.5462  | 11246    | 8.89185  | 13017    | 7.68208  | 35 |
| 26 | 07753    | 12.8981  | 09511    | 10.5136  | 11276    | 8.86862  | 13047    | 7.66466  | 34 |
| 27 | 07782    | 12.8496  | 09541    | 10.4813  | 11305    | 8.84551  | 13076    | 7.64732  | 33 |
| 28 | 07812    | 12.8014  | 09570    | 10.4491  | 11335    | 8.82252  | 13106    | 7.63005  | 32 |
| 29 | 07841    | 12.7536  | 09600    | 10.4172  | 11364    | 8.79964  | 13136    | 7.61287  | 31 |
| 30 | 07870    | 12.7062  | 09629    | 10.3854  | 11394    | 8.77689  | 13165    | 7.59575  | 30 |
| 31 | 07899    | 12.6591  | 09658    | 10.3538  | 11423    | 8.75425  | 13195    | 7.57872  | 29 |
| 32 | 07929    | 12.6124  | 09688    | 10.3224  | 11452    | 8.73172  | 13224    | 7.56176  | 28 |
| 33 | 07958    | 12.5660  | 09717    | 10.2913  | 11482    | 8.70931  | 13254    | 7.54487  | 27 |
| 34 | 07987    | 12.5199  | 09746    | 10.2602  | 11511    | 8.68701  | 13284    | 7.52806  | 26 |
| 35 | 08017    | 12.4742  | 09776    | 10.2294  | 11541    | 8.66482  | 13313    | 7.51132  | 25 |
| 36 | 08046    | 12.4288  | 09805    | 10.1988  | 11570    | 8.64275  | 13343    | 7.49465  | 24 |
| 37 | 08075    | 12.3838  | 09834    | 10.1683  | 11600    | 8.62078  | 13372    | 7.47806  | 23 |
| 38 | 08104    | 12.3390  | 09864    | 10.1381  | 11629    | 8.59893  | 13402    | 7.46154  | 22 |
| 39 | 08134    | 12.2946  | 09893    | 10.1080  | 11659    | 8.57718  | 13432    | 7.44509  | 21 |
| 40 | 08163    | 12.2505  | 09923    | 10.0780  | 11688    | 8.55555  | 13461    | 7.42871  | 20 |
| 41 | 08192    | 12.2067  | 09952    | 10.0483  | 11718    | 8.53402  | 13491    | 7.41240  | 19 |
| 42 | 08221    | 12.1632  | 09981    | 10.0187  | 11747    | 8.51259  | 13521    | 7.39616  | 18 |
| 43 | 08251    | 12.1201  | 10011    | 9.98930  | 11777    | 8.49128  | 13550    | 7.37999  | 17 |
| 44 | 08280    | 12.0772  | 10040    | 9.96007  | 11806    | 8.47007  | 13580    | 7.36389  | 16 |
| 45 | 08309    | 12.0346  | 10069    | 9.93101  | 11836    | 8.44896  | 13609    | 7.34786  | 15 |
| 46 | 08339    | 11.9923  | 10099    | 9.90211  | 11865    | 8.42795  | 13639    | 7.33190  | 14 |
| 47 | 08368    | 11.9504  | 10128    | 9.87338  | 11895    | 8.40705  | 13669    | 7.31600  | 13 |
| 48 | 08397    | 11.9087  | 10158    | 9.84482  | 11924    | 8.38625  | 13698    | 7.30018  | 12 |
| 49 | 08427    | 11.8673  | 10187    | 9.81641  | 11954    | 8.36555  | 13728    | 7.28442  | 11 |
| 50 | 08456    | 11.8262  | 10216    | 9.78817  | 11983    | 8.34496  | 13758    | 7.26873  | 10 |
| 51 | 08485    | 11.7853  | 10246    | 9.76009  | 12013    | 8.32446  | 13787    | 7.25310  | 9  |
| 52 | 08514    | 11.7448  | 10275    | 9.73217  | 12042    | 8.30406  | 13817    | 7.23754  | 8  |
| 53 | 08544    | 11.7045  | 10305    | 9.70441  | 12072    | 8.28376  | 13846    | 7.22204  | 7  |
| 54 | 08573    | 11.6645  | 10334    | 9.67680  | 12101    | 8.26355  | 13876    | 7.20661  | 6  |
| 55 | 08602    | 11.6248  | 10363    | 9.64935  | 12131    | 8.24345  | 13906    | 7.19125  | 5  |
| 56 | 08632    | 11.5853  | 10393    | 9.62205  | 12160    | 8.22344  | 13935    | 7.17594  | 4  |
| 57 | 08661    | 11.5461  | 10422    | 9.59490  | 12190    | 8.20352  | 13965    | 7.16071  | 3  |
| 58 | 08690    | 11.5072  | 10452    | 9.56791  | 12219    | 8.18370  | 13995    | 7.14553  | 2  |
| 59 | 08720    | 11.4685  | 10481    | 9.54106  | 12249    | 8.16398  | 14024    | 7.13042  | 1  |
| 60 | 08749    | 11.4301  | 10510    | 9.51436  | 12278    | 8.14435  | 14054    | 7.11537  | 0  |
| °  | 85°      |          | 84°      |          | 83°      |          | 82°      |          | °  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |

TABLE III. NATURAL TANGENTS AND COTANGENTS. 75

|    | 8°       |          | 9°       |          | 10°      |          | 11°      |          |    |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 14054    | 7.11537  | 15838    | 6.31375  | 17633    | 5.67128  | 19438    | 5.14455  | 60 |
| 1  | 14084    | 7.10038  | 15868    | 6.30189  | 17663    | 5.66165  | 19468    | 5.13658  | 59 |
| 2  | 14113    | 7.08546  | 15898    | 6.29007  | 17693    | 5.65205  | 19498    | 5.12862  | 58 |
| 3  | 14143    | 7.07059  | 15928    | 6.27829  | 17723    | 5.64248  | 19529    | 5.12069  | 57 |
| 4  | 14173    | 7.05579  | 15958    | 6.26655  | 17753    | 5.63295  | 19559    | 5.11279  | 56 |
| 5  | 14202    | 7.04105  | 15988    | 6.25486  | 17783    | 5.62344  | 19589    | 5.10490  | 55 |
| 6  | 14232    | 7.02637  | 16017    | 6.24321  | 17813    | 5.61397  | 19619    | 5.09704  | 54 |
| 7  | 14262    | 7.01174  | 16047    | 6.23160  | 17843    | 5.60452  | 19649    | 5.08921  | 53 |
| 8  | 14291    | 6.99718  | 16077    | 6.22003  | 17873    | 5.59511  | 19680    | 5.08139  | 52 |
| 9  | 14321    | 6.98268  | 16107    | 6.20851  | 17903    | 5.58573  | 19710    | 5.07360  | 51 |
| 10 | 14351    | 6.96823  | 16137    | 6.19703  | 17933    | 5.57638  | 19740    | 5.06584  | 50 |
| 11 | 14381    | 6.95385  | 16167    | 6.18559  | 17963    | 5.56706  | 19770    | 5.05809  | 49 |
| 12 | 14410    | 6.93952  | 16196    | 6.17419  | 17993    | 5.55777  | 19801    | 5.05037  | 48 |
| 13 | 14440    | 6.92525  | 16226    | 6.16283  | 18023    | 5.54851  | 19831    | 5.04267  | 47 |
| 14 | 14470    | 6.91104  | 16256    | 6.15151  | 18053    | 5.53927  | 19861    | 5.03499  | 46 |
| 15 | 14499    | 6.89688  | 16286    | 6.14023  | 18083    | 5.53007  | 19891    | 5.02734  | 45 |
| 16 | 14529    | 6.88278  | 16316    | 6.12899  | 18113    | 5.52090  | 19921    | 5.01971  | 44 |
| 17 | 14559    | 6.86874  | 16346    | 6.11779  | 18143    | 5.51176  | 19952    | 5.01210  | 43 |
| 18 | 14588    | 6.85475  | 16376    | 6.10664  | 18173    | 5.50264  | 19982    | 5.00451  | 42 |
| 19 | 14618    | 6.84082  | 16405    | 6.09552  | 18203    | 5.49356  | 20012    | 4.99695  | 41 |
| 20 | 14648    | 6.82694  | 16435    | 6.08444  | 18233    | 5.48451  | 20042    | 4.98940  | 40 |
| 21 | 14678    | 6.81312  | 16465    | 6.07340  | 18263    | 5.47548  | 20073    | 4.98188  | 39 |
| 22 | 14707    | 6.79936  | 16495    | 6.06240  | 18293    | 5.46648  | 20103    | 4.97438  | 38 |
| 23 | 14737    | 6.78564  | 16525    | 6.05143  | 18323    | 5.45751  | 20133    | 4.96690  | 37 |
| 24 | 14767    | 6.77199  | 16555    | 6.04051  | 18353    | 5.44857  | 20164    | 4.95945  | 36 |
| 25 | 14796    | 6.75838  | 16585    | 6.02962  | 18383    | 5.43966  | 20194    | 4.95201  | 35 |
| 26 | 14826    | 6.74483  | 16615    | 6.01878  | 18414    | 5.43077  | 20224    | 4.94460  | 34 |
| 27 | 14856    | 6.73133  | 16645    | 6.00797  | 18444    | 5.42192  | 20254    | 4.93721  | 33 |
| 28 | 14886    | 6.71789  | 16674    | 5.99720  | 18474    | 5.41309  | 20285    | 4.92984  | 32 |
| 29 | 14915    | 6.70450  | 16704    | 5.98646  | 18504    | 5.40429  | 20315    | 4.92249  | 31 |
| 30 | 14945    | 6.69116  | 16734    | 5.97576  | 18534    | 5.39552  | 20345    | 4.91516  | 30 |
| 31 | 14975    | 6.67787  | 16764    | 5.96510  | 18564    | 5.38677  | 20376    | 4.90785  | 29 |
| 32 | 15005    | 6.66463  | 16794    | 5.95448  | 18594    | 5.37805  | 20406    | 4.90056  | 28 |
| 33 | 15034    | 6.65144  | 16824    | 5.94390  | 18624    | 5.36936  | 20436    | 4.89330  | 27 |
| 34 | 15064    | 6.63831  | 16854    | 5.93335  | 18654    | 5.36070  | 20466    | 4.88605  | 26 |
| 35 | 15094    | 6.62523  | 16884    | 5.92283  | 18684    | 5.35206  | 20497    | 4.87882  | 25 |
| 36 | 15124    | 6.61219  | 16914    | 5.91235  | 18714    | 5.34345  | 20527    | 4.87162  | 24 |
| 37 | 15153    | 6.59921  | 16944    | 5.90191  | 18745    | 5.33487  | 20557    | 4.86444  | 23 |
| 38 | 15183    | 6.58627  | 16974    | 5.89151  | 18775    | 5.32631  | 20588    | 4.85727  | 22 |
| 39 | 15213    | 6.57339  | 17004    | 5.88114  | 18805    | 5.31778  | 20618    | 4.85013  | 21 |
| 40 | 15243    | 6.56055  | 17033    | 5.87080  | 18835    | 5.30928  | 20648    | 4.84300  | 20 |
| 41 | 15272    | 6.54777  | 17063    | 5.86051  | 18865    | 5.30080  | 20679    | 4.83590  | 19 |
| 42 | 15302    | 6.53503  | 17093    | 5.85024  | 18895    | 5.29235  | 20709    | 4.82882  | 18 |
| 43 | 15332    | 6.52234  | 17123    | 5.84001  | 18925    | 5.28393  | 20739    | 4.82175  | 17 |
| 44 | 15362    | 6.50970  | 17153    | 5.82982  | 18955    | 5.27553  | 20770    | 4.81471  | 16 |
| 45 | 15391    | 6.49710  | 17183    | 5.81966  | 18986    | 5.26715  | 20800    | 4.80769  | 15 |
| 46 | 15421    | 6.48456  | 17213    | 5.80953  | 19016    | 5.25880  | 20830    | 4.80068  | 14 |
| 47 | 15451    | 6.47206  | 17243    | 5.79944  | 19046    | 5.25048  | 20861    | 4.79370  | 13 |
| 48 | 15481    | 6.45961  | 17273    | 5.78938  | 19076    | 5.24218  | 20891    | 4.78673  | 12 |
| 49 | 15511    | 6.44720  | 17303    | 5.77936  | 19106    | 5.23391  | 20921    | 4.77978  | 11 |
| 50 | 15540    | 6.43484  | 17333    | 5.76937  | 19136    | 5.22566  | 20952    | 4.77286  | 10 |
| 51 | 15570    | 6.42253  | 17363    | 5.75941  | 19166    | 5.21744  | 20982    | 4.76595  | 9  |
| 52 | 15600    | 6.41026  | 17393    | 5.74949  | 19197    | 5.20925  | 21013    | 4.75906  | 8  |
| 53 | 15630    | 6.39804  | 17423    | 5.73960  | 19227    | 5.20107  | 21043    | 4.75219  | 7  |
| 54 | 15660    | 6.38587  | 17453    | 5.72974  | 19257    | 5.19293  | 21073    | 4.74534  | 6  |
| 55 | 15689    | 6.37374  | 17483    | 5.71992  | 19287    | 5.18480  | 21104    | 4.73851  | 5  |
| 56 | 15719    | 6.36165  | 17513    | 5.71013  | 19317    | 5.17671  | 21134    | 4.73170  | 4  |
| 57 | 15749    | 6.34961  | 17543    | 5.70037  | 19347    | 5.16863  | 21164    | 4.72490  | 3  |
| 58 | 15779    | 6.33761  | 17573    | 5.69064  | 19378    | 5.16058  | 21195    | 4.71813  | 2  |
| 59 | 15809    | 6.32566  | 17603    | 5.68094  | 19408    | 5.15256  | 21225    | 4.71137  | 1  |
| 60 | 15838    | 6.31375  | 17633    | 5.67128  | 19438    | 5.14455  | 21256    | 4.70463  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 81°      |          | 80°      |          | 79°      |          | 78°      |          |    |

| °  | 4°       |          | 5°       |          | 6°       |          | 7°       |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 06993    | 14.3007  | 08749    | 11.4301  | 10510    | 9.51436  | 12278    | 8.14435  | 60 |
| 1  | 07022    | 14.2411  | 08778    | 11.3919  | 10540    | 9.48781  | 12308    | 8.12481  | 59 |
| 2  | 07051    | 14.1821  | 08807    | 11.3540  | 10569    | 9.46141  | 12338    | 8.10536  | 58 |
| 3  | 07080    | 14.1235  | 08837    | 11.3163  | 10599    | 9.43515  | 12367    | 8.08600  | 57 |
| 4  | 07110    | 14.0655  | 08866    | 11.2789  | 10628    | 9.40904  | 12397    | 8.06674  | 56 |
| 5  | 07139    | 14.0079  | 08895    | 11.2417  | 10657    | 9.38307  | 12426    | 8.04756  | 55 |
| 6  | 07168    | 13.9507  | 08925    | 11.2048  | 10687    | 9.35724  | 12456    | 8.02848  | 54 |
| 7  | 07197    | 13.8940  | 08954    | 11.1681  | 10716    | 9.33154  | 12485    | 8.00948  | 53 |
| 8  | 07227    | 13.8378  | 08983    | 11.1316  | 10746    | 9.30599  | 12515    | 7.99058  | 52 |
| 9  | 07256    | 13.7821  | 09013    | 11.0954  | 10775    | 9.28058  | 12544    | 7.97176  | 51 |
| 10 | 07285    | 13.7267  | 09042    | 11.0594  | 10805    | 9.25530  | 12574    | 7.95302  | 50 |
| 11 | 07314    | 13.6719  | 09071    | 11.0237  | 10834    | 9.23016  | 12603    | 7.93438  | 49 |
| 12 | 07344    | 13.6174  | 09101    | 10.9882  | 10863    | 9.20516  | 12633    | 7.91582  | 48 |
| 13 | 07373    | 13.5634  | 09130    | 10.9529  | 10893    | 9.18028  | 12662    | 7.89734  | 47 |
| 14 | 07402    | 13.5098  | 09159    | 10.9178  | 10922    | 9.15554  | 12692    | 7.87895  | 46 |
| 15 | 07431    | 13.4566  | 09189    | 10.8829  | 10952    | 9.13093  | 12722    | 7.86064  | 45 |
| 16 | 07461    | 13.4039  | 09218    | 10.8483  | 10981    | 9.10646  | 12751    | 7.84242  | 44 |
| 17 | 07490    | 13.3515  | 09247    | 10.8139  | 11011    | 9.08211  | 12781    | 7.82428  | 43 |
| 18 | 07519    | 13.2996  | 09277    | 10.7797  | 11040    | 9.05789  | 12810    | 7.80622  | 42 |
| 19 | 07548    | 13.2480  | 09306    | 10.7457  | 11070    | 9.03379  | 12840    | 7.78825  | 41 |
| 20 | 07578    | 13.1969  | 09335    | 10.7119  | 11099    | 9.00983  | 12869    | 7.77035  | 40 |
| 21 | 07607    | 13.1461  | 09365    | 10.6783  | 11128    | 8.98598  | 12899    | 7.75254  | 39 |
| 22 | 07636    | 13.0958  | 09394    | 10.6450  | 11158    | 8.96227  | 12929    | 7.73480  | 38 |
| 23 | 07665    | 13.0458  | 09423    | 10.6118  | 11187    | 8.93867  | 12958    | 7.71715  | 37 |
| 24 | 07695    | 12.9962  | 09453    | 10.5789  | 11217    | 8.91520  | 12988    | 7.69957  | 36 |
| 25 | 07724    | 12.9469  | 09482    | 10.5462  | 11246    | 8.89185  | 13017    | 7.68208  | 35 |
| 26 | 07753    | 12.8981  | 09511    | 10.5136  | 11276    | 8.86862  | 13047    | 7.66466  | 34 |
| 27 | 07782    | 12.8496  | 09541    | 10.4813  | 11305    | 8.84551  | 13076    | 7.64732  | 33 |
| 28 | 07812    | 12.8014  | 09570    | 10.4491  | 11335    | 8.82252  | 13106    | 7.63005  | 32 |
| 29 | 07841    | 12.7536  | 09600    | 10.4172  | 11364    | 8.79964  | 13136    | 7.61287  | 31 |
| 30 | 07870    | 12.7062  | 09629    | 10.3854  | 11394    | 8.77689  | 13165    | 7.59575  | 30 |
| 31 | 07899    | 12.6591  | 09658    | 10.3538  | 11423    | 8.75425  | 13195    | 7.57872  | 29 |
| 32 | 07929    | 12.6124  | 09688    | 10.3224  | 11452    | 8.73172  | 13224    | 7.56176  | 28 |
| 33 | 07958    | 12.5660  | 09717    | 10.2913  | 11482    | 8.70931  | 13254    | 7.54487  | 27 |
| 34 | 07987    | 12.5199  | 09746    | 10.2602  | 11511    | 8.68701  | 13284    | 7.52806  | 26 |
| 35 | 08017    | 12.4742  | 09776    | 10.2294  | 11541    | 8.66482  | 13313    | 7.51132  | 25 |
| 36 | 08046    | 12.4288  | 09805    | 10.1988  | 11570    | 8.64275  | 13343    | 7.49465  | 24 |
| 37 | 08075    | 12.3838  | 09834    | 10.1683  | 11600    | 8.62078  | 13372    | 7.47806  | 23 |
| 38 | 08104    | 12.3390  | 09864    | 10.1381  | 11629    | 8.59893  | 13402    | 7.46154  | 22 |
| 39 | 08134    | 12.2946  | 09893    | 10.1080  | 11659    | 8.57718  | 13432    | 7.44509  | 21 |
| 40 | 08163    | 12.2505  | 09923    | 10.0780  | 11688    | 8.55555  | 13461    | 7.42871  | 20 |
| 41 | 08192    | 12.2067  | 09952    | 10.0483  | 11718    | 8.53402  | 13491    | 7.41240  | 19 |
| 42 | 08221    | 12.1632  | 09981    | 10.0187  | 11747    | 8.51259  | 13521    | 7.39616  | 18 |
| 43 | 08251    | 12.1201  | 10011    | 9.98930  | 11777    | 8.49128  | 13550    | 7.37999  | 17 |
| 44 | 08280    | 12.0772  | 10040    | 9.96007  | 11806    | 8.47007  | 13580    | 7.36389  | 16 |
| 45 | 08309    | 12.0346  | 10069    | 9.93101  | 11836    | 8.44896  | 13609    | 7.34786  | 15 |
| 46 | 08339    | 11.9923  | 10099    | 9.90211  | 11865    | 8.42795  | 13639    | 7.33190  | 14 |
| 47 | 08368    | 11.9504  | 10128    | 9.87338  | 11895    | 8.40705  | 13669    | 7.31600  | 13 |
| 48 | 08397    | 11.9087  | 10158    | 9.84482  | 11924    | 8.38625  | 13698    | 7.30018  | 12 |
| 49 | 08427    | 11.8673  | 10187    | 9.81641  | 11954    | 8.36555  | 13728    | 7.28442  | 11 |
| 50 | 08456    | 11.8262  | 10216    | 9.78817  | 11983    | 8.34496  | 13758    | 7.26873  | 10 |
| 51 | 08485    | 11.7853  | 10246    | 9.76009  | 12013    | 8.32446  | 13787    | 7.25310  | 9  |
| 52 | 08514    | 11.7448  | 10275    | 9.73217  | 12042    | 8.30406  | 13817    | 7.23754  | 8  |
| 53 | 08544    | 11.7045  | 10305    | 9.70441  | 12072    | 8.28376  | 13846    | 7.22204  | 7  |
| 54 | 08573    | 11.6645  | 10334    | 9.67680  | 12101    | 8.26355  | 13876    | 7.20661  | 6  |
| 55 | 08602    | 11.6248  | 10363    | 9.64935  | 12131    | 8.24345  | 13906    | 7.19125  | 5  |
| 56 | 08632    | 11.5853  | 10393    | 9.62205  | 12160    | 8.22344  | 13935    | 7.17594  | 4  |
| 57 | 08661    | 11.5461  | 10422    | 9.59490  | 12190    | 8.20352  | 13965    | 7.16071  | 3  |
| 58 | 08690    | 11.5072  | 10452    | 9.56791  | 12219    | 8.18370  | 13995    | 7.14553  | 2  |
| 59 | 08720    | 11.4685  | 10481    | 9.54106  | 12249    | 8.16398  | 14024    | 7.13042  | 1  |
| 60 | 08749    | 11.4301  | 10510    | 9.51436  | 12278    | 8.14435  | 14054    | 7.11537  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 85°      |          | 84°      |          | 83°      |          | 82°      |          |    |

TABLE III

## NATURAL TANGENTS AND COTANGENTS.

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| °  | 8°       |          | 9°       |          | 10°      |          | 11°      |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 14054    | 7.11537  | 15838    | 6.31375  | 17633    | 5.67128  | 19438    | 5.14455  | 60 |
| 1  | 14084    | 7.10038  | 15868    | 6.30189  | 17663    | 5.66165  | 19468    | 5.13658  | 59 |
| 2  | 14113    | 7.08546  | 15898    | 6.29007  | 17693    | 5.65205  | 19498    | 5.12862  | 58 |
| 3  | 14143    | 7.07059  | 15928    | 6.27829  | 17723    | 5.64248  | 19529    | 5.12069  | 57 |
| 4  | 14173    | 7.05579  | 15958    | 6.26655  | 17753    | 5.63295  | 19559    | 5.11279  | 56 |
| 5  | 14202    | 7.04105  | 15988    | 6.25486  | 17783    | 5.62344  | 19589    | 5.10490  | 55 |
| 6  | 14232    | 7.02637  | 16017    | 6.24321  | 17813    | 5.61397  | 19619    | 5.09704  | 54 |
| 7  | 14262    | 7.01174  | 16047    | 6.23160  | 17843    | 5.60452  | 19649    | 5.08921  | 53 |
| 8  | 14291    | 6.99718  | 16077    | 6.22003  | 17873    | 5.59511  | 19680    | 5.08139  | 52 |
| 9  | 14321    | 6.98268  | 16107    | 6.20851  | 17903    | 5.58573  | 19710    | 5.07360  | 51 |
| 10 | 14351    | 6.96823  | 16137    | 6.19703  | 17933    | 5.57638  | 19740    | 5.06584  | 50 |
| 11 | 14381    | 6.95385  | 16167    | 6.18559  | 17963    | 5.56706  | 19770    | 5.05809  | 49 |
| 12 | 14410    | 6.93952  | 16196    | 6.17419  | 17993    | 5.55777  | 19801    | 5.05037  | 48 |
| 13 | 14440    | 6.92525  | 16226    | 6.16283  | 18023    | 5.54851  | 19831    | 5.04267  | 47 |
| 14 | 14470    | 6.91104  | 16256    | 6.15151  | 18053    | 5.53927  | 19861    | 5.03499  | 46 |
| 15 | 14499    | 6.89688  | 16286    | 6.14023  | 18083    | 5.53007  | 19891    | 5.02734  | 45 |
| 16 | 14529    | 6.88278  | 16316    | 6.12899  | 18113    | 5.52090  | 19921    | 5.01971  | 44 |
| 17 | 14559    | 6.86874  | 16346    | 6.11779  | 18143    | 5.51176  | 19952    | 5.01210  | 43 |
| 18 | 14588    | 6.85475  | 16376    | 6.10664  | 18173    | 5.50264  | 19982    | 5.00451  | 42 |
| 19 | 14618    | 6.84082  | 16405    | 6.09552  | 18203    | 5.49356  | 20012    | 4.99695  | 41 |
| 20 | 14648    | 6.82694  | 16435    | 6.08444  | 18233    | 5.48451  | 20042    | 4.98940  | 40 |
| 21 | 14678    | 6.81312  | 16465    | 6.07340  | 18263    | 5.47548  | 20073    | 4.98188  | 39 |
| 22 | 14707    | 6.79936  | 16495    | 6.06240  | 18293    | 5.46648  | 20103    | 4.97438  | 38 |
| 23 | 14737    | 6.78564  | 16525    | 6.05143  | 18323    | 5.45751  | 20133    | 4.96690  | 37 |
| 24 | 14767    | 6.77199  | 16555    | 6.04051  | 18353    | 5.44857  | 20164    | 4.95945  | 36 |
| 25 | 14796    | 6.75838  | 16585    | 6.02962  | 18383    | 5.43966  | 20194    | 4.95201  | 35 |
| 26 | 14826    | 6.74483  | 16615    | 6.01878  | 18414    | 5.43077  | 20224    | 4.94460  | 34 |
| 27 | 14856    | 6.73133  | 16645    | 6.00797  | 18444    | 5.42192  | 20254    | 4.93721  | 33 |
| 28 | 14886    | 6.71789  | 16674    | 5.99720  | 18474    | 5.41309  | 20285    | 4.92984  | 32 |
| 29 | 14915    | 6.70450  | 16704    | 5.98646  | 18504    | 5.40429  | 20315    | 4.92249  | 31 |
| 30 | 14945    | 6.69116  | 16734    | 5.97576  | 18534    | 5.39552  | 20345    | 4.91516  | 30 |
| 31 | 14975    | 6.67787  | 16764    | 5.96510  | 18564    | 5.38677  | 20376    | 4.90785  | 29 |
| 32 | 15005    | 6.66463  | 16794    | 5.95448  | 18594    | 5.37805  | 20406    | 4.90056  | 28 |
| 33 | 15034    | 6.65144  | 16824    | 5.94390  | 18624    | 5.36936  | 20436    | 4.89330  | 27 |
| 34 | 15064    | 6.63831  | 16854    | 5.93335  | 18654    | 5.36070  | 20466    | 4.88605  | 26 |
| 35 | 15094    | 6.62523  | 16884    | 5.92283  | 18684    | 5.35206  | 20497    | 4.87882  | 25 |
| 36 | 15124    | 6.61219  | 16914    | 5.91235  | 18714    | 5.34345  | 20527    | 4.87162  | 24 |
| 37 | 15153    | 6.59921  | 16944    | 5.90191  | 18745    | 5.33487  | 20557    | 4.86444  | 23 |
| 38 | 15183    | 6.58627  | 16974    | 5.89151  | 18775    | 5.32631  | 20588    | 4.85727  | 22 |
| 39 | 15213    | 6.57339  | 17004    | 5.88114  | 18805    | 5.31778  | 20618    | 4.85013  | 21 |
| 40 | 15243    | 6.56055  | 17033    | 5.87080  | 18835    | 5.30928  | 20648    | 4.84300  | 20 |
| 41 | 15272    | 6.54777  | 17063    | 5.86051  | 18865    | 5.30080  | 20679    | 4.83590  | 19 |
| 42 | 15302    | 6.53503  | 17093    | 5.85024  | 18895    | 5.29235  | 20709    | 4.82882  | 18 |
| 43 | 15332    | 6.52234  | 17123    | 5.84001  | 18925    | 5.28393  | 20739    | 4.82175  | 17 |
| 44 | 15362    | 6.50970  | 17153    | 5.82982  | 18955    | 5.27553  | 20770    | 4.81471  | 16 |
| 45 | 15391    | 6.49710  | 17183    | 5.81966  | 18986    | 5.26715  | 20800    | 4.80769  | 15 |
| 46 | 15421    | 6.48456  | 17213    | 5.80953  | 19016    | 5.25880  | 20830    | 4.80068  | 14 |
| 47 | 15451    | 6.47206  | 17243    | 5.79944  | 19046    | 5.25048  | 20861    | 4.79370  | 13 |
| 48 | 15481    | 6.45961  | 17273    | 5.78938  | 19076    | 5.24218  | 20891    | 4.78673  | 12 |
| 49 | 15511    | 6.44720  | 17303    | 5.77936  | 19106    | 5.23391  | 20921    | 4.77978  | 11 |
| 50 | 15540    | 6.43484  | 17333    | 5.76937  | 19136    | 5.22566  | 20952    | 4.77286  | 10 |
| 51 | 15570    | 6.42253  | 17363    | 5.75941  | 19166    | 5.21744  | 20982    | 4.76595  | 9  |
| 52 | 15600    | 6.41026  | 17393    | 5.74949  | 19197    | 5.20925  | 21013    | 4.75906  | 8  |
| 53 | 15630    | 6.39804  | 17423    | 5.73960  | 19227    | 5.20107  | 21043    | 4.75219  | 7  |
| 54 | 15660    | 6.38587  | 17453    | 5.72974  | 19257    | 5.19293  | 21073    | 4.74534  | 6  |
| 55 | 15689    | 6.37374  | 17483    | 5.71992  | 19287    | 5.18480  | 21104    | 4.73851  | 5  |
| 56 | 15719    | 6.36165  | 17513    | 5.71013  | 19317    | 5.17671  | 21134    | 4.73170  | 4  |
| 57 | 15749    | 6.34961  | 17543    | 5.70037  | 19347    | 5.16863  | 21164    | 4.72490  | 3  |
| 58 | 15779    | 6.33761  | 17573    | 5.69064  | 19378    | 5.16058  | 21195    | 4.71813  | 2  |
| 59 | 15809    | 6.32566  | 17603    | 5.68094  | 19408    | 5.15256  | 21225    | 4.71137  | 1  |
| 60 | 15838    | 6.31375  | 17633    | 5.67128  | 19438    | 5.14455  | 21256    | 4.70463  | 0  |
| °  | 81°      |          | 80°      |          | 79°      |          | 78°      |          | °  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |

| °  | 12°      |          | 13°      |          | 14°      |          | 15°      |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 21256    | 4.70463  | 23087    | 4.33148  | 24933    | 4.01078  | 26795    | 3.73205  | 60 |
| 1  | 21286    | 4.69791  | 23117    | 4.32573  | 24964    | 4.00582  | 26826    | 3.72771  | 59 |
| 2  | 21316    | 4.69121  | 23148    | 4.32001  | 24995    | 4.00086  | 26857    | 3.72338  | 58 |
| 3  | 21347    | 4.68452  | 23179    | 4.31430  | 25026    | 3.99592  | 26888    | 3.71907  | 57 |
| 4  | 21377    | 4.67786  | 23209    | 4.30860  | 25056    | 3.99099  | 26920    | 3.71476  | 56 |
| 5  | 21408    | 4.67121  | 23240    | 4.30291  | 25087    | 3.98607  | 26951    | 3.71046  | 55 |
| 6  | 21438    | 4.66458  | 23271    | 4.29724  | 25118    | 3.98117  | 26982    | 3.70616  | 54 |
| 7  | 21469    | 4.65797  | 23301    | 4.29159  | 25149    | 3.97627  | 27013    | 3.70188  | 53 |
| 8  | 21499    | 4.65138  | 23332    | 4.28595  | 25180    | 3.97139  | 27044    | 3.69761  | 52 |
| 9  | 21529    | 4.64480  | 23363    | 4.28032  | 25211    | 3.96651  | 27076    | 3.69335  | 51 |
| 10 | 21560    | 4.63825  | 23393    | 4.27471  | 25242    | 3.96165  | 27107    | 3.68909  | 50 |
| 11 | 21590    | 4.63171  | 23424    | 4.26911  | 25273    | 3.95680  | 27138    | 3.68485  | 49 |
| 12 | 21621    | 4.62518  | 23455    | 4.26352  | 25304    | 3.95196  | 27169    | 3.68061  | 48 |
| 13 | 21651    | 4.61868  | 23485    | 4.25795  | 25335    | 3.94713  | 27201    | 3.67638  | 47 |
| 14 | 21682    | 4.61219  | 23516    | 4.25239  | 25366    | 3.94232  | 27232    | 3.67217  | 46 |
| 15 | 21712    | 4.60572  | 23547    | 4.24685  | 25397    | 3.93751  | 27263    | 3.66796  | 45 |
| 16 | 21743    | 4.59927  | 23578    | 4.24132  | 25428    | 3.93271  | 27294    | 3.66376  | 44 |
| 17 | 21773    | 4.59283  | 23608    | 4.23580  | 25459    | 3.92793  | 27326    | 3.65957  | 43 |
| 18 | 21804    | 4.58641  | 23639    | 4.23030  | 25490    | 3.92316  | 27357    | 3.65538  | 42 |
| 19 | 21834    | 4.58001  | 23670    | 4.22481  | 25521    | 3.91839  | 27388    | 3.65121  | 41 |
| 20 | 21864    | 4.57363  | 23700    | 4.21933  | 25552    | 3.91364  | 27419    | 3.64705  | 40 |
| 21 | 21895    | 4.56726  | 23731    | 4.21387  | 25583    | 3.90890  | 27451    | 3.64289  | 39 |
| 22 | 21925    | 4.56091  | 23762    | 4.20842  | 25614    | 3.90417  | 27482    | 3.63874  | 38 |
| 23 | 21956    | 4.55458  | 23793    | 4.20298  | 25645    | 3.89945  | 27513    | 3.63461  | 37 |
| 24 | 21986    | 4.54826  | 23823    | 4.19756  | 25676    | 3.89474  | 27545    | 3.63048  | 36 |
| 25 | 22017    | 4.54196  | 23854    | 4.19215  | 25707    | 3.89004  | 27576    | 3.62636  | 35 |
| 26 | 22047    | 4.53568  | 23885    | 4.18675  | 25738    | 3.88536  | 27607    | 3.62224  | 34 |
| 27 | 22078    | 4.52941  | 23916    | 4.18137  | 25769    | 3.88068  | 27638    | 3.61814  | 33 |
| 28 | 22108    | 4.52316  | 23946    | 4.17600  | 25800    | 3.87601  | 27670    | 3.61405  | 32 |
| 29 | 22139    | 4.51693  | 23977    | 4.17064  | 25831    | 3.87136  | 27701    | 3.60996  | 31 |
| 30 | 22169    | 4.51071  | 24008    | 4.16530  | 25862    | 3.86671  | 27732    | 3.60588  | 30 |
| 31 | 22200    | 4.50451  | 24039    | 4.15997  | 25893    | 3.86208  | 27764    | 3.60181  | 29 |
| 32 | 22231    | 4.49832  | 24069    | 4.15465  | 25924    | 3.85745  | 27795    | 3.59775  | 28 |
| 33 | 22261    | 4.49215  | 24100    | 4.14934  | 25955    | 3.85284  | 27826    | 3.59370  | 27 |
| 34 | 22292    | 4.48600  | 24131    | 4.14405  | 25986    | 3.84824  | 27858    | 3.58966  | 26 |
| 35 | 22322    | 4.47986  | 24162    | 4.13877  | 26017    | 3.84364  | 27889    | 3.58562  | 25 |
| 36 | 22353    | 4.47374  | 24193    | 4.13350  | 26048    | 3.83906  | 27920    | 3.58160  | 24 |
| 37 | 22383    | 4.46764  | 24223    | 4.12825  | 26079    | 3.83449  | 27952    | 3.57758  | 23 |
| 38 | 22414    | 4.46155  | 24254    | 4.12301  | 26110    | 3.82992  | 27983    | 3.57357  | 22 |
| 39 | 22444    | 4.45548  | 24285    | 4.11778  | 26141    | 3.82537  | 28015    | 3.56957  | 21 |
| 40 | 22475    | 4.44942  | 24316    | 4.11256  | 26172    | 3.82083  | 28046    | 3.56557  | 20 |
| 41 | 22505    | 4.44338  | 24347    | 4.10736  | 26203    | 3.81630  | 28077    | 3.56159  | 19 |
| 42 | 22536    | 4.43735  | 24377    | 4.10216  | 26235    | 3.81177  | 28109    | 3.55761  | 18 |
| 43 | 22567    | 4.43134  | 24408    | 4.09699  | 26266    | 3.80726  | 28140    | 3.55364  | 17 |
| 44 | 22597    | 4.42534  | 24439    | 4.09182  | 26297    | 3.80276  | 28172    | 3.54968  | 16 |
| 45 | 22628    | 4.41936  | 24470    | 4.08666  | 26328    | 3.79827  | 28203    | 3.54573  | 15 |
| 46 | 22658    | 4.41340  | 24501    | 4.08152  | 26359    | 3.79378  | 28234    | 3.54179  | 14 |
| 47 | 22689    | 4.40745  | 24532    | 4.07639  | 26390    | 3.78931  | 28266    | 3.53785  | 13 |
| 48 | 22719    | 4.40152  | 24562    | 4.07127  | 26421    | 3.78485  | 28297    | 3.53393  | 12 |
| 49 | 22750    | 4.39560  | 24593    | 4.06616  | 26452    | 3.78040  | 28329    | 3.53001  | 11 |
| 50 | 22781    | 4.38969  | 24624    | 4.06107  | 26483    | 3.77595  | 28360    | 3.52609  | 10 |
| 51 | 22811    | 4.38381  | 24655    | 4.05599  | 26515    | 3.77152  | 28391    | 3.52219  | 9  |
| 52 | 22842    | 4.37793  | 24686    | 4.05092  | 26546    | 3.76709  | 28423    | 3.51829  | 8  |
| 53 | 22872    | 4.37207  | 24717    | 4.04586  | 26577    | 3.76268  | 28454    | 3.51441  | 7  |
| 54 | 22903    | 4.36623  | 24747    | 4.04081  | 26608    | 3.75828  | 28486    | 3.51053  | 6  |
| 55 | 22934    | 4.36040  | 24778    | 4.03578  | 26639    | 3.75388  | 28517    | 3.50666  | 5  |
| 56 | 22964    | 4.35459  | 24809    | 4.03075  | 26670    | 3.74950  | 28549    | 3.50279  | 4  |
| 57 | 22995    | 4.34879  | 24840    | 4.02574  | 26701    | 3.74512  | 28580    | 3.49894  | 3  |
| 58 | 23026    | 4.34300  | 24871    | 4.02074  | 26733    | 3.74075  | 28612    | 3.49509  | 2  |
| 59 | 23056    | 4.33723  | 24902    | 4.01576  | 26764    | 3.73640  | 28643    | 3.49125  | 1  |
| 60 | 23087    | 4.33148  | 24933    | 4.01078  | 26795    | 3.73205  | 28675    | 3.48741  | 0  |
| °  | 77°      |          | 76°      |          | 75°      |          | 74°      |          | °  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |



TABLE III. NATURAL TANGENTS AND COTANGENTS. 77

|    | 16°      |          | 17°      |          | 18°      |          | 19°      |          |    |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 28675    | 3.48741  | 30573    | 3.27085  | 32492    | 3.07768  | 34433    | 2.90421  | 60 |
| 1  | 28706    | 3.48359  | 30605    | 3.26745  | 32524    | 3.07464  | 34465    | 2.90147  | 59 |
| 2  | 28738    | 3.47977  | 30637    | 3.26406  | 32556    | 3.07160  | 34498    | 2.89873  | 58 |
| 3  | 28769    | 3.47596  | 30669    | 3.26067  | 32588    | 3.06857  | 34530    | 2.89600  | 57 |
| 4  | 28800    | 3.47216  | 30700    | 3.25729  | 32621    | 3.06554  | 34563    | 2.89327  | 56 |
| 5  | 28832    | 3.46837  | 30732    | 3.25392  | 32653    | 3.06252  | 34596    | 2.89055  | 55 |
| 6  | 28864    | 3.46458  | 30764    | 3.25055  | 32685    | 3.05950  | 34628    | 2.88783  | 54 |
| 7  | 28895    | 3.46080  | 30796    | 3.24719  | 32717    | 3.05649  | 34661    | 2.88511  | 53 |
| 8  | 28927    | 3.45703  | 30828    | 3.24383  | 32749    | 3.05349  | 34693    | 2.88240  | 52 |
| 9  | 28958    | 3.45327  | 30860    | 3.24049  | 32782    | 3.05049  | 34726    | 2.87970  | 51 |
| 10 | 28990    | 3.44951  | 30891    | 3.23714  | 32814    | 3.04749  | 34758    | 2.87700  | 50 |
| 11 | 29021    | 3.44576  | 30923    | 3.23381  | 32846    | 3.04450  | 34791    | 2.87430  | 49 |
| 12 | 29053    | 3.44202  | 30955    | 3.23048  | 32878    | 3.04152  | 34824    | 2.87161  | 48 |
| 13 | 29084    | 3.43829  | 30987    | 3.22715  | 32911    | 3.03854  | 34856    | 2.86892  | 47 |
| 14 | 29116    | 3.43456  | 31019    | 3.22384  | 32943    | 3.03556  | 34889    | 2.86624  | 46 |
| 15 | 29147    | 3.43084  | 31051    | 3.22053  | 32975    | 3.03260  | 34922    | 2.86356  | 45 |
| 16 | 29179    | 3.42713  | 31083    | 3.21722  | 33007    | 3.02963  | 34954    | 2.86089  | 44 |
| 17 | 29210    | 3.42343  | 31115    | 3.21392  | 33040    | 3.02667  | 34987    | 2.85822  | 43 |
| 18 | 29242    | 3.41973  | 31147    | 3.21063  | 33072    | 3.02372  | 35019    | 2.85555  | 42 |
| 19 | 29274    | 3.41604  | 31178    | 3.20734  | 33104    | 3.02077  | 35052    | 2.85289  | 41 |
| 20 | 29305    | 3.41236  | 31210    | 3.20406  | 33136    | 3.01783  | 35085    | 2.85023  | 40 |
| 21 | 29337    | 3.40869  | 31242    | 3.20079  | 33169    | 3.01489  | 35117    | 2.84758  | 39 |
| 22 | 29368    | 3.40502  | 31274    | 3.19752  | 33201    | 3.01196  | 35150    | 2.84494  | 38 |
| 23 | 29400    | 3.40136  | 31306    | 3.19426  | 33233    | 3.00903  | 35183    | 2.84229  | 37 |
| 24 | 29432    | 3.39771  | 31338    | 3.19100  | 33266    | 3.00611  | 35216    | 2.83965  | 36 |
| 25 | 29463    | 3.39406  | 31370    | 3.18775  | 33298    | 3.00319  | 35248    | 2.83702  | 35 |
| 26 | 29495    | 3.39042  | 31402    | 3.18451  | 33330    | 3.00028  | 35281    | 2.83439  | 34 |
| 27 | 29526    | 3.38679  | 31434    | 3.18127  | 33363    | 2.99738  | 35314    | 2.83176  | 33 |
| 28 | 29558    | 3.38317  | 31466    | 3.17804  | 33395    | 2.99447  | 35346    | 2.82914  | 32 |
| 29 | 29590    | 3.37955  | 31498    | 3.17481  | 33427    | 2.99158  | 35379    | 2.82653  | 31 |
| 30 | 29621    | 3.37594  | 31530    | 3.17159  | 33460    | 2.98868  | 35412    | 2.82391  | 30 |
| 31 | 29653    | 3.37234  | 31562    | 3.16838  | 33492    | 2.98580  | 35445    | 2.82130  | 29 |
| 32 | 29685    | 3.36875  | 31594    | 3.16517  | 33524    | 2.98292  | 35477    | 2.81870  | 28 |
| 33 | 29716    | 3.36516  | 31626    | 3.16197  | 33557    | 2.98004  | 35510    | 2.81610  | 27 |
| 34 | 29748    | 3.36158  | 31658    | 3.15877  | 33589    | 2.97717  | 35543    | 2.81350  | 26 |
| 35 | 29780    | 3.35800  | 31690    | 3.15558  | 33621    | 2.97430  | 35576    | 2.81091  | 25 |
| 36 | 29811    | 3.35443  | 31722    | 3.15240  | 33654    | 2.97144  | 35608    | 2.80833  | 24 |
| 37 | 29843    | 3.35087  | 31754    | 3.14922  | 33686    | 2.96858  | 35641    | 2.80574  | 23 |
| 38 | 29875    | 3.34732  | 31786    | 3.14605  | 33718    | 2.96573  | 35674    | 2.80316  | 22 |
| 39 | 29906    | 3.34377  | 31818    | 3.14288  | 33751    | 2.96288  | 35707    | 2.80059  | 21 |
| 40 | 29938    | 3.34023  | 31850    | 3.13972  | 33783    | 2.96004  | 35740    | 2.79802  | 20 |
| 41 | 29970    | 3.33669  | 31882    | 3.13656  | 33816    | 2.95721  | 35772    | 2.79545  | 19 |
| 42 | 30001    | 3.33317  | 31914    | 3.13341  | 33848    | 2.95437  | 35805    | 2.79289  | 18 |
| 43 | 30033    | 3.32965  | 31946    | 3.13027  | 33881    | 2.95155  | 35838    | 2.79033  | 17 |
| 44 | 30065    | 3.32614  | 31978    | 3.12713  | 33913    | 2.94872  | 35871    | 2.78778  | 16 |
| 45 | 30097    | 3.32264  | 32010    | 3.12400  | 33945    | 2.94590  | 35904    | 2.78523  | 15 |
| 46 | 30128    | 3.31914  | 32042    | 3.12087  | 33978    | 2.94309  | 35937    | 2.78269  | 14 |
| 47 | 30160    | 3.31565  | 32074    | 3.11775  | 34010    | 2.94028  | 35969    | 2.78014  | 13 |
| 48 | 30192    | 3.31216  | 32106    | 3.11464  | 34043    | 2.93748  | 36002    | 2.77761  | 12 |
| 49 | 30224    | 3.30868  | 32139    | 3.11153  | 34075    | 2.93468  | 36035    | 2.77507  | 11 |
| 50 | 30255    | 3.30521  | 32171    | 3.10842  | 34108    | 2.93189  | 36068    | 2.77254  | 10 |
| 51 | 30287    | 3.30174  | 32203    | 3.10532  | 34140    | 2.92910  | 36101    | 2.77002  | 9  |
| 52 | 30319    | 3.29829  | 32235    | 3.10223  | 34173    | 2.92632  | 36134    | 2.76750  | 8  |
| 53 | 30351    | 3.29483  | 32267    | 3.09914  | 34205    | 2.92354  | 36167    | 2.76498  | 7  |
| 54 | 30382    | 3.29139  | 32299    | 3.09606  | 34238    | 2.92076  | 36199    | 2.76247  | 6  |
| 55 | 30414    | 3.28795  | 32331    | 3.09298  | 34270    | 2.91799  | 36232    | 2.75996  | 5  |
| 56 | 30446    | 3.28452  | 32363    | 3.08991  | 34303    | 2.91523  | 36265    | 2.75746  | 4  |
| 57 | 30478    | 3.28109  | 32396    | 3.08685  | 34335    | 2.91246  | 36298    | 2.75496  | 3  |
| 58 | 30509    | 3.27767  | 32428    | 3.08379  | 34368    | 2.90971  | 36331    | 2.75246  | 2  |
| 59 | 30541    | 3.27426  | 32460    | 3.08073  | 34400    | 2.90696  | 36364    | 2.74997  | 1  |
| 60 | 30573    | 3.27085  | 32492    | 3.07768  | 34433    | 2.90421  | 36397    | 2.74748  | 0  |
|    | 16°      |          | 17°      |          | 18°      |          | 19°      |          |    |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 78°      |          | 72°      |          | 71°      |          | 70°      |          |    |

|    | 20°      |          | 21°      |          | 22°      |          | 23°      |          |    |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 36397    | 2.74748  | 38386    | 2.60509  | 40403    | 2.47509  | 42447    | 2.35585  | 60 |
| 1  | 36430    | 2.74499  | 38420    | 2.60283  | 40436    | 2.47302  | 42482    | 2.35395  | 59 |
| 2  | 36463    | 2.74251  | 38453    | 2.60057  | 40470    | 2.47095  | 42516    | 2.35205  | 58 |
| 3  | 36496    | 2.74004  | 38487    | 2.59831  | 40504    | 2.46888  | 42551    | 2.35015  | 57 |
| 4  | 36529    | 2.73756  | 38520    | 2.59606  | 40538    | 2.46682  | 42585    | 2.34825  | 56 |
| 5  | 36562    | 2.73509  | 38553    | 2.59381  | 40572    | 2.46476  | 42619    | 2.34636  | 55 |
| 6  | 36595    | 2.73263  | 38587    | 2.59156  | 40606    | 2.46270  | 42654    | 2.34447  | 54 |
| 7  | 36628    | 2.73017  | 38620    | 2.58932  | 40640    | 2.46065  | 42688    | 2.34258  | 53 |
| 8  | 36661    | 2.72771  | 38654    | 2.58708  | 40674    | 2.45860  | 42722    | 2.34069  | 52 |
| 9  | 36694    | 2.72526  | 38687    | 2.58484  | 40707    | 2.45655  | 42757    | 2.33881  | 51 |
| 10 | 36727    | 2.72281  | 38721    | 2.58261  | 40741    | 2.45451  | 42791    | 2.33693  | 50 |
| 11 | 36760    | 2.72036  | 38754    | 2.58038  | 40775    | 2.45246  | 42826    | 2.33505  | 49 |
| 12 | 36793    | 2.71792  | 38787    | 2.57815  | 40809    | 2.45043  | 42860    | 2.33317  | 48 |
| 13 | 36826    | 2.71548  | 38821    | 2.57593  | 40843    | 2.44839  | 42894    | 2.33130  | 47 |
| 14 | 36859    | 2.71305  | 38854    | 2.57371  | 40877    | 2.44636  | 42929    | 2.32943  | 46 |
| 15 | 36892    | 2.71062  | 38888    | 2.57150  | 40911    | 2.44433  | 42963    | 2.32756  | 45 |
| 16 | 36925    | 2.70819  | 38921    | 2.56928  | 40945    | 2.44230  | 42998    | 2.32570  | 44 |
| 17 | 36958    | 2.70577  | 38955    | 2.56707  | 40979    | 2.44027  | 43032    | 2.32383  | 43 |
| 18 | 36991    | 2.70335  | 38988    | 2.56487  | 41013    | 2.43825  | 43067    | 2.32197  | 42 |
| 19 | 37024    | 2.70094  | 39022    | 2.56266  | 41047    | 2.43623  | 43101    | 2.32012  | 41 |
| 20 | 37057    | 2.69853  | 39055    | 2.56046  | 41081    | 2.43422  | 43136    | 2.31826  | 40 |
| 21 | 37090    | 2.69612  | 39089    | 2.55827  | 41115    | 2.43220  | 43170    | 2.31641  | 39 |
| 22 | 37124    | 2.69371  | 39122    | 2.55608  | 41149    | 2.43019  | 43205    | 2.31456  | 38 |
| 23 | 37157    | 2.69131  | 39156    | 2.55389  | 41183    | 2.42819  | 43239    | 2.31271  | 37 |
| 24 | 37190    | 2.68892  | 39190    | 2.55170  | 41217    | 2.42618  | 43274    | 2.31086  | 36 |
| 25 | 37223    | 2.68653  | 39223    | 2.54952  | 41251    | 2.42418  | 43308    | 2.30902  | 35 |
| 26 | 37256    | 2.68414  | 39257    | 2.54734  | 41285    | 2.42218  | 43343    | 2.30718  | 34 |
| 27 | 37289    | 2.68175  | 39290    | 2.54516  | 41319    | 2.42019  | 43378    | 2.30534  | 33 |
| 28 | 37322    | 2.67937  | 39324    | 2.54299  | 41353    | 2.41819  | 43412    | 2.30351  | 32 |
| 29 | 37355    | 2.67700  | 39357    | 2.54082  | 41387    | 2.41620  | 43447    | 2.30167  | 31 |
| 30 | 37388    | 2.67462  | 39391    | 2.53865  | 41421    | 2.41421  | 43481    | 2.29984  | 30 |
| 31 | 37422    | 2.67225  | 39425    | 2.53648  | 41455    | 2.41223  | 43516    | 2.29801  | 29 |
| 32 | 37455    | 2.66989  | 39458    | 2.53432  | 41490    | 2.41025  | 43550    | 2.29619  | 28 |
| 33 | 37488    | 2.66752  | 39492    | 2.53217  | 41524    | 2.40827  | 43585    | 2.29437  | 27 |
| 34 | 37521    | 2.66516  | 39526    | 2.53001  | 41558    | 2.40629  | 43620    | 2.29254  | 26 |
| 35 | 37554    | 2.66281  | 39559    | 2.52786  | 41592    | 2.40432  | 43654    | 2.29073  | 25 |
| 36 | 37588    | 2.66046  | 39593    | 2.52571  | 41626    | 2.40235  | 43689    | 2.28891  | 24 |
| 37 | 37621    | 2.65811  | 39626    | 2.52357  | 41660    | 2.40038  | 43724    | 2.28710  | 23 |
| 38 | 37654    | 2.65576  | 39660    | 2.52142  | 41694    | 2.39841  | 43758    | 2.28528  | 22 |
| 39 | 37687    | 2.65342  | 39694    | 2.51929  | 41728    | 2.39645  | 43793    | 2.28348  | 21 |
| 40 | 37720    | 2.65109  | 39727    | 2.51715  | 41763    | 2.39449  | 43828    | 2.28167  | 20 |
| 41 | 37754    | 2.64875  | 39761    | 2.51502  | 41797    | 2.39253  | 43862    | 2.27987  | 19 |
| 42 | 37787    | 2.64642  | 39795    | 2.51289  | 41831    | 2.39058  | 43897    | 2.27806  | 18 |
| 43 | 37820    | 2.64410  | 39829    | 2.51076  | 41865    | 2.38862  | 43932    | 2.27627  | 17 |
| 44 | 37853    | 2.64177  | 39862    | 2.50864  | 41899    | 2.38668  | 43966    | 2.27447  | 16 |
| 45 | 37887    | 2.63945  | 39896    | 2.50652  | 41933    | 2.38473  | 44001    | 2.27267  | 15 |
| 46 | 37920    | 2.63714  | 39930    | 2.50440  | 41968    | 2.38279  | 44036    | 2.27088  | 14 |
| 47 | 37953    | 2.63483  | 39963    | 2.50229  | 42002    | 2.38084  | 44071    | 2.26909  | 13 |
| 48 | 37986    | 2.63252  | 39997    | 2.50018  | 42036    | 2.37891  | 44105    | 2.26730  | 12 |
| 49 | 38020    | 2.63021  | 40031    | 2.49807  | 42070    | 2.37697  | 44140    | 2.26552  | 11 |
| 50 | 38053    | 2.62791  | 40065    | 2.49597  | 42105    | 2.37504  | 44175    | 2.26374  | 10 |
| 51 | 38086    | 2.62561  | 40099    | 2.49386  | 42139    | 2.37311  | 44210    | 2.26196  | 9  |
| 52 | 38120    | 2.62332  | 40132    | 2.49177  | 42173    | 2.37118  | 44244    | 2.26018  | 8  |
| 53 | 38153    | 2.62103  | 40166    | 2.48968  | 42207    | 2.36925  | 44279    | 2.25840  | 7  |
| 54 | 38186    | 2.61874  | 40200    | 2.48758  | 42242    | 2.36733  | 44314    | 2.25663  | 6  |
| 55 | 38220    | 2.61646  | 40234    | 2.48549  | 42276    | 2.36541  | 44349    | 2.25486  | 5  |
| 56 | 38253    | 2.61418  | 40267    | 2.48340  | 42310    | 2.36349  | 44384    | 2.25309  | 4  |
| 57 | 38286    | 2.61190  | 40301    | 2.48132  | 42345    | 2.36158  | 44418    | 2.25132  | 3  |
| 58 | 38320    | 2.60963  | 40335    | 2.47924  | 42379    | 2.35967  | 44453    | 2.24956  | 2  |
| 59 | 38353    | 2.60736  | 40369    | 2.47716  | 42413    | 2.35776  | 44488    | 2.24780  | 1  |
| 60 | 38386    | 2.60509  | 40403    | 2.47509  | 42447    | 2.35585  | 44523    | 2.24604  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 69°      |          | 68°      |          | 67°      |          | 66°      |          |    |

TABLE III. NATURAL TANGENTS AND COTANGENTS.

79

| °  | 24°      |          | 25°      |          | 26°      |          | 27°      |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 44523    | 2.24604  | 46631    | 2.14451  | 48773    | 2.05330  | 50953    | 1.96261  | 60 |
| 1  | 44558    | 2.24428  | 46666    | 2.14288  | 48809    | 2.04879  | 50989    | 1.96120  | 59 |
| 2  | 44593    | 2.24252  | 46702    | 2.14125  | 48845    | 2.04428  | 51026    | 1.95979  | 58 |
| 3  | 44627    | 2.24077  | 46737    | 2.13963  | 48881    | 2.03977  | 51063    | 1.95838  | 57 |
| 4  | 44662    | 2.23902  | 46772    | 2.13801  | 48917    | 2.03526  | 51099    | 1.95698  | 56 |
| 5  | 44697    | 2.23727  | 46808    | 2.13639  | 48953    | 2.03075  | 51136    | 1.95557  | 55 |
| 6  | 44732    | 2.23553  | 46843    | 2.13477  | 48989    | 2.02624  | 51173    | 1.95417  | 54 |
| 7  | 44767    | 2.23378  | 46879    | 2.13316  | 49026    | 2.02173  | 51209    | 1.95277  | 53 |
| 8  | 44802    | 2.23204  | 46914    | 2.13154  | 49062    | 2.01722  | 51246    | 1.95137  | 52 |
| 9  | 44837    | 2.23030  | 46950    | 2.12993  | 49098    | 2.01271  | 51283    | 1.94997  | 51 |
| 10 | 44872    | 2.22857  | 46985    | 2.12832  | 49134    | 2.00820  | 51319    | 1.94858  | 50 |
| 11 | 44907    | 2.22683  | 47021    | 2.12671  | 49170    | 2.00369  | 51356    | 1.94718  | 49 |
| 12 | 44942    | 2.22510  | 47056    | 2.12511  | 49206    | 2.00018  | 51393    | 1.94579  | 48 |
| 13 | 44977    | 2.22337  | 47092    | 2.12350  | 49242    | 2.00000  | 51430    | 1.94440  | 47 |
| 14 | 45012    | 2.22164  | 47128    | 2.12190  | 49278    | 2.00000  | 51467    | 1.94301  | 46 |
| 15 | 45047    | 2.21992  | 47163    | 2.12030  | 49315    | 2.00000  | 51503    | 1.94162  | 45 |
| 16 | 45082    | 2.21819  | 47199    | 2.11871  | 49351    | 2.00000  | 51540    | 1.94023  | 44 |
| 17 | 45117    | 2.21647  | 47234    | 2.11711  | 49387    | 2.00000  | 51577    | 1.93885  | 43 |
| 18 | 45152    | 2.21475  | 47270    | 2.11552  | 49423    | 2.00000  | 51614    | 1.93746  | 42 |
| 19 | 45187    | 2.21304  | 47305    | 2.11392  | 49459    | 2.00000  | 51651    | 1.93608  | 41 |
| 20 | 45222    | 2.21132  | 47341    | 2.11233  | 49495    | 2.00000  | 51688    | 1.93470  | 40 |
| 21 | 45257    | 2.20961  | 47377    | 2.11075  | 49532    | 2.00000  | 51724    | 1.93332  | 39 |
| 22 | 45292    | 2.20790  | 47412    | 2.10916  | 49568    | 2.00000  | 51761    | 1.93195  | 38 |
| 23 | 45327    | 2.20619  | 47448    | 2.10758  | 49604    | 2.00000  | 51798    | 1.93057  | 37 |
| 24 | 45362    | 2.20448  | 47483    | 2.10600  | 49640    | 2.00000  | 51835    | 1.92920  | 36 |
| 25 | 45397    | 2.20278  | 47519    | 2.10442  | 49677    | 2.00000  | 51872    | 1.92782  | 35 |
| 26 | 45432    | 2.20108  | 47555    | 2.10284  | 49713    | 2.00000  | 51909    | 1.92645  | 34 |
| 27 | 45467    | 2.19938  | 47590    | 2.10126  | 49749    | 2.00000  | 51946    | 1.92508  | 33 |
| 28 | 45502    | 2.19769  | 47626    | 2.09969  | 49786    | 2.00000  | 51983    | 1.92371  | 32 |
| 29 | 45537    | 2.19599  | 47662    | 2.09811  | 49822    | 2.00000  | 52020    | 1.92235  | 31 |
| 30 | 45573    | 2.19430  | 47698    | 2.09654  | 49858    | 2.00000  | 52057    | 1.92098  | 30 |
| 31 | 45608    | 2.19261  | 47733    | 2.09498  | 49894    | 2.00000  | 52094    | 1.91962  | 29 |
| 32 | 45643    | 2.19092  | 47769    | 2.09341  | 49931    | 2.00000  | 52131    | 1.91826  | 28 |
| 33 | 45678    | 2.18923  | 47805    | 2.09184  | 49967    | 2.00000  | 52168    | 1.91690  | 27 |
| 34 | 45713    | 2.18755  | 47840    | 2.09028  | 50004    | 1.99986  | 52205    | 1.91554  | 26 |
| 35 | 45748    | 2.18587  | 47876    | 2.08872  | 50040    | 1.99972  | 52242    | 1.91418  | 25 |
| 36 | 45784    | 2.18419  | 47912    | 2.08716  | 50076    | 1.99958  | 52279    | 1.91282  | 24 |
| 37 | 45819    | 2.18251  | 47948    | 2.08560  | 50113    | 1.99944  | 52316    | 1.91147  | 23 |
| 38 | 45854    | 2.18084  | 47984    | 2.08405  | 50149    | 1.99930  | 52353    | 1.91012  | 22 |
| 39 | 45889    | 2.17916  | 48019    | 2.08250  | 50185    | 1.99916  | 52390    | 1.90876  | 21 |
| 40 | 45924    | 2.17749  | 48055    | 2.08094  | 50222    | 1.99902  | 52427    | 1.90741  | 20 |
| 41 | 45960    | 2.17582  | 48091    | 2.07939  | 50258    | 1.99888  | 52464    | 1.90607  | 19 |
| 42 | 45995    | 2.17416  | 48127    | 2.07785  | 50295    | 1.99874  | 52501    | 1.90472  | 18 |
| 43 | 46030    | 2.17249  | 48163    | 2.07630  | 50331    | 1.99860  | 52538    | 1.90337  | 17 |
| 44 | 46065    | 2.17083  | 48198    | 2.07476  | 50368    | 1.99846  | 52575    | 1.90203  | 16 |
| 45 | 46101    | 2.16917  | 48234    | 2.07321  | 50404    | 1.99832  | 52613    | 1.90069  | 15 |
| 46 | 46136    | 2.16751  | 48270    | 2.07167  | 50441    | 1.99818  | 52650    | 1.89935  | 14 |
| 47 | 46171    | 2.16585  | 48306    | 2.07014  | 50477    | 1.99804  | 52687    | 1.89801  | 13 |
| 48 | 46206    | 2.16420  | 48342    | 2.06860  | 50514    | 1.99790  | 52724    | 1.89667  | 12 |
| 49 | 46242    | 2.16255  | 48378    | 2.06706  | 50550    | 1.99776  | 52761    | 1.89533  | 11 |
| 50 | 46277    | 2.16090  | 48414    | 2.06553  | 50587    | 1.99762  | 52798    | 1.89400  | 10 |
| 51 | 46312    | 2.15925  | 48450    | 2.06400  | 50623    | 1.99748  | 52836    | 1.89266  | 9  |
| 52 | 46348    | 2.15760  | 48486    | 2.06247  | 50660    | 1.99734  | 52873    | 1.89133  | 8  |
| 53 | 46383    | 2.15596  | 48521    | 2.06094  | 50696    | 1.99720  | 52910    | 1.89000  | 7  |
| 54 | 46418    | 2.15432  | 48557    | 2.05942  | 50733    | 1.99706  | 52947    | 1.88867  | 6  |
| 55 | 46454    | 2.15268  | 48593    | 2.05790  | 50769    | 1.99692  | 52984    | 1.88734  | 5  |
| 56 | 46489    | 2.15104  | 48629    | 2.05637  | 50806    | 1.99678  | 53022    | 1.88602  | 4  |
| 57 | 46525    | 2.14940  | 48665    | 2.05485  | 50843    | 1.99664  | 53059    | 1.88469  | 3  |
| 58 | 46560    | 2.14777  | 48701    | 2.05333  | 50879    | 1.99650  | 53096    | 1.88337  | 2  |
| 59 | 46595    | 2.14614  | 48737    | 2.05182  | 50916    | 1.99636  | 53134    | 1.88205  | 1  |
| 60 | 46631    | 2.14451  | 48773    | 2.05030  | 50953    | 1.99622  | 53171    | 1.88073  | 0  |
| °  | 24°      |          | 25°      |          | 26°      |          | 27°      |          | °  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 65°      |          | 64°      |          | 63°      |          | 62°      |          |    |

|    | 28°      |          | 29°      |          | 30°      |          | 31°      |          |    |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 53171    | 1.88073  | 55431    | 1.80405  | 57735    | 1.73205  | 60086    | 1.66428  | 60 |
| 1  | 53208    | 1.87941  | 55469    | 1.80281  | 57774    | 1.73089  | 60126    | 1.66318  | 59 |
| 2  | 53246    | 1.87809  | 55507    | 1.80158  | 57813    | 1.72973  | 60165    | 1.66209  | 58 |
| 3  | 53283    | 1.87677  | 55545    | 1.80034  | 57851    | 1.72857  | 60205    | 1.66099  | 57 |
| 4  | 53320    | 1.87546  | 55583    | 1.79911  | 57890    | 1.72741  | 60245    | 1.65990  | 56 |
| 5  | 53358    | 1.87415  | 55621    | 1.79788  | 57929    | 1.72625  | 60284    | 1.65881  | 55 |
| 6  | 53395    | 1.87283  | 55659    | 1.79665  | 57968    | 1.72509  | 60324    | 1.65772  | 54 |
| 7  | 53432    | 1.87152  | 55697    | 1.79542  | 58007    | 1.72393  | 60364    | 1.65663  | 53 |
| 8  | 53470    | 1.87021  | 55736    | 1.79419  | 58046    | 1.72278  | 60403    | 1.65554  | 52 |
| 9  | 53507    | 1.86891  | 55774    | 1.79296  | 58085    | 1.72163  | 60443    | 1.65445  | 51 |
| 10 | 53545    | 1.86760  | 55812    | 1.79174  | 58124    | 1.72047  | 60483    | 1.65337  | 50 |
| 11 | 53582    | 1.86630  | 55850    | 1.79051  | 58162    | 1.71932  | 60522    | 1.65228  | 49 |
| 12 | 53620    | 1.86499  | 55888    | 1.78929  | 58201    | 1.71817  | 60562    | 1.65120  | 48 |
| 13 | 53657    | 1.86369  | 55926    | 1.78807  | 58240    | 1.71702  | 60602    | 1.65011  | 47 |
| 14 | 53694    | 1.86239  | 55964    | 1.78685  | 58279    | 1.71588  | 60642    | 1.64903  | 46 |
| 15 | 53732    | 1.86109  | 56003    | 1.78563  | 58318    | 1.71473  | 60681    | 1.64795  | 45 |
| 16 | 53769    | 1.85979  | 56041    | 1.78441  | 58357    | 1.71358  | 60721    | 1.64687  | 44 |
| 17 | 53807    | 1.85850  | 56079    | 1.78319  | 58396    | 1.71244  | 60761    | 1.64579  | 43 |
| 18 | 53844    | 1.85720  | 56117    | 1.78198  | 58435    | 1.71129  | 60801    | 1.64471  | 42 |
| 19 | 53882    | 1.85591  | 56156    | 1.78077  | 58474    | 1.71015  | 60841    | 1.64363  | 41 |
| 20 | 53920    | 1.85462  | 56194    | 1.77955  | 58513    | 1.70901  | 60881    | 1.64256  | 40 |
| 21 | 53957    | 1.85333  | 56232    | 1.77834  | 58552    | 1.70787  | 60921    | 1.64148  | 39 |
| 22 | 53995    | 1.85204  | 56270    | 1.77713  | 58591    | 1.70673  | 60960    | 1.64041  | 38 |
| 23 | 54032    | 1.85075  | 56309    | 1.77592  | 58631    | 1.70560  | 61000    | 1.63934  | 37 |
| 24 | 54070    | 1.84946  | 56347    | 1.77471  | 58670    | 1.70446  | 61040    | 1.63826  | 36 |
| 25 | 54107    | 1.84818  | 56385    | 1.77351  | 58709    | 1.70332  | 61080    | 1.63719  | 35 |
| 26 | 54145    | 1.84689  | 56424    | 1.77230  | 58748    | 1.70219  | 61120    | 1.63612  | 34 |
| 27 | 54183    | 1.84561  | 56462    | 1.77110  | 58787    | 1.70106  | 61160    | 1.63505  | 33 |
| 28 | 54220    | 1.84433  | 56500    | 1.76990  | 58826    | 1.69992  | 61200    | 1.63398  | 32 |
| 29 | 54258    | 1.84305  | 56539    | 1.76869  | 58865    | 1.69879  | 61240    | 1.63292  | 31 |
| 30 | 54296    | 1.84177  | 56577    | 1.76749  | 58904    | 1.69766  | 61280    | 1.63185  | 30 |
| 31 | 54333    | 1.84049  | 56616    | 1.76630  | 58944    | 1.69653  | 61320    | 1.63079  | 29 |
| 32 | 54371    | 1.83922  | 56654    | 1.76510  | 58983    | 1.69541  | 61360    | 1.62972  | 28 |
| 33 | 54409    | 1.83794  | 56693    | 1.76390  | 59022    | 1.69428  | 61400    | 1.62866  | 27 |
| 34 | 54446    | 1.83667  | 56731    | 1.76271  | 59061    | 1.69316  | 61440    | 1.62760  | 26 |
| 35 | 54484    | 1.83540  | 56769    | 1.76151  | 59101    | 1.69203  | 61480    | 1.62654  | 25 |
| 36 | 54522    | 1.83413  | 56808    | 1.76032  | 59140    | 1.69091  | 61520    | 1.62548  | 24 |
| 37 | 54560    | 1.83286  | 56846    | 1.75913  | 59179    | 1.68979  | 61561    | 1.62442  | 23 |
| 38 | 54597    | 1.83159  | 56885    | 1.75794  | 59218    | 1.68866  | 61601    | 1.62336  | 22 |
| 39 | 54635    | 1.83033  | 56923    | 1.75675  | 59258    | 1.68754  | 61641    | 1.62230  | 21 |
| 40 | 54673    | 1.82906  | 56962    | 1.75556  | 59297    | 1.68643  | 61681    | 1.62125  | 20 |
| 41 | 54711    | 1.82780  | 57000    | 1.75437  | 59336    | 1.68531  | 61721    | 1.62019  | 19 |
| 42 | 54748    | 1.82654  | 57039    | 1.75319  | 59376    | 1.68419  | 61761    | 1.61914  | 18 |
| 43 | 54786    | 1.82528  | 57078    | 1.75200  | 59415    | 1.68308  | 61801    | 1.61808  | 17 |
| 44 | 54824    | 1.82402  | 57116    | 1.75082  | 59454    | 1.68196  | 61842    | 1.61703  | 16 |
| 45 | 54862    | 1.82276  | 57155    | 1.74964  | 59494    | 1.68085  | 61882    | 1.61598  | 15 |
| 46 | 54900    | 1.82150  | 57193    | 1.74846  | 59533    | 1.67974  | 61922    | 1.61493  | 14 |
| 47 | 54938    | 1.82025  | 57232    | 1.74728  | 59573    | 1.67863  | 61962    | 1.61388  | 13 |
| 48 | 54975    | 1.81899  | 57271    | 1.74610  | 59612    | 1.67752  | 62003    | 1.61283  | 12 |
| 49 | 55013    | 1.81774  | 57309    | 1.74492  | 59651    | 1.67641  | 62043    | 1.61179  | 11 |
| 50 | 55051    | 1.81649  | 57348    | 1.74375  | 59691    | 1.67530  | 62083    | 1.61074  | 10 |
| 51 | 55089    | 1.81524  | 57386    | 1.74257  | 59730    | 1.67419  | 62124    | 1.60970  | 9  |
| 52 | 55127    | 1.81399  | 57425    | 1.74140  | 59770    | 1.67309  | 62164    | 1.60865  | 8  |
| 53 | 55165    | 1.81274  | 57464    | 1.74022  | 59809    | 1.67198  | 62204    | 1.60761  | 7  |
| 54 | 55203    | 1.81150  | 57503    | 1.73905  | 59849    | 1.67088  | 62245    | 1.60657  | 6  |
| 55 | 55241    | 1.81025  | 57541    | 1.73788  | 59888    | 1.66978  | 62285    | 1.60553  | 5  |
| 56 | 55279    | 1.80901  | 57580    | 1.73671  | 59928    | 1.66867  | 62325    | 1.60449  | 4  |
| 57 | 55317    | 1.80777  | 57619    | 1.73555  | 59967    | 1.66757  | 62366    | 1.60345  | 3  |
| 58 | 55355    | 1.80653  | 57657    | 1.73438  | 60007    | 1.66647  | 62406    | 1.60241  | 2  |
| 59 | 55393    | 1.80529  | 57696    | 1.73321  | 60046    | 1.66538  | 62446    | 1.60137  | 1  |
| 60 | 55431    | 1.80405  | 57735    | 1.73205  | 60086    | 1.66428  | 62487    | 1.60033  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 61°      |          | 60°      |          | 59°      |          | 58°      |          |    |

TABLE III. NATURAL TANGENTS AND COTANGENTS. 81

|    | 82°      |          | 88°      |          | 84°      |          | 80°      |          |    |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 62487    | 1.60033  | 64941    | 1.53986  | 67451    | 1.48256  | 70021    | 1.42815  | 60 |
| 1  | 62527    | 1.59930  | 64982    | 1.53888  | 67493    | 1.48163  | 70064    | 1.42726  | 59 |
| 2  | 62568    | 1.59826  | 65023    | 1.53791  | 67536    | 1.48070  | 70107    | 1.42638  | 58 |
| 3  | 62608    | 1.59723  | 65065    | 1.53693  | 67578    | 1.47977  | 70151    | 1.42550  | 57 |
| 4  | 62649    | 1.59620  | 65106    | 1.53595  | 67620    | 1.47885  | 70194    | 1.42462  | 56 |
| 5  | 62689    | 1.59517  | 65148    | 1.53497  | 67663    | 1.47792  | 70238    | 1.42374  | 55 |
| 6  | 62730    | 1.59414  | 65189    | 1.53400  | 67705    | 1.47699  | 70281    | 1.42286  | 54 |
| 7  | 62770    | 1.59311  | 65231    | 1.53302  | 67748    | 1.47607  | 70325    | 1.42198  | 53 |
| 8  | 62811    | 1.59208  | 65272    | 1.53205  | 67790    | 1.47514  | 70368    | 1.42110  | 52 |
| 9  | 62852    | 1.59105  | 65314    | 1.53107  | 67832    | 1.47422  | 70412    | 1.42022  | 51 |
| 10 | 62893    | 1.59002  | 65355    | 1.53010  | 67875    | 1.47330  | 70455    | 1.41934  | 50 |
| 11 | 62933    | 1.58900  | 65397    | 1.52913  | 67917    | 1.47238  | 70499    | 1.41847  | 49 |
| 12 | 62973    | 1.58797  | 65438    | 1.52816  | 67960    | 1.47146  | 70542    | 1.41759  | 48 |
| 13 | 63014    | 1.58695  | 65480    | 1.52719  | 68002    | 1.47053  | 70586    | 1.41672  | 47 |
| 14 | 63055    | 1.58593  | 65521    | 1.52622  | 68045    | 1.46962  | 70629    | 1.41584  | 46 |
| 15 | 63095    | 1.58490  | 65563    | 1.52525  | 68088    | 1.46870  | 70673    | 1.41497  | 45 |
| 16 | 63136    | 1.58388  | 65604    | 1.52429  | 68130    | 1.46778  | 70717    | 1.41409  | 44 |
| 17 | 63177    | 1.58286  | 65646    | 1.52332  | 68173    | 1.46686  | 70760    | 1.41322  | 43 |
| 18 | 63217    | 1.58184  | 65688    | 1.52235  | 68215    | 1.46595  | 70804    | 1.41235  | 42 |
| 19 | 63258    | 1.58083  | 65729    | 1.52139  | 68258    | 1.46503  | 70848    | 1.41148  | 41 |
| 20 | 63299    | 1.57981  | 65771    | 1.52043  | 68301    | 1.46411  | 70891    | 1.41061  | 40 |
| 21 | 63340    | 1.57879  | 65813    | 1.51946  | 68343    | 1.46320  | 70935    | 1.40974  | 39 |
| 22 | 63380    | 1.57777  | 65854    | 1.51850  | 68386    | 1.46229  | 70979    | 1.40887  | 38 |
| 23 | 63421    | 1.57676  | 65896    | 1.51754  | 68429    | 1.46137  | 71023    | 1.40800  | 37 |
| 24 | 63462    | 1.57575  | 65938    | 1.51658  | 68471    | 1.46046  | 71066    | 1.40714  | 36 |
| 25 | 63503    | 1.57474  | 65980    | 1.51562  | 68514    | 1.45955  | 71110    | 1.40627  | 35 |
| 26 | 63544    | 1.57372  | 66021    | 1.51466  | 68557    | 1.45864  | 71154    | 1.40540  | 34 |
| 27 | 63584    | 1.57271  | 66063    | 1.51370  | 68600    | 1.45773  | 71198    | 1.40454  | 33 |
| 28 | 63625    | 1.57170  | 66105    | 1.51275  | 68642    | 1.45682  | 71242    | 1.40367  | 32 |
| 29 | 63666    | 1.57069  | 66147    | 1.51179  | 68685    | 1.45591  | 71285    | 1.40281  | 31 |
| 30 | 63707    | 1.56969  | 66189    | 1.51084  | 68728    | 1.45502  | 71329    | 1.40195  | 30 |
| 31 | 63748    | 1.56868  | 66230    | 1.50988  | 68771    | 1.45410  | 71373    | 1.40109  | 29 |
| 32 | 63789    | 1.56767  | 66272    | 1.50893  | 68814    | 1.45320  | 71417    | 1.40022  | 28 |
| 33 | 63830    | 1.56667  | 66314    | 1.50797  | 68857    | 1.45229  | 71461    | 1.39936  | 27 |
| 34 | 63871    | 1.56566  | 66356    | 1.50702  | 68900    | 1.45139  | 71505    | 1.39850  | 26 |
| 35 | 63912    | 1.56466  | 66398    | 1.50607  | 68942    | 1.45049  | 71549    | 1.39764  | 25 |
| 36 | 63953    | 1.56366  | 66440    | 1.50512  | 68985    | 1.44958  | 71593    | 1.39679  | 24 |
| 37 | 63994    | 1.56265  | 66482    | 1.50417  | 69028    | 1.44868  | 71637    | 1.39593  | 23 |
| 38 | 64035    | 1.56165  | 66524    | 1.50322  | 69071    | 1.44778  | 71681    | 1.39507  | 22 |
| 39 | 64076    | 1.56065  | 66566    | 1.50228  | 69114    | 1.44688  | 71725    | 1.39421  | 21 |
| 40 | 64117    | 1.55966  | 66608    | 1.50133  | 69157    | 1.44598  | 71769    | 1.39336  | 20 |
| 41 | 64158    | 1.55866  | 66650    | 1.50038  | 69200    | 1.44508  | 71813    | 1.39250  | 19 |
| 42 | 64199    | 1.55766  | 66692    | 1.49944  | 69243    | 1.44418  | 71857    | 1.39165  | 18 |
| 43 | 64240    | 1.55666  | 66734    | 1.49849  | 69286    | 1.44329  | 71901    | 1.39079  | 17 |
| 44 | 64281    | 1.55567  | 66776    | 1.49755  | 69329    | 1.44239  | 71946    | 1.38994  | 16 |
| 45 | 64322    | 1.55467  | 66818    | 1.49661  | 69372    | 1.44149  | 71990    | 1.38909  | 15 |
| 46 | 64363    | 1.55368  | 66860    | 1.49566  | 69416    | 1.44060  | 72034    | 1.38824  | 14 |
| 47 | 64404    | 1.55269  | 66902    | 1.49472  | 69459    | 1.43970  | 72078    | 1.38738  | 13 |
| 48 | 64446    | 1.55170  | 66944    | 1.49378  | 69502    | 1.43881  | 72122    | 1.38653  | 12 |
| 49 | 64487    | 1.55071  | 66986    | 1.49284  | 69545    | 1.43792  | 72166    | 1.38568  | 11 |
| 50 | 64528    | 1.54972  | 67028    | 1.49190  | 69588    | 1.43703  | 72211    | 1.38484  | 10 |
| 51 | 64569    | 1.54873  | 67071    | 1.49097  | 69631    | 1.43614  | 72255    | 1.38399  | 9  |
| 52 | 64610    | 1.54774  | 67113    | 1.49003  | 69675    | 1.43525  | 72299    | 1.38314  | 8  |
| 53 | 64652    | 1.54675  | 67155    | 1.48909  | 69718    | 1.43436  | 72344    | 1.38229  | 7  |
| 54 | 64693    | 1.54576  | 67197    | 1.48816  | 69761    | 1.43347  | 72388    | 1.38145  | 6  |
| 55 | 64734    | 1.54478  | 67239    | 1.48722  | 69804    | 1.43258  | 72432    | 1.38060  | 5  |
| 56 | 64775    | 1.54379  | 67282    | 1.48629  | 69847    | 1.43169  | 72477    | 1.37976  | 4  |
| 57 | 64817    | 1.54281  | 67324    | 1.48536  | 69891    | 1.43080  | 72521    | 1.37891  | 3  |
| 58 | 64858    | 1.54183  | 67366    | 1.48442  | 69934    | 1.42992  | 72565    | 1.37807  | 2  |
| 59 | 64899    | 1.54085  | 67409    | 1.48349  | 69977    | 1.42903  | 72610    | 1.37722  | 1  |
| 60 | 64941    | 1.53986  | 67451    | 1.48256  | 70021    | 1.42815  | 72654    | 1.37638  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 57°      |          | 56°      |          | 55°      |          | 54°      |          |    |

|    | 86°      |          | 87°      |          | 88°      |          | 89°      |          |    |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 72654    | 1.37638  | 75355    | 1.32704  | 78129    | 1.27994  | 80978    | 1.23490  | 60 |
| 1  | 72699    | 1.37554  | 75401    | 1.32624  | 78175    | 1.27917  | 81027    | 1.23416  | 59 |
| 2  | 72743    | 1.37470  | 75447    | 1.32544  | 78222    | 1.27841  | 81075    | 1.23343  | 58 |
| 3  | 72788    | 1.37386  | 75492    | 1.32464  | 78269    | 1.27764  | 81123    | 1.23270  | 57 |
| 4  | 72832    | 1.37302  | 75538    | 1.32384  | 78316    | 1.27688  | 81171    | 1.23196  | 56 |
| 5  | 72877    | 1.37218  | 75584    | 1.32304  | 78363    | 1.27611  | 81220    | 1.23123  | 55 |
| 6  | 72921    | 1.37134  | 75629    | 1.32224  | 78410    | 1.27535  | 81268    | 1.23050  | 54 |
| 7  | 72966    | 1.37050  | 75675    | 1.32144  | 78457    | 1.27458  | 81316    | 1.22977  | 53 |
| 8  | 73010    | 1.36967  | 75721    | 1.32064  | 78504    | 1.27382  | 81364    | 1.22904  | 52 |
| 9  | 73055    | 1.36883  | 75767    | 1.31984  | 78551    | 1.27306  | 81413    | 1.22831  | 51 |
| 10 | 73100    | 1.36800  | 75812    | 1.31904  | 78598    | 1.27230  | 81461    | 1.22758  | 50 |
| 11 | 73144    | 1.36716  | 75858    | 1.31825  | 78645    | 1.27153  | 81510    | 1.22685  | 49 |
| 12 | 73189    | 1.36633  | 75904    | 1.31745  | 78692    | 1.27077  | 81558    | 1.22612  | 48 |
| 13 | 73234    | 1.36549  | 75950    | 1.31666  | 78739    | 1.27001  | 81606    | 1.22539  | 47 |
| 14 | 73278    | 1.36466  | 75996    | 1.31586  | 78786    | 1.26925  | 81655    | 1.22467  | 46 |
| 15 | 73323    | 1.36383  | 76042    | 1.31507  | 78834    | 1.26849  | 81703    | 1.22394  | 45 |
| 16 | 73368    | 1.36300  | 76088    | 1.31427  | 78881    | 1.26774  | 81752    | 1.22321  | 44 |
| 17 | 73413    | 1.36217  | 76134    | 1.31348  | 78928    | 1.26698  | 81800    | 1.22249  | 43 |
| 18 | 73457    | 1.36133  | 76180    | 1.31269  | 78975    | 1.26622  | 81849    | 1.22176  | 42 |
| 19 | 73502    | 1.36051  | 76226    | 1.31190  | 79022    | 1.26546  | 81898    | 1.22104  | 41 |
| 20 | 73547    | 1.35968  | 76272    | 1.31110  | 79070    | 1.26471  | 81946    | 1.22031  | 40 |
| 21 | 73592    | 1.35885  | 76318    | 1.31031  | 79117    | 1.26395  | 81995    | 1.21959  | 39 |
| 22 | 73637    | 1.35802  | 76364    | 1.30952  | 79164    | 1.26319  | 82044    | 1.21886  | 38 |
| 23 | 73681    | 1.35719  | 76410    | 1.30873  | 79212    | 1.26244  | 82092    | 1.21814  | 37 |
| 24 | 73726    | 1.35637  | 76456    | 1.30795  | 79259    | 1.26169  | 82141    | 1.21742  | 36 |
| 25 | 73771    | 1.35554  | 76502    | 1.30716  | 79306    | 1.26093  | 82190    | 1.21670  | 35 |
| 26 | 73816    | 1.35472  | 76548    | 1.30637  | 79354    | 1.26018  | 82238    | 1.21598  | 34 |
| 27 | 73861    | 1.35389  | 76594    | 1.30558  | 79401    | 1.25943  | 82287    | 1.21526  | 33 |
| 28 | 73906    | 1.35307  | 76640    | 1.30480  | 79449    | 1.25867  | 82336    | 1.21454  | 32 |
| 29 | 73951    | 1.35224  | 76686    | 1.30401  | 79496    | 1.25792  | 82385    | 1.21382  | 31 |
| 30 | 73996    | 1.35142  | 76733    | 1.30323  | 79544    | 1.25717  | 82434    | 1.21310  | 30 |
| 31 | 74041    | 1.35060  | 76779    | 1.30244  | 79591    | 1.25642  | 82483    | 1.21238  | 29 |
| 32 | 74086    | 1.34978  | 76825    | 1.30166  | 79639    | 1.25567  | 82531    | 1.21166  | 28 |
| 33 | 74131    | 1.34896  | 76871    | 1.30087  | 79686    | 1.25492  | 82580    | 1.21094  | 27 |
| 34 | 74176    | 1.34814  | 76918    | 1.30009  | 79734    | 1.25417  | 82629    | 1.21023  | 26 |
| 35 | 74221    | 1.34732  | 76964    | 1.29931  | 79781    | 1.25343  | 82678    | 1.20951  | 25 |
| 36 | 74267    | 1.34650  | 77010    | 1.29853  | 79829    | 1.25268  | 82727    | 1.20879  | 24 |
| 37 | 74312    | 1.34568  | 77057    | 1.29775  | 79877    | 1.25193  | 82776    | 1.20808  | 23 |
| 38 | 74357    | 1.34487  | 77103    | 1.29696  | 79924    | 1.25118  | 82825    | 1.20736  | 22 |
| 39 | 74402    | 1.34405  | 77149    | 1.29618  | 79972    | 1.25044  | 82874    | 1.20665  | 21 |
| 40 | 74447    | 1.34323  | 77196    | 1.29541  | 80020    | 1.24969  | 82923    | 1.20593  | 20 |
| 41 | 74492    | 1.34242  | 77242    | 1.29463  | 80067    | 1.24895  | 82972    | 1.20522  | 19 |
| 42 | 74538    | 1.34160  | 77289    | 1.29385  | 80115    | 1.24820  | 83022    | 1.20451  | 18 |
| 43 | 74583    | 1.34079  | 77335    | 1.29307  | 80163    | 1.24746  | 83071    | 1.20379  | 17 |
| 44 | 74628    | 1.33998  | 77382    | 1.29229  | 80211    | 1.24672  | 83120    | 1.20308  | 16 |
| 45 | 74674    | 1.33916  | 77428    | 1.29152  | 80258    | 1.24597  | 83169    | 1.20237  | 15 |
| 46 | 74719    | 1.33835  | 77475    | 1.29074  | 80306    | 1.24523  | 83218    | 1.20166  | 14 |
| 47 | 74764    | 1.33754  | 77521    | 1.28997  | 80354    | 1.24449  | 83268    | 1.20095  | 13 |
| 48 | 74810    | 1.33673  | 77568    | 1.28919  | 80402    | 1.24375  | 83317    | 1.20024  | 12 |
| 49 | 74855    | 1.33592  | 77615    | 1.28842  | 80450    | 1.24301  | 83366    | 1.19953  | 11 |
| 50 | 74900    | 1.33511  | 77661    | 1.28764  | 80498    | 1.24227  | 83415    | 1.19882  | 10 |
| 51 | 74946    | 1.33430  | 77708    | 1.28687  | 80546    | 1.24153  | 83465    | 1.19811  | 9  |
| 52 | 74991    | 1.33349  | 77754    | 1.28610  | 80594    | 1.24079  | 83514    | 1.19740  | 8  |
| 53 | 75037    | 1.33268  | 77801    | 1.28533  | 80642    | 1.24005  | 83564    | 1.19669  | 7  |
| 54 | 75082    | 1.33187  | 77848    | 1.28456  | 80690    | 1.23931  | 83613    | 1.19599  | 6  |
| 55 | 75128    | 1.33107  | 77895    | 1.28379  | 80738    | 1.23858  | 83662    | 1.19528  | 5  |
| 56 | 75173    | 1.33026  | 77941    | 1.28302  | 80786    | 1.23784  | 83712    | 1.19457  | 4  |
| 57 | 75219    | 1.32946  | 77988    | 1.28225  | 80834    | 1.23710  | 83761    | 1.19387  | 3  |
| 58 | 75264    | 1.32865  | 78035    | 1.28148  | 80882    | 1.23637  | 83811    | 1.19316  | 2  |
| 59 | 75310    | 1.32785  | 78082    | 1.28071  | 80930    | 1.23563  | 83860    | 1.19246  | 1  |
| 60 | 75355    | 1.32704  | 78129    | 1.27994  | 80978    | 1.23490  | 83910    | 1.19175  | 0  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |
|    | 53°      |          | 52°      |          | 51°      |          | 50°      |          |    |

TABLE III. NATURAL TANGENTS AND COTANGENTS.

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| °  | 40°      |          | 41°      |          | 42°      |          | 43°      |          | °  |
|----|----------|----------|----------|----------|----------|----------|----------|----------|----|
|    | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  |    |
| 0  | 83910    | 1.19175  | 86929    | 1.15637  | 90040    | 1.11061  | 93252    | 1.07237  | 60 |
| 1  | 83960    | 1.19105  | 86980    | 1.14969  | 90093    | 1.10996  | 93306    | 1.07174  | 59 |
| 2  | 84009    | 1.19035  | 87031    | 1.14902  | 90146    | 1.10931  | 93360    | 1.07112  | 58 |
| 3  | 84059    | 1.18964  | 87082    | 1.14834  | 90199    | 1.10867  | 93415    | 1.07049  | 57 |
| 4  | 84108    | 1.18894  | 87133    | 1.14767  | 90251    | 1.10802  | 93469    | 1.06987  | 56 |
| 5  | 84158    | 1.18824  | 87184    | 1.14699  | 90304    | 1.10737  | 93524    | 1.06925  | 55 |
| 6  | 84208    | 1.18754  | 87236    | 1.14632  | 90357    | 1.10672  | 93578    | 1.06862  | 54 |
| 7  | 84258    | 1.18684  | 87287    | 1.14565  | 90410    | 1.10607  | 93633    | 1.06800  | 53 |
| 8  | 84307    | 1.18614  | 87338    | 1.14498  | 90463    | 1.10543  | 93688    | 1.06738  | 52 |
| 9  | 84357    | 1.18544  | 87389    | 1.14430  | 90516    | 1.10478  | 93742    | 1.06676  | 51 |
| 10 | 84407    | 1.18474  | 87441    | 1.14363  | 90569    | 1.10414  | 93797    | 1.06613  | 50 |
| 11 | 84457    | 1.18404  | 87492    | 1.14296  | 90621    | 1.10349  | 93852    | 1.06551  | 49 |
| 12 | 84507    | 1.18334  | 87543    | 1.14229  | 90674    | 1.10285  | 93906    | 1.06489  | 48 |
| 13 | 84556    | 1.18264  | 87595    | 1.14162  | 90727    | 1.10220  | 93961    | 1.06427  | 47 |
| 14 | 84606    | 1.18194  | 87646    | 1.14095  | 90781    | 1.10156  | 94016    | 1.06365  | 46 |
| 15 | 84656    | 1.18125  | 87698    | 1.14028  | 90834    | 1.10091  | 94071    | 1.06303  | 45 |
| 16 | 84706    | 1.18055  | 87749    | 1.13961  | 90887    | 1.10027  | 94125    | 1.06241  | 44 |
| 17 | 84756    | 1.17986  | 87801    | 1.13894  | 90940    | 1.09963  | 94180    | 1.06179  | 43 |
| 18 | 84806    | 1.17916  | 87852    | 1.13828  | 90993    | 1.09899  | 94235    | 1.06117  | 42 |
| 19 | 84856    | 1.17846  | 87904    | 1.13761  | 91046    | 1.09834  | 94290    | 1.06055  | 41 |
| 20 | 84906    | 1.17777  | 87955    | 1.13694  | 91099    | 1.09770  | 94345    | 1.05994  | 40 |
| 21 | 84956    | 1.17708  | 88007    | 1.13627  | 91153    | 1.09706  | 94400    | 1.05932  | 39 |
| 22 | 85006    | 1.17638  | 88059    | 1.13561  | 91206    | 1.09642  | 94455    | 1.05870  | 38 |
| 23 | 85057    | 1.17569  | 88110    | 1.13494  | 91259    | 1.09578  | 94510    | 1.05809  | 37 |
| 24 | 85107    | 1.17500  | 88162    | 1.13428  | 91313    | 1.09514  | 94565    | 1.05747  | 36 |
| 25 | 85157    | 1.17430  | 88214    | 1.13361  | 91366    | 1.09450  | 94620    | 1.05685  | 35 |
| 26 | 85207    | 1.17361  | 88265    | 1.13295  | 91419    | 1.09386  | 94676    | 1.05624  | 34 |
| 27 | 85257    | 1.17292  | 88317    | 1.13228  | 91473    | 1.09322  | 94731    | 1.05562  | 33 |
| 28 | 85307    | 1.17223  | 88369    | 1.13162  | 91526    | 1.09258  | 94786    | 1.05501  | 32 |
| 29 | 85358    | 1.17154  | 88421    | 1.13096  | 91580    | 1.09195  | 94841    | 1.05439  | 31 |
| 30 | 85408    | 1.17085  | 88473    | 1.13029  | 91633    | 1.09131  | 94896    | 1.05378  | 30 |
| 31 | 85458    | 1.17016  | 88524    | 1.12963  | 91687    | 1.09067  | 94952    | 1.05317  | 29 |
| 32 | 85509    | 1.16947  | 88576    | 1.12897  | 91740    | 1.09003  | 95007    | 1.05255  | 28 |
| 33 | 85559    | 1.16878  | 88628    | 1.12831  | 91794    | 1.08939  | 95062    | 1.05194  | 27 |
| 34 | 85609    | 1.16809  | 88680    | 1.12765  | 91847    | 1.08876  | 95118    | 1.05133  | 26 |
| 35 | 85660    | 1.16741  | 88732    | 1.12699  | 91901    | 1.08813  | 95173    | 1.05072  | 25 |
| 36 | 85710    | 1.16672  | 88784    | 1.12633  | 91955    | 1.08749  | 95229    | 1.05010  | 24 |
| 37 | 85761    | 1.16603  | 88836    | 1.12567  | 92008    | 1.08686  | 95284    | 1.04949  | 23 |
| 38 | 85811    | 1.16535  | 88888    | 1.12501  | 92062    | 1.08622  | 95340    | 1.04888  | 22 |
| 39 | 85862    | 1.16466  | 88940    | 1.12435  | 92116    | 1.08559  | 95395    | 1.04827  | 21 |
| 40 | 85912    | 1.16398  | 88992    | 1.12369  | 92170    | 1.08496  | 95451    | 1.04766  | 20 |
| 41 | 85963    | 1.16329  | 89045    | 1.12303  | 92223    | 1.08432  | 95506    | 1.04705  | 19 |
| 42 | 86014    | 1.16261  | 89097    | 1.12238  | 92277    | 1.08369  | 95562    | 1.04644  | 18 |
| 43 | 86064    | 1.16192  | 89149    | 1.12172  | 92331    | 1.08306  | 95618    | 1.04583  | 17 |
| 44 | 86115    | 1.16124  | 89201    | 1.12106  | 92385    | 1.08243  | 95673    | 1.04522  | 16 |
| 45 | 86166    | 1.16056  | 89253    | 1.12041  | 92439    | 1.08179  | 95729    | 1.04461  | 15 |
| 46 | 86216    | 1.15987  | 89306    | 1.11975  | 92493    | 1.08116  | 95785    | 1.04401  | 14 |
| 47 | 86267    | 1.15919  | 89358    | 1.11909  | 92547    | 1.08053  | 95841    | 1.04340  | 13 |
| 48 | 86318    | 1.15851  | 89410    | 1.11844  | 92601    | 1.07990  | 95897    | 1.04279  | 12 |
| 49 | 86368    | 1.15783  | 89463    | 1.11778  | 92655    | 1.07927  | 95952    | 1.04218  | 11 |
| 50 | 86419    | 1.15715  | 89515    | 1.11713  | 92709    | 1.07864  | 96008    | 1.04158  | 10 |
| 51 | 86470    | 1.15647  | 89567    | 1.11648  | 92763    | 1.07801  | 96064    | 1.04097  | 9  |
| 52 | 86521    | 1.15579  | 89620    | 1.11582  | 92817    | 1.07738  | 96120    | 1.04036  | 8  |
| 53 | 86572    | 1.15511  | 89672    | 1.11517  | 92872    | 1.07676  | 96176    | 1.03976  | 7  |
| 54 | 86623    | 1.15443  | 89725    | 1.11452  | 92926    | 1.07613  | 96232    | 1.03915  | 6  |
| 55 | 86674    | 1.15375  | 89777    | 1.11387  | 92980    | 1.07550  | 96288    | 1.03855  | 5  |
| 56 | 86725    | 1.15308  | 89830    | 1.11321  | 93034    | 1.07487  | 96344    | 1.03794  | 4  |
| 57 | 86776    | 1.15240  | 89883    | 1.11256  | 93088    | 1.07425  | 96400    | 1.03734  | 3  |
| 58 | 86827    | 1.15172  | 89935    | 1.11191  | 93143    | 1.07362  | 96457    | 1.03674  | 2  |
| 59 | 86878    | 1.15104  | 89988    | 1.11126  | 93197    | 1.07299  | 96513    | 1.03613  | 1  |
| 60 | 86929    | 1.15037  | 90040    | 1.11061  | 93252    | 1.07237  | 96569    | 1.03553  | 0  |
| °  | 49°      |          | 48°      |          | 47°      |          | 46°      |          | °  |
|    | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. | Cotang.  | Tangent. |    |

| 44° |          |          | 44° |          |          |
|-----|----------|----------|-----|----------|----------|
|     | Tangent. | Cotang.  |     | Tangent. | Cotang.  |
| 0   | 0.6569   | 1.03553  | 60  | 0.8327   | 1.01702  |
| 1   | 0.6625   | 1.03493  | 59  | 0.8384   | 1.01642  |
| 2   | 0.6681   | 1.03433  | 58  | 0.8441   | 1.01583  |
| 3   | 0.6738   | 1.03372  | 57  | 0.8499   | 1.01524  |
| 4   | 0.6794   | 1.03312  | 56  | 0.8556   | 1.01465  |
| 5   | 0.6850   | 1.03252  | 55  | 0.8613   | 1.01406  |
| 6   | 0.6907   | 1.03192  | 54  | 0.8671   | 1.01347  |
| 7   | 0.6963   | 1.03132  | 53  | 0.8728   | 1.01288  |
| 8   | 0.7020   | 1.03072  | 52  | 0.8786   | 1.01229  |
| 9   | 0.7076   | 1.03012  | 51  | 0.8843   | 1.01170  |
| 10  | 0.7133   | 1.02952  | 50  | 0.8901   | 1.01112  |
| 11  | 0.7189   | 1.02892  | 49  | 0.8958   | 1.01053  |
| 12  | 0.7246   | 1.02832  | 48  | 0.9016   | 1.00994  |
| 13  | 0.7302   | 1.02772  | 47  | 0.9073   | 1.00935  |
| 14  | 0.7359   | 1.02713  | 46  | 0.9131   | 1.00876  |
| 15  | 0.7416   | 1.02653  | 45  | 0.9189   | 1.00818  |
| 16  | 0.7472   | 1.02593  | 44  | 0.9247   | 1.00759  |
| 17  | 0.7529   | 1.02533  | 43  | 0.9304   | 1.00701  |
| 18  | 0.7586   | 1.02474  | 42  | 0.9362   | 1.00642  |
| 19  | 0.7643   | 1.02414  | 41  | 0.9420   | 1.00583  |
| 20  | 0.7700   | 1.02355  | 40  | 0.9478   | 1.00525  |
| 21  | 0.7756   | 1.02295  | 39  | 0.9536   | 1.00467  |
| 22  | 0.7813   | 1.02236  | 38  | 0.9594   | 1.00408  |
| 23  | 0.7870   | 1.02176  | 37  | 0.9652   | 1.00350  |
| 24  | 0.7927   | 1.02117  | 36  | 0.9710   | 1.00291  |
| 25  | 0.7984   | 1.02057  | 35  | 0.9768   | 1.00233  |
| 26  | 0.8041   | 1.01998  | 34  | 0.9826   | 1.00175  |
| 27  | 0.8098   | 1.01939  | 33  | 0.9884   | 1.00116  |
| 28  | 0.8155   | 1.01879  | 32  | 0.9942   | 1.00058  |
| 29  | 0.8213   | 1.01820  | 31  | Unit.    | Unit.    |
| 30  | 0.8270   | 1.01761  | 30  |          |          |
| 45° |          |          | 45° |          |          |
|     | Cotang.  | Tangent. |     | Cotang.  | Tangent. |

## TABLE OF CONSTANTS.

Base of Napier's system of logarithms =  $\epsilon = 2.718281828459$

Mod. of common syst. of logarithms = .... com. log.  $\epsilon = M = 0.434294481903$

Ratio of circumference to diameter of a circle = .....  $\pi = 3.141592653590$

log.  $\pi = 0.497149872694$

$\pi^2 = 9.869604401089$  .....  $\sqrt{\pi} = 1.772453850906$

Arc of same length as radius = .....  $180^\circ + \pi = 10800' + \pi = 648000'' + \pi$

$180^\circ + \pi = 57^\circ.2957795130$ , ..... log. =  $1.758122632409$

$10800' + \pi = 3437'.7467707849$ , ..... log. =  $3.536273882793$

$648000'' + \pi = 206264''.8062470964$ , ..... log. =  $5.314425133476$

Tropical year = 365d. 5h. 48m. 47s. 588 = 365d. 242217456, log. =  $2.5625810$

Sidereal year = 365d. 6h. 9m. 10s. 742 = 365d. 256374332, log. =  $2.5625978$

24h. sol. t. = 24h. 3m. 56s. 555335 sid. t. = 24h.  $\times 1.00273791$ , log.  $1.002 = 0.0011874$

24h. sid. t. = 24h.  $-(3m. 55s. 90944)$  sol. t. = 24h.  $\times 0.9972696$ , log.  $0.997 = 0.9988126$

British imperial gallon = 277.274 cubic inches, ..... log. =  $2.4429091$

Length of sec. pend., in inches, at London, 39.13929; Paris, 39.1285; New York, 39.1285.

French metre = 3.2808992 English feet = 39.3707904 inches.

1 cubic inch of water (bar. 30 inches, Fahr. therm. 62°) = 252.458 Troy grains.



A TABLE OF MEAN REFRACTIONS IN DECLINATION.

85

| Hour Angle.           | Refraction in Declination. |       |       |      |      |      |       |       |       |
|-----------------------|----------------------------|-------|-------|------|------|------|-------|-------|-------|
|                       | For Latitude 15°.          |       |       |      |      |      |       |       |       |
|                       | + 20°                      | + 15° | + 10° | + 5° | 0°   | - 5° | - 10° | - 15° | - 20° |
| 0 h.                  | -05"                       | 0"    | +05"  | 10"  | 15"  | 21"  | 27"   | 33"   | 40"   |
| 1                     | -03                        | +02   | 07    | 12   | 18   | 23   | 29    | 36    | 43    |
| 2                     | +01                        | 05    | 11    | 16   | 22   | 28   | 34    | 41    | 49    |
| 3                     | 08                         | 12    | 19    | 24   | 30   | 37   | 44    | 53    | 1'04  |
| 4                     | 29                         | 34    | 41    | 49   | 59   | 1'10 | 1'24  | 1'43  | 2'08  |
| For Latitude 17° 30'. |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | -02"                       | +02"  | 08"   | 13"  | 18"  | 24"  | 30"   | 36"   | 44"   |
| 1                     | 0                          | 05    | 10    | 15   | 21   | 27   | 33    | 40    | 48    |
| 2                     | +02                        | 10    | 15    | 21   | 27   | 33   | 40    | 48    | 57    |
| 3                     | 13                         | 18    | 23    | 29   | 35   | 43   | 51    | 1'01  | 1'13  |
| 4                     | 34                         | 41    | 49    | 58   | 1'10 | 1'23 | 1'41  | 2'06  | 2'42  |
| For Latitude 20°.     |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | 0"                         | 05"   | 10"   | 15"  | 21"  | 27"  | 33"   | 40"   | 48"   |
| 1                     | 03                         | 07    | 13    | 18   | 24   | 30   | 36    | 44    | 52    |
| 2                     | 06                         | 13    | 18    | 24   | 30   | 36   | 44    | 52    | 1'02  |
| 3                     | 17                         | 22    | 28    | 35   | 42   | 50   | 1'00  | 1'11  | 1'26  |
| 4                     | 39                         | 47    | 57    | 1'07 | 1'20 | 1'37 | 2'00  | 2'32  | 3'25  |
| For Latitude 22° 30'. |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | 02"                        | 08"   | 13"   | 18"  | 24"  | 30"  | 36"   | 44"   | 52"   |
| 1                     | 06                         | 11    | 15    | 21   | 27   | 33   | 40    | 48    | 57    |
| 2                     | 11                         | 15    | 21    | 27   | 33   | 40   | 48    | 57    | 1'08  |
| 3                     | 20                         | 26    | 32    | 39   | 46   | 56   | 1'07  | 1'19  | 1'37  |
| 4                     | 45                         | 53    | 1'03  | 1'16 | 1'31 | 1'52 | 2'21  | 3'07  | 4'28  |
| For Latitude 25°.     |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | 05"                        | 10"   | 15"   | 21"  | 27"  | 33"  | 40"   | 48"   | 57"   |
| 1                     | 08                         | 14    | 19    | 25   | 31   | 38   | 46    | 54    | 1'05  |
| 2                     | 12                         | 18    | 24    | 30   | 37   | 44   | 53    | 1'04  | 1'18  |
| 3                     | 23                         | 29    | 35    | 45   | 53   | 1'03 | 1'16  | 1'31  | 1'52  |
| 4                     | 49                         | 59    | 1'10  | 1'24 | 1'50 | 2'07 | 2'44  | 3'46  | 5'43  |
| For Latitude 27° 30'. |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | 08"                        | 13"   | 18"   | 24"  | 30"  | 36"  | 44"   | 52"   | 1'02" |
| 1                     | 11                         | 16    | 22    | 28   | 34   | 41   | 49    | 1'00  | 1'10  |
| 2                     | 17                         | 22    | 28    | 35   | 42   | 50   | 1'00  | 1'11  | 1'26  |
| 3                     | 28                         | 35    | 42    | 50   | 1'00 | 1'11 | 1'26  | 1'43  | 2'09  |
| 4                     | 54                         | 1'05  | 1'18  | 1'34 | 1'54 | 2'24 | 3'11  | 4'38  | 8'15  |
| For Latitude 30°.     |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | 10"                        | 15"   | 21"   | 27"  | 33"  | 40"  | 48"   | 57"   | 1'08" |
| 1                     | 14                         | 19    | 25    | 31   | 38   | 46   | 54    | 1'05  | 1'18  |
| 2                     | 20                         | 26    | 32    | 39   | 47   | 55   | 1'06  | 1'19  | 1'36  |
| 3                     | 32                         | 39    | 46    | 52   | 1'06 | 1'19 | 1'35  | 1'57  | 2'29  |
| 4                     | 1'00                       | 1'10  | 1'24  | 1'52 | 2'07 | 2'44 | 3'46  | 5'43  | 13'06 |
| For Latitude 32° 30'. |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | 13"                        | 18"   | 24"   | 30"  | 36"  | 44"  | 52"   | 1'02" | 1'14" |
| 1                     | 17                         | 22    | 28    | 35   | 42   | 50   | 1'00  | 1'11  | 1'26  |
| 2                     | 23                         | 29    | 35    | 43   | 51   | 1'01 | 1'13  | 1'28  | 1'47  |
| 3                     | 35                         | 43    | 51    | 1'01 | 1'13 | 1'27 | 1'46  | 2'13  | 2'54  |
| 4                     | 1'03                       | 1'15  | 1'31  | 1'53 | 2'20 | 3'05 | 4'25  | 7'36  |       |
| For Latitude 35°.     |                            |       |       |      |      |      |       |       |       |
| 0 h.                  | 15"                        | 21"   | 27"   | 33"  | 40"  | 48"  | 57"   | 1'08" | 1'21" |
| 1                     | 20                         | 25    | 32    | 38   | 46   | 55   | 1'05  | 1'18  | 1'35  |
| 2                     | 26                         | 33    | 39    | 47   | 56   | 1'07 | 1'21  | 1'38  | 2'00  |
| 3                     | 39                         | 47    | 56    | 1'07 | 1'20 | 1'36 | 1'59  | 2'32  | 3'25  |
| 4                     | 1'07                       | 1'20  | 1'38  | 2'00 | 2'34 | 3'29 | 5'14  | 10'16 |       |

## REFRACTION IN DECLINATION.

| HOUR<br>ANGLE.        | FOR LATITUDE 37° 30'. |       |       |       |       |       |       |       |       |
|-----------------------|-----------------------|-------|-------|-------|-------|-------|-------|-------|-------|
|                       | + 20°                 | + 15° | + 10° | + 5°  | 0°    | - 5°  | - 10° | - 15° | - 20° |
| 0 h.                  | 18"                   | 24"   | 30"   | 36"   | 44"   | 52"   | 1'02" | 1'14" | 1'29" |
| 1                     | 22                    | 28    | 35    | 42    | 50    | 1'00  | 1'12  | 1'26  | 1'45  |
| 2                     | 29                    | 36    | 43    | 52    | 1'02  | 1'14  | 1'29  | 1'49  | 2'16  |
| 3                     | 43                    | 51    | 1'01  | 1'13  | 1'27  | 1'49  | 2'14  | 2'54  | 4'05  |
| 4                     | 1'11                  | 1'26  | 1'54  | 2'10  | 2'49  | 3'55  | 6'15  | 14'58 |       |
| FOR LATITUDE 40°.     |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 21"                   | 27"   | 33"   | 40"   | 48"   | 57"   | 1'08" | 1'21" | 1'39" |
| 1                     | 25                    | 32    | 39    | 46    | 52    | 1'06  | 1'19  | 1'35  | 1'57  |
| 2                     | 33                    | 40    | 48    | 57    | 1'08  | 1'21  | 1'38  | 2'02  | 2'36  |
| 3                     | 47                    | 55    | 1'06  | 1'19  | 1'36  | 1'58  | 2'30  | 3'21  | 4'59  |
| 4                     | 1'15                  | 1'31  | 1'51  | 2'20  | 3'05  | 4'25  | 7'34  | 25'18 |       |
| FOR LATITUDE 42° 30'. |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 24"                   | 30"   | 36"   | 44"   | 52"   | 1'02" | 1'14" | 1'29" | 1'49" |
| 1                     | 28                    | 35    | 39    | 50    | 1'00  | 1'12  | 1'26  | 1'45  | 2'11  |
| 2                     | 36                    | 43    | 52    | 1'02  | 1'13  | 1'29  | 1'49  | 2'17  | 2'59  |
| 3                     | 50                    | 1'00  | 1'11  | 1'26  | 1'44  | 2'10  | 2'49  | 3'55  | 6'16  |
| 4                     | 1'16                  | 1'36  | 1'58  | 2'30  | 3'22  | 5'00  | 9'24  |       |       |
| FOR LATITUDE 45°.     |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 27"                   | 33"   | 40"   | 48"   | 57"   | 1'08" | 1'21" | 1'39" | 2'02" |
| 1                     | 32                    | 39    | 46    | 52    | 1'06  | 1'19  | 1'35  | 1'57  | 2'29  |
| 2                     | 40                    | 47    | 56    | 1'07  | 1'21  | 1'38  | 2'00  | 2'34  | 3'29  |
| 3                     | 54                    | 1'04  | 1'16  | 1'33  | 1'54  | 2'24  | 3'11  | 4'38  | 8'15  |
| 4                     | 1'23                  | 1'41  | 2'05  | 2'41  | 3'40  | 5'40  | 12'02 |       |       |
| FOR LATITUDE 47° 30'. |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 30"                   | 36"   | 44"   | 52"   | 1'02" | 1'14" | 1'29" | 1'49" | 2'18" |
| 1                     | 35                    | 42    | 50    | 1'00  | 1'12  | 1'26  | 1'45  | 2'01  | 2'51  |
| 2                     | 43                    | 51    | 1'01  | 1'13  | 1'28  | 1'47  | 2'15  | 2'56  | 4'08  |
| 3                     | 56                    | 1'09  | 1'23  | 1'40  | 2'05  | 2'40  | 3'39  | 5'37  | 11'18 |
| 4                     | 1'27                  | 1'46  | 2'12  | 2'52  | 4'01  | 6'30  | 16'19 |       |       |
| FOR LATITUDE 50°.     |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 33"                   | 40"   | 48"   | 57"   | 1'08" | 1'21" | 1'39" | 2'02" | 2'36" |
| 1                     | 38                    | 46    | 55    | 1'06  | 1'18  | 1'35  | 1'57  | 2'28  | 3'19  |
| 2                     | 47                    | 56    | 1'06  | 1'19  | 1'36  | 2'00  | 2'31  | 3'23  | 5'02  |
| 3                     | 1'08                  | 1'14  | 1'29  | 1'48  | 2'16  | 2'58  | 4'18  | 6'59  | 19'47 |
| 4                     | 1'30                  | 1'51  | 2'29  | 3'04  | 4'22  | 7'28  | 24'10 |       |       |
| FOR LATITUDE 52° 30'. |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 36"                   | 44"   | 52"   | 1'02" | 1'14" | 1'29" | 1'49" | 2'18" | 3'05" |
| 1                     | 43                    | 50    | 59    | 1'11  | 1'26  | 1'42  | 2'23  | 2'40  | 3'55  |
| 2                     | 50                    | 1'00  | 1'11  | 1'26  | 1'45  | 2'11  | 2'51  | 2'58  | 6'22  |
| 3                     | 1'05                  | 1'18  | 1'35  | 2'10  | 2'28  | 3'19  | 4'53  | 8'42  |       |
| 4                     | 1'34                  | 1'56  | 2'27  | 3'16  | 4'47  | 8'52  |       |       |       |
| FOR LATITUDE 55°.     |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 40"                   | 48"   | 57"   | 1'08" | 1'21" | 1'39" | 2'02" | 2'36" | 3'33" |
| 1                     | 46                    | 55    | 1'05  | 1'18  | 1'34  | 1'56  | 2'30  | 3'15  | 4'47  |
| 2                     | 55                    | 1'06  | 1'19  | 1'35  | 1'58  | 2'30  | 3'21  | 4'58  | 9'19  |
| 3                     | 1'10                  | 1'23  | 1'42  | 2'06  | 2'43  | 3'44  | 5'49  | 12'41 |       |
| 4                     | 1'37                  | 2'01  | 2'34  | 3'28  | 5'15  | 10'18 |       |       |       |
| FOR LATITUDE 57° 30'. |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 44"                   | 52"   | 1'02" | 1'14" | 1'29" | 1'49" | 2'18" | 3'05" | 4'37" |
| 1                     | 50                    | 59    | 1'11  | 1'25  | 1'43  | 2'09  | 2'47  | 3'51  | 6'04  |
| 2                     | 58                    | 1'10  | 1'24  | 1'42  | 2'07  | 2'43  | 3'45  | 5'50  | 12'47 |
| 3                     | 1'11                  | 1'25  | 1'43  | 2'10  | 2'50  | 3'55  | 6'14  | 14'49 |       |
| 4                     | 1'41                  | 2'06  | 2'42  | 3'42  | 5'46  | 12'26 |       |       |       |
| FOR LATITUDE 60°.     |                       |       |       |       |       |       |       |       |       |
| 0 h.                  | 48"                   | 57"   | 1'08" | 1'21" | 1'39" | 2'02" | 2'36" | 3'33" | 5'23" |
| 1                     | 54                    | 1'04  | 1'17  | 1'33  | 1'54  | 2'24  | 3'12  | 4'38  | 8'15  |
| 2                     | 1'03                  | 1'15  | 1'30  | 1'51  | 2'20  | 3'04  | 4'24  | 7'31  | 24'44 |
| 3                     | 1'18                  | 1'34  | 1'56  | 2'28  | 3'18  | 4'50  | 8'53  |       |       |
| 4                     | 1'45                  | 2'11  | 2'50  | 3'57  | 6'21  | 15'32 |       |       |       |

**TABLES**  
**FOR OBTAINING**  
**HORIZONTAL DISTANCES**  
**AND**  
**DIFFERENCES OF LEVEL,**  
**FROM**  
**STADIA READINGS.**



**TABLES**  
**FOR OBTAINING**  
**HORIZONTAL DISTANCES**  
**AND**  
**DIFFERENCES OF LEVEL,**  
**FROM**  
**STADIA READINGS.**



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 00 |
| 0.0003 | 0.0006 | 0.0009 | 0.0012 | 0.0015 | 0.0017 | 0.0020 | 0.0023 | 0.0026 | 0.0004 | 01 |
| 0.0006 | 0.0012 | 0.0017 | 0.0023 | 0.0029 | 0.0035 | 0.0041 | 0.0046 | 0.0052 | 0.0008 | 02 |
| 0.0009 | 0.0017 | 0.0026 | 0.0035 | 0.0044 | 0.0052 | 0.0061 | 0.0070 | 0.0078 | 0.0012 | 03 |
| 0.0012 | 0.0023 | 0.0035 | 0.0046 | 0.0058 | 0.0070 | 0.0081 | 0.0093 | 0.0105 | 0.0016 | 04 |
| 0.0015 | 0.0029 | 0.0044 | 0.0058 | 0.0073 | 0.0087 | 0.0102 | 0.0116 | 0.0131 | 0.0020 | 05 |
| 0.0017 | 0.0035 | 0.0052 | 0.0070 | 0.0087 | 0.0105 | 0.0122 | 0.0139 | 0.0157 | 0.0024 | 06 |
| 0.0020 | 0.0041 | 0.0061 | 0.0081 | 0.0102 | 0.0122 | 0.0142 | 0.0163 | 0.0183 | 0.0029 | 07 |
| 0.0023 | 0.0046 | 0.0070 | 0.0093 | 0.0116 | 0.0139 | 0.0163 | 0.0186 | 0.0209 | 0.0033 | 08 |
| 0.0026 | 0.0052 | 0.0078 | 0.0105 | 0.0131 | 0.0157 | 0.0183 | 0.0209 | 0.0235 | 0.0037 | 09 |
| 0.0029 | 0.0058 | 0.0087 | 0.0116 | 0.0145 | 0.0174 | 0.0203 | 0.0232 | 0.0261 | 0.0041 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0032 | 0.0064 | 0.0096 | 0.0128 | 0.0160 | 0.0192 | 0.0224 | 0.0256 | 0.0288 | 0.0045 | 11 |
| 0.0035 | 0.0070 | 0.0105 | 0.0139 | 0.0174 | 0.0209 | 0.0244 | 0.0279 | 0.0314 | 0.0049 | 12 |
| 0.0038 | 0.0076 | 0.0113 | 0.0151 | 0.0189 | 0.0227 | 0.0264 | 0.0302 | 0.0340 | 0.0053 | 13 |
| 0.0041 | 0.0081 | 0.0122 | 0.0163 | 0.0203 | 0.0244 | 0.0285 | 0.0325 | 0.0366 | 0.0057 | 14 |
| 0.0044 | 0.0087 | 0.0131 | 0.0174 | 0.0218 | 0.0261 | 0.0305 | 0.0349 | 0.0392 | 0.0061 | 15 |
| 0.0046 | 0.0093 | 0.0139 | 0.0186 | 0.0232 | 0.0279 | 0.0325 | 0.0372 | 0.0418 | 0.0065 | 16 |
| 0.0049 | 0.0099 | 0.0148 | 0.0198 | 0.0247 | 0.0296 | 0.0346 | 0.0395 | 0.0444 | 0.0069 | 17 |
| 0.0052 | 0.0105 | 0.0157 | 0.0209 | 0.0261 | 0.0314 | 0.0366 | 0.0418 | 0.0471 | 0.0073 | 18 |
| 0.0055 | 0.0110 | 0.0166 | 0.0221 | 0.0276 | 0.0331 | 0.0386 | 0.0442 | 0.0497 | 0.0077 | 19 |
| 0.0058 | 0.0116 | 0.0174 | 0.0232 | 0.0290 | 0.0349 | 0.0407 | 0.0465 | 0.0523 | 0.0081 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0061 | 0.0122 | 0.0183 | 0.0244 | 0.0305 | 0.0366 | 0.0427 | 0.0488 | 0.0549 | 0.0086 | 21 |
| 0.0064 | 0.0128 | 0.0192 | 0.0256 | 0.0320 | 0.0383 | 0.0447 | 0.0511 | 0.0575 | 0.0090 | 22 |
| 0.0067 | 0.0134 | 0.0200 | 0.0267 | 0.0334 | 0.0401 | 0.0468 | 0.0534 | 0.0601 | 0.0094 | 23 |
| 0.0070 | 0.0139 | 0.0209 | 0.0279 | 0.0349 | 0.0418 | 0.0488 | 0.0558 | 0.0627 | 0.0098 | 24 |
| 0.0073 | 0.0145 | 0.0218 | 0.0290 | 0.0363 | 0.0436 | 0.0508 | 0.0581 | 0.0654 | 0.0102 | 25 |
| 0.0076 | 0.0151 | 0.0227 | 0.0302 | 0.0378 | 0.0453 | 0.0529 | 0.0604 | 0.0680 | 0.0106 | 26 |
| 0.0078 | 0.0157 | 0.0235 | 0.0314 | 0.0392 | 0.0471 | 0.0549 | 0.0627 | 0.0706 | 0.0110 | 27 |
| 0.0081 | 0.0163 | 0.0244 | 0.0325 | 0.0407 | 0.0488 | 0.0569 | 0.0651 | 0.0732 | 0.0114 | 28 |
| 0.0084 | 0.0168 | 0.0253 | 0.0337 | 0.0421 | 0.0505 | 0.0590 | 0.0674 | 0.0758 | 0.0118 | 29 |
| 0.0087 | 0.0174 | 0.0261 | 0.0349 | 0.0436 | 0.0523 | 0.0610 | 0.0697 | 0.0784 | 0.0122 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0090 | 0.0180 | 0.0270 | 0.0360 | 0.0450 | 0.0540 | 0.0630 | 0.0720 | 0.0810 | 0.0126 | 31 |
| 0.0093 | 0.0186 | 0.0279 | 0.0372 | 0.0465 | 0.0558 | 0.0651 | 0.0744 | 0.0837 | 0.0130 | 32 |
| 0.0096 | 0.0192 | 0.0288 | 0.0383 | 0.0479 | 0.0575 | 0.0671 | 0.0767 | 0.0863 | 0.0134 | 33 |
| 0.0099 | 0.0198 | 0.0296 | 0.0395 | 0.0494 | 0.0593 | 0.0691 | 0.0790 | 0.0889 | 0.0138 | 34 |
| 0.0102 | 0.0203 | 0.0305 | 0.0407 | 0.0508 | 0.0610 | 0.0712 | 0.0813 | 0.0915 | 0.0143 | 35 |
| 0.0105 | 0.0209 | 0.0314 | 0.0418 | 0.0523 | 0.0627 | 0.0732 | 0.0836 | 0.0941 | 0.0147 | 36 |
| 0.0107 | 0.0215 | 0.0322 | 0.0430 | 0.0537 | 0.0645 | 0.0752 | 0.0860 | 0.0967 | 0.0151 | 37 |
| 0.0110 | 0.0221 | 0.0331 | 0.0441 | 0.0552 | 0.0662 | 0.0773 | 0.0883 | 0.0993 | 0.0155 | 38 |
| 0.0113 | 0.0227 | 0.0340 | 0.0453 | 0.0566 | 0.0680 | 0.0793 | 0.0906 | 0.1019 | 0.0159 | 39 |
| 0.0116 | 0.0232 | 0.0349 | 0.0465 | 0.0581 | 0.0697 | 0.0813 | 0.0929 | 0.1046 | 0.0163 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0119 | 0.0238 | 0.0357 | 0.0476 | 0.0595 | 0.0715 | 0.0834 | 0.0953 | 0.1072 | 0.0167 | 41 |
| 0.0122 | 0.0244 | 0.0366 | 0.0488 | 0.0610 | 0.0732 | 0.0854 | 0.0976 | 0.1098 | 0.0171 | 42 |
| 0.0125 | 0.0250 | 0.0375 | 0.0500 | 0.0624 | 0.0749 | 0.0874 | 0.0999 | 0.1124 | 0.0175 | 43 |
| 0.0128 | 0.0256 | 0.0383 | 0.0511 | 0.0639 | 0.0767 | 0.0895 | 0.1022 | 0.1150 | 0.0179 | 44 |
| 0.0131 | 0.0261 | 0.0392 | 0.0523 | 0.0654 | 0.0784 | 0.0915 | 0.1046 | 0.1176 | 0.0183 | 45 |
| 0.0134 | 0.0267 | 0.0401 | 0.0534 | 0.0668 | 0.0802 | 0.0935 | 0.1069 | 0.1202 | 0.0187 | 46 |
| 0.0137 | 0.0273 | 0.0410 | 0.0546 | 0.0683 | 0.0819 | 0.0955 | 0.1092 | 0.1229 | 0.0191 | 47 |
| 0.0139 | 0.0279 | 0.0418 | 0.0558 | 0.0697 | 0.0836 | 0.0976 | 0.1115 | 0.1255 | 0.0195 | 48 |
| 0.0142 | 0.0285 | 0.0427 | 0.0569 | 0.0712 | 0.0854 | 0.0996 | 0.1138 | 0.1281 | 0.0200 | 49 |
| 0.0145 | 0.0290 | 0.0436 | 0.0581 | 0.0726 | 0.0871 | 0.1017 | 0.1162 | 0.1307 | 0.0204 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0148 | 0.0296 | 0.0444 | 0.0592 | 0.0741 | 0.0889 | 0.1037 | 0.1185 | 0.1333 | 0.0208 | 51 |
| 0.0151 | 0.0302 | 0.0453 | 0.0604 | 0.0755 | 0.0906 | 0.1057 | 0.1208 | 0.1359 | 0.0212 | 52 |
| 0.0154 | 0.0308 | 0.0462 | 0.0616 | 0.0770 | 0.0923 | 0.1077 | 0.1231 | 0.1385 | 0.0216 | 53 |
| 0.0157 | 0.0314 | 0.0470 | 0.0627 | 0.0784 | 0.0941 | 0.1098 | 0.1254 | 0.1411 | 0.0220 | 54 |
| 0.0160 | 0.0319 | 0.0479 | 0.0639 | 0.0799 | 0.0958 | 0.1118 | 0.1278 | 0.1437 | 0.0224 | 55 |
| 0.0163 | 0.0325 | 0.0488 | 0.0650 | 0.0813 | 0.0976 | 0.1138 | 0.1301 | 0.1463 | 0.0228 | 56 |
| 0.0166 | 0.0331 | 0.0497 | 0.0662 | 0.0828 | 0.0993 | 0.1159 | 0.1324 | 0.1490 | 0.0232 | 57 |
| 0.0168 | 0.0337 | 0.0505 | 0.0674 | 0.0842 | 0.1011 | 0.1179 | 0.1348 | 0.1516 | 0.0236 | 58 |
| 0.0171 | 0.0343 | 0.0514 | 0.0685 | 0.0857 | 0.1028 | 0.1199 | 0.1371 | 0.1542 | 0.0240 | 59 |
| 0.0174 | 0.0349 | 0.0523 | 0.0697 | 0.0871 | 0.1046 | 0.1220 | 0.1394 | 0.1568 | 0.0244 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9983 | 1.9966 | 2.9949 | 3.9932 | 4.9915 | 5.9898 | 6.9881 | 7.9864 | 8.9847 | 1.3998 |
| 01 | 0.9983 | 1.9966 | 2.9949 | 3.9931 | 4.9914 | 5.9897 | 6.9880 | 7.9863 | 8.9846 | 1.3997 |
| 02 | 0.9983 | 1.9965 | 2.9948 | 3.9931 | 4.9914 | 5.9896 | 6.9879 | 7.9862 | 8.9845 | 1.3997 |
| 03 | 0.9983 | 1.9965 | 2.9948 | 3.9931 | 4.9913 | 5.9896 | 6.9878 | 7.9861 | 8.9844 | 1.3997 |
| 04 | 0.9983 | 1.9965 | 2.9948 | 3.9930 | 4.9913 | 5.9895 | 6.9878 | 7.9860 | 8.9843 | 1.3997 |
| 05 | 0.9982 | 1.9965 | 2.9947 | 3.9930 | 4.9912 | 5.9894 | 6.9877 | 7.9859 | 8.9842 | 1.3997 |
| 06 | 0.9982 | 1.9965 | 2.9947 | 3.9929 | 4.9912 | 5.9894 | 6.9876 | 7.9858 | 8.9841 | 1.3997 |
| 07 | 0.9982 | 1.9964 | 2.9947 | 3.9929 | 4.9911 | 5.9893 | 6.9875 | 7.9858 | 8.9840 | 1.3997 |
| 08 | 0.9982 | 1.9964 | 2.9946 | 3.9928 | 4.9910 | 5.9892 | 6.9875 | 7.9857 | 8.9839 | 1.3997 |
| 09 | 0.9982 | 1.9964 | 2.9946 | 3.9928 | 4.9910 | 5.9892 | 6.9874 | 7.9856 | 8.9838 | 1.3997 |
| 10 | 0.9982 | 1.9964 | 2.9946 | 3.9927 | 4.9909 | 5.9891 | 6.9873 | 7.9855 | 8.9837 | 1.3997 |
| 11 | 0.9982 | 1.9963 | 2.9945 | 3.9927 | 4.9909 | 5.9890 | 6.9872 | 7.9854 | 8.9836 | 1.3997 |
| 12 | 0.9982 | 1.9963 | 2.9945 | 3.9926 | 4.9908 | 5.9890 | 6.9871 | 7.9853 | 8.9834 | 1.3997 |
| 13 | 0.9981 | 1.9963 | 2.9944 | 3.9926 | 4.9907 | 5.9889 | 6.9870 | 7.9852 | 8.9833 | 1.3997 |
| 14 | 0.9981 | 1.9963 | 2.9944 | 3.9925 | 4.9907 | 5.9888 | 6.9870 | 7.9851 | 8.9832 | 1.3996 |
| 15 | 0.9981 | 1.9962 | 2.9944 | 3.9925 | 4.9906 | 5.9887 | 6.9869 | 7.9850 | 8.9831 | 1.3996 |
| 16 | 0.9981 | 1.9962 | 2.9943 | 3.9924 | 4.9906 | 5.9887 | 6.9868 | 7.9849 | 8.9830 | 1.3996 |
| 17 | 0.9981 | 1.9962 | 2.9943 | 3.9924 | 4.9905 | 5.9886 | 6.9867 | 7.9848 | 8.9829 | 1.3996 |
| 18 | 0.9981 | 1.9962 | 2.9943 | 3.9923 | 4.9904 | 5.9885 | 6.9866 | 7.9847 | 8.9828 | 1.3996 |
| 19 | 0.9981 | 1.9962 | 2.9942 | 3.9923 | 4.9904 | 5.9884 | 6.9865 | 7.9846 | 8.9827 | 1.3996 |
| 20 | 0.9981 | 1.9961 | 2.9942 | 3.9922 | 4.9903 | 5.9884 | 6.9864 | 7.9845 | 8.9825 | 1.3996 |
| 21 | 0.9980 | 1.9961 | 2.9941 | 3.9922 | 4.9902 | 5.9883 | 6.9863 | 7.9844 | 8.9824 | 1.3996 |
| 22 | 0.9980 | 1.9961 | 2.9941 | 3.9921 | 4.9902 | 5.9882 | 6.9862 | 7.9842 | 8.9823 | 1.3996 |
| 23 | 0.9980 | 1.9960 | 2.9941 | 3.9921 | 4.9901 | 5.9881 | 6.9861 | 7.9841 | 8.9822 | 1.3996 |
| 24 | 0.9980 | 1.9960 | 2.9940 | 3.9920 | 4.9900 | 5.9880 | 6.9860 | 7.9840 | 8.9820 | 1.3996 |
| 25 | 0.9980 | 1.9960 | 2.9940 | 3.9920 | 4.9899 | 5.9879 | 6.9859 | 7.9839 | 8.9819 | 1.3995 |
| 26 | 0.9980 | 1.9959 | 2.9939 | 3.9919 | 4.9899 | 5.9878 | 6.9858 | 7.9838 | 8.9818 | 1.3995 |
| 27 | 0.9980 | 1.9959 | 2.9939 | 3.9918 | 4.9898 | 5.9878 | 6.9857 | 7.9837 | 8.9816 | 1.3995 |
| 28 | 0.9979 | 1.9959 | 2.9938 | 3.9918 | 4.9897 | 5.9877 | 6.9856 | 7.9836 | 8.9815 | 1.3995 |
| 29 | 0.9979 | 1.9959 | 2.9938 | 3.9917 | 4.9897 | 5.9876 | 6.9855 | 7.9834 | 8.9814 | 1.3995 |
| 30 | 0.9979 | 1.9958 | 2.9937 | 3.9917 | 4.9896 | 5.9875 | 6.9854 | 7.9833 | 8.9812 | 1.3995 |
| 31 | 0.9979 | 1.9958 | 2.9937 | 3.9916 | 4.9895 | 5.9874 | 6.9853 | 7.9832 | 8.9811 | 1.3995 |
| 32 | 0.9979 | 1.9958 | 2.9937 | 3.9915 | 4.9894 | 5.9873 | 6.9852 | 7.9831 | 8.9810 | 1.3995 |
| 33 | 0.9979 | 1.9957 | 2.9936 | 3.9915 | 4.9893 | 5.9872 | 6.9851 | 7.9829 | 8.9808 | 1.3995 |
| 34 | 0.9979 | 1.9957 | 2.9936 | 3.9914 | 4.9893 | 5.9871 | 6.9850 | 7.9828 | 8.9807 | 1.3995 |
| 35 | 0.9978 | 1.9957 | 2.9935 | 3.9913 | 4.9892 | 5.9870 | 6.9849 | 7.9827 | 8.9805 | 1.3995 |
| 36 | 0.9978 | 1.9956 | 2.9935 | 3.9913 | 4.9891 | 5.9869 | 6.9847 | 7.9826 | 8.9804 | 1.3994 |
| 37 | 0.9978 | 1.9956 | 2.9934 | 3.9912 | 4.9890 | 5.9868 | 6.9846 | 7.9824 | 8.9802 | 1.3994 |
| 38 | 0.9978 | 1.9956 | 2.9934 | 3.9911 | 4.9889 | 5.9867 | 6.9845 | 7.9823 | 8.9801 | 1.3994 |
| 39 | 0.9978 | 1.9955 | 2.9933 | 3.9911 | 4.9889 | 5.9866 | 6.9844 | 7.9822 | 8.9799 | 1.3994 |
| 40 | 0.9978 | 1.9955 | 2.9933 | 3.9910 | 4.9888 | 5.9865 | 6.9843 | 7.9820 | 8.9798 | 1.3994 |
| 41 | 0.9977 | 1.9955 | 2.9932 | 3.9909 | 4.9887 | 5.9864 | 6.9842 | 7.9819 | 8.9796 | 1.3994 |
| 42 | 0.9977 | 1.9954 | 2.9932 | 3.9909 | 4.9886 | 5.9863 | 6.9840 | 7.9818 | 8.9795 | 1.3994 |
| 43 | 0.9977 | 1.9954 | 2.9931 | 3.9908 | 4.9885 | 5.9862 | 6.9839 | 7.9816 | 8.9793 | 1.3994 |
| 44 | 0.9977 | 1.9954 | 2.9931 | 3.9907 | 4.9884 | 5.9861 | 6.9838 | 7.9815 | 8.9792 | 1.3994 |
| 45 | 0.9977 | 1.9953 | 2.9930 | 3.9907 | 4.9883 | 5.9860 | 6.9837 | 7.9813 | 8.9790 | 1.3994 |
| 46 | 0.9976 | 1.9953 | 2.9929 | 3.9906 | 4.9882 | 5.9859 | 6.9835 | 7.9812 | 8.9788 | 1.3993 |
| 47 | 0.9976 | 1.9953 | 2.9929 | 3.9905 | 4.9882 | 5.9858 | 6.9834 | 7.9810 | 8.9787 | 1.3993 |
| 48 | 0.9976 | 1.9952 | 2.9928 | 3.9905 | 4.9881 | 5.9857 | 6.9833 | 7.9809 | 8.9785 | 1.3993 |
| 49 | 0.9976 | 1.9952 | 2.9928 | 3.9904 | 4.9880 | 5.9856 | 6.9832 | 7.9808 | 8.9784 | 1.3993 |
| 50 | 0.9976 | 1.9952 | 2.9927 | 3.9903 | 4.9879 | 5.9855 | 6.9830 | 7.9806 | 8.9782 | 1.3993 |
| 51 | 0.9976 | 1.9951 | 2.9927 | 3.9902 | 4.9878 | 5.9854 | 6.9829 | 7.9805 | 8.9780 | 1.3993 |
| 52 | 0.9975 | 1.9951 | 2.9926 | 3.9902 | 4.9877 | 5.9852 | 6.9828 | 7.9803 | 8.9779 | 1.3993 |
| 53 | 0.9975 | 1.9950 | 2.9926 | 3.9901 | 4.9876 | 5.9851 | 6.9826 | 7.9802 | 8.9777 | 1.3993 |
| 54 | 0.9975 | 1.9950 | 2.9925 | 3.9900 | 4.9875 | 5.9850 | 6.9825 | 7.9800 | 8.9775 | 1.3993 |
| 55 | 0.9975 | 1.9950 | 2.9924 | 3.9899 | 4.9874 | 5.9849 | 6.9824 | 7.9798 | 8.9773 | 1.3992 |
| 56 | 0.9975 | 1.9949 | 2.9924 | 3.9898 | 4.9873 | 5.9848 | 6.9822 | 7.9797 | 8.9772 | 1.3992 |
| 57 | 0.9974 | 1.9949 | 2.9923 | 3.9898 | 4.9872 | 5.9847 | 6.9821 | 7.9795 | 8.9770 | 1.3992 |
| 58 | 0.9974 | 1.9948 | 2.9923 | 3.9897 | 4.9871 | 5.9845 | 6.9820 | 7.9794 | 8.9768 | 1.3992 |
| 59 | 0.9974 | 1.9948 | 2.9922 | 3.9896 | 4.9870 | 5.9844 | 6.9818 | 7.9792 | 8.9766 | 1.3992 |
| 60 | 0.9974 | 1.9948 | 2.9922 | 3.9895 | 4.9869 | 5.9843 | 6.9817 | 7.9791 | 8.9765 | 1.3992 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0174 | 0.0349 | 0.0523 | 0.0697 | 0.0871 | 0.1046 | 0.1220 | 0.1394 | 0.1568 | 0.0244 | 00 |
| 0.0177 | 0.0354 | 0.0531 | 0.0708 | 0.0886 | 0.1063 | 0.1240 | 0.1417 | 0.1594 | 0.0248 | 01 |
| 0.0180 | 0.0360 | 0.0540 | 0.0720 | 0.0900 | 0.1080 | 0.1260 | 0.1440 | 0.1620 | 0.0253 | 02 |
| 0.0183 | 0.0366 | 0.0549 | 0.0732 | 0.0915 | 0.1098 | 0.1281 | 0.1464 | 0.1647 | 0.0257 | 03 |
| 0.0186 | 0.0372 | 0.0558 | 0.0743 | 0.0929 | 0.1115 | 0.1301 | 0.1487 | 0.1673 | 0.0261 | 04 |
| 0.0189 | 0.0378 | 0.0566 | 0.0755 | 0.0944 | 0.1133 | 0.1321 | 0.1510 | 0.1699 | 0.0265 | 05 |
| 0.0192 | 0.0383 | 0.0575 | 0.0767 | 0.0958 | 0.1150 | 0.1342 | 0.1533 | 0.1725 | 0.0269 | 06 |
| 0.0195 | 0.0389 | 0.0584 | 0.0778 | 0.0973 | 0.1167 | 0.1362 | 0.1557 | 0.1751 | 0.0273 | 07 |
| 0.0197 | 0.0395 | 0.0592 | 0.0790 | 0.0987 | 0.1185 | 0.1382 | 0.1580 | 0.1777 | 0.0277 | 08 |
| 0.0200 | 0.0401 | 0.0601 | 0.0802 | 0.1002 | 0.1202 | 0.1403 | 0.1603 | 0.1803 | 0.0281 | 09 |
| 0.0203 | 0.0407 | 0.0610 | 0.0813 | 0.1016 | 0.1220 | 0.1423 | 0.1626 | 0.1830 | 0.0285 | 10 |
| 0.0206 | 0.0412 | 0.0619 | 0.0825 | 0.1031 | 0.1237 | 0.1443 | 0.1649 | 0.1856 | 0.0289 | 11 |
| 0.0209 | 0.0418 | 0.0627 | 0.0836 | 0.1045 | 0.1255 | 0.1464 | 0.1673 | 0.1882 | 0.0293 | 12 |
| 0.0212 | 0.0424 | 0.0636 | 0.0848 | 0.1060 | 0.1272 | 0.1484 | 0.1690 | 0.1908 | 0.0297 | 13 |
| 0.0215 | 0.0430 | 0.0645 | 0.0860 | 0.1075 | 0.1289 | 0.1504 | 0.1719 | 0.1934 | 0.0301 | 14 |
| 0.0218 | 0.0436 | 0.0653 | 0.0871 | 0.1089 | 0.1307 | 0.1525 | 0.1742 | 0.1960 | 0.0305 | 15 |
| 0.0221 | 0.0441 | 0.0662 | 0.0883 | 0.1104 | 0.1324 | 0.1545 | 0.1766 | 0.1986 | 0.0309 | 16 |
| 0.0224 | 0.0447 | 0.0671 | 0.0894 | 0.1118 | 0.1342 | 0.1565 | 0.1789 | 0.2012 | 0.0314 | 17 |
| 0.0227 | 0.0453 | 0.0680 | 0.0906 | 0.1133 | 0.1359 | 0.1586 | 0.1812 | 0.2039 | 0.0318 | 18 |
| 0.0229 | 0.0459 | 0.0688 | 0.0918 | 0.1147 | 0.1376 | 0.1606 | 0.1835 | 0.2065 | 0.0322 | 19 |
| 0.0232 | 0.0465 | 0.0697 | 0.0929 | 0.1162 | 0.1394 | 0.1626 | 0.1858 | 0.2091 | 0.0326 | 20 |
| 0.0235 | 0.0470 | 0.0706 | 0.0941 | 0.1176 | 0.1411 | 0.1646 | 0.1882 | 0.2117 | 0.0330 | 21 |
| 0.0238 | 0.0476 | 0.0714 | 0.0952 | 0.1191 | 0.1429 | 0.1667 | 0.1905 | 0.2143 | 0.0334 | 22 |
| 0.0241 | 0.0482 | 0.0723 | 0.0964 | 0.1205 | 0.1446 | 0.1687 | 0.1928 | 0.2169 | 0.0338 | 23 |
| 0.0244 | 0.0488 | 0.0732 | 0.0976 | 0.1220 | 0.1463 | 0.1707 | 0.1951 | 0.2195 | 0.0342 | 24 |
| 0.0247 | 0.0494 | 0.0740 | 0.0987 | 0.1234 | 0.1481 | 0.1728 | 0.1974 | 0.2221 | 0.0346 | 25 |
| 0.0250 | 0.0499 | 0.0749 | 0.0999 | 0.1249 | 0.1498 | 0.1748 | 0.1998 | 0.2247 | 0.0350 | 26 |
| 0.0253 | 0.0505 | 0.0758 | 0.1010 | 0.1263 | 0.1516 | 0.1768 | 0.2021 | 0.2273 | 0.0354 | 27 |
| 0.0256 | 0.0511 | 0.0767 | 0.1022 | 0.1278 | 0.1533 | 0.1789 | 0.2044 | 0.2300 | 0.0358 | 28 |
| 0.0258 | 0.0517 | 0.0775 | 0.1034 | 0.1292 | 0.1550 | 0.1809 | 0.2067 | 0.2326 | 0.0362 | 29 |
| 0.0261 | 0.0523 | 0.0784 | 0.1045 | 0.1307 | 0.1568 | 0.1829 | 0.2090 | 0.2352 | 0.0366 | 30 |
| 0.0264 | 0.0528 | 0.0793 | 0.1057 | 0.1321 | 0.1585 | 0.1849 | 0.2114 | 0.2378 | 0.0371 | 31 |
| 0.0267 | 0.0534 | 0.0801 | 0.1068 | 0.1336 | 0.1603 | 0.1870 | 0.2137 | 0.2404 | 0.0375 | 32 |
| 0.0270 | 0.0540 | 0.0810 | 0.1080 | 0.1350 | 0.1620 | 0.1890 | 0.2160 | 0.2430 | 0.0379 | 33 |
| 0.0273 | 0.0546 | 0.0819 | 0.1092 | 0.1365 | 0.1637 | 0.1910 | 0.2183 | 0.2456 | 0.0383 | 34 |
| 0.0276 | 0.0552 | 0.0827 | 0.1103 | 0.1379 | 0.1655 | 0.1931 | 0.2206 | 0.2482 | 0.0387 | 35 |
| 0.0279 | 0.0557 | 0.0836 | 0.1115 | 0.1394 | 0.1672 | 0.1951 | 0.2230 | 0.2508 | 0.0391 | 36 |
| 0.0282 | 0.0563 | 0.0845 | 0.1126 | 0.1408 | 0.1690 | 0.1971 | 0.2253 | 0.2534 | 0.0395 | 37 |
| 0.0285 | 0.0569 | 0.0854 | 0.1138 | 0.1423 | 0.1707 | 0.1992 | 0.2276 | 0.2561 | 0.0399 | 38 |
| 0.0287 | 0.0575 | 0.0862 | 0.1150 | 0.1437 | 0.1724 | 0.2012 | 0.2299 | 0.2587 | 0.0403 | 39 |
| 0.0290 | 0.0581 | 0.0871 | 0.1161 | 0.1452 | 0.1742 | 0.2032 | 0.2322 | 0.2613 | 0.0407 | 40 |
| 0.0293 | 0.0586 | 0.0880 | 0.1173 | 0.1466 | 0.1759 | 0.2052 | 0.2346 | 0.2639 | 0.0411 | 41 |
| 0.0296 | 0.0592 | 0.0888 | 0.1184 | 0.1481 | 0.1777 | 0.2073 | 0.2369 | 0.2665 | 0.0415 | 42 |
| 0.0299 | 0.0598 | 0.0897 | 0.1196 | 0.1495 | 0.1794 | 0.2093 | 0.2392 | 0.2691 | 0.0419 | 43 |
| 0.0302 | 0.0604 | 0.0906 | 0.1208 | 0.1510 | 0.1811 | 0.2113 | 0.2415 | 0.2717 | 0.0423 | 44 |
| 0.0305 | 0.0610 | 0.0914 | 0.1219 | 0.1524 | 0.1829 | 0.2134 | 0.2438 | 0.2743 | 0.0428 | 45 |
| 0.0308 | 0.0615 | 0.0923 | 0.1231 | 0.1539 | 0.1846 | 0.2154 | 0.2462 | 0.2769 | 0.0432 | 46 |
| 0.0311 | 0.0621 | 0.0932 | 0.1242 | 0.1553 | 0.1864 | 0.2174 | 0.2485 | 0.2795 | 0.0436 | 47 |
| 0.0314 | 0.0627 | 0.0941 | 0.1254 | 0.1568 | 0.1881 | 0.2195 | 0.2508 | 0.2822 | 0.0440 | 48 |
| 0.0316 | 0.0633 | 0.0949 | 0.1266 | 0.1582 | 0.1898 | 0.2215 | 0.2531 | 0.2848 | 0.0444 | 49 |
| 0.0319 | 0.0639 | 0.0958 | 0.1277 | 0.1597 | 0.1916 | 0.2235 | 0.2554 | 0.2874 | 0.0448 | 50 |
| 0.0322 | 0.0644 | 0.0967 | 0.1289 | 0.1611 | 0.1933 | 0.2255 | 0.2578 | 0.2900 | 0.0452 | 51 |
| 0.0325 | 0.0650 | 0.0975 | 0.1300 | 0.1626 | 0.1951 | 0.2276 | 0.2601 | 0.2926 | 0.0456 | 52 |
| 0.0328 | 0.0656 | 0.0984 | 0.1312 | 0.1640 | 0.1968 | 0.2296 | 0.2624 | 0.2952 | 0.0460 | 53 |
| 0.0331 | 0.0662 | 0.0993 | 0.1324 | 0.1655 | 0.1985 | 0.2316 | 0.2647 | 0.2978 | 0.0464 | 54 |
| 0.0334 | 0.0668 | 0.1001 | 0.1335 | 0.1669 | 0.2003 | 0.2336 | 0.2670 | 0.3004 | 0.0468 | 55 |
| 0.0337 | 0.0673 | 0.1010 | 0.1347 | 0.1684 | 0.2020 | 0.2357 | 0.2694 | 0.3030 | 0.0472 | 56 |
| 0.0340 | 0.0679 | 0.1019 | 0.1358 | 0.1698 | 0.2038 | 0.2377 | 0.2717 | 0.3056 | 0.0476 | 57 |
| 0.0342 | 0.0685 | 0.1027 | 0.1370 | 0.1712 | 0.2055 | 0.2397 | 0.2740 | 0.3082 | 0.0480 | 58 |
| 0.0345 | 0.0691 | 0.1036 | 0.1382 | 0.1727 | 0.2072 | 0.2418 | 0.2763 | 0.3109 | 0.0485 | 59 |
| 0.0348 | 0.0697 | 0.1045 | 0.1393 | 0.1742 | 0.2090 | 0.2438 | 0.2786 | 0.3135 | 0.0489 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9974 | 1.9948 | 2.9922 | 3.9895 | 4.9869 | 5.9843 | 6.9817 | 7.9791 | 8.9765 | 1.3992 |
| 01 | 0.9974 | 1.9947 | 2.9921 | 3.9895 | 4.9868 | 5.9842 | 6.9815 | 7.9789 | 8.9763 | 1.3992 |
| 02 | 0.9973 | 1.9947 | 2.9920 | 3.9894 | 4.9867 | 5.9841 | 6.9814 | 7.9787 | 8.9761 | 1.3992 |
| 03 | 0.9973 | 1.9946 | 2.9920 | 3.9893 | 4.9866 | 5.9839 | 6.9812 | 7.9786 | 8.9759 | 1.3992 |
| 04 | 0.9973 | 1.9946 | 2.9919 | 3.9892 | 4.9865 | 5.9838 | 6.9811 | 7.9784 | 8.9757 | 1.3991 |
| 05 | 0.9973 | 1.9946 | 2.9918 | 3.9891 | 4.9864 | 5.9837 | 6.9810 | 7.9782 | 8.9755 | 1.3991 |
| 06 | 0.9973 | 1.9945 | 2.9918 | 3.9890 | 4.9863 | 5.9835 | 6.9808 | 7.9781 | 8.9753 | 1.3991 |
| 07 | 0.9972 | 1.9945 | 2.9917 | 3.9889 | 4.9862 | 5.9834 | 6.9807 | 7.9779 | 8.9751 | 1.3991 |
| 08 | 0.9972 | 1.9944 | 2.9916 | 3.9888 | 4.9861 | 5.9833 | 6.9805 | 7.9777 | 8.9749 | 1.3991 |
| 09 | 0.9972 | 1.9944 | 2.9916 | 3.9888 | 4.9860 | 5.9832 | 6.9804 | 7.9776 | 8.9747 | 1.3991 |
| 10 | 0.9972 | 1.9943 | 2.9915 | 3.9887 | 4.9859 | 5.9830 | 6.9802 | 7.9774 | 8.9746 | 1.3991 |
| 11 | 0.9972 | 1.9943 | 2.9915 | 3.9886 | 4.9858 | 5.9829 | 6.9801 | 7.9772 | 8.9744 | 1.3990 |
| 12 | 0.9971 | 1.9943 | 2.9914 | 3.9885 | 4.9856 | 5.9828 | 6.9799 | 7.9770 | 8.9741 | 1.3990 |
| 13 | 0.9971 | 1.9942 | 2.9913 | 3.9884 | 4.9855 | 5.9826 | 6.9797 | 7.9768 | 8.9739 | 1.3990 |
| 14 | 0.9971 | 1.9942 | 2.9912 | 3.9883 | 4.9854 | 5.9825 | 6.9796 | 7.9767 | 8.9737 | 1.3990 |
| 15 | 0.9971 | 1.9941 | 2.9912 | 3.9882 | 4.9853 | 5.9824 | 6.9794 | 7.9765 | 8.9735 | 1.3990 |
| 16 | 0.9970 | 1.9941 | 2.9911 | 3.9881 | 4.9852 | 5.9822 | 6.9793 | 7.9763 | 8.9733 | 1.3990 |
| 17 | 0.9970 | 1.9940 | 2.9910 | 3.9881 | 4.9851 | 5.9821 | 6.9791 | 7.9761 | 8.9731 | 1.3989 |
| 18 | 0.9970 | 1.9940 | 2.9910 | 3.9880 | 4.9850 | 5.9819 | 6.9789 | 7.9759 | 8.9729 | 1.3989 |
| 19 | 0.9970 | 1.9939 | 2.9909 | 3.9879 | 4.9848 | 5.9818 | 6.9788 | 7.9757 | 8.9727 | 1.3989 |
| 20 | 0.9969 | 1.9939 | 2.9908 | 3.9878 | 4.9847 | 5.9817 | 6.9786 | 7.9756 | 8.9725 | 1.3989 |
| 21 | 0.9969 | 1.9938 | 2.9908 | 3.9877 | 4.9846 | 5.9815 | 6.9784 | 7.9754 | 8.9723 | 1.3989 |
| 22 | 0.9969 | 1.9938 | 2.9907 | 3.9876 | 4.9845 | 5.9814 | 6.9783 | 7.9752 | 8.9721 | 1.3989 |
| 23 | 0.9969 | 1.9937 | 2.9906 | 3.9875 | 4.9844 | 5.9812 | 6.9781 | 7.9750 | 8.9718 | 1.3988 |
| 24 | 0.9968 | 1.9937 | 2.9905 | 3.9874 | 4.9842 | 5.9811 | 6.9779 | 7.9748 | 8.9716 | 1.3988 |
| 25 | 0.9968 | 1.9936 | 2.9905 | 3.9873 | 4.9841 | 5.9809 | 6.9778 | 7.9746 | 8.9714 | 1.3988 |
| 26 | 0.9968 | 1.9936 | 2.9904 | 3.9872 | 4.9840 | 5.9808 | 6.9776 | 7.9744 | 8.9712 | 1.3988 |
| 27 | 0.9968 | 1.9935 | 2.9903 | 3.9871 | 4.9839 | 5.9806 | 6.9774 | 7.9742 | 8.9710 | 1.3988 |
| 28 | 0.9967 | 1.9935 | 2.9902 | 3.9870 | 4.9837 | 5.9805 | 6.9772 | 7.9740 | 8.9707 | 1.3987 |
| 29 | 0.9967 | 1.9934 | 2.9902 | 3.9869 | 4.9836 | 5.9803 | 6.9771 | 7.9738 | 8.9705 | 1.3987 |
| 30 | 0.9967 | 1.9934 | 2.9901 | 3.9868 | 4.9835 | 5.9802 | 6.9769 | 7.9736 | 8.9703 | 1.3987 |
| 31 | 0.9967 | 1.9933 | 2.9900 | 3.9867 | 4.9834 | 5.9800 | 6.9767 | 7.9734 | 8.9701 | 1.3987 |
| 32 | 0.9966 | 1.9933 | 2.9899 | 3.9866 | 4.9832 | 5.9799 | 6.9765 | 7.9732 | 8.9698 | 1.3987 |
| 33 | 0.9966 | 1.9932 | 2.9899 | 3.9865 | 4.9831 | 5.9797 | 6.9764 | 7.9730 | 8.9696 | 1.3987 |
| 34 | 0.9966 | 1.9932 | 2.9898 | 3.9864 | 4.9830 | 5.9796 | 6.9762 | 7.9728 | 8.9694 | 1.3986 |
| 35 | 0.9966 | 1.9931 | 2.9897 | 3.9863 | 4.9828 | 5.9794 | 6.9760 | 7.9726 | 8.9691 | 1.3986 |
| 36 | 0.9965 | 1.9931 | 2.9896 | 3.9862 | 4.9827 | 5.9793 | 6.9758 | 7.9723 | 8.9689 | 1.3986 |
| 37 | 0.9965 | 1.9930 | 2.9896 | 3.9861 | 4.9826 | 5.9791 | 6.9756 | 7.9721 | 8.9687 | 1.3986 |
| 38 | 0.9965 | 1.9930 | 2.9895 | 3.9860 | 4.9825 | 5.9789 | 6.9754 | 7.9719 | 8.9684 | 1.3986 |
| 39 | 0.9965 | 1.9929 | 2.9894 | 3.9859 | 4.9823 | 5.9788 | 6.9753 | 7.9717 | 8.9682 | 1.3985 |
| 40 | 0.9964 | 1.9929 | 2.9893 | 3.9858 | 4.9822 | 5.9786 | 6.9751 | 7.9715 | 8.9680 | 1.3985 |
| 41 | 0.9964 | 1.9928 | 2.9892 | 3.9856 | 4.9821 | 5.9785 | 6.9749 | 7.9713 | 8.9677 | 1.3985 |
| 42 | 0.9964 | 1.9928 | 2.9891 | 3.9855 | 4.9819 | 5.9783 | 6.9747 | 7.9711 | 8.9674 | 1.3985 |
| 43 | 0.9964 | 1.9927 | 2.9891 | 3.9854 | 4.9818 | 5.9781 | 6.9745 | 7.9708 | 8.9672 | 1.3985 |
| 44 | 0.9963 | 1.9927 | 2.9890 | 3.9853 | 4.9816 | 5.9780 | 6.9743 | 7.9706 | 8.9669 | 1.3984 |
| 45 | 0.9963 | 1.9926 | 2.9889 | 3.9852 | 4.9815 | 5.9778 | 6.9741 | 7.9704 | 8.9667 | 1.3984 |
| 46 | 0.9963 | 1.9925 | 2.9888 | 3.9851 | 4.9814 | 5.9776 | 6.9739 | 7.9702 | 8.9664 | 1.3984 |
| 47 | 0.9962 | 1.9925 | 2.9887 | 3.9850 | 4.9812 | 5.9775 | 6.9737 | 7.9700 | 8.9662 | 1.3984 |
| 48 | 0.9962 | 1.9924 | 2.9886 | 3.9849 | 4.9811 | 5.9773 | 6.9735 | 7.9697 | 8.9659 | 1.3984 |
| 49 | 0.9962 | 1.9924 | 2.9886 | 3.9848 | 4.9809 | 5.9771 | 6.9733 | 7.9695 | 8.9657 | 1.3983 |
| 50 | 0.9962 | 1.9923 | 2.9885 | 3.9846 | 4.9808 | 5.9770 | 6.9731 | 7.9693 | 8.9654 | 1.3983 |
| 51 | 0.9961 | 1.9923 | 2.9884 | 3.9845 | 4.9807 | 5.9768 | 6.9729 | 7.9690 | 8.9652 | 1.3983 |
| 52 | 0.9961 | 1.9922 | 2.9883 | 3.9844 | 4.9805 | 5.9766 | 6.9727 | 7.9688 | 8.9649 | 1.3983 |
| 53 | 0.9961 | 1.9921 | 2.9882 | 3.9843 | 4.9804 | 5.9764 | 6.9725 | 7.9686 | 8.9646 | 1.3983 |
| 54 | 0.9960 | 1.9921 | 2.9881 | 3.9842 | 4.9802 | 5.9763 | 6.9723 | 7.9683 | 8.9644 | 1.3982 |
| 55 | 0.9960 | 1.9920 | 2.9880 | 3.9841 | 4.9801 | 5.9761 | 6.9721 | 7.9681 | 8.9641 | 1.3982 |
| 56 | 0.9960 | 1.9920 | 2.9879 | 3.9839 | 4.9799 | 5.9759 | 6.9719 | 7.9679 | 8.9638 | 1.3982 |
| 57 | 0.9960 | 1.9919 | 2.9879 | 3.9838 | 4.9798 | 5.9757 | 6.9717 | 7.9676 | 8.9636 | 1.3982 |
| 58 | 0.9959 | 1.9918 | 2.9878 | 3.9837 | 4.9796 | 5.9756 | 6.9715 | 7.9674 | 8.9633 | 1.3981 |
| 59 | 0.9959 | 1.9918 | 2.9877 | 3.9836 | 4.9795 | 5.9754 | 6.9713 | 7.9672 | 8.9631 | 1.3981 |
| 60 | 0.9959 | 1.9917 | 2.9876 | 3.9835 | 4.9793 | 5.9752 | 6.9711 | 7.9669 | 8.9628 | 1.3981 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0348 | 0.0697 | 0.1045 | 0.1393 | 0.1742 | 0.2090 | 0.2438 | 0.2786 | 0.3135 | 0.0489 | 00 |
| 0.0351 | 0.0702 | 0.1054 | 0.1405 | 0.1756 | 0.2107 | 0.2458 | 0.2810 | 0.3161 | 0.0493 | 01 |
| 0.0354 | 0.0708 | 0.1062 | 0.1416 | 0.1771 | 0.2125 | 0.2479 | 0.2833 | 0.3187 | 0.0497 | 02 |
| 0.0357 | 0.0714 | 0.1071 | 0.1428 | 0.1785 | 0.2142 | 0.2499 | 0.2856 | 0.3213 | 0.0501 | 03 |
| 0.0360 | 0.0720 | 0.1080 | 0.1440 | 0.1800 | 0.2159 | 0.2519 | 0.2879 | 0.3239 | 0.0505 | 04 |
| 0.0363 | 0.0726 | 0.1088 | 0.1451 | 0.1814 | 0.2177 | 0.2540 | 0.2902 | 0.3265 | 0.0509 | 05 |
| 0.0366 | 0.0731 | 0.1097 | 0.1463 | 0.1828 | 0.2194 | 0.2560 | 0.2926 | 0.3291 | 0.0513 | 06 |
| 0.0369 | 0.0737 | 0.1106 | 0.1474 | 0.1843 | 0.2212 | 0.2580 | 0.2949 | 0.3317 | 0.0517 | 07 |
| 0.0371 | 0.0743 | 0.1114 | 0.1486 | 0.1857 | 0.2229 | 0.2600 | 0.2972 | 0.3343 | 0.0521 | 08 |
| 0.0374 | 0.0749 | 0.1123 | 0.1498 | 0.1872 | 0.2246 | 0.2621 | 0.2995 | 0.3370 | 0.0525 | 09 |
| 0.0377 | 0.0755 | 0.1132 | 0.1509 | 0.1886 | 0.2264 | 0.2641 | 0.3018 | 0.3396 | 0.0529 | 10 |
| 0.0380 | 0.0760 | 0.1141 | 0.1521 | 0.1901 | 0.2281 | 0.2661 | 0.3042 | 0.3422 | 0.0533 | 11 |
| 0.0383 | 0.0766 | 0.1149 | 0.1532 | 0.1915 | 0.2299 | 0.2682 | 0.3065 | 0.3448 | 0.0537 | 12 |
| 0.0386 | 0.0772 | 0.1158 | 0.1544 | 0.1930 | 0.2316 | 0.2702 | 0.3088 | 0.3474 | 0.0541 | 13 |
| 0.0389 | 0.0778 | 0.1167 | 0.1556 | 0.1944 | 0.2333 | 0.2722 | 0.3111 | 0.3500 | 0.0546 | 14 |
| 0.0392 | 0.0783 | 0.1175 | 0.1567 | 0.1959 | 0.2350 | 0.2742 | 0.3134 | 0.3526 | 0.0550 | 15 |
| 0.0395 | 0.0789 | 0.1184 | 0.1578 | 0.1973 | 0.2368 | 0.2762 | 0.3157 | 0.3552 | 0.0554 | 16 |
| 0.0398 | 0.0795 | 0.1193 | 0.1590 | 0.1988 | 0.2385 | 0.2783 | 0.3180 | 0.3578 | 0.0558 | 17 |
| 0.0400 | 0.0801 | 0.1201 | 0.1602 | 0.2002 | 0.2402 | 0.2803 | 0.3203 | 0.3604 | 0.0562 | 18 |
| 0.0403 | 0.0807 | 0.1210 | 0.1613 | 0.0017 | 0.2420 | 0.2823 | 0.3226 | 0.3630 | 0.0566 | 19 |
| 0.0406 | 0.0812 | 0.1219 | 0.1625 | 0.2031 | 0.2437 | 0.2843 | 0.3250 | 0.3656 | 0.0570 | 20 |
| 0.0409 | 0.0818 | 0.1227 | 0.1636 | 0.2046 | 0.2455 | 0.2864 | 0.3273 | 0.3682 | 0.0574 | 21 |
| 0.0412 | 0.0824 | 0.1236 | 0.1648 | 0.2060 | 0.2472 | 0.2884 | 0.3296 | 0.3708 | 0.0578 | 22 |
| 0.0415 | 0.0830 | 0.1245 | 0.1660 | 0.2075 | 0.2489 | 0.2904 | 0.3319 | 0.3734 | 0.0582 | 23 |
| 0.0418 | 0.0836 | 0.1253 | 0.1671 | 0.2089 | 0.2507 | 0.2925 | 0.3342 | 0.3760 | 0.0586 | 24 |
| 0.0421 | 0.0841 | 0.1262 | 0.1683 | 0.2103 | 0.2524 | 0.2945 | 0.3366 | 0.3786 | 0.0590 | 25 |
| 0.0424 | 0.0847 | 0.1271 | 0.1694 | 0.2118 | 0.2542 | 0.2965 | 0.3389 | 0.3812 | 0.0594 | 26 |
| 0.0426 | 0.0853 | 0.1279 | 0.1706 | 0.2132 | 0.2559 | 0.2985 | 0.3412 | 0.3838 | 0.0598 | 27 |
| 0.0429 | 0.0859 | 0.1288 | 0.1718 | 0.2147 | 0.2576 | 0.3000 | 0.3435 | 0.3865 | 0.0602 | 28 |
| 0.0432 | 0.0865 | 0.1297 | 0.1729 | 0.2161 | 0.2594 | 0.3026 | 0.3458 | 0.3891 | 0.0607 | 29 |
| 0.0435 | 0.0870 | 0.1306 | 0.1741 | 0.2176 | 0.2611 | 0.3046 | 0.3482 | 0.3917 | 0.0611 | 30 |
| 0.0438 | 0.0876 | 0.1314 | 0.1752 | 0.2190 | 0.2629 | 0.3067 | 0.3505 | 0.3943 | 0.0615 | 31 |
| 0.0441 | 0.0882 | 0.1323 | 0.1764 | 0.2205 | 0.2646 | 0.3087 | 0.3528 | 0.3969 | 0.0619 | 32 |
| 0.0444 | 0.0888 | 0.1331 | 0.1775 | 0.2219 | 0.2663 | 0.3107 | 0.3551 | 0.3995 | 0.0623 | 33 |
| 0.0447 | 0.0893 | 0.1340 | 0.1787 | 0.2234 | 0.2680 | 0.3127 | 0.3574 | 0.4021 | 0.0627 | 34 |
| 0.0450 | 0.0899 | 0.1349 | 0.1798 | 0.2248 | 0.2698 | 0.3147 | 0.3597 | 0.4047 | 0.0631 | 35 |
| 0.0453 | 0.0905 | 0.1358 | 0.1810 | 0.2263 | 0.2715 | 0.3168 | 0.3620 | 0.4073 | 0.0635 | 36 |
| 0.0455 | 0.0911 | 0.1366 | 0.1822 | 0.2277 | 0.2732 | 0.3188 | 0.3643 | 0.4099 | 0.0639 | 37 |
| 0.0458 | 0.0917 | 0.1375 | 0.1833 | 0.2292 | 0.2750 | 0.3208 | 0.3666 | 0.4125 | 0.0643 | 38 |
| 0.0461 | 0.0922 | 0.1384 | 0.1845 | 0.2306 | 0.2767 | 0.3228 | 0.3690 | 0.4151 | 0.0647 | 39 |
| 0.0464 | 0.0928 | 0.1392 | 0.1856 | 0.2321 | 0.2785 | 0.3249 | 0.3713 | 0.4177 | 0.0651 | 40 |
| 0.0467 | 0.0934 | 0.1401 | 0.1868 | 0.2335 | 0.2802 | 0.3269 | 0.3736 | 0.3203 | 0.0655 | 41 |
| 0.0470 | 0.0940 | 0.1410 | 0.1880 | 0.2350 | 0.2819 | 0.3289 | 0.3759 | 0.4229 | 0.0659 | 42 |
| 0.0473 | 0.0946 | 0.1418 | 0.1891 | 0.2364 | 0.2837 | 0.3310 | 0.3782 | 0.4255 | 0.0664 | 43 |
| 0.0476 | 0.0951 | 0.1427 | 0.1903 | 0.2378 | 0.2854 | 0.3330 | 0.3806 | 0.4281 | 0.0668 | 44 |
| 0.0479 | 0.0957 | 0.1436 | 0.1914 | 0.2393 | 0.2872 | 0.3350 | 0.3829 | 0.4307 | 0.0672 | 45 |
| 0.0481 | 0.0963 | 0.1444 | 0.1926 | 0.2407 | 0.2889 | 0.3370 | 0.3852 | 0.4333 | 0.0676 | 46 |
| 0.0484 | 0.0969 | 0.1453 | 0.1937 | 0.2422 | 0.2906 | 0.3390 | 0.3875 | 0.4359 | 0.0680 | 47 |
| 0.0487 | 0.0974 | 0.1462 | 0.1949 | 0.2436 | 0.2923 | 0.3410 | 0.3898 | 0.4385 | 0.0684 | 48 |
| 0.0490 | 0.0980 | 0.1470 | 0.1960 | 0.2451 | 0.2941 | 0.3431 | 0.3921 | 0.4411 | 0.0688 | 49 |
| 0.0493 | 0.0986 | 0.1479 | 0.1972 | 0.2465 | 0.2958 | 0.3451 | 0.3944 | 0.4437 | 0.0692 | 50 |
| 0.0496 | 0.0992 | 0.1488 | 0.1984 | 0.2480 | 0.2975 | 0.3471 | 0.3967 | 0.4463 | 0.0696 | 51 |
| 0.0499 | 0.0998 | 0.1496 | 0.1995 | 0.2494 | 0.2993 | 0.3492 | 0.3990 | 0.4489 | 0.0700 | 52 |
| 0.0502 | 0.1003 | 0.1505 | 0.2007 | 0.2508 | 0.3010 | 0.3512 | 0.4014 | 0.4515 | 0.0704 | 53 |
| 0.0505 | 0.1009 | 0.1514 | 0.2018 | 0.2523 | 0.3028 | 0.3532 | 0.4037 | 0.4541 | 0.0708 | 54 |
| 0.0507 | 0.1015 | 0.1522 | 0.2030 | 0.2537 | 0.3045 | 0.3552 | 0.4060 | 0.4567 | 0.0712 | 55 |
| 0.0510 | 0.1021 | 0.1531 | 0.2042 | 0.2562 | 0.3062 | 0.3573 | 0.4083 | 0.4593 | 0.0716 | 56 |
| 0.0513 | 0.1026 | 0.1540 | 0.2053 | 0.2566 | 0.3079 | 0.3593 | 0.4106 | 0.4619 | 0.0721 | 57 |
| 0.0516 | 0.1032 | 0.1548 | 0.2064 | 0.2581 | 0.3097 | 0.3613 | 0.4129 | 0.4645 | 0.0725 | 58 |
| 0.0519 | 0.1038 | 0.1557 | 0.2076 | 0.2595 | 0.3114 | 0.3633 | 0.4152 | 0.4671 | 0.0729 | 59 |
| 0.0522 | 0.1044 | 0.1566 | 0.2088 | 0.2610 | 0.3131 | 0.3653 | 0.4175 | 0.4697 | 0.0733 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9959 | 1.9917 | 2.9876 | 3.9835 | 4.9793 | 5.9752 | 6.9711 | 7.9669 | 8.9628 | 1.3981 |
| 01 | 0.9958 | 1.9917 | 2.9875 | 3.9833 | 4.9792 | 5.9750 | 6.9708 | 7.9667 | 8.9625 | 1.3981 |
| 02 | 0.9958 | 1.9916 | 2.9874 | 3.9832 | 4.9790 | 5.9748 | 6.9706 | 7.9664 | 8.9622 | 1.3981 |
| 03 | 0.9958 | 1.9915 | 2.9873 | 3.9831 | 4.9789 | 5.9746 | 6.9704 | 7.9662 | 8.9619 | 1.3980 |
| 04 | 0.9957 | 1.9915 | 2.9872 | 3.9830 | 4.9787 | 5.9744 | 6.9702 | 7.9659 | 8.9617 | 1.3980 |
| 05 | 0.9957 | 1.9914 | 2.9871 | 3.9828 | 4.9785 | 5.9743 | 6.9700 | 7.9657 | 8.9614 | 1.3980 |
| 06 | 0.9957 | 1.9914 | 2.9870 | 3.9827 | 4.9784 | 5.9741 | 6.9697 | 7.9654 | 8.9611 | 1.3980 |
| 07 | 0.9956 | 1.9913 | 2.9869 | 3.9826 | 4.9782 | 5.9739 | 6.9695 | 7.9652 | 8.9608 | 1.3980 |
| 08 | 0.9956 | 1.9912 | 2.9868 | 3.9825 | 4.9781 | 5.9737 | 6.9693 | 7.9649 | 8.9605 | 1.3979 |
| 09 | 0.9956 | 1.9912 | 2.9868 | 3.9823 | 4.9779 | 5.9735 | 6.9691 | 7.9647 | 8.9603 | 1.3979 |
| 10 | 0.9956 | 1.9911 | 2.9867 | 3.9822 | 4.9778 | 5.9733 | 6.9689 | 7.9644 | 8.9600 | 1.3979 |
| 11 | 0.9955 | 1.9910 | 2.9866 | 3.9821 | 4.9776 | 5.9731 | 6.9686 | 7.9642 | 8.9597 | 1.3979 |
| 12 | 0.9955 | 1.9910 | 2.9865 | 3.9819 | 4.9774 | 5.9729 | 6.9684 | 7.9639 | 8.9594 | 1.3978 |
| 13 | 0.9955 | 1.9909 | 2.9864 | 3.9818 | 4.9773 | 5.9727 | 6.9682 | 7.9636 | 8.9591 | 1.3978 |
| 14 | 0.9954 | 1.9908 | 2.9863 | 3.9817 | 4.9771 | 5.9725 | 6.9679 | 7.9634 | 8.9588 | 1.3978 |
| 15 | 0.9954 | 1.9908 | 2.9862 | 3.9816 | 4.9769 | 5.9723 | 6.9677 | 7.9631 | 8.9585 | 1.3978 |
| 16 | 0.9954 | 1.9907 | 2.9861 | 3.9814 | 4.9768 | 5.9721 | 6.9675 | 7.9628 | 8.9582 | 1.3977 |
| 17 | 0.9953 | 1.9906 | 2.9860 | 3.9813 | 4.9766 | 5.9719 | 6.9673 | 7.9626 | 8.9579 | 1.3977 |
| 18 | 0.9953 | 1.9906 | 2.9859 | 3.9812 | 4.9764 | 5.9717 | 6.9670 | 7.9623 | 8.9576 | 1.3977 |
| 19 | 0.9953 | 1.9905 | 2.9858 | 3.9810 | 4.9763 | 5.9715 | 6.9668 | 7.9621 | 8.9573 | 1.3977 |
| 20 | 0.9952 | 1.9904 | 2.9857 | 3.9809 | 4.9761 | 5.9713 | 6.9666 | 7.9618 | 8.9570 | 1.3976 |
| 21 | 0.9952 | 1.9904 | 2.9856 | 3.9808 | 4.9759 | 5.9711 | 6.9663 | 7.9615 | 8.9567 | 1.3976 |
| 22 | 0.9952 | 1.9903 | 2.9855 | 3.9806 | 4.9758 | 5.9709 | 6.9661 | 7.9612 | 8.9564 | 1.3976 |
| 23 | 0.9951 | 1.9902 | 2.9854 | 3.9805 | 4.9756 | 5.9707 | 6.9658 | 7.9610 | 8.9561 | 1.3976 |
| 24 | 0.9951 | 1.9902 | 2.9853 | 3.9803 | 4.9754 | 5.9705 | 6.9656 | 7.9607 | 8.9558 | 1.3975 |
| 25 | 0.9951 | 1.9901 | 2.9852 | 3.9802 | 4.9753 | 5.9703 | 6.9654 | 7.9604 | 8.9555 | 1.3975 |
| 26 | 0.9950 | 1.9900 | 2.9850 | 3.9801 | 4.9751 | 5.9701 | 6.9651 | 7.9601 | 8.9551 | 1.3975 |
| 27 | 0.9950 | 1.9900 | 2.9849 | 3.9799 | 4.9749 | 5.9699 | 6.9649 | 7.9599 | 8.9548 | 1.3975 |
| 28 | 0.9949 | 1.9899 | 2.9848 | 3.9798 | 4.9747 | 5.9697 | 6.9646 | 7.9596 | 8.9545 | 1.3974 |
| 29 | 0.9949 | 1.9898 | 2.9847 | 3.9797 | 4.9746 | 5.9695 | 6.9644 | 7.9595 | 8.9542 | 1.3974 |
| 30 | 0.9949 | 1.9898 | 2.9846 | 3.9795 | 4.9744 | 5.9693 | 6.9641 | 7.9590 | 8.9539 | 1.3974 |
| 31 | 0.9948 | 1.9897 | 2.9845 | 3.9794 | 4.9742 | 5.9691 | 6.9639 | 7.9587 | 8.9536 | 1.3973 |
| 32 | 0.9948 | 1.9896 | 2.9844 | 3.9792 | 4.9740 | 5.9688 | 6.9636 | 7.9584 | 8.9533 | 1.3973 |
| 33 | 0.9948 | 1.9895 | 2.9843 | 3.9791 | 4.9738 | 5.9686 | 6.9634 | 7.9582 | 8.9529 | 1.3973 |
| 34 | 0.9947 | 1.9895 | 2.9842 | 3.9789 | 4.9737 | 5.9684 | 6.9631 | 7.9579 | 8.9526 | 1.3973 |
| 35 | 0.9947 | 1.9894 | 2.9841 | 3.9788 | 4.9735 | 5.9682 | 6.9629 | 7.9576 | 8.9523 | 1.3972 |
| 36 | 0.9947 | 1.9893 | 2.9840 | 3.9786 | 4.9733 | 5.9680 | 6.9626 | 7.9573 | 8.9519 | 1.3972 |
| 37 | 0.9946 | 1.9893 | 2.9839 | 3.9785 | 4.9731 | 5.9678 | 6.9624 | 7.9570 | 8.9516 | 1.3972 |
| 38 | 0.9946 | 1.9892 | 2.9838 | 3.9784 | 4.9729 | 5.9675 | 6.9621 | 7.9567 | 8.9513 | 1.3972 |
| 39 | 0.9946 | 1.9891 | 2.9837 | 3.9782 | 4.9728 | 5.9673 | 6.9619 | 7.9564 | 8.9510 | 1.3971 |
| 40 | 0.9945 | 1.9890 | 2.9835 | 3.9781 | 4.9726 | 5.9671 | 6.9616 | 7.9561 | 8.9506 | 1.3971 |
| 41 | 0.9945 | 1.9890 | 2.9834 | 3.9779 | 4.9724 | 5.9669 | 6.9613 | 7.9558 | 8.9503 | 1.3971 |
| 42 | 0.9944 | 1.9889 | 2.9833 | 3.9778 | 4.9722 | 5.9666 | 6.9611 | 7.9555 | 8.9500 | 1.3971 |
| 43 | 0.9944 | 1.9888 | 2.9832 | 3.9776 | 4.9720 | 5.9664 | 6.9608 | 7.9552 | 8.9496 | 1.3970 |
| 44 | 0.9944 | 1.9887 | 2.9831 | 3.9775 | 4.9718 | 5.9662 | 6.9605 | 7.9549 | 8.9493 | 1.3970 |
| 45 | 0.9943 | 1.9887 | 2.9830 | 3.9773 | 4.9716 | 5.9660 | 6.9603 | 7.9546 | 8.9489 | 1.3970 |
| 46 | 0.9943 | 1.9886 | 2.9829 | 3.9772 | 4.9714 | 5.9657 | 6.9600 | 7.9543 | 8.9486 | 1.3969 |
| 47 | 0.9943 | 1.9885 | 2.9828 | 3.9770 | 4.9713 | 5.9655 | 6.9598 | 7.9540 | 8.9483 | 1.3969 |
| 48 | 0.9942 | 1.9884 | 2.9826 | 3.9769 | 4.9711 | 5.9653 | 6.9595 | 7.9537 | 8.9479 | 1.3969 |
| 49 | 0.9942 | 1.9884 | 2.9825 | 3.9767 | 4.9709 | 5.9651 | 6.9592 | 7.9534 | 8.9476 | 1.3969 |
| 50 | 0.9941 | 1.9883 | 2.9824 | 3.9765 | 4.9707 | 5.9648 | 6.9590 | 7.9531 | 8.9472 | 1.3968 |
| 51 | 0.9941 | 1.9882 | 2.9823 | 3.9764 | 4.9705 | 5.9646 | 6.9587 | 7.9528 | 8.9469 | 1.3968 |
| 52 | 0.9941 | 1.9881 | 2.9822 | 3.9762 | 4.9703 | 5.9643 | 6.9584 | 7.9525 | 8.9465 | 1.3968 |
| 53 | 0.9940 | 1.9880 | 2.9821 | 3.9761 | 4.9701 | 5.9641 | 6.9581 | 7.9521 | 8.9462 | 1.3968 |
| 54 | 0.9940 | 1.9880 | 2.9819 | 3.9759 | 4.9699 | 5.9639 | 6.9579 | 7.9518 | 8.9458 | 1.3967 |
| 55 | 0.9939 | 1.9879 | 2.9818 | 3.9758 | 4.9697 | 5.9636 | 6.9576 | 7.9515 | 8.9455 | 1.3967 |
| 56 | 0.9939 | 1.9878 | 2.9817 | 3.9756 | 4.9695 | 5.9634 | 6.9573 | 7.9512 | 8.9451 | 1.3967 |
| 57 | 0.9939 | 1.9877 | 2.9816 | 3.9754 | 4.9693 | 5.9632 | 6.9570 | 7.9509 | 8.9447 | 1.3967 |
| 58 | 0.9938 | 1.9876 | 2.9815 | 3.9753 | 4.9691 | 5.9629 | 6.9567 | 7.9506 | 8.9444 | 1.3966 |
| 59 | 0.9938 | 1.9876 | 2.9813 | 3.9751 | 4.9689 | 5.9627 | 6.9565 | 7.9502 | 8.9440 | 1.3966 |
| 60 | 0.9937 | 1.9875 | 2.9812 | 3.9750 | 4.9687 | 5.9624 | 6.9562 | 7.9499 | 8.9437 | 1.3966 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0522 | 0.1044 | 0.1566 | 0.2088 | 0.2610 | 0.3131 | 0.3653 | 0.4175 | 0.4697 | 0.0733 | 00 |
| 0.0525 | 0.1050 | 0.1574 | 0.2099 | 0.2624 | 0.3149 | 0.3674 | 0.4198 | 0.4723 | 0.0737 | 01 |
| 0.0528 | 0.1055 | 0.1583 | 0.2111 | 0.2638 | 0.3166 | 0.3694 | 0.4222 | 0.4749 | 0.0741 | 02 |
| 0.0531 | 0.1061 | 0.1592 | 0.2122 | 0.2653 | 0.3184 | 0.3714 | 0.4245 | 0.4775 | 0.0745 | 03 |
| 0.0533 | 0.1067 | 0.1600 | 0.2134 | 0.2667 | 0.3201 | 0.3734 | 0.4268 | 0.4801 | 0.0749 | 04 |
| 0.0536 | 0.1073 | 0.1609 | 0.2145 | 0.2682 | 0.3218 | 0.3754 | 0.4291 | 0.4827 | 0.0753 | 05 |
| 0.0539 | 0.1078 | 0.1618 | 0.2157 | 0.2696 | 0.3235 | 0.3774 | 0.4314 | 0.4853 | 0.0757 | 06 |
| 0.0542 | 0.1084 | 0.1626 | 0.2168 | 0.2711 | 0.3253 | 0.3795 | 0.4337 | 0.4879 | 0.0761 | 07 |
| 0.0545 | 0.1090 | 0.1635 | 0.2180 | 0.2725 | 0.3270 | 0.3815 | 0.4360 | 0.4905 | 0.0765 | 08 |
| 0.0548 | 0.1096 | 0.1644 | 0.2192 | 0.2739 | 0.3287 | 0.3835 | 0.4383 | 0.4931 | 0.0769 | 09 |
| 0.0551 | 0.1102 | 0.1652 | 0.2203 | 0.2754 | 0.3305 | 0.3856 | 0.4406 | 0.4957 | 0.0773 | 10 |
| 0.0554 | 0.1107 | 0.1661 | 0.2215 | 0.2768 | 0.3322 | 0.3876 | 0.4430 | 0.4983 | 0.0777 | 11 |
| 0.0557 | 0.1113 | 0.1670 | 0.2226 | 0.2783 | 0.3340 | 0.3896 | 0.4453 | 0.5009 | 0.0781 | 12 |
| 0.0559 | 0.1119 | 0.1678 | 0.2238 | 0.2797 | 0.3356 | 0.3916 | 0.4475 | 0.5035 | 0.0786 | 13 |
| 0.0562 | 0.1125 | 0.1687 | 0.2249 | 0.2812 | 0.3374 | 0.3936 | 0.4498 | 0.5061 | 0.0790 | 14 |
| 0.0565 | 0.1130 | 0.1696 | 0.2261 | 0.2826 | 0.3391 | 0.3956 | 0.4522 | 0.5087 | 0.0794 | 15 |
| 0.0568 | 0.1136 | 0.1704 | 0.2272 | 0.2841 | 0.3409 | 0.3977 | 0.4545 | 0.5113 | 0.0798 | 16 |
| 0.0571 | 0.1142 | 0.1713 | 0.2284 | 0.2855 | 0.3426 | 0.3997 | 0.4568 | 0.5139 | 0.0802 | 17 |
| 0.0574 | 0.1148 | 0.1722 | 0.2296 | 0.2869 | 0.3443 | 0.4017 | 0.4591 | 0.5165 | 0.0806 | 18 |
| 0.0577 | 0.1154 | 0.1730 | 0.2307 | 0.2884 | 0.3461 | 0.4038 | 0.4614 | 0.5191 | 0.0810 | 19 |
| 0.0580 | 0.1159 | 0.1739 | 0.2319 | 0.2898 | 0.3478 | 0.4058 | 0.4638 | 0.5217 | 0.0814 | 20 |
| 0.0583 | 0.1165 | 0.1748 | 0.2330 | 0.2913 | 0.3495 | 0.4078 | 0.4660 | 0.5243 | 0.0818 | 21 |
| 0.0585 | 0.1171 | 0.1756 | 0.2342 | 0.2927 | 0.3512 | 0.4098 | 0.4683 | 0.5269 | 0.0822 | 22 |
| 0.0588 | 0.1177 | 0.1765 | 0.2353 | 0.2942 | 0.3530 | 0.4118 | 0.4706 | 0.5295 | 0.0826 | 23 |
| 0.0591 | 0.1182 | 0.1774 | 0.2365 | 0.2956 | 0.3547 | 0.4138 | 0.4730 | 0.5321 | 0.0830 | 24 |
| 0.0594 | 0.1188 | 0.1782 | 0.2376 | 0.2971 | 0.3565 | 0.4159 | 0.4753 | 0.5347 | 0.0834 | 25 |
| 0.0597 | 0.1194 | 0.1791 | 0.2388 | 0.2985 | 0.3582 | 0.4179 | 0.4776 | 0.5373 | 0.0838 | 26 |
| 0.0600 | 0.1200 | 0.1799 | 0.2399 | 0.2999 | 0.3599 | 0.4199 | 0.4799 | 0.5399 | 0.0842 | 27 |
| 0.0603 | 0.1205 | 0.1808 | 0.2411 | 0.3014 | 0.3616 | 0.4219 | 0.4822 | 0.5425 | 0.0847 | 28 |
| 0.0606 | 0.1211 | 0.1817 | 0.2422 | 0.3028 | 0.3634 | 0.4239 | 0.4845 | 0.5451 | 0.0851 | 29 |
| 0.0608 | 0.1217 | 0.1825 | 0.2434 | 0.3042 | 0.3651 | 0.4259 | 0.4868 | 0.5477 | 0.0855 | 30 |
| 0.0611 | 0.1223 | 0.1834 | 0.2446 | 0.3057 | 0.3668 | 0.4280 | 0.4891 | 0.5503 | 0.0859 | 31 |
| 0.0614 | 0.1229 | 0.1843 | 0.2457 | 0.3071 | 0.3686 | 0.4300 | 0.4914 | 0.5529 | 0.0863 | 32 |
| 0.0617 | 0.1234 | 0.1851 | 0.2468 | 0.3086 | 0.3703 | 0.4320 | 0.4937 | 0.5554 | 0.0867 | 33 |
| 0.0620 | 0.1240 | 0.1860 | 0.2480 | 0.3100 | 0.3720 | 0.4340 | 0.4960 | 0.5580 | 0.0871 | 34 |
| 0.0623 | 0.1246 | 0.1869 | 0.2492 | 0.3115 | 0.3737 | 0.4360 | 0.4983 | 0.5606 | 0.0875 | 35 |
| 0.0626 | 0.1252 | 0.1877 | 0.2503 | 0.3129 | 0.3755 | 0.4381 | 0.5006 | 0.5632 | 0.0879 | 36 |
| 0.0629 | 0.1257 | 0.1886 | 0.2515 | 0.3143 | 0.3772 | 0.4401 | 0.5030 | 0.5658 | 0.0883 | 37 |
| 0.0632 | 0.1263 | 0.1895 | 0.2526 | 0.3158 | 0.3789 | 0.4421 | 0.5053 | 0.5684 | 0.0887 | 38 |
| 0.0634 | 0.1269 | 0.1903 | 0.2538 | 0.3172 | 0.3806 | 0.4441 | 0.5075 | 0.5710 | 0.0891 | 39 |
| 0.0637 | 0.1275 | 0.1912 | 0.2549 | 0.3187 | 0.3824 | 0.4461 | 0.5098 | 0.5736 | 0.0895 | 40 |
| 0.0640 | 0.1280 | 0.1921 | 0.2561 | 0.3201 | 0.3841 | 0.4481 | 0.5122 | 0.5762 | 0.0899 | 41 |
| 0.0643 | 0.1286 | 0.1929 | 0.2572 | 0.3215 | 0.3859 | 0.4502 | 0.5145 | 0.5788 | 0.0903 | 42 |
| 0.0646 | 0.1292 | 0.1938 | 0.2584 | 0.3230 | 0.3876 | 0.4522 | 0.5168 | 0.5814 | 0.0908 | 43 |
| 0.0649 | 0.1298 | 0.1946 | 0.2595 | 0.3244 | 0.3893 | 0.4542 | 0.5190 | 0.5839 | 0.0912 | 44 |
| 0.0652 | 0.1303 | 0.1955 | 0.2607 | 0.3259 | 0.3910 | 0.4562 | 0.5214 | 0.5865 | 0.0916 | 45 |
| 0.0655 | 0.1309 | 0.1964 | 0.2618 | 0.3273 | 0.3928 | 0.4582 | 0.5237 | 0.5891 | 0.0920 | 46 |
| 0.0657 | 0.1315 | 0.1972 | 0.2630 | 0.3287 | 0.3945 | 0.4602 | 0.5260 | 0.5917 | 0.0924 | 47 |
| 0.0660 | 0.1321 | 0.1981 | 0.2642 | 0.3302 | 0.3962 | 0.4622 | 0.5283 | 0.5943 | 0.0928 | 48 |
| 0.0663 | 0.1326 | 0.1990 | 0.2653 | 0.3316 | 0.3979 | 0.4642 | 0.5306 | 0.5969 | 0.0932 | 49 |
| 0.0666 | 0.1332 | 0.1998 | 0.2664 | 0.3331 | 0.3997 | 0.4663 | 0.5329 | 0.5995 | 0.0936 | 50 |
| 0.0669 | 0.1338 | 0.2007 | 0.2676 | 0.3345 | 0.4014 | 0.4683 | 0.5352 | 0.6021 | 0.0940 | 51 |
| 0.0672 | 0.1344 | 0.2016 | 0.2688 | 0.3359 | 0.4031 | 0.4703 | 0.5375 | 0.6047 | 0.0944 | 52 |
| 0.0675 | 0.1349 | 0.2024 | 0.2699 | 0.3374 | 0.4048 | 0.4723 | 0.5398 | 0.6073 | 0.0948 | 53 |
| 0.0678 | 0.1355 | 0.2033 | 0.2710 | 0.3388 | 0.4066 | 0.4743 | 0.5421 | 0.6099 | 0.0952 | 54 |
| 0.0681 | 0.1361 | 0.2042 | 0.2722 | 0.3403 | 0.4083 | 0.4764 | 0.5444 | 0.6125 | 0.0956 | 55 |
| 0.0683 | 0.1367 | 0.2050 | 0.2734 | 0.3417 | 0.4100 | 0.4784 | 0.5467 | 0.6151 | 0.0961 | 56 |
| 0.0686 | 0.1373 | 0.2059 | 0.2745 | 0.3431 | 0.4118 | 0.4804 | 0.5490 | 0.6177 | 0.0965 | 57 |
| 0.0689 | 0.1378 | 0.2067 | 0.2756 | 0.3446 | 0.4135 | 0.4824 | 0.5513 | 0.6202 | 0.0969 | 58 |
| 0.0692 | 0.1384 | 0.2076 | 0.2768 | 0.3460 | 0.4152 | 0.4844 | 0.5536 | 0.6228 | 0.0973 | 59 |
| 0.0695 | 0.1390 | 0.2085 | 0.2780 | 0.3474 | 0.4169 | 0.4864 | 0.5559 | 0.6254 | 0.0977 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9937 | 1.9875 | 2.9812 | 3.9750 | 4.9687 | 5.9624 | 6.9562 | 7.9499 | 8.9437 | 1.3966 |
| 01 | 0.9937 | 1.9874 | 2.9811 | 3.9748 | 4.9685 | 5.9622 | 6.9559 | 7.9496 | 8.9433 | 1.3966 |
| 02 | 0.9937 | 1.9873 | 2.9810 | 3.9746 | 4.9683 | 5.9619 | 6.9556 | 7.9493 | 8.9429 | 1.3965 |
| 03 | 0.9936 | 1.9872 | 2.9809 | 3.9745 | 4.9681 | 5.9617 | 6.9553 | 7.9489 | 8.9426 | 1.3965 |
| 04 | 0.9936 | 1.9872 | 2.9807 | 3.9743 | 4.9679 | 5.9615 | 6.9550 | 7.9486 | 8.9422 | 1.3965 |
| 05 | 0.9935 | 1.9871 | 2.9806 | 3.9741 | 4.9677 | 5.9612 | 6.9547 | 7.9483 | 8.9418 | 1.3965 |
| 06 | 0.9935 | 1.9870 | 2.9805 | 3.9740 | 4.9675 | 5.9610 | 6.9545 | 7.9479 | 8.9414 | 1.3964 |
| 07 | 0.9935 | 1.9869 | 2.9804 | 3.9738 | 4.9673 | 5.9607 | 6.9542 | 7.9476 | 8.9411 | 1.3964 |
| 08 | 0.9934 | 1.9868 | 2.9802 | 3.9736 | 4.9671 | 5.9605 | 6.9539 | 7.9473 | 8.9407 | 1.3964 |
| 09 | 0.9934 | 1.9867 | 2.9801 | 3.9735 | 4.9668 | 5.9602 | 6.9536 | 7.9470 | 8.9403 | 1.3963 |
| 10 | 0.9933 | 1.9867 | 2.9800 | 3.9734 | 4.9666 | 5.9600 | 6.9533 | 7.9466 | 8.9400 | 1.3963 |
| 11 | 0.9933 | 1.9866 | 2.9799 | 3.9731 | 4.9664 | 5.9597 | 6.9530 | 7.9463 | 8.9396 | 1.3963 |
| 12 | 0.9932 | 1.9865 | 2.9797 | 3.9730 | 4.9662 | 5.9595 | 6.9527 | 7.9459 | 8.9392 | 1.3963 |
| 13 | 0.9932 | 1.9864 | 2.9796 | 3.9728 | 4.9660 | 5.9592 | 6.9524 | 7.9456 | 8.9388 | 1.3962 |
| 14 | 0.9932 | 1.9863 | 2.9795 | 3.9726 | 4.9658 | 5.9589 | 6.9521 | 7.9452 | 8.9384 | 1.3962 |
| 15 | 0.9931 | 1.9862 | 2.9793 | 3.9725 | 4.9656 | 5.9587 | 6.9518 | 7.9449 | 8.9380 | 1.3962 |
| 16 | 0.9931 | 1.9861 | 2.9792 | 3.9723 | 4.9654 | 5.9584 | 6.9515 | 7.9446 | 8.9376 | 1.3962 |
| 17 | 0.9930 | 1.9861 | 2.9791 | 3.9721 | 4.9651 | 5.9582 | 6.9512 | 7.9442 | 8.9373 | 1.3961 |
| 18 | 0.9930 | 1.9860 | 2.9790 | 3.9719 | 4.9649 | 5.9579 | 6.9509 | 7.9439 | 8.9369 | 1.3961 |
| 19 | 0.9929 | 1.9859 | 2.9788 | 3.9718 | 4.9647 | 5.9577 | 6.9506 | 7.9435 | 8.9365 | 1.3961 |
| 20 | 0.9929 | 1.9858 | 2.9787 | 3.9716 | 4.9645 | 5.9574 | 6.9503 | 7.9432 | 8.9361 | 1.3960 |
| 21 | 0.9929 | 1.9857 | 2.9786 | 3.9714 | 4.9643 | 5.9571 | 6.9500 | 7.9428 | 8.9357 | 1.3960 |
| 22 | 0.9928 | 1.9856 | 2.9784 | 3.9712 | 4.9641 | 5.9569 | 6.9497 | 7.9425 | 8.9353 | 1.3960 |
| 23 | 0.9928 | 1.9855 | 2.9783 | 3.9711 | 4.9638 | 5.9566 | 6.9494 | 7.9421 | 8.9349 | 1.3959 |
| 24 | 0.9927 | 1.9854 | 2.9782 | 3.9709 | 4.9636 | 5.9563 | 6.9490 | 7.9418 | 8.9345 | 1.3959 |
| 25 | 0.9927 | 1.9854 | 2.9780 | 3.9707 | 4.9634 | 5.9561 | 6.9487 | 7.9414 | 8.9341 | 1.3959 |
| 26 | 0.9926 | 1.9853 | 2.9779 | 3.9705 | 4.9632 | 5.9558 | 6.9484 | 7.9410 | 8.9337 | 1.3958 |
| 27 | 0.9926 | 1.9852 | 2.9778 | 3.9703 | 4.9629 | 5.9555 | 6.9481 | 7.9407 | 8.9333 | 1.3958 |
| 28 | 0.9925 | 1.9851 | 2.9776 | 3.9702 | 4.9627 | 5.9553 | 6.9478 | 7.9403 | 8.9329 | 1.3958 |
| 29 | 0.9925 | 1.9850 | 2.9775 | 3.9700 | 4.9625 | 5.9550 | 6.9475 | 7.9400 | 8.9325 | 1.3958 |
| 30 | 0.9925 | 1.9849 | 2.9774 | 3.9698 | 4.9623 | 5.9547 | 6.9472 | 7.9396 | 8.9321 | 1.3957 |
| 31 | 0.9924 | 1.9848 | 2.9772 | 3.9696 | 4.9620 | 5.9544 | 6.9468 | 7.9393 | 8.9317 | 1.3957 |
| 32 | 0.9924 | 1.9847 | 2.9771 | 3.9694 | 4.9618 | 5.9542 | 6.9465 | 7.9389 | 8.9312 | 1.3957 |
| 33 | 0.9923 | 1.9846 | 2.9769 | 3.9693 | 4.9616 | 5.9539 | 6.9462 | 7.9385 | 8.9308 | 1.3956 |
| 34 | 0.9923 | 1.9845 | 2.9768 | 3.9691 | 4.9613 | 5.9536 | 6.9459 | 7.9381 | 8.9304 | 1.3956 |
| 35 | 0.9922 | 1.9844 | 2.9767 | 3.9689 | 4.9611 | 5.9533 | 6.9456 | 7.9378 | 8.9300 | 1.3956 |
| 36 | 0.9922 | 1.9844 | 2.9765 | 3.9687 | 4.9609 | 5.9531 | 6.9452 | 7.9374 | 8.9296 | 1.3955 |
| 37 | 0.9921 | 1.9843 | 2.9764 | 3.9685 | 4.9606 | 5.9528 | 6.9449 | 7.9370 | 8.9292 | 1.3955 |
| 38 | 0.9921 | 1.9842 | 2.9762 | 3.9683 | 4.9604 | 5.9525 | 6.9446 | 7.9367 | 8.9287 | 1.3955 |
| 39 | 0.9920 | 1.9841 | 2.9761 | 3.9681 | 4.9602 | 5.9522 | 6.9443 | 7.9363 | 8.9283 | 1.3954 |
| 40 | 0.9920 | 1.9840 | 2.9760 | 3.9680 | 4.9600 | 5.9519 | 6.9439 | 7.9359 | 8.9279 | 1.3954 |
| 41 | 0.9919 | 1.9839 | 2.9758 | 3.9678 | 4.9597 | 5.9517 | 6.9436 | 7.9355 | 8.9275 | 1.3954 |
| 42 | 0.9919 | 1.9838 | 2.9757 | 3.9676 | 4.9595 | 5.9514 | 6.9433 | 7.9352 | 8.9270 | 1.3953 |
| 43 | 0.9918 | 1.9837 | 2.9755 | 3.9674 | 4.9592 | 5.9511 | 6.9429 | 7.9348 | 8.9266 | 1.3953 |
| 44 | 0.9918 | 1.9836 | 2.9754 | 3.9672 | 4.9590 | 5.9508 | 6.9426 | 7.9344 | 8.9262 | 1.3953 |
| 45 | 0.9918 | 1.9835 | 2.9753 | 3.9670 | 4.9588 | 5.9505 | 6.9423 | 7.9340 | 8.9258 | 1.3952 |
| 46 | 0.9917 | 1.9834 | 2.9751 | 3.9668 | 4.9585 | 5.9502 | 6.9419 | 7.9336 | 8.9253 | 1.3952 |
| 47 | 0.9917 | 1.9833 | 2.9750 | 3.9666 | 4.9583 | 5.9499 | 6.9416 | 7.9332 | 8.9249 | 1.3952 |
| 48 | 0.9916 | 1.9832 | 2.9748 | 3.9664 | 4.9580 | 5.9496 | 6.9412 | 7.9329 | 8.9245 | 1.3951 |
| 49 | 0.9916 | 1.9831 | 2.9747 | 3.9662 | 4.9578 | 5.9494 | 6.9409 | 7.9325 | 8.9240 | 1.3951 |
| 50 | 0.9915 | 1.9830 | 2.9745 | 3.9660 | 4.9576 | 5.9491 | 6.9406 | 7.9321 | 8.9236 | 1.3951 |
| 51 | 0.9915 | 1.9829 | 2.9744 | 3.9658 | 4.9573 | 5.9488 | 6.9402 | 7.9317 | 8.9231 | 1.3950 |
| 52 | 0.9914 | 1.9828 | 2.9742 | 3.9656 | 4.9571 | 5.9485 | 6.9399 | 7.9313 | 8.9227 | 1.3950 |
| 53 | 0.9914 | 1.9827 | 2.9741 | 3.9654 | 4.9568 | 5.9482 | 6.9395 | 7.9309 | 8.9223 | 1.3950 |
| 54 | 0.9913 | 1.9826 | 2.9739 | 3.9653 | 4.9566 | 5.9479 | 6.9392 | 7.9305 | 8.9218 | 1.3949 |
| 55 | 0.9913 | 1.9825 | 2.9738 | 3.9651 | 4.9563 | 5.9476 | 6.9388 | 7.9301 | 8.9214 | 1.3949 |
| 56 | 0.9912 | 1.9824 | 2.9736 | 3.9649 | 4.9561 | 5.9473 | 6.9385 | 7.9297 | 8.9209 | 1.3949 |
| 57 | 0.9912 | 1.9823 | 2.9735 | 3.9647 | 4.9558 | 5.9470 | 6.9381 | 7.9293 | 8.9205 | 1.3948 |
| 58 | 0.9911 | 1.9822 | 2.9733 | 3.9645 | 4.9556 | 5.9467 | 6.9378 | 7.9289 | 8.9200 | 1.3948 |
| 59 | 0.9911 | 1.9821 | 2.9732 | 3.9643 | 4.9553 | 5.9464 | 6.9375 | 7.9285 | 8.9196 | 1.3948 |
| 60 | 0.9910 | 1.9820 | 2.9730 | 3.9641 | 4.9551 | 5.9461 | 6.9371 | 7.9281 | 8.9191 | 1.3947 |

| 4°     |        | HEIGHTS. |        |        |        |        |        |        |        |    | 97 |
|--------|--------|----------|--------|--------|--------|--------|--------|--------|--------|----|----|
| 1      | 2      | 3        | 4      | 5      | 6      | 7      | 8      | 9      | b      | /  |    |
| 0.0695 | 0.1390 | 0.2085   | 0.2780 | 0.3474 | 0.4169 | 0.4864 | 0.5559 | 0.6254 | 0.6977 | 00 |    |
| 0.0698 | 0.1396 | 0.2093   | 0.2791 | 0.3489 | 0.4187 | 0.4884 | 0.5582 | 0.6280 | 0.6981 | 01 |    |
| 0.0701 | 0.1401 | 0.2102   | 0.2802 | 0.3503 | 0.4204 | 0.4904 | 0.5605 | 0.6306 | 0.6985 | 02 |    |
| 0.0704 | 0.1407 | 0.2111   | 0.2814 | 0.3518 | 0.4221 | 0.4925 | 0.5628 | 0.6332 | 0.6989 | 03 |    |
| 0.0706 | 0.1413 | 0.2119   | 0.2826 | 0.3532 | 0.4238 | 0.4945 | 0.5651 | 0.6358 | 0.6993 | 04 |    |
| 0.0709 | 0.1419 | 0.2128   | 0.2837 | 0.3546 | 0.4256 | 0.4965 | 0.5674 | 0.6384 | 0.6997 | 05 |    |
| 0.0712 | 0.1424 | 0.2136   | 0.2848 | 0.3561 | 0.4273 | 0.4985 | 0.5697 | 0.6409 | 0.1001 | 06 |    |
| 0.0715 | 0.1430 | 0.2145   | 0.2860 | 0.3575 | 0.4290 | 0.5005 | 0.5720 | 0.6435 | 0.1005 | 07 |    |
| 0.0718 | 0.1436 | 0.2154   | 0.2872 | 0.3589 | 0.4307 | 0.5025 | 0.5743 | 0.6461 | 0.1009 | 08 |    |
| 0.0721 | 0.1442 | 0.2162   | 0.2883 | 0.3604 | 0.4325 | 0.5045 | 0.5766 | 0.6487 | 0.1013 | 09 |    |
| 0.0724 | 0.1447 | 0.2171   | 0.2894 | 0.3618 | 0.4342 | 0.5065 | 0.5789 | 0.6513 | 0.1017 | 10 |    |
| 0.0727 | 0.1453 | 0.2180   | 0.2906 | 0.3633 | 0.4359 | 0.5086 | 0.5812 | 0.6539 | 0.1021 | 11 |    |
| 0.0729 | 0.1459 | 0.2188   | 0.2918 | 0.3647 | 0.4376 | 0.5106 | 0.5835 | 0.6565 | 0.1025 | 12 |    |
| 0.0732 | 0.1465 | 0.2197   | 0.2929 | 0.3661 | 0.4394 | 0.5126 | 0.5858 | 0.6591 | 0.1029 | 13 |    |
| 0.0735 | 0.1470 | 0.2205   | 0.2940 | 0.3676 | 0.4411 | 0.5146 | 0.5881 | 0.6616 | 0.1033 | 14 |    |
| 0.0738 | 0.1476 | 0.2214   | 0.2952 | 0.3690 | 0.4428 | 0.5166 | 0.5904 | 0.6642 | 0.1037 | 15 |    |
| 0.0741 | 0.1482 | 0.2223   | 0.2964 | 0.3704 | 0.4445 | 0.5186 | 0.5927 | 0.6668 | 0.1041 | 16 |    |
| 0.0744 | 0.1488 | 0.2231   | 0.2975 | 0.3719 | 0.4463 | 0.5206 | 0.5950 | 0.6694 | 0.1046 | 17 |    |
| 0.0747 | 0.1493 | 0.2240   | 0.2986 | 0.3733 | 0.4480 | 0.5226 | 0.5973 | 0.6720 | 0.1050 | 18 |    |
| 0.0749 | 0.1499 | 0.2248   | 0.2998 | 0.3747 | 0.4497 | 0.5246 | 0.5996 | 0.6746 | 0.1054 | 19 |    |
| 0.0752 | 0.1505 | 0.2257   | 0.3010 | 0.3762 | 0.4514 | 0.5266 | 0.6019 | 0.6772 | 0.1058 | 20 |    |
| 0.0755 | 0.1510 | 0.2266   | 0.3021 | 0.3776 | 0.4531 | 0.5286 | 0.6042 | 0.6797 | 0.1062 | 21 |    |
| 0.0758 | 0.1516 | 0.2274   | 0.3032 | 0.3791 | 0.4549 | 0.5307 | 0.6065 | 0.6823 | 0.1066 | 22 |    |
| 0.0761 | 0.1522 | 0.2283   | 0.3044 | 0.3805 | 0.4566 | 0.5327 | 0.6088 | 0.6849 | 0.1070 | 23 |    |
| 0.0764 | 0.1528 | 0.2292   | 0.3056 | 0.3819 | 0.4583 | 0.5347 | 0.6111 | 0.6875 | 0.1074 | 24 |    |
| 0.0767 | 0.1533 | 0.2300   | 0.3067 | 0.3834 | 0.4600 | 0.5367 | 0.6134 | 0.6900 | 0.1078 | 25 |    |
| 0.0770 | 0.1539 | 0.2309   | 0.3078 | 0.3848 | 0.4618 | 0.5387 | 0.6157 | 0.6926 | 0.1082 | 26 |    |
| 0.0772 | 0.1545 | 0.2317   | 0.3090 | 0.3862 | 0.4635 | 0.5407 | 0.6180 | 0.6952 | 0.1086 | 27 |    |
| 0.0775 | 0.1551 | 0.2326   | 0.3101 | 0.3877 | 0.4652 | 0.5427 | 0.6203 | 0.6978 | 0.1090 | 28 |    |
| 0.0778 | 0.1556 | 0.2335   | 0.3113 | 0.3891 | 0.4669 | 0.5447 | 0.6226 | 0.7004 | 0.1094 | 29 |    |
| 0.0781 | 0.1562 | 0.2343   | 0.3124 | 0.3905 | 0.4687 | 0.5467 | 0.6249 | 0.7030 | 0.1098 | 30 |    |
| 0.0784 | 0.1568 | 0.2352   | 0.3136 | 0.3920 | 0.4703 | 0.5487 | 0.6271 | 0.7055 | 0.1102 | 31 |    |
| 0.0787 | 0.1574 | 0.2360   | 0.3147 | 0.3934 | 0.4721 | 0.5508 | 0.6294 | 0.7081 | 0.1107 | 32 |    |
| 0.0790 | 0.1579 | 0.2369   | 0.3159 | 0.3948 | 0.4738 | 0.5528 | 0.6318 | 0.7107 | 0.1111 | 33 |    |
| 0.0793 | 0.1585 | 0.2378   | 0.3170 | 0.3963 | 0.4755 | 0.5548 | 0.6340 | 0.7133 | 0.1115 | 34 |    |
| 0.0795 | 0.1591 | 0.2386   | 0.3182 | 0.3977 | 0.4772 | 0.5568 | 0.6363 | 0.7159 | 0.1119 | 35 |    |
| 0.0798 | 0.1597 | 0.2395   | 0.3193 | 0.3991 | 0.4790 | 0.5588 | 0.6386 | 0.7185 | 0.1123 | 36 |    |
| 0.0801 | 0.1602 | 0.2403   | 0.3204 | 0.4007 | 0.4807 | 0.5608 | 0.6409 | 0.7210 | 0.1127 | 37 |    |
| 0.0804 | 0.1608 | 0.2412   | 0.3216 | 0.4020 | 0.4824 | 0.5628 | 0.6432 | 0.7236 | 0.1131 | 38 |    |
| 0.0807 | 0.1614 | 0.2421   | 0.3228 | 0.4034 | 0.4841 | 0.5648 | 0.6455 | 0.7262 | 0.1135 | 39 |    |
| 0.0810 | 0.1620 | 0.2429   | 0.3239 | 0.4049 | 0.4859 | 0.5668 | 0.6478 | 0.7288 | 0.1139 | 40 |    |
| 0.0813 | 0.1625 | 0.2438   | 0.3250 | 0.4063 | 0.4876 | 0.5688 | 0.6501 | 0.7313 | 0.1143 | 41 |    |
| 0.0815 | 0.1631 | 0.2446   | 0.3262 | 0.4077 | 0.4893 | 0.5708 | 0.6524 | 0.7339 | 0.1147 | 42 |    |
| 0.0818 | 0.1637 | 0.2455   | 0.3273 | 0.4092 | 0.4910 | 0.5728 | 0.6546 | 0.7365 | 0.1151 | 43 |    |
| 0.0821 | 0.1642 | 0.2464   | 0.3285 | 0.4106 | 0.4927 | 0.5748 | 0.6570 | 0.7391 | 0.1155 | 44 |    |
| 0.0824 | 0.1648 | 0.2472   | 0.3296 | 0.4120 | 0.4945 | 0.5768 | 0.6593 | 0.7417 | 0.1159 | 45 |    |
| 0.0827 | 0.1654 | 0.2481   | 0.3308 | 0.4135 | 0.4961 | 0.5788 | 0.6615 | 0.7442 | 0.1163 | 46 |    |
| 0.0830 | 0.1660 | 0.2489   | 0.3319 | 0.4149 | 0.4979 | 0.5809 | 0.6638 | 0.7468 | 0.1167 | 47 |    |
| 0.0833 | 0.1665 | 0.2498   | 0.3331 | 0.4163 | 0.4996 | 0.5829 | 0.6662 | 0.7494 | 0.1171 | 48 |    |
| 0.0836 | 0.1671 | 0.2507   | 0.3342 | 0.4178 | 0.5013 | 0.5849 | 0.6684 | 0.7520 | 0.1176 | 49 |    |
| 0.0838 | 0.1677 | 0.2515   | 0.3354 | 0.4192 | 0.5030 | 0.5869 | 0.6707 | 0.7546 | 0.1180 | 50 |    |
| 0.0841 | 0.1683 | 0.2524   | 0.3365 | 0.4206 | 0.5048 | 0.5889 | 0.6730 | 0.7572 | 0.1184 | 51 |    |
| 0.0844 | 0.1688 | 0.2532   | 0.3376 | 0.4221 | 0.5065 | 0.5909 | 0.6753 | 0.7597 | 0.1188 | 52 |    |
| 0.0847 | 0.1694 | 0.2541   | 0.3388 | 0.4235 | 0.5082 | 0.5929 | 0.6776 | 0.7623 | 0.1192 | 53 |    |
| 0.0850 | 0.1700 | 0.2549   | 0.3399 | 0.4249 | 0.5099 | 0.5949 | 0.6798 | 0.7648 | 0.1196 | 54 |    |
| 0.0853 | 0.1705 | 0.2558   | 0.3411 | 0.4264 | 0.5116 | 0.5969 | 0.6822 | 0.7674 | 0.1200 | 55 |    |
| 0.0856 | 0.1711 | 0.2567   | 0.3422 | 0.4278 | 0.5134 | 0.5989 | 0.6845 | 0.7700 | 0.1204 | 56 |    |
| 0.0858 | 0.1717 | 0.2575   | 0.3434 | 0.4292 | 0.5150 | 0.6009 | 0.6867 | 0.7726 | 0.1208 | 57 |    |
| 0.0861 | 0.1723 | 0.2584   | 0.3445 | 0.4306 | 0.5168 | 0.6029 | 0.6890 | 0.7752 | 0.1212 | 58 |    |
| 0.0864 | 0.1728 | 0.2593   | 0.3457 | 0.4321 | 0.5185 | 0.6049 | 0.6914 | 0.7778 | 0.1216 | 59 |    |
| 0.0867 | 0.1734 | 0.2601   | 0.3468 | 0.4335 | 0.5202 | 0.6069 | 0.6936 | 0.7803 | 0.1220 | 60 |    |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9937 | 1.9875 | 2.9812 | 3.9750 | 4.9687 | 5.9624 | 6.9562 | 7.9499 | 8.9437 | 1.3966 |
| 01 | 0.9937 | 1.9874 | 2.9811 | 3.9748 | 4.9685 | 5.9622 | 6.9559 | 7.9496 | 8.9433 | 1.3966 |
| 02 | 0.9937 | 1.9873 | 2.9810 | 3.9746 | 4.9683 | 5.9619 | 6.9556 | 7.9493 | 8.9429 | 1.3965 |
| 03 | 0.9936 | 1.9872 | 2.9809 | 3.9745 | 4.9681 | 5.9617 | 6.9553 | 7.9489 | 8.9426 | 1.3965 |
| 04 | 0.9936 | 1.9872 | 2.9807 | 3.9743 | 4.9679 | 5.9615 | 6.9550 | 7.9486 | 8.9422 | 1.3965 |
| 05 | 0.9935 | 1.9871 | 2.9806 | 3.9741 | 4.9677 | 5.9612 | 6.9547 | 7.9483 | 8.9418 | 1.3965 |
| 06 | 0.9935 | 1.9870 | 2.9805 | 3.9740 | 4.9675 | 5.9610 | 6.9545 | 7.9479 | 8.9414 | 1.3964 |
| 07 | 0.9935 | 1.9869 | 2.9804 | 3.9738 | 4.9673 | 5.9607 | 6.9542 | 7.9476 | 8.9411 | 1.3964 |
| 08 | 0.9934 | 1.9868 | 2.9802 | 3.9736 | 4.9671 | 5.9605 | 6.9539 | 7.9473 | 8.9407 | 1.3964 |
| 09 | 0.9934 | 1.9867 | 2.9801 | 3.9735 | 4.9668 | 5.9602 | 6.9536 | 7.9470 | 8.9403 | 1.3963 |
| 10 | 0.9933 | 1.9867 | 2.9800 | 3.9734 | 4.9666 | 5.9600 | 6.9533 | 7.9466 | 8.9400 | 1.3963 |
| 11 | 0.9933 | 1.9866 | 2.9799 | 3.9731 | 4.9664 | 5.9597 | 6.9530 | 7.9463 | 8.9396 | 1.3963 |
| 12 | 0.9932 | 1.9865 | 2.9797 | 3.9730 | 4.9662 | 5.9595 | 6.9527 | 7.9459 | 8.9392 | 1.3963 |
| 13 | 0.9932 | 1.9864 | 2.9796 | 3.9728 | 4.9660 | 5.9592 | 6.9524 | 7.9456 | 8.9388 | 1.3962 |
| 14 | 0.9932 | 1.9863 | 2.9795 | 3.9726 | 4.9658 | 5.9589 | 6.9521 | 7.9452 | 8.9384 | 1.3962 |
| 15 | 0.9931 | 1.9862 | 2.9793 | 3.9725 | 4.9656 | 5.9587 | 6.9518 | 7.9449 | 8.9380 | 1.3962 |
| 16 | 0.9931 | 1.9861 | 2.9792 | 3.9723 | 4.9654 | 5.9584 | 6.9515 | 7.9446 | 8.9376 | 1.3962 |
| 17 | 0.9930 | 1.9861 | 2.9791 | 3.9721 | 4.9651 | 5.9582 | 6.9512 | 7.9442 | 8.9373 | 1.3961 |
| 18 | 0.9930 | 1.9860 | 2.9790 | 3.9719 | 4.9649 | 5.9579 | 6.9509 | 7.9439 | 8.9369 | 1.3961 |
| 19 | 0.9929 | 1.9859 | 2.9788 | 3.9718 | 4.9647 | 5.9577 | 6.9506 | 7.9435 | 8.9365 | 1.3961 |
| 20 | 0.9929 | 1.9858 | 2.9787 | 3.9716 | 4.9645 | 5.9574 | 6.9503 | 7.9432 | 8.9361 | 1.3960 |
| 21 | 0.9929 | 1.9857 | 2.9786 | 3.9714 | 4.9643 | 5.9571 | 6.9500 | 7.9428 | 8.9357 | 1.3960 |
| 22 | 0.9928 | 1.9856 | 2.9784 | 3.9712 | 4.9641 | 5.9569 | 6.9497 | 7.9425 | 8.9353 | 1.3960 |
| 23 | 0.9928 | 1.9855 | 2.9783 | 3.9711 | 4.9638 | 5.9566 | 6.9494 | 7.9421 | 8.9349 | 1.3959 |
| 24 | 0.9927 | 1.9854 | 2.9782 | 3.9709 | 4.9636 | 5.9563 | 6.9490 | 7.9418 | 8.9345 | 1.3959 |
| 25 | 0.9927 | 1.9854 | 2.9780 | 3.9707 | 4.9634 | 5.9561 | 6.9487 | 7.9414 | 8.9341 | 1.3959 |
| 26 | 0.9926 | 1.9853 | 2.9779 | 3.9705 | 4.9632 | 5.9558 | 6.9484 | 7.9410 | 8.9337 | 1.3958 |
| 27 | 0.9926 | 1.9852 | 2.9778 | 3.9703 | 4.9629 | 5.9555 | 6.9481 | 7.9407 | 8.9333 | 1.3958 |
| 28 | 0.9925 | 1.9851 | 2.9776 | 3.9702 | 4.9627 | 5.9553 | 6.9478 | 7.9403 | 8.9329 | 1.3958 |
| 29 | 0.9925 | 1.9850 | 2.9775 | 3.9700 | 4.9625 | 5.9550 | 6.9475 | 7.9400 | 8.9325 | 1.3958 |
| 30 | 0.9925 | 1.9849 | 2.9774 | 3.9698 | 4.9623 | 5.9547 | 6.9472 | 7.9396 | 8.9321 | 1.3957 |
| 31 | 0.9924 | 1.9848 | 2.9772 | 3.9696 | 4.9620 | 5.9544 | 6.9468 | 7.9393 | 8.9317 | 1.3957 |
| 32 | 0.9924 | 1.9847 | 2.9771 | 3.9694 | 4.9618 | 5.9542 | 6.9465 | 7.9389 | 8.9312 | 1.3957 |
| 33 | 0.9923 | 1.9846 | 2.9769 | 3.9693 | 4.9616 | 5.9539 | 6.9462 | 7.9385 | 8.9308 | 1.3956 |
| 34 | 0.9923 | 1.9845 | 2.9768 | 3.9691 | 4.9613 | 5.9536 | 6.9459 | 7.9381 | 8.9304 | 1.3956 |
| 35 | 0.9922 | 1.9844 | 2.9767 | 3.9689 | 4.9611 | 5.9533 | 6.9456 | 7.9378 | 8.9300 | 1.3956 |
| 36 | 0.9922 | 1.9844 | 2.9765 | 3.9687 | 4.9609 | 5.9531 | 6.9452 | 7.9374 | 8.9296 | 1.3955 |
| 37 | 0.9921 | 1.9843 | 2.9764 | 3.9685 | 4.9606 | 5.9528 | 6.9449 | 7.9370 | 8.9292 | 1.3955 |
| 38 | 0.9921 | 1.9842 | 2.9762 | 3.9683 | 4.9604 | 5.9525 | 6.9446 | 7.9367 | 8.9287 | 1.3955 |
| 39 | 0.9920 | 1.9841 | 2.9761 | 3.9681 | 4.9602 | 5.9522 | 6.9443 | 7.9363 | 8.9283 | 1.3954 |
| 40 | 0.9920 | 1.9840 | 2.9760 | 3.9680 | 4.9600 | 5.9519 | 6.9439 | 7.9359 | 8.9279 | 1.3954 |
| 41 | 0.9919 | 1.9839 | 2.9758 | 3.9678 | 4.9597 | 5.9517 | 6.9436 | 7.9355 | 8.9275 | 1.3954 |
| 42 | 0.9919 | 1.9838 | 2.9757 | 3.9676 | 4.9595 | 5.9514 | 6.9433 | 7.9352 | 8.9270 | 1.3953 |
| 43 | 0.9918 | 1.9837 | 2.9755 | 3.9674 | 4.9592 | 5.9511 | 6.9429 | 7.9348 | 8.9266 | 1.3953 |
| 44 | 0.9918 | 1.9836 | 2.9754 | 3.9672 | 4.9590 | 5.9508 | 6.9426 | 7.9344 | 8.9262 | 1.3953 |
| 45 | 0.9918 | 1.9835 | 2.9753 | 3.9670 | 4.9588 | 5.9505 | 6.9423 | 7.9340 | 8.9258 | 1.3952 |
| 46 | 0.9917 | 1.9834 | 2.9751 | 3.9668 | 4.9585 | 5.9502 | 6.9419 | 7.9336 | 8.9253 | 1.3952 |
| 47 | 0.9917 | 1.9833 | 2.9750 | 3.9666 | 4.9583 | 5.9499 | 6.9416 | 7.9332 | 8.9249 | 1.3952 |
| 48 | 0.9916 | 1.9832 | 2.9748 | 3.9664 | 4.9580 | 5.9496 | 6.9412 | 7.9329 | 8.9245 | 1.3951 |
| 49 | 0.9916 | 1.9831 | 2.9747 | 3.9662 | 4.9578 | 5.9494 | 6.9409 | 7.9325 | 8.9240 | 1.3951 |
| 50 | 0.9915 | 1.9830 | 2.9745 | 3.9660 | 4.9576 | 5.9491 | 6.9406 | 7.9321 | 8.9236 | 1.3951 |
| 51 | 0.9915 | 1.9829 | 2.9744 | 3.9658 | 4.9573 | 5.9488 | 6.9402 | 7.9317 | 8.9231 | 1.3950 |
| 52 | 0.9914 | 1.9828 | 2.9742 | 3.9656 | 4.9571 | 5.9485 | 6.9399 | 7.9313 | 8.9227 | 1.3950 |
| 53 | 0.9914 | 1.9827 | 2.9741 | 3.9654 | 4.9568 | 5.9482 | 6.9395 | 7.9309 | 8.9223 | 1.3950 |
| 54 | 0.9913 | 1.9826 | 2.9739 | 3.9653 | 4.9566 | 5.9479 | 6.9392 | 7.9305 | 8.9218 | 1.3949 |
| 55 | 0.9913 | 1.9825 | 2.9738 | 3.9651 | 4.9563 | 5.9476 | 6.9388 | 7.9301 | 8.9214 | 1.3949 |
| 56 | 0.9912 | 1.9824 | 2.9736 | 3.9649 | 4.9561 | 5.9473 | 6.9385 | 7.9297 | 8.9209 | 1.3949 |
| 57 | 0.9912 | 1.9823 | 2.9735 | 3.9647 | 4.9558 | 5.9470 | 6.9381 | 7.9293 | 8.9205 | 1.3948 |
| 58 | 0.9911 | 1.9822 | 2.9733 | 3.9645 | 4.9556 | 5.9467 | 6.9378 | 7.9289 | 8.9200 | 1.3948 |
| 59 | 0.9911 | 1.9821 | 2.9732 | 3.9643 | 4.9553 | 5.9464 | 6.9375 | 7.9285 | 8.9196 | 1.3948 |
| 60 | 0.9910 | 1.9820 | 2.9730 | 3.9641 | 4.9551 | 5.9461 | 6.9371 | 7.9281 | 8.9191 | 1.3947 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0695 | 0.1390 | 0.2085 | 0.2780 | 0.3474 | 0.4169 | 0.4864 | 0.5559 | 0.6254 | 0.0977 | 00 |
| 0.0698 | 0.1396 | 0.2093 | 0.2791 | 0.3489 | 0.4187 | 0.4884 | 0.5582 | 0.6280 | 0.0981 | 01 |
| 0.0701 | 0.1401 | 0.2102 | 0.2802 | 0.3503 | 0.4204 | 0.4904 | 0.5605 | 0.6306 | 0.0985 | 02 |
| 0.0704 | 0.1407 | 0.2111 | 0.2814 | 0.3518 | 0.4221 | 0.4925 | 0.5628 | 0.6332 | 0.0989 | 03 |
| 0.0706 | 0.1413 | 0.2119 | 0.2826 | 0.3532 | 0.4238 | 0.4945 | 0.5651 | 0.6358 | 0.0993 | 04 |
| 0.0709 | 0.1419 | 0.2128 | 0.2837 | 0.3546 | 0.4256 | 0.4965 | 0.5674 | 0.6384 | 0.0997 | 05 |
| 0.0712 | 0.1424 | 0.2136 | 0.2848 | 0.3561 | 0.4273 | 0.4985 | 0.5697 | 0.6409 | 0.1001 | 06 |
| 0.0715 | 0.1430 | 0.2145 | 0.2860 | 0.3575 | 0.4290 | 0.5005 | 0.5720 | 0.6435 | 0.1005 | 07 |
| 0.0718 | 0.1436 | 0.2154 | 0.2872 | 0.3589 | 0.4307 | 0.5025 | 0.5743 | 0.6461 | 0.1009 | 08 |
| 0.0721 | 0.1442 | 0.2162 | 0.2883 | 0.3604 | 0.4325 | 0.5045 | 0.5766 | 0.6487 | 0.1013 | 09 |
| 0.0724 | 0.1447 | 0.2171 | 0.2894 | 0.3618 | 0.4342 | 0.5065 | 0.5789 | 0.6513 | 0.1017 | 10 |
| 0.0727 | 0.1453 | 0.2180 | 0.2906 | 0.3633 | 0.4359 | 0.5086 | 0.5812 | 0.6539 | 0.1021 | 11 |
| 0.0729 | 0.1459 | 0.2188 | 0.2918 | 0.3647 | 0.4376 | 0.5106 | 0.5835 | 0.6565 | 0.1025 | 12 |
| 0.0732 | 0.1465 | 0.2197 | 0.2929 | 0.3661 | 0.4394 | 0.5126 | 0.5858 | 0.6591 | 0.1029 | 13 |
| 0.0735 | 0.1470 | 0.2205 | 0.2940 | 0.3676 | 0.4411 | 0.5146 | 0.5881 | 0.6616 | 0.1033 | 14 |
| 0.0738 | 0.1476 | 0.2214 | 0.2952 | 0.3690 | 0.4428 | 0.5166 | 0.5904 | 0.6642 | 0.1037 | 15 |
| 0.0741 | 0.1482 | 0.2223 | 0.2964 | 0.3704 | 0.4445 | 0.5186 | 0.5927 | 0.6668 | 0.1041 | 16 |
| 0.0744 | 0.1488 | 0.2231 | 0.2975 | 0.3719 | 0.4463 | 0.5206 | 0.5950 | 0.6694 | 0.1046 | 17 |
| 0.0747 | 0.1493 | 0.2240 | 0.2986 | 0.3733 | 0.4480 | 0.5226 | 0.5973 | 0.6720 | 0.1050 | 18 |
| 0.0749 | 0.1499 | 0.2248 | 0.2998 | 0.3747 | 0.4497 | 0.5246 | 0.5996 | 0.6746 | 0.1054 | 19 |
| 0.0752 | 0.1505 | 0.2257 | 0.3010 | 0.3762 | 0.4514 | 0.5266 | 0.6019 | 0.6772 | 0.1058 | 20 |
| 0.0755 | 0.1510 | 0.2266 | 0.3021 | 0.3776 | 0.4531 | 0.5286 | 0.6042 | 0.6797 | 0.1062 | 21 |
| 0.0758 | 0.1516 | 0.2274 | 0.3032 | 0.3791 | 0.4549 | 0.5307 | 0.6065 | 0.6823 | 0.1066 | 22 |
| 0.0761 | 0.1522 | 0.2283 | 0.3044 | 0.3805 | 0.4566 | 0.5327 | 0.6088 | 0.6849 | 0.1070 | 23 |
| 0.0764 | 0.1528 | 0.2292 | 0.3056 | 0.3819 | 0.4583 | 0.5347 | 0.6111 | 0.6875 | 0.1074 | 24 |
| 0.0767 | 0.1533 | 0.2300 | 0.3067 | 0.3834 | 0.4600 | 0.5367 | 0.6134 | 0.6900 | 0.1078 | 25 |
| 0.0770 | 0.1539 | 0.2309 | 0.3078 | 0.3848 | 0.4618 | 0.5387 | 0.6157 | 0.6926 | 0.1082 | 26 |
| 0.0772 | 0.1545 | 0.2317 | 0.3090 | 0.3862 | 0.4635 | 0.5407 | 0.6180 | 0.6952 | 0.1086 | 27 |
| 0.0775 | 0.1551 | 0.2326 | 0.3101 | 0.3877 | 0.4652 | 0.5427 | 0.6203 | 0.6978 | 0.1090 | 28 |
| 0.0778 | 0.1556 | 0.2335 | 0.3113 | 0.3891 | 0.4669 | 0.5447 | 0.6226 | 0.7004 | 0.1094 | 29 |
| 0.0781 | 0.1562 | 0.2343 | 0.3124 | 0.3905 | 0.4687 | 0.5467 | 0.6249 | 0.7030 | 0.1098 | 30 |
| 0.0784 | 0.1568 | 0.2352 | 0.3136 | 0.3920 | 0.4703 | 0.5487 | 0.6271 | 0.7055 | 0.1102 | 31 |
| 0.0787 | 0.1574 | 0.2360 | 0.3147 | 0.3934 | 0.4721 | 0.5508 | 0.6294 | 0.7081 | 0.1107 | 32 |
| 0.0790 | 0.1579 | 0.2369 | 0.3159 | 0.3948 | 0.4738 | 0.5528 | 0.6318 | 0.7107 | 0.1111 | 33 |
| 0.0793 | 0.1585 | 0.2378 | 0.3170 | 0.3963 | 0.4755 | 0.5548 | 0.6340 | 0.7133 | 0.1115 | 34 |
| 0.0795 | 0.1591 | 0.2386 | 0.3182 | 0.3977 | 0.4772 | 0.5568 | 0.6363 | 0.7159 | 0.1119 | 35 |
| 0.0798 | 0.1597 | 0.2395 | 0.3193 | 0.3991 | 0.4790 | 0.5588 | 0.6386 | 0.7185 | 0.1123 | 36 |
| 0.0801 | 0.1602 | 0.2403 | 0.3204 | 0.4007 | 0.4807 | 0.5608 | 0.6409 | 0.7210 | 0.1127 | 37 |
| 0.0804 | 0.1608 | 0.2412 | 0.3216 | 0.4020 | 0.4824 | 0.5628 | 0.6432 | 0.7236 | 0.1131 | 38 |
| 0.0807 | 0.1614 | 0.2421 | 0.3228 | 0.4034 | 0.4841 | 0.5648 | 0.6455 | 0.7262 | 0.1135 | 39 |
| 0.0810 | 0.1620 | 0.2429 | 0.3239 | 0.4049 | 0.4859 | 0.5668 | 0.6478 | 0.7288 | 0.1139 | 40 |
| 0.0813 | 0.1625 | 0.2438 | 0.3250 | 0.4063 | 0.4876 | 0.5688 | 0.6501 | 0.7313 | 0.1143 | 41 |
| 0.0815 | 0.1631 | 0.2446 | 0.3262 | 0.4077 | 0.4893 | 0.5708 | 0.6524 | 0.7339 | 0.1147 | 42 |
| 0.0818 | 0.1637 | 0.2455 | 0.3273 | 0.4092 | 0.4910 | 0.5728 | 0.6546 | 0.7365 | 0.1151 | 43 |
| 0.0821 | 0.1642 | 0.2464 | 0.3285 | 0.4106 | 0.4927 | 0.5748 | 0.6570 | 0.7391 | 0.1155 | 44 |
| 0.0824 | 0.1648 | 0.2472 | 0.3296 | 0.4120 | 0.4945 | 0.5768 | 0.6593 | 0.7417 | 0.1159 | 45 |
| 0.0827 | 0.1654 | 0.2481 | 0.3308 | 0.4135 | 0.4961 | 0.5788 | 0.6615 | 0.7442 | 0.1163 | 46 |
| 0.0830 | 0.1660 | 0.2489 | 0.3319 | 0.4149 | 0.4979 | 0.5809 | 0.6638 | 0.7468 | 0.1167 | 47 |
| 0.0833 | 0.1665 | 0.2498 | 0.3331 | 0.4163 | 0.4996 | 0.5829 | 0.6662 | 0.7494 | 0.1171 | 48 |
| 0.0836 | 0.1671 | 0.2507 | 0.3342 | 0.4178 | 0.5013 | 0.5849 | 0.6684 | 0.7520 | 0.1176 | 49 |
| 0.0838 | 0.1677 | 0.2515 | 0.3354 | 0.4192 | 0.5030 | 0.5869 | 0.6707 | 0.7546 | 0.1180 | 50 |
| 0.0841 | 0.1683 | 0.2524 | 0.3365 | 0.4206 | 0.5048 | 0.5889 | 0.6730 | 0.7572 | 0.1184 | 51 |
| 0.0844 | 0.1688 | 0.2532 | 0.3376 | 0.4221 | 0.5065 | 0.5909 | 0.6753 | 0.7597 | 0.1188 | 52 |
| 0.0847 | 0.1694 | 0.2541 | 0.3388 | 0.4235 | 0.5082 | 0.5929 | 0.6776 | 0.7623 | 0.1192 | 53 |
| 0.0850 | 0.1700 | 0.2549 | 0.3399 | 0.4249 | 0.5099 | 0.5949 | 0.6798 | 0.7648 | 0.1196 | 54 |
| 0.0853 | 0.1705 | 0.2558 | 0.3411 | 0.4264 | 0.5116 | 0.5969 | 0.6822 | 0.7674 | 0.1200 | 55 |
| 0.0856 | 0.1711 | 0.2567 | 0.3422 | 0.4278 | 0.5134 | 0.5989 | 0.6845 | 0.7700 | 0.1204 | 56 |
| 0.0858 | 0.1717 | 0.2575 | 0.3434 | 0.4292 | 0.5150 | 0.6009 | 0.6867 | 0.7726 | 0.1208 | 57 |
| 0.0861 | 0.1723 | 0.2584 | 0.3445 | 0.4306 | 0.5168 | 0.6029 | 0.6890 | 0.7752 | 0.1212 | 58 |
| 0.0864 | 0.1728 | 0.2593 | 0.3457 | 0.4321 | 0.5185 | 0.6049 | 0.6914 | 0.7778 | 0.1216 | 59 |
| 0.0867 | 0.1734 | 0.2601 | 0.3468 | 0.4335 | 0.5202 | 0.6069 | 0.6936 | 0.7803 | 0.1220 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | n      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9910 | 1.9820 | 2.9730 | 3.9641 | 4.9551 | 5.9461 | 6.9371 | 7.9281 | 8.9191 | 1.3947 |
| 01 | 0.9910 | 1.9819 | 2.9729 | 3.9639 | 4.9548 | 5.9458 | 6.9367 | 7.9277 | 8.9187 | 1.3947 |
| 02 | 0.9909 | 1.9818 | 2.9727 | 3.9636 | 4.9546 | 5.9455 | 6.9364 | 7.9273 | 8.9182 | 1.3946 |
| 03 | 0.9909 | 1.9817 | 2.9726 | 3.9634 | 4.9543 | 5.9452 | 6.9360 | 7.9269 | 8.9177 | 1.3946 |
| 04 | 0.9908 | 1.9816 | 2.9724 | 3.9632 | 4.9541 | 5.9449 | 6.9357 | 7.9265 | 8.9173 | 1.3946 |
| 05 | 0.9908 | 1.9815 | 2.9723 | 3.9630 | 4.9538 | 5.9446 | 6.9353 | 7.9261 | 8.9168 | 1.3945 |
| 06 | 0.9907 | 1.9814 | 2.9721 | 3.9628 | 4.9535 | 5.9442 | 6.9349 | 7.9257 | 8.9164 | 1.3945 |
| 07 | 0.9907 | 1.9813 | 2.9720 | 3.9626 | 4.9533 | 5.9439 | 6.9346 | 7.9252 | 8.9159 | 1.3944 |
| 08 | 0.9906 | 1.9812 | 2.9718 | 3.9624 | 4.9530 | 5.9436 | 6.9342 | 7.9248 | 8.9154 | 1.3944 |
| 09 | 0.9906 | 1.9811 | 2.9717 | 3.9622 | 4.9528 | 5.9433 | 6.9339 | 7.9244 | 8.9150 | 1.3944 |
| 10 | 0.9905 | 1.9810 | 2.9715 | 3.9620 | 4.9525 | 5.9430 | 6.9335 | 7.9240 | 8.9145 | 1.3943 |
| 11 | 0.9904 | 1.9809 | 2.9713 | 3.9618 | 4.9522 | 5.9427 | 6.9331 | 7.9236 | 8.9140 | 1.3943 |
| 12 | 0.9904 | 1.9808 | 2.9712 | 3.9616 | 4.9520 | 5.9424 | 6.9328 | 7.9232 | 8.9136 | 1.3942 |
| 13 | 0.9903 | 1.9807 | 2.9710 | 3.9614 | 4.9517 | 5.9421 | 6.9324 | 7.9227 | 8.9131 | 1.3942 |
| 14 | 0.9903 | 1.9806 | 2.9709 | 3.9612 | 4.9515 | 5.9417 | 6.9320 | 7.9223 | 8.9126 | 1.3941 |
| 15 | 0.9902 | 1.9805 | 2.9707 | 3.9610 | 4.9512 | 5.9414 | 6.9317 | 7.9219 | 8.9121 | 1.3941 |
| 16 | 0.9902 | 1.9804 | 2.9706 | 3.9607 | 4.9509 | 5.9411 | 6.9313 | 7.9215 | 8.9117 | 1.3941 |
| 17 | 0.9901 | 1.9803 | 2.9704 | 3.9605 | 4.9507 | 5.9408 | 6.9309 | 7.9211 | 8.9112 | 1.3940 |
| 18 | 0.9901 | 1.9802 | 2.9702 | 3.9603 | 4.9504 | 5.9405 | 6.9306 | 7.9206 | 8.9107 | 1.3940 |
| 19 | 0.9900 | 1.9801 | 2.9701 | 3.9601 | 4.9501 | 5.9402 | 6.9302 | 7.9202 | 8.9102 | 1.3940 |
| 20 | 0.9900 | 1.9799 | 2.9699 | 3.9599 | 4.9499 | 5.9398 | 6.9298 | 7.9198 | 8.9098 | 1.3939 |
| 21 | 0.9899 | 1.9798 | 2.9698 | 3.9597 | 4.9496 | 5.9395 | 6.9294 | 7.9193 | 8.9093 | 1.3939 |
| 22 | 0.9899 | 1.9797 | 2.9696 | 3.9595 | 4.9493 | 5.9392 | 6.9290 | 7.9189 | 8.9088 | 1.3938 |
| 23 | 0.9898 | 1.9796 | 2.9694 | 3.9592 | 4.9490 | 5.9389 | 6.9287 | 7.9185 | 8.9083 | 1.3938 |
| 24 | 0.9898 | 1.9795 | 2.9693 | 3.9590 | 4.9488 | 5.9385 | 6.9283 | 7.9180 | 8.9078 | 1.3938 |
| 25 | 0.9897 | 1.9794 | 2.9691 | 3.9588 | 4.9485 | 5.9382 | 6.9279 | 7.9176 | 8.9073 | 1.3937 |
| 26 | 0.9896 | 1.9793 | 2.9689 | 3.9586 | 4.9482 | 5.9379 | 6.9275 | 7.9172 | 8.9068 | 1.3937 |
| 27 | 0.9896 | 1.9792 | 2.9688 | 3.9584 | 4.9480 | 5.9375 | 6.9271 | 7.9167 | 8.9063 | 1.3936 |
| 28 | 0.9895 | 1.9791 | 2.9686 | 3.9581 | 4.9477 | 5.9372 | 6.9268 | 7.9163 | 8.9058 | 1.3936 |
| 29 | 0.9895 | 1.9790 | 2.9684 | 3.9579 | 4.9474 | 5.9369 | 6.9264 | 7.9159 | 8.9053 | 1.3936 |
| 30 | 0.9894 | 1.9789 | 2.9683 | 3.9577 | 4.9471 | 5.9366 | 6.9260 | 7.9154 | 8.9048 | 1.3935 |
| 31 | 0.9894 | 1.9787 | 2.9681 | 3.9575 | 4.9469 | 5.9362 | 6.9256 | 7.9150 | 8.9043 | 1.3935 |
| 32 | 0.9893 | 1.9786 | 2.9679 | 3.9573 | 4.9466 | 5.9359 | 6.9252 | 7.9145 | 8.9038 | 1.3934 |
| 33 | 0.9893 | 1.9783 | 2.9678 | 3.9570 | 4.9463 | 5.9355 | 6.9248 | 7.9141 | 8.9033 | 1.3934 |
| 34 | 0.9892 | 1.9784 | 2.9676 | 3.9568 | 4.9460 | 5.9352 | 6.9244 | 7.9136 | 8.9028 | 1.3934 |
| 35 | 0.9891 | 1.9783 | 2.9674 | 3.9566 | 4.9457 | 5.9349 | 6.9240 | 7.9132 | 8.9023 | 1.3933 |
| 36 | 0.9891 | 1.9782 | 2.9673 | 3.9564 | 4.9454 | 5.9345 | 6.9236 | 7.9127 | 8.9018 | 1.3933 |
| 37 | 0.9890 | 1.9781 | 2.9671 | 3.9561 | 4.9452 | 5.9342 | 6.9232 | 7.9123 | 8.9013 | 1.3932 |
| 38 | 0.9890 | 1.9780 | 2.9669 | 3.9559 | 4.9449 | 5.9339 | 6.9228 | 7.9118 | 8.9008 | 1.3932 |
| 39 | 0.9889 | 1.9778 | 2.9668 | 3.9557 | 4.9446 | 5.9335 | 6.9224 | 7.9114 | 8.9003 | 1.3932 |
| 40 | 0.9889 | 1.9777 | 2.9666 | 3.9555 | 4.9443 | 5.9332 | 6.9220 | 7.9109 | 8.9098 | 1.3931 |
| 41 | 0.9888 | 1.9776 | 2.9664 | 3.9552 | 4.9440 | 5.9328 | 6.9216 | 7.9104 | 8.9093 | 1.3931 |
| 42 | 0.9887 | 1.9775 | 2.9662 | 3.9550 | 4.9437 | 5.9325 | 6.9212 | 7.9100 | 8.9087 | 1.3930 |
| 43 | 0.9887 | 1.9774 | 2.9661 | 3.9548 | 4.9435 | 5.9321 | 6.9208 | 7.9095 | 8.9082 | 1.3930 |
| 44 | 0.9886 | 1.9773 | 2.9659 | 3.9545 | 4.9432 | 5.9318 | 6.9204 | 7.9091 | 8.9077 | 1.3930 |
| 45 | 0.9886 | 1.9772 | 2.9657 | 3.9543 | 4.9429 | 5.9315 | 6.9200 | 7.9086 | 8.9072 | 1.3929 |
| 46 | 0.9885 | 1.9770 | 2.9656 | 3.9541 | 4.9426 | 5.9311 | 6.9196 | 7.9081 | 8.9067 | 1.3929 |
| 47 | 0.9885 | 1.9769 | 2.9654 | 3.9538 | 4.9423 | 5.9308 | 6.9192 | 7.9077 | 8.9061 | 1.3928 |
| 48 | 0.9884 | 1.9768 | 2.9652 | 3.9536 | 4.9420 | 5.9304 | 6.9188 | 7.9072 | 8.9056 | 1.3928 |
| 49 | 0.9883 | 1.9767 | 2.9650 | 3.9534 | 4.9417 | 5.9300 | 6.9184 | 7.9067 | 8.9051 | 1.3928 |
| 50 | 0.9883 | 1.9766 | 2.9649 | 3.9531 | 4.9414 | 5.9297 | 6.9180 | 7.9063 | 8.9046 | 1.3927 |
| 51 | 0.9882 | 1.9765 | 2.9647 | 3.9529 | 4.9411 | 5.9294 | 6.9176 | 7.9058 | 8.9040 | 1.3927 |
| 52 | 0.9882 | 1.9763 | 2.9645 | 3.9527 | 4.9408 | 5.9290 | 6.9172 | 7.9053 | 8.9035 | 1.3926 |
| 53 | 0.9881 | 1.9762 | 2.9643 | 3.9524 | 4.9405 | 5.9286 | 6.9167 | 7.9048 | 8.9030 | 1.3926 |
| 54 | 0.9880 | 1.9761 | 2.9641 | 3.9522 | 4.9402 | 5.9283 | 6.9163 | 7.9044 | 8.9024 | 1.3926 |
| 55 | 0.9880 | 1.9760 | 2.9640 | 3.9519 | 4.9399 | 5.9279 | 6.9159 | 7.9039 | 8.9019 | 1.3925 |
| 56 | 0.9879 | 1.9759 | 2.9638 | 3.9517 | 4.9396 | 5.9276 | 6.9155 | 7.9034 | 8.9013 | 1.3925 |
| 57 | 0.9879 | 1.9757 | 2.9636 | 3.9515 | 4.9393 | 5.9272 | 6.9151 | 7.9029 | 8.9008 | 1.3924 |
| 58 | 0.9878 | 1.9756 | 2.9634 | 3.9512 | 4.9390 | 5.9268 | 6.9147 | 7.9025 | 8.9003 | 1.3924 |
| 59 | 0.9877 | 1.9755 | 2.9632 | 3.9510 | 4.9387 | 5.9265 | 6.9142 | 7.9020 | 8.9007 | 1.3924 |
| 60 | 0.9877 | 1.9754 | 2.9631 | 3.9508 | 4.9384 | 5.9261 | 6.9138 | 7.9015 | 8.9002 | 1.3923 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0867 | 0.1734 | 0.2601 | 0.3468 | 0.4335 | 0.5202 | 0.6069 | 0.6936 | 0.7803 | 0.1220 | 00 |
| 0.0870 | 0.1740 | 0.2610 | 0.3480 | 0.4349 | 0.5219 | 0.6089 | 0.6959 | 0.7829 | 0.1224 | 01 |
| 0.0873 | 0.1745 | 0.2618 | 0.3491 | 0.4364 | 0.5236 | 0.6109 | 0.6982 | 0.7854 | 0.1228 | 02 |
| 0.0876 | 0.1751 | 0.2627 | 0.3502 | 0.4378 | 0.5254 | 0.6129 | 0.7005 | 0.7880 | 0.1232 | 03 |
| 0.0878 | 0.1757 | 0.2635 | 0.3514 | 0.4392 | 0.5271 | 0.6149 | 0.7028 | 0.7906 | 0.1236 | 04 |
| 0.0881 | 0.1763 | 0.2644 | 0.3525 | 0.4407 | 0.5288 | 0.6169 | 0.7050 | 0.7932 | 0.1240 | 05 |
| 0.0884 | 0.1768 | 0.2653 | 0.3537 | 0.4421 | 0.5305 | 0.6189 | 0.7074 | 0.7958 | 0.1244 | 06 |
| 0.0887 | 0.1774 | 0.2661 | 0.3548 | 0.4435 | 0.5322 | 0.6209 | 0.7096 | 0.7983 | 0.1248 | 07 |
| 0.0890 | 0.1780 | 0.2670 | 0.3560 | 0.4450 | 0.5339 | 0.6229 | 0.7119 | 0.8009 | 0.1253 | 08 |
| 0.0893 | 0.1786 | 0.2678 | 0.3571 | 0.4464 | 0.5357 | 0.6249 | 0.7142 | 0.8035 | 0.1257 | 09 |
| 0.0896 | 0.1791 | 0.2687 | 0.3582 | 0.4478 | 0.5374 | 0.6269 | 0.7165 | 0.8060 | 0.1261 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0898 | 0.1797 | 0.2695 | 0.3594 | 0.4492 | 0.5391 | 0.6289 | 0.7188 | 0.8086 | 0.1265 | 11 |
| 0.0901 | 0.1803 | 0.2704 | 0.3605 | 0.4507 | 0.5408 | 0.6309 | 0.7211 | 0.8112 | 0.1269 | 12 |
| 0.0904 | 0.1808 | 0.2713 | 0.3617 | 0.4521 | 0.5425 | 0.6329 | 0.7234 | 0.8138 | 0.1273 | 13 |
| 0.0907 | 0.1814 | 0.2721 | 0.3628 | 0.4535 | 0.5442 | 0.6349 | 0.7256 | 0.8163 | 0.1277 | 14 |
| 0.0910 | 0.1820 | 0.2730 | 0.3640 | 0.4550 | 0.5459 | 0.6369 | 0.7279 | 0.8189 | 0.1281 | 15 |
| 0.0913 | 0.1826 | 0.2738 | 0.3651 | 0.4564 | 0.5477 | 0.6389 | 0.7302 | 0.8215 | 0.1285 | 16 |
| 0.0916 | 0.1831 | 0.2747 | 0.3662 | 0.4578 | 0.5494 | 0.6409 | 0.7325 | 0.8240 | 0.1289 | 17 |
| 0.0918 | 0.1837 | 0.2755 | 0.3674 | 0.4592 | 0.5511 | 0.6429 | 0.7348 | 0.8266 | 0.1293 | 18 |
| 0.0921 | 0.1843 | 0.2764 | 0.3685 | 0.4607 | 0.5528 | 0.6449 | 0.7371 | 0.8292 | 0.1297 | 19 |
| 0.0924 | 0.1848 | 0.2773 | 0.3697 | 0.4621 | 0.5545 | 0.6469 | 0.7394 | 0.8318 | 0.1301 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0927 | 0.1854 | 0.2781 | 0.3708 | 0.4635 | 0.5562 | 0.6489 | 0.7416 | 0.8343 | 0.1305 | 21 |
| 0.0930 | 0.1860 | 0.2790 | 0.3720 | 0.4649 | 0.5579 | 0.6509 | 0.7439 | 0.8369 | 0.1309 | 22 |
| 0.0933 | 0.1865 | 0.2798 | 0.3731 | 0.4664 | 0.5596 | 0.6529 | 0.7462 | 0.8394 | 0.1313 | 23 |
| 0.0936 | 0.1871 | 0.2807 | 0.3742 | 0.4678 | 0.5614 | 0.6549 | 0.7485 | 0.8420 | 0.1317 | 24 |
| 0.0938 | 0.1877 | 0.2815 | 0.3754 | 0.4692 | 0.5631 | 0.6569 | 0.7507 | 0.8446 | 0.1321 | 25 |
| 0.0941 | 0.1883 | 0.2824 | 0.3765 | 0.4706 | 0.5648 | 0.6589 | 0.7530 | 0.8472 | 0.1326 | 26 |
| 0.0944 | 0.1888 | 0.2833 | 0.3777 | 0.4721 | 0.5665 | 0.6609 | 0.7553 | 0.8498 | 0.1330 | 27 |
| 0.0947 | 0.1894 | 0.2841 | 0.3788 | 0.4735 | 0.5682 | 0.6629 | 0.7576 | 0.8523 | 0.1334 | 28 |
| 0.0950 | 0.1900 | 0.2850 | 0.3800 | 0.4749 | 0.5699 | 0.6649 | 0.7599 | 0.8549 | 0.1338 | 29 |
| 0.0953 | 0.1905 | 0.2858 | 0.3811 | 0.4764 | 0.5716 | 0.6669 | 0.7622 | 0.8574 | 0.1342 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0956 | 0.1911 | 0.2867 | 0.3822 | 0.4778 | 0.5734 | 0.6689 | 0.7645 | 0.8600 | 0.1346 | 31 |
| 0.0958 | 0.1917 | 0.2875 | 0.3834 | 0.4792 | 0.5751 | 0.6709 | 0.7667 | 0.8626 | 0.1350 | 32 |
| 0.0961 | 0.1923 | 0.2884 | 0.3845 | 0.4806 | 0.5768 | 0.6729 | 0.7690 | 0.8652 | 0.1354 | 33 |
| 0.0964 | 0.1928 | 0.2892 | 0.3856 | 0.4820 | 0.5785 | 0.6749 | 0.7713 | 0.8677 | 0.1358 | 34 |
| 0.0967 | 0.1934 | 0.2901 | 0.3868 | 0.4835 | 0.5802 | 0.6769 | 0.7736 | 0.8703 | 0.1362 | 35 |
| 0.0970 | 0.1940 | 0.2909 | 0.3879 | 0.4849 | 0.5819 | 0.6789 | 0.7759 | 0.8728 | 0.1366 | 36 |
| 0.0973 | 0.1945 | 0.2918 | 0.3891 | 0.4863 | 0.5836 | 0.6809 | 0.7782 | 0.8754 | 0.1370 | 37 |
| 0.0976 | 0.1951 | 0.2927 | 0.3902 | 0.4878 | 0.5853 | 0.6829 | 0.7804 | 0.8780 | 0.1374 | 38 |
| 0.0978 | 0.1957 | 0.2935 | 0.3914 | 0.4892 | 0.5870 | 0.6849 | 0.7827 | 0.8806 | 0.1378 | 39 |
| 0.0981 | 0.1962 | 0.2944 | 0.3925 | 0.4906 | 0.5887 | 0.6869 | 0.7850 | 0.8831 | 0.1382 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0984 | 0.1968 | 0.2952 | 0.3936 | 0.4920 | 0.5905 | 0.6889 | 0.7873 | 0.8857 | 0.1386 | 41 |
| 0.0987 | 0.1974 | 0.2961 | 0.3948 | 0.4935 | 0.5921 | 0.6909 | 0.7895 | 0.8882 | 0.1390 | 42 |
| 0.0990 | 0.1979 | 0.2969 | 0.3959 | 0.4948 | 0.5938 | 0.6928 | 0.7918 | 0.8907 | 0.1395 | 43 |
| 0.0993 | 0.1985 | 0.2978 | 0.3970 | 0.4963 | 0.5956 | 0.6948 | 0.7941 | 0.8933 | 0.1399 | 44 |
| 0.0995 | 0.1991 | 0.2986 | 0.3982 | 0.4977 | 0.5973 | 0.6968 | 0.7963 | 0.8959 | 0.1403 | 45 |
| 0.0998 | 0.1997 | 0.2995 | 0.3993 | 0.4991 | 0.5990 | 0.6988 | 0.7986 | 0.8985 | 0.1407 | 46 |
| 0.1001 | 0.2002 | 0.3003 | 0.4004 | 0.5006 | 0.6007 | 0.7008 | 0.8009 | 0.9010 | 0.1411 | 47 |
| 0.1004 | 0.2008 | 0.3012 | 0.4016 | 0.5020 | 0.6024 | 0.7028 | 0.8032 | 0.9036 | 0.1415 | 48 |
| 0.1007 | 0.2014 | 0.3020 | 0.4027 | 0.5034 | 0.6041 | 0.7048 | 0.8054 | 0.9061 | 0.1419 | 49 |
| 0.1010 | 0.2019 | 0.3029 | 0.4039 | 0.5049 | 0.6058 | 0.7068 | 0.8078 | 0.9087 | 0.1423 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1013 | 0.2025 | 0.3038 | 0.4050 | 0.5063 | 0.6075 | 0.7088 | 0.8100 | 0.9113 | 0.1427 | 51 |
| 0.1015 | 0.2031 | 0.3046 | 0.4062 | 0.5077 | 0.6092 | 0.7108 | 0.8123 | 0.9139 | 0.1431 | 52 |
| 0.1018 | 0.2036 | 0.3055 | 0.4073 | 0.5091 | 0.6109 | 0.7127 | 0.8146 | 0.9164 | 0.1435 | 53 |
| 0.1021 | 0.2042 | 0.3063 | 0.4084 | 0.5105 | 0.6126 | 0.7147 | 0.8168 | 0.9189 | 0.1439 | 54 |
| 0.1024 | 0.2048 | 0.3072 | 0.4096 | 0.5119 | 0.6143 | 0.7167 | 0.8191 | 0.9215 | 0.1443 | 55 |
| 0.1027 | 0.2053 | 0.3080 | 0.4107 | 0.5134 | 0.6160 | 0.7187 | 0.8214 | 0.9240 | 0.1447 | 56 |
| 0.1030 | 0.2059 | 0.3089 | 0.4118 | 0.5148 | 0.6177 | 0.7207 | 0.8237 | 0.9266 | 0.1451 | 57 |
| 0.1032 | 0.2065 | 0.3097 | 0.4130 | 0.5162 | 0.6194 | 0.7227 | 0.8259 | 0.9292 | 0.1455 | 58 |
| 0.1035 | 0.2071 | 0.3106 | 0.4141 | 0.5176 | 0.6212 | 0.7247 | 0.8282 | 0.9318 | 0.1459 | 59 |
| 0.1038 | 0.2076 | 0.3114 | 0.4153 | 0.5191 | 0.6229 | 0.7267 | 0.8305 | 0.9343 | 0.1463 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9877 | 1.9754 | 2.9631 | 3.9508 | 4.9384 | 5.9261 | 6.9138 | 7.9015 | 8.8892 | 1.3923 |
| 01 | 0.9876 | 1.9753 | 2.9629 | 3.9505 | 4.9381 | 5.9258 | 6.9134 | 7.9010 | 8.8887 | 1.3923 |
| 02 | 0.9876 | 1.9751 | 2.9627 | 3.9503 | 4.9378 | 5.9254 | 6.9130 | 7.9005 | 8.8881 | 1.3922 |
| 03 | 0.9875 | 1.9750 | 2.9625 | 3.9500 | 4.9375 | 5.9250 | 6.9125 | 7.9000 | 8.8875 | 1.3922 |
| 04 | 0.9874 | 1.9749 | 2.9623 | 3.9498 | 4.9372 | 5.9247 | 6.9121 | 7.8996 | 8.8870 | 1.3921 |
| 05 | 0.9874 | 1.9748 | 2.9621 | 3.9495 | 4.9369 | 5.9243 | 6.9117 | 7.8991 | 8.8864 | 1.3921 |
| 06 | 0.9873 | 1.9746 | 2.9620 | 3.9493 | 4.9366 | 5.9239 | 6.9113 | 7.8986 | 8.8859 | 1.3921 |
| 07 | 0.9873 | 1.9745 | 2.9618 | 3.9490 | 4.9363 | 5.9236 | 6.9108 | 7.8981 | 8.8853 | 1.3920 |
| 08 | 0.9872 | 1.9744 | 2.9616 | 3.9488 | 4.9360 | 5.9232 | 6.9104 | 7.8976 | 8.8848 | 1.3920 |
| 09 | 0.9871 | 1.9743 | 2.9614 | 3.9486 | 4.9357 | 5.9228 | 6.9100 | 7.8971 | 8.8842 | 1.3919 |
| 10 | 0.9871 | 1.9742 | 2.9612 | 3.9483 | 4.9354 | 5.9225 | 6.9095 | 7.8966 | 8.8837 | 1.3919 |
| 11 | 0.9870 | 1.9740 | 2.9610 | 3.9481 | 4.9351 | 5.9221 | 6.9091 | 7.8961 | 8.8831 | 1.3919 |
| 12 | 0.9870 | 1.9739 | 2.9609 | 3.9478 | 4.9348 | 5.9217 | 6.9087 | 7.8956 | 8.8826 | 1.3918 |
| 13 | 0.9869 | 1.9738 | 2.9607 | 3.9476 | 4.9344 | 5.9213 | 6.9082 | 7.8951 | 8.8820 | 1.3918 |
| 14 | 0.9868 | 1.9737 | 2.9605 | 3.9473 | 4.9341 | 5.9210 | 6.9078 | 7.8946 | 8.8814 | 1.3917 |
| 15 | 0.9868 | 1.9735 | 2.9603 | 3.9471 | 4.9338 | 5.9206 | 6.9073 | 7.8941 | 8.8809 | 1.3917 |
| 16 | 0.9867 | 1.9734 | 2.9601 | 3.9468 | 4.9335 | 5.9202 | 6.9069 | 7.8936 | 8.8803 | 1.3917 |
| 17 | 0.9866 | 1.9733 | 2.9599 | 3.9465 | 4.9332 | 5.9198 | 6.9065 | 7.8931 | 8.8797 | 1.3916 |
| 18 | 0.9866 | 1.9732 | 2.9597 | 3.9463 | 4.9329 | 5.9195 | 6.9060 | 7.8926 | 8.8792 | 1.3916 |
| 19 | 0.9865 | 1.9730 | 2.9595 | 3.9460 | 4.9326 | 5.9191 | 6.9056 | 7.8921 | 8.8786 | 1.3915 |
| 20 | 0.9864 | 1.9729 | 2.9593 | 3.9458 | 4.9322 | 5.9187 | 6.9051 | 7.8916 | 8.8780 | 1.3915 |
| 21 | 0.9864 | 1.9728 | 2.9592 | 3.9455 | 4.9319 | 5.9183 | 6.9047 | 7.8911 | 8.8775 | 1.3915 |
| 22 | 0.9863 | 1.9726 | 2.9590 | 3.9453 | 4.9316 | 5.9179 | 6.9042 | 7.8906 | 8.8769 | 1.3914 |
| 23 | 0.9863 | 1.9725 | 2.9588 | 3.9450 | 4.9313 | 5.9175 | 6.9038 | 7.8900 | 8.8763 | 1.3914 |
| 24 | 0.9862 | 1.9724 | 2.9586 | 3.9448 | 4.9310 | 5.9171 | 6.9033 | 7.8895 | 8.8757 | 1.3913 |
| 25 | 0.9861 | 1.9723 | 2.9584 | 3.9445 | 4.9306 | 5.9168 | 6.9029 | 7.8890 | 8.8751 | 1.3913 |
| 26 | 0.9861 | 1.9721 | 2.9582 | 3.9442 | 4.9303 | 5.9164 | 6.9024 | 7.8885 | 8.8745 | 1.3913 |
| 27 | 0.9860 | 1.9720 | 2.9580 | 3.9440 | 4.9300 | 5.9160 | 6.9020 | 7.8880 | 8.8740 | 1.3912 |
| 28 | 0.9859 | 1.9719 | 2.9578 | 3.9437 | 4.9297 | 5.9156 | 6.9015 | 7.8875 | 8.8734 | 1.3912 |
| 29 | 0.9859 | 1.9717 | 2.9576 | 3.9435 | 4.9293 | 5.9152 | 6.9011 | 7.8870 | 8.8728 | 1.3911 |
| 30 | 0.9858 | 1.9716 | 2.9574 | 3.9432 | 4.9290 | 5.9148 | 6.9006 | 7.8864 | 8.8722 | 1.3911 |
| 31 | 0.9857 | 1.9715 | 2.9572 | 3.9429 | 4.9287 | 5.9144 | 6.9002 | 7.8859 | 8.8716 | 1.3910 |
| 32 | 0.9857 | 1.9713 | 2.9570 | 3.9427 | 4.9284 | 5.9140 | 6.8997 | 7.8854 | 8.8710 | 1.3910 |
| 33 | 0.9856 | 1.9712 | 2.9568 | 3.9424 | 4.9280 | 5.9136 | 6.8992 | 7.8848 | 8.8704 | 1.3910 |
| 34 | 0.9855 | 1.9711 | 2.9566 | 3.9422 | 4.9277 | 5.9132 | 6.8988 | 7.8843 | 8.8698 | 1.3909 |
| 35 | 0.9855 | 1.9709 | 2.9564 | 3.9419 | 4.9274 | 5.9128 | 6.8983 | 7.8838 | 8.8692 | 1.3909 |
| 36 | 0.9854 | 1.9708 | 2.9562 | 3.9416 | 4.9270 | 5.9124 | 6.8978 | 7.8832 | 8.8687 | 1.3908 |
| 37 | 0.9853 | 1.9707 | 2.9560 | 3.9414 | 4.9267 | 5.9120 | 6.8974 | 7.8827 | 8.8681 | 1.3908 |
| 38 | 0.9853 | 1.9705 | 2.9558 | 3.9411 | 4.9264 | 5.9116 | 6.8969 | 7.8822 | 8.8675 | 1.3907 |
| 39 | 0.9852 | 1.9704 | 2.9556 | 3.9408 | 4.9260 | 5.9112 | 6.8964 | 7.8817 | 8.8669 | 1.3907 |
| 40 | 0.9851 | 1.9703 | 2.9554 | 3.9406 | 4.9257 | 5.9108 | 6.8960 | 7.8811 | 8.8663 | 1.3906 |
| 41 | 0.9851 | 1.9701 | 2.9552 | 3.9403 | 4.9254 | 5.9104 | 6.8955 | 7.8806 | 8.8657 | 1.3906 |
| 42 | 0.9850 | 1.9700 | 2.9550 | 3.9400 | 4.9250 | 5.9100 | 6.8950 | 7.8800 | 8.8650 | 1.3905 |
| 43 | 0.9849 | 1.9699 | 2.9548 | 3.9398 | 4.9247 | 5.9096 | 6.8946 | 7.8795 | 8.8644 | 1.3905 |
| 44 | 0.9849 | 1.9697 | 2.9546 | 3.9395 | 4.9244 | 5.9092 | 6.8941 | 7.8790 | 8.8638 | 1.3904 |
| 45 | 0.9848 | 1.9696 | 2.9544 | 3.9392 | 4.9240 | 5.9088 | 6.8936 | 7.8784 | 8.8632 | 1.3904 |
| 46 | 0.9847 | 1.9695 | 2.9542 | 3.9389 | 4.9237 | 5.9084 | 6.8931 | 7.8779 | 8.8626 | 1.3903 |
| 47 | 0.9847 | 1.9693 | 2.9540 | 3.9387 | 4.9233 | 5.9080 | 6.8927 | 7.8773 | 8.8620 | 1.3903 |
| 48 | 0.9846 | 1.9692 | 2.9538 | 3.9384 | 4.9230 | 5.9076 | 6.8922 | 7.8768 | 8.8614 | 1.3902 |
| 49 | 0.9845 | 1.9691 | 2.9536 | 3.9381 | 4.9227 | 5.9072 | 6.8917 | 7.8762 | 8.8608 | 1.3902 |
| 50 | 0.9845 | 1.9689 | 2.9534 | 3.9379 | 4.9223 | 5.9068 | 6.8912 | 7.8757 | 8.8602 | 1.3901 |
| 51 | 0.9844 | 1.9688 | 2.9532 | 3.9376 | 4.9220 | 5.9064 | 6.8908 | 7.8752 | 8.8595 | 1.3901 |
| 52 | 0.9843 | 1.9686 | 2.9530 | 3.9373 | 4.9216 | 5.9059 | 6.8903 | 7.8746 | 8.8589 | 1.3900 |
| 53 | 0.9843 | 1.9685 | 2.9528 | 3.9370 | 4.9213 | 5.9055 | 6.8898 | 7.8740 | 8.8583 | 1.3900 |
| 54 | 0.9842 | 1.9684 | 2.9526 | 3.9367 | 4.9209 | 5.9051 | 6.8893 | 7.8735 | 8.8577 | 1.3899 |
| 55 | 0.9841 | 1.9682 | 2.9523 | 3.9365 | 4.9206 | 5.9047 | 6.8888 | 7.8729 | 8.8570 | 1.3899 |
| 56 | 0.9840 | 1.9681 | 2.9521 | 3.9362 | 4.9202 | 5.9043 | 6.8883 | 7.8724 | 8.8564 | 1.3898 |
| 57 | 0.9840 | 1.9680 | 2.9519 | 3.9359 | 4.9199 | 5.9039 | 6.8878 | 7.8718 | 8.8558 | 1.3898 |
| 58 | 0.9839 | 1.9678 | 2.9517 | 3.9356 | 4.9195 | 5.9034 | 6.8874 | 7.8713 | 8.8552 | 1.3897 |
| 59 | 0.9838 | 1.9677 | 2.9515 | 3.9354 | 4.9192 | 5.9030 | 6.8869 | 7.8707 | 8.8545 | 1.3897 |
| 60 | 0.9838 | 1.9675 | 2.9513 | 3.9351 | 4.9188 | 5.9026 | 6.8864 | 7.8702 | 8.8539 | 1.3896 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1038 | 0.2076 | 0.3114 | 0.4153 | 0.5191 | 0.6229 | 0.7267 | 0.8305 | 0.9343 | 0.1463 | 00 |
| 0.1041 | 0.2082 | 0.3123 | 0.4164 | 0.5205 | 0.6246 | 0.7287 | 0.8327 | 0.9368 | 0.1467 | 01 |
| 0.1044 | 0.2088 | 0.3131 | 0.4175 | 0.5219 | 0.6263 | 0.7307 | 0.8350 | 0.9394 | 0.1471 | 02 |
| 0.1047 | 0.2093 | 0.3140 | 0.4186 | 0.5233 | 0.6280 | 0.7326 | 0.8373 | 0.9419 | 0.1476 | 03 |
| 0.1049 | 0.2099 | 0.3148 | 0.4198 | 0.5247 | 0.6297 | 0.7346 | 0.8396 | 0.9445 | 0.1480 | 04 |
| 0.1052 | 0.2105 | 0.3157 | 0.4209 | 0.5262 | 0.6314 | 0.7366 | 0.8418 | 0.9471 | 0.1484 | 05 |
| 0.1055 | 0.2110 | 0.3165 | 0.4220 | 0.5276 | 0.6331 | 0.7386 | 0.8441 | 0.9496 | 0.1488 | 06 |
| 0.1058 | 0.2116 | 0.3174 | 0.4232 | 0.5290 | 0.6348 | 0.7406 | 0.8464 | 0.9522 | 0.1492 | 07 |
| 0.1061 | 0.2122 | 0.3182 | 0.4243 | 0.5304 | 0.6365 | 0.7426 | 0.8486 | 0.9547 | 0.1496 | 08 |
| 0.1064 | 0.2127 | 0.3191 | 0.4255 | 0.5318 | 0.6382 | 0.7446 | 0.8509 | 0.9573 | 0.1500 | 09 |
| 0.1067 | 0.2133 | 0.3200 | 0.4266 | 0.5333 | 0.6399 | 0.7466 | 0.8532 | 0.9599 | 0.1504 | 10 |
| 0.1069 | 0.2139 | 0.3208 | 0.4277 | 0.5347 | 0.6416 | 0.7485 | 0.8554 | 0.9624 | 0.1508 | 11 |
| 0.1072 | 0.2144 | 0.3217 | 0.4389 | 0.5361 | 0.6433 | 0.7505 | 0.8577 | 0.9650 | 0.1512 | 12 |
| 0.1075 | 0.2150 | 0.3225 | 0.4300 | 0.5375 | 0.6450 | 0.7525 | 0.8600 | 0.9675 | 0.1516 | 13 |
| 0.1078 | 0.2156 | 0.3233 | 0.4311 | 0.5389 | 0.6467 | 0.7545 | 0.8622 | 0.9700 | 0.1520 | 14 |
| 0.1081 | 0.2161 | 0.3242 | 0.4323 | 0.5403 | 0.6484 | 0.7565 | 0.8645 | 0.9726 | 0.1524 | 15 |
| 0.1084 | 0.2167 | 0.3251 | 0.4334 | 0.5418 | 0.6501 | 0.7585 | 0.8668 | 0.9752 | 0.1528 | 16 |
| 0.1086 | 0.2173 | 0.3259 | 0.4346 | 0.5432 | 0.6518 | 0.7605 | 0.8691 | 0.9778 | 0.1532 | 17 |
| 0.1089 | 0.2178 | 0.3268 | 0.4357 | 0.5446 | 0.6535 | 0.7624 | 0.8714 | 0.9803 | 0.1536 | 18 |
| 0.1092 | 0.2184 | 0.3276 | 0.4368 | 0.5460 | 0.6552 | 0.7644 | 0.8736 | 0.9828 | 0.1540 | 19 |
| 0.1095 | 0.2190 | 0.3285 | 0.4380 | 0.5474 | 0.6569 | 0.7664 | 0.8759 | 0.9854 | 0.1544 | 20 |
| 0.1098 | 0.2195 | 0.3293 | 0.4391 | 0.5488 | 0.6586 | 0.7684 | 0.8782 | 0.9879 | 0.1548 | 21 |
| 0.1101 | 0.2201 | 0.3302 | 0.4402 | 0.5503 | 0.6603 | 0.7704 | 0.8804 | 0.9905 | 0.1552 | 22 |
| 0.1103 | 0.2207 | 0.3310 | 0.4414 | 0.5517 | 0.6620 | 0.7724 | 0.8827 | 0.9931 | 0.1556 | 23 |
| 0.1106 | 0.2212 | 0.3319 | 0.4425 | 0.5531 | 0.6637 | 0.7743 | 0.8850 | 0.9956 | 0.1561 | 24 |
| 0.1109 | 0.2218 | 0.3327 | 0.4436 | 0.5545 | 0.6654 | 0.7763 | 0.8872 | 0.9981 | 0.1565 | 25 |
| 0.1112 | 0.2224 | 0.3336 | 0.4448 | 0.5559 | 0.6671 | 0.7783 | 0.8895 | 1.0007 | 0.1569 | 26 |
| 0.1115 | 0.2229 | 0.3344 | 0.4459 | 0.5573 | 0.6688 | 0.7803 | 0.8918 | 1.0032 | 0.1573 | 27 |
| 0.1118 | 0.2235 | 0.3353 | 0.4470 | 0.5588 | 0.6705 | 0.7823 | 0.8940 | 1.0058 | 0.1577 | 28 |
| 0.1120 | 0.2241 | 0.3361 | 0.4481 | 0.5602 | 0.6722 | 0.7842 | 0.8963 | 1.0083 | 0.1581 | 29 |
| 0.1123 | 0.2246 | 0.3370 | 0.4493 | 0.5616 | 0.6739 | 0.7862 | 0.8986 | 1.0109 | 0.1585 | 30 |
| 0.1126 | 0.2252 | 0.3378 | 0.4504 | 0.5630 | 0.6756 | 0.7882 | 0.9008 | 1.0134 | 0.1589 | 31 |
| 0.1129 | 0.2258 | 0.3386 | 0.4515 | 0.5644 | 0.6773 | 0.7902 | 0.9031 | 1.0159 | 0.1593 | 32 |
| 0.1132 | 0.2263 | 0.3395 | 0.4527 | 0.5659 | 0.6790 | 0.7922 | 0.9054 | 1.0185 | 0.1597 | 33 |
| 0.1134 | 0.2269 | 0.3403 | 0.4538 | 0.5673 | 0.6807 | 0.7941 | 0.9076 | 1.0210 | 0.1601 | 34 |
| 0.1137 | 0.2275 | 0.3412 | 0.4549 | 0.5687 | 0.6824 | 0.7961 | 0.9098 | 1.0236 | 0.1605 | 35 |
| 0.1140 | 0.2280 | 0.3421 | 0.4561 | 0.5701 | 0.6841 | 0.8081 | 0.9121 | 1.0262 | 0.1609 | 36 |
| 0.1143 | 0.2286 | 0.3429 | 0.4572 | 0.5715 | 0.6858 | 0.8001 | 0.9144 | 1.0287 | 0.1613 | 37 |
| 0.1146 | 0.2292 | 0.3437 | 0.4583 | 0.5729 | 0.6875 | 0.8021 | 0.9166 | 1.0312 | 0.1617 | 38 |
| 0.1149 | 0.2297 | 0.3446 | 0.4594 | 0.5743 | 0.6892 | 0.8040 | 0.9189 | 1.0337 | 0.1621 | 39 |
| 0.1151 | 0.2303 | 0.3454 | 0.4606 | 0.5757 | 0.6909 | 0.8060 | 0.9212 | 1.0363 | 0.1625 | 40 |
| 0.1154 | 0.2309 | 0.3463 | 0.4617 | 0.5771 | 0.6926 | 0.8080 | 0.9234 | 1.0389 | 0.1629 | 41 |
| 0.1157 | 0.2314 | 0.3471 | 0.4628 | 0.5786 | 0.6943 | 0.8100 | 0.9257 | 1.0414 | 0.1633 | 42 |
| 0.1160 | 0.2320 | 0.3480 | 0.4640 | 0.5800 | 0.6960 | 0.8119 | 0.9279 | 1.0439 | 0.1637 | 43 |
| 0.1163 | 0.2326 | 0.3488 | 0.4651 | 0.5814 | 0.6977 | 0.8139 | 0.9302 | 1.0465 | 0.1641 | 44 |
| 0.1166 | 0.2331 | 0.3497 | 0.4662 | 0.5828 | 0.6994 | 0.8159 | 0.9325 | 1.0490 | 0.1645 | 45 |
| 0.1168 | 0.2337 | 0.3505 | 0.4674 | 0.5842 | 0.7010 | 0.8179 | 0.9347 | 1.0516 | 0.1650 | 46 |
| 0.1171 | 0.2342 | 0.3514 | 0.4685 | 0.5856 | 0.7027 | 0.8199 | 0.9370 | 1.0541 | 0.1654 | 47 |
| 0.1174 | 0.2348 | 0.3522 | 0.4696 | 0.5870 | 0.7045 | 0.8219 | 0.9393 | 1.0567 | 0.1658 | 48 |
| 0.1177 | 0.2354 | 0.3531 | 0.4708 | 0.5884 | 0.7061 | 0.8238 | 0.9415 | 1.0592 | 0.1662 | 49 |
| 0.1180 | 0.2359 | 0.3539 | 0.4719 | 0.5899 | 0.7078 | 0.8258 | 0.9438 | 1.0617 | 0.1666 | 50 |
| 0.1183 | 0.2365 | 0.3548 | 0.4730 | 0.5913 | 0.7095 | 0.8278 | 0.9460 | 1.0643 | 0.1670 | 51 |
| 0.1185 | 0.2371 | 0.3556 | 0.4742 | 0.5927 | 0.7112 | 0.8298 | 0.9483 | 1.0669 | 0.1674 | 52 |
| 0.1188 | 0.2376 | 0.3565 | 0.4753 | 0.5941 | 0.7129 | 0.8317 | 0.9506 | 1.0694 | 0.1678 | 53 |
| 0.1191 | 0.2382 | 0.3573 | 0.4764 | 0.5955 | 0.7146 | 0.8337 | 0.9528 | 1.0719 | 0.1682 | 54 |
| 0.1194 | 0.2388 | 0.3581 | 0.4775 | 0.5969 | 0.7163 | 0.8357 | 0.9550 | 1.0744 | 0.1686 | 55 |
| 0.1197 | 0.2393 | 0.3590 | 0.4786 | 0.5983 | 0.7180 | 0.8376 | 0.9573 | 1.0769 | 0.1690 | 56 |
| 0.1199 | 0.2399 | 0.3598 | 0.4798 | 0.5997 | 0.7197 | 0.8396 | 0.9596 | 1.0795 | 0.1694 | 57 |
| 0.1202 | 0.2405 | 0.3607 | 0.4809 | 0.6011 | 0.7214 | 0.8416 | 0.9618 | 1.0821 | 0.1698 | 58 |
| 0.1205 | 0.2410 | 0.3615 | 0.4820 | 0.6025 | 0.7231 | 0.8436 | 0.9641 | 1.0846 | 0.1702 | 59 |
| 0.1208 | 0.2416 | 0.3624 | 0.4832 | 0.6040 | 0.7247 | 0.8455 | 0.9663 | 1.0871 | 0.1706 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9838 | 1.9675 | 2.9513 | 3.9351 | 4.9188 | 5.9026 | 6.8864 | 7.8702 | 8.8539 | 1.3896 |
| 01 | 0.9837 | 1.9674 | 2.9511 | 3.9348 | 4.9185 | 5.9022 | 6.8859 | 7.8696 | 8.8533 | 1.3896 |
| 02 | 0.9836 | 1.9673 | 2.9509 | 3.9345 | 4.9181 | 5.9018 | 6.8854 | 7.8690 | 8.8526 | 1.3895 |
| 03 | 0.9835 | 1.9671 | 2.9507 | 3.9342 | 4.9178 | 5.9013 | 6.8849 | 7.8684 | 8.8520 | 1.3895 |
| 04 | 0.9835 | 1.9670 | 2.9505 | 3.9339 | 4.9174 | 5.9009 | 6.8844 | 7.8679 | 8.8514 | 1.3894 |
| 05 | 0.9834 | 1.9668 | 2.9502 | 3.9337 | 4.9171 | 5.9005 | 6.8839 | 7.8673 | 8.8507 | 1.3894 |
| 06 | 0.9833 | 1.9667 | 2.9500 | 3.9334 | 4.9167 | 5.9001 | 6.8834 | 7.8667 | 8.8501 | 1.3893 |
| 07 | 0.9833 | 1.9665 | 2.9498 | 3.9331 | 4.9164 | 5.8996 | 6.8829 | 7.8662 | 8.8494 | 1.3893 |
| 08 | 0.9832 | 1.9664 | 2.9496 | 3.9328 | 4.9160 | 5.8992 | 6.8824 | 7.8656 | 8.8488 | 1.3892 |
| 09 | 0.9831 | 1.9663 | 2.9494 | 3.9325 | 4.9156 | 5.8988 | 6.8819 | 7.8650 | 8.8482 | 1.3892 |
| 10 | 0.9831 | 1.9661 | 2.9492 | 3.9322 | 4.9153 | 5.8983 | 6.8814 | 7.8645 | 8.8475 | 1.3891 |
| 11 | 0.9830 | 1.9660 | 2.9490 | 3.9319 | 4.9149 | 5.8979 | 6.8809 | 7.8639 | 8.8469 | 1.3891 |
| 12 | 0.9829 | 1.9658 | 2.9487 | 3.9316 | 4.9146 | 5.8975 | 6.8804 | 7.8633 | 8.8462 | 1.3890 |
| 13 | 0.9828 | 1.9657 | 2.9485 | 3.9314 | 4.9142 | 5.8970 | 6.8799 | 7.8627 | 8.8456 | 1.3890 |
| 14 | 0.9828 | 1.9655 | 2.9483 | 3.9311 | 4.9138 | 5.8966 | 6.8794 | 7.8621 | 8.8449 | 1.3889 |
| 15 | 0.9827 | 1.9654 | 2.9481 | 3.9308 | 4.9135 | 5.8962 | 6.8789 | 7.8616 | 8.8442 | 1.3889 |
| 16 | 0.9826 | 1.9652 | 2.9479 | 3.9305 | 4.9131 | 5.8957 | 6.8783 | 7.8610 | 8.8436 | 1.3888 |
| 17 | 0.9825 | 1.9651 | 2.9476 | 3.9302 | 4.9127 | 5.8953 | 6.8778 | 7.8604 | 8.8429 | 1.3888 |
| 18 | 0.9825 | 1.9650 | 2.9474 | 3.9299 | 4.9124 | 5.8949 | 6.8773 | 7.8598 | 8.8423 | 1.3887 |
| 19 | 0.9824 | 1.9648 | 2.9472 | 3.9296 | 4.9120 | 5.8944 | 6.8768 | 7.8592 | 8.8416 | 1.3887 |
| 20 | 0.9823 | 1.9647 | 2.9470 | 3.9293 | 4.9117 | 5.8940 | 6.8763 | 7.8586 | 8.8410 | 1.3886 |
| 21 | 0.9823 | 1.9645 | 2.9468 | 3.9290 | 4.9113 | 5.8935 | 6.8758 | 7.8580 | 8.8403 | 1.3886 |
| 22 | 0.9822 | 1.9644 | 2.9465 | 3.9287 | 4.9109 | 5.8931 | 6.8753 | 7.8574 | 8.8396 | 1.3885 |
| 23 | 0.9821 | 1.9642 | 2.9463 | 3.9284 | 4.9105 | 5.8926 | 6.8747 | 7.8569 | 8.8390 | 1.3885 |
| 24 | 0.9820 | 1.9641 | 2.9461 | 3.9281 | 4.9102 | 5.8922 | 6.8742 | 7.8563 | 8.8383 | 1.3884 |
| 25 | 0.9820 | 1.9639 | 2.9459 | 3.9278 | 4.9098 | 5.8918 | 6.8737 | 7.8557 | 8.8376 | 1.3884 |
| 26 | 0.9819 | 1.9638 | 2.9457 | 3.9275 | 4.9094 | 5.8913 | 6.8732 | 7.8551 | 8.8370 | 1.3883 |
| 27 | 0.9818 | 1.9636 | 2.9454 | 3.9272 | 4.9091 | 5.8909 | 6.8727 | 7.8545 | 8.8363 | 1.3883 |
| 28 | 0.9817 | 1.9635 | 2.9452 | 3.9269 | 4.9087 | 5.8904 | 6.8722 | 7.8539 | 8.8356 | 1.3882 |
| 29 | 0.9817 | 1.9633 | 2.9450 | 3.9266 | 4.9083 | 5.8900 | 6.8716 | 7.8533 | 8.8349 | 1.3882 |
| 30 | 0.9816 | 1.9632 | 2.9448 | 3.9263 | 4.9079 | 5.8895 | 6.8711 | 7.8527 | 8.8343 | 1.3881 |
| 31 | 0.9815 | 1.9630 | 2.9445 | 3.9260 | 4.9076 | 5.8891 | 6.8706 | 7.8521 | 8.8336 | 1.3881 |
| 32 | 0.9814 | 1.9629 | 2.9443 | 3.9257 | 4.9072 | 5.8886 | 6.8700 | 7.8515 | 8.8329 | 1.3880 |
| 33 | 0.9814 | 1.9627 | 2.9441 | 3.9254 | 4.9068 | 5.8882 | 6.8695 | 7.8509 | 8.8322 | 1.3880 |
| 34 | 0.9813 | 1.9626 | 2.9438 | 3.9251 | 4.9064 | 5.8877 | 6.8690 | 7.8503 | 8.8315 | 1.3879 |
| 35 | 0.9812 | 1.9624 | 2.9436 | 3.9248 | 4.9060 | 5.8872 | 6.8684 | 7.8497 | 8.8309 | 1.3879 |
| 36 | 0.9811 | 1.9623 | 2.9434 | 3.9245 | 4.9057 | 5.8868 | 6.8679 | 7.8490 | 8.8302 | 1.3878 |
| 37 | 0.9811 | 1.9621 | 2.9432 | 3.9242 | 4.9053 | 5.8863 | 6.8674 | 7.8484 | 8.8295 | 1.3878 |
| 38 | 0.9810 | 1.9620 | 2.9429 | 3.9239 | 4.9049 | 5.8859 | 6.8669 | 7.8478 | 8.8288 | 1.3877 |
| 39 | 0.9809 | 1.9618 | 2.9427 | 3.9236 | 4.9045 | 5.8854 | 6.8663 | 7.8472 | 8.8281 | 1.3876 |
| 40 | 0.9808 | 1.9617 | 2.9425 | 3.9233 | 4.9041 | 5.8850 | 6.8658 | 7.8466 | 8.8274 | 1.3876 |
| 41 | 0.9807 | 1.9615 | 2.9422 | 3.9230 | 4.9037 | 5.8845 | 6.8652 | 7.8460 | 8.8267 | 1.3875 |
| 42 | 0.9807 | 1.9613 | 2.9420 | 3.9227 | 4.9034 | 5.8840 | 6.8647 | 7.8454 | 8.8260 | 1.3875 |
| 43 | 0.9806 | 1.9612 | 2.9418 | 3.9224 | 4.9030 | 5.8836 | 6.8642 | 7.8448 | 8.8253 | 1.3874 |
| 44 | 0.9805 | 1.9610 | 2.9416 | 3.9221 | 4.9026 | 5.8831 | 6.8636 | 7.8441 | 8.8247 | 1.3874 |
| 45 | 0.9804 | 1.9609 | 2.9413 | 3.9218 | 4.9022 | 5.8826 | 6.8631 | 7.8435 | 8.8240 | 1.3873 |
| 46 | 0.9804 | 1.9607 | 2.9411 | 3.9214 | 4.9018 | 5.8822 | 6.8625 | 7.8429 | 8.8233 | 1.3872 |
| 47 | 0.9803 | 1.9606 | 2.9409 | 3.9211 | 4.9014 | 5.8817 | 6.8620 | 7.8423 | 8.8226 | 1.3872 |
| 48 | 0.9802 | 1.9604 | 2.9406 | 3.9208 | 4.9010 | 5.8812 | 6.8614 | 7.8416 | 8.8219 | 1.3871 |
| 49 | 0.9801 | 1.9603 | 2.9404 | 3.9205 | 4.9006 | 5.8808 | 6.8609 | 7.8410 | 8.8212 | 1.3871 |
| 50 | 0.9801 | 1.9601 | 2.9402 | 3.9202 | 4.9003 | 5.8803 | 6.8604 | 7.8404 | 8.8205 | 1.3870 |
| 51 | 0.9800 | 1.9599 | 2.9399 | 3.9199 | 4.8999 | 5.8798 | 6.8598 | 7.8398 | 8.8197 | 1.3870 |
| 52 | 0.9799 | 1.9598 | 2.9397 | 3.9196 | 4.8995 | 5.8794 | 6.8592 | 7.8391 | 8.8190 | 1.3869 |
| 53 | 0.9798 | 1.9596 | 2.9394 | 3.9193 | 4.8991 | 5.8789 | 6.8587 | 7.8385 | 8.8183 | 1.3868 |
| 54 | 0.9797 | 1.9595 | 2.9392 | 3.9189 | 4.8987 | 5.8784 | 6.8581 | 7.8379 | 8.8176 | 1.3868 |
| 55 | 0.9797 | 1.9593 | 2.9390 | 3.9186 | 4.8983 | 5.8779 | 6.8576 | 7.8372 | 8.8169 | 1.3867 |
| 56 | 0.9796 | 1.9592 | 2.9387 | 3.9183 | 4.8979 | 5.8775 | 6.8570 | 7.8366 | 8.8162 | 1.3866 |
| 57 | 0.9795 | 1.9590 | 2.9385 | 3.9180 | 4.8975 | 5.8770 | 6.8565 | 7.8360 | 8.8155 | 1.3866 |
| 58 | 0.9794 | 1.9588 | 2.9383 | 3.9177 | 4.8971 | 5.8765 | 6.8559 | 7.8353 | 8.8148 | 1.3865 |
| 59 | 0.9793 | 1.9587 | 2.9380 | 3.9173 | 4.8967 | 5.8760 | 6.8554 | 7.8347 | 8.8140 | 1.3865 |
| 60 | 0.9793 | 1.9585 | 2.9378 | 3.9170 | 4.8963 | 5.8755 | 6.8548 | 7.8341 | 8.8133 | 1.3864 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1208 | 0.2416 | 0.3624 | 0.4832 | 0.6040 | 0.7247 | 0.8455 | 0.9663 | 1.0871 | 0.1706 | 00 |
| 0.1211 | 0.2421 | 0.3632 | 0.4843 | 0.6054 | 0.7264 | 0.8475 | 0.9686 | 1.0896 | 0.1710 | 01 |
| 0.1214 | 0.2427 | 0.3641 | 0.4854 | 0.6068 | 0.7281 | 0.8495 | 0.9709 | 1.0922 | 0.1714 | 02 |
| 0.1216 | 0.2433 | 0.3649 | 0.4866 | 0.6082 | 0.7298 | 0.8515 | 0.9731 | 1.0948 | 0.1718 | 03 |
| 0.1219 | 0.2438 | 0.3658 | 0.4877 | 0.6196 | 0.7315 | 0.8534 | 0.9754 | 1.0973 | 0.1722 | 04 |
| 0.1222 | 0.2444 | 0.3666 | 0.4888 | 0.6110 | 0.7332 | 0.8554 | 0.9776 | 1.0998 | 0.1726 | 05 |
| 0.1225 | 0.2450 | 0.3674 | 0.4899 | 0.6124 | 0.7349 | 0.8574 | 0.9798 | 1.1023 | 0.1730 | 06 |
| 0.1228 | 0.2455 | 0.3683 | 0.4910 | 0.6138 | 0.7366 | 0.8593 | 0.9821 | 1.1048 | 0.1734 | 07 |
| 0.1230 | 0.2461 | 0.3691 | 0.4922 | 0.6152 | 0.7382 | 0.8613 | 0.9843 | 1.1074 | 0.1738 | 08 |
| 0.1233 | 0.2467 | 0.3700 | 0.4933 | 0.6166 | 0.7400 | 0.8633 | 0.9866 | 1.1100 | 0.1743 | 09 |
| 0.1236 | 0.2472 | 0.3708 | 0.4944 | 0.6180 | 0.7417 | 0.8653 | 0.9889 | 1.1125 | 0.1747 | 10 |
| 0.1239 | 0.2478 | 0.3717 | 0.4956 | 0.6194 | 0.7433 | 0.8672 | 0.9911 | 1.1150 | 0.1751 | 11 |
| 0.1242 | 0.2483 | 0.3725 | 0.4967 | 0.6209 | 0.7450 | 0.8692 | 0.9934 | 1.1175 | 0.1755 | 12 |
| 0.1245 | 0.2489 | 0.3734 | 0.4978 | 0.6223 | 0.7467 | 0.8712 | 0.9956 | 1.1201 | 0.1759 | 13 |
| 0.1247 | 0.2495 | 0.3742 | 0.4989 | 0.6237 | 0.7484 | 0.8731 | 0.9978 | 1.1226 | 0.1763 | 14 |
| 0.1250 | 0.2500 | 0.3750 | 0.5000 | 0.6251 | 0.7501 | 0.8751 | 1.0001 | 1.1251 | 0.1767 | 15 |
| 0.1253 | 0.2506 | 0.3759 | 0.5012 | 0.6265 | 0.7518 | 0.8771 | 1.0024 | 1.1277 | 0.1771 | 16 |
| 0.1256 | 0.2512 | 0.3767 | 0.5023 | 0.6279 | 0.7535 | 0.8791 | 1.0046 | 1.1302 | 0.1775 | 17 |
| 0.1259 | 0.2517 | 0.3776 | 0.5034 | 0.6293 | 0.7552 | 0.8810 | 1.0069 | 1.1327 | 0.1779 | 18 |
| 0.1261 | 0.2523 | 0.3784 | 0.5046 | 0.6307 | 0.7568 | 0.8830 | 1.0091 | 1.1353 | 0.1783 | 19 |
| 0.1264 | 0.2528 | 0.3793 | 0.5057 | 0.6321 | 0.7585 | 0.8849 | 1.0114 | 1.1378 | 0.1787 | 20 |
| 0.1267 | 0.2534 | 0.3801 | 0.5068 | 0.6335 | 0.7602 | 0.8869 | 1.0136 | 1.1403 | 0.1791 | 21 |
| 0.1270 | 0.2540 | 0.3809 | 0.5079 | 0.6349 | 0.7619 | 0.8889 | 1.0158 | 1.1428 | 0.1795 | 22 |
| 0.1273 | 0.2545 | 0.3818 | 0.5090 | 0.6363 | 0.7636 | 0.8908 | 1.0181 | 1.1453 | 0.1799 | 23 |
| 0.1275 | 0.2551 | 0.3826 | 0.5102 | 0.6377 | 0.7652 | 0.8928 | 1.0203 | 1.1479 | 0.1803 | 24 |
| 0.1278 | 0.2556 | 0.3835 | 0.5113 | 0.6391 | 0.7669 | 0.8947 | 1.0226 | 1.1504 | 0.1807 | 25 |
| 0.1281 | 0.2562 | 0.3843 | 0.5124 | 0.6405 | 0.7686 | 0.8967 | 1.0248 | 1.1529 | 0.1811 | 26 |
| 0.1284 | 0.2568 | 0.3852 | 0.5136 | 0.6419 | 0.7703 | 0.8987 | 1.0271 | 1.1555 | 0.1815 | 27 |
| 0.1287 | 0.2573 | 0.3860 | 0.5147 | 0.6433 | 0.7720 | 0.9007 | 1.0294 | 1.1580 | 0.1819 | 28 |
| 0.1289 | 0.2579 | 0.3868 | 0.5158 | 0.6447 | 0.7737 | 0.9026 | 1.0316 | 1.1605 | 0.1823 | 29 |
| 0.1292 | 0.2585 | 0.3877 | 0.5169 | 0.6461 | 0.7754 | 0.9046 | 1.0338 | 1.1631 | 0.1827 | 30 |
| 0.1295 | 0.2590 | 0.3885 | 0.5180 | 0.6475 | 0.7771 | 0.9066 | 1.0361 | 1.1656 | 0.1831 | 31 |
| 0.1298 | 0.2596 | 0.3894 | 0.5192 | 0.6489 | 0.7787 | 0.9085 | 1.0383 | 1.1681 | 0.1835 | 32 |
| 0.1301 | 0.2601 | 0.3902 | 0.5203 | 0.6503 | 0.7804 | 0.9105 | 1.0406 | 1.1706 | 0.1839 | 33 |
| 0.1303 | 0.2607 | 0.3910 | 0.5214 | 0.6517 | 0.7821 | 0.9124 | 1.0428 | 1.1731 | 0.1843 | 34 |
| 0.1306 | 0.2613 | 0.3919 | 0.5225 | 0.6532 | 0.7838 | 0.9144 | 1.0450 | 1.1757 | 0.1847 | 35 |
| 0.1309 | 0.2618 | 0.3927 | 0.5236 | 0.6546 | 0.7855 | 0.9164 | 1.0473 | 1.1782 | 0.1852 | 36 |
| 0.1312 | 0.2624 | 0.3936 | 0.5248 | 0.6560 | 0.7871 | 0.9183 | 1.0495 | 1.1807 | 0.1856 | 37 |
| 0.1315 | 0.2629 | 0.3944 | 0.5259 | 0.6574 | 0.7888 | 0.9203 | 1.0518 | 1.1832 | 0.1860 | 38 |
| 0.1318 | 0.2635 | 0.3953 | 0.5270 | 0.6588 | 0.7905 | 0.9223 | 1.0540 | 1.1858 | 0.1864 | 39 |
| 0.1320 | 0.2641 | 0.3961 | 0.5281 | 0.6602 | 0.7922 | 0.9242 | 1.0562 | 1.1883 | 0.1868 | 40 |
| 0.1323 | 0.2646 | 0.3969 | 0.5292 | 0.6616 | 0.7939 | 0.9262 | 1.0585 | 1.1908 | 0.1872 | 41 |
| 0.1326 | 0.2652 | 0.3978 | 0.5304 | 0.6630 | 0.7955 | 0.9281 | 1.0607 | 1.1933 | 0.1876 | 42 |
| 0.1329 | 0.2657 | 0.3986 | 0.5315 | 0.6644 | 0.7972 | 0.9301 | 1.0630 | 1.1958 | 0.1880 | 43 |
| 0.1332 | 0.2663 | 0.3995 | 0.5326 | 0.6658 | 0.7989 | 0.9321 | 1.0652 | 1.1984 | 0.1884 | 44 |
| 0.1334 | 0.2669 | 0.4003 | 0.5337 | 0.6672 | 0.8006 | 0.9340 | 1.0674 | 1.2009 | 0.1888 | 45 |
| 0.1337 | 0.2674 | 0.4011 | 0.5348 | 0.6686 | 0.8023 | 0.9360 | 1.0697 | 1.2034 | 0.1892 | 46 |
| 0.1340 | 0.2680 | 0.4020 | 0.5360 | 0.6700 | 0.8039 | 0.9379 | 1.0719 | 1.2059 | 0.1896 | 47 |
| 0.1343 | 0.2685 | 0.4028 | 0.5371 | 0.6714 | 0.8056 | 0.9399 | 1.0742 | 1.2084 | 0.1900 | 48 |
| 0.1346 | 0.2691 | 0.4037 | 0.5382 | 0.6728 | 0.8073 | 0.9419 | 1.0764 | 1.2110 | 0.1904 | 49 |
| 0.1348 | 0.2697 | 0.4045 | 0.5393 | 0.6742 | 0.8090 | 0.9438 | 1.0786 | 1.2135 | 0.1908 | 50 |
| 0.1351 | 0.2702 | 0.4053 | 0.5404 | 0.6756 | 0.8107 | 0.9458 | 1.0809 | 1.2160 | 0.1912 | 51 |
| 0.1354 | 0.2708 | 0.4062 | 0.5416 | 0.6770 | 0.8123 | 0.9477 | 1.0831 | 1.2185 | 0.1916 | 52 |
| 0.1357 | 0.2713 | 0.4070 | 0.5427 | 0.6783 | 0.8140 | 0.9497 | 1.0854 | 1.2210 | 0.1920 | 53 |
| 0.1359 | 0.2719 | 0.4078 | 0.5438 | 0.6797 | 0.8157 | 0.9516 | 1.0876 | 1.2235 | 0.1924 | 54 |
| 0.1362 | 0.2725 | 0.4087 | 0.5449 | 0.6811 | 0.8174 | 0.9536 | 1.0898 | 1.2261 | 0.1928 | 55 |
| 0.1365 | 0.2730 | 0.4095 | 0.5460 | 0.6825 | 0.8191 | 0.9556 | 1.0921 | 1.2286 | 0.1932 | 56 |
| 0.1368 | 0.2736 | 0.4104 | 0.5472 | 0.6839 | 0.8207 | 0.9575 | 1.0943 | 1.2311 | 0.1936 | 57 |
| 0.1371 | 0.2741 | 0.4112 | 0.5483 | 0.6853 | 0.8224 | 0.9595 | 1.0966 | 1.2336 | 0.1940 | 58 |
| 0.1374 | 0.2747 | 0.4121 | 0.5494 | 0.6867 | 0.8241 | 0.9615 | 1.0988 | 1.2362 | 0.1944 | 59 |
| 0.1376 | 0.2753 | 0.4129 | 0.5505 | 0.6881 | 0.8258 | 0.9634 | 1.1010 | 1.2387 | 0.1948 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9793 | 1.9585 | 2.9378 | 3.9170 | 4.8963 | 5.8755 | 6.8548 | 7.8341 | 8.8133 | 1.3864 |
| 01 | 0.9792 | 1.9584 | 2.9375 | 3.9167 | 4.8959 | 5.8751 | 6.8542 | 7.8334 | 8.8126 | 1.3863 |
| 02 | 0.9791 | 1.9582 | 2.9373 | 3.9164 | 4.8955 | 5.8746 | 6.8537 | 7.8328 | 8.8119 | 1.3862 |
| 03 | 0.9790 | 1.9580 | 2.9370 | 3.9161 | 4.8951 | 5.8741 | 6.8531 | 7.8321 | 8.8111 | 1.3861 |
| 04 | 0.9789 | 1.9579 | 2.9368 | 3.9157 | 4.8947 | 5.8736 | 6.8525 | 7.8315 | 8.8104 | 1.3861 |
| 05 | 0.9789 | 1.9577 | 2.9366 | 3.9154 | 4.8943 | 5.8731 | 6.8520 | 7.8308 | 8.8097 | 1.3861 |
| 06 | 0.9788 | 1.9575 | 2.9363 | 3.9151 | 4.8939 | 5.8726 | 6.8514 | 7.8302 | 8.8090 | 1.3860 |
| 07 | 0.9787 | 1.9574 | 2.9361 | 3.9148 | 4.8935 | 5.8722 | 6.8508 | 7.8295 | 8.8082 | 1.3860 |
| 08 | 0.9786 | 1.9572 | 2.9358 | 3.9144 | 4.8931 | 5.8717 | 6.8503 | 7.8289 | 8.8075 | 1.3859 |
| 09 | 0.9785 | 1.9571 | 2.9356 | 3.9141 | 4.8927 | 5.8712 | 6.8497 | 7.8282 | 8.8068 | 1.3859 |
| 10 | 0.9785 | 1.9569 | 2.9354 | 3.9138 | 4.8923 | 5.8707 | 6.8492 | 7.8276 | 8.8061 | 1.3858 |
| 11 | 0.9784 | 1.9567 | 2.9351 | 3.9135 | 4.8918 | 5.8702 | 6.8486 | 7.8269 | 8.8053 | 1.3858 |
| 12 | 0.9783 | 1.9566 | 2.9349 | 3.9131 | 4.8914 | 5.8697 | 6.8480 | 7.8263 | 8.8046 | 1.3857 |
| 13 | 0.9782 | 1.9564 | 2.9346 | 3.9128 | 4.8910 | 5.8692 | 6.8474 | 7.8256 | 8.8038 | 1.3856 |
| 14 | 0.9781 | 1.9562 | 2.9344 | 3.9125 | 4.8906 | 5.8687 | 6.8468 | 7.8250 | 8.8031 | 1.3856 |
| 15 | 0.9780 | 1.9561 | 2.9341 | 3.9122 | 4.8902 | 5.8682 | 6.8463 | 7.8243 | 8.8023 | 1.3855 |
| 16 | 0.9780 | 1.9559 | 2.9339 | 3.9118 | 4.8898 | 5.8677 | 6.8457 | 7.8236 | 8.8016 | 1.3854 |
| 17 | 0.9779 | 1.9557 | 2.9336 | 3.9115 | 4.8894 | 5.8672 | 6.8451 | 7.8230 | 8.8009 | 1.3854 |
| 18 | 0.9778 | 1.9556 | 2.9334 | 3.9112 | 4.8890 | 5.8667 | 6.8445 | 7.8223 | 8.8001 | 1.3853 |
| 19 | 0.9777 | 1.9554 | 2.9331 | 3.9108 | 4.8885 | 5.8662 | 6.8440 | 7.8217 | 8.7994 | 1.3853 |
| 20 | 0.9776 | 1.9553 | 2.9329 | 3.9105 | 4.8881 | 5.8657 | 6.8434 | 7.8210 | 8.7986 | 1.3852 |
| 21 | 0.9775 | 1.9551 | 2.9326 | 3.9102 | 4.8877 | 5.8652 | 6.8428 | 7.8203 | 8.7979 | 1.3852 |
| 22 | 0.9775 | 1.9549 | 2.9324 | 3.9098 | 4.8873 | 5.8647 | 6.8422 | 7.8197 | 8.7971 | 1.3851 |
| 23 | 0.9774 | 1.9547 | 2.9321 | 3.9095 | 4.8869 | 5.8642 | 6.8416 | 7.8190 | 8.7964 | 1.3850 |
| 24 | 0.9773 | 1.9546 | 2.9319 | 3.9092 | 4.8864 | 5.8637 | 6.8410 | 7.8183 | 8.7956 | 1.3850 |
| 25 | 0.9772 | 1.9544 | 2.9316 | 3.9088 | 4.8860 | 5.8632 | 6.8404 | 7.8176 | 8.7948 | 1.3849 |
| 26 | 0.9771 | 1.9542 | 2.9314 | 3.9085 | 4.8856 | 5.8627 | 6.8398 | 7.8170 | 8.7941 | 1.3849 |
| 27 | 0.9770 | 1.9541 | 2.9311 | 3.9081 | 4.8852 | 5.8622 | 6.8393 | 7.8163 | 8.7933 | 1.3848 |
| 28 | 0.9770 | 1.9539 | 2.9309 | 3.9078 | 4.8848 | 5.8617 | 6.8387 | 7.8156 | 8.7926 | 1.3847 |
| 29 | 0.9769 | 1.9537 | 2.9306 | 3.9075 | 4.8843 | 5.8612 | 6.8381 | 7.8149 | 8.7918 | 1.3847 |
| 30 | 0.9768 | 1.9535 | 2.9304 | 3.9071 | 4.8839 | 5.8607 | 6.8375 | 7.8143 | 8.7911 | 1.3846 |
| 31 | 0.9767 | 1.9534 | 2.9301 | 3.9068 | 4.8835 | 5.8602 | 6.8369 | 7.8136 | 8.7903 | 1.3846 |
| 32 | 0.9766 | 1.9532 | 2.9298 | 3.9064 | 4.8831 | 5.8597 | 6.8363 | 7.8129 | 8.7895 | 1.3845 |
| 33 | 0.9765 | 1.9531 | 2.9296 | 3.9061 | 4.8826 | 5.8592 | 6.8357 | 7.8122 | 8.7887 | 1.3844 |
| 34 | 0.9764 | 1.9529 | 2.9293 | 3.9058 | 4.8822 | 5.8586 | 6.8351 | 7.8115 | 8.7880 | 1.3844 |
| 35 | 0.9764 | 1.9527 | 2.9291 | 3.9054 | 4.8818 | 5.8581 | 6.8345 | 7.8108 | 8.7872 | 1.3843 |
| 36 | 0.9763 | 1.9525 | 2.9288 | 3.9051 | 4.8813 | 5.8576 | 6.8339 | 7.8102 | 8.7864 | 1.3843 |
| 37 | 0.9762 | 1.9524 | 2.9285 | 3.9047 | 4.8809 | 5.8571 | 6.8333 | 7.8095 | 8.7856 | 1.3842 |
| 38 | 0.9761 | 1.9522 | 2.9283 | 3.9044 | 4.8805 | 5.8566 | 6.8327 | 7.8088 | 8.7849 | 1.3841 |
| 39 | 0.9760 | 1.9520 | 2.9280 | 3.9040 | 4.8801 | 5.8561 | 6.8321 | 7.8081 | 8.7841 | 1.3841 |
| 40 | 0.9759 | 1.9519 | 2.9278 | 3.9037 | 4.8796 | 5.8556 | 6.8315 | 7.8074 | 8.7833 | 1.3840 |
| 41 | 0.9758 | 1.9517 | 2.9275 | 3.9034 | 4.8792 | 5.8550 | 6.8309 | 7.8067 | 8.7826 | 1.3840 |
| 42 | 0.9758 | 1.9515 | 2.9273 | 3.9030 | 4.8788 | 5.8545 | 6.8303 | 7.8060 | 8.7818 | 1.3839 |
| 43 | 0.9757 | 1.9513 | 2.9270 | 3.9027 | 4.8783 | 5.8540 | 6.8296 | 7.8053 | 8.7810 | 1.3838 |
| 44 | 0.9756 | 1.9512 | 2.9267 | 3.9023 | 4.8779 | 5.8535 | 6.8290 | 7.8046 | 8.7802 | 1.3838 |
| 45 | 0.9755 | 1.9510 | 2.9265 | 3.9020 | 4.8774 | 5.8529 | 6.8284 | 7.8039 | 8.7794 | 1.3837 |
| 46 | 0.9754 | 1.9508 | 2.9262 | 3.9016 | 4.8770 | 5.8524 | 6.8278 | 7.8032 | 8.7786 | 1.3837 |
| 47 | 0.9753 | 1.9506 | 2.9259 | 3.9013 | 4.8766 | 5.8519 | 6.8272 | 7.8025 | 8.7778 | 1.3836 |
| 48 | 0.9752 | 1.9505 | 2.9257 | 3.9009 | 4.8761 | 5.8514 | 6.8266 | 7.8018 | 8.7770 | 1.3835 |
| 49 | 0.9751 | 1.9503 | 2.9254 | 3.9006 | 4.8757 | 5.8508 | 6.8260 | 7.8011 | 8.7763 | 1.3835 |
| 50 | 0.9751 | 1.9501 | 2.9252 | 3.9002 | 4.8753 | 5.8503 | 6.8254 | 7.8004 | 8.7755 | 1.3834 |
| 51 | 0.9750 | 1.9499 | 2.9249 | 3.8999 | 4.8748 | 5.8498 | 6.8247 | 7.7997 | 8.7747 | 1.3834 |
| 52 | 0.9749 | 1.9497 | 2.9246 | 3.8995 | 4.8744 | 5.8492 | 6.8241 | 7.7990 | 8.7739 | 1.3833 |
| 53 | 0.9748 | 1.9496 | 2.9244 | 3.8991 | 4.8739 | 5.8487 | 6.8235 | 7.7983 | 8.7731 | 1.3832 |
| 54 | 0.9747 | 1.9494 | 2.9241 | 3.8988 | 4.8735 | 5.8482 | 6.8229 | 7.7976 | 8.7723 | 1.3832 |
| 55 | 0.9746 | 1.9492 | 2.9238 | 3.8984 | 4.8730 | 5.8476 | 6.8222 | 7.7969 | 8.7715 | 1.3831 |
| 56 | 0.9745 | 1.9490 | 2.9236 | 3.8981 | 4.8726 | 5.8471 | 6.8216 | 7.7961 | 8.7707 | 1.3831 |
| 57 | 0.9744 | 1.9489 | 2.9233 | 3.8977 | 4.8721 | 5.8466 | 6.8210 | 7.7954 | 8.7699 | 1.3830 |
| 58 | 0.9743 | 1.9487 | 2.9230 | 3.8974 | 4.8717 | 5.8460 | 6.8204 | 7.7947 | 8.7691 | 1.3829 |
| 59 | 0.9743 | 1.9485 | 2.9228 | 3.8970 | 4.8713 | 5.8455 | 6.8198 | 7.7940 | 8.7683 | 1.3828 |
| 60 | 0.9742 | 1.9483 | 2.9225 | 3.8966 | 4.8708 | 5.8450 | 6.8191 | 7.7933 | 8.7675 | 1.3828 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1376 | 0.2753 | 0.4129 | 0.5505 | 0.6881 | 0.8258 | 0.9634 | 1.1010 | 1.2387 | 0.1948 | 00 |
| 0.1380 | 0.2758 | 0.4137 | 0.5516 | 0.6895 | 0.8275 | 0.9654 | 1.1033 | 1.2412 | 0.1952 | 01 |
| 0.1382 | 0.2764 | 0.4145 | 0.5527 | 0.6909 | 0.8291 | 0.9673 | 1.1055 | 1.2437 | 0.1956 | 02 |
| 0.1385 | 0.2769 | 0.4154 | 0.5538 | 0.6923 | 0.8308 | 0.9692 | 1.1077 | 1.2462 | 0.1960 | 03 |
| 0.1387 | 0.2775 | 0.4162 | 0.5550 | 0.6937 | 0.8324 | 0.9712 | 1.1099 | 1.2487 | 0.1965 | 04 |
| 0.1390 | 0.2780 | 0.4171 | 0.5561 | 0.6951 | 0.8341 | 0.9731 | 1.1122 | 1.2512 | 0.1969 | 05 |
| 0.1393 | 0.2786 | 0.4179 | 0.5572 | 0.6965 | 0.8358 | 0.9751 | 1.1144 | 1.2537 | 0.1973 | 06 |
| 0.1396 | 0.2792 | 0.4187 | 0.5583 | 0.6979 | 0.8375 | 0.9771 | 1.1166 | 1.2562 | 0.1977 | 07 |
| 0.1399 | 0.2797 | 0.4196 | 0.5594 | 0.6993 | 0.8392 | 0.9790 | 1.1189 | 1.2587 | 0.1981 | 08 |
| 0.1401 | 0.2803 | 0.4204 | 0.5606 | 0.7007 | 0.8408 | 0.9810 | 1.1211 | 1.2613 | 0.1985 | 09 |
| 0.1404 | 0.2808 | 0.4213 | 0.5617 | 0.7021 | 0.8425 | 0.9829 | 1.1234 | 1.2638 | 0.1989 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1407 | 0.2814 | 0.4221 | 0.5628 | 0.7035 | 0.8441 | 0.9849 | 1.1256 | 1.2663 | 0.1993 | 11 |
| 0.1410 | 0.2819 | 0.4229 | 0.5639 | 0.7049 | 0.8458 | 0.9868 | 1.1278 | 1.2688 | 0.1997 | 12 |
| 0.1413 | 0.2825 | 0.4238 | 0.5650 | 0.7063 | 0.8475 | 0.9888 | 1.1300 | 1.2713 | 0.2001 | 13 |
| 0.1415 | 0.2831 | 0.4246 | 0.5661 | 0.7077 | 0.8492 | 0.9907 | 1.1322 | 1.2738 | 0.2005 | 14 |
| 0.1418 | 0.2836 | 0.4254 | 0.5672 | 0.7091 | 0.8509 | 0.9927 | 1.1345 | 1.2763 | 0.2009 | 15 |
| 0.1421 | 0.2842 | 0.4263 | 0.5684 | 0.7104 | 0.8525 | 0.9946 | 1.1367 | 1.2788 | 0.2013 | 16 |
| 0.1424 | 0.2847 | 0.4271 | 0.5695 | 0.7118 | 0.8542 | 0.9966 | 1.1390 | 1.2813 | 0.2017 | 17 |
| 0.1426 | 0.2853 | 0.4279 | 0.5706 | 0.7132 | 0.8558 | 0.9985 | 1.1412 | 1.2838 | 0.2021 | 18 |
| 0.1429 | 0.2858 | 0.4288 | 0.5717 | 0.7146 | 0.8575 | 1.0005 | 1.1434 | 1.2863 | 0.2025 | 19 |
| 0.1432 | 0.2864 | 0.4296 | 0.5728 | 0.7160 | 0.8592 | 1.0024 | 1.1456 | 1.2888 | 0.2029 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1435 | 0.2870 | 0.4304 | 0.5739 | 0.7174 | 0.8609 | 1.0044 | 1.1478 | 1.2913 | 0.2033 | 21 |
| 0.1438 | 0.2875 | 0.4313 | 0.5750 | 0.7188 | 0.8626 | 1.0063 | 1.1501 | 1.2938 | 0.2037 | 22 |
| 0.1440 | 0.2881 | 0.4321 | 0.5762 | 0.7202 | 0.8642 | 1.0083 | 1.1523 | 1.2963 | 0.2041 | 23 |
| 0.1443 | 0.2886 | 0.4329 | 0.5773 | 0.7216 | 0.8659 | 1.0102 | 1.1545 | 1.2988 | 0.2045 | 24 |
| 0.1446 | 0.2892 | 0.4338 | 0.5784 | 0.7230 | 0.8675 | 1.0121 | 1.1567 | 1.3013 | 0.2049 | 25 |
| 0.1449 | 0.2897 | 0.4346 | 0.5795 | 0.7243 | 0.8692 | 1.0141 | 1.1590 | 1.3038 | 0.2053 | 26 |
| 0.1451 | 0.2903 | 0.4354 | 0.5806 | 0.7257 | 0.8709 | 1.0160 | 1.1612 | 1.3063 | 0.2057 | 27 |
| 0.1454 | 0.2909 | 0.4363 | 0.5817 | 0.7271 | 0.8726 | 1.0180 | 1.1634 | 1.3088 | 0.2061 | 28 |
| 0.1457 | 0.2914 | 0.4371 | 0.5828 | 0.7285 | 0.8742 | 1.0199 | 1.1656 | 1.3113 | 0.2065 | 29 |
| 0.1460 | 0.2920 | 0.4379 | 0.5839 | 0.7299 | 0.8759 | 1.0219 | 1.1678 | 1.3138 | 0.2069 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1463 | 0.2925 | 0.4388 | 0.5850 | 0.7313 | 0.8776 | 1.0238 | 1.1701 | 1.3163 | 0.2073 | 31 |
| 0.1465 | 0.2931 | 0.4396 | 0.5862 | 0.7327 | 0.8792 | 1.0258 | 1.1723 | 1.3188 | 0.2077 | 32 |
| 0.1468 | 0.2936 | 0.4404 | 0.5873 | 0.7341 | 0.8809 | 1.0277 | 1.1745 | 1.3213 | 0.2081 | 33 |
| 0.1471 | 0.2942 | 0.4413 | 0.5884 | 0.7355 | 0.8825 | 1.0296 | 1.1767 | 1.3238 | 0.2085 | 34 |
| 0.1474 | 0.2947 | 0.4421 | 0.5895 | 0.7368 | 0.8842 | 1.0316 | 1.1790 | 1.3263 | 0.2089 | 35 |
| 0.1476 | 0.2953 | 0.4429 | 0.5906 | 0.7382 | 0.8859 | 1.0335 | 1.1812 | 1.3288 | 0.2093 | 36 |
| 0.1479 | 0.2958 | 0.4438 | 0.5917 | 0.7396 | 0.8875 | 1.0355 | 1.1834 | 1.3313 | 0.2097 | 37 |
| 0.1482 | 0.2964 | 0.4446 | 0.5928 | 0.7410 | 0.8892 | 1.0374 | 1.1856 | 1.3338 | 0.2101 | 38 |
| 0.1485 | 0.2970 | 0.4454 | 0.5939 | 0.7424 | 0.8909 | 1.0394 | 1.1878 | 1.3363 | 0.2105 | 39 |
| 0.1488 | 0.2975 | 0.4463 | 0.5950 | 0.7438 | 0.8926 | 1.0413 | 1.1901 | 1.3388 | 0.2110 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1490 | 0.2981 | 0.4471 | 0.5961 | 0.7452 | 0.8942 | 1.0432 | 1.1923 | 1.3413 | 0.2114 | 41 |
| 0.1493 | 0.2986 | 0.4479 | 0.5972 | 0.7466 | 0.8959 | 1.0452 | 1.1945 | 1.3438 | 0.2118 | 42 |
| 0.1496 | 0.2992 | 0.4488 | 0.5984 | 0.7479 | 0.8975 | 1.0471 | 1.1967 | 1.3463 | 0.2122 | 43 |
| 0.1499 | 0.2997 | 0.4496 | 0.5995 | 0.7493 | 0.8992 | 1.0491 | 1.1989 | 1.3488 | 0.2126 | 44 |
| 0.1501 | 0.3003 | 0.4504 | 0.6006 | 0.7507 | 0.9008 | 1.0510 | 1.2011 | 1.3513 | 0.2130 | 45 |
| 0.1504 | 0.3008 | 0.4513 | 0.6017 | 0.7521 | 0.9025 | 1.0529 | 1.2034 | 1.3538 | 0.2134 | 46 |
| 0.1507 | 0.3014 | 0.4521 | 0.6028 | 0.7535 | 0.9042 | 1.0549 | 1.2056 | 1.3563 | 0.2138 | 47 |
| 0.1510 | 0.3019 | 0.4529 | 0.6039 | 0.7549 | 0.9058 | 1.0568 | 1.2078 | 1.3588 | 0.2142 | 48 |
| 0.1513 | 0.3025 | 0.4538 | 0.6050 | 0.7563 | 0.9075 | 1.0588 | 1.2100 | 1.3613 | 0.2146 | 49 |
| 0.1515 | 0.3031 | 0.4546 | 0.6061 | 0.7576 | 0.9092 | 1.0607 | 1.2122 | 1.3638 | 0.2150 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1518 | 0.3036 | 0.4554 | 0.6072 | 0.7590 | 0.9108 | 1.0626 | 1.2144 | 1.3663 | 0.2154 | 51 |
| 0.1521 | 0.3042 | 0.4562 | 0.6083 | 0.7604 | 0.9125 | 1.0646 | 1.2166 | 1.3687 | 0.2158 | 52 |
| 0.1524 | 0.3047 | 0.4571 | 0.6094 | 0.7618 | 0.9142 | 1.0665 | 1.2189 | 1.3712 | 0.2162 | 53 |
| 0.1526 | 0.3053 | 0.4579 | 0.6105 | 0.7632 | 0.9158 | 1.0684 | 1.2211 | 1.3737 | 0.2166 | 54 |
| 0.1529 | 0.3058 | 0.4587 | 0.6116 | 0.7646 | 0.9175 | 1.0704 | 1.2233 | 1.3762 | 0.2170 | 55 |
| 0.1532 | 0.3064 | 0.4596 | 0.6128 | 0.7660 | 0.9191 | 1.0723 | 1.2255 | 1.3787 | 0.2174 | 56 |
| 0.1535 | 0.3069 | 0.4604 | 0.6139 | 0.7673 | 0.9208 | 1.0742 | 1.2277 | 1.3812 | 0.2178 | 57 |
| 0.1537 | 0.3075 | 0.4612 | 0.6150 | 0.7687 | 0.9224 | 1.0762 | 1.2299 | 1.3837 | 0.2182 | 58 |
| 0.1540 | 0.3080 | 0.4621 | 0.6161 | 0.7701 | 0.9241 | 1.0781 | 1.2321 | 1.3862 | 0.2186 | 59 |
| 0.1543 | 0.3086 | 0.4629 | 0.6172 | 0.7715 | 0.9257 | 1.0800 | 1.2343 | 1.3886 | 0.2190 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9793 | 1.9585 | 2.9378 | 3.9170 | 4.8963 | 5.8755 | 6.8548 | 7.8341 | 8.8133 | 1.3864 |
| 01 | 0.9792 | 1.9584 | 2.9375 | 3.9167 | 4.8959 | 5.8751 | 6.8542 | 7.8334 | 8.8126 | 1.3863 |
| 02 | 0.9791 | 1.9582 | 2.9373 | 3.9164 | 4.8955 | 5.8746 | 6.8537 | 7.8328 | 8.8119 | 1.3862 |
| 03 | 0.9790 | 1.9580 | 2.9370 | 3.9161 | 4.8951 | 5.8741 | 6.8531 | 7.8321 | 8.8111 | 1.3861 |
| 04 | 0.9789 | 1.9579 | 2.9368 | 3.9157 | 4.8947 | 5.8736 | 6.8525 | 7.8315 | 8.8104 | 1.3861 |
| 05 | 0.9789 | 1.9577 | 2.9366 | 3.9154 | 4.8943 | 5.8731 | 6.8520 | 7.8308 | 8.8097 | 1.3861 |
| 06 | 0.9788 | 1.9575 | 2.9363 | 3.9151 | 4.8939 | 5.8726 | 6.8514 | 7.8302 | 8.8090 | 1.3860 |
| 07 | 0.9787 | 1.9574 | 2.9361 | 3.9148 | 4.8935 | 5.8722 | 6.8508 | 7.8295 | 8.8082 | 1.3860 |
| 08 | 0.9786 | 1.9572 | 2.9358 | 3.9144 | 4.8931 | 5.8717 | 6.8503 | 7.8289 | 8.8075 | 1.3859 |
| 09 | 0.9785 | 1.9571 | 2.9356 | 3.9141 | 4.8927 | 5.8712 | 6.8497 | 7.8282 | 8.8068 | 1.3859 |
| 10 | 0.9785 | 1.9569 | 2.9354 | 3.9138 | 4.8923 | 5.8707 | 6.8492 | 7.8276 | 8.8061 | 1.3858 |
| 11 | 0.9784 | 1.9567 | 2.9351 | 3.9135 | 4.8918 | 5.8702 | 6.8486 | 7.8269 | 8.8053 | 1.3858 |
| 12 | 0.9783 | 1.9566 | 2.9349 | 3.9131 | 4.8914 | 5.8697 | 6.8480 | 7.8263 | 8.8046 | 1.3857 |
| 13 | 0.9782 | 1.9564 | 2.9346 | 3.9128 | 4.8910 | 5.8692 | 6.8474 | 7.8256 | 8.8038 | 1.3856 |
| 14 | 0.9781 | 1.9562 | 2.9344 | 3.9125 | 4.8906 | 5.8687 | 6.8468 | 7.8250 | 8.8031 | 1.3856 |
| 15 | 0.9780 | 1.9561 | 2.9341 | 3.9122 | 4.8902 | 5.8682 | 6.8463 | 7.8243 | 8.8023 | 1.3855 |
| 16 | 0.9780 | 1.9559 | 2.9339 | 3.9118 | 4.8898 | 5.8677 | 6.8457 | 7.8236 | 8.8016 | 1.3854 |
| 17 | 0.9779 | 1.9557 | 2.9336 | 3.9115 | 4.8894 | 5.8672 | 6.8451 | 7.8230 | 8.8009 | 1.3854 |
| 18 | 0.9778 | 1.9556 | 2.9334 | 3.9112 | 4.8890 | 5.8667 | 6.8445 | 7.8223 | 8.8001 | 1.3853 |
| 19 | 0.9777 | 1.9554 | 2.9331 | 3.9108 | 4.8885 | 5.8662 | 6.8440 | 7.8217 | 8.7994 | 1.3853 |
| 20 | 0.9776 | 1.9553 | 2.9329 | 3.9105 | 4.8881 | 5.8657 | 6.8434 | 7.8210 | 8.7986 | 1.3852 |
| 21 | 0.9775 | 1.9551 | 2.9326 | 3.9102 | 4.8877 | 5.8652 | 6.8428 | 7.8203 | 8.7979 | 1.3852 |
| 22 | 0.9775 | 1.9549 | 2.9324 | 3.9098 | 4.8873 | 5.8647 | 6.8422 | 7.8197 | 8.7971 | 1.3851 |
| 23 | 0.9774 | 1.9547 | 2.9321 | 3.9095 | 4.8869 | 5.8642 | 6.8416 | 7.8190 | 8.7964 | 1.3850 |
| 24 | 0.9773 | 1.9546 | 2.9319 | 3.9092 | 4.8864 | 5.8637 | 6.8410 | 7.8183 | 8.7956 | 1.3850 |
| 25 | 0.9772 | 1.9544 | 2.9316 | 3.9088 | 4.8860 | 5.8632 | 6.8404 | 7.8176 | 8.7948 | 1.3849 |
| 26 | 0.9771 | 1.9542 | 2.9314 | 3.9085 | 4.8856 | 5.8627 | 6.8398 | 7.8170 | 8.7941 | 1.3849 |
| 27 | 0.9770 | 1.9541 | 2.9311 | 3.9081 | 4.8852 | 5.8622 | 6.8393 | 7.8163 | 8.7933 | 1.3848 |
| 28 | 0.9770 | 1.9539 | 2.9309 | 3.9078 | 4.8848 | 5.8617 | 6.8387 | 7.8156 | 8.7926 | 1.3847 |
| 29 | 0.9769 | 1.9537 | 2.9306 | 3.9075 | 4.8843 | 5.8612 | 6.8381 | 7.8149 | 8.7918 | 1.3847 |
| 30 | 0.9768 | 1.9536 | 2.9304 | 3.9071 | 4.8839 | 5.8607 | 6.8375 | 7.8143 | 8.7911 | 1.3846 |
| 31 | 0.9767 | 1.9534 | 2.9301 | 3.9068 | 4.8835 | 5.8602 | 6.8369 | 7.8136 | 8.7903 | 1.3846 |
| 32 | 0.9766 | 1.9532 | 2.9298 | 3.9064 | 4.8831 | 5.8597 | 6.8363 | 7.8129 | 8.7895 | 1.3845 |
| 33 | 0.9765 | 1.9531 | 2.9296 | 3.9061 | 4.8826 | 5.8592 | 6.8357 | 7.8122 | 8.7887 | 1.3844 |
| 34 | 0.9764 | 1.9529 | 2.9293 | 3.9058 | 4.8822 | 5.8586 | 6.8351 | 7.8115 | 8.7880 | 1.3844 |
| 35 | 0.9764 | 1.9527 | 2.9291 | 3.9054 | 4.8818 | 5.8581 | 6.8345 | 7.8108 | 8.7872 | 1.3843 |
| 36 | 0.9763 | 1.9525 | 2.9288 | 3.9051 | 4.8813 | 5.8576 | 6.8339 | 7.8102 | 8.7864 | 1.3843 |
| 37 | 0.9762 | 1.9524 | 2.9285 | 3.9047 | 4.8809 | 5.8571 | 6.8333 | 7.8095 | 8.7856 | 1.3842 |
| 38 | 0.9761 | 1.9522 | 2.9283 | 3.9044 | 4.8805 | 5.8566 | 6.8327 | 7.8088 | 8.7849 | 1.3841 |
| 39 | 0.9760 | 1.9520 | 2.9280 | 3.9040 | 4.8801 | 5.8561 | 6.8321 | 7.8081 | 8.7841 | 1.3841 |
| 40 | 0.9759 | 1.9519 | 2.9278 | 3.9037 | 4.8796 | 5.8556 | 6.8315 | 7.8074 | 8.7833 | 1.3840 |
| 41 | 0.9758 | 1.9517 | 2.9275 | 3.9034 | 4.8792 | 5.8550 | 6.8309 | 7.8067 | 8.7826 | 1.3840 |
| 42 | 0.9758 | 1.9515 | 2.9273 | 3.9030 | 4.8788 | 5.8545 | 6.8303 | 7.8060 | 8.7818 | 1.3839 |
| 43 | 0.9757 | 1.9513 | 2.9270 | 3.9027 | 4.8783 | 5.8540 | 6.8296 | 7.8053 | 8.7810 | 1.3838 |
| 44 | 0.9756 | 1.9512 | 2.9267 | 3.9023 | 4.8779 | 5.8535 | 6.8290 | 7.8046 | 8.7802 | 1.3838 |
| 45 | 0.9755 | 1.9510 | 2.9265 | 3.9020 | 4.8774 | 5.8529 | 6.8284 | 7.8039 | 8.7794 | 1.3837 |
| 46 | 0.9754 | 1.9508 | 2.9262 | 3.9016 | 4.8770 | 5.8524 | 6.8278 | 7.8032 | 8.7786 | 1.3837 |
| 47 | 0.9753 | 1.9506 | 2.9259 | 3.9013 | 4.8766 | 5.8519 | 6.8272 | 7.8025 | 8.7778 | 1.3836 |
| 48 | 0.9752 | 1.9505 | 2.9257 | 3.9009 | 4.8761 | 5.8514 | 6.8266 | 7.8018 | 8.7770 | 1.3835 |
| 49 | 0.9751 | 1.9503 | 2.9254 | 3.9006 | 4.8757 | 5.8508 | 6.8260 | 7.8011 | 8.7763 | 1.3835 |
| 50 | 0.9751 | 1.9501 | 2.9252 | 3.9002 | 4.8753 | 5.8503 | 6.8254 | 7.8004 | 8.7755 | 1.3834 |
| 51 | 0.9750 | 1.9499 | 2.9249 | 3.8999 | 4.8748 | 5.8498 | 6.8247 | 7.7997 | 8.7747 | 1.3834 |
| 52 | 0.9749 | 1.9497 | 2.9246 | 3.8995 | 4.8744 | 5.8492 | 6.8241 | 7.7990 | 8.7739 | 1.3833 |
| 53 | 0.9748 | 1.9496 | 2.9244 | 3.8991 | 4.8739 | 5.8487 | 6.8235 | 7.7983 | 8.7731 | 1.3832 |
| 54 | 0.9747 | 1.9494 | 2.9241 | 3.8988 | 4.8735 | 5.8482 | 6.8229 | 7.7976 | 8.7723 | 1.3832 |
| 55 | 0.9746 | 1.9492 | 2.9238 | 3.8984 | 4.8730 | 5.8476 | 6.8222 | 7.7969 | 8.7715 | 1.3831 |
| 56 | 0.9745 | 1.9490 | 2.9236 | 3.8981 | 4.8726 | 5.8471 | 6.8216 | 7.7961 | 8.7707 | 1.3831 |
| 57 | 0.9744 | 1.9489 | 2.9233 | 3.8977 | 4.8721 | 5.8466 | 6.8210 | 7.7954 | 8.7699 | 1.3830 |
| 58 | 0.9743 | 1.9487 | 2.9230 | 3.8974 | 4.8717 | 5.8460 | 6.8204 | 7.7947 | 8.7691 | 1.3829 |
| 59 | 0.9743 | 1.9485 | 2.9228 | 3.8970 | 4.8713 | 5.8455 | 6.8198 | 7.7940 | 8.7683 | 1.3829 |
| 60 | 0.9742 | 1.9483 | 2.9225 | 3.8966 | 4.8708 | 5.8450 | 6.8191 | 7.7933 | 8.7675 | 1.3828 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1376 | 0.2753 | 0.4129 | 0.5505 | 0.6881 | 0.8258 | 0.9634 | 1.1010 | 1.2387 | 0.1948 | 00 |
| 0.1380 | 0.2758 | 0.4137 | 0.5516 | 0.6895 | 0.8275 | 0.9654 | 1.1033 | 1.2412 | 0.1952 | 01 |
| 0.1382 | 0.2764 | 0.4145 | 0.5527 | 0.6909 | 0.8291 | 0.9673 | 1.1055 | 1.2437 | 0.1956 | 02 |
| 0.1385 | 0.2769 | 0.4154 | 0.5538 | 0.6923 | 0.8308 | 0.9692 | 1.1077 | 1.2462 | 0.1960 | 03 |
| 0.1387 | 0.2775 | 0.4162 | 0.5550 | 0.6937 | 0.8324 | 0.9712 | 1.1099 | 1.2487 | 0.1965 | 04 |
| 0.1390 | 0.2780 | 0.4171 | 0.5561 | 0.6951 | 0.8341 | 0.9731 | 1.1122 | 1.2512 | 0.1969 | 05 |
| 0.1393 | 0.2786 | 0.4179 | 0.5572 | 0.6965 | 0.8358 | 0.9751 | 1.1144 | 1.2537 | 0.1973 | 06 |
| 0.1396 | 0.2792 | 0.4187 | 0.5583 | 0.6979 | 0.8375 | 0.9771 | 1.1166 | 1.2562 | 0.1977 | 07 |
| 0.1399 | 0.2797 | 0.4196 | 0.5594 | 0.6993 | 0.8392 | 0.9790 | 1.1189 | 1.2587 | 0.1981 | 08 |
| 0.1401 | 0.2803 | 0.4204 | 0.5606 | 0.7007 | 0.8408 | 0.9810 | 1.1211 | 1.2613 | 0.1985 | 09 |
| 0.1404 | 0.2808 | 0.4213 | 0.5617 | 0.7021 | 0.8425 | 0.9829 | 1.1234 | 1.2638 | 0.1989 | 10 |
| 0.1407 | 0.2814 | 0.4221 | 0.5628 | 0.7035 | 0.8441 | 0.9849 | 1.1256 | 1.2663 | 0.1993 | 11 |
| 0.1410 | 0.2819 | 0.4229 | 0.5639 | 0.7049 | 0.8458 | 0.9868 | 1.1278 | 1.2688 | 0.1997 | 12 |
| 0.1413 | 0.2825 | 0.4238 | 0.5650 | 0.7063 | 0.8475 | 0.9888 | 1.1300 | 1.2713 | 0.2001 | 13 |
| 0.1415 | 0.2831 | 0.4246 | 0.5661 | 0.7077 | 0.8492 | 0.9907 | 1.1322 | 1.2738 | 0.2005 | 14 |
| 0.1418 | 0.2836 | 0.4254 | 0.5672 | 0.7091 | 0.8509 | 0.9927 | 1.1345 | 1.2763 | 0.2009 | 15 |
| 0.1421 | 0.2842 | 0.4263 | 0.5684 | 0.7104 | 0.8525 | 0.9946 | 1.1367 | 1.2788 | 0.2013 | 16 |
| 0.1424 | 0.2847 | 0.4271 | 0.5695 | 0.7118 | 0.8542 | 0.9966 | 1.1390 | 1.2813 | 0.2017 | 17 |
| 0.1426 | 0.2853 | 0.4279 | 0.5706 | 0.7132 | 0.8558 | 0.9985 | 1.1412 | 1.2838 | 0.2021 | 18 |
| 0.1429 | 0.2858 | 0.4288 | 0.5717 | 0.7146 | 0.8575 | 1.0005 | 1.1434 | 1.2863 | 0.2025 | 19 |
| 0.1432 | 0.2864 | 0.4296 | 0.5728 | 0.7160 | 0.8592 | 1.0024 | 1.1456 | 1.2888 | 0.2029 | 20 |
| 0.1435 | 0.2870 | 0.4304 | 0.5739 | 0.7174 | 0.8609 | 1.0044 | 1.1478 | 1.2913 | 0.2033 | 21 |
| 0.1438 | 0.2875 | 0.4313 | 0.5750 | 0.7188 | 0.8626 | 1.0063 | 1.1501 | 1.2938 | 0.2037 | 22 |
| 0.1440 | 0.2881 | 0.4321 | 0.5762 | 0.7202 | 0.8642 | 1.0083 | 1.1523 | 1.2963 | 0.2041 | 23 |
| 0.1443 | 0.2886 | 0.4329 | 0.5773 | 0.7216 | 0.8659 | 1.0102 | 1.1545 | 1.2988 | 0.2045 | 24 |
| 0.1446 | 0.2892 | 0.4338 | 0.5784 | 0.7230 | 0.8675 | 1.0121 | 1.1567 | 1.3013 | 0.2049 | 25 |
| 0.1449 | 0.2897 | 0.4346 | 0.5795 | 0.7243 | 0.8692 | 1.0141 | 1.1590 | 1.3038 | 0.2053 | 26 |
| 0.1451 | 0.2903 | 0.4354 | 0.5806 | 0.7257 | 0.8709 | 1.0160 | 1.1612 | 1.3063 | 0.2057 | 27 |
| 0.1454 | 0.2909 | 0.4363 | 0.5817 | 0.7271 | 0.8726 | 1.0180 | 1.1634 | 1.3088 | 0.2061 | 28 |
| 0.1457 | 0.2914 | 0.4371 | 0.5828 | 0.7285 | 0.8742 | 1.0199 | 1.1656 | 1.3113 | 0.2065 | 29 |
| 0.1460 | 0.2920 | 0.4379 | 0.5839 | 0.7299 | 0.8759 | 1.0219 | 1.1678 | 1.3138 | 0.2069 | 30 |
| 0.1463 | 0.2925 | 0.4388 | 0.5850 | 0.7313 | 0.8776 | 1.0238 | 1.1701 | 1.3163 | 0.2073 | 31 |
| 0.1465 | 0.2931 | 0.4396 | 0.5862 | 0.7327 | 0.8792 | 1.0258 | 1.1723 | 1.3188 | 0.2077 | 32 |
| 0.1468 | 0.2936 | 0.4404 | 0.5873 | 0.7341 | 0.8809 | 1.0277 | 1.1745 | 1.3213 | 0.2081 | 33 |
| 0.1471 | 0.2942 | 0.4413 | 0.5884 | 0.7355 | 0.8825 | 1.0296 | 1.1767 | 1.3238 | 0.2085 | 34 |
| 0.1474 | 0.2947 | 0.4421 | 0.5895 | 0.7368 | 0.8842 | 1.0316 | 1.1790 | 1.3263 | 0.2089 | 35 |
| 0.1476 | 0.2953 | 0.4429 | 0.5906 | 0.7382 | 0.8859 | 1.0335 | 1.1812 | 1.3288 | 0.2093 | 36 |
| 0.1479 | 0.2958 | 0.4438 | 0.5917 | 0.7396 | 0.8875 | 1.0355 | 1.1834 | 1.3313 | 0.2097 | 37 |
| 0.1482 | 0.2964 | 0.4446 | 0.5928 | 0.7410 | 0.8892 | 1.0374 | 1.1856 | 1.3338 | 0.2101 | 38 |
| 0.1485 | 0.2970 | 0.4454 | 0.5939 | 0.7424 | 0.8909 | 1.0394 | 1.1878 | 1.3363 | 0.2105 | 39 |
| 0.1488 | 0.2975 | 0.4463 | 0.5950 | 0.7438 | 0.8926 | 1.0413 | 1.1901 | 1.3388 | 0.2110 | 40 |
| 0.1490 | 0.2981 | 0.4471 | 0.5961 | 0.7452 | 0.8942 | 1.0432 | 1.1923 | 1.3413 | 0.2114 | 41 |
| 0.1493 | 0.2986 | 0.4479 | 0.5972 | 0.7466 | 0.8959 | 1.0452 | 1.1945 | 1.3438 | 0.2118 | 42 |
| 0.1496 | 0.2992 | 0.4488 | 0.5984 | 0.7479 | 0.8975 | 1.0471 | 1.1967 | 1.3463 | 0.2122 | 43 |
| 0.1499 | 0.2997 | 0.4496 | 0.5995 | 0.7493 | 0.8992 | 1.0491 | 1.1989 | 1.3488 | 0.2126 | 44 |
| 0.1501 | 0.3003 | 0.4504 | 0.6006 | 0.7507 | 0.9008 | 1.0510 | 1.2011 | 1.3513 | 0.2130 | 45 |
| 0.1504 | 0.3008 | 0.4513 | 0.6017 | 0.7521 | 0.9025 | 1.0529 | 1.2034 | 1.3538 | 0.2134 | 46 |
| 0.1507 | 0.3014 | 0.4521 | 0.6028 | 0.7535 | 0.9042 | 1.0549 | 1.2056 | 1.3563 | 0.2138 | 47 |
| 0.1510 | 0.3019 | 0.4529 | 0.6039 | 0.7549 | 0.9058 | 1.0568 | 1.2078 | 1.3588 | 0.2142 | 48 |
| 0.1513 | 0.3025 | 0.4538 | 0.6050 | 0.7563 | 0.9075 | 1.0588 | 1.2100 | 1.3613 | 0.2146 | 49 |
| 0.1515 | 0.3031 | 0.4546 | 0.6061 | 0.7576 | 0.9092 | 1.0607 | 1.2122 | 1.3638 | 0.2150 | 50 |
| 0.1518 | 0.3036 | 0.4554 | 0.6072 | 0.7590 | 0.9108 | 1.0626 | 1.2144 | 1.3662 | 0.2154 | 51 |
| 0.1521 | 0.3042 | 0.4562 | 0.6083 | 0.7604 | 0.9125 | 1.0646 | 1.2166 | 1.3687 | 0.2158 | 52 |
| 0.1524 | 0.3047 | 0.4571 | 0.6094 | 0.7618 | 0.9142 | 1.0665 | 1.2189 | 1.3711 | 0.2162 | 53 |
| 0.1526 | 0.3053 | 0.4579 | 0.6105 | 0.7632 | 0.9158 | 1.0684 | 1.2211 | 1.3737 | 0.2166 | 54 |
| 0.1529 | 0.3058 | 0.4587 | 0.6116 | 0.7646 | 0.9175 | 1.0704 | 1.2233 | 1.3762 | 0.2170 | 55 |
| 0.1532 | 0.3064 | 0.4596 | 0.6128 | 0.7660 | 0.9191 | 1.0723 | 1.2255 | 1.3787 | 0.2174 | 56 |
| 0.1535 | 0.3069 | 0.4604 | 0.6139 | 0.7673 | 0.9208 | 1.0742 | 1.2277 | 1.3812 | 0.2178 | 57 |
| 0.1537 | 0.3075 | 0.4612 | 0.6150 | 0.7687 | 0.9224 | 1.0762 | 1.2299 | 1.3837 | 0.2182 | 58 |
| 0.1540 | 0.3080 | 0.4621 | 0.6161 | 0.7701 | 0.9241 | 1.0781 | 1.2321 | 1.3862 | 0.2186 | 59 |
| 0.1543 | 0.3086 | 0.4629 | 0.6172 | 0.7715 | 0.9257 | 1.0800 | 1.2343 | 1.3886 | 0.2190 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 0      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 2.5740 | 1.5463 | 2.5225 | 3.4986 | 4.4748 | 5.4509 | 6.4271 | 7.4033 | 8.3795 | 1.3558 |
| 01 | 2.5741 | 1.5464 | 2.5226 | 3.4987 | 4.4749 | 5.4510 | 6.4272 | 7.4034 | 8.3796 | 1.3559 |
| 02 | 2.5742 | 1.5465 | 2.5227 | 3.4988 | 4.4750 | 5.4511 | 6.4273 | 7.4035 | 8.3797 | 1.3560 |
| 03 | 2.5743 | 1.5466 | 2.5228 | 3.4989 | 4.4751 | 5.4512 | 6.4274 | 7.4036 | 8.3798 | 1.3561 |
| 04 | 2.5744 | 1.5467 | 2.5229 | 3.4990 | 4.4752 | 5.4513 | 6.4275 | 7.4037 | 8.3799 | 1.3562 |
| 05 | 2.5745 | 1.5468 | 2.5230 | 3.4991 | 4.4753 | 5.4514 | 6.4276 | 7.4038 | 8.3800 | 1.3563 |
| 06 | 2.5746 | 1.5469 | 2.5231 | 3.4992 | 4.4754 | 5.4515 | 6.4277 | 7.4039 | 8.3801 | 1.3564 |
| 07 | 2.5747 | 1.5470 | 2.5232 | 3.4993 | 4.4755 | 5.4516 | 6.4278 | 7.4040 | 8.3802 | 1.3565 |
| 08 | 2.5748 | 1.5471 | 2.5233 | 3.4994 | 4.4756 | 5.4517 | 6.4279 | 7.4041 | 8.3803 | 1.3566 |
| 09 | 2.5749 | 1.5472 | 2.5234 | 3.4995 | 4.4757 | 5.4518 | 6.4280 | 7.4042 | 8.3804 | 1.3567 |
| 10 | 2.5750 | 1.5473 | 2.5235 | 3.4996 | 4.4758 | 5.4519 | 6.4281 | 7.4043 | 8.3805 | 1.3568 |
| 11 | 2.5751 | 1.5474 | 2.5236 | 3.4997 | 4.4759 | 5.4520 | 6.4282 | 7.4044 | 8.3806 | 1.3569 |
| 12 | 2.5752 | 1.5475 | 2.5237 | 3.4998 | 4.4760 | 5.4521 | 6.4283 | 7.4045 | 8.3807 | 1.3570 |
| 13 | 2.5753 | 1.5476 | 2.5238 | 3.4999 | 4.4761 | 5.4522 | 6.4284 | 7.4046 | 8.3808 | 1.3571 |
| 14 | 2.5754 | 1.5477 | 2.5239 | 3.5000 | 4.4762 | 5.4523 | 6.4285 | 7.4047 | 8.3809 | 1.3572 |
| 15 | 2.5755 | 1.5478 | 2.5240 | 3.5001 | 4.4763 | 5.4524 | 6.4286 | 7.4048 | 8.3810 | 1.3573 |
| 16 | 2.5756 | 1.5479 | 2.5241 | 3.5002 | 4.4764 | 5.4525 | 6.4287 | 7.4049 | 8.3811 | 1.3574 |
| 17 | 2.5757 | 1.5480 | 2.5242 | 3.5003 | 4.4765 | 5.4526 | 6.4288 | 7.4050 | 8.3812 | 1.3575 |
| 18 | 2.5758 | 1.5481 | 2.5243 | 3.5004 | 4.4766 | 5.4527 | 6.4289 | 7.4051 | 8.3813 | 1.3576 |
| 19 | 2.5759 | 1.5482 | 2.5244 | 3.5005 | 4.4767 | 5.4528 | 6.4290 | 7.4052 | 8.3814 | 1.3577 |
| 20 | 2.5760 | 1.5483 | 2.5245 | 3.5006 | 4.4768 | 5.4529 | 6.4291 | 7.4053 | 8.3815 | 1.3578 |
| 21 | 2.5761 | 1.5484 | 2.5246 | 3.5007 | 4.4769 | 5.4530 | 6.4292 | 7.4054 | 8.3816 | 1.3579 |
| 22 | 2.5762 | 1.5485 | 2.5247 | 3.5008 | 4.4770 | 5.4531 | 6.4293 | 7.4055 | 8.3817 | 1.3580 |
| 23 | 2.5763 | 1.5486 | 2.5248 | 3.5009 | 4.4771 | 5.4532 | 6.4294 | 7.4056 | 8.3818 | 1.3581 |
| 24 | 2.5764 | 1.5487 | 2.5249 | 3.5010 | 4.4772 | 5.4533 | 6.4295 | 7.4057 | 8.3819 | 1.3582 |
| 25 | 2.5765 | 1.5488 | 2.5250 | 3.5011 | 4.4773 | 5.4534 | 6.4296 | 7.4058 | 8.3820 | 1.3583 |
| 26 | 2.5766 | 1.5489 | 2.5251 | 3.5012 | 4.4774 | 5.4535 | 6.4297 | 7.4059 | 8.3821 | 1.3584 |
| 27 | 2.5767 | 1.5490 | 2.5252 | 3.5013 | 4.4775 | 5.4536 | 6.4298 | 7.4060 | 8.3822 | 1.3585 |
| 28 | 2.5768 | 1.5491 | 2.5253 | 3.5014 | 4.4776 | 5.4537 | 6.4299 | 7.4061 | 8.3823 | 1.3586 |
| 29 | 2.5769 | 1.5492 | 2.5254 | 3.5015 | 4.4777 | 5.4538 | 6.4300 | 7.4062 | 8.3824 | 1.3587 |
| 30 | 2.5770 | 1.5493 | 2.5255 | 3.5016 | 4.4778 | 5.4539 | 6.4301 | 7.4063 | 8.3825 | 1.3588 |
| 31 | 2.5771 | 1.5494 | 2.5256 | 3.5017 | 4.4779 | 5.4540 | 6.4302 | 7.4064 | 8.3826 | 1.3589 |
| 32 | 2.5772 | 1.5495 | 2.5257 | 3.5018 | 4.4780 | 5.4541 | 6.4303 | 7.4065 | 8.3827 | 1.3590 |
| 33 | 2.5773 | 1.5496 | 2.5258 | 3.5019 | 4.4781 | 5.4542 | 6.4304 | 7.4066 | 8.3828 | 1.3591 |
| 34 | 2.5774 | 1.5497 | 2.5259 | 3.5020 | 4.4782 | 5.4543 | 6.4305 | 7.4067 | 8.3829 | 1.3592 |
| 35 | 2.5775 | 1.5498 | 2.5260 | 3.5021 | 4.4783 | 5.4544 | 6.4306 | 7.4068 | 8.3830 | 1.3593 |
| 36 | 2.5776 | 1.5499 | 2.5261 | 3.5022 | 4.4784 | 5.4545 | 6.4307 | 7.4069 | 8.3831 | 1.3594 |
| 37 | 2.5777 | 1.5500 | 2.5262 | 3.5023 | 4.4785 | 5.4546 | 6.4308 | 7.4070 | 8.3832 | 1.3595 |
| 38 | 2.5778 | 1.5501 | 2.5263 | 3.5024 | 4.4786 | 5.4547 | 6.4309 | 7.4071 | 8.3833 | 1.3596 |
| 39 | 2.5779 | 1.5502 | 2.5264 | 3.5025 | 4.4787 | 5.4548 | 6.4310 | 7.4072 | 8.3834 | 1.3597 |
| 40 | 2.5780 | 1.5503 | 2.5265 | 3.5026 | 4.4788 | 5.4549 | 6.4311 | 7.4073 | 8.3835 | 1.3598 |
| 41 | 2.5781 | 1.5504 | 2.5266 | 3.5027 | 4.4789 | 5.4550 | 6.4312 | 7.4074 | 8.3836 | 1.3599 |
| 42 | 2.5782 | 1.5505 | 2.5267 | 3.5028 | 4.4790 | 5.4551 | 6.4313 | 7.4075 | 8.3837 | 1.3600 |
| 43 | 2.5783 | 1.5506 | 2.5268 | 3.5029 | 4.4791 | 5.4552 | 6.4314 | 7.4076 | 8.3838 | 1.3601 |
| 44 | 2.5784 | 1.5507 | 2.5269 | 3.5030 | 4.4792 | 5.4553 | 6.4315 | 7.4077 | 8.3839 | 1.3602 |
| 45 | 2.5785 | 1.5508 | 2.5270 | 3.5031 | 4.4793 | 5.4554 | 6.4316 | 7.4078 | 8.3840 | 1.3603 |
| 46 | 2.5786 | 1.5509 | 2.5271 | 3.5032 | 4.4794 | 5.4555 | 6.4317 | 7.4079 | 8.3841 | 1.3604 |
| 47 | 2.5787 | 1.5510 | 2.5272 | 3.5033 | 4.4795 | 5.4556 | 6.4318 | 7.4080 | 8.3842 | 1.3605 |
| 48 | 2.5788 | 1.5511 | 2.5273 | 3.5034 | 4.4796 | 5.4557 | 6.4319 | 7.4081 | 8.3843 | 1.3606 |
| 49 | 2.5789 | 1.5512 | 2.5274 | 3.5035 | 4.4797 | 5.4558 | 6.4320 | 7.4082 | 8.3844 | 1.3607 |
| 50 | 2.5790 | 1.5513 | 2.5275 | 3.5036 | 4.4798 | 5.4559 | 6.4321 | 7.4083 | 8.3845 | 1.3608 |
| 51 | 2.5791 | 1.5514 | 2.5276 | 3.5037 | 4.4799 | 5.4560 | 6.4322 | 7.4084 | 8.3846 | 1.3609 |
| 52 | 2.5792 | 1.5515 | 2.5277 | 3.5038 | 4.4800 | 5.4561 | 6.4323 | 7.4085 | 8.3847 | 1.3610 |
| 53 | 2.5793 | 1.5516 | 2.5278 | 3.5039 | 4.4801 | 5.4562 | 6.4324 | 7.4086 | 8.3848 | 1.3611 |
| 54 | 2.5794 | 1.5517 | 2.5279 | 3.5040 | 4.4802 | 5.4563 | 6.4325 | 7.4087 | 8.3849 | 1.3612 |
| 55 | 2.5795 | 1.5518 | 2.5280 | 3.5041 | 4.4803 | 5.4564 | 6.4326 | 7.4088 | 8.3850 | 1.3613 |
| 56 | 2.5796 | 1.5519 | 2.5281 | 3.5042 | 4.4804 | 5.4565 | 6.4327 | 7.4089 | 8.3851 | 1.3614 |
| 57 | 2.5797 | 1.5520 | 2.5282 | 3.5043 | 4.4805 | 5.4566 | 6.4328 | 7.4090 | 8.3852 | 1.3615 |
| 58 | 2.5798 | 1.5521 | 2.5283 | 3.5044 | 4.4806 | 5.4567 | 6.4329 | 7.4091 | 8.3853 | 1.3616 |
| 59 | 2.5799 | 1.5522 | 2.5284 | 3.5045 | 4.4807 | 5.4568 | 6.4330 | 7.4092 | 8.3854 | 1.3617 |
| 60 | 2.5800 | 1.5523 | 2.5285 | 3.5046 | 4.4808 | 5.4569 | 6.4331 | 7.4093 | 8.3855 | 1.3618 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1543 | 0.3086 | 0.4629 | 0.6172 | 0.7715 | 0.9257 | 1.0800 | 1.2343 | 1.3886 | 0.2190 | 00 |
| 0.1546 | 0.3091 | 0.4637 | 0.6183 | 0.7720 | 0.9274 | 1.0820 | 1.2365 | 1.3911 | 0.2194 | 01 |
| 0.1548 | 0.3097 | 0.4645 | 0.6194 | 0.7724 | 0.9290 | 1.0839 | 1.2387 | 1.3936 | 0.2198 | 02 |
| 0.1551 | 0.3102 | 0.4654 | 0.6205 | 0.7756 | 0.9307 | 1.0858 | 1.2410 | 1.3961 | 0.2202 | 03 |
| 0.1554 | 0.3108 | 0.4662 | 0.6216 | 0.7770 | 0.9324 | 1.0878 | 1.2432 | 1.3986 | 0.2206 | 04 |
| 0.1557 | 0.3113 | 0.4670 | 0.6227 | 0.7784 | 0.9340 | 1.0897 | 1.2454 | 1.4010 | 0.2210 | 05 |
| 0.1559 | 0.3119 | 0.4678 | 0.6238 | 0.7797 | 0.9357 | 1.0916 | 1.2476 | 1.4035 | 0.2214 | 06 |
| 0.1562 | 0.3124 | 0.4687 | 0.6249 | 0.7811 | 0.9373 | 1.0936 | 1.2498 | 1.4060 | 0.2218 | 07 |
| 0.1565 | 0.3130 | 0.4695 | 0.6260 | 0.7825 | 0.9390 | 1.0955 | 1.2520 | 1.4085 | 0.2222 | 08 |
| 0.1568 | 0.3136 | 0.4703 | 0.6271 | 0.7839 | 0.9407 | 1.0975 | 1.2542 | 1.4110 | 0.2226 | 09 |
| 0.1571 | 0.3141 | 0.4712 | 0.6282 | 0.7853 | 0.9423 | 1.0994 | 1.2564 | 1.4135 | 0.2230 | 10 |
| 0.1573 | 0.3147 | 0.4720 | 0.6293 | 0.7866 | 0.9440 | 1.1013 | 1.2586 | 1.4160 | 0.2234 | 11 |
| 0.1576 | 0.3152 | 0.4728 | 0.6304 | 0.7880 | 0.9456 | 1.1032 | 1.2608 | 1.4184 | 0.2238 | 12 |
| 0.1579 | 0.3158 | 0.4736 | 0.6315 | 0.7894 | 0.9473 | 1.1052 | 1.2630 | 1.4209 | 0.2242 | 13 |
| 0.1582 | 0.3163 | 0.4745 | 0.6326 | 0.7908 | 0.9489 | 1.1071 | 1.2652 | 1.4234 | 0.2246 | 14 |
| 0.1584 | 0.3169 | 0.4753 | 0.6337 | 0.7922 | 0.9506 | 1.1090 | 1.2674 | 1.4259 | 0.2250 | 15 |
| 0.1587 | 0.3174 | 0.4761 | 0.6348 | 0.7935 | 0.9523 | 1.1110 | 1.2697 | 1.4284 | 0.2254 | 16 |
| 0.1590 | 0.3180 | 0.4769 | 0.6359 | 0.7949 | 0.9539 | 1.1129 | 1.2719 | 1.4308 | 0.2258 | 17 |
| 0.1593 | 0.3185 | 0.4778 | 0.6370 | 0.7963 | 0.9556 | 1.1148 | 1.2741 | 1.4333 | 0.2262 | 18 |
| 0.1595 | 0.3191 | 0.4786 | 0.6381 | 0.7977 | 0.9572 | 1.1167 | 1.2763 | 1.4358 | 0.2266 | 19 |
| 0.1598 | 0.3196 | 0.4794 | 0.6392 | 0.7991 | 0.9589 | 1.1187 | 1.2785 | 1.4383 | 0.2270 | 20 |
| 0.1601 | 0.3202 | 0.4802 | 0.6403 | 0.8004 | 0.9605 | 1.1206 | 1.2807 | 1.4407 | 0.2274 | 21 |
| 0.1604 | 0.3207 | 0.4811 | 0.6414 | 0.8018 | 0.9622 | 1.1225 | 1.2829 | 1.4432 | 0.2278 | 22 |
| 0.1606 | 0.3213 | 0.4819 | 0.6425 | 0.8032 | 0.9638 | 1.1244 | 1.2851 | 1.4457 | 0.2282 | 23 |
| 0.1609 | 0.3218 | 0.4827 | 0.6436 | 0.8046 | 0.9655 | 1.1264 | 1.2873 | 1.4482 | 0.2287 | 24 |
| 0.1612 | 0.3224 | 0.4835 | 0.6447 | 0.8059 | 0.9671 | 1.1283 | 1.2895 | 1.4506 | 0.2291 | 25 |
| 0.1615 | 0.3229 | 0.4844 | 0.6458 | 0.8073 | 0.9688 | 1.1302 | 1.2917 | 1.4531 | 0.2295 | 26 |
| 0.1617 | 0.3235 | 0.4852 | 0.6469 | 0.8087 | 0.9704 | 1.1321 | 1.2939 | 1.4556 | 0.2299 | 27 |
| 0.1620 | 0.3240 | 0.4860 | 0.6480 | 0.8100 | 0.9721 | 1.1341 | 1.2961 | 1.4581 | 0.2303 | 28 |
| 0.1623 | 0.3246 | 0.4868 | 0.6491 | 0.8114 | 0.9737 | 1.1360 | 1.2983 | 1.4605 | 0.2307 | 29 |
| 0.1626 | 0.3251 | 0.4877 | 0.6502 | 0.8128 | 0.9754 | 1.1379 | 1.3005 | 1.4630 | 0.2311 | 30 |
| 0.1628 | 0.3257 | 0.4885 | 0.6513 | 0.8142 | 0.9770 | 1.1398 | 1.3027 | 1.4655 | 0.2315 | 31 |
| 0.1631 | 0.3262 | 0.4893 | 0.6524 | 0.8155 | 0.9787 | 1.1418 | 1.3049 | 1.4680 | 0.2319 | 32 |
| 0.1634 | 0.3268 | 0.4901 | 0.6535 | 0.8169 | 0.9803 | 1.1437 | 1.3071 | 1.4704 | 0.2323 | 33 |
| 0.1637 | 0.3273 | 0.4910 | 0.6546 | 0.8183 | 0.9819 | 1.1456 | 1.3092 | 1.4729 | 0.2327 | 34 |
| 0.1639 | 0.3279 | 0.4918 | 0.6557 | 0.8196 | 0.9836 | 1.1475 | 1.3114 | 1.4754 | 0.2331 | 35 |
| 0.1642 | 0.3284 | 0.4926 | 0.6568 | 0.8210 | 0.9852 | 1.1494 | 1.3136 | 1.4778 | 0.2335 | 36 |
| 0.1645 | 0.3290 | 0.4934 | 0.6579 | 0.8224 | 0.9869 | 1.1514 | 1.3158 | 1.4803 | 0.2339 | 37 |
| 0.1648 | 0.3295 | 0.4943 | 0.6590 | 0.8238 | 0.9885 | 1.1533 | 1.3180 | 1.4828 | 0.2343 | 38 |
| 0.1650 | 0.3301 | 0.4951 | 0.6601 | 0.8251 | 0.9902 | 1.1552 | 1.3202 | 1.4853 | 0.2347 | 39 |
| 0.1653 | 0.3306 | 0.4959 | 0.6612 | 0.8265 | 0.9918 | 1.1571 | 1.3224 | 1.4877 | 0.2351 | 40 |
| 0.1656 | 0.3311 | 0.4967 | 0.6623 | 0.8279 | 0.9934 | 1.1590 | 1.3246 | 1.4901 | 0.2355 | 41 |
| 0.1658 | 0.3317 | 0.4975 | 0.6634 | 0.8292 | 0.9951 | 1.1609 | 1.3268 | 1.4926 | 0.2359 | 42 |
| 0.1661 | 0.3322 | 0.4984 | 0.6645 | 0.8306 | 0.9967 | 1.1629 | 1.3290 | 1.4951 | 0.2363 | 43 |
| 0.1664 | 0.3328 | 0.4992 | 0.6656 | 0.8320 | 0.9984 | 1.1648 | 1.3312 | 1.4976 | 0.2367 | 44 |
| 0.1667 | 0.3333 | 0.5000 | 0.6667 | 0.8334 | 1.0000 | 1.1667 | 1.3334 | 1.5000 | 0.2371 | 45 |
| 0.1669 | 0.3339 | 0.5008 | 0.6678 | 0.8347 | 1.0016 | 1.1686 | 1.3355 | 1.5025 | 0.2375 | 46 |
| 0.1672 | 0.3344 | 0.5017 | 0.6689 | 0.8361 | 1.0033 | 1.1705 | 1.3378 | 1.5050 | 0.2379 | 47 |
| 0.1675 | 0.3350 | 0.5025 | 0.6700 | 0.8375 | 1.0049 | 1.1724 | 1.3399 | 1.5074 | 0.2383 | 48 |
| 0.1678 | 0.3355 | 0.5033 | 0.6711 | 0.8388 | 1.0066 | 1.1743 | 1.3421 | 1.5098 | 0.2387 | 49 |
| 0.1680 | 0.3361 | 0.5041 | 0.6722 | 0.8402 | 1.0082 | 1.1763 | 1.3443 | 1.5123 | 0.2391 | 50 |
| 0.1683 | 0.3366 | 0.5049 | 0.6732 | 0.8416 | 1.0099 | 1.1782 | 1.3465 | 1.5148 | 0.2395 | 51 |
| 0.1686 | 0.3372 | 0.5057 | 0.6743 | 0.8429 | 1.0115 | 1.1801 | 1.3487 | 1.5172 | 0.2399 | 52 |
| 0.1689 | 0.3377 | 0.5066 | 0.6754 | 0.8443 | 1.0132 | 1.1820 | 1.3509 | 1.5197 | 0.2403 | 53 |
| 0.1691 | 0.3383 | 0.5074 | 0.6765 | 0.8457 | 1.0148 | 1.1839 | 1.3531 | 1.5222 | 0.2407 | 54 |
| 0.1694 | 0.3388 | 0.5082 | 0.6776 | 0.8470 | 1.0165 | 1.1859 | 1.3553 | 1.5247 | 0.2411 | 55 |
| 0.1697 | 0.3394 | 0.5090 | 0.6787 | 0.8484 | 1.0181 | 1.1878 | 1.3574 | 1.5271 | 0.2415 | 56 |
| 0.1700 | 0.3399 | 0.5099 | 0.6798 | 0.8498 | 1.0197 | 1.1897 | 1.3596 | 1.5296 | 0.2419 | 57 |
| 0.1702 | 0.3404 | 0.5107 | 0.6809 | 0.8511 | 1.0213 | 1.1916 | 1.3618 | 1.5320 | 0.2423 | 58 |
| 0.1705 | 0.3410 | 0.5115 | 0.6820 | 0.8525 | 1.0230 | 1.1935 | 1.3640 | 1.5345 | 0.2427 | 59 |
| 0.1708 | 0.3415 | 0.5123 | 0.6831 | 0.8539 | 1.0246 | 1.1954 | 1.3662 | 1.5369 | 0.2431 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9685 | 1.9370 | 2.9055 | 3.8740 | 4.8424 | 5.8109 | 6.7794 | 7.7479 | 8.7164 | 1.3788 |
| 01 | 0.9684 | 1.9368 | 2.9052 | 3.8736 | 4.8419 | 5.8103 | 6.7787 | 7.7471 | 8.7155 | 1.3787 |
| 02 | 0.9683 | 1.9366 | 2.9049 | 3.8732 | 4.8414 | 5.8097 | 6.7780 | 7.7463 | 8.7146 | 1.3786 |
| 03 | 0.9682 | 1.9364 | 2.9046 | 3.8728 | 4.8409 | 5.8091 | 6.7773 | 7.7455 | 8.7137 | 1.3786 |
| 04 | 0.9681 | 1.9362 | 2.9043 | 3.8724 | 4.8404 | 5.8085 | 6.7766 | 7.7447 | 8.7128 | 1.3785 |
| 05 | 0.9680 | 1.9360 | 2.9040 | 3.8720 | 4.8399 | 5.8079 | 6.7759 | 7.7439 | 8.7119 | 1.3784 |
| 06 | 0.9679 | 1.9358 | 2.9037 | 3.8716 | 4.8394 | 5.8073 | 6.7752 | 7.7431 | 8.7110 | 1.3783 |
| 07 | 0.9678 | 1.9356 | 2.9034 | 3.8712 | 4.8389 | 5.8067 | 6.7745 | 7.7423 | 8.7101 | 1.3783 |
| 08 | 0.9677 | 1.9354 | 2.9031 | 3.8707 | 4.8384 | 5.8061 | 6.7738 | 7.7415 | 8.7092 | 1.3782 |
| 09 | 0.9676 | 1.9352 | 2.9028 | 3.8703 | 4.8379 | 5.8055 | 6.7731 | 7.7407 | 8.7083 | 1.3781 |
| 10 | 0.9675 | 1.9350 | 2.9025 | 3.8699 | 4.8374 | 5.8049 | 6.7724 | 7.7399 | 8.7074 | 1.3780 |
| 11 | 0.9674 | 1.9348 | 2.9022 | 3.8695 | 4.8369 | 5.8043 | 6.7717 | 7.7391 | 8.7065 | 1.3780 |
| 12 | 0.9673 | 1.9346 | 2.9019 | 3.8691 | 4.8364 | 5.8037 | 6.7710 | 7.7383 | 8.7056 | 1.3779 |
| 13 | 0.9672 | 1.9344 | 2.9015 | 3.8687 | 4.8359 | 5.8031 | 6.7703 | 7.7375 | 8.7046 | 1.3778 |
| 14 | 0.9671 | 1.9342 | 2.9012 | 3.8683 | 4.8354 | 5.8025 | 6.7696 | 7.7366 | 8.7037 | 1.3777 |
| 15 | 0.9670 | 1.9340 | 2.9009 | 3.8679 | 4.8349 | 5.8019 | 6.7689 | 7.7358 | 8.7028 | 1.3776 |
| 16 | 0.9669 | 1.9338 | 2.9006 | 3.8675 | 4.8344 | 5.8011 | 6.7681 | 7.7350 | 8.7019 | 1.3776 |
| 17 | 0.9668 | 1.9336 | 2.9003 | 3.8671 | 4.8339 | 5.8007 | 6.7674 | 7.7342 | 8.7010 | 1.3775 |
| 18 | 0.9667 | 1.9333 | 2.9000 | 3.8667 | 4.8334 | 5.8000 | 6.7667 | 7.7334 | 8.7001 | 1.3774 |
| 19 | 0.9666 | 1.9331 | 2.8997 | 3.8663 | 4.8329 | 5.7994 | 6.7660 | 7.7326 | 8.6991 | 1.3773 |
| 20 | 0.9665 | 1.9329 | 2.8994 | 3.8659 | 4.8324 | 5.7988 | 6.7653 | 7.7318 | 8.6982 | 1.3773 |
| 21 | 0.9664 | 1.9327 | 2.8991 | 3.8655 | 4.8318 | 5.7982 | 6.7646 | 7.7309 | 8.6973 | 1.3772 |
| 22 | 0.9663 | 1.9325 | 2.8988 | 3.8651 | 4.8313 | 5.7976 | 6.7638 | 7.7301 | 8.6964 | 1.3771 |
| 23 | 0.9662 | 1.9323 | 2.8985 | 3.8646 | 4.8308 | 5.7970 | 6.7631 | 7.7293 | 8.6954 | 1.3770 |
| 24 | 0.9661 | 1.9321 | 2.8982 | 3.8642 | 4.8303 | 5.7963 | 6.7624 | 7.7285 | 8.6945 | 1.3769 |
| 25 | 0.9660 | 1.9319 | 2.8979 | 3.8638 | 4.8298 | 5.7957 | 6.7617 | 7.7276 | 8.6936 | 1.3769 |
| 26 | 0.9659 | 1.9317 | 2.8976 | 3.8634 | 4.8293 | 5.7951 | 6.7610 | 7.7268 | 8.6927 | 1.3768 |
| 27 | 0.9657 | 1.9315 | 2.8972 | 3.8630 | 4.8287 | 5.7945 | 6.7602 | 7.7260 | 8.6917 | 1.3767 |
| 28 | 0.9656 | 1.9313 | 2.8969 | 3.8626 | 4.8282 | 5.7939 | 6.7595 | 7.7252 | 8.6908 | 1.3766 |
| 29 | 0.9655 | 1.9311 | 2.8966 | 3.8622 | 4.8277 | 5.7932 | 6.7588 | 7.7243 | 8.6899 | 1.3765 |
| 30 | 0.9654 | 1.9309 | 2.8963 | 3.8617 | 4.8272 | 5.7926 | 6.7581 | 7.7235 | 8.6889 | 1.3765 |
| 31 | 0.9653 | 1.9307 | 2.8960 | 3.8613 | 4.8267 | 5.7920 | 6.7573 | 7.7227 | 8.6880 | 1.3764 |
| 32 | 0.9652 | 1.9305 | 2.8957 | 3.8609 | 4.8261 | 5.7914 | 6.7566 | 7.7218 | 8.6870 | 1.3763 |
| 33 | 0.9651 | 1.9302 | 2.8954 | 3.8605 | 4.8256 | 5.7907 | 6.7559 | 7.7210 | 8.6861 | 1.3762 |
| 34 | 0.9650 | 1.9300 | 2.8951 | 3.8601 | 4.8251 | 5.7901 | 6.7551 | 7.7201 | 8.6852 | 1.3761 |
| 35 | 0.9649 | 1.9298 | 2.8947 | 3.8597 | 4.8246 | 5.7895 | 6.7544 | 7.7193 | 8.6842 | 1.3761 |
| 36 | 0.9648 | 1.9296 | 2.8944 | 3.8592 | 4.8240 | 5.7888 | 6.7537 | 7.7185 | 8.6833 | 1.3760 |
| 37 | 0.9647 | 1.9294 | 2.8941 | 3.8588 | 4.8235 | 5.7882 | 6.7529 | 7.7176 | 8.6823 | 1.3759 |
| 38 | 0.9646 | 1.9292 | 2.8938 | 3.8584 | 4.8230 | 5.7876 | 6.7522 | 7.7168 | 8.6814 | 1.3759 |
| 39 | 0.9645 | 1.9290 | 2.8935 | 3.8580 | 4.8225 | 5.7870 | 6.7515 | 7.7159 | 8.6804 | 1.3758 |
| 40 | 0.9644 | 1.9288 | 2.8932 | 3.8576 | 4.8219 | 5.7863 | 6.7507 | 7.7151 | 8.6795 | 1.3757 |
| 41 | 0.9643 | 1.9286 | 2.8928 | 3.8571 | 4.8214 | 5.7857 | 6.7500 | 7.7143 | 8.6785 | 1.3756 |
| 42 | 0.9642 | 1.9284 | 2.8925 | 3.8567 | 4.8209 | 5.7851 | 6.7492 | 7.7134 | 8.6776 | 1.3755 |
| 43 | 0.9641 | 1.9281 | 2.8922 | 3.8563 | 4.8203 | 5.7844 | 6.7485 | 7.7126 | 8.6766 | 1.3755 |
| 44 | 0.9640 | 1.9279 | 2.8919 | 3.8558 | 4.8198 | 5.7838 | 6.7477 | 7.7117 | 8.6757 | 1.3754 |
| 45 | 0.9639 | 1.9277 | 2.8916 | 3.8554 | 4.8193 | 5.7831 | 6.7470 | 7.7108 | 8.6747 | 1.3753 |
| 46 | 0.9638 | 1.9275 | 2.8912 | 3.8550 | 4.8187 | 5.7825 | 6.7462 | 7.7100 | 8.6737 | 1.3752 |
| 47 | 0.9636 | 1.9273 | 2.8909 | 3.8546 | 4.8182 | 5.7819 | 6.7455 | 7.7091 | 8.6728 | 1.3752 |
| 48 | 0.9635 | 1.9271 | 2.8906 | 3.8541 | 4.8177 | 5.7812 | 6.7448 | 7.7083 | 8.6718 | 1.3751 |
| 49 | 0.9634 | 1.9269 | 2.8903 | 3.8537 | 4.8172 | 5.7806 | 6.7440 | 7.7074 | 8.6709 | 1.3750 |
| 50 | 0.9633 | 1.9266 | 2.8900 | 3.8533 | 4.8166 | 5.7799 | 6.7433 | 7.7066 | 8.6699 | 1.3749 |
| 51 | 0.9632 | 1.9264 | 2.8896 | 3.8529 | 4.8161 | 5.7793 | 6.7425 | 7.7057 | 8.6689 | 1.3748 |
| 52 | 0.9631 | 1.9262 | 2.8893 | 3.8524 | 4.8155 | 5.7786 | 6.7417 | 7.7049 | 8.6680 | 1.3748 |
| 53 | 0.9630 | 1.9260 | 2.8890 | 3.8520 | 4.8150 | 5.7780 | 6.7410 | 7.7040 | 8.6670 | 1.3747 |
| 54 | 0.9629 | 1.9258 | 2.8887 | 3.8516 | 4.8145 | 5.7773 | 6.7402 | 7.7031 | 8.6660 | 1.3746 |
| 55 | 0.9628 | 1.9256 | 2.8883 | 3.8511 | 4.8139 | 5.7767 | 6.7395 | 7.7023 | 8.6650 | 1.3745 |
| 56 | 0.9627 | 1.9254 | 2.8880 | 3.8507 | 4.8134 | 5.7761 | 6.7387 | 7.7014 | 8.6641 | 1.3744 |
| 57 | 0.9626 | 1.9251 | 2.8877 | 3.8503 | 4.8128 | 5.7754 | 6.7380 | 7.7005 | 8.6631 | 1.3744 |
| 58 | 0.9625 | 1.9249 | 2.8874 | 3.8498 | 4.8123 | 5.7748 | 6.7372 | 7.6997 | 8.6621 | 1.3743 |
| 59 | 0.9624 | 1.9247 | 2.8871 | 3.8494 | 4.8118 | 5.7741 | 6.7365 | 7.6988 | 8.6612 | 1.3742 |
| 60 | 0.9622 | 1.9245 | 2.8867 | 3.8490 | 4.8112 | 5.7735 | 6.7357 | 7.6979 | 8.6602 | 1.3742 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1708 | 0.3415 | 0.5123 | 0.6831 | 0.8539 | 1.0246 | 1.1954 | 1.3662 | 1.5369 | 0.2431 | 00 |
| 0.1710 | 0.3421 | 0.5131 | 0.6842 | 0.8552 | 1.0262 | 1.1973 | 1.3683 | 1.5394 | 0.2435 | 01 |
| 0.1713 | 0.3426 | 0.5140 | 0.6853 | 0.8566 | 1.0279 | 1.1992 | 1.3705 | 1.5419 | 0.2439 | 02 |
| 0.1716 | 0.3432 | 0.5148 | 0.6864 | 0.8580 | 1.0295 | 1.2011 | 1.3727 | 1.5443 | 0.2443 | 03 |
| 0.1719 | 0.3437 | 0.5156 | 0.6875 | 0.8593 | 1.0312 | 1.2030 | 1.3749 | 1.5468 | 0.2447 | 04 |
| 0.1721 | 0.3443 | 0.5164 | 0.6886 | 0.8607 | 1.0328 | 1.2050 | 1.3771 | 1.5493 | 0.2451 | 05 |
| 0.1724 | 0.3448 | 0.5173 | 0.6896 | 0.8620 | 1.0345 | 1.2069 | 1.3793 | 1.5517 | 0.2455 | 06 |
| 0.1727 | 0.3454 | 0.5180 | 0.6907 | 0.8634 | 1.0361 | 1.2088 | 1.3814 | 1.5541 | 0.2459 | 07 |
| 0.1730 | 0.3459 | 0.5189 | 0.6918 | 0.8648 | 1.0377 | 1.2107 | 1.3836 | 1.5566 | 0.2463 | 08 |
| 0.1732 | 0.3464 | 0.5197 | 0.6929 | 0.8661 | 1.0393 | 1.2126 | 1.3858 | 1.5590 | 0.2467 | 09 |
| 0.1735 | 0.3470 | 0.5205 | 0.6940 | 0.8675 | 1.0410 | 1.2145 | 1.3880 | 1.5615 | 0.2471 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1738 | 0.3475 | 0.5213 | 0.6951 | 0.8688 | 1.0426 | 1.2164 | 1.3902 | 1.5639 | 0.2475 | 11 |
| 0.1740 | 0.3481 | 0.5221 | 0.6962 | 0.8702 | 1.0442 | 1.2183 | 1.3923 | 1.5664 | 0.2479 | 12 |
| 0.1743 | 0.3486 | 0.5229 | 0.6973 | 0.8716 | 1.0459 | 1.2202 | 1.3945 | 1.5688 | 0.2483 | 13 |
| 0.1746 | 0.3492 | 0.5238 | 0.6984 | 0.8729 | 1.0475 | 1.2221 | 1.3967 | 1.5713 | 0.2487 | 14 |
| 0.1749 | 0.3497 | 0.5246 | 0.6994 | 0.8743 | 1.0492 | 1.2240 | 1.3989 | 1.5737 | 0.2491 | 15 |
| 0.1751 | 0.3503 | 0.5254 | 0.7005 | 0.8757 | 1.0508 | 1.2259 | 1.4010 | 1.5762 | 0.2495 | 16 |
| 0.1754 | 0.3508 | 0.5262 | 0.7016 | 0.8770 | 1.0524 | 1.2278 | 1.4032 | 1.5786 | 0.2499 | 17 |
| 0.1757 | 0.3513 | 0.5270 | 0.7027 | 0.8784 | 1.0540 | 1.2297 | 1.4054 | 1.5810 | 0.2503 | 18 |
| 0.1759 | 0.3519 | 0.5278 | 0.7038 | 0.8797 | 1.0557 | 1.2316 | 1.4076 | 1.5835 | 0.2507 | 19 |
| 0.1762 | 0.3524 | 0.5287 | 0.7049 | 0.8811 | 1.0573 | 1.2335 | 1.4098 | 1.5860 | 0.2511 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1765 | 0.3530 | 0.5295 | 0.7060 | 0.8824 | 1.0589 | 1.2354 | 1.4119 | 1.5884 | 0.2515 | 21 |
| 0.1768 | 0.3535 | 0.5303 | 0.7070 | 0.8838 | 1.0606 | 1.2373 | 1.4141 | 1.5908 | 0.2519 | 22 |
| 0.1770 | 0.3541 | 0.5311 | 0.7081 | 0.8852 | 1.0622 | 1.2392 | 1.4162 | 1.5933 | 0.2523 | 23 |
| 0.1773 | 0.3546 | 0.5319 | 0.7092 | 0.8865 | 1.0638 | 1.2411 | 1.4184 | 1.5957 | 0.2527 | 24 |
| 0.1776 | 0.3552 | 0.5327 | 0.7103 | 0.8879 | 1.0655 | 1.2430 | 1.4206 | 1.5982 | 0.2531 | 25 |
| 0.1778 | 0.3557 | 0.5335 | 0.7114 | 0.8892 | 1.0671 | 1.2449 | 1.4228 | 1.6006 | 0.2535 | 26 |
| 0.1781 | 0.3562 | 0.5344 | 0.7125 | 0.8906 | 1.0687 | 1.2468 | 1.4250 | 1.6031 | 0.2539 | 27 |
| 0.1784 | 0.3568 | 0.5352 | 0.7136 | 0.8920 | 1.0703 | 1.2487 | 1.4271 | 1.6055 | 0.2543 | 28 |
| 0.1787 | 0.3573 | 0.5360 | 0.7146 | 0.8933 | 1.0720 | 1.2506 | 1.4293 | 1.6079 | 0.2547 | 29 |
| 0.1789 | 0.3579 | 0.5368 | 0.7157 | 0.8947 | 1.0736 | 1.2525 | 1.4314 | 1.6104 | 0.2551 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1792 | 0.3584 | 0.5376 | 0.7168 | 0.8960 | 1.0752 | 1.2544 | 1.4336 | 1.6128 | 0.2555 | 31 |
| 0.1795 | 0.3590 | 0.5384 | 0.7179 | 0.8974 | 1.0769 | 1.2563 | 1.4358 | 1.6153 | 0.2559 | 32 |
| 0.1797 | 0.3595 | 0.5392 | 0.7190 | 0.8987 | 1.0785 | 1.2582 | 1.4380 | 1.6177 | 0.2563 | 33 |
| 0.1800 | 0.3600 | 0.5401 | 0.7201 | 0.9001 | 1.0801 | 1.2601 | 1.4402 | 1.6202 | 0.2567 | 34 |
| 0.1803 | 0.3606 | 0.5409 | 0.7212 | 0.9014 | 1.0817 | 1.2620 | 1.4423 | 1.6226 | 0.2571 | 35 |
| 0.1806 | 0.3611 | 0.5417 | 0.7222 | 0.9028 | 1.0834 | 1.2639 | 1.4445 | 1.6250 | 0.2575 | 36 |
| 0.1808 | 0.3617 | 0.5425 | 0.7233 | 0.9041 | 1.0850 | 1.2658 | 1.4466 | 1.6275 | 0.2579 | 37 |
| 0.1811 | 0.3622 | 0.5433 | 0.7244 | 0.9055 | 1.0866 | 1.2677 | 1.4488 | 1.6299 | 0.2583 | 38 |
| 0.1814 | 0.3627 | 0.5441 | 0.7255 | 0.9069 | 1.0882 | 1.2696 | 1.4510 | 1.6323 | 0.2587 | 39 |
| 0.1816 | 0.3633 | 0.5449 | 0.7266 | 0.9082 | 1.0898 | 1.2715 | 1.4531 | 1.6348 | 0.2591 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1819 | 0.3638 | 0.5457 | 0.7276 | 0.9096 | 1.0915 | 1.2734 | 1.4553 | 1.6372 | 0.2595 | 41 |
| 0.1822 | 0.3644 | 0.5465 | 0.7287 | 0.9109 | 1.0931 | 1.2753 | 1.4574 | 1.6396 | 0.2599 | 42 |
| 0.1825 | 0.3649 | 0.5474 | 0.7298 | 0.9123 | 1.0947 | 1.2772 | 1.4596 | 1.6421 | 0.2603 | 43 |
| 0.1827 | 0.3654 | 0.5482 | 0.7309 | 0.9136 | 1.0963 | 1.2790 | 1.4618 | 1.6445 | 0.2607 | 44 |
| 0.1830 | 0.3660 | 0.5490 | 0.7320 | 0.9150 | 1.0979 | 1.2809 | 1.4639 | 1.6469 | 0.2611 | 45 |
| 0.1833 | 0.3665 | 0.5498 | 0.7330 | 0.9163 | 1.0996 | 1.2828 | 1.4661 | 1.6493 | 0.2615 | 46 |
| 0.1835 | 0.3671 | 0.5506 | 0.7341 | 0.9177 | 1.1012 | 1.2847 | 1.4682 | 1.6518 | 0.2619 | 47 |
| 0.1838 | 0.3676 | 0.5514 | 0.7352 | 0.9190 | 1.1028 | 1.2866 | 1.4704 | 1.6542 | 0.2623 | 48 |
| 0.1841 | 0.3681 | 0.5522 | 0.7363 | 0.9204 | 1.1044 | 1.2885 | 1.4726 | 1.6566 | 0.2627 | 49 |
| 0.1843 | 0.3687 | 0.5530 | 0.7374 | 0.9217 | 1.1061 | 1.2904 | 1.4748 | 1.6591 | 0.2631 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1846 | 0.3692 | 0.5538 | 0.7384 | 0.9231 | 1.1077 | 1.2923 | 1.4769 | 1.6615 | 0.2635 | 51 |
| 0.1849 | 0.3698 | 0.5546 | 0.7395 | 0.9244 | 1.1093 | 1.2942 | 1.4790 | 1.6639 | 0.2639 | 52 |
| 0.1852 | 0.3703 | 0.5555 | 0.7406 | 0.9258 | 1.1109 | 1.2961 | 1.4812 | 1.6664 | 0.2643 | 53 |
| 0.1854 | 0.3708 | 0.5563 | 0.7417 | 0.9271 | 1.1125 | 1.2979 | 1.4834 | 1.6688 | 0.2647 | 54 |
| 0.1857 | 0.3714 | 0.5571 | 0.7428 | 0.9285 | 1.1141 | 1.2998 | 1.4855 | 1.6712 | 0.2651 | 55 |
| 0.1860 | 0.3719 | 0.5579 | 0.7438 | 0.9298 | 1.1158 | 1.3017 | 1.4877 | 1.6736 | 0.2655 | 56 |
| 0.1862 | 0.3725 | 0.5587 | 0.7449 | 0.9312 | 1.1174 | 1.3036 | 1.4898 | 1.6761 | 0.2659 | 57 |
| 0.1865 | 0.3730 | 0.5595 | 0.7460 | 0.9325 | 1.1190 | 1.3055 | 1.4920 | 1.6785 | 0.2663 | 58 |
| 0.1868 | 0.3735 | 0.5603 | 0.7471 | 0.9339 | 1.1206 | 1.3074 | 1.4942 | 1.6809 | 0.2667 | 59 |
| 0.1870 | 0.3741 | 0.5611 | 0.7482 | 0.9352 | 1.1222 | 1.3093 | 1.4963 | 1.6834 | 0.2671 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9877 | 1.9754 | 2.9631 | 3.9508 | 4.9384 | 5.9261 | 6.9138 | 7.9015 | 8.8892 | 1.3923 |
| 01 | 0.9876 | 1.9753 | 2.9629 | 3.9505 | 4.9381 | 5.9258 | 6.9134 | 7.9010 | 8.8887 | 1.3923 |
| 02 | 0.9876 | 1.9751 | 2.9627 | 3.9503 | 4.9378 | 5.9254 | 6.9130 | 7.9005 | 8.8881 | 1.3922 |
| 03 | 0.9875 | 1.9750 | 2.9625 | 3.9500 | 4.9375 | 5.9250 | 6.9125 | 7.9000 | 8.8875 | 1.3922 |
| 04 | 0.9874 | 1.9749 | 2.9623 | 3.9498 | 4.9372 | 5.9247 | 6.9121 | 7.8996 | 8.8870 | 1.3921 |
| 05 | 0.9874 | 1.9748 | 2.9621 | 3.9495 | 4.9369 | 5.9243 | 6.9117 | 7.8991 | 8.8864 | 1.3921 |
| 06 | 0.9873 | 1.9746 | 2.9620 | 3.9493 | 4.9366 | 5.9239 | 6.9113 | 7.8986 | 8.8859 | 1.3921 |
| 07 | 0.9873 | 1.9745 | 2.9618 | 3.9490 | 4.9363 | 5.9236 | 6.9108 | 7.8981 | 8.8853 | 1.3920 |
| 08 | 0.9872 | 1.9744 | 2.9616 | 3.9488 | 4.9360 | 5.9232 | 6.9104 | 7.8976 | 8.8848 | 1.3920 |
| 09 | 0.9871 | 1.9743 | 2.9614 | 3.9486 | 4.9357 | 5.9228 | 6.9100 | 7.8971 | 8.8842 | 1.3919 |
| 10 | 0.9871 | 1.9742 | 2.9612 | 3.9483 | 4.9354 | 5.9225 | 6.9095 | 7.8966 | 8.8837 | 1.3919 |
| 11 | 0.9870 | 1.9740 | 2.9610 | 3.9481 | 4.9351 | 5.9221 | 6.9091 | 7.8961 | 8.8831 | 1.3919 |
| 12 | 0.9870 | 1.9739 | 2.9609 | 3.9478 | 4.9348 | 5.9217 | 6.9087 | 7.8956 | 8.8826 | 1.3918 |
| 13 | 0.9869 | 1.9738 | 2.9607 | 3.9476 | 4.9344 | 5.9213 | 6.9082 | 7.8951 | 8.8820 | 1.3918 |
| 14 | 0.9868 | 1.9737 | 2.9605 | 3.9473 | 4.9341 | 5.9210 | 6.9078 | 7.8946 | 8.8814 | 1.3917 |
| 15 | 0.9868 | 1.9735 | 2.9603 | 3.9471 | 4.9338 | 5.9206 | 6.9073 | 7.8941 | 8.8809 | 1.3917 |
| 16 | 0.9867 | 1.9734 | 2.9601 | 3.9468 | 4.9335 | 5.9202 | 6.9069 | 7.8936 | 8.8803 | 1.3917 |
| 17 | 0.9866 | 1.9733 | 2.9599 | 3.9465 | 4.9332 | 5.9198 | 6.9065 | 7.8931 | 8.8797 | 1.3916 |
| 18 | 0.9866 | 1.9732 | 2.9597 | 3.9463 | 4.9329 | 5.9195 | 6.9060 | 7.8926 | 8.8792 | 1.3916 |
| 19 | 0.9865 | 1.9730 | 2.9595 | 3.9460 | 4.9326 | 5.9191 | 6.9056 | 7.8921 | 8.8786 | 1.3915 |
| 20 | 0.9864 | 1.9729 | 2.9593 | 3.9458 | 4.9322 | 5.9187 | 6.9051 | 7.8916 | 8.8780 | 1.3915 |
| 21 | 0.9864 | 1.9728 | 2.9592 | 3.9455 | 4.9319 | 5.9183 | 6.9047 | 7.8911 | 8.8775 | 1.3915 |
| 22 | 0.9863 | 1.9726 | 2.9590 | 3.9453 | 4.9316 | 5.9179 | 6.9042 | 7.8906 | 8.8769 | 1.3914 |
| 23 | 0.9863 | 1.9725 | 2.9588 | 3.9450 | 4.9313 | 5.9175 | 6.9038 | 7.8900 | 8.8763 | 1.3914 |
| 24 | 0.9862 | 1.9724 | 2.9586 | 3.9448 | 4.9310 | 5.9171 | 6.9033 | 7.8895 | 8.8757 | 1.3913 |
| 25 | 0.9861 | 1.9723 | 2.9584 | 3.9445 | 4.9306 | 5.9168 | 6.9029 | 7.8890 | 8.8751 | 1.3913 |
| 26 | 0.9861 | 1.9721 | 2.9582 | 3.9442 | 4.9303 | 5.9164 | 6.9024 | 7.8885 | 8.8745 | 1.3913 |
| 27 | 0.9860 | 1.9720 | 2.9580 | 3.9440 | 4.9300 | 5.9160 | 6.9020 | 7.8880 | 8.8740 | 1.3912 |
| 28 | 0.9859 | 1.9719 | 2.9578 | 3.9437 | 4.9297 | 5.9156 | 6.9015 | 7.8875 | 8.8734 | 1.3912 |
| 29 | 0.9859 | 1.9717 | 2.9576 | 3.9435 | 4.9293 | 5.9152 | 6.9011 | 7.8870 | 8.8728 | 1.3911 |
| 30 | 0.9858 | 1.9716 | 2.9574 | 3.9432 | 4.9290 | 5.9148 | 6.9006 | 7.8864 | 8.8722 | 1.3911 |
| 31 | 0.9857 | 1.9715 | 2.9572 | 3.9429 | 4.9287 | 5.9144 | 6.9002 | 7.8859 | 8.8716 | 1.3910 |
| 32 | 0.9857 | 1.9713 | 2.9570 | 3.9427 | 4.9284 | 5.9140 | 6.9007 | 7.8854 | 8.8710 | 1.3910 |
| 33 | 0.9856 | 1.9712 | 2.9568 | 3.9424 | 4.9280 | 5.9136 | 6.9002 | 7.8848 | 8.8704 | 1.3910 |
| 34 | 0.9855 | 1.9711 | 2.9566 | 3.9422 | 4.9277 | 5.9132 | 6.9008 | 7.8843 | 8.8698 | 1.3909 |
| 35 | 0.9855 | 1.9709 | 2.9564 | 3.9419 | 4.9274 | 5.9128 | 6.9003 | 7.8838 | 8.8692 | 1.3909 |
| 36 | 0.9854 | 1.9708 | 2.9562 | 3.9416 | 4.9270 | 5.9124 | 6.9078 | 7.8832 | 8.8687 | 1.3908 |
| 37 | 0.9853 | 1.9707 | 2.9560 | 3.9414 | 4.9267 | 5.9120 | 6.9074 | 7.8827 | 8.8681 | 1.3908 |
| 38 | 0.9853 | 1.9705 | 2.9558 | 3.9411 | 4.9264 | 5.9116 | 6.9069 | 7.8822 | 8.8675 | 1.3907 |
| 39 | 0.9852 | 1.9704 | 2.9556 | 3.9408 | 4.9260 | 5.9112 | 6.9064 | 7.8817 | 8.8669 | 1.3907 |
| 40 | 0.9851 | 1.9703 | 2.9554 | 3.9406 | 4.9257 | 5.9108 | 6.9060 | 7.8811 | 8.8663 | 1.3906 |
| 41 | 0.9851 | 1.9701 | 2.9552 | 3.9403 | 4.9254 | 5.9104 | 6.9055 | 7.8806 | 8.8657 | 1.3906 |
| 42 | 0.9850 | 1.9700 | 2.9550 | 3.9400 | 4.9250 | 5.9100 | 6.9050 | 7.8800 | 8.8650 | 1.3905 |
| 43 | 0.9849 | 1.9699 | 2.9548 | 3.9398 | 4.9247 | 5.9096 | 6.9046 | 7.8795 | 8.8644 | 1.3905 |
| 44 | 0.9849 | 1.9697 | 2.9546 | 3.9395 | 4.9244 | 5.9092 | 6.9041 | 7.8790 | 8.8638 | 1.3904 |
| 45 | 0.9848 | 1.9696 | 2.9544 | 3.9392 | 4.9240 | 5.9088 | 6.9036 | 7.8784 | 8.8632 | 1.3904 |
| 46 | 0.9847 | 1.9695 | 2.9542 | 3.9389 | 4.9237 | 5.9084 | 6.9031 | 7.8779 | 8.8626 | 1.3903 |
| 47 | 0.9847 | 1.9693 | 2.9540 | 3.9387 | 4.9233 | 5.9080 | 6.9027 | 7.8773 | 8.8620 | 1.3903 |
| 48 | 0.9846 | 1.9692 | 2.9538 | 3.9384 | 4.9230 | 5.9076 | 6.9022 | 7.8768 | 8.8614 | 1.3902 |
| 49 | 0.9845 | 1.9691 | 2.9536 | 3.9381 | 4.9227 | 5.9072 | 6.9017 | 7.8762 | 8.8608 | 1.3902 |
| 50 | 0.9845 | 1.9689 | 2.9534 | 3.9379 | 4.9223 | 5.9068 | 6.9012 | 7.8757 | 8.8602 | 1.3901 |
| 51 | 0.9844 | 1.9688 | 2.9532 | 3.9376 | 4.9220 | 5.9064 | 6.9008 | 7.8752 | 8.8595 | 1.3901 |
| 52 | 0.9843 | 1.9686 | 2.9530 | 3.9373 | 4.9216 | 5.9059 | 6.9003 | 7.8746 | 8.8589 | 1.3900 |
| 53 | 0.9843 | 1.9685 | 2.9528 | 3.9370 | 4.9213 | 5.9055 | 6.9008 | 7.8740 | 8.8583 | 1.3900 |
| 54 | 0.9842 | 1.9684 | 2.9526 | 3.9367 | 4.9209 | 5.9051 | 6.9003 | 7.8735 | 8.8577 | 1.3899 |
| 55 | 0.9841 | 1.9682 | 2.9523 | 3.9365 | 4.9206 | 5.9047 | 6.9008 | 7.8729 | 8.8570 | 1.3899 |
| 56 | 0.9840 | 1.9681 | 2.9521 | 3.9362 | 4.9202 | 5.9043 | 6.9003 | 7.8724 | 8.8564 | 1.3898 |
| 57 | 0.9840 | 1.9680 | 2.9519 | 3.9359 | 4.9199 | 5.9039 | 6.9008 | 7.8718 | 8.8558 | 1.3898 |
| 58 | 0.9839 | 1.9678 | 2.9517 | 3.9356 | 4.9195 | 5.9034 | 6.9004 | 7.8713 | 8.8552 | 1.3897 |
| 59 | 0.9838 | 1.9677 | 2.9515 | 3.9354 | 4.9192 | 5.9030 | 6.9009 | 7.8707 | 8.8545 | 1.3897 |
| 60 | 0.9838 | 1.9675 | 2.9513 | 3.9351 | 4.9188 | 5.9026 | 6.9004 | 7.8702 | 8.8539 | 1.3896 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1038 | 0.2076 | 0.3114 | 0.4153 | 0.5191 | 0.6229 | 0.7267 | 0.8305 | 0.9343 | 0.1463 | 00 |
| 0.1041 | 0.2082 | 0.3123 | 0.4164 | 0.5205 | 0.6246 | 0.7287 | 0.8327 | 0.9368 | 0.1467 | 01 |
| 0.1044 | 0.2088 | 0.3131 | 0.4175 | 0.5219 | 0.6263 | 0.7307 | 0.8350 | 0.9394 | 0.1471 | 02 |
| 0.1047 | 0.2093 | 0.3140 | 0.4186 | 0.5233 | 0.6280 | 0.7326 | 0.8373 | 0.9419 | 0.1476 | 03 |
| 0.1049 | 0.2099 | 0.3148 | 0.4198 | 0.5247 | 0.6297 | 0.7346 | 0.8396 | 0.9445 | 0.1480 | 04 |
| 0.1052 | 0.2105 | 0.3157 | 0.4209 | 0.5262 | 0.6314 | 0.7366 | 0.8418 | 0.9471 | 0.1484 | 05 |
| 0.1055 | 0.2110 | 0.3165 | 0.4220 | 0.5276 | 0.6331 | 0.7386 | 0.8441 | 0.9496 | 0.1488 | 06 |
| 0.1058 | 0.2116 | 0.3174 | 0.4232 | 0.5290 | 0.6348 | 0.7406 | 0.8464 | 0.9522 | 0.1492 | 07 |
| 0.1061 | 0.2122 | 0.3182 | 0.4243 | 0.5304 | 0.6365 | 0.7426 | 0.8486 | 0.9547 | 0.1496 | 08 |
| 0.1064 | 0.2127 | 0.3191 | 0.4255 | 0.5318 | 0.6382 | 0.7446 | 0.8509 | 0.9573 | 0.1500 | 09 |
| 0.1067 | 0.2133 | 0.3200 | 0.4266 | 0.5333 | 0.6399 | 0.7466 | 0.8532 | 0.9599 | 0.1504 | 10 |
| 0.1069 | 0.2139 | 0.3208 | 0.4277 | 0.5347 | 0.6416 | 0.7485 | 0.8554 | 0.9624 | 0.1508 | 11 |
| 0.1072 | 0.2144 | 0.3217 | 0.4289 | 0.5361 | 0.6433 | 0.7505 | 0.8577 | 0.9650 | 0.1512 | 12 |
| 0.1075 | 0.2150 | 0.3225 | 0.4300 | 0.5375 | 0.6450 | 0.7525 | 0.8600 | 0.9675 | 0.1516 | 13 |
| 0.1078 | 0.2156 | 0.3233 | 0.4311 | 0.5389 | 0.6467 | 0.7545 | 0.8622 | 0.9700 | 0.1520 | 14 |
| 0.1081 | 0.2161 | 0.3242 | 0.4323 | 0.5403 | 0.6484 | 0.7565 | 0.8645 | 0.9726 | 0.1524 | 15 |
| 0.1084 | 0.2167 | 0.3251 | 0.4334 | 0.5418 | 0.6501 | 0.7585 | 0.8668 | 0.9752 | 0.1528 | 16 |
| 0.1086 | 0.2173 | 0.3259 | 0.4346 | 0.5432 | 0.6518 | 0.7605 | 0.8691 | 0.9778 | 0.1532 | 17 |
| 0.1089 | 0.2178 | 0.3268 | 0.4357 | 0.5446 | 0.6535 | 0.7624 | 0.8714 | 0.9803 | 0.1536 | 18 |
| 0.1092 | 0.2184 | 0.3276 | 0.4368 | 0.5460 | 0.6552 | 0.7644 | 0.8736 | 0.9828 | 0.1540 | 19 |
| 0.1095 | 0.2190 | 0.3285 | 0.4380 | 0.5474 | 0.6569 | 0.7664 | 0.8759 | 0.9854 | 0.1544 | 20 |
| 0.1098 | 0.2195 | 0.3293 | 0.4391 | 0.5488 | 0.6586 | 0.7684 | 0.8782 | 0.9879 | 0.1548 | 21 |
| 0.1101 | 0.2201 | 0.3302 | 0.4402 | 0.5503 | 0.6603 | 0.7704 | 0.8804 | 0.9905 | 0.1552 | 22 |
| 0.1103 | 0.2207 | 0.3310 | 0.4414 | 0.5517 | 0.6620 | 0.7724 | 0.8827 | 0.9931 | 0.1556 | 23 |
| 0.1106 | 0.2212 | 0.3319 | 0.4425 | 0.5531 | 0.6637 | 0.7743 | 0.8850 | 0.9956 | 0.1561 | 24 |
| 0.1109 | 0.2218 | 0.3327 | 0.4436 | 0.5545 | 0.6654 | 0.7763 | 0.8872 | 0.9981 | 0.1565 | 25 |
| 0.1112 | 0.2224 | 0.3336 | 0.4448 | 0.5559 | 0.6671 | 0.7783 | 0.8895 | 1.0007 | 0.1569 | 26 |
| 0.1115 | 0.2229 | 0.3344 | 0.4459 | 0.5573 | 0.6688 | 0.7803 | 0.8918 | 1.0032 | 0.1573 | 27 |
| 0.1118 | 0.2235 | 0.3353 | 0.4470 | 0.5588 | 0.6705 | 0.7823 | 0.8940 | 1.0058 | 0.1577 | 28 |
| 0.1120 | 0.2241 | 0.3361 | 0.4481 | 0.5602 | 0.6722 | 0.7842 | 0.8963 | 1.0083 | 0.1581 | 29 |
| 0.1123 | 0.2246 | 0.3370 | 0.4493 | 0.5616 | 0.6739 | 0.7862 | 0.8986 | 1.0109 | 0.1585 | 30 |
| 0.1126 | 0.2252 | 0.3378 | 0.4504 | 0.5630 | 0.6756 | 0.7882 | 0.9008 | 1.0134 | 0.1589 | 31 |
| 0.1129 | 0.2258 | 0.3386 | 0.4515 | 0.5644 | 0.6773 | 0.7902 | 0.9031 | 1.0159 | 0.1593 | 32 |
| 0.1132 | 0.2263 | 0.3395 | 0.4527 | 0.5659 | 0.6790 | 0.7922 | 0.9054 | 1.0185 | 0.1597 | 33 |
| 0.1134 | 0.2269 | 0.3403 | 0.4538 | 0.5673 | 0.6807 | 0.7941 | 0.9076 | 1.0210 | 0.1601 | 34 |
| 0.1137 | 0.2275 | 0.3412 | 0.4549 | 0.5687 | 0.6824 | 0.7961 | 0.9098 | 1.0236 | 0.1605 | 35 |
| 0.1140 | 0.2280 | 0.3421 | 0.4561 | 0.5701 | 0.6841 | 0.8081 | 0.9121 | 1.0262 | 0.1609 | 36 |
| 0.1143 | 0.2286 | 0.3429 | 0.4572 | 0.5715 | 0.6858 | 0.8001 | 0.9144 | 1.0287 | 0.1613 | 37 |
| 0.1146 | 0.2292 | 0.3437 | 0.4583 | 0.5729 | 0.6875 | 0.8021 | 0.9166 | 1.0312 | 0.1617 | 38 |
| 0.1149 | 0.2297 | 0.3446 | 0.4594 | 0.5743 | 0.6892 | 0.8040 | 0.9189 | 1.0337 | 0.1621 | 39 |
| 0.1151 | 0.2303 | 0.3454 | 0.4606 | 0.5757 | 0.6909 | 0.8060 | 0.9212 | 1.0363 | 0.1625 | 40 |
| 0.1154 | 0.2309 | 0.3463 | 0.4617 | 0.5771 | 0.6926 | 0.8080 | 0.9234 | 1.0389 | 0.1629 | 41 |
| 0.1157 | 0.2314 | 0.3471 | 0.4628 | 0.5786 | 0.6943 | 0.8100 | 0.9257 | 1.0414 | 0.1633 | 42 |
| 0.1160 | 0.2320 | 0.3480 | 0.4640 | 0.5800 | 0.6960 | 0.8119 | 0.9279 | 1.0439 | 0.1637 | 43 |
| 0.1163 | 0.2326 | 0.3488 | 0.4651 | 0.5814 | 0.6977 | 0.8139 | 0.9302 | 1.0465 | 0.1641 | 44 |
| 0.1166 | 0.2331 | 0.3497 | 0.4662 | 0.5828 | 0.6994 | 0.8159 | 0.9325 | 1.0490 | 0.1645 | 45 |
| 0.1168 | 0.2337 | 0.3505 | 0.4674 | 0.5842 | 0.7010 | 0.8179 | 0.9347 | 1.0516 | 0.1650 | 46 |
| 0.1171 | 0.2342 | 0.3514 | 0.4685 | 0.5856 | 0.7027 | 0.8199 | 0.9370 | 1.0541 | 0.1654 | 47 |
| 0.1174 | 0.2348 | 0.3522 | 0.4696 | 0.5870 | 0.7045 | 0.8219 | 0.9393 | 1.0567 | 0.1658 | 48 |
| 0.1177 | 0.2354 | 0.3531 | 0.4708 | 0.5884 | 0.7061 | 0.8238 | 0.9415 | 1.0592 | 0.1662 | 49 |
| 0.1180 | 0.2359 | 0.3539 | 0.4719 | 0.5899 | 0.7078 | 0.8258 | 0.9438 | 1.0617 | 0.1666 | 50 |
| 0.1183 | 0.2365 | 0.3548 | 0.4730 | 0.5913 | 0.7095 | 0.8278 | 0.9460 | 1.0643 | 0.1670 | 51 |
| 0.1185 | 0.2371 | 0.3556 | 0.4742 | 0.5927 | 0.7112 | 0.8298 | 0.9483 | 1.0669 | 0.1674 | 52 |
| 0.1188 | 0.2376 | 0.3565 | 0.4753 | 0.5941 | 0.7129 | 0.8317 | 0.9506 | 1.0694 | 0.1678 | 53 |
| 0.1191 | 0.2382 | 0.3573 | 0.4764 | 0.5955 | 0.7146 | 0.8337 | 0.9528 | 1.0719 | 0.1682 | 54 |
| 0.1194 | 0.2388 | 0.3581 | 0.4775 | 0.5969 | 0.7163 | 0.8357 | 0.9550 | 1.0744 | 0.1686 | 55 |
| 0.1197 | 0.2393 | 0.3590 | 0.4786 | 0.5983 | 0.7180 | 0.8376 | 0.9573 | 1.0769 | 0.1690 | 56 |
| 0.1199 | 0.2399 | 0.3598 | 0.4798 | 0.5997 | 0.7197 | 0.8396 | 0.9596 | 1.0795 | 0.1694 | 57 |
| 0.1202 | 0.2405 | 0.3607 | 0.4809 | 0.6011 | 0.7214 | 0.8416 | 0.9618 | 1.0821 | 0.1698 | 58 |
| 0.1205 | 0.2410 | 0.3615 | 0.4820 | 0.6025 | 0.7231 | 0.8436 | 0.9641 | 1.0846 | 0.1702 | 59 |
| 0.1208 | 0.2416 | 0.3624 | 0.4832 | 0.6040 | 0.7247 | 0.8455 | 0.9663 | 1.0871 | 0.1706 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.6838 | 1.6675 | 2.9513 | 3.9351 | 4.9188 | 5.9026 | 6.8864 | 7.8702 | 8.8539 | 1.3896 |
| 01 | 0.6837 | 1.6674 | 2.9511 | 3.9348 | 4.9185 | 5.9022 | 6.8859 | 7.8696 | 8.8533 | 1.3896 |
| 02 | 0.6836 | 1.6673 | 2.9509 | 3.9345 | 4.9181 | 5.9018 | 6.8854 | 7.8690 | 8.8526 | 1.3895 |
| 03 | 0.6835 | 1.6671 | 2.9507 | 3.9342 | 4.9178 | 5.9013 | 6.8849 | 7.8684 | 8.8520 | 1.3895 |
| 04 | 0.6835 | 1.6670 | 2.9505 | 3.9339 | 4.9174 | 5.9009 | 6.8844 | 7.8679 | 8.8514 | 1.3894 |
| 05 | 0.6834 | 1.6668 | 2.9502 | 3.9337 | 4.9171 | 5.9005 | 6.8839 | 7.8673 | 8.8507 | 1.3894 |
| 06 | 0.6833 | 1.6667 | 2.9500 | 3.9334 | 4.9167 | 5.9001 | 6.8834 | 7.8667 | 8.8501 | 1.3893 |
| 07 | 0.6833 | 1.6665 | 2.9498 | 3.9331 | 4.9164 | 5.8996 | 6.8829 | 7.8662 | 8.8494 | 1.3893 |
| 08 | 0.6832 | 1.6664 | 2.9496 | 3.9328 | 4.9160 | 5.8992 | 6.8824 | 7.8656 | 8.8488 | 1.3892 |
| 09 | 0.6831 | 1.6663 | 2.9494 | 3.9325 | 4.9156 | 5.8988 | 6.8819 | 7.8650 | 8.8482 | 1.3892 |
| 10 | 0.6831 | 1.6661 | 2.9492 | 3.9322 | 4.9153 | 5.8983 | 6.8814 | 7.8645 | 8.8475 | 1.3891 |
| 11 | 0.6830 | 1.6660 | 2.9490 | 3.9319 | 4.9149 | 5.8979 | 6.8809 | 7.8639 | 8.8469 | 1.3891 |
| 12 | 0.6829 | 1.6658 | 2.9487 | 3.9316 | 4.9146 | 5.8975 | 6.8804 | 7.8633 | 8.8462 | 1.3890 |
| 13 | 0.6828 | 1.6657 | 2.9485 | 3.9314 | 4.9142 | 5.8970 | 6.8799 | 7.8627 | 8.8456 | 1.3890 |
| 14 | 0.6828 | 1.6655 | 2.9483 | 3.9311 | 4.9138 | 5.8966 | 6.8794 | 7.8621 | 8.8449 | 1.3889 |
| 15 | 0.6827 | 1.6654 | 2.9481 | 3.9308 | 4.9135 | 5.8962 | 6.8789 | 7.8616 | 8.8442 | 1.3889 |
| 16 | 0.6826 | 1.6652 | 2.9479 | 3.9305 | 4.9131 | 5.8957 | 6.8783 | 7.8610 | 8.8436 | 1.3888 |
| 17 | 0.6825 | 1.6651 | 2.9476 | 3.9302 | 4.9127 | 5.8953 | 6.8778 | 7.8604 | 8.8429 | 1.3888 |
| 18 | 0.6825 | 1.6650 | 2.9474 | 3.9299 | 4.9124 | 5.8949 | 6.8773 | 7.8598 | 8.8423 | 1.3887 |
| 19 | 0.6824 | 1.6648 | 2.9472 | 3.9296 | 4.9120 | 5.8944 | 6.8768 | 7.8592 | 8.8416 | 1.3887 |
| 20 | 0.6823 | 1.6647 | 2.9470 | 3.9293 | 4.9117 | 5.8940 | 6.8763 | 7.8586 | 8.8410 | 1.3886 |
| 21 | 0.6823 | 1.6645 | 2.9468 | 3.9290 | 4.9113 | 5.8935 | 6.8758 | 7.8580 | 8.8403 | 1.3886 |
| 22 | 0.6822 | 1.6644 | 2.9465 | 3.9287 | 4.9109 | 5.8931 | 6.8753 | 7.8574 | 8.8396 | 1.3885 |
| 23 | 0.6821 | 1.6642 | 2.9463 | 3.9284 | 4.9105 | 5.8926 | 6.8747 | 7.8569 | 8.8390 | 1.3885 |
| 24 | 0.6820 | 1.6641 | 2.9461 | 3.9281 | 4.9102 | 5.8922 | 6.8742 | 7.8563 | 8.8383 | 1.3884 |
| 25 | 0.6820 | 1.6639 | 2.9459 | 3.9278 | 4.9098 | 5.8918 | 6.8737 | 7.8557 | 8.8376 | 1.3884 |
| 26 | 0.6819 | 1.6638 | 2.9457 | 3.9275 | 4.9094 | 5.8913 | 6.8732 | 7.8551 | 8.8370 | 1.3883 |
| 27 | 0.6818 | 1.6636 | 2.9454 | 3.9272 | 4.9091 | 5.8909 | 6.8727 | 7.8545 | 8.8363 | 1.3883 |
| 28 | 0.6817 | 1.6635 | 2.9452 | 3.9269 | 4.9087 | 5.8904 | 6.8722 | 7.8539 | 8.8356 | 1.3882 |
| 29 | 0.6817 | 1.6633 | 2.9450 | 3.9266 | 4.9083 | 5.8900 | 6.8716 | 7.8533 | 8.8349 | 1.3882 |
| 30 | 0.6816 | 1.6632 | 2.9448 | 3.9263 | 4.9079 | 5.8895 | 6.8711 | 7.8527 | 8.8343 | 1.3881 |
| 31 | 0.6815 | 1.6630 | 2.9445 | 3.9260 | 4.9076 | 5.8891 | 6.8706 | 7.8521 | 8.8336 | 1.3881 |
| 32 | 0.6814 | 1.6629 | 2.9443 | 3.9257 | 4.9072 | 5.8886 | 6.8700 | 7.8515 | 8.8329 | 1.3880 |
| 33 | 0.6814 | 1.6627 | 2.9441 | 3.9254 | 4.9068 | 5.8882 | 6.8695 | 7.8509 | 8.8322 | 1.3880 |
| 34 | 0.6813 | 1.6626 | 2.9438 | 3.9251 | 4.9064 | 5.8877 | 6.8690 | 7.8503 | 8.8315 | 1.3879 |
| 35 | 0.6812 | 1.6624 | 2.9436 | 3.9248 | 4.9060 | 5.8872 | 6.8684 | 7.8497 | 8.8309 | 1.3879 |
| 36 | 0.6811 | 1.6623 | 2.9434 | 3.9245 | 4.9057 | 5.8868 | 6.8679 | 7.8490 | 8.8302 | 1.3878 |
| 37 | 0.6811 | 1.6621 | 2.9432 | 3.9242 | 4.9053 | 5.8863 | 6.8674 | 7.8484 | 8.8295 | 1.3878 |
| 38 | 0.6810 | 1.6620 | 2.9429 | 3.9239 | 4.9049 | 5.8859 | 6.8669 | 7.8478 | 8.8288 | 1.3877 |
| 39 | 0.6809 | 1.6618 | 2.9427 | 3.9236 | 4.9045 | 5.8854 | 6.8663 | 7.8472 | 8.8281 | 1.3876 |
| 40 | 0.6808 | 1.6617 | 2.9425 | 3.9233 | 4.9041 | 5.8850 | 6.8658 | 7.8466 | 8.8274 | 1.3876 |
| 41 | 0.6807 | 1.6615 | 2.9422 | 3.9230 | 4.9037 | 5.8845 | 6.8652 | 7.8460 | 8.8267 | 1.3875 |
| 42 | 0.6807 | 1.6613 | 2.9420 | 3.9227 | 4.9034 | 5.8840 | 6.8647 | 7.8454 | 8.8260 | 1.3875 |
| 43 | 0.6806 | 1.6612 | 2.9418 | 3.9224 | 4.9030 | 5.8836 | 6.8642 | 7.8448 | 8.8253 | 1.3874 |
| 44 | 0.6805 | 1.6610 | 2.9416 | 3.9221 | 4.9026 | 5.8831 | 6.8636 | 7.8441 | 8.8247 | 1.3874 |
| 45 | 0.6804 | 1.6609 | 2.9413 | 3.9218 | 4.9022 | 5.8826 | 6.8631 | 7.8435 | 8.8240 | 1.3873 |
| 46 | 0.6804 | 1.6607 | 2.9411 | 3.9214 | 4.9018 | 5.8822 | 6.8625 | 7.8429 | 8.8233 | 1.3872 |
| 47 | 0.6803 | 1.6606 | 2.9409 | 3.9211 | 4.9014 | 5.8817 | 6.8620 | 7.8423 | 8.8226 | 1.3872 |
| 48 | 0.6802 | 1.6604 | 2.9406 | 3.9208 | 4.9010 | 5.8812 | 6.8614 | 7.8416 | 8.8219 | 1.3871 |
| 49 | 0.6801 | 1.6603 | 2.9404 | 3.9205 | 4.9006 | 5.8808 | 6.8609 | 7.8410 | 8.8212 | 1.3871 |
| 50 | 0.6801 | 1.6601 | 2.9402 | 3.9202 | 4.9003 | 5.8803 | 6.8604 | 7.8404 | 8.8205 | 1.3870 |
| 51 | 0.6800 | 1.9599 | 2.9399 | 3.9199 | 4.8999 | 5.8798 | 6.8598 | 7.8398 | 8.8197 | 1.3870 |
| 52 | 0.6799 | 1.9598 | 2.9397 | 3.9196 | 4.8995 | 5.8794 | 6.8592 | 7.8391 | 8.8190 | 1.3869 |
| 53 | 0.6798 | 1.9596 | 2.9394 | 3.9193 | 4.8991 | 5.8789 | 6.8587 | 7.8385 | 8.8183 | 1.3868 |
| 54 | 0.6797 | 1.9595 | 2.9392 | 3.9189 | 4.8987 | 5.8784 | 6.8581 | 7.8379 | 8.8176 | 1.3868 |
| 55 | 0.6797 | 1.9593 | 2.9390 | 3.9186 | 4.8983 | 5.8779 | 6.8576 | 7.8372 | 8.8169 | 1.3867 |
| 56 | 0.6796 | 1.9592 | 2.9387 | 3.9183 | 4.8979 | 5.8775 | 6.8570 | 7.8366 | 8.8162 | 1.3866 |
| 57 | 0.6795 | 1.9590 | 2.9385 | 3.9180 | 4.8975 | 5.8770 | 6.8565 | 7.8360 | 8.8155 | 1.3866 |
| 58 | 0.6794 | 1.9588 | 2.9383 | 3.9177 | 4.8971 | 5.8765 | 6.8559 | 7.8353 | 8.8148 | 1.3865 |
| 59 | 0.6793 | 1.9587 | 2.9380 | 3.9173 | 4.8967 | 5.8760 | 6.8554 | 7.8347 | 8.8140 | 1.3865 |
| 60 | 0.6793 | 1.9585 | 2.9378 | 3.9170 | 4.8963 | 5.8755 | 6.8548 | 7.8341 | 8.8133 | 1.3864 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1208 | 0.2416 | 0.3624 | 0.4832 | 0.6040 | 0.7247 | 0.8455 | 0.9663 | 1.0871 | 0.1706 | 00 |
| 0.1211 | 0.2421 | 0.3632 | 0.4843 | 0.6054 | 0.7264 | 0.8475 | 0.9686 | 1.0896 | 0.1710 | 01 |
| 0.1214 | 0.2427 | 0.3641 | 0.4854 | 0.6068 | 0.7281 | 0.8495 | 0.9709 | 1.0922 | 0.1714 | 02 |
| 0.1216 | 0.2433 | 0.3649 | 0.4866 | 0.6082 | 0.7298 | 0.8515 | 0.9731 | 1.0948 | 0.1718 | 03 |
| 0.1219 | 0.2438 | 0.3658 | 0.4877 | 0.6196 | 0.7315 | 0.8534 | 0.9754 | 1.0973 | 0.1722 | 04 |
| 0.1222 | 0.2444 | 0.3666 | 0.4888 | 0.6110 | 0.7332 | 0.8554 | 0.9776 | 1.0998 | 0.1726 | 05 |
| 0.1225 | 0.2450 | 0.3674 | 0.4899 | 0.6124 | 0.7349 | 0.8574 | 0.9798 | 1.1023 | 0.1730 | 06 |
| 0.1228 | 0.2455 | 0.3683 | 0.4910 | 0.6138 | 0.7366 | 0.8593 | 0.9821 | 1.1048 | 0.1734 | 07 |
| 0.1230 | 0.2461 | 0.3691 | 0.4922 | 0.6152 | 0.7382 | 0.8613 | 0.9843 | 1.1074 | 0.1738 | 08 |
| 0.1233 | 0.2467 | 0.3700 | 0.4933 | 0.6166 | 0.7400 | 0.8633 | 0.9866 | 1.1100 | 0.1743 | 09 |
| 0.1236 | 0.2472 | 0.3708 | 0.4944 | 0.6180 | 0.7417 | 0.8653 | 0.9889 | 1.1125 | 0.1747 | 10 |
| 0.1239 | 0.2478 | 0.3717 | 0.4956 | 0.6194 | 0.7433 | 0.8672 | 0.9911 | 1.1150 | 0.1751 | 11 |
| 0.1242 | 0.2483 | 0.3725 | 0.4967 | 0.6209 | 0.7450 | 0.8692 | 0.9934 | 1.1175 | 0.1755 | 12 |
| 0.1245 | 0.2489 | 0.3734 | 0.4978 | 0.6223 | 0.7467 | 0.8712 | 0.9956 | 1.1201 | 0.1759 | 13 |
| 0.1247 | 0.2495 | 0.3742 | 0.4989 | 0.6237 | 0.7484 | 0.8731 | 0.9978 | 1.1226 | 0.1763 | 14 |
| 0.1250 | 0.2500 | 0.3750 | 0.5000 | 0.6251 | 0.7501 | 0.8751 | 1.0001 | 1.1251 | 0.1767 | 15 |
| 0.1253 | 0.2506 | 0.3759 | 0.5012 | 0.6265 | 0.7518 | 0.8771 | 1.0024 | 1.1277 | 0.1771 | 16 |
| 0.1256 | 0.2512 | 0.3767 | 0.5023 | 0.6279 | 0.7535 | 0.8791 | 1.0046 | 1.1302 | 0.1775 | 17 |
| 0.1259 | 0.2517 | 0.3776 | 0.5034 | 0.6293 | 0.7552 | 0.8810 | 1.0069 | 1.1327 | 0.1779 | 18 |
| 0.1261 | 0.2523 | 0.3784 | 0.5046 | 0.6307 | 0.7568 | 0.8830 | 1.0091 | 1.1353 | 0.1783 | 19 |
| 0.1264 | 0.2528 | 0.3793 | 0.5057 | 0.6321 | 0.7585 | 0.8849 | 1.0114 | 1.1378 | 0.1787 | 20 |
| 0.1267 | 0.2534 | 0.3801 | 0.5068 | 0.6335 | 0.7602 | 0.8869 | 1.0136 | 1.1403 | 0.1791 | 21 |
| 0.1270 | 0.2540 | 0.3809 | 0.5079 | 0.6349 | 0.7619 | 0.8889 | 1.0158 | 1.1428 | 0.1795 | 22 |
| 0.1273 | 0.2545 | 0.3818 | 0.5090 | 0.6363 | 0.7636 | 0.8908 | 1.0181 | 1.1453 | 0.1799 | 23 |
| 0.1275 | 0.2551 | 0.3826 | 0.5102 | 0.6377 | 0.7652 | 0.8928 | 1.0203 | 1.1479 | 0.1803 | 24 |
| 0.1278 | 0.2556 | 0.3835 | 0.5113 | 0.6391 | 0.7669 | 0.8947 | 1.0226 | 1.1504 | 0.1807 | 25 |
| 0.1281 | 0.2562 | 0.3843 | 0.5124 | 0.6405 | 0.7686 | 0.8967 | 1.0248 | 1.1529 | 0.1811 | 26 |
| 0.1284 | 0.2568 | 0.3852 | 0.5136 | 0.6419 | 0.7703 | 0.8987 | 1.0271 | 1.1555 | 0.1815 | 27 |
| 0.1287 | 0.2573 | 0.3860 | 0.5147 | 0.6433 | 0.7720 | 0.9007 | 1.0294 | 1.1580 | 0.1819 | 28 |
| 0.1289 | 0.2579 | 0.3868 | 0.5158 | 0.6447 | 0.7737 | 0.9026 | 1.0316 | 1.1605 | 0.1823 | 29 |
| 0.1292 | 0.2585 | 0.3877 | 0.5169 | 0.6461 | 0.7754 | 0.9046 | 1.0338 | 1.1631 | 0.1827 | 30 |
| 0.1295 | 0.2590 | 0.3885 | 0.5180 | 0.6475 | 0.7771 | 0.9066 | 1.0361 | 1.1656 | 0.1831 | 31 |
| 0.1298 | 0.2596 | 0.3894 | 0.5192 | 0.6489 | 0.7787 | 0.9085 | 1.0383 | 1.1681 | 0.1835 | 32 |
| 0.1301 | 0.2601 | 0.3902 | 0.5203 | 0.6503 | 0.7804 | 0.9105 | 1.0406 | 1.1706 | 0.1839 | 33 |
| 0.1303 | 0.2607 | 0.3910 | 0.5214 | 0.6517 | 0.7821 | 0.9124 | 1.0428 | 1.1731 | 0.1843 | 34 |
| 0.1306 | 0.2613 | 0.3919 | 0.5225 | 0.6532 | 0.7838 | 0.9144 | 1.0450 | 1.1757 | 0.1847 | 35 |
| 0.1309 | 0.2618 | 0.3927 | 0.5236 | 0.6546 | 0.7855 | 0.9164 | 1.0473 | 1.1782 | 0.1852 | 36 |
| 0.1312 | 0.2624 | 0.3936 | 0.5248 | 0.6560 | 0.7871 | 0.9183 | 1.0495 | 1.1807 | 0.1856 | 37 |
| 0.1315 | 0.2629 | 0.3944 | 0.5259 | 0.6574 | 0.7888 | 0.9203 | 1.0518 | 1.1832 | 0.1860 | 38 |
| 0.1318 | 0.2635 | 0.3953 | 0.5270 | 0.6588 | 0.7905 | 0.9223 | 1.0540 | 1.1858 | 0.1864 | 39 |
| 0.1320 | 0.2641 | 0.3961 | 0.5281 | 0.6602 | 0.7922 | 0.9242 | 1.0562 | 1.1883 | 0.1868 | 40 |
| 0.1323 | 0.2646 | 0.3969 | 0.5292 | 0.6616 | 0.7939 | 0.9262 | 1.0585 | 1.1908 | 0.1872 | 41 |
| 0.1326 | 0.2652 | 0.3978 | 0.5304 | 0.6630 | 0.7955 | 0.9281 | 1.0607 | 1.1933 | 0.1876 | 42 |
| 0.1329 | 0.2657 | 0.3986 | 0.5315 | 0.6644 | 0.7972 | 0.9301 | 1.0630 | 1.1958 | 0.1880 | 43 |
| 0.1332 | 0.2663 | 0.3995 | 0.5326 | 0.6658 | 0.7989 | 0.9321 | 1.0652 | 1.1984 | 0.1884 | 44 |
| 0.1334 | 0.2669 | 0.4003 | 0.5337 | 0.6672 | 0.8006 | 0.9340 | 1.0674 | 1.2009 | 0.1888 | 45 |
| 0.1337 | 0.2674 | 0.4011 | 0.5348 | 0.6686 | 0.8023 | 0.9360 | 1.0697 | 1.2034 | 0.1892 | 46 |
| 0.1340 | 0.2680 | 0.4020 | 0.5360 | 0.6700 | 0.8039 | 0.9379 | 1.0719 | 1.2059 | 0.1896 | 47 |
| 0.1343 | 0.2685 | 0.4028 | 0.5371 | 0.6714 | 0.8056 | 0.9399 | 1.0742 | 1.2084 | 0.1900 | 48 |
| 0.1346 | 0.2691 | 0.4037 | 0.5382 | 0.6728 | 0.8073 | 0.9419 | 1.0764 | 1.2110 | 0.1904 | 49 |
| 0.1348 | 0.2697 | 0.4045 | 0.5393 | 0.6742 | 0.8090 | 0.9438 | 1.0786 | 1.2135 | 0.1908 | 50 |
| 0.1351 | 0.2702 | 0.4053 | 0.5404 | 0.6756 | 0.8107 | 0.9458 | 1.0809 | 1.2160 | 0.1912 | 51 |
| 0.1354 | 0.2708 | 0.4062 | 0.5416 | 0.6770 | 0.8123 | 0.9477 | 1.0831 | 1.2185 | 0.1916 | 52 |
| 0.1357 | 0.2713 | 0.4070 | 0.5427 | 0.6783 | 0.8140 | 0.9497 | 1.0854 | 1.2210 | 0.1920 | 53 |
| 0.1359 | 0.2719 | 0.4078 | 0.5438 | 0.6797 | 0.8157 | 0.9516 | 1.0876 | 1.2235 | 0.1924 | 54 |
| 0.1362 | 0.2725 | 0.4087 | 0.5449 | 0.6811 | 0.8174 | 0.9536 | 1.0898 | 1.2261 | 0.1928 | 55 |
| 0.1365 | 0.2730 | 0.4095 | 0.5460 | 0.6825 | 0.8191 | 0.9556 | 1.0921 | 1.2286 | 0.1932 | 56 |
| 0.1368 | 0.2736 | 0.4104 | 0.5472 | 0.6839 | 0.8207 | 0.9575 | 1.0943 | 1.2311 | 0.1936 | 57 |
| 0.1371 | 0.2741 | 0.4112 | 0.5483 | 0.6853 | 0.8224 | 0.9595 | 1.0966 | 1.2336 | 0.1940 | 58 |
| 0.1374 | 0.2747 | 0.4121 | 0.5494 | 0.6867 | 0.8241 | 0.9615 | 1.0988 | 1.2362 | 0.1944 | 59 |
| 0.1376 | 0.2753 | 0.4129 | 0.5505 | 0.6881 | 0.8258 | 0.9634 | 1.1010 | 1.2387 | 0.1948 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9999 | 1.9917 | 2.9875 | 3.9835 | 4.9793 | 5.9752 | 6.9711 | 7.9669 | 8.9628 | 1.3981 |
| 01 | 0.9998 | 1.9917 | 2.9875 | 3.9833 | 4.9792 | 5.9750 | 6.9708 | 7.9667 | 8.9625 | 1.3981 |
| 02 | 0.9998 | 1.9916 | 2.9874 | 3.9832 | 4.9790 | 5.9748 | 6.9706 | 7.9664 | 8.9622 | 1.3981 |
| 03 | 0.9998 | 1.9915 | 2.9873 | 3.9831 | 4.9789 | 5.9746 | 6.9704 | 7.9662 | 8.9619 | 1.3980 |
| 04 | 0.9997 | 1.9915 | 2.9872 | 3.9830 | 4.9787 | 5.9744 | 6.9702 | 7.9659 | 8.9617 | 1.3980 |
| 05 | 0.9997 | 1.9914 | 2.9871 | 3.9828 | 4.9785 | 5.9743 | 6.9700 | 7.9657 | 8.9614 | 1.3980 |
| 06 | 0.9997 | 1.9914 | 2.9870 | 3.9827 | 4.9784 | 5.9741 | 6.9697 | 7.9654 | 8.9611 | 1.3980 |
| 07 | 0.9996 | 1.9913 | 2.9869 | 3.9826 | 4.9782 | 5.9739 | 6.9695 | 7.9652 | 8.9608 | 1.3980 |
| 08 | 0.9996 | 1.9912 | 2.9868 | 3.9825 | 4.9781 | 5.9737 | 6.9693 | 7.9649 | 8.9605 | 1.3979 |
| 09 | 0.9996 | 1.9912 | 2.9868 | 3.9823 | 4.9779 | 5.9735 | 6.9691 | 7.9647 | 8.9603 | 1.3979 |
| 10 | 0.9996 | 1.9911 | 2.9867 | 3.9822 | 4.9778 | 5.9733 | 6.9689 | 7.9644 | 8.9600 | 1.3979 |
| 11 | 0.9995 | 1.9910 | 2.9866 | 3.9821 | 4.9776 | 5.9731 | 6.9686 | 7.9642 | 8.9597 | 1.3979 |
| 12 | 0.9995 | 1.9910 | 2.9865 | 3.9819 | 4.9774 | 5.9729 | 6.9684 | 7.9639 | 8.9594 | 1.3978 |
| 13 | 0.9995 | 1.9909 | 2.9864 | 3.9818 | 4.9773 | 5.9727 | 6.9682 | 7.9636 | 8.9591 | 1.3978 |
| 14 | 0.9994 | 1.9908 | 2.9863 | 3.9817 | 4.9771 | 5.9725 | 6.9679 | 7.9634 | 8.9588 | 1.3978 |
| 15 | 0.9994 | 1.9908 | 2.9862 | 3.9816 | 4.9769 | 5.9723 | 6.9677 | 7.9631 | 8.9585 | 1.3978 |
| 16 | 0.9994 | 1.9907 | 2.9861 | 3.9814 | 4.9768 | 5.9721 | 6.9675 | 7.9628 | 8.9582 | 1.3977 |
| 17 | 0.9993 | 1.9906 | 2.9860 | 3.9813 | 4.9766 | 5.9719 | 6.9673 | 7.9626 | 8.9579 | 1.3977 |
| 18 | 0.9993 | 1.9906 | 2.9859 | 3.9812 | 4.9764 | 5.9717 | 6.9670 | 7.9623 | 8.9576 | 1.3977 |
| 19 | 0.9993 | 1.9905 | 2.9858 | 3.9810 | 4.9763 | 5.9715 | 6.9668 | 7.9621 | 8.9573 | 1.3977 |
| 20 | 0.9992 | 1.9904 | 2.9857 | 3.9809 | 4.9761 | 5.9713 | 6.9666 | 7.9618 | 8.9570 | 1.3976 |
| 21 | 0.9992 | 1.9904 | 2.9856 | 3.9808 | 4.9759 | 5.9711 | 6.9663 | 7.9615 | 8.9567 | 1.3976 |
| 22 | 0.9992 | 1.9903 | 2.9855 | 3.9806 | 4.9758 | 5.9709 | 6.9661 | 7.9612 | 8.9564 | 1.3976 |
| 23 | 0.9991 | 1.9902 | 2.9854 | 3.9805 | 4.9756 | 5.9707 | 6.9658 | 7.9610 | 8.9561 | 1.3976 |
| 24 | 0.9991 | 1.9902 | 2.9853 | 3.9803 | 4.9754 | 5.9705 | 6.9656 | 7.9607 | 8.9558 | 1.3975 |
| 25 | 0.9991 | 1.9901 | 2.9852 | 3.9802 | 4.9753 | 5.9703 | 6.9654 | 7.9604 | 8.9555 | 1.3975 |
| 26 | 0.9990 | 1.9900 | 2.9850 | 3.9801 | 4.9751 | 5.9701 | 6.9651 | 7.9601 | 8.9551 | 1.3975 |
| 27 | 0.9990 | 1.9900 | 2.9849 | 3.9799 | 4.9749 | 5.9699 | 6.9649 | 7.9599 | 8.9548 | 1.3975 |
| 28 | 0.9989 | 1.9899 | 2.9848 | 3.9798 | 4.9747 | 5.9697 | 6.9646 | 7.9596 | 8.9545 | 1.3974 |
| 29 | 0.9989 | 1.9898 | 2.9847 | 3.9797 | 4.9746 | 5.9695 | 6.9644 | 7.9595 | 8.9542 | 1.3974 |
| 30 | 0.9989 | 1.9898 | 2.9846 | 3.9795 | 4.9744 | 5.9693 | 6.9641 | 7.9593 | 8.9539 | 1.3974 |
| 31 | 0.9988 | 1.9897 | 2.9845 | 3.9794 | 4.9742 | 5.9691 | 6.9639 | 7.9587 | 8.9536 | 1.3973 |
| 32 | 0.9988 | 1.9896 | 2.9844 | 3.9792 | 4.9740 | 5.9688 | 6.9636 | 7.9584 | 8.9533 | 1.3973 |
| 33 | 0.9988 | 1.9895 | 2.9843 | 3.9791 | 4.9738 | 5.9686 | 6.9634 | 7.9582 | 8.9529 | 1.3973 |
| 34 | 0.9987 | 1.9895 | 2.9842 | 3.9789 | 4.9737 | 5.9684 | 6.9631 | 7.9579 | 8.9526 | 1.3973 |
| 35 | 0.9987 | 1.9894 | 2.9841 | 3.9788 | 4.9735 | 5.9682 | 6.9629 | 7.9576 | 8.9523 | 1.3972 |
| 36 | 0.9987 | 1.9893 | 2.9840 | 3.9786 | 4.9733 | 5.9680 | 6.9626 | 7.9573 | 8.9519 | 1.3972 |
| 37 | 0.9986 | 1.9893 | 2.9839 | 3.9785 | 4.9731 | 5.9678 | 6.9624 | 7.9570 | 8.9516 | 1.3972 |
| 38 | 0.9986 | 1.9892 | 2.9838 | 3.9784 | 4.9729 | 5.9675 | 6.9621 | 7.9567 | 8.9513 | 1.3972 |
| 39 | 0.9986 | 1.9891 | 2.9837 | 3.9782 | 4.9728 | 5.9673 | 6.9619 | 7.9564 | 8.9510 | 1.3971 |
| 40 | 0.9985 | 1.9890 | 2.9835 | 3.9781 | 4.9726 | 5.9671 | 6.9616 | 7.9561 | 8.9506 | 1.3971 |
| 41 | 0.9985 | 1.9890 | 2.9834 | 3.9779 | 4.9724 | 5.9669 | 6.9613 | 7.9558 | 8.9503 | 1.3971 |
| 42 | 0.9984 | 1.9889 | 2.9833 | 3.9778 | 4.9722 | 5.9666 | 6.9611 | 7.9555 | 8.9500 | 1.3971 |
| 43 | 0.9984 | 1.9888 | 2.9832 | 3.9776 | 4.9720 | 5.9664 | 6.9608 | 7.9552 | 8.9496 | 1.3970 |
| 44 | 0.9984 | 1.9887 | 2.9831 | 3.9775 | 4.9718 | 5.9662 | 6.9605 | 7.9549 | 8.9493 | 1.3970 |
| 45 | 0.9983 | 1.9887 | 2.9830 | 3.9773 | 4.9716 | 5.9660 | 6.9603 | 7.9546 | 8.9489 | 1.3970 |
| 46 | 0.9983 | 1.9886 | 2.9829 | 3.9772 | 4.9714 | 5.9657 | 6.9600 | 7.9543 | 8.9486 | 1.3969 |
| 47 | 0.9983 | 1.9885 | 2.9828 | 3.9770 | 4.9713 | 5.9655 | 6.9598 | 7.9540 | 8.9483 | 1.3969 |
| 48 | 0.9982 | 1.9884 | 2.9826 | 3.9769 | 4.9711 | 5.9653 | 6.9595 | 7.9537 | 8.9479 | 1.3969 |
| 49 | 0.9982 | 1.9884 | 2.9825 | 3.9767 | 4.9709 | 5.9651 | 6.9592 | 7.9534 | 8.9476 | 1.3968 |
| 50 | 0.9981 | 1.9883 | 2.9824 | 3.9765 | 4.9707 | 5.9648 | 6.9590 | 7.9531 | 8.9472 | 1.3968 |
| 51 | 0.9981 | 1.9882 | 2.9823 | 3.9764 | 4.9705 | 5.9646 | 6.9587 | 7.9528 | 8.9469 | 1.3968 |
| 52 | 0.9981 | 1.9881 | 2.9822 | 3.9762 | 4.9703 | 5.9643 | 6.9584 | 7.9525 | 8.9465 | 1.3968 |
| 53 | 0.9980 | 1.9880 | 2.9821 | 3.9761 | 4.9701 | 5.9641 | 6.9581 | 7.9521 | 8.9462 | 1.3968 |
| 54 | 0.9980 | 1.9880 | 2.9819 | 3.9759 | 4.9699 | 5.9639 | 6.9579 | 7.9518 | 8.9458 | 1.3967 |
| 55 | 0.9979 | 1.9879 | 2.9818 | 3.9758 | 4.9697 | 5.9636 | 6.9576 | 7.9515 | 8.9455 | 1.3967 |
| 56 | 0.9979 | 1.9878 | 2.9817 | 3.9756 | 4.9695 | 5.9634 | 6.9573 | 7.9512 | 8.9451 | 1.3967 |
| 57 | 0.9979 | 1.9877 | 2.9816 | 3.9754 | 4.9693 | 5.9632 | 6.9570 | 7.9509 | 8.9447 | 1.3967 |
| 58 | 0.9978 | 1.9876 | 2.9815 | 3.9753 | 4.9691 | 5.9629 | 6.9567 | 7.9506 | 8.9444 | 1.3966 |
| 59 | 0.9978 | 1.9876 | 2.9813 | 3.9751 | 4.9689 | 5.9627 | 6.9565 | 7.9502 | 8.9440 | 1.3966 |
| 60 | 0.9977 | 1.9875 | 2.9812 | 3.9750 | 4.9687 | 5.9624 | 6.9562 | 7.9499 | 8.9437 | 1.3966 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0522 | 0.1044 | 0.1566 | 0.2088 | 0.2610 | 0.3131 | 0.3653 | 0.4175 | 0.4697 | 0.0733 | 00 |
| 0.0525 | 0.1050 | 0.1574 | 0.2099 | 0.2624 | 0.3149 | 0.3674 | 0.4198 | 0.4723 | 0.0737 | 01 |
| 0.0528 | 0.1055 | 0.1583 | 0.2111 | 0.2638 | 0.3166 | 0.3694 | 0.4222 | 0.4749 | 0.0741 | 02 |
| 0.0531 | 0.1061 | 0.1592 | 0.2122 | 0.2653 | 0.3184 | 0.3714 | 0.4245 | 0.4775 | 0.0745 | 03 |
| 0.0533 | 0.1067 | 0.1600 | 0.2134 | 0.2667 | 0.3201 | 0.3734 | 0.4268 | 0.4801 | 0.0749 | 04 |
| 0.0536 | 0.1073 | 0.1609 | 0.2145 | 0.2682 | 0.3218 | 0.3754 | 0.4291 | 0.4827 | 0.0753 | 05 |
| 0.0539 | 0.1078 | 0.1618 | 0.2157 | 0.2696 | 0.3235 | 0.3774 | 0.4314 | 0.4853 | 0.0757 | 06 |
| 0.0542 | 0.1084 | 0.1626 | 0.2168 | 0.2711 | 0.3253 | 0.3795 | 0.4337 | 0.4879 | 0.0761 | 07 |
| 0.0545 | 0.1090 | 0.1635 | 0.2180 | 0.2725 | 0.3270 | 0.3815 | 0.4360 | 0.4905 | 0.0765 | 08 |
| 0.0548 | 0.1096 | 0.1644 | 0.2192 | 0.2739 | 0.3287 | 0.3835 | 0.4383 | 0.4931 | 0.0769 | 09 |
| 0.0551 | 0.1102 | 0.1652 | 0.2203 | 0.2754 | 0.3305 | 0.3856 | 0.4406 | 0.4957 | 0.0773 | 10 |
| 0.0554 | 0.1107 | 0.1661 | 0.2215 | 0.2768 | 0.3322 | 0.3876 | 0.4430 | 0.4983 | 0.0777 | 11 |
| 0.0557 | 0.1113 | 0.1670 | 0.2226 | 0.2783 | 0.3340 | 0.3896 | 0.4453 | 0.5009 | 0.0781 | 12 |
| 0.0559 | 0.1119 | 0.1678 | 0.2238 | 0.2797 | 0.3356 | 0.3916 | 0.4475 | 0.5035 | 0.0786 | 13 |
| 0.0562 | 0.1125 | 0.1687 | 0.2249 | 0.2812 | 0.3374 | 0.3936 | 0.4498 | 0.5061 | 0.0790 | 14 |
| 0.0565 | 0.1130 | 0.1696 | 0.2261 | 0.2826 | 0.3391 | 0.3956 | 0.4522 | 0.5087 | 0.0794 | 15 |
| 0.0568 | 0.1136 | 0.1704 | 0.2272 | 0.2841 | 0.3409 | 0.3977 | 0.4545 | 0.5113 | 0.0798 | 16 |
| 0.0571 | 0.1142 | 0.1713 | 0.2284 | 0.2855 | 0.3426 | 0.3997 | 0.4568 | 0.5139 | 0.0802 | 17 |
| 0.0574 | 0.1148 | 0.1722 | 0.2296 | 0.2869 | 0.3443 | 0.4017 | 0.4591 | 0.5165 | 0.0806 | 18 |
| 0.0577 | 0.1154 | 0.1730 | 0.2307 | 0.2884 | 0.3461 | 0.4038 | 0.4614 | 0.5191 | 0.0810 | 19 |
| 0.0580 | 0.1159 | 0.1739 | 0.2319 | 0.2898 | 0.3478 | 0.4058 | 0.4638 | 0.5217 | 0.0814 | 20 |
| 0.0583 | 0.1165 | 0.1748 | 0.2330 | 0.2913 | 0.3495 | 0.4078 | 0.4660 | 0.5243 | 0.0818 | 21 |
| 0.0585 | 0.1171 | 0.1756 | 0.2342 | 0.2927 | 0.3512 | 0.4098 | 0.4683 | 0.5269 | 0.0822 | 22 |
| 0.0588 | 0.1177 | 0.1765 | 0.2353 | 0.2942 | 0.3530 | 0.4118 | 0.4706 | 0.5295 | 0.0826 | 23 |
| 0.0591 | 0.1182 | 0.1774 | 0.2365 | 0.2956 | 0.3547 | 0.4138 | 0.4730 | 0.5321 | 0.0830 | 24 |
| 0.0594 | 0.1188 | 0.1782 | 0.2376 | 0.2971 | 0.3565 | 0.4159 | 0.4753 | 0.5347 | 0.0834 | 25 |
| 0.0597 | 0.1194 | 0.1791 | 0.2388 | 0.2985 | 0.3582 | 0.4179 | 0.4776 | 0.5373 | 0.0838 | 26 |
| 0.0600 | 0.1200 | 0.1799 | 0.2399 | 0.2999 | 0.3599 | 0.4199 | 0.4799 | 0.5399 | 0.0842 | 27 |
| 0.0603 | 0.1205 | 0.1808 | 0.2411 | 0.3014 | 0.3616 | 0.4219 | 0.4822 | 0.5425 | 0.0847 | 28 |
| 0.0606 | 0.1211 | 0.1817 | 0.2422 | 0.3028 | 0.3634 | 0.4239 | 0.4845 | 0.5451 | 0.0851 | 29 |
| 0.0608 | 0.1217 | 0.1825 | 0.2434 | 0.3042 | 0.3651 | 0.4259 | 0.4868 | 0.5477 | 0.0855 | 30 |
| 0.0611 | 0.1223 | 0.1834 | 0.2446 | 0.3057 | 0.3668 | 0.4280 | 0.4891 | 0.5503 | 0.0859 | 31 |
| 0.0614 | 0.1229 | 0.1843 | 0.2457 | 0.3071 | 0.3686 | 0.4300 | 0.4914 | 0.5529 | 0.0863 | 32 |
| 0.0617 | 0.1234 | 0.1851 | 0.2468 | 0.3086 | 0.3703 | 0.4320 | 0.4937 | 0.5554 | 0.0867 | 33 |
| 0.0620 | 0.1240 | 0.1860 | 0.2480 | 0.3100 | 0.3720 | 0.4340 | 0.4960 | 0.5580 | 0.0871 | 34 |
| 0.0623 | 0.1246 | 0.1869 | 0.2492 | 0.3115 | 0.3737 | 0.4360 | 0.4983 | 0.5606 | 0.0875 | 35 |
| 0.0626 | 0.1252 | 0.1877 | 0.2503 | 0.3129 | 0.3755 | 0.4381 | 0.5006 | 0.5632 | 0.0879 | 36 |
| 0.0629 | 0.1257 | 0.1886 | 0.2515 | 0.3143 | 0.3772 | 0.4401 | 0.5030 | 0.5658 | 0.0883 | 37 |
| 0.0632 | 0.1263 | 0.1895 | 0.2526 | 0.3158 | 0.3789 | 0.4421 | 0.5053 | 0.5684 | 0.0887 | 38 |
| 0.0634 | 0.1269 | 0.1903 | 0.2538 | 0.3172 | 0.3806 | 0.4441 | 0.5075 | 0.5710 | 0.0891 | 39 |
| 0.0637 | 0.1275 | 0.1912 | 0.2549 | 0.3187 | 0.3824 | 0.4461 | 0.5098 | 0.5736 | 0.0895 | 40 |
| 0.0640 | 0.1280 | 0.1921 | 0.2561 | 0.3201 | 0.3841 | 0.4481 | 0.5122 | 0.5762 | 0.0899 | 41 |
| 0.0643 | 0.1286 | 0.1929 | 0.2572 | 0.3215 | 0.3859 | 0.4502 | 0.5145 | 0.5788 | 0.0903 | 42 |
| 0.0646 | 0.1292 | 0.1938 | 0.2584 | 0.3230 | 0.3876 | 0.4522 | 0.5168 | 0.5814 | 0.0908 | 43 |
| 0.0649 | 0.1298 | 0.1946 | 0.2595 | 0.3244 | 0.3893 | 0.4542 | 0.5190 | 0.5839 | 0.0912 | 44 |
| 0.0652 | 0.1303 | 0.1955 | 0.2607 | 0.3259 | 0.3910 | 0.4562 | 0.5214 | 0.5865 | 0.0916 | 45 |
| 0.0655 | 0.1309 | 0.1964 | 0.2618 | 0.3273 | 0.3928 | 0.4582 | 0.5237 | 0.5891 | 0.0920 | 46 |
| 0.0657 | 0.1315 | 0.1972 | 0.2630 | 0.3287 | 0.3945 | 0.4602 | 0.5260 | 0.5917 | 0.0924 | 47 |
| 0.0660 | 0.1321 | 0.1981 | 0.2642 | 0.3302 | 0.3962 | 0.4622 | 0.5283 | 0.5943 | 0.0928 | 48 |
| 0.0663 | 0.1326 | 0.1990 | 0.2653 | 0.3316 | 0.3979 | 0.4642 | 0.5306 | 0.5969 | 0.0932 | 49 |
| 0.0666 | 0.1332 | 0.1998 | 0.2664 | 0.3331 | 0.3997 | 0.4663 | 0.5329 | 0.5995 | 0.0936 | 50 |
| 0.0669 | 0.1338 | 0.2007 | 0.2676 | 0.3345 | 0.4014 | 0.4683 | 0.5352 | 0.6021 | 0.0940 | 51 |
| 0.0672 | 0.1344 | 0.2016 | 0.2688 | 0.3359 | 0.4031 | 0.4703 | 0.5375 | 0.6047 | 0.0944 | 52 |
| 0.0675 | 0.1349 | 0.2024 | 0.2699 | 0.3374 | 0.4048 | 0.4723 | 0.5398 | 0.6073 | 0.0948 | 53 |
| 0.0678 | 0.1355 | 0.2033 | 0.2710 | 0.3388 | 0.4066 | 0.4743 | 0.5421 | 0.6099 | 0.0952 | 54 |
| 0.0681 | 0.1361 | 0.2042 | 0.2722 | 0.3403 | 0.4083 | 0.4764 | 0.5444 | 0.6125 | 0.0956 | 55 |
| 0.0683 | 0.1367 | 0.2050 | 0.2734 | 0.3417 | 0.4100 | 0.4784 | 0.5467 | 0.6151 | 0.0961 | 56 |
| 0.0686 | 0.1373 | 0.2059 | 0.2745 | 0.3431 | 0.4118 | 0.4804 | 0.5490 | 0.6177 | 0.0965 | 57 |
| 0.0689 | 0.1378 | 0.2067 | 0.2756 | 0.3446 | 0.4135 | 0.4824 | 0.5513 | 0.6202 | 0.0969 | 58 |
| 0.0692 | 0.1384 | 0.2076 | 0.2768 | 0.3460 | 0.4152 | 0.4844 | 0.5536 | 0.6228 | 0.0973 | 59 |
| 0.0695 | 0.1390 | 0.2085 | 0.2780 | 0.3474 | 0.4169 | 0.4864 | 0.5559 | 0.6254 | 0.0977 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9937 | 1.9875 | 2.9812 | 3.9750 | 4.9687 | 5.9624 | 6.9562 | 7.9499 | 8.9437 | 1.3966 |
| 01 | 0.9937 | 1.9874 | 2.9811 | 3.9748 | 4.9685 | 5.9622 | 6.9559 | 7.9496 | 8.9433 | 1.3966 |
| 02 | 0.9937 | 1.9873 | 2.9810 | 3.9746 | 4.9683 | 5.9619 | 6.9556 | 7.9493 | 8.9429 | 1.3965 |
| 03 | 0.9936 | 1.9872 | 2.9809 | 3.9745 | 4.9681 | 5.9617 | 6.9553 | 7.9489 | 8.9426 | 1.3965 |
| 04 | 0.9936 | 1.9872 | 2.9807 | 3.9743 | 4.9679 | 5.9615 | 6.9550 | 7.9486 | 8.9422 | 1.3965 |
| 05 | 0.9935 | 1.9871 | 2.9806 | 3.9741 | 4.9677 | 5.9612 | 6.9547 | 7.9483 | 8.9418 | 1.3965 |
| 06 | 0.9935 | 1.9870 | 2.9805 | 3.9740 | 4.9675 | 5.9610 | 6.9545 | 7.9479 | 8.9414 | 1.3964 |
| 07 | 0.9935 | 1.9869 | 2.9804 | 3.9738 | 4.9673 | 5.9607 | 6.9542 | 7.9476 | 8.9411 | 1.3964 |
| 08 | 0.9934 | 1.9868 | 2.9802 | 3.9736 | 4.9671 | 5.9605 | 6.9539 | 7.9473 | 8.9407 | 1.3964 |
| 09 | 0.9934 | 1.9867 | 2.9801 | 3.9735 | 4.9668 | 5.9602 | 6.9536 | 7.9470 | 8.9403 | 1.3963 |
| 10 | 0.9933 | 1.9867 | 2.9800 | 3.9734 | 4.9666 | 5.9600 | 6.9533 | 7.9466 | 8.9400 | 1.3963 |
| 11 | 0.9933 | 1.9866 | 2.9799 | 3.9731 | 4.9664 | 5.9597 | 6.9530 | 7.9463 | 8.9396 | 1.3963 |
| 12 | 0.9932 | 1.9865 | 2.9797 | 3.9730 | 4.9662 | 5.9595 | 6.9527 | 7.9459 | 8.9392 | 1.3963 |
| 13 | 0.9932 | 1.9864 | 2.9796 | 3.9728 | 4.9660 | 5.9592 | 6.9524 | 7.9456 | 8.9388 | 1.3962 |
| 14 | 0.9932 | 1.9863 | 2.9795 | 3.9726 | 4.9658 | 5.9589 | 6.9521 | 7.9452 | 8.9384 | 1.3962 |
| 15 | 0.9931 | 1.9862 | 2.9793 | 3.9725 | 4.9656 | 5.9587 | 6.9518 | 7.9449 | 8.9380 | 1.3962 |
| 16 | 0.9931 | 1.9861 | 2.9792 | 3.9723 | 4.9654 | 5.9584 | 6.9515 | 7.9446 | 8.9376 | 1.3962 |
| 17 | 0.9930 | 1.9861 | 2.9791 | 3.9721 | 4.9651 | 5.9582 | 6.9512 | 7.9442 | 8.9373 | 1.3961 |
| 18 | 0.9930 | 1.9860 | 2.9790 | 3.9719 | 4.9649 | 5.9579 | 6.9509 | 7.9439 | 8.9369 | 1.3961 |
| 19 | 0.9929 | 1.9859 | 2.9788 | 3.9718 | 4.9647 | 5.9577 | 6.9506 | 7.9435 | 8.9365 | 1.3961 |
| 20 | 0.9929 | 1.9858 | 2.9787 | 3.9716 | 4.9645 | 5.9574 | 6.9503 | 7.9432 | 8.9361 | 1.3960 |
| 21 | 0.9929 | 1.9857 | 2.9786 | 3.9714 | 4.9643 | 5.9571 | 6.9500 | 7.9428 | 8.9357 | 1.3960 |
| 22 | 0.9928 | 1.9856 | 2.9784 | 3.9712 | 4.9641 | 5.9569 | 6.9497 | 7.9425 | 8.9353 | 1.3960 |
| 23 | 0.9928 | 1.9855 | 2.9783 | 3.9711 | 4.9638 | 5.9566 | 6.9494 | 7.9421 | 8.9349 | 1.3959 |
| 24 | 0.9927 | 1.9854 | 2.9782 | 3.9709 | 4.9636 | 5.9563 | 6.9490 | 7.9418 | 8.9345 | 1.3959 |
| 25 | 0.9927 | 1.9854 | 2.9780 | 3.9707 | 4.9634 | 5.9561 | 6.9487 | 7.9414 | 8.9341 | 1.3959 |
| 26 | 0.9926 | 1.9853 | 2.9779 | 3.9705 | 4.9632 | 5.9558 | 6.9484 | 7.9410 | 8.9337 | 1.3958 |
| 27 | 0.9926 | 1.9852 | 2.9778 | 3.9703 | 4.9629 | 5.9555 | 6.9481 | 7.9407 | 8.9333 | 1.3958 |
| 28 | 0.9925 | 1.9851 | 2.9776 | 3.9702 | 4.9627 | 5.9553 | 6.9478 | 7.9403 | 8.9329 | 1.3958 |
| 29 | 0.9925 | 1.9850 | 2.9775 | 3.9700 | 4.9625 | 5.9550 | 6.9475 | 7.9400 | 8.9325 | 1.3958 |
| 30 | 0.9925 | 1.9849 | 2.9774 | 3.9698 | 4.9623 | 5.9547 | 6.9472 | 7.9396 | 8.9321 | 1.3957 |
| 31 | 0.9924 | 1.9848 | 2.9772 | 3.9696 | 4.9620 | 5.9544 | 6.9468 | 7.9393 | 8.9317 | 1.3957 |
| 32 | 0.9924 | 1.9847 | 2.9771 | 3.9694 | 4.9618 | 5.9542 | 6.9465 | 7.9389 | 8.9312 | 1.3957 |
| 33 | 0.9923 | 1.9846 | 2.9769 | 3.9693 | 4.9616 | 5.9539 | 6.9462 | 7.9385 | 8.9308 | 1.3956 |
| 34 | 0.9923 | 1.9845 | 2.9768 | 3.9691 | 4.9613 | 5.9536 | 6.9459 | 7.9381 | 8.9304 | 1.3956 |
| 35 | 0.9922 | 1.9844 | 2.9767 | 3.9689 | 4.9611 | 5.9533 | 6.9456 | 7.9378 | 8.9300 | 1.3956 |
| 36 | 0.9922 | 1.9844 | 2.9765 | 3.9687 | 4.9609 | 5.9531 | 6.9452 | 7.9374 | 8.9296 | 1.3955 |
| 37 | 0.9921 | 1.9843 | 2.9764 | 3.9685 | 4.9606 | 5.9528 | 6.9449 | 7.9370 | 8.9292 | 1.3955 |
| 38 | 0.9921 | 1.9842 | 2.9762 | 3.9683 | 4.9604 | 5.9525 | 6.9446 | 7.9367 | 8.9287 | 1.3955 |
| 39 | 0.9920 | 1.9841 | 2.9761 | 3.9681 | 4.9602 | 5.9522 | 6.9443 | 7.9363 | 8.9283 | 1.3954 |
| 40 | 0.9920 | 1.9840 | 2.9760 | 3.9680 | 4.9600 | 5.9519 | 6.9439 | 7.9359 | 8.9279 | 1.3954 |
| 41 | 0.9919 | 1.9839 | 2.9758 | 3.9678 | 4.9597 | 5.9517 | 6.9436 | 7.9355 | 8.9275 | 1.3954 |
| 42 | 0.9919 | 1.9838 | 2.9757 | 3.9676 | 4.9595 | 5.9514 | 6.9433 | 7.9352 | 8.9270 | 1.3953 |
| 43 | 0.9918 | 1.9837 | 2.9755 | 3.9674 | 4.9592 | 5.9511 | 6.9429 | 7.9348 | 8.9266 | 1.3953 |
| 44 | 0.9918 | 1.9836 | 2.9754 | 3.9672 | 4.9590 | 5.9508 | 6.9426 | 7.9344 | 8.9262 | 1.3953 |
| 45 | 0.9918 | 1.9835 | 2.9753 | 3.9670 | 4.9588 | 5.9505 | 6.9423 | 7.9340 | 8.9258 | 1.3952 |
| 46 | 0.9917 | 1.9834 | 2.9751 | 3.9668 | 4.9585 | 5.9502 | 6.9419 | 7.9336 | 8.9253 | 1.3952 |
| 47 | 0.9917 | 1.9833 | 2.9750 | 3.9666 | 4.9583 | 5.9499 | 6.9416 | 7.9332 | 8.9249 | 1.3952 |
| 48 | 0.9916 | 1.9832 | 2.9748 | 3.9664 | 4.9580 | 5.9496 | 6.9412 | 7.9329 | 8.9245 | 1.3951 |
| 49 | 0.9916 | 1.9831 | 2.9747 | 3.9662 | 4.9578 | 5.9494 | 6.9409 | 7.9325 | 8.9240 | 1.3951 |
| 50 | 0.9915 | 1.9830 | 2.9745 | 3.9660 | 4.9576 | 5.9491 | 6.9406 | 7.9321 | 8.9236 | 1.3951 |
| 51 | 0.9915 | 1.9829 | 2.9744 | 3.9658 | 4.9573 | 5.9488 | 6.9402 | 7.9317 | 8.9231 | 1.3950 |
| 52 | 0.9914 | 1.9828 | 2.9742 | 3.9656 | 4.9571 | 5.9485 | 6.9399 | 7.9313 | 8.9227 | 1.3950 |
| 53 | 0.9914 | 1.9827 | 2.9741 | 3.9654 | 4.9568 | 5.9482 | 6.9395 | 7.9309 | 8.9223 | 1.3950 |
| 54 | 0.9913 | 1.9826 | 2.9739 | 3.9653 | 4.9566 | 5.9479 | 6.9392 | 7.9305 | 8.9218 | 1.3949 |
| 55 | 0.9913 | 1.9825 | 2.9738 | 3.9651 | 4.9563 | 5.9476 | 6.9388 | 7.9301 | 8.9214 | 1.3949 |
| 56 | 0.9912 | 1.9824 | 2.9736 | 3.9649 | 4.9561 | 5.9473 | 6.9385 | 7.9297 | 8.9209 | 1.3949 |
| 57 | 0.9912 | 1.9823 | 2.9735 | 3.9647 | 4.9558 | 5.9470 | 6.9381 | 7.9293 | 8.9205 | 1.3948 |
| 58 | 0.9911 | 1.9822 | 2.9733 | 3.9645 | 4.9556 | 5.9467 | 6.9378 | 7.9289 | 8.9200 | 1.3948 |
| 59 | 0.9911 | 1.9821 | 2.9732 | 3.9643 | 4.9553 | 5.9464 | 6.9375 | 7.9285 | 8.9196 | 1.3948 |
| 60 | 0.9910 | 1.9820 | 2.9730 | 3.9641 | 4.9551 | 5.9461 | 6.9371 | 7.9281 | 8.9191 | 1.3947 |

| 4°     |        | HEIGHTS. |        |        |        |        |        |        |        | 97 |
|--------|--------|----------|--------|--------|--------|--------|--------|--------|--------|----|
| 1      | 2      | 3        | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
| 0.0695 | 0.1390 | 0.2085   | 0.2780 | 0.3474 | 0.4169 | 0.4864 | 0.5559 | 0.6254 | 0.0977 | 00 |
| 0.0698 | 0.1396 | 0.2093   | 0.2791 | 0.3489 | 0.4187 | 0.4884 | 0.5582 | 0.6280 | 0.0981 | 01 |
| 0.0701 | 0.1401 | 0.2102   | 0.2802 | 0.3503 | 0.4204 | 0.4904 | 0.5605 | 0.6306 | 0.0985 | 02 |
| 0.0704 | 0.1407 | 0.2111   | 0.2814 | 0.3518 | 0.4221 | 0.4925 | 0.5628 | 0.6332 | 0.0989 | 03 |
| 0.0706 | 0.1413 | 0.2119   | 0.2826 | 0.3532 | 0.4238 | 0.4945 | 0.5651 | 0.6358 | 0.0993 | 04 |
| 0.0709 | 0.1419 | 0.2128   | 0.2837 | 0.3546 | 0.4256 | 0.4965 | 0.5674 | 0.6384 | 0.0997 | 05 |
| 0.0712 | 0.1424 | 0.2136   | 0.2848 | 0.3561 | 0.4273 | 0.4985 | 0.5697 | 0.6409 | 0.1001 | 06 |
| 0.0715 | 0.1430 | 0.2145   | 0.2860 | 0.3575 | 0.4290 | 0.5005 | 0.5720 | 0.6435 | 0.1005 | 07 |
| 0.0718 | 0.1436 | 0.2154   | 0.2872 | 0.3589 | 0.4307 | 0.5025 | 0.5743 | 0.6461 | 0.1009 | 08 |
| 0.0721 | 0.1442 | 0.2162   | 0.2883 | 0.3604 | 0.4325 | 0.5045 | 0.5766 | 0.6487 | 0.1013 | 09 |
| 0.0724 | 0.1447 | 0.2171   | 0.2894 | 0.3618 | 0.4342 | 0.5065 | 0.5789 | 0.6513 | 0.1017 | 10 |
| 0.0727 | 0.1453 | 0.2180   | 0.2906 | 0.3633 | 0.4359 | 0.5086 | 0.5812 | 0.6539 | 0.1021 | 11 |
| 0.0729 | 0.1459 | 0.2188   | 0.2918 | 0.3647 | 0.4376 | 0.5106 | 0.5835 | 0.6565 | 0.1025 | 12 |
| 0.0732 | 0.1465 | 0.2197   | 0.2929 | 0.3661 | 0.4394 | 0.5126 | 0.5858 | 0.6591 | 0.1029 | 13 |
| 0.0735 | 0.1470 | 0.2205   | 0.2940 | 0.3676 | 0.4411 | 0.5146 | 0.5881 | 0.6616 | 0.1033 | 14 |
| 0.0738 | 0.1476 | 0.2214   | 0.2952 | 0.3690 | 0.4428 | 0.5166 | 0.5904 | 0.6642 | 0.1037 | 15 |
| 0.0741 | 0.1482 | 0.2223   | 0.2964 | 0.3704 | 0.4445 | 0.5186 | 0.5927 | 0.6668 | 0.1041 | 16 |
| 0.0744 | 0.1488 | 0.2231   | 0.2975 | 0.3719 | 0.4463 | 0.5206 | 0.5950 | 0.6694 | 0.1046 | 17 |
| 0.0747 | 0.1493 | 0.2240   | 0.2986 | 0.3733 | 0.4480 | 0.5226 | 0.5973 | 0.6720 | 0.1050 | 18 |
| 0.0749 | 0.1499 | 0.2248   | 0.2998 | 0.3747 | 0.4497 | 0.5246 | 0.5996 | 0.6746 | 0.1054 | 19 |
| 0.0752 | 0.1505 | 0.2257   | 0.3010 | 0.3762 | 0.4514 | 0.5266 | 0.6019 | 0.6772 | 0.1058 | 20 |
| 0.0755 | 0.1510 | 0.2266   | 0.3021 | 0.3776 | 0.4531 | 0.5286 | 0.6042 | 0.6797 | 0.1062 | 21 |
| 0.0758 | 0.1516 | 0.2274   | 0.3032 | 0.3791 | 0.4549 | 0.5307 | 0.6065 | 0.6823 | 0.1066 | 22 |
| 0.0761 | 0.1522 | 0.2283   | 0.3044 | 0.3805 | 0.4566 | 0.5327 | 0.6088 | 0.6849 | 0.1070 | 23 |
| 0.0764 | 0.1528 | 0.2292   | 0.3056 | 0.3819 | 0.4583 | 0.5347 | 0.6111 | 0.6875 | 0.1074 | 24 |
| 0.0767 | 0.1533 | 0.2300   | 0.3067 | 0.3834 | 0.4600 | 0.5367 | 0.6134 | 0.6900 | 0.1078 | 25 |
| 0.0770 | 0.1539 | 0.2309   | 0.3078 | 0.3848 | 0.4618 | 0.5387 | 0.6157 | 0.6926 | 0.1082 | 26 |
| 0.0772 | 0.1545 | 0.2317   | 0.3090 | 0.3862 | 0.4635 | 0.5407 | 0.6180 | 0.6952 | 0.1086 | 27 |
| 0.0775 | 0.1551 | 0.2326   | 0.3101 | 0.3877 | 0.4652 | 0.5427 | 0.6203 | 0.6978 | 0.1090 | 28 |
| 0.0778 | 0.1556 | 0.2335   | 0.3113 | 0.3891 | 0.4669 | 0.5447 | 0.6226 | 0.7004 | 0.1094 | 29 |
| 0.0781 | 0.1562 | 0.2343   | 0.3124 | 0.3905 | 0.4687 | 0.5467 | 0.6249 | 0.7030 | 0.1098 | 30 |
| 0.0784 | 0.1568 | 0.2352   | 0.3136 | 0.3920 | 0.4703 | 0.5487 | 0.6271 | 0.7055 | 0.1102 | 31 |
| 0.0787 | 0.1574 | 0.2360   | 0.3147 | 0.3934 | 0.4721 | 0.5508 | 0.6294 | 0.7081 | 0.1107 | 32 |
| 0.0790 | 0.1579 | 0.2369   | 0.3159 | 0.3948 | 0.4738 | 0.5528 | 0.6318 | 0.7107 | 0.1111 | 33 |
| 0.0793 | 0.1585 | 0.2378   | 0.3170 | 0.3963 | 0.4755 | 0.5548 | 0.6340 | 0.7133 | 0.1115 | 34 |
| 0.0795 | 0.1591 | 0.2386   | 0.3182 | 0.3977 | 0.4772 | 0.5568 | 0.6363 | 0.7159 | 0.1119 | 35 |
| 0.0798 | 0.1597 | 0.2395   | 0.3193 | 0.3991 | 0.4790 | 0.5588 | 0.6386 | 0.7185 | 0.1123 | 36 |
| 0.0801 | 0.1602 | 0.2403   | 0.3204 | 0.4007 | 0.4807 | 0.5608 | 0.6409 | 0.7210 | 0.1127 | 37 |
| 0.0804 | 0.1608 | 0.2412   | 0.3216 | 0.4020 | 0.4824 | 0.5628 | 0.6432 | 0.7236 | 0.1131 | 38 |
| 0.0807 | 0.1614 | 0.2421   | 0.3228 | 0.4034 | 0.4841 | 0.5648 | 0.6455 | 0.7262 | 0.1135 | 39 |
| 0.0810 | 0.1620 | 0.2429   | 0.3239 | 0.4049 | 0.4859 | 0.5668 | 0.6478 | 0.7288 | 0.1139 | 40 |
| 0.0813 | 0.1625 | 0.2438   | 0.3250 | 0.4063 | 0.4876 | 0.5688 | 0.6501 | 0.7313 | 0.1143 | 41 |
| 0.0815 | 0.1631 | 0.2446   | 0.3262 | 0.4077 | 0.4893 | 0.5708 | 0.6524 | 0.7339 | 0.1147 | 42 |
| 0.0818 | 0.1637 | 0.2455   | 0.3273 | 0.4092 | 0.4910 | 0.5728 | 0.6546 | 0.7365 | 0.1151 | 43 |
| 0.0821 | 0.1642 | 0.2464   | 0.3285 | 0.4106 | 0.4927 | 0.5748 | 0.6570 | 0.7391 | 0.1155 | 44 |
| 0.0824 | 0.1648 | 0.2472   | 0.3296 | 0.4120 | 0.4945 | 0.5768 | 0.6593 | 0.7417 | 0.1159 | 45 |
| 0.0827 | 0.1654 | 0.2481   | 0.3308 | 0.4135 | 0.4961 | 0.5788 | 0.6615 | 0.7442 | 0.1163 | 46 |
| 0.0830 | 0.1660 | 0.2489   | 0.3319 | 0.4149 | 0.4979 | 0.5809 | 0.6638 | 0.7468 | 0.1167 | 47 |
| 0.0833 | 0.1665 | 0.2498   | 0.3331 | 0.4163 | 0.4996 | 0.5829 | 0.6662 | 0.7494 | 0.1171 | 48 |
| 0.0836 | 0.1671 | 0.2507   | 0.3342 | 0.4178 | 0.5013 | 0.5849 | 0.6684 | 0.7520 | 0.1176 | 49 |
| 0.0838 | 0.1677 | 0.2515   | 0.3354 | 0.4192 | 0.5030 | 0.5869 | 0.6707 | 0.7546 | 0.1180 | 50 |
| 0.0841 | 0.1683 | 0.2524   | 0.3365 | 0.4206 | 0.5048 | 0.5889 | 0.6730 | 0.7572 | 0.1184 | 51 |
| 0.0844 | 0.1688 | 0.2532   | 0.3376 | 0.4221 | 0.5065 | 0.5909 | 0.6753 | 0.7597 | 0.1188 | 52 |
| 0.0847 | 0.1694 | 0.2541   | 0.3388 | 0.4235 | 0.5082 | 0.5929 | 0.6776 | 0.7623 | 0.1192 | 53 |
| 0.0850 | 0.1700 | 0.2549   | 0.3399 | 0.4249 | 0.5099 | 0.5949 | 0.6798 | 0.7648 | 0.1196 | 54 |
| 0.0853 | 0.1705 | 0.2558   | 0.3411 | 0.4264 | 0.5116 | 0.5969 | 0.6822 | 0.7674 | 0.1200 | 55 |
| 0.0856 | 0.1711 | 0.2567   | 0.3422 | 0.4278 | 0.5134 | 0.5989 | 0.6845 | 0.7700 | 0.1204 | 56 |
| 0.0858 | 0.1717 | 0.2575   | 0.3434 | 0.4292 | 0.5150 | 0.6009 | 0.6867 | 0.7726 | 0.1208 | 57 |
| 0.0861 | 0.1723 | 0.2584   | 0.3445 | 0.4306 | 0.5168 | 0.6029 | 0.6890 | 0.7752 | 0.1212 | 58 |
| 0.0864 | 0.1728 | 0.2593   | 0.3457 | 0.4321 | 0.5185 | 0.6049 | 0.6914 | 0.7778 | 0.1216 | 59 |
| 0.0867 | 0.1734 | 0.2601   | 0.3468 | 0.4335 | 0.5202 | 0.6069 | 0.6936 | 0.7803 | 0.1220 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10     |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9910 | 1.0820 | 2.9730 | 3.9641 | 4.9551 | 5.9461 | 6.9371 | 7.9281 | 8.9191 | 1.3947 |
| 01 | 0.9910 | 1.0819 | 2.9729 | 3.9639 | 4.9548 | 5.9458 | 6.9367 | 7.9277 | 8.9187 | 1.3947 |
| 02 | 0.9909 | 1.0818 | 2.9727 | 3.9636 | 4.9546 | 5.9455 | 6.9364 | 7.9273 | 8.9182 | 1.3946 |
| 03 | 0.9909 | 1.0817 | 2.9726 | 3.9634 | 4.9543 | 5.9452 | 6.9360 | 7.9269 | 8.9177 | 1.3946 |
| 04 | 0.9908 | 1.0816 | 2.9724 | 3.9632 | 4.9541 | 5.9449 | 6.9357 | 7.9265 | 8.9173 | 1.3946 |
| 05 | 0.9908 | 1.0815 | 2.9723 | 3.9630 | 4.9538 | 5.9446 | 6.9353 | 7.9261 | 8.9168 | 1.3945 |
| 06 | 0.9907 | 1.0814 | 2.9721 | 3.9628 | 4.9535 | 5.9442 | 6.9349 | 7.9257 | 8.9164 | 1.3945 |
| 07 | 0.9907 | 1.0813 | 2.9720 | 3.9626 | 4.9533 | 5.9439 | 6.9346 | 7.9252 | 8.9159 | 1.3944 |
| 08 | 0.9906 | 1.0812 | 2.9718 | 3.9624 | 4.9530 | 5.9436 | 6.9342 | 7.9248 | 8.9154 | 1.3944 |
| 09 | 0.9906 | 1.0811 | 2.9717 | 3.9622 | 4.9528 | 5.9433 | 6.9339 | 7.9244 | 8.9150 | 1.3944 |
| 10 | 0.9905 | 1.0810 | 2.9715 | 3.9620 | 4.9525 | 5.9430 | 6.9335 | 7.9240 | 8.9145 | 1.3943 |
| 11 | 0.9904 | 1.0809 | 2.9713 | 3.9618 | 4.9522 | 5.9427 | 6.9331 | 7.9236 | 8.9140 | 1.3943 |
| 12 | 0.9904 | 1.0808 | 2.9712 | 3.9616 | 4.9520 | 5.9424 | 6.9328 | 7.9232 | 8.9136 | 1.3942 |
| 13 | 0.9903 | 1.0807 | 2.9710 | 3.9614 | 4.9517 | 5.9421 | 6.9324 | 7.9227 | 8.9131 | 1.3942 |
| 14 | 0.9903 | 1.0806 | 2.9709 | 3.9612 | 4.9515 | 5.9417 | 6.9320 | 7.9223 | 8.9126 | 1.3941 |
| 15 | 0.9902 | 1.0805 | 2.9707 | 3.9610 | 4.9512 | 5.9414 | 6.9317 | 7.9219 | 8.9121 | 1.3941 |
| 16 | 0.9902 | 1.0804 | 2.9706 | 3.9607 | 4.9509 | 5.9411 | 6.9313 | 7.9215 | 8.9117 | 1.3941 |
| 17 | 0.9901 | 1.0803 | 2.9704 | 3.9605 | 4.9507 | 5.9408 | 6.9309 | 7.9211 | 8.9112 | 1.3940 |
| 18 | 0.9901 | 1.0802 | 2.9702 | 3.9603 | 4.9504 | 5.9405 | 6.9306 | 7.9206 | 8.9107 | 1.3940 |
| 19 | 0.9900 | 1.0801 | 2.9701 | 3.9601 | 4.9501 | 5.9402 | 6.9302 | 7.9202 | 8.9102 | 1.3940 |
| 20 | 0.9900 | 1.0799 | 2.9699 | 3.9599 | 4.9499 | 5.9398 | 6.9298 | 7.9198 | 8.9098 | 1.3939 |
| 21 | 0.9899 | 1.0798 | 2.9698 | 3.9597 | 4.9496 | 5.9395 | 6.9294 | 7.9193 | 8.9093 | 1.3939 |
| 22 | 0.9899 | 1.0797 | 2.9696 | 3.9595 | 4.9493 | 5.9392 | 6.9290 | 7.9189 | 8.9088 | 1.3938 |
| 23 | 0.9898 | 1.0796 | 2.9694 | 3.9592 | 4.9490 | 5.9389 | 6.9287 | 7.9185 | 8.9083 | 1.3938 |
| 24 | 0.9898 | 1.0795 | 2.9693 | 3.9590 | 4.9488 | 5.9385 | 6.9283 | 7.9180 | 8.9078 | 1.3938 |
| 25 | 0.9897 | 1.0794 | 2.9691 | 3.9588 | 4.9485 | 5.9382 | 6.9279 | 7.9176 | 8.9073 | 1.3937 |
| 26 | 0.9896 | 1.0793 | 2.9689 | 3.9586 | 4.9482 | 5.9379 | 6.9275 | 7.9172 | 8.9068 | 1.3937 |
| 27 | 0.9896 | 1.0792 | 2.9688 | 3.9584 | 4.9480 | 5.9375 | 6.9271 | 7.9167 | 8.9063 | 1.3936 |
| 28 | 0.9895 | 1.0791 | 2.9686 | 3.9581 | 4.9477 | 5.9372 | 6.9268 | 7.9163 | 8.9058 | 1.3936 |
| 29 | 0.9895 | 1.0790 | 2.9684 | 3.9579 | 4.9474 | 5.9369 | 6.9264 | 7.9159 | 8.9053 | 1.3936 |
| 30 | 0.9894 | 1.0789 | 2.9683 | 3.9577 | 4.9471 | 5.9366 | 6.9260 | 7.9154 | 8.9048 | 1.3935 |
| 31 | 0.9894 | 1.0787 | 2.9681 | 3.9575 | 4.9469 | 5.9362 | 6.9256 | 7.9150 | 8.9043 | 1.3935 |
| 32 | 0.9893 | 1.0786 | 2.9679 | 3.9573 | 4.9466 | 5.9359 | 6.9252 | 7.9145 | 8.9038 | 1.3934 |
| 33 | 0.9893 | 1.0783 | 2.9678 | 3.9570 | 4.9463 | 5.9355 | 6.9248 | 7.9141 | 8.9033 | 1.3934 |
| 34 | 0.9892 | 1.0784 | 2.9676 | 3.9568 | 4.9460 | 5.9352 | 6.9244 | 7.9136 | 8.9028 | 1.3934 |
| 35 | 0.9891 | 1.0783 | 2.9674 | 3.9566 | 4.9457 | 5.9349 | 6.9240 | 7.9132 | 8.9023 | 1.3933 |
| 36 | 0.9891 | 1.0782 | 2.9673 | 3.9564 | 4.9454 | 5.9345 | 6.9236 | 7.9127 | 8.9018 | 1.3933 |
| 37 | 0.9890 | 1.0781 | 2.9671 | 3.9561 | 4.9452 | 5.9342 | 6.9232 | 7.9123 | 8.9013 | 1.3932 |
| 38 | 0.9890 | 1.0780 | 2.9669 | 3.9559 | 4.9449 | 5.9339 | 6.9228 | 7.9118 | 8.9008 | 1.3932 |
| 39 | 0.9889 | 1.0778 | 2.9668 | 3.9557 | 4.9446 | 5.9335 | 6.9224 | 7.9114 | 8.9003 | 1.3932 |
| 40 | 0.9889 | 1.0777 | 2.9666 | 3.9555 | 4.9443 | 5.9332 | 6.9220 | 7.9109 | 8.9098 | 1.3931 |
| 41 | 0.9888 | 1.0776 | 2.9664 | 3.9552 | 4.9440 | 5.9328 | 6.9216 | 7.9104 | 8.9093 | 1.3931 |
| 42 | 0.9887 | 1.0775 | 2.9662 | 3.9550 | 4.9437 | 5.9325 | 6.9212 | 7.9100 | 8.9087 | 1.3930 |
| 43 | 0.9887 | 1.0774 | 2.9661 | 3.9548 | 4.9435 | 5.9321 | 6.9208 | 7.9095 | 8.9082 | 1.3930 |
| 44 | 0.9886 | 1.0773 | 2.9659 | 3.9545 | 4.9432 | 5.9318 | 6.9204 | 7.9091 | 8.9077 | 1.3930 |
| 45 | 0.9886 | 1.0772 | 2.9657 | 3.9543 | 4.9429 | 5.9315 | 6.9200 | 7.9086 | 8.9072 | 1.3929 |
| 46 | 0.9885 | 1.0770 | 2.9656 | 3.9541 | 4.9426 | 5.9311 | 6.9196 | 7.9081 | 8.9067 | 1.3929 |
| 47 | 0.9885 | 1.0769 | 2.9654 | 3.9538 | 4.9423 | 5.9308 | 6.9192 | 7.9077 | 8.9061 | 1.3928 |
| 48 | 0.9884 | 1.0768 | 2.9652 | 3.9536 | 4.9420 | 5.9304 | 6.9188 | 7.9072 | 8.9056 | 1.3928 |
| 49 | 0.9883 | 1.0767 | 2.9650 | 3.9534 | 4.9417 | 5.9300 | 6.9184 | 7.9067 | 8.9051 | 1.3928 |
| 50 | 0.9883 | 1.0766 | 2.9649 | 3.9531 | 4.9414 | 5.9297 | 6.9180 | 7.9063 | 8.9046 | 1.3927 |
| 51 | 0.9882 | 1.0765 | 2.9647 | 3.9529 | 4.9411 | 5.9294 | 6.9176 | 7.9058 | 8.9040 | 1.3927 |
| 52 | 0.9882 | 1.0763 | 2.9645 | 3.9527 | 4.9408 | 5.9290 | 6.9172 | 7.9053 | 8.9035 | 1.3926 |
| 53 | 0.9881 | 1.0762 | 2.9643 | 3.9524 | 4.9405 | 5.9286 | 6.9167 | 7.9048 | 8.9030 | 1.3926 |
| 54 | 0.9880 | 1.0761 | 2.9641 | 3.9522 | 4.9402 | 5.9283 | 6.9163 | 7.9044 | 8.9024 | 1.3926 |
| 55 | 0.9880 | 1.0760 | 2.9640 | 3.9519 | 4.9399 | 5.9279 | 6.9159 | 7.9039 | 8.9019 | 1.3925 |
| 56 | 0.9879 | 1.0759 | 2.9638 | 3.9517 | 4.9396 | 5.9276 | 6.9155 | 7.9034 | 8.9013 | 1.3925 |
| 57 | 0.9879 | 1.0757 | 2.9636 | 3.9515 | 4.9393 | 5.9272 | 6.9151 | 7.9029 | 8.9008 | 1.3924 |
| 58 | 0.9878 | 1.0756 | 2.9634 | 3.9512 | 4.9390 | 5.9268 | 6.9147 | 7.9025 | 8.9003 | 1.3924 |
| 59 | 0.9877 | 1.0755 | 2.9632 | 3.9510 | 4.9387 | 5.9265 | 6.9142 | 7.9020 | 8.8997 | 1.3924 |
| 60 | 0.9877 | 1.0754 | 2.9631 | 3.9508 | 4.9384 | 5.9261 | 6.9138 | 7.9015 | 8.8992 | 1.3923 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | /  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0867 | 0.1734 | 0.2601 | 0.3468 | 0.4335 | 0.5202 | 0.6069 | 0.6936 | 0.7803 | 0.1220 | 00 |
| 0.0870 | 0.1740 | 0.2610 | 0.3480 | 0.4349 | 0.5219 | 0.6089 | 0.6959 | 0.7829 | 0.1224 | 01 |
| 0.0873 | 0.1745 | 0.2618 | 0.3491 | 0.4364 | 0.5236 | 0.6109 | 0.6982 | 0.7854 | 0.1228 | 02 |
| 0.0876 | 0.1751 | 0.2627 | 0.3502 | 0.4378 | 0.5254 | 0.6129 | 0.7005 | 0.7880 | 0.1232 | 03 |
| 0.0878 | 0.1757 | 0.2635 | 0.3514 | 0.4392 | 0.5271 | 0.6149 | 0.7028 | 0.7906 | 0.1236 | 04 |
| 0.0881 | 0.1763 | 0.2644 | 0.3525 | 0.4407 | 0.5288 | 0.6169 | 0.7050 | 0.7932 | 0.1240 | 05 |
| 0.0884 | 0.1768 | 0.2653 | 0.3537 | 0.4421 | 0.5305 | 0.6189 | 0.7074 | 0.7958 | 0.1244 | 06 |
| 0.0887 | 0.1774 | 0.2661 | 0.3548 | 0.4435 | 0.5322 | 0.6209 | 0.7096 | 0.7983 | 0.1248 | 07 |
| 0.0890 | 0.1780 | 0.2670 | 0.3560 | 0.4450 | 0.5339 | 0.6229 | 0.7119 | 0.8009 | 0.1253 | 08 |
| 0.0893 | 0.1786 | 0.2678 | 0.3571 | 0.4464 | 0.5357 | 0.6249 | 0.7142 | 0.8035 | 0.1257 | 09 |
| 0.0896 | 0.1791 | 0.2687 | 0.3582 | 0.4478 | 0.5374 | 0.6269 | 0.7165 | 0.8060 | 0.1261 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0898 | 0.1797 | 0.2695 | 0.3594 | 0.4492 | 0.5391 | 0.6289 | 0.7188 | 0.8086 | 0.1265 | 11 |
| 0.0901 | 0.1803 | 0.2704 | 0.3605 | 0.4507 | 0.5408 | 0.6309 | 0.7211 | 0.8112 | 0.1269 | 12 |
| 0.0904 | 0.1808 | 0.2713 | 0.3617 | 0.4521 | 0.5425 | 0.6329 | 0.7234 | 0.8138 | 0.1273 | 13 |
| 0.0907 | 0.1814 | 0.2721 | 0.3628 | 0.4535 | 0.5442 | 0.6349 | 0.7256 | 0.8163 | 0.1277 | 14 |
| 0.0910 | 0.1820 | 0.2730 | 0.3640 | 0.4550 | 0.5459 | 0.6369 | 0.7279 | 0.8189 | 0.1281 | 15 |
| 0.0913 | 0.1826 | 0.2738 | 0.3651 | 0.4564 | 0.5477 | 0.6389 | 0.7302 | 0.8215 | 0.1285 | 16 |
| 0.0916 | 0.1831 | 0.2747 | 0.3662 | 0.4578 | 0.5494 | 0.6409 | 0.7325 | 0.8240 | 0.1289 | 17 |
| 0.0918 | 0.1837 | 0.2755 | 0.3674 | 0.4592 | 0.5511 | 0.6429 | 0.7348 | 0.8266 | 0.1293 | 18 |
| 0.0921 | 0.1843 | 0.2764 | 0.3685 | 0.4607 | 0.5528 | 0.6449 | 0.7371 | 0.8292 | 0.1297 | 19 |
| 0.0924 | 0.1848 | 0.2773 | 0.3697 | 0.4621 | 0.5545 | 0.6469 | 0.7394 | 0.8318 | 0.1301 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0927 | 0.1854 | 0.2781 | 0.3708 | 0.4635 | 0.5562 | 0.6489 | 0.7416 | 0.8343 | 0.1305 | 21 |
| 0.0930 | 0.1860 | 0.2790 | 0.3720 | 0.4649 | 0.5579 | 0.6509 | 0.7439 | 0.8369 | 0.1309 | 22 |
| 0.0933 | 0.1865 | 0.2798 | 0.3731 | 0.4664 | 0.5596 | 0.6529 | 0.7462 | 0.8394 | 0.1313 | 23 |
| 0.0936 | 0.1871 | 0.2807 | 0.3742 | 0.4678 | 0.5614 | 0.6549 | 0.7485 | 0.8420 | 0.1317 | 24 |
| 0.0938 | 0.1877 | 0.2815 | 0.3754 | 0.4692 | 0.5631 | 0.6569 | 0.7507 | 0.8446 | 0.1321 | 25 |
| 0.0941 | 0.1883 | 0.2824 | 0.3765 | 0.4706 | 0.5648 | 0.6589 | 0.7530 | 0.8472 | 0.1326 | 26 |
| 0.0944 | 0.1888 | 0.2833 | 0.3777 | 0.4721 | 0.5665 | 0.6609 | 0.7553 | 0.8498 | 0.1330 | 27 |
| 0.0947 | 0.1894 | 0.2841 | 0.3788 | 0.4735 | 0.5682 | 0.6629 | 0.7576 | 0.8523 | 0.1334 | 28 |
| 0.0950 | 0.1900 | 0.2850 | 0.3800 | 0.4749 | 0.5699 | 0.6649 | 0.7599 | 0.8549 | 0.1338 | 29 |
| 0.0953 | 0.1905 | 0.2858 | 0.3811 | 0.4764 | 0.5716 | 0.6669 | 0.7622 | 0.8574 | 0.1342 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0956 | 0.1911 | 0.2867 | 0.3822 | 0.4778 | 0.5734 | 0.6689 | 0.7645 | 0.8600 | 0.1346 | 31 |
| 0.0958 | 0.1917 | 0.2875 | 0.3834 | 0.4792 | 0.5751 | 0.6709 | 0.7667 | 0.8626 | 0.1350 | 32 |
| 0.0961 | 0.1923 | 0.2884 | 0.3845 | 0.4806 | 0.5768 | 0.6729 | 0.7690 | 0.8652 | 0.1354 | 33 |
| 0.0964 | 0.1928 | 0.2892 | 0.3856 | 0.4820 | 0.5785 | 0.6749 | 0.7713 | 0.8677 | 0.1358 | 34 |
| 0.0967 | 0.1934 | 0.2901 | 0.3868 | 0.4835 | 0.5802 | 0.6769 | 0.7736 | 0.8703 | 0.1362 | 35 |
| 0.0970 | 0.1940 | 0.2909 | 0.3879 | 0.4849 | 0.5819 | 0.6789 | 0.7759 | 0.8728 | 0.1366 | 36 |
| 0.0973 | 0.1945 | 0.2918 | 0.3891 | 0.4863 | 0.5836 | 0.6809 | 0.7782 | 0.8754 | 0.1370 | 37 |
| 0.0976 | 0.1951 | 0.2927 | 0.3902 | 0.4878 | 0.5853 | 0.6829 | 0.7804 | 0.8780 | 0.1374 | 38 |
| 0.0978 | 0.1957 | 0.2935 | 0.3914 | 0.4892 | 0.5870 | 0.6849 | 0.7827 | 0.8806 | 0.1378 | 39 |
| 0.0981 | 0.1962 | 0.2944 | 0.3925 | 0.4906 | 0.5887 | 0.6869 | 0.7850 | 0.8831 | 0.1382 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.0984 | 0.1968 | 0.2952 | 0.3936 | 0.4920 | 0.5905 | 0.6889 | 0.7873 | 0.8857 | 0.1389 | 41 |
| 0.0987 | 0.1974 | 0.2961 | 0.3948 | 0.4935 | 0.5921 | 0.6908 | 0.7895 | 0.8882 | 0.1390 | 42 |
| 0.0990 | 0.1979 | 0.2969 | 0.3959 | 0.4948 | 0.5938 | 0.6928 | 0.7918 | 0.8907 | 0.1395 | 43 |
| 0.0993 | 0.1985 | 0.2978 | 0.3970 | 0.4963 | 0.5956 | 0.6948 | 0.7941 | 0.8933 | 0.1399 | 44 |
| 0.0995 | 0.1991 | 0.2986 | 0.3982 | 0.4977 | 0.5973 | 0.6968 | 0.7963 | 0.8959 | 0.1403 | 45 |
| 0.0998 | 0.1997 | 0.2995 | 0.3993 | 0.4991 | 0.5990 | 0.6988 | 0.7986 | 0.8985 | 0.1407 | 46 |
| 0.1001 | 0.2002 | 0.3003 | 0.4004 | 0.5006 | 0.6007 | 0.7008 | 0.8009 | 0.9010 | 0.1411 | 47 |
| 0.1004 | 0.2008 | 0.3012 | 0.4016 | 0.5020 | 0.6024 | 0.7028 | 0.8032 | 0.9036 | 0.1415 | 48 |
| 0.1007 | 0.2014 | 0.3020 | 0.4027 | 0.5034 | 0.6041 | 0.7048 | 0.8054 | 0.9061 | 0.1419 | 49 |
| 0.1010 | 0.2019 | 0.3029 | 0.4039 | 0.5049 | 0.6058 | 0.7068 | 0.8078 | 0.9087 | 0.1423 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1013 | 0.2025 | 0.3038 | 0.4050 | 0.5063 | 0.6075 | 0.7088 | 0.8100 | 0.9113 | 0.1427 | 51 |
| 0.1015 | 0.2031 | 0.3046 | 0.4062 | 0.5077 | 0.6092 | 0.7108 | 0.8123 | 0.9139 | 0.1431 | 52 |
| 0.1018 | 0.2036 | 0.3055 | 0.4073 | 0.5091 | 0.6109 | 0.7127 | 0.8146 | 0.9164 | 0.1435 | 53 |
| 0.1021 | 0.2042 | 0.3063 | 0.4084 | 0.5105 | 0.6126 | 0.7147 | 0.8168 | 0.9189 | 0.1439 | 54 |
| 0.1024 | 0.2048 | 0.3072 | 0.4096 | 0.5119 | 0.6143 | 0.7167 | 0.8191 | 0.9215 | 0.1443 | 55 |
| 0.1027 | 0.2053 | 0.3080 | 0.4107 | 0.5134 | 0.6160 | 0.7187 | 0.8214 | 0.9240 | 0.1447 | 56 |
| 0.1030 | 0.2059 | 0.3089 | 0.4118 | 0.5148 | 0.6177 | 0.7207 | 0.8237 | 0.9266 | 0.1451 | 57 |
| 0.1032 | 0.2065 | 0.3097 | 0.4130 | 0.5162 | 0.6194 | 0.7227 | 0.8259 | 0.9292 | 0.1455 | 58 |
| 0.1035 | 0.2071 | 0.3106 | 0.4141 | 0.5176 | 0.6212 | 0.7247 | 0.8282 | 0.9318 | 0.1459 | 59 |
| 0.1038 | 0.2076 | 0.3114 | 0.4153 | 0.5191 | 0.6229 | 0.7267 | 0.8305 | 0.9343 | 0.1463 | 60 |

[illegible]

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1038 | 0.2076 | 0.3114 | 0.4153 | 0.5191 | 0.6229 | 0.7267 | 0.8305 | 0.9343 | 0.1463 | 00 |
| 0.1041 | 0.2082 | 0.3123 | 0.4164 | 0.5205 | 0.6246 | 0.7287 | 0.8327 | 0.9368 | 0.1467 | 01 |
| 0.1044 | 0.2088 | 0.3131 | 0.4175 | 0.5219 | 0.6263 | 0.7307 | 0.8350 | 0.9394 | 0.1471 | 02 |
| 0.1047 | 0.2093 | 0.3140 | 0.4186 | 0.5233 | 0.6280 | 0.7326 | 0.8373 | 0.9419 | 0.1476 | 03 |
| 0.1049 | 0.2099 | 0.3148 | 0.4198 | 0.5247 | 0.6297 | 0.7346 | 0.8396 | 0.9445 | 0.1480 | 04 |
| 0.1052 | 0.2105 | 0.3157 | 0.4209 | 0.5262 | 0.6314 | 0.7366 | 0.8418 | 0.9471 | 0.1484 | 05 |
| 0.1055 | 0.2110 | 0.3165 | 0.4220 | 0.5276 | 0.6331 | 0.7386 | 0.8441 | 0.9496 | 0.1488 | 06 |
| 0.1058 | 0.2116 | 0.3174 | 0.4232 | 0.5290 | 0.6348 | 0.7406 | 0.8464 | 0.9522 | 0.1492 | 07 |
| 0.1061 | 0.2122 | 0.3182 | 0.4243 | 0.5304 | 0.6365 | 0.7426 | 0.8486 | 0.9547 | 0.1496 | 08 |
| 0.1064 | 0.2127 | 0.3191 | 0.4255 | 0.5318 | 0.6382 | 0.7446 | 0.8509 | 0.9573 | 0.1500 | 09 |
| 0.1067 | 0.2133 | 0.3200 | 0.4266 | 0.5333 | 0.6399 | 0.7466 | 0.8532 | 0.9599 | 0.1504 | 10 |
| 0.1069 | 0.2139 | 0.3208 | 0.4277 | 0.5347 | 0.6416 | 0.7485 | 0.8554 | 0.9624 | 0.1508 | 11 |
| 0.1072 | 0.2144 | 0.3217 | 0.4389 | 0.5361 | 0.6433 | 0.7505 | 0.8577 | 0.9650 | 0.1512 | 12 |
| 0.1075 | 0.2150 | 0.3225 | 0.4300 | 0.5375 | 0.6450 | 0.7525 | 0.8600 | 0.9675 | 0.1516 | 13 |
| 0.1078 | 0.2156 | 0.3233 | 0.4311 | 0.5389 | 0.6467 | 0.7545 | 0.8622 | 0.9700 | 0.1520 | 14 |
| 0.1081 | 0.2161 | 0.3242 | 0.4323 | 0.5403 | 0.6484 | 0.7565 | 0.8645 | 0.9726 | 0.1524 | 15 |
| 0.1084 | 0.2167 | 0.3251 | 0.4334 | 0.5418 | 0.6501 | 0.7585 | 0.8668 | 0.9752 | 0.1528 | 16 |
| 0.1086 | 0.2173 | 0.3259 | 0.4346 | 0.5432 | 0.6518 | 0.7605 | 0.8691 | 0.9778 | 0.1532 | 17 |
| 0.1089 | 0.2178 | 0.3268 | 0.4357 | 0.5446 | 0.6535 | 0.7624 | 0.8714 | 0.9803 | 0.1536 | 18 |
| 0.1092 | 0.2184 | 0.3276 | 0.4368 | 0.5460 | 0.6552 | 0.7644 | 0.8736 | 0.9828 | 0.1540 | 19 |
| 0.1095 | 0.2190 | 0.3285 | 0.4380 | 0.5474 | 0.6569 | 0.7664 | 0.8759 | 0.9854 | 0.1544 | 20 |
| 0.1098 | 0.2195 | 0.3293 | 0.4391 | 0.5488 | 0.6586 | 0.7684 | 0.8782 | 0.9879 | 0.1548 | 21 |
| 0.1101 | 0.2201 | 0.3302 | 0.4402 | 0.5503 | 0.6603 | 0.7704 | 0.8804 | 0.9905 | 0.1552 | 22 |
| 0.1103 | 0.2207 | 0.3310 | 0.4414 | 0.5517 | 0.6620 | 0.7724 | 0.8827 | 0.9931 | 0.1556 | 23 |
| 0.1106 | 0.2212 | 0.3319 | 0.4425 | 0.5531 | 0.6637 | 0.7743 | 0.8850 | 0.9956 | 0.1561 | 24 |
| 0.1109 | 0.2218 | 0.3327 | 0.4436 | 0.5545 | 0.6654 | 0.7763 | 0.8872 | 0.9981 | 0.1565 | 25 |
| 0.1112 | 0.2224 | 0.3336 | 0.4448 | 0.5559 | 0.6671 | 0.7783 | 0.8895 | 1.0007 | 0.1569 | 26 |
| 0.1115 | 0.2229 | 0.3344 | 0.4459 | 0.5573 | 0.6688 | 0.7803 | 0.8918 | 1.0032 | 0.1573 | 27 |
| 0.1118 | 0.2235 | 0.3353 | 0.4470 | 0.5588 | 0.6705 | 0.7823 | 0.8940 | 1.0058 | 0.1577 | 28 |
| 0.1120 | 0.2241 | 0.3361 | 0.4481 | 0.5602 | 0.6722 | 0.7842 | 0.8963 | 1.0083 | 0.1581 | 29 |
| 0.1123 | 0.2246 | 0.3370 | 0.4493 | 0.5616 | 0.6739 | 0.7862 | 0.8986 | 1.0109 | 0.1585 | 30 |
| 0.1126 | 0.2252 | 0.3378 | 0.4504 | 0.5630 | 0.6756 | 0.7882 | 0.9008 | 1.0134 | 0.1589 | 31 |
| 0.1129 | 0.2258 | 0.3386 | 0.4515 | 0.5644 | 0.6773 | 0.7902 | 0.9031 | 1.0159 | 0.1593 | 32 |
| 0.1132 | 0.2263 | 0.3395 | 0.4527 | 0.5659 | 0.6790 | 0.7922 | 0.9054 | 1.0185 | 0.1597 | 33 |
| 0.1134 | 0.2269 | 0.3403 | 0.4538 | 0.5673 | 0.6807 | 0.7941 | 0.9076 | 1.0210 | 0.1601 | 34 |
| 0.1137 | 0.2275 | 0.3412 | 0.4549 | 0.5687 | 0.6824 | 0.7961 | 0.9098 | 1.0236 | 0.1605 | 35 |
| 0.1140 | 0.2280 | 0.3421 | 0.4561 | 0.5701 | 0.6841 | 0.8081 | 0.9121 | 1.0262 | 0.1609 | 36 |
| 0.1143 | 0.2286 | 0.3429 | 0.4572 | 0.5715 | 0.6858 | 0.8001 | 0.9144 | 1.0287 | 0.1613 | 37 |
| 0.1146 | 0.2292 | 0.3437 | 0.4583 | 0.5729 | 0.6875 | 0.8021 | 0.9166 | 1.0312 | 0.1617 | 38 |
| 0.1149 | 0.2297 | 0.3446 | 0.4594 | 0.5743 | 0.6892 | 0.8040 | 0.9189 | 1.0337 | 0.1621 | 39 |
| 0.1151 | 0.2303 | 0.3454 | 0.4606 | 0.5757 | 0.6909 | 0.8060 | 0.9212 | 1.0363 | 0.1625 | 40 |
| 0.1154 | 0.2309 | 0.3463 | 0.4617 | 0.5771 | 0.6926 | 0.8080 | 0.9234 | 1.0389 | 0.1629 | 41 |
| 0.1157 | 0.2314 | 0.3471 | 0.4628 | 0.5786 | 0.6943 | 0.8100 | 0.9257 | 1.0414 | 0.1633 | 42 |
| 0.1160 | 0.2320 | 0.3480 | 0.4640 | 0.5800 | 0.6960 | 0.8119 | 0.9279 | 1.0439 | 0.1637 | 43 |
| 0.1163 | 0.2326 | 0.3488 | 0.4651 | 0.5814 | 0.6977 | 0.8139 | 0.9302 | 1.0465 | 0.1641 | 44 |
| 0.1166 | 0.2331 | 0.3497 | 0.4662 | 0.5828 | 0.6994 | 0.8159 | 0.9325 | 1.0490 | 0.1645 | 45 |
| 0.1168 | 0.2337 | 0.3505 | 0.4674 | 0.5842 | 0.7010 | 0.8179 | 0.9347 | 1.0516 | 0.1650 | 46 |
| 0.1171 | 0.2342 | 0.3514 | 0.4685 | 0.5856 | 0.7027 | 0.8199 | 0.9370 | 1.0541 | 0.1654 | 47 |
| 0.1174 | 0.2348 | 0.3522 | 0.4696 | 0.5870 | 0.7045 | 0.8219 | 0.9393 | 1.0567 | 0.1658 | 48 |
| 0.1177 | 0.2354 | 0.3531 | 0.4708 | 0.5884 | 0.7061 | 0.8238 | 0.9415 | 1.0592 | 0.1662 | 49 |
| 0.1180 | 0.2359 | 0.3539 | 0.4719 | 0.5899 | 0.7078 | 0.8258 | 0.9438 | 1.0617 | 0.1666 | 50 |
| 0.1183 | 0.2365 | 0.3548 | 0.4730 | 0.5913 | 0.7095 | 0.8278 | 0.9460 | 1.0643 | 0.1670 | 51 |
| 0.1186 | 0.2371 | 0.3556 | 0.4742 | 0.5927 | 0.7112 | 0.8298 | 0.9483 | 1.0669 | 0.1674 | 52 |
| 0.1188 | 0.2376 | 0.3565 | 0.4753 | 0.5941 | 0.7129 | 0.8317 | 0.9506 | 1.0694 | 0.1678 | 53 |
| 0.1191 | 0.2382 | 0.3573 | 0.4764 | 0.5955 | 0.7146 | 0.8337 | 0.9528 | 1.0719 | 0.1682 | 54 |
| 0.1194 | 0.2388 | 0.3581 | 0.4775 | 0.5969 | 0.7163 | 0.8357 | 0.9550 | 1.0744 | 0.1686 | 55 |
| 0.1197 | 0.2393 | 0.3590 | 0.4786 | 0.5983 | 0.7180 | 0.8376 | 0.9573 | 1.0769 | 0.1690 | 56 |
| 0.1199 | 0.2399 | 0.3598 | 0.4798 | 0.5997 | 0.7197 | 0.8396 | 0.9596 | 1.0795 | 0.1694 | 57 |
| 0.1202 | 0.2405 | 0.3607 | 0.4809 | 0.6011 | 0.7214 | 0.8416 | 0.9618 | 1.0821 | 0.1698 | 58 |
| 0.1205 | 0.2410 | 0.3615 | 0.4820 | 0.6025 | 0.7231 | 0.8436 | 0.9641 | 1.0846 | 0.1702 | 59 |
| 0.1208 | 0.2416 | 0.3624 | 0.4832 | 0.6040 | 0.7247 | 0.8455 | 0.9663 | 1.0871 | 0.1706 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9974 | 1.9948 | 2.9922 | 3.9895 | 4.9869 | 5.9843 | 6.9817 | 7.9791 | 8.9765 | 1.3992 |
| 01 | 0.9974 | 1.9947 | 2.9921 | 3.9895 | 4.9868 | 5.9842 | 6.9815 | 7.9789 | 8.9763 | 1.3992 |
| 02 | 0.9973 | 1.9947 | 2.9920 | 3.9894 | 4.9867 | 5.9841 | 6.9814 | 7.9787 | 8.9761 | 1.3992 |
| 03 | 0.9973 | 1.9946 | 2.9920 | 3.9893 | 4.9866 | 5.9839 | 6.9812 | 7.9786 | 8.9759 | 1.3992 |
| 04 | 0.9973 | 1.9946 | 2.9919 | 3.9892 | 4.9865 | 5.9838 | 6.9811 | 7.9784 | 8.9757 | 1.3991 |
| 05 | 0.9973 | 1.9946 | 2.9918 | 3.9891 | 4.9864 | 5.9837 | 6.9810 | 7.9782 | 8.9755 | 1.3991 |
| 06 | 0.9973 | 1.9945 | 2.9918 | 3.9890 | 4.9863 | 5.9835 | 6.9808 | 7.9781 | 8.9753 | 1.3991 |
| 07 | 0.9972 | 1.9945 | 2.9917 | 3.9889 | 4.9862 | 5.9834 | 6.9807 | 7.9779 | 8.9751 | 1.3991 |
| 08 | 0.9972 | 1.9944 | 2.9916 | 3.9889 | 4.9861 | 5.9833 | 6.9805 | 7.9777 | 8.9749 | 1.3991 |
| 09 | 0.9972 | 1.9944 | 2.9916 | 3.9888 | 4.9860 | 5.9832 | 6.9804 | 7.9776 | 8.9747 | 1.3991 |
| 10 | 0.9972 | 1.9943 | 2.9915 | 3.9887 | 4.9859 | 5.9830 | 6.9802 | 7.9774 | 8.9746 | 1.3991 |
| 11 | 0.9972 | 1.9943 | 2.9915 | 3.9886 | 4.9858 | 5.9829 | 6.9801 | 7.9772 | 8.9744 | 1.3990 |
| 12 | 0.9971 | 1.9943 | 2.9914 | 3.9885 | 4.9856 | 5.9828 | 6.9799 | 7.9770 | 8.9741 | 1.3990 |
| 13 | 0.9971 | 1.9942 | 2.9913 | 3.9884 | 4.9855 | 5.9826 | 6.9797 | 7.9768 | 8.9739 | 1.3990 |
| 14 | 0.9971 | 1.9942 | 2.9912 | 3.9883 | 4.9854 | 5.9825 | 6.9796 | 7.9767 | 8.9737 | 1.3990 |
| 15 | 0.9971 | 1.9941 | 2.9912 | 3.9882 | 4.9853 | 5.9824 | 6.9794 | 7.9765 | 8.9735 | 1.3990 |
| 16 | 0.9970 | 1.9941 | 2.9911 | 3.9881 | 4.9852 | 5.9822 | 6.9793 | 7.9763 | 8.9733 | 1.3990 |
| 17 | 0.9970 | 1.9940 | 2.9910 | 3.9881 | 4.9851 | 5.9821 | 6.9791 | 7.9761 | 8.9731 | 1.3989 |
| 18 | 0.9970 | 1.9940 | 2.9910 | 3.9880 | 4.9850 | 5.9819 | 6.9789 | 7.9759 | 8.9729 | 1.3989 |
| 19 | 0.9970 | 1.9939 | 2.9909 | 3.9879 | 4.9848 | 5.9818 | 6.9788 | 7.9757 | 8.9727 | 1.3989 |
| 20 | 0.9969 | 1.9939 | 2.9908 | 3.9878 | 4.9847 | 5.9817 | 6.9786 | 7.9756 | 8.9725 | 1.3989 |
| 21 | 0.9969 | 1.9938 | 2.9908 | 3.9877 | 4.9846 | 5.9815 | 6.9784 | 7.9754 | 8.9723 | 1.3989 |
| 22 | 0.9969 | 1.9938 | 2.9907 | 3.9876 | 4.9845 | 5.9814 | 6.9783 | 7.9752 | 8.9721 | 1.3989 |
| 23 | 0.9969 | 1.9937 | 2.9906 | 3.9875 | 4.9844 | 5.9812 | 6.9781 | 7.9750 | 8.9718 | 1.3988 |
| 24 | 0.9968 | 1.9937 | 2.9905 | 3.9874 | 4.9842 | 5.9811 | 6.9779 | 7.9748 | 8.9716 | 1.3988 |
| 25 | 0.9968 | 1.9936 | 2.9905 | 3.9873 | 4.9841 | 5.9809 | 6.9778 | 7.9746 | 8.9714 | 1.3988 |
| 26 | 0.9968 | 1.9936 | 2.9904 | 3.9872 | 4.9840 | 5.9808 | 6.9776 | 7.9744 | 8.9712 | 1.3988 |
| 27 | 0.9968 | 1.9935 | 2.9903 | 3.9871 | 4.9839 | 5.9806 | 6.9774 | 7.9742 | 8.9710 | 1.3988 |
| 28 | 0.9967 | 1.9935 | 2.9902 | 3.9870 | 4.9837 | 5.9805 | 6.9772 | 7.9740 | 8.9707 | 1.3987 |
| 29 | 0.9967 | 1.9934 | 2.9902 | 3.9869 | 4.9836 | 5.9803 | 6.9771 | 7.9738 | 8.9705 | 1.3987 |
| 30 | 0.9967 | 1.9934 | 2.9901 | 3.9868 | 4.9835 | 5.9802 | 6.9769 | 7.9736 | 8.9703 | 1.3987 |
| 31 | 0.9967 | 1.9933 | 2.9900 | 3.9867 | 4.9834 | 5.9800 | 6.9767 | 7.9734 | 8.9701 | 1.3987 |
| 32 | 0.9966 | 1.9933 | 2.9899 | 3.9866 | 4.9832 | 5.9799 | 6.9765 | 7.9732 | 8.9698 | 1.3987 |
| 33 | 0.9966 | 1.9932 | 2.9899 | 3.9865 | 4.9831 | 5.9797 | 6.9764 | 7.9730 | 8.9696 | 1.3987 |
| 34 | 0.9966 | 1.9932 | 2.9898 | 3.9864 | 4.9830 | 5.9796 | 6.9762 | 7.9728 | 8.9694 | 1.3986 |
| 35 | 0.9966 | 1.9931 | 2.9897 | 3.9863 | 4.9828 | 5.9794 | 6.9760 | 7.9726 | 8.9691 | 1.3986 |
| 36 | 0.9965 | 1.9931 | 2.9896 | 3.9862 | 4.9827 | 5.9793 | 6.9758 | 7.9723 | 8.9689 | 1.3986 |
| 37 | 0.9965 | 1.9930 | 2.9896 | 3.9861 | 4.9826 | 5.9791 | 6.9756 | 7.9721 | 8.9687 | 1.3986 |
| 38 | 0.9965 | 1.9930 | 2.9895 | 3.9860 | 4.9825 | 5.9789 | 6.9754 | 7.9719 | 8.9684 | 1.3986 |
| 39 | 0.9965 | 1.9929 | 2.9894 | 3.9859 | 4.9823 | 5.9788 | 6.9753 | 7.9717 | 8.9682 | 1.3985 |
| 40 | 0.9964 | 1.9929 | 2.9893 | 3.9858 | 4.9822 | 5.9786 | 6.9751 | 7.9715 | 8.9680 | 1.3985 |
| 41 | 0.9964 | 1.9928 | 2.9892 | 3.9856 | 4.9821 | 5.9785 | 6.9749 | 7.9713 | 8.9677 | 1.3985 |
| 42 | 0.9964 | 1.9928 | 2.9891 | 3.9855 | 4.9819 | 5.9783 | 6.9747 | 7.9711 | 8.9674 | 1.3985 |
| 43 | 0.9964 | 1.9927 | 2.9891 | 3.9854 | 4.9818 | 5.9781 | 6.9745 | 7.9708 | 8.9672 | 1.3985 |
| 44 | 0.9963 | 1.9927 | 2.9890 | 3.9853 | 4.9816 | 5.9780 | 6.9743 | 7.9706 | 8.9669 | 1.3984 |
| 45 | 0.9963 | 1.9926 | 2.9889 | 3.9852 | 4.9815 | 5.9778 | 6.9741 | 7.9704 | 8.9667 | 1.3984 |
| 46 | 0.9963 | 1.9925 | 2.9888 | 3.9851 | 4.9814 | 5.9776 | 6.9739 | 7.9702 | 8.9664 | 1.3984 |
| 47 | 0.9962 | 1.9925 | 2.9887 | 3.9850 | 4.9812 | 5.9775 | 6.9737 | 7.9700 | 8.9662 | 1.3984 |
| 48 | 0.9962 | 1.9924 | 2.9886 | 3.9849 | 4.9811 | 5.9773 | 6.9735 | 7.9697 | 8.9659 | 1.3984 |
| 49 | 0.9962 | 1.9924 | 2.9886 | 3.9848 | 4.9809 | 5.9771 | 6.9733 | 7.9695 | 8.9657 | 1.3983 |
| 50 | 0.9962 | 1.9923 | 2.9885 | 3.9846 | 4.9808 | 5.9770 | 6.9731 | 7.9693 | 8.9654 | 1.3983 |
| 51 | 0.9961 | 1.9923 | 2.9884 | 3.9845 | 4.9807 | 5.9768 | 6.9729 | 7.9690 | 8.9652 | 1.3983 |
| 52 | 0.9961 | 1.9922 | 2.9883 | 3.9844 | 4.9805 | 5.9766 | 6.9727 | 7.9688 | 8.9649 | 1.3983 |
| 53 | 0.9961 | 1.9921 | 2.9882 | 3.9843 | 4.9804 | 5.9764 | 6.9725 | 7.9686 | 8.9646 | 1.3983 |
| 54 | 0.9960 | 1.9921 | 2.9881 | 3.9842 | 4.9802 | 5.9763 | 6.9723 | 7.9683 | 8.9644 | 1.3982 |
| 55 | 0.9960 | 1.9920 | 2.9880 | 3.9841 | 4.9801 | 5.9761 | 6.9721 | 7.9681 | 8.9641 | 1.3982 |
| 56 | 0.9960 | 1.9920 | 2.9879 | 3.9839 | 4.9799 | 5.9759 | 6.9719 | 7.9679 | 8.9638 | 1.3982 |
| 57 | 0.9960 | 1.9919 | 2.9879 | 3.9838 | 4.9798 | 5.9757 | 6.9717 | 7.9677 | 8.9636 | 1.3982 |
| 58 | 0.9959 | 1.9918 | 2.9878 | 3.9837 | 4.9796 | 5.9755 | 6.9715 | 7.9674 | 8.9633 | 1.3981 |
| 59 | 0.9959 | 1.9918 | 2.9877 | 3.9836 | 4.9795 | 5.9754 | 6.9713 | 7.9672 | 8.9631 | 1.3981 |
| 60 | 0.9959 | 1.9917 | 2.9876 | 3.9835 | 4.9793 | 5.9752 | 6.9711 | 7.9669 | 8.9628 | 1.3981 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0348 | 0.0697 | 0.1045 | 0.1393 | 0.1742 | 0.2090 | 0.2438 | 0.2786 | 0.3135 | 0.0489 | 00 |
| 0.0351 | 0.0702 | 0.1054 | 0.1405 | 0.1756 | 0.2107 | 0.2458 | 0.2810 | 0.3161 | 0.0493 | 01 |
| 0.0354 | 0.0708 | 0.1062 | 0.1416 | 0.1771 | 0.2125 | 0.2479 | 0.2833 | 0.3187 | 0.0497 | 02 |
| 0.0357 | 0.0714 | 0.1071 | 0.1428 | 0.1785 | 0.2142 | 0.2499 | 0.2856 | 0.3213 | 0.0501 | 03 |
| 0.0360 | 0.0720 | 0.1080 | 0.1440 | 0.1800 | 0.2159 | 0.2519 | 0.2879 | 0.3239 | 0.0505 | 04 |
| 0.0363 | 0.0726 | 0.1088 | 0.1451 | 0.1814 | 0.2177 | 0.2540 | 0.2902 | 0.3265 | 0.0509 | 05 |
| 0.0366 | 0.0731 | 0.1097 | 0.1463 | 0.1828 | 0.2194 | 0.2560 | 0.2926 | 0.3291 | 0.0513 | 06 |
| 0.0369 | 0.0737 | 0.1106 | 0.1474 | 0.1843 | 0.2212 | 0.2580 | 0.2949 | 0.3317 | 0.0517 | 07 |
| 0.0371 | 0.0743 | 0.1114 | 0.1486 | 0.1857 | 0.2229 | 0.2600 | 0.2972 | 0.3343 | 0.0521 | 08 |
| 0.0374 | 0.0749 | 0.1123 | 0.1498 | 0.1872 | 0.2246 | 0.2621 | 0.2995 | 0.3370 | 0.0525 | 09 |
| 0.0377 | 0.0755 | 0.1132 | 0.1509 | 0.1886 | 0.2264 | 0.2641 | 0.3018 | 0.3396 | 0.0529 | 10 |
| 0.0380 | 0.0760 | 0.1141 | 0.1521 | 0.1901 | 0.2281 | 0.2661 | 0.3042 | 0.3422 | 0.0533 | 11 |
| 0.0383 | 0.0766 | 0.1149 | 0.1532 | 0.1915 | 0.2299 | 0.2682 | 0.3065 | 0.3448 | 0.0537 | 12 |
| 0.0386 | 0.0772 | 0.1158 | 0.1544 | 0.1930 | 0.2316 | 0.2702 | 0.3088 | 0.3474 | 0.0541 | 13 |
| 0.0389 | 0.0778 | 0.1167 | 0.1556 | 0.1944 | 0.2333 | 0.2722 | 0.3111 | 0.3500 | 0.0546 | 14 |
| 0.0392 | 0.0783 | 0.1175 | 0.1567 | 0.1959 | 0.2350 | 0.2742 | 0.3134 | 0.3526 | 0.0550 | 15 |
| 0.0395 | 0.0789 | 0.1184 | 0.1578 | 0.1973 | 0.2368 | 0.2762 | 0.3157 | 0.3552 | 0.0554 | 16 |
| 0.0398 | 0.0795 | 0.1193 | 0.1590 | 0.1988 | 0.2385 | 0.2783 | 0.3180 | 0.3578 | 0.0558 | 17 |
| 0.0400 | 0.0801 | 0.1201 | 0.1602 | 0.2002 | 0.2402 | 0.2803 | 0.3203 | 0.3604 | 0.0562 | 18 |
| 0.0403 | 0.0807 | 0.1210 | 0.1613 | 0.0017 | 0.2420 | 0.2823 | 0.3226 | 0.3630 | 0.0566 | 19 |
| 0.0406 | 0.0812 | 0.1219 | 0.1625 | 0.2031 | 0.2437 | 0.2843 | 0.3250 | 0.3656 | 0.0570 | 20 |
| 0.0409 | 0.0818 | 0.1227 | 0.1636 | 0.2046 | 0.2455 | 0.2864 | 0.3273 | 0.3682 | 0.0574 | 21 |
| 0.0412 | 0.0824 | 0.1236 | 0.1648 | 0.2060 | 0.2472 | 0.2884 | 0.3296 | 0.3708 | 0.0578 | 22 |
| 0.0415 | 0.0830 | 0.1245 | 0.1660 | 0.2075 | 0.2489 | 0.2904 | 0.3319 | 0.3734 | 0.0582 | 23 |
| 0.0418 | 0.0836 | 0.1253 | 0.1671 | 0.2089 | 0.2507 | 0.2925 | 0.3342 | 0.3760 | 0.0586 | 24 |
| 0.0421 | 0.0841 | 0.1262 | 0.1683 | 0.2103 | 0.2524 | 0.2945 | 0.3366 | 0.3786 | 0.0590 | 25 |
| 0.0424 | 0.0847 | 0.1271 | 0.1694 | 0.2118 | 0.2542 | 0.2965 | 0.3389 | 0.3812 | 0.0594 | 26 |
| 0.0426 | 0.0853 | 0.1279 | 0.1706 | 0.2132 | 0.2559 | 0.2985 | 0.3412 | 0.3838 | 0.0598 | 27 |
| 0.0429 | 0.0859 | 0.1288 | 0.1718 | 0.2147 | 0.2576 | 0.3006 | 0.3435 | 0.3865 | 0.0602 | 28 |
| 0.0432 | 0.0865 | 0.1297 | 0.1729 | 0.2161 | 0.2594 | 0.3026 | 0.3458 | 0.3891 | 0.0607 | 29 |
| 0.0435 | 0.0870 | 0.1306 | 0.1741 | 0.2176 | 0.2611 | 0.3046 | 0.3482 | 0.3917 | 0.0611 | 30 |
| 0.0438 | 0.0876 | 0.1314 | 0.1752 | 0.2190 | 0.2629 | 0.3067 | 0.3505 | 0.3943 | 0.0615 | 31 |
| 0.0441 | 0.0882 | 0.1323 | 0.1764 | 0.2205 | 0.2646 | 0.3087 | 0.3528 | 0.3969 | 0.0619 | 32 |
| 0.0444 | 0.0888 | 0.1331 | 0.1775 | 0.2219 | 0.2663 | 0.3107 | 0.3551 | 0.3995 | 0.0623 | 33 |
| 0.0447 | 0.0893 | 0.1340 | 0.1787 | 0.2234 | 0.2680 | 0.3127 | 0.3574 | 0.4021 | 0.0627 | 34 |
| 0.0450 | 0.0899 | 0.1349 | 0.1798 | 0.2248 | 0.2698 | 0.3147 | 0.3597 | 0.4047 | 0.0631 | 35 |
| 0.0453 | 0.0905 | 0.1358 | 0.1810 | 0.2263 | 0.2715 | 0.3168 | 0.3620 | 0.4073 | 0.0635 | 36 |
| 0.0455 | 0.0911 | 0.1366 | 0.1822 | 0.2277 | 0.2732 | 0.3188 | 0.3643 | 0.4099 | 0.0639 | 37 |
| 0.0458 | 0.0917 | 0.1375 | 0.1833 | 0.2292 | 0.2750 | 0.3208 | 0.3666 | 0.4125 | 0.0643 | 38 |
| 0.0461 | 0.0922 | 0.1384 | 0.1845 | 0.2306 | 0.2767 | 0.3228 | 0.3690 | 0.4151 | 0.0647 | 39 |
| 0.0464 | 0.0928 | 0.1392 | 0.1856 | 0.2321 | 0.2785 | 0.3249 | 0.3713 | 0.4177 | 0.0651 | 40 |
| 0.0467 | 0.0934 | 0.1401 | 0.1868 | 0.2335 | 0.2802 | 0.3269 | 0.3736 | 0.4203 | 0.0655 | 41 |
| 0.0470 | 0.0940 | 0.1410 | 0.1880 | 0.2350 | 0.2819 | 0.3289 | 0.3759 | 0.4229 | 0.0659 | 42 |
| 0.0473 | 0.0946 | 0.1418 | 0.1891 | 0.2364 | 0.2837 | 0.3310 | 0.3782 | 0.4255 | 0.0664 | 43 |
| 0.0476 | 0.0951 | 0.1427 | 0.1903 | 0.2378 | 0.2854 | 0.3330 | 0.3806 | 0.4281 | 0.0668 | 44 |
| 0.0479 | 0.0957 | 0.1436 | 0.1914 | 0.2393 | 0.2872 | 0.3350 | 0.3829 | 0.4307 | 0.0672 | 45 |
| 0.0481 | 0.0963 | 0.1444 | 0.1926 | 0.2407 | 0.2889 | 0.3370 | 0.3852 | 0.4333 | 0.0676 | 46 |
| 0.0484 | 0.0969 | 0.1453 | 0.1937 | 0.2422 | 0.2906 | 0.3390 | 0.3875 | 0.4359 | 0.0680 | 47 |
| 0.0487 | 0.0974 | 0.1462 | 0.1949 | 0.2436 | 0.2923 | 0.3410 | 0.3898 | 0.4385 | 0.0684 | 48 |
| 0.0490 | 0.0980 | 0.1470 | 0.1960 | 0.2451 | 0.2941 | 0.3431 | 0.3921 | 0.4411 | 0.0688 | 49 |
| 0.0493 | 0.0986 | 0.1479 | 0.1972 | 0.2465 | 0.2958 | 0.3451 | 0.3944 | 0.4437 | 0.0692 | 50 |
| 0.0496 | 0.0992 | 0.1488 | 0.1984 | 0.2480 | 0.2975 | 0.3471 | 0.3967 | 0.4463 | 0.0696 | 51 |
| 0.0499 | 0.0998 | 0.1496 | 0.1995 | 0.2494 | 0.2993 | 0.3492 | 0.3990 | 0.4489 | 0.0700 | 52 |
| 0.0502 | 0.1003 | 0.1505 | 0.2007 | 0.2508 | 0.3010 | 0.3512 | 0.4014 | 0.4515 | 0.0704 | 53 |
| 0.0505 | 0.1009 | 0.1514 | 0.2018 | 0.2523 | 0.3028 | 0.3532 | 0.4037 | 0.4541 | 0.0708 | 54 |
| 0.0507 | 0.1015 | 0.1522 | 0.2030 | 0.2537 | 0.3045 | 0.3552 | 0.4060 | 0.4567 | 0.0712 | 55 |
| 0.0510 | 0.1021 | 0.1531 | 0.2042 | 0.2552 | 0.3062 | 0.3573 | 0.4083 | 0.4593 | 0.0716 | 56 |
| 0.0513 | 0.1026 | 0.1540 | 0.2053 | 0.2566 | 0.3079 | 0.3593 | 0.4106 | 0.4619 | 0.0721 | 57 |
| 0.0516 | 0.1032 | 0.1548 | 0.2064 | 0.2581 | 0.3097 | 0.3613 | 0.4129 | 0.4645 | 0.0725 | 58 |
| 0.0519 | 0.1038 | 0.1557 | 0.2076 | 0.2595 | 0.3114 | 0.3633 | 0.4152 | 0.4671 | 0.0729 | 59 |
| 0.0522 | 0.1044 | 0.1566 | 0.2088 | 0.2610 | 0.3131 | 0.3653 | 0.4175 | 0.4697 | 0.0733 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9959 | 1.9917 | 2.9876 | 3.9835 | 4.9793 | 5.9752 | 6.9711 | 7.9669 | 8.9628 | 1.3981 |
| 01 | 0.9958 | 1.9917 | 2.9875 | 3.9833 | 4.9792 | 5.9750 | 6.9708 | 7.9667 | 8.9625 | 1.3981 |
| 02 | 0.9958 | 1.9916 | 2.9874 | 3.9832 | 4.9790 | 5.9748 | 6.9706 | 7.9664 | 8.9622 | 1.3981 |
| 03 | 0.9958 | 1.9915 | 2.9873 | 3.9831 | 4.9789 | 5.9746 | 6.9704 | 7.9662 | 8.9619 | 1.3980 |
| 04 | 0.9957 | 1.9915 | 2.9872 | 3.9830 | 4.9787 | 5.9744 | 6.9702 | 7.9659 | 8.9617 | 1.3980 |
| 05 | 0.9957 | 1.9914 | 2.9871 | 3.9828 | 4.9785 | 5.9743 | 6.9700 | 7.9657 | 8.9614 | 1.3980 |
| 06 | 0.9957 | 1.9914 | 2.9870 | 3.9827 | 4.9784 | 5.9741 | 6.9697 | 7.9654 | 8.9611 | 1.3980 |
| 07 | 0.9956 | 1.9913 | 2.9869 | 3.9826 | 4.9782 | 5.9739 | 6.9695 | 7.9652 | 8.9608 | 1.3980 |
| 08 | 0.9956 | 1.9912 | 2.9868 | 3.9825 | 4.9781 | 5.9737 | 6.9693 | 7.9649 | 8.9605 | 1.3979 |
| 09 | 0.9956 | 1.9912 | 2.9868 | 3.9823 | 4.9779 | 5.9735 | 6.9691 | 7.9647 | 8.9603 | 1.3979 |
| 10 | 0.9956 | 1.9911 | 2.9867 | 3.9822 | 4.9778 | 5.9733 | 6.9689 | 7.9644 | 8.9600 | 1.3979 |
| 11 | 0.9955 | 1.9910 | 2.9866 | 3.9821 | 4.9776 | 5.9731 | 6.9686 | 7.9642 | 8.9597 | 1.3979 |
| 12 | 0.9955 | 1.9910 | 2.9865 | 3.9819 | 4.9774 | 5.9729 | 6.9684 | 7.9639 | 8.9594 | 1.3978 |
| 13 | 0.9955 | 1.9909 | 2.9864 | 3.9818 | 4.9773 | 5.9727 | 6.9682 | 7.9636 | 8.9591 | 1.3978 |
| 14 | 0.9954 | 1.9908 | 2.9863 | 3.9817 | 4.9771 | 5.9725 | 6.9679 | 7.9634 | 8.9588 | 1.3978 |
| 15 | 0.9954 | 1.9908 | 2.9862 | 3.9816 | 4.9769 | 5.9723 | 6.9677 | 7.9631 | 8.9585 | 1.3978 |
| 16 | 0.9954 | 1.9907 | 2.9861 | 3.9814 | 4.9768 | 5.9721 | 6.9675 | 7.9628 | 8.9582 | 1.3977 |
| 17 | 0.9953 | 1.9906 | 2.9860 | 3.9813 | 4.9766 | 5.9719 | 6.9673 | 7.9626 | 8.9579 | 1.3977 |
| 18 | 0.9953 | 1.9906 | 2.9859 | 3.9812 | 4.9764 | 5.9717 | 6.9670 | 7.9623 | 8.9576 | 1.3977 |
| 19 | 0.9953 | 1.9905 | 2.9858 | 3.9810 | 4.9763 | 5.9715 | 6.9668 | 7.9621 | 8.9573 | 1.3977 |
| 20 | 0.9952 | 1.9904 | 2.9857 | 3.9809 | 4.9761 | 5.9713 | 6.9666 | 7.9618 | 8.9570 | 1.3976 |
| 21 | 0.9952 | 1.9904 | 2.9856 | 3.9808 | 4.9759 | 5.9711 | 6.9663 | 7.9615 | 8.9567 | 1.3976 |
| 22 | 0.9952 | 1.9903 | 2.9855 | 3.9806 | 4.9758 | 5.9709 | 6.9661 | 7.9612 | 8.9564 | 1.3976 |
| 23 | 0.9951 | 1.9902 | 2.9854 | 3.9805 | 4.9756 | 5.9707 | 6.9658 | 7.9610 | 8.9561 | 1.3976 |
| 24 | 0.9951 | 1.9902 | 2.9853 | 3.9803 | 4.9754 | 5.9705 | 6.9656 | 7.9607 | 8.9558 | 1.3975 |
| 25 | 0.9951 | 1.9901 | 2.9852 | 3.9802 | 4.9753 | 5.9703 | 6.9654 | 7.9604 | 8.9555 | 1.3975 |
| 26 | 0.9950 | 1.9900 | 2.9850 | 3.9801 | 4.9751 | 5.9701 | 6.9651 | 7.9601 | 8.9551 | 1.3975 |
| 27 | 0.9950 | 1.9900 | 2.9849 | 3.9799 | 4.9749 | 5.9699 | 6.9649 | 7.9599 | 8.9548 | 1.3975 |
| 28 | 0.9949 | 1.9899 | 2.9848 | 3.9798 | 4.9747 | 5.9697 | 6.9646 | 7.9598 | 8.9545 | 1.3974 |
| 29 | 0.9949 | 1.9898 | 2.9847 | 3.9797 | 4.9746 | 5.9695 | 6.9644 | 7.9597 | 8.9542 | 1.3974 |
| 30 | 0.9949 | 1.9898 | 2.9846 | 3.9795 | 4.9744 | 5.9693 | 6.9641 | 7.9595 | 8.9539 | 1.3974 |
| 31 | 0.9948 | 1.9897 | 2.9845 | 3.9794 | 4.9742 | 5.9691 | 6.9639 | 7.9587 | 8.9536 | 1.3973 |
| 32 | 0.9948 | 1.9896 | 2.9844 | 3.9792 | 4.9740 | 5.9688 | 6.9636 | 7.9584 | 8.9533 | 1.3973 |
| 33 | 0.9948 | 1.9895 | 2.9843 | 3.9791 | 4.9738 | 5.9686 | 6.9634 | 7.9582 | 8.9529 | 1.3973 |
| 34 | 0.9947 | 1.9895 | 2.9842 | 3.9789 | 4.9737 | 5.9684 | 6.9631 | 7.9579 | 8.9526 | 1.3973 |
| 35 | 0.9947 | 1.9894 | 2.9841 | 3.9788 | 4.9735 | 5.9682 | 6.9629 | 7.9576 | 8.9523 | 1.3972 |
| 36 | 0.9947 | 1.9893 | 2.9840 | 3.9786 | 4.9733 | 5.9680 | 6.9626 | 7.9573 | 8.9519 | 1.3972 |
| 37 | 0.9946 | 1.9893 | 2.9839 | 3.9785 | 4.9731 | 5.9678 | 6.9624 | 7.9570 | 8.9516 | 1.3972 |
| 38 | 0.9946 | 1.9892 | 2.9838 | 3.9784 | 4.9729 | 5.9675 | 6.9621 | 7.9567 | 8.9513 | 1.3972 |
| 39 | 0.9946 | 1.9891 | 2.9837 | 3.9782 | 4.9728 | 5.9673 | 6.9619 | 7.9564 | 8.9510 | 1.3971 |
| 40 | 0.9945 | 1.9890 | 2.9835 | 3.9781 | 4.9726 | 5.9671 | 6.9616 | 7.9561 | 8.9506 | 1.3971 |
| 41 | 0.9945 | 1.9890 | 2.9834 | 3.9779 | 4.9724 | 5.9669 | 6.9613 | 7.9558 | 8.9503 | 1.3971 |
| 42 | 0.9944 | 1.9889 | 2.9833 | 3.9778 | 4.9722 | 5.9666 | 6.9611 | 7.9555 | 8.9500 | 1.3971 |
| 43 | 0.9944 | 1.9888 | 2.9832 | 3.9776 | 4.9720 | 5.9664 | 6.9608 | 7.9552 | 8.9496 | 1.3970 |
| 44 | 0.9944 | 1.9887 | 2.9831 | 3.9775 | 4.9718 | 5.9662 | 6.9605 | 7.9549 | 8.9493 | 1.3970 |
| 45 | 0.9943 | 1.9887 | 2.9830 | 3.9773 | 4.9716 | 5.9660 | 6.9603 | 7.9546 | 8.9489 | 1.3970 |
| 46 | 0.9943 | 1.9886 | 2.9829 | 3.9772 | 4.9714 | 5.9657 | 6.9600 | 7.9543 | 8.9486 | 1.3969 |
| 47 | 0.9943 | 1.9885 | 2.9828 | 3.9770 | 4.9713 | 5.9655 | 6.9598 | 7.9540 | 8.9483 | 1.3969 |
| 48 | 0.9942 | 1.9884 | 2.9826 | 3.9769 | 4.9711 | 5.9653 | 6.9595 | 7.9537 | 8.9479 | 1.3969 |
| 49 | 0.9942 | 1.9884 | 2.9825 | 3.9767 | 4.9709 | 5.9651 | 6.9592 | 7.9534 | 8.9476 | 1.3969 |
| 50 | 0.9941 | 1.9883 | 2.9824 | 3.9765 | 4.9707 | 5.9648 | 6.9590 | 7.9531 | 8.9472 | 1.3968 |
| 51 | 0.9941 | 1.9882 | 2.9823 | 3.9764 | 4.9705 | 5.9646 | 6.9587 | 7.9528 | 8.9469 | 1.3968 |
| 52 | 0.9941 | 1.9881 | 2.9822 | 3.9762 | 4.9703 | 5.9643 | 6.9584 | 7.9525 | 8.9465 | 1.3968 |
| 53 | 0.9940 | 1.9880 | 2.9821 | 3.9761 | 4.9701 | 5.9641 | 6.9581 | 7.9521 | 8.9462 | 1.3968 |
| 54 | 0.9940 | 1.9880 | 2.9819 | 3.9759 | 4.9699 | 5.9639 | 6.9579 | 7.9518 | 8.9458 | 1.3967 |
| 55 | 0.9939 | 1.9879 | 2.9818 | 3.9758 | 4.9697 | 5.9636 | 6.9576 | 7.9515 | 8.9455 | 1.3967 |
| 56 | 0.9939 | 1.9878 | 2.9817 | 3.9756 | 4.9695 | 5.9634 | 6.9573 | 7.9512 | 8.9451 | 1.3967 |
| 57 | 0.9939 | 1.9877 | 2.9816 | 3.9754 | 4.9693 | 5.9632 | 6.9570 | 7.9509 | 8.9447 | 1.3967 |
| 58 | 0.9938 | 1.9876 | 2.9815 | 3.9753 | 4.9691 | 5.9629 | 6.9567 | 7.9506 | 8.9444 | 1.3966 |
| 59 | 0.9938 | 1.9876 | 2.9813 | 3.9751 | 4.9689 | 5.9627 | 6.9565 | 7.9502 | 8.9440 | 1.3966 |
| 60 | 0.9937 | 1.9875 | 2.9812 | 3.9750 | 4.9687 | 5.9624 | 6.9562 | 7.9499 | 8.9437 | 1.3966 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | d      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0522 | 0.1044 | 0.1566 | 0.2088 | 0.2610 | 0.3131 | 0.3653 | 0.4175 | 0.4697 | 0.0733 | 00 |
| 0.0525 | 0.1050 | 0.1574 | 0.2099 | 0.2624 | 0.3149 | 0.3674 | 0.4198 | 0.4723 | 0.0737 | 01 |
| 0.0528 | 0.1055 | 0.1583 | 0.2111 | 0.2638 | 0.3166 | 0.3694 | 0.4222 | 0.4749 | 0.0741 | 02 |
| 0.0531 | 0.1061 | 0.1592 | 0.2122 | 0.2653 | 0.3184 | 0.3714 | 0.4245 | 0.4775 | 0.0745 | 03 |
| 0.0533 | 0.1067 | 0.1600 | 0.2134 | 0.2667 | 0.3201 | 0.3734 | 0.4268 | 0.4801 | 0.0749 | 04 |
| 0.0536 | 0.1073 | 0.1609 | 0.2145 | 0.2682 | 0.3218 | 0.3754 | 0.4291 | 0.4827 | 0.0753 | 05 |
| 0.0539 | 0.1078 | 0.1618 | 0.2157 | 0.2696 | 0.3235 | 0.3774 | 0.4314 | 0.4853 | 0.0757 | 06 |
| 0.0542 | 0.1084 | 0.1626 | 0.2168 | 0.2711 | 0.3253 | 0.3795 | 0.4337 | 0.4879 | 0.0761 | 07 |
| 0.0545 | 0.1090 | 0.1635 | 0.2180 | 0.2725 | 0.3270 | 0.3815 | 0.4360 | 0.4905 | 0.0765 | 08 |
| 0.0548 | 0.1096 | 0.1644 | 0.2192 | 0.2739 | 0.3287 | 0.3835 | 0.4383 | 0.4931 | 0.0769 | 09 |
| 0.0551 | 0.1102 | 0.1652 | 0.2203 | 0.2754 | 0.3305 | 0.3856 | 0.4406 | 0.4957 | 0.0773 | 10 |
| 0.0554 | 0.1107 | 0.1661 | 0.2215 | 0.2768 | 0.3322 | 0.3876 | 0.4430 | 0.4983 | 0.0777 | 11 |
| 0.0557 | 0.1113 | 0.1670 | 0.2226 | 0.2783 | 0.3340 | 0.3896 | 0.4453 | 0.5009 | 0.0781 | 12 |
| 0.0559 | 0.1119 | 0.1678 | 0.2238 | 0.2797 | 0.3356 | 0.3916 | 0.4475 | 0.5035 | 0.0786 | 13 |
| 0.0562 | 0.1125 | 0.1687 | 0.2249 | 0.2812 | 0.3374 | 0.3936 | 0.4498 | 0.5061 | 0.0790 | 14 |
| 0.0565 | 0.1130 | 0.1696 | 0.2261 | 0.2826 | 0.3391 | 0.3956 | 0.4522 | 0.5087 | 0.0794 | 15 |
| 0.0568 | 0.1136 | 0.1704 | 0.2272 | 0.2841 | 0.3409 | 0.3977 | 0.4545 | 0.5113 | 0.0798 | 16 |
| 0.0571 | 0.1142 | 0.1713 | 0.2284 | 0.2855 | 0.3426 | 0.3997 | 0.4568 | 0.5139 | 0.0802 | 17 |
| 0.0574 | 0.1148 | 0.1722 | 0.2296 | 0.2869 | 0.3443 | 0.4017 | 0.4591 | 0.5165 | 0.0806 | 18 |
| 0.0577 | 0.1154 | 0.1730 | 0.2307 | 0.2884 | 0.3461 | 0.4038 | 0.4614 | 0.5191 | 0.0810 | 19 |
| 0.0580 | 0.1159 | 0.1739 | 0.2319 | 0.2898 | 0.3478 | 0.4058 | 0.4638 | 0.5217 | 0.0814 | 20 |
| 0.0583 | 0.1165 | 0.1748 | 0.2330 | 0.2913 | 0.3495 | 0.4078 | 0.4660 | 0.5243 | 0.0818 | 21 |
| 0.0585 | 0.1171 | 0.1756 | 0.2342 | 0.2927 | 0.3512 | 0.4098 | 0.4683 | 0.5269 | 0.0822 | 22 |
| 0.0588 | 0.1177 | 0.1765 | 0.2353 | 0.2942 | 0.3530 | 0.4118 | 0.4706 | 0.5295 | 0.0826 | 23 |
| 0.0591 | 0.1182 | 0.1774 | 0.2365 | 0.2956 | 0.3547 | 0.4138 | 0.4730 | 0.5321 | 0.0830 | 24 |
| 0.0594 | 0.1188 | 0.1782 | 0.2376 | 0.2971 | 0.3565 | 0.4159 | 0.4753 | 0.5347 | 0.0834 | 25 |
| 0.0597 | 0.1194 | 0.1791 | 0.2388 | 0.2985 | 0.3582 | 0.4179 | 0.4776 | 0.5373 | 0.0838 | 26 |
| 0.0600 | 0.1200 | 0.1799 | 0.2399 | 0.2999 | 0.3599 | 0.4199 | 0.4799 | 0.5399 | 0.0842 | 27 |
| 0.0603 | 0.1205 | 0.1808 | 0.2411 | 0.3014 | 0.3616 | 0.4219 | 0.4822 | 0.5425 | 0.0847 | 28 |
| 0.0606 | 0.1211 | 0.1817 | 0.2422 | 0.3028 | 0.3634 | 0.4239 | 0.4845 | 0.5451 | 0.0851 | 29 |
| 0.0608 | 0.1217 | 0.1825 | 0.2434 | 0.3042 | 0.3651 | 0.4259 | 0.4868 | 0.5477 | 0.0855 | 30 |
| 0.0611 | 0.1223 | 0.1834 | 0.2446 | 0.3057 | 0.3668 | 0.4280 | 0.4891 | 0.5503 | 0.0859 | 31 |
| 0.0614 | 0.1229 | 0.1843 | 0.2457 | 0.3071 | 0.3686 | 0.4300 | 0.4914 | 0.5529 | 0.0863 | 32 |
| 0.0617 | 0.1234 | 0.1851 | 0.2468 | 0.3086 | 0.3703 | 0.4320 | 0.4937 | 0.5554 | 0.0867 | 33 |
| 0.0620 | 0.1240 | 0.1860 | 0.2480 | 0.3100 | 0.3720 | 0.4340 | 0.4960 | 0.5580 | 0.0871 | 34 |
| 0.0623 | 0.1246 | 0.1869 | 0.2492 | 0.3115 | 0.3737 | 0.4360 | 0.4983 | 0.5606 | 0.0875 | 35 |
| 0.0626 | 0.1252 | 0.1877 | 0.2503 | 0.3129 | 0.3755 | 0.4381 | 0.5006 | 0.5632 | 0.0879 | 36 |
| 0.0629 | 0.1257 | 0.1886 | 0.2515 | 0.3143 | 0.3772 | 0.4401 | 0.5030 | 0.5658 | 0.0883 | 37 |
| 0.0632 | 0.1263 | 0.1895 | 0.2526 | 0.3158 | 0.3789 | 0.4421 | 0.5053 | 0.5684 | 0.0887 | 38 |
| 0.0634 | 0.1269 | 0.1903 | 0.2538 | 0.3172 | 0.3806 | 0.4441 | 0.5075 | 0.5710 | 0.0891 | 39 |
| 0.0637 | 0.1275 | 0.1912 | 0.2549 | 0.3187 | 0.3824 | 0.4461 | 0.5098 | 0.5736 | 0.0895 | 40 |
| 0.0640 | 0.1280 | 0.1921 | 0.2561 | 0.3201 | 0.3841 | 0.4481 | 0.5122 | 0.5762 | 0.0899 | 41 |
| 0.0643 | 0.1286 | 0.1929 | 0.2572 | 0.3215 | 0.3859 | 0.4502 | 0.5145 | 0.5788 | 0.0903 | 42 |
| 0.0646 | 0.1292 | 0.1938 | 0.2584 | 0.3230 | 0.3876 | 0.4522 | 0.5168 | 0.5814 | 0.0908 | 43 |
| 0.0649 | 0.1298 | 0.1946 | 0.2595 | 0.3244 | 0.3893 | 0.4542 | 0.5190 | 0.5839 | 0.0912 | 44 |
| 0.0652 | 0.1303 | 0.1955 | 0.2607 | 0.3259 | 0.3910 | 0.4562 | 0.5214 | 0.5865 | 0.0916 | 45 |
| 0.0655 | 0.1309 | 0.1964 | 0.2618 | 0.3273 | 0.3928 | 0.4582 | 0.5237 | 0.5891 | 0.0920 | 46 |
| 0.0657 | 0.1315 | 0.1972 | 0.2630 | 0.3287 | 0.3945 | 0.4602 | 0.5260 | 0.5917 | 0.0924 | 47 |
| 0.0660 | 0.1321 | 0.1981 | 0.2642 | 0.3302 | 0.3962 | 0.4622 | 0.5283 | 0.5943 | 0.0928 | 48 |
| 0.0663 | 0.1326 | 0.1990 | 0.2653 | 0.3316 | 0.3979 | 0.4642 | 0.5306 | 0.5969 | 0.0932 | 49 |
| 0.0666 | 0.1332 | 0.1998 | 0.2664 | 0.3331 | 0.3997 | 0.4663 | 0.5329 | 0.5995 | 0.0936 | 50 |
| 0.0669 | 0.1338 | 0.2007 | 0.2676 | 0.3345 | 0.4014 | 0.4683 | 0.5352 | 0.6021 | 0.0940 | 51 |
| 0.0672 | 0.1344 | 0.2016 | 0.2688 | 0.3359 | 0.4031 | 0.4703 | 0.5375 | 0.6047 | 0.0944 | 52 |
| 0.0675 | 0.1349 | 0.2024 | 0.2699 | 0.3374 | 0.4048 | 0.4723 | 0.5398 | 0.6073 | 0.0948 | 53 |
| 0.0678 | 0.1355 | 0.2033 | 0.2710 | 0.3388 | 0.4066 | 0.4743 | 0.5421 | 0.6099 | 0.0952 | 54 |
| 0.0681 | 0.1361 | 0.2042 | 0.2722 | 0.3403 | 0.4083 | 0.4764 | 0.5444 | 0.6125 | 0.0956 | 55 |
| 0.0683 | 0.1367 | 0.2050 | 0.2734 | 0.3417 | 0.4100 | 0.4784 | 0.5467 | 0.6151 | 0.0961 | 56 |
| 0.0686 | 0.1373 | 0.2059 | 0.2745 | 0.3431 | 0.4118 | 0.4804 | 0.5490 | 0.6177 | 0.0965 | 57 |
| 0.0689 | 0.1378 | 0.2067 | 0.2756 | 0.3446 | 0.4135 | 0.4824 | 0.5513 | 0.6202 | 0.0969 | 58 |
| 0.0692 | 0.1384 | 0.2076 | 0.2768 | 0.3460 | 0.4152 | 0.4844 | 0.5536 | 0.6228 | 0.0973 | 59 |
| 0.0695 | 0.1390 | 0.2085 | 0.2780 | 0.3474 | 0.4169 | 0.4864 | 0.5559 | 0.6254 | 0.0977 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9937 | 1.9875 | 2.9812 | 3.9750 | 4.9687 | 5.9624 | 6.9562 | 7.9499 | 8.9437 | 1.3966 |
| 01 | 0.9937 | 1.9874 | 2.9811 | 3.9748 | 4.9685 | 5.9622 | 6.9559 | 7.9496 | 8.9433 | 1.3966 |
| 02 | 0.9937 | 1.9873 | 2.9810 | 3.9746 | 4.9683 | 5.9619 | 6.9556 | 7.9493 | 8.9429 | 1.3965 |
| 03 | 0.9936 | 1.9872 | 2.9809 | 3.9745 | 4.9681 | 5.9617 | 6.9553 | 7.9489 | 8.9426 | 1.3965 |
| 04 | 0.9936 | 1.9872 | 2.9807 | 3.9743 | 4.9679 | 5.9615 | 6.9550 | 7.9486 | 8.9422 | 1.3965 |
| 05 | 0.9935 | 1.9871 | 2.9806 | 3.9741 | 4.9677 | 5.9612 | 6.9547 | 7.9483 | 8.9418 | 1.3965 |
| 06 | 0.9935 | 1.9870 | 2.9805 | 3.9740 | 4.9675 | 5.9610 | 6.9545 | 7.9479 | 8.9414 | 1.3964 |
| 07 | 0.9935 | 1.9869 | 2.9804 | 3.9738 | 4.9673 | 5.9607 | 6.9542 | 7.9476 | 8.9411 | 1.3964 |
| 08 | 0.9934 | 1.9868 | 2.9802 | 3.9736 | 4.9671 | 5.9605 | 6.9539 | 7.9473 | 8.9407 | 1.3964 |
| 09 | 0.9934 | 1.9867 | 2.9801 | 3.9735 | 4.9668 | 5.9602 | 6.9536 | 7.9470 | 8.9403 | 1.3963 |
| 10 | 0.9933 | 1.9867 | 2.9800 | 3.9734 | 4.9666 | 5.9600 | 6.9533 | 7.9466 | 8.9400 | 1.3963 |
| 11 | 0.9933 | 1.9866 | 2.9799 | 3.9731 | 4.9664 | 5.9597 | 6.9530 | 7.9463 | 8.9396 | 1.3963 |
| 12 | 0.9932 | 1.9865 | 2.9797 | 3.9730 | 4.9662 | 5.9595 | 6.9527 | 7.9459 | 8.9392 | 1.3963 |
| 13 | 0.9932 | 1.9864 | 2.9796 | 3.9728 | 4.9660 | 5.9592 | 6.9524 | 7.9456 | 8.9388 | 1.3962 |
| 14 | 0.9932 | 1.9863 | 2.9795 | 3.9726 | 4.9658 | 5.9589 | 6.9521 | 7.9452 | 8.9384 | 1.3962 |
| 15 | 0.9931 | 1.9862 | 2.9793 | 3.9725 | 4.9656 | 5.9587 | 6.9518 | 7.9449 | 8.9380 | 1.3962 |
| 16 | 0.9931 | 1.9861 | 2.9792 | 3.9723 | 4.9654 | 5.9584 | 6.9515 | 7.9446 | 8.9376 | 1.3962 |
| 17 | 0.9930 | 1.9861 | 2.9791 | 3.9721 | 4.9651 | 5.9582 | 6.9512 | 7.9442 | 8.9373 | 1.3961 |
| 18 | 0.9930 | 1.9860 | 2.9790 | 3.9719 | 4.9649 | 5.9579 | 6.9509 | 7.9439 | 8.9369 | 1.3961 |
| 19 | 0.9929 | 1.9859 | 2.9788 | 3.9718 | 4.9647 | 5.9577 | 6.9506 | 7.9435 | 8.9365 | 1.3961 |
| 20 | 0.9929 | 1.9858 | 2.9787 | 3.9716 | 4.9645 | 5.9574 | 6.9503 | 7.9432 | 8.9361 | 1.3960 |
| 21 | 0.9929 | 1.9857 | 2.9786 | 3.9714 | 4.9643 | 5.9571 | 6.9500 | 7.9428 | 8.9357 | 1.3960 |
| 22 | 0.9928 | 1.9856 | 2.9784 | 3.9712 | 4.9641 | 5.9569 | 6.9497 | 7.9425 | 8.9353 | 1.3960 |
| 23 | 0.9928 | 1.9855 | 2.9783 | 3.9711 | 4.9638 | 5.9566 | 6.9494 | 7.9421 | 8.9349 | 1.3959 |
| 24 | 0.9927 | 1.9854 | 2.9782 | 3.9709 | 4.9636 | 5.9563 | 6.9490 | 7.9418 | 8.9345 | 1.3959 |
| 25 | 0.9927 | 1.9854 | 2.9780 | 3.9707 | 4.9634 | 5.9561 | 6.9487 | 7.9414 | 8.9341 | 1.3959 |
| 26 | 0.9926 | 1.9853 | 2.9779 | 3.9705 | 4.9632 | 5.9558 | 6.9484 | 7.9410 | 8.9337 | 1.3958 |
| 27 | 0.9926 | 1.9852 | 2.9778 | 3.9703 | 4.9629 | 5.9555 | 6.9481 | 7.9407 | 8.9333 | 1.3958 |
| 28 | 0.9925 | 1.9851 | 2.9776 | 3.9702 | 4.9627 | 5.9553 | 6.9478 | 7.9403 | 8.9329 | 1.3958 |
| 29 | 0.9925 | 1.9850 | 2.9775 | 3.9700 | 4.9625 | 5.9550 | 6.9475 | 7.9400 | 8.9325 | 1.3958 |
| 30 | 0.9925 | 1.9849 | 2.9774 | 3.9698 | 4.9623 | 5.9547 | 6.9472 | 7.9396 | 8.9321 | 1.3957 |
| 31 | 0.9924 | 1.9848 | 2.9772 | 3.9696 | 4.9620 | 5.9544 | 6.9468 | 7.9393 | 8.9317 | 1.3957 |
| 32 | 0.9924 | 1.9847 | 2.9771 | 3.9694 | 4.9618 | 5.9542 | 6.9465 | 7.9389 | 8.9312 | 1.3957 |
| 33 | 0.9923 | 1.9846 | 2.9769 | 3.9693 | 4.9616 | 5.9539 | 6.9462 | 7.9385 | 8.9308 | 1.3956 |
| 34 | 0.9923 | 1.9845 | 2.9768 | 3.9691 | 4.9613 | 5.9536 | 6.9459 | 7.9381 | 8.9304 | 1.3956 |
| 35 | 0.9922 | 1.9844 | 2.9767 | 3.9689 | 4.9611 | 5.9533 | 6.9456 | 7.9378 | 8.9300 | 1.3956 |
| 36 | 0.9922 | 1.9844 | 2.9765 | 3.9687 | 4.9609 | 5.9531 | 6.9452 | 7.9374 | 8.9296 | 1.3955 |
| 37 | 0.9921 | 1.9843 | 2.9764 | 3.9685 | 4.9606 | 5.9528 | 6.9449 | 7.9370 | 8.9292 | 1.3955 |
| 38 | 0.9921 | 1.9842 | 2.9762 | 3.9683 | 4.9604 | 5.9525 | 6.9446 | 7.9367 | 8.9287 | 1.3955 |
| 39 | 0.9920 | 1.9841 | 2.9761 | 3.9681 | 4.9602 | 5.9522 | 6.9443 | 7.9363 | 8.9283 | 1.3954 |
| 40 | 0.9920 | 1.9840 | 2.9760 | 3.9680 | 4.9600 | 5.9519 | 6.9439 | 7.9359 | 8.9279 | 1.3954 |
| 41 | 0.9919 | 1.9839 | 2.9758 | 3.9678 | 4.9597 | 5.9517 | 6.9436 | 7.9355 | 8.9275 | 1.3954 |
| 42 | 0.9919 | 1.9838 | 2.9757 | 3.9676 | 4.9595 | 5.9514 | 6.9433 | 7.9352 | 8.9270 | 1.3953 |
| 43 | 0.9918 | 1.9837 | 2.9755 | 3.9674 | 4.9592 | 5.9511 | 6.9429 | 7.9348 | 8.9266 | 1.3953 |
| 44 | 0.9918 | 1.9836 | 2.9754 | 3.9672 | 4.9590 | 5.9508 | 6.9426 | 7.9344 | 8.9262 | 1.3953 |
| 45 | 0.9918 | 1.9835 | 2.9753 | 3.9670 | 4.9588 | 5.9505 | 6.9423 | 7.9340 | 8.9258 | 1.3952 |
| 46 | 0.9917 | 1.9834 | 2.9751 | 3.9668 | 4.9585 | 5.9502 | 6.9419 | 7.9336 | 8.9253 | 1.3952 |
| 47 | 0.9917 | 1.9833 | 2.9750 | 3.9666 | 4.9583 | 5.9499 | 6.9416 | 7.9332 | 8.9249 | 1.3952 |
| 48 | 0.9916 | 1.9832 | 2.9748 | 3.9664 | 4.9580 | 5.9496 | 6.9412 | 7.9329 | 8.9245 | 1.3951 |
| 49 | 0.9916 | 1.9831 | 2.9747 | 3.9662 | 4.9578 | 5.9494 | 6.9409 | 7.9325 | 8.9240 | 1.3951 |
| 50 | 0.9915 | 1.9830 | 2.9745 | 3.9660 | 4.9576 | 5.9491 | 6.9406 | 7.9321 | 8.9236 | 1.3951 |
| 51 | 0.9915 | 1.9829 | 2.9744 | 3.9658 | 4.9573 | 5.9488 | 6.9402 | 7.9317 | 8.9231 | 1.3950 |
| 52 | 0.9914 | 1.9828 | 2.9742 | 3.9656 | 4.9571 | 5.9485 | 6.9399 | 7.9313 | 8.9227 | 1.3950 |
| 53 | 0.9914 | 1.9827 | 2.9741 | 3.9654 | 4.9568 | 5.9482 | 6.9395 | 7.9309 | 8.9223 | 1.3950 |
| 54 | 0.9913 | 1.9826 | 2.9739 | 3.9653 | 4.9566 | 5.9479 | 6.9392 | 7.9305 | 8.9218 | 1.3949 |
| 55 | 0.9913 | 1.9825 | 2.9738 | 3.9651 | 4.9563 | 5.9476 | 6.9388 | 7.9301 | 8.9214 | 1.3949 |
| 56 | 0.9912 | 1.9824 | 2.9736 | 3.9649 | 4.9561 | 5.9473 | 6.9385 | 7.9297 | 8.9209 | 1.3949 |
| 57 | 0.9912 | 1.9823 | 2.9735 | 3.9647 | 4.9558 | 5.9470 | 6.9381 | 7.9293 | 8.9205 | 1.3948 |
| 58 | 0.9911 | 1.9822 | 2.9733 | 3.9645 | 4.9556 | 5.9467 | 6.9378 | 7.9289 | 8.9200 | 1.3948 |
| 59 | 0.9911 | 1.9821 | 2.9732 | 3.9643 | 4.9553 | 5.9464 | 6.9375 | 7.9285 | 8.9196 | 1.3948 |
| 60 | 0.9910 | 1.9820 | 2.9730 | 3.9641 | 4.9551 | 5.9461 | 6.9371 | 7.9281 | 8.9191 | 1.3947 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0695 | 0.1390 | 0.2085 | 0.2780 | 0.3474 | 0.4169 | 0.4864 | 0.5559 | 0.6254 | 0.0977 | 00 |
| 0.0698 | 0.1396 | 0.2093 | 0.2791 | 0.3489 | 0.4187 | 0.4884 | 0.5582 | 0.6280 | 0.0981 | 01 |
| 0.0701 | 0.1401 | 0.2102 | 0.2802 | 0.3503 | 0.4204 | 0.4904 | 0.5605 | 0.6306 | 0.0985 | 02 |
| 0.0704 | 0.1407 | 0.2111 | 0.2814 | 0.3518 | 0.4221 | 0.4925 | 0.5628 | 0.6332 | 0.0989 | 03 |
| 0.0706 | 0.1413 | 0.2119 | 0.2826 | 0.3532 | 0.4238 | 0.4945 | 0.5651 | 0.6358 | 0.0993 | 04 |
| 0.0709 | 0.1419 | 0.2128 | 0.2837 | 0.3546 | 0.4255 | 0.4965 | 0.5674 | 0.6384 | 0.0997 | 05 |
| 0.0712 | 0.1424 | 0.2136 | 0.2848 | 0.3561 | 0.4273 | 0.4985 | 0.5697 | 0.6409 | 0.1001 | 06 |
| 0.0715 | 0.1430 | 0.2145 | 0.2860 | 0.3575 | 0.4290 | 0.5005 | 0.5720 | 0.6435 | 0.1005 | 07 |
| 0.0718 | 0.1436 | 0.2154 | 0.2872 | 0.3589 | 0.4307 | 0.5025 | 0.5743 | 0.6461 | 0.1009 | 08 |
| 0.0721 | 0.1442 | 0.2162 | 0.2883 | 0.3604 | 0.4325 | 0.5045 | 0.5766 | 0.6487 | 0.1013 | 09 |
| 0.0724 | 0.1447 | 0.2171 | 0.2894 | 0.3618 | 0.4342 | 0.5065 | 0.5789 | 0.6513 | 0.1017 | 10 |
| 0.0727 | 0.1453 | 0.2180 | 0.2906 | 0.3633 | 0.4359 | 0.5086 | 0.5812 | 0.6539 | 0.1021 | 11 |
| 0.0729 | 0.1459 | 0.2188 | 0.2918 | 0.3647 | 0.4376 | 0.5106 | 0.5835 | 0.6565 | 0.1025 | 12 |
| 0.0732 | 0.1465 | 0.2197 | 0.2929 | 0.3661 | 0.4394 | 0.5126 | 0.5858 | 0.6591 | 0.1029 | 13 |
| 0.0735 | 0.1470 | 0.2205 | 0.2940 | 0.3676 | 0.4411 | 0.5146 | 0.5881 | 0.6616 | 0.1033 | 14 |
| 0.0738 | 0.1476 | 0.2214 | 0.2952 | 0.3690 | 0.4428 | 0.5166 | 0.5904 | 0.6642 | 0.1037 | 15 |
| 0.0741 | 0.1482 | 0.2223 | 0.2964 | 0.3704 | 0.4445 | 0.5186 | 0.5927 | 0.6668 | 0.1041 | 16 |
| 0.0744 | 0.1488 | 0.2231 | 0.2975 | 0.3719 | 0.4463 | 0.5206 | 0.5950 | 0.6694 | 0.1046 | 17 |
| 0.0747 | 0.1493 | 0.2240 | 0.2986 | 0.3733 | 0.4480 | 0.5226 | 0.5973 | 0.6720 | 0.1050 | 18 |
| 0.0749 | 0.1499 | 0.2248 | 0.2998 | 0.3747 | 0.4497 | 0.5246 | 0.5996 | 0.6746 | 0.1054 | 19 |
| 0.0752 | 0.1505 | 0.2257 | 0.3010 | 0.3762 | 0.4514 | 0.5266 | 0.6019 | 0.6772 | 0.1058 | 20 |
| 0.0755 | 0.1510 | 0.2266 | 0.3021 | 0.3776 | 0.4531 | 0.5286 | 0.6042 | 0.6797 | 0.1062 | 21 |
| 0.0758 | 0.1516 | 0.2274 | 0.3032 | 0.3791 | 0.4549 | 0.5307 | 0.6065 | 0.6823 | 0.1066 | 22 |
| 0.0761 | 0.1522 | 0.2283 | 0.3044 | 0.3805 | 0.4566 | 0.5327 | 0.6088 | 0.6849 | 0.1070 | 23 |
| 0.0764 | 0.1528 | 0.2292 | 0.3056 | 0.3819 | 0.4583 | 0.5347 | 0.6111 | 0.6875 | 0.1074 | 24 |
| 0.0767 | 0.1533 | 0.2300 | 0.3067 | 0.3834 | 0.4600 | 0.5367 | 0.6134 | 0.6900 | 0.1078 | 25 |
| 0.0770 | 0.1539 | 0.2309 | 0.3078 | 0.3848 | 0.4618 | 0.5387 | 0.6157 | 0.6926 | 0.1082 | 26 |
| 0.0772 | 0.1545 | 0.2317 | 0.3090 | 0.3862 | 0.4635 | 0.5407 | 0.6180 | 0.6952 | 0.1086 | 27 |
| 0.0775 | 0.1551 | 0.2326 | 0.3101 | 0.3877 | 0.4652 | 0.5427 | 0.6203 | 0.6978 | 0.1090 | 28 |
| 0.0778 | 0.1556 | 0.2335 | 0.3113 | 0.3891 | 0.4669 | 0.5447 | 0.6226 | 0.7004 | 0.1094 | 29 |
| 0.0781 | 0.1562 | 0.2343 | 0.3124 | 0.3905 | 0.4687 | 0.5467 | 0.6249 | 0.7030 | 0.1098 | 30 |
| 0.0784 | 0.1568 | 0.2352 | 0.3136 | 0.3920 | 0.4703 | 0.5487 | 0.6271 | 0.7055 | 0.1102 | 31 |
| 0.0787 | 0.1574 | 0.2360 | 0.3147 | 0.3934 | 0.4721 | 0.5508 | 0.6294 | 0.7081 | 0.1107 | 32 |
| 0.0790 | 0.1579 | 0.2369 | 0.3159 | 0.3948 | 0.4738 | 0.5528 | 0.6318 | 0.7107 | 0.1111 | 33 |
| 0.0793 | 0.1585 | 0.2378 | 0.3170 | 0.3963 | 0.4755 | 0.5548 | 0.6340 | 0.7133 | 0.1115 | 34 |
| 0.0795 | 0.1591 | 0.2386 | 0.3182 | 0.3977 | 0.4772 | 0.5568 | 0.6363 | 0.7159 | 0.1119 | 35 |
| 0.0798 | 0.1597 | 0.2395 | 0.3193 | 0.3991 | 0.4790 | 0.5588 | 0.6386 | 0.7185 | 0.1123 | 36 |
| 0.0801 | 0.1602 | 0.2403 | 0.3204 | 0.4007 | 0.4807 | 0.5608 | 0.6409 | 0.7210 | 0.1127 | 37 |
| 0.0804 | 0.1608 | 0.2412 | 0.3216 | 0.4020 | 0.4824 | 0.5628 | 0.6432 | 0.7236 | 0.1131 | 38 |
| 0.0807 | 0.1614 | 0.2421 | 0.3228 | 0.4034 | 0.4841 | 0.5648 | 0.6455 | 0.7262 | 0.1135 | 39 |
| 0.0810 | 0.1620 | 0.2429 | 0.3239 | 0.4049 | 0.4859 | 0.5668 | 0.6478 | 0.7288 | 0.1139 | 40 |
| 0.0813 | 0.1625 | 0.2438 | 0.3250 | 0.4063 | 0.4876 | 0.5688 | 0.6501 | 0.7313 | 0.1143 | 41 |
| 0.0815 | 0.1631 | 0.2446 | 0.3262 | 0.4077 | 0.4893 | 0.5708 | 0.6524 | 0.7339 | 0.1147 | 42 |
| 0.0818 | 0.1637 | 0.2455 | 0.3273 | 0.4092 | 0.4910 | 0.5728 | 0.6546 | 0.7365 | 0.1151 | 43 |
| 0.0821 | 0.1642 | 0.2464 | 0.3285 | 0.4106 | 0.4927 | 0.5748 | 0.6570 | 0.7391 | 0.1155 | 44 |
| 0.0824 | 0.1648 | 0.2472 | 0.3296 | 0.4120 | 0.4945 | 0.5768 | 0.6593 | 0.7417 | 0.1159 | 45 |
| 0.0827 | 0.1654 | 0.2481 | 0.3308 | 0.4135 | 0.4961 | 0.5788 | 0.6615 | 0.7442 | 0.1163 | 46 |
| 0.0830 | 0.1660 | 0.2489 | 0.3319 | 0.4149 | 0.4979 | 0.5809 | 0.6638 | 0.7468 | 0.1167 | 47 |
| 0.0833 | 0.1665 | 0.2498 | 0.3331 | 0.4163 | 0.4996 | 0.5829 | 0.6662 | 0.7494 | 0.1171 | 48 |
| 0.0836 | 0.1671 | 0.2507 | 0.3342 | 0.4178 | 0.5013 | 0.5849 | 0.6684 | 0.7520 | 0.1176 | 49 |
| 0.0838 | 0.1677 | 0.2515 | 0.3354 | 0.4192 | 0.5030 | 0.5869 | 0.6707 | 0.7546 | 0.1180 | 50 |
| 0.0841 | 0.1683 | 0.2524 | 0.3365 | 0.4206 | 0.5048 | 0.5889 | 0.6730 | 0.7572 | 0.1184 | 51 |
| 0.0844 | 0.1688 | 0.2532 | 0.3376 | 0.4221 | 0.5065 | 0.5909 | 0.6753 | 0.7597 | 0.1188 | 52 |
| 0.0847 | 0.1694 | 0.2541 | 0.3388 | 0.4235 | 0.5082 | 0.5929 | 0.6776 | 0.7623 | 0.1192 | 53 |
| 0.0850 | 0.1700 | 0.2549 | 0.3399 | 0.4249 | 0.5099 | 0.5949 | 0.6798 | 0.7648 | 0.1196 | 54 |
| 0.0853 | 0.1705 | 0.2558 | 0.3411 | 0.4264 | 0.5116 | 0.5969 | 0.6822 | 0.7674 | 0.1200 | 55 |
| 0.0856 | 0.1711 | 0.2567 | 0.3422 | 0.4278 | 0.5134 | 0.5989 | 0.6845 | 0.7700 | 0.1204 | 56 |
| 0.0858 | 0.1717 | 0.2575 | 0.3434 | 0.4292 | 0.5150 | 0.6009 | 0.6867 | 0.7726 | 0.1208 | 57 |
| 0.0861 | 0.1723 | 0.2584 | 0.3445 | 0.4306 | 0.5168 | 0.6029 | 0.6890 | 0.7752 | 0.1212 | 58 |
| 0.0864 | 0.1728 | 0.2593 | 0.3457 | 0.4321 | 0.5185 | 0.6049 | 0.6914 | 0.7778 | 0.1216 | 59 |
| 0.0867 | 0.1734 | 0.2601 | 0.3468 | 0.4335 | 0.5202 | 0.6069 | 0.6936 | 0.7803 | 0.1220 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9910 | 1.9820 | 2.9730 | 3.9641 | 4.9551 | 5.9461 | 6.9371 | 7.9281 | 8.9191 | 1.3947 |
| 01 | 0.9910 | 1.9819 | 2.9729 | 3.9639 | 4.9548 | 5.9458 | 6.9367 | 7.9277 | 8.9187 | 1.3947 |
| 02 | 0.9909 | 1.9818 | 2.9727 | 3.9636 | 4.9546 | 5.9455 | 6.9364 | 7.9273 | 8.9182 | 1.3946 |
| 03 | 0.9909 | 1.9817 | 2.9726 | 3.9634 | 4.9543 | 5.9452 | 6.9360 | 7.9269 | 8.9177 | 1.3946 |
| 04 | 0.9908 | 1.9816 | 2.9724 | 3.9632 | 4.9541 | 5.9449 | 6.9357 | 7.9265 | 8.9173 | 1.3946 |
| 05 | 0.9908 | 1.9815 | 2.9723 | 3.9630 | 4.9538 | 5.9446 | 6.9353 | 7.9261 | 8.9168 | 1.3945 |
| 06 | 0.9907 | 1.9814 | 2.9721 | 3.9628 | 4.9535 | 5.9442 | 6.9349 | 7.9257 | 8.9164 | 1.3945 |
| 07 | 0.9907 | 1.9813 | 2.9720 | 3.9626 | 4.9533 | 5.9439 | 6.9346 | 7.9252 | 8.9159 | 1.3944 |
| 08 | 0.9906 | 1.9812 | 2.9718 | 3.9624 | 4.9530 | 5.9436 | 6.9342 | 7.9248 | 8.9154 | 1.3944 |
| 09 | 0.9906 | 1.9811 | 2.9717 | 3.9622 | 4.9528 | 5.9433 | 6.9339 | 7.9244 | 8.9150 | 1.3944 |
| 10 | 0.9905 | 1.9810 | 2.9715 | 3.9620 | 4.9525 | 5.9430 | 6.9335 | 7.9240 | 8.9145 | 1.3943 |
| 11 | 0.9904 | 1.9809 | 2.9713 | 3.9618 | 4.9522 | 5.9427 | 6.9331 | 7.9236 | 8.9140 | 1.3943 |
| 12 | 0.9904 | 1.9808 | 2.9712 | 3.9616 | 4.9520 | 5.9424 | 6.9328 | 7.9232 | 8.9136 | 1.3942 |
| 13 | 0.9903 | 1.9807 | 2.9710 | 3.9614 | 4.9517 | 5.9421 | 6.9324 | 7.9227 | 8.9131 | 1.3942 |
| 14 | 0.9903 | 1.9806 | 2.9709 | 3.9612 | 4.9515 | 5.9417 | 6.9320 | 7.9223 | 8.9126 | 1.3941 |
| 15 | 0.9902 | 1.9805 | 2.9707 | 3.9610 | 4.9512 | 5.9414 | 6.9317 | 7.9219 | 8.9121 | 1.3941 |
| 16 | 0.9902 | 1.9804 | 2.9706 | 3.9607 | 4.9509 | 5.9411 | 6.9313 | 7.9215 | 8.9117 | 1.3941 |
| 17 | 0.9901 | 1.9803 | 2.9704 | 3.9605 | 4.9507 | 5.9408 | 6.9309 | 7.9211 | 8.9112 | 1.3940 |
| 18 | 0.9901 | 1.9802 | 2.9702 | 3.9603 | 4.9504 | 5.9405 | 6.9306 | 7.9206 | 8.9107 | 1.3940 |
| 19 | 0.9900 | 1.9801 | 2.9701 | 3.9601 | 4.9501 | 5.9402 | 6.9302 | 7.9202 | 8.9102 | 1.3940 |
| 20 | 0.9900 | 1.9799 | 2.9699 | 3.9599 | 4.9499 | 5.9398 | 6.9298 | 7.9198 | 8.9098 | 1.3939 |
| 21 | 0.9899 | 1.9798 | 2.9698 | 3.9597 | 4.9496 | 5.9395 | 6.9294 | 7.9193 | 8.9093 | 1.3939 |
| 22 | 0.9899 | 1.9797 | 2.9696 | 3.9595 | 4.9493 | 5.9392 | 6.9290 | 7.9189 | 8.9088 | 1.3938 |
| 23 | 0.9898 | 1.9796 | 2.9694 | 3.9592 | 4.9490 | 5.9387 | 6.9287 | 7.9185 | 8.9083 | 1.3938 |
| 24 | 0.9898 | 1.9795 | 2.9693 | 3.9590 | 4.9488 | 5.9385 | 6.9283 | 7.9180 | 8.9078 | 1.3938 |
| 25 | 0.9897 | 1.9794 | 2.9691 | 3.9588 | 4.9485 | 5.9382 | 6.9279 | 7.9176 | 8.9073 | 1.3937 |
| 26 | 0.9896 | 1.9793 | 2.9689 | 3.9586 | 4.9482 | 5.9379 | 6.9275 | 7.9172 | 8.9068 | 1.3937 |
| 27 | 0.9896 | 1.9792 | 2.9688 | 3.9584 | 4.9480 | 5.9375 | 6.9271 | 7.9167 | 8.9063 | 1.3936 |
| 28 | 0.9895 | 1.9791 | 2.9686 | 3.9581 | 4.9477 | 5.9372 | 6.9268 | 7.9163 | 8.9058 | 1.3936 |
| 29 | 0.9895 | 1.9790 | 2.9684 | 3.9579 | 4.9474 | 5.9369 | 6.9264 | 7.9159 | 8.9053 | 1.3936 |
| 30 | 0.9894 | 1.9789 | 2.9683 | 3.9577 | 4.9471 | 5.9366 | 6.9260 | 7.9154 | 8.9048 | 1.3935 |
| 31 | 0.9894 | 1.9787 | 2.9681 | 3.9575 | 4.9469 | 5.9362 | 6.9256 | 7.9150 | 8.9043 | 1.3935 |
| 32 | 0.9893 | 1.9786 | 2.9679 | 3.9573 | 4.9466 | 5.9359 | 6.9252 | 7.9145 | 8.9038 | 1.3934 |
| 33 | 0.9893 | 1.9783 | 2.9678 | 3.9570 | 4.9463 | 5.9355 | 6.9248 | 7.9141 | 8.9033 | 1.3934 |
| 34 | 0.9892 | 1.9784 | 2.9676 | 3.9568 | 4.9460 | 5.9352 | 6.9244 | 7.9136 | 8.9028 | 1.3934 |
| 35 | 0.9891 | 1.9783 | 2.9674 | 3.9566 | 4.9457 | 5.9349 | 6.9240 | 7.9132 | 8.9023 | 1.3933 |
| 36 | 0.9891 | 1.9782 | 2.9673 | 3.9564 | 4.9454 | 5.9345 | 6.9236 | 7.9127 | 8.9018 | 1.3933 |
| 37 | 0.9890 | 1.9781 | 2.9671 | 3.9561 | 4.9452 | 5.9342 | 6.9232 | 7.9123 | 8.9013 | 1.3932 |
| 38 | 0.9890 | 1.9780 | 2.9669 | 3.9559 | 4.9449 | 5.9339 | 6.9228 | 7.9118 | 8.9008 | 1.3932 |
| 39 | 0.9889 | 1.9778 | 2.9668 | 3.9557 | 4.9446 | 5.9335 | 6.9224 | 7.9114 | 8.9003 | 1.3932 |
| 40 | 0.9889 | 1.9777 | 2.9666 | 3.9555 | 4.9443 | 5.9332 | 6.9220 | 7.9109 | 8.9098 | 1.3931 |
| 41 | 0.9888 | 1.9776 | 2.9664 | 3.9552 | 4.9440 | 5.9328 | 6.9216 | 7.9104 | 8.9093 | 1.3931 |
| 42 | 0.9887 | 1.9775 | 2.9662 | 3.9550 | 4.9437 | 5.9325 | 6.9212 | 7.9100 | 8.9087 | 1.3930 |
| 43 | 0.9887 | 1.9774 | 2.9661 | 3.9548 | 4.9435 | 5.9321 | 6.9208 | 7.9095 | 8.9082 | 1.3930 |
| 44 | 0.9886 | 1.9773 | 2.9659 | 3.9545 | 4.9432 | 5.9318 | 6.9204 | 7.9091 | 8.9077 | 1.3930 |
| 45 | 0.9886 | 1.9772 | 2.9657 | 3.9543 | 4.9429 | 5.9315 | 6.9200 | 7.9086 | 8.9072 | 1.3929 |
| 46 | 0.9885 | 1.9770 | 2.9656 | 3.9541 | 4.9426 | 5.9311 | 6.9196 | 7.9081 | 8.9067 | 1.3929 |
| 47 | 0.9885 | 1.9769 | 2.9654 | 3.9538 | 4.9423 | 5.9308 | 6.9192 | 7.9077 | 8.9061 | 1.3928 |
| 48 | 0.9884 | 1.9768 | 2.9652 | 3.9536 | 4.9420 | 5.9304 | 6.9188 | 7.9072 | 8.9056 | 1.3928 |
| 49 | 0.9883 | 1.9767 | 2.9650 | 3.9534 | 4.9417 | 5.9300 | 6.9184 | 7.9067 | 8.9051 | 1.3928 |
| 50 | 0.9883 | 1.9766 | 2.9649 | 3.9531 | 4.9414 | 5.9297 | 6.9180 | 7.9063 | 8.9046 | 1.3927 |
| 51 | 0.9882 | 1.9765 | 2.9647 | 3.9529 | 4.9411 | 5.9294 | 6.9176 | 7.9058 | 8.9040 | 1.3927 |
| 52 | 0.9882 | 1.9763 | 2.9645 | 3.9527 | 4.9408 | 5.9290 | 6.9172 | 7.9053 | 8.9035 | 1.3926 |
| 53 | 0.9881 | 1.9762 | 2.9643 | 3.9524 | 4.9405 | 5.9286 | 6.9167 | 7.9048 | 8.9030 | 1.3926 |
| 54 | 0.9880 | 1.9761 | 2.9641 | 3.9522 | 4.9402 | 5.9283 | 6.9163 | 7.9044 | 8.9024 | 1.3926 |
| 55 | 0.9880 | 1.9760 | 2.9640 | 3.9519 | 4.9399 | 5.9279 | 6.9159 | 7.9039 | 8.9019 | 1.3925 |
| 56 | 0.9879 | 1.9759 | 2.9638 | 3.9517 | 4.9396 | 5.9276 | 6.9155 | 7.9034 | 8.9013 | 1.3925 |
| 57 | 0.9879 | 1.9757 | 2.9636 | 3.9515 | 4.9393 | 5.9272 | 6.9151 | 7.9029 | 8.9008 | 1.3924 |
| 58 | 0.9878 | 1.9756 | 2.9634 | 3.9512 | 4.9390 | 5.9268 | 6.9147 | 7.9025 | 8.9003 | 1.3924 |
| 59 | 0.9877 | 1.9755 | 2.9632 | 3.9510 | 4.9387 | 5.9265 | 6.9142 | 7.9020 | 8.9007 | 1.3924 |
| 60 | 0.9877 | 1.9754 | 2.9631 | 3.9508 | 4.9384 | 5.9261 | 6.9138 | 7.9015 | 8.9002 | 1.3923 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.0867 | 0.1734 | 0.2601 | 0.3468 | 0.4335 | 0.5202 | 0.6069 | 0.6936 | 0.7803 | 0.1220 | 00 |
| 0.0870 | 0.1740 | 0.2610 | 0.3480 | 0.4349 | 0.5219 | 0.6089 | 0.6959 | 0.7829 | 0.1224 | 01 |
| 0.0873 | 0.1745 | 0.2618 | 0.3491 | 0.4364 | 0.5236 | 0.6109 | 0.6982 | 0.7854 | 0.1228 | 02 |
| 0.0876 | 0.1751 | 0.2627 | 0.3502 | 0.4378 | 0.5254 | 0.6129 | 0.7005 | 0.7880 | 0.1232 | 03 |
| 0.0878 | 0.1757 | 0.2635 | 0.3514 | 0.4392 | 0.5271 | 0.6149 | 0.7028 | 0.7906 | 0.1236 | 04 |
| 0.0881 | 0.1763 | 0.2644 | 0.3525 | 0.4407 | 0.5288 | 0.6169 | 0.7050 | 0.7932 | 0.1240 | 05 |
| 0.0884 | 0.1768 | 0.2653 | 0.3537 | 0.4421 | 0.5305 | 0.6189 | 0.7074 | 0.7958 | 0.1244 | 06 |
| 0.0887 | 0.1774 | 0.2661 | 0.3548 | 0.4435 | 0.5322 | 0.6209 | 0.7096 | 0.7983 | 0.1248 | 07 |
| 0.0890 | 0.1780 | 0.2670 | 0.3560 | 0.4450 | 0.5339 | 0.6229 | 0.7119 | 0.8009 | 0.1253 | 08 |
| 0.0893 | 0.1786 | 0.2678 | 0.3571 | 0.4464 | 0.5357 | 0.6249 | 0.7142 | 0.8035 | 0.1257 | 09 |
| 0.0896 | 0.1791 | 0.2687 | 0.3582 | 0.4478 | 0.5374 | 0.6269 | 0.7165 | 0.8060 | 0.1261 | 10 |
| 0.0898 | 0.1797 | 0.2695 | 0.3594 | 0.4492 | 0.5391 | 0.6289 | 0.7188 | 0.8086 | 0.1265 | 11 |
| 0.0901 | 0.1803 | 0.2704 | 0.3605 | 0.4507 | 0.5408 | 0.6309 | 0.7211 | 0.8112 | 0.1269 | 12 |
| 0.0904 | 0.1808 | 0.2713 | 0.3617 | 0.4521 | 0.5425 | 0.6329 | 0.7234 | 0.8138 | 0.1273 | 13 |
| 0.0907 | 0.1814 | 0.2721 | 0.3628 | 0.4535 | 0.5442 | 0.6349 | 0.7257 | 0.8163 | 0.1277 | 14 |
| 0.0910 | 0.1820 | 0.2730 | 0.3640 | 0.4550 | 0.5459 | 0.6369 | 0.7279 | 0.8189 | 0.1281 | 15 |
| 0.0913 | 0.1826 | 0.2738 | 0.3651 | 0.4564 | 0.5477 | 0.6389 | 0.7302 | 0.8215 | 0.1285 | 16 |
| 0.0916 | 0.1831 | 0.2747 | 0.3662 | 0.4578 | 0.5494 | 0.6409 | 0.7325 | 0.8240 | 0.1289 | 17 |
| 0.0918 | 0.1837 | 0.2755 | 0.3674 | 0.4592 | 0.5511 | 0.6429 | 0.7348 | 0.8266 | 0.1293 | 18 |
| 0.0921 | 0.1843 | 0.2764 | 0.3685 | 0.4607 | 0.5528 | 0.6449 | 0.7371 | 0.8292 | 0.1297 | 19 |
| 0.0924 | 0.1848 | 0.2773 | 0.3697 | 0.4621 | 0.5545 | 0.6469 | 0.7394 | 0.8318 | 0.1301 | 20 |
| 0.0927 | 0.1854 | 0.2781 | 0.3708 | 0.4635 | 0.5562 | 0.6489 | 0.7416 | 0.8343 | 0.1305 | 21 |
| 0.0930 | 0.1860 | 0.2790 | 0.3720 | 0.4649 | 0.5579 | 0.6509 | 0.7439 | 0.8369 | 0.1309 | 22 |
| 0.0933 | 0.1865 | 0.2798 | 0.3731 | 0.4664 | 0.5596 | 0.6529 | 0.7462 | 0.8394 | 0.1313 | 23 |
| 0.0936 | 0.1871 | 0.2807 | 0.3742 | 0.4678 | 0.5614 | 0.6549 | 0.7485 | 0.8420 | 0.1317 | 24 |
| 0.0938 | 0.1877 | 0.2815 | 0.3754 | 0.4692 | 0.5631 | 0.6569 | 0.7507 | 0.8446 | 0.1321 | 25 |
| 0.0941 | 0.1883 | 0.2824 | 0.3765 | 0.4706 | 0.5648 | 0.6589 | 0.7530 | 0.8472 | 0.1326 | 26 |
| 0.0944 | 0.1888 | 0.2833 | 0.3777 | 0.4721 | 0.5665 | 0.6609 | 0.7553 | 0.8498 | 0.1330 | 27 |
| 0.0947 | 0.1894 | 0.2841 | 0.3788 | 0.4735 | 0.5682 | 0.6629 | 0.7576 | 0.8523 | 0.1334 | 28 |
| 0.0950 | 0.1900 | 0.2850 | 0.3800 | 0.4749 | 0.5699 | 0.6649 | 0.7599 | 0.8549 | 0.1338 | 29 |
| 0.0953 | 0.1905 | 0.2858 | 0.3811 | 0.4764 | 0.5716 | 0.6669 | 0.7622 | 0.8574 | 0.1342 | 30 |
| 0.0956 | 0.1911 | 0.2867 | 0.3822 | 0.4778 | 0.5734 | 0.6689 | 0.7645 | 0.8600 | 0.1346 | 31 |
| 0.0958 | 0.1917 | 0.2875 | 0.3834 | 0.4792 | 0.5751 | 0.6709 | 0.7667 | 0.8626 | 0.1350 | 32 |
| 0.0961 | 0.1923 | 0.2884 | 0.3845 | 0.4806 | 0.5768 | 0.6729 | 0.7690 | 0.8652 | 0.1354 | 33 |
| 0.0964 | 0.1928 | 0.2892 | 0.3856 | 0.4820 | 0.5785 | 0.6749 | 0.7713 | 0.8677 | 0.1358 | 34 |
| 0.0967 | 0.1934 | 0.2901 | 0.3868 | 0.4835 | 0.5802 | 0.6769 | 0.7736 | 0.8703 | 0.1362 | 35 |
| 0.0970 | 0.1940 | 0.2909 | 0.3879 | 0.4849 | 0.5819 | 0.6789 | 0.7759 | 0.8728 | 0.1366 | 36 |
| 0.0973 | 0.1945 | 0.2918 | 0.3891 | 0.4863 | 0.5836 | 0.6809 | 0.7782 | 0.8754 | 0.1370 | 37 |
| 0.0976 | 0.1951 | 0.2927 | 0.3902 | 0.4878 | 0.5853 | 0.6829 | 0.7804 | 0.8780 | 0.1374 | 38 |
| 0.0978 | 0.1957 | 0.2935 | 0.3914 | 0.4892 | 0.5870 | 0.6849 | 0.7827 | 0.8806 | 0.1378 | 39 |
| 0.0981 | 0.1962 | 0.2944 | 0.3925 | 0.4906 | 0.5887 | 0.6869 | 0.7850 | 0.8831 | 0.1382 | 40 |
| 0.0984 | 0.1968 | 0.2952 | 0.3936 | 0.4920 | 0.5905 | 0.6889 | 0.7873 | 0.8857 | 0.1386 | 41 |
| 0.0987 | 0.1974 | 0.2961 | 0.3948 | 0.4935 | 0.5921 | 0.6908 | 0.7895 | 0.8882 | 0.1390 | 42 |
| 0.0990 | 0.1979 | 0.2969 | 0.3959 | 0.4948 | 0.5938 | 0.6928 | 0.7918 | 0.8907 | 0.1395 | 43 |
| 0.0993 | 0.1985 | 0.2978 | 0.3970 | 0.4963 | 0.5956 | 0.6948 | 0.7941 | 0.8933 | 0.1399 | 44 |
| 0.0995 | 0.1991 | 0.2986 | 0.3982 | 0.4977 | 0.5973 | 0.6968 | 0.7963 | 0.8959 | 0.1403 | 45 |
| 0.0998 | 0.1997 | 0.2995 | 0.3993 | 0.4991 | 0.5990 | 0.6988 | 0.7986 | 0.8985 | 0.1407 | 46 |
| 0.1001 | 0.2002 | 0.3003 | 0.4004 | 0.5006 | 0.6007 | 0.7008 | 0.8009 | 0.9010 | 0.1411 | 47 |
| 0.1004 | 0.2008 | 0.3012 | 0.4016 | 0.5020 | 0.6024 | 0.7028 | 0.8032 | 0.9036 | 0.1415 | 48 |
| 0.1007 | 0.2014 | 0.3020 | 0.4027 | 0.5034 | 0.6041 | 0.7048 | 0.8054 | 0.9061 | 0.1419 | 49 |
| 0.1010 | 0.2019 | 0.3029 | 0.4039 | 0.5049 | 0.6058 | 0.7068 | 0.8078 | 0.9087 | 0.1423 | 50 |
| 0.1013 | 0.2025 | 0.3038 | 0.4050 | 0.5063 | 0.6075 | 0.7088 | 0.8100 | 0.9113 | 0.1427 | 51 |
| 0.1015 | 0.2031 | 0.3046 | 0.4062 | 0.5077 | 0.6092 | 0.7108 | 0.8123 | 0.9139 | 0.1431 | 52 |
| 0.1018 | 0.2036 | 0.3055 | 0.4073 | 0.5091 | 0.6109 | 0.7127 | 0.8146 | 0.9164 | 0.1435 | 53 |
| 0.1021 | 0.2042 | 0.3063 | 0.4084 | 0.5105 | 0.6126 | 0.7147 | 0.8168 | 0.9189 | 0.1439 | 54 |
| 0.1024 | 0.2048 | 0.3072 | 0.4096 | 0.5119 | 0.6143 | 0.7167 | 0.8191 | 0.9215 | 0.1443 | 55 |
| 0.1027 | 0.2053 | 0.3080 | 0.4107 | 0.5134 | 0.6160 | 0.7187 | 0.8214 | 0.9240 | 0.1447 | 56 |
| 0.1030 | 0.2059 | 0.3089 | 0.4118 | 0.5148 | 0.6177 | 0.7207 | 0.8237 | 0.9266 | 0.1451 | 57 |
| 0.1032 | 0.2065 | 0.3097 | 0.4130 | 0.5162 | 0.6194 | 0.7227 | 0.8259 | 0.9292 | 0.1455 | 58 |
| 0.1035 | 0.2071 | 0.3106 | 0.4141 | 0.5176 | 0.6212 | 0.7247 | 0.8282 | 0.9318 | 0.1459 | 59 |
| 0.1038 | 0.2076 | 0.3114 | 0.4153 | 0.5191 | 0.6229 | 0.7267 | 0.8305 | 0.9343 | 0.1463 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9877 | 1.9754 | 2.9631 | 3.9508 | 4.9384 | 5.9261 | 6.9138 | 7.9015 | 8.8892 | 1.3923 |
| 01 | 0.9876 | 1.9753 | 2.9629 | 3.9505 | 4.9381 | 5.9258 | 6.9134 | 7.9010 | 8.8887 | 1.3923 |
| 02 | 0.9876 | 1.9751 | 2.9627 | 3.9503 | 4.9378 | 5.9254 | 6.9130 | 7.9005 | 8.8881 | 1.3922 |
| 03 | 0.9875 | 1.9750 | 2.9625 | 3.9500 | 4.9375 | 5.9250 | 6.9125 | 7.9000 | 8.8875 | 1.3922 |
| 04 | 0.9874 | 1.9749 | 2.9623 | 3.9498 | 4.9372 | 5.9247 | 6.9121 | 7.8996 | 8.8870 | 1.3921 |
| 05 | 0.9874 | 1.9748 | 2.9621 | 3.9495 | 4.9369 | 5.9243 | 6.9117 | 7.8991 | 8.8864 | 1.3921 |
| 06 | 0.9873 | 1.9746 | 2.9620 | 3.9493 | 4.9366 | 5.9239 | 6.9113 | 7.8986 | 8.8859 | 1.3921 |
| 07 | 0.9873 | 1.9745 | 2.9618 | 3.9490 | 4.9363 | 5.9236 | 6.9108 | 7.8981 | 8.8853 | 1.3920 |
| 08 | 0.9872 | 1.9744 | 2.9616 | 3.9488 | 4.9360 | 5.9232 | 6.9104 | 7.8976 | 8.8848 | 1.3920 |
| 09 | 0.9871 | 1.9743 | 2.9614 | 3.9486 | 4.9357 | 5.9228 | 6.9100 | 7.8971 | 8.8842 | 1.3919 |
| 10 | 0.9871 | 1.9742 | 2.9612 | 3.9483 | 4.9354 | 5.9225 | 6.9095 | 7.8966 | 8.8837 | 1.3919 |
| 11 | 0.9870 | 1.9740 | 2.9610 | 3.9481 | 4.9351 | 5.9221 | 6.9091 | 7.8961 | 8.8831 | 1.3919 |
| 12 | 0.9870 | 1.9739 | 2.9609 | 3.9478 | 4.9348 | 5.9217 | 6.9087 | 7.8955 | 8.8826 | 1.3918 |
| 13 | 0.9869 | 1.9738 | 2.9607 | 3.9476 | 4.9344 | 5.9213 | 6.9082 | 7.8951 | 8.8820 | 1.3918 |
| 14 | 0.9868 | 1.9737 | 2.9605 | 3.9473 | 4.9341 | 5.9210 | 6.9078 | 7.8946 | 8.8814 | 1.3917 |
| 15 | 0.9868 | 1.9735 | 2.9603 | 3.9471 | 4.9338 | 5.9206 | 6.9073 | 7.8941 | 8.8809 | 1.3917 |
| 16 | 0.9867 | 1.9734 | 2.9601 | 3.9468 | 4.9335 | 5.9202 | 6.9069 | 7.8936 | 8.8803 | 1.3917 |
| 17 | 0.9866 | 1.9733 | 2.9599 | 3.9465 | 4.9332 | 5.9198 | 6.9065 | 7.8931 | 8.8797 | 1.3916 |
| 18 | 0.9866 | 1.9732 | 2.9597 | 3.9463 | 4.9329 | 5.9195 | 6.9060 | 7.8926 | 8.8792 | 1.3916 |
| 19 | 0.9865 | 1.9730 | 2.9595 | 3.9460 | 4.9326 | 5.9191 | 6.9056 | 7.8921 | 8.8786 | 1.3915 |
| 20 | 0.9864 | 1.9729 | 2.9593 | 3.9458 | 4.9322 | 5.9187 | 6.9051 | 7.8916 | 8.8780 | 1.3915 |
| 21 | 0.9864 | 1.9728 | 2.9592 | 3.9455 | 4.9319 | 5.9183 | 6.9047 | 7.8911 | 8.8775 | 1.3915 |
| 22 | 0.9863 | 1.9726 | 2.9590 | 3.9453 | 4.9316 | 5.9179 | 6.9042 | 7.8906 | 8.8769 | 1.3914 |
| 23 | 0.9863 | 1.9725 | 2.9588 | 3.9450 | 4.9313 | 5.9175 | 6.9038 | 7.8900 | 8.8763 | 1.3914 |
| 24 | 0.9862 | 1.9724 | 2.9586 | 3.9448 | 4.9310 | 5.9171 | 6.9033 | 7.8895 | 8.8757 | 1.3913 |
| 25 | 0.9861 | 1.9723 | 2.9584 | 3.9445 | 4.9306 | 5.9168 | 6.9029 | 7.8890 | 8.8751 | 1.3913 |
| 26 | 0.9861 | 1.9721 | 2.9582 | 3.9442 | 4.9303 | 5.9164 | 6.9024 | 7.8885 | 8.8745 | 1.3913 |
| 27 | 0.9860 | 1.9720 | 2.9580 | 3.9440 | 4.9300 | 5.9160 | 6.9020 | 7.8880 | 8.8740 | 1.3912 |
| 28 | 0.9859 | 1.9719 | 2.9578 | 3.9437 | 4.9297 | 5.9156 | 6.9015 | 7.8875 | 8.8734 | 1.3912 |
| 29 | 0.9859 | 1.9717 | 2.9576 | 3.9435 | 4.9293 | 5.9152 | 6.9011 | 7.8869 | 8.8728 | 1.3911 |
| 30 | 0.9858 | 1.9716 | 2.9574 | 3.9432 | 4.9290 | 5.9148 | 6.9006 | 7.8864 | 8.8722 | 1.3911 |
| 31 | 0.9857 | 1.9715 | 2.9572 | 3.9429 | 4.9287 | 5.9144 | 6.9002 | 7.8859 | 8.8716 | 1.3910 |
| 32 | 0.9857 | 1.9713 | 2.9570 | 3.9427 | 4.9284 | 5.9140 | 6.9997 | 7.8854 | 8.8710 | 1.3910 |
| 33 | 0.9856 | 1.9712 | 2.9568 | 3.9424 | 4.9280 | 5.9136 | 6.9992 | 7.8848 | 8.8704 | 1.3910 |
| 34 | 0.9855 | 1.9711 | 2.9566 | 3.9422 | 4.9277 | 5.9132 | 6.9988 | 7.8843 | 8.8698 | 1.3909 |
| 35 | 0.9855 | 1.9709 | 2.9564 | 3.9419 | 4.9274 | 5.9128 | 6.9983 | 7.8838 | 8.8692 | 1.3909 |
| 36 | 0.9854 | 1.9708 | 2.9562 | 3.9416 | 4.9270 | 5.9124 | 6.9978 | 7.8832 | 8.8687 | 1.3908 |
| 37 | 0.9853 | 1.9707 | 2.9560 | 3.9414 | 4.9267 | 5.9120 | 6.9974 | 7.8827 | 8.8681 | 1.3908 |
| 38 | 0.9853 | 1.9705 | 2.9558 | 3.9411 | 4.9264 | 5.9116 | 6.9969 | 7.8822 | 8.8675 | 1.3907 |
| 39 | 0.9852 | 1.9704 | 2.9556 | 3.9408 | 4.9260 | 5.9112 | 6.9964 | 7.8817 | 8.8669 | 1.3907 |
| 40 | 0.9851 | 1.9703 | 2.9554 | 3.9406 | 4.9257 | 5.9108 | 6.9960 | 7.8811 | 8.8663 | 1.3906 |
| 41 | 0.9851 | 1.9701 | 2.9552 | 3.9403 | 4.9254 | 5.9104 | 6.9955 | 7.8806 | 8.8657 | 1.3906 |
| 42 | 0.9850 | 1.9700 | 2.9550 | 3.9400 | 4.9250 | 5.9100 | 6.9950 | 7.8800 | 8.8650 | 1.3905 |
| 43 | 0.9849 | 1.9699 | 2.9548 | 3.9398 | 4.9247 | 5.9096 | 6.9946 | 7.8795 | 8.8644 | 1.3905 |
| 44 | 0.9849 | 1.9697 | 2.9546 | 3.9395 | 4.9244 | 5.9092 | 6.9941 | 7.8790 | 8.8638 | 1.3904 |
| 45 | 0.9848 | 1.9696 | 2.9544 | 3.9392 | 4.9240 | 5.9088 | 6.9936 | 7.8784 | 8.8632 | 1.3904 |
| 46 | 0.9847 | 1.9695 | 2.9542 | 3.9389 | 4.9237 | 5.9084 | 6.9931 | 7.8779 | 8.8626 | 1.3903 |
| 47 | 0.9847 | 1.9693 | 2.9540 | 3.9387 | 4.9233 | 5.9080 | 6.9927 | 7.8773 | 8.8620 | 1.3903 |
| 48 | 0.9846 | 1.9692 | 2.9538 | 3.9384 | 4.9230 | 5.9076 | 6.9922 | 7.8768 | 8.8614 | 1.3902 |
| 49 | 0.9845 | 1.9691 | 2.9536 | 3.9381 | 4.9227 | 5.9072 | 6.9917 | 7.8762 | 8.8608 | 1.3902 |
| 50 | 0.9845 | 1.9689 | 2.9534 | 3.9379 | 4.9223 | 5.9068 | 6.9912 | 7.8757 | 8.8602 | 1.3901 |
| 51 | 0.9844 | 1.9688 | 2.9532 | 3.9376 | 4.9220 | 5.9064 | 6.9908 | 7.8752 | 8.8595 | 1.3901 |
| 52 | 0.9843 | 1.9686 | 2.9530 | 3.9373 | 4.9216 | 5.9059 | 6.9903 | 7.8746 | 8.8589 | 1.3900 |
| 53 | 0.9843 | 1.9685 | 2.9528 | 3.9370 | 4.9213 | 5.9055 | 6.9898 | 7.8740 | 8.8583 | 1.3900 |
| 54 | 0.9842 | 1.9684 | 2.9526 | 3.9367 | 4.9209 | 5.9051 | 6.9893 | 7.8735 | 8.8577 | 1.3899 |
| 55 | 0.9841 | 1.9682 | 2.9523 | 3.9365 | 4.9206 | 5.9047 | 6.9888 | 7.8729 | 8.8570 | 1.3899 |
| 56 | 0.9840 | 1.9681 | 2.9521 | 3.9362 | 4.9202 | 5.9043 | 6.9883 | 7.8724 | 8.8564 | 1.3898 |
| 57 | 0.9840 | 1.9680 | 2.9519 | 3.9359 | 4.9199 | 5.9039 | 6.9878 | 7.8718 | 8.8558 | 1.3898 |
| 58 | 0.9839 | 1.9678 | 2.9517 | 3.9356 | 4.9195 | 5.9034 | 6.9874 | 7.8713 | 8.8552 | 1.3897 |
| 59 | 0.9838 | 1.9677 | 2.9515 | 3.9354 | 4.9192 | 5.9030 | 6.9869 | 7.8707 | 8.8545 | 1.3897 |
| 60 | 0.9838 | 1.9675 | 2.9513 | 3.9351 | 4.9188 | 5.9026 | 6.9864 | 7.8702 | 8.8539 | 1.3896 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10     | 11 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1038 | 0.2076 | 0.3114 | 0.4153 | 0.5191 | 0.6229 | 0.7267 | 0.8305 | 0.9343 | 0.1463 | 00 |
| 0.1041 | 0.2082 | 0.3123 | 0.4164 | 0.5205 | 0.6246 | 0.7287 | 0.8327 | 0.9368 | 0.1467 | 01 |
| 0.1044 | 0.2088 | 0.3131 | 0.4175 | 0.5219 | 0.6263 | 0.7307 | 0.8350 | 0.9394 | 0.1471 | 02 |
| 0.1047 | 0.2093 | 0.3140 | 0.4186 | 0.5233 | 0.6280 | 0.7326 | 0.8373 | 0.9419 | 0.1476 | 03 |
| 0.1049 | 0.2099 | 0.3148 | 0.4198 | 0.5247 | 0.6297 | 0.7346 | 0.8396 | 0.9445 | 0.1480 | 04 |
| 0.1052 | 0.2105 | 0.3157 | 0.4209 | 0.5262 | 0.6314 | 0.7366 | 0.8418 | 0.9471 | 0.1484 | 05 |
| 0.1055 | 0.2110 | 0.3165 | 0.4220 | 0.5276 | 0.6331 | 0.7386 | 0.8441 | 0.9496 | 0.1488 | 06 |
| 0.1058 | 0.2116 | 0.3174 | 0.4232 | 0.5290 | 0.6348 | 0.7406 | 0.8464 | 0.9522 | 0.1492 | 07 |
| 0.1061 | 0.2122 | 0.3182 | 0.4243 | 0.5304 | 0.6365 | 0.7426 | 0.8486 | 0.9547 | 0.1496 | 08 |
| 0.1064 | 0.2127 | 0.3191 | 0.4255 | 0.5318 | 0.6382 | 0.7446 | 0.8509 | 0.9573 | 0.1500 | 09 |
| 0.1067 | 0.2133 | 0.3200 | 0.4266 | 0.5333 | 0.6399 | 0.7466 | 0.8532 | 0.9599 | 0.1504 | 10 |
| 0.1069 | 0.2139 | 0.3208 | 0.4277 | 0.5347 | 0.6416 | 0.7485 | 0.8554 | 0.9624 | 0.1508 | 11 |
| 0.1072 | 0.2144 | 0.3217 | 0.4389 | 0.5361 | 0.6433 | 0.7505 | 0.8577 | 0.9650 | 0.1512 | 12 |
| 0.1075 | 0.2150 | 0.3225 | 0.4300 | 0.5375 | 0.6450 | 0.7525 | 0.8600 | 0.9675 | 0.1516 | 13 |
| 0.1078 | 0.2156 | 0.3233 | 0.4311 | 0.5389 | 0.6467 | 0.7545 | 0.8622 | 0.9700 | 0.1520 | 14 |
| 0.1081 | 0.2161 | 0.3242 | 0.4323 | 0.5403 | 0.6484 | 0.7565 | 0.8645 | 0.9726 | 0.1524 | 15 |
| 0.1084 | 0.2167 | 0.3251 | 0.4334 | 0.5418 | 0.6501 | 0.7585 | 0.8668 | 0.9752 | 0.1528 | 16 |
| 0.1086 | 0.2173 | 0.3259 | 0.4346 | 0.5432 | 0.6518 | 0.7605 | 0.8691 | 0.9778 | 0.1532 | 17 |
| 0.1089 | 0.2178 | 0.3268 | 0.4357 | 0.5446 | 0.6535 | 0.7624 | 0.8714 | 0.9803 | 0.1536 | 18 |
| 0.1092 | 0.2184 | 0.3276 | 0.4368 | 0.5460 | 0.6552 | 0.7644 | 0.8736 | 0.9828 | 0.1540 | 19 |
| 0.1095 | 0.2190 | 0.3285 | 0.4380 | 0.5474 | 0.6569 | 0.7664 | 0.8759 | 0.9854 | 0.1544 | 20 |
| 0.1098 | 0.2195 | 0.3293 | 0.4391 | 0.5488 | 0.6586 | 0.7684 | 0.8782 | 0.9879 | 0.1548 | 21 |
| 0.1101 | 0.2201 | 0.3302 | 0.4402 | 0.5503 | 0.6603 | 0.7704 | 0.8804 | 0.9905 | 0.1552 | 22 |
| 0.1103 | 0.2207 | 0.3310 | 0.4414 | 0.5517 | 0.6620 | 0.7724 | 0.8827 | 0.9931 | 0.1556 | 23 |
| 0.1106 | 0.2212 | 0.3319 | 0.4425 | 0.5531 | 0.6637 | 0.7743 | 0.8850 | 0.9956 | 0.1561 | 24 |
| 0.1109 | 0.2218 | 0.3327 | 0.4436 | 0.5545 | 0.6654 | 0.7763 | 0.8872 | 0.9981 | 0.1565 | 25 |
| 0.1112 | 0.2224 | 0.3336 | 0.4448 | 0.5559 | 0.6671 | 0.7783 | 0.8895 | 1.0007 | 0.1569 | 26 |
| 0.1115 | 0.2229 | 0.3344 | 0.4459 | 0.5573 | 0.6688 | 0.7803 | 0.8918 | 1.0032 | 0.1573 | 27 |
| 0.1118 | 0.2235 | 0.3353 | 0.4470 | 0.5588 | 0.6705 | 0.7823 | 0.8940 | 1.0058 | 0.1577 | 28 |
| 0.1120 | 0.2241 | 0.3361 | 0.4481 | 0.5602 | 0.6722 | 0.7842 | 0.8963 | 1.0083 | 0.1581 | 29 |
| 0.1123 | 0.2246 | 0.3370 | 0.4493 | 0.5616 | 0.6739 | 0.7862 | 0.8986 | 1.0109 | 0.1585 | 30 |
| 0.1126 | 0.2252 | 0.3378 | 0.4504 | 0.5630 | 0.6756 | 0.7882 | 0.9008 | 1.0134 | 0.1589 | 31 |
| 0.1129 | 0.2258 | 0.3386 | 0.4515 | 0.5644 | 0.6773 | 0.7902 | 0.9031 | 1.0159 | 0.1593 | 32 |
| 0.1132 | 0.2263 | 0.3395 | 0.4527 | 0.5659 | 0.6790 | 0.7922 | 0.9054 | 1.0185 | 0.1597 | 33 |
| 0.1134 | 0.2269 | 0.3403 | 0.4538 | 0.5673 | 0.6807 | 0.7941 | 0.9076 | 1.0210 | 0.1601 | 34 |
| 0.1137 | 0.2275 | 0.3412 | 0.4549 | 0.5687 | 0.6824 | 0.7961 | 0.9098 | 1.0236 | 0.1605 | 35 |
| 0.1140 | 0.2280 | 0.3421 | 0.4561 | 0.5701 | 0.6841 | 0.8081 | 0.9121 | 1.0262 | 0.1609 | 36 |
| 0.1143 | 0.2286 | 0.3429 | 0.4572 | 0.5715 | 0.6858 | 0.8001 | 0.9144 | 1.0287 | 0.1613 | 37 |
| 0.1146 | 0.2292 | 0.3437 | 0.4583 | 0.5729 | 0.6875 | 0.8021 | 0.9166 | 1.0312 | 0.1617 | 38 |
| 0.1149 | 0.2297 | 0.3446 | 0.4594 | 0.5743 | 0.6892 | 0.8040 | 0.9189 | 1.0337 | 0.1621 | 39 |
| 0.1151 | 0.2303 | 0.3454 | 0.4606 | 0.5757 | 0.6909 | 0.8060 | 0.9212 | 1.0363 | 0.1625 | 40 |
| 0.1154 | 0.2309 | 0.3463 | 0.4617 | 0.5771 | 0.6926 | 0.8080 | 0.9234 | 1.0389 | 0.1629 | 41 |
| 0.1157 | 0.2314 | 0.3471 | 0.4628 | 0.5786 | 0.6943 | 0.8100 | 0.9257 | 1.0414 | 0.1633 | 42 |
| 0.1160 | 0.2320 | 0.3480 | 0.4640 | 0.5800 | 0.6960 | 0.8119 | 0.9279 | 1.0439 | 0.1637 | 43 |
| 0.1163 | 0.2326 | 0.3488 | 0.4651 | 0.5814 | 0.6977 | 0.8139 | 0.9302 | 1.0465 | 0.1641 | 44 |
| 0.1166 | 0.2331 | 0.3497 | 0.4662 | 0.5828 | 0.6994 | 0.8159 | 0.9325 | 1.0490 | 0.1645 | 45 |
| 0.1168 | 0.2337 | 0.3505 | 0.4674 | 0.5842 | 0.7010 | 0.8179 | 0.9347 | 1.0516 | 0.1650 | 46 |
| 0.1171 | 0.2342 | 0.3514 | 0.4685 | 0.5856 | 0.7027 | 0.8199 | 0.9370 | 1.0541 | 0.1654 | 47 |
| 0.1174 | 0.2348 | 0.3522 | 0.4696 | 0.5870 | 0.7045 | 0.8219 | 0.9393 | 1.0567 | 0.1658 | 48 |
| 0.1177 | 0.2354 | 0.3531 | 0.4708 | 0.5884 | 0.7061 | 0.8238 | 0.9415 | 1.0592 | 0.1662 | 49 |
| 0.1180 | 0.2359 | 0.3539 | 0.4719 | 0.5899 | 0.7078 | 0.8258 | 0.9438 | 1.0617 | 0.1666 | 50 |
| 0.1183 | 0.2365 | 0.3548 | 0.4730 | 0.5913 | 0.7095 | 0.8278 | 0.9460 | 1.0643 | 0.1670 | 51 |
| 0.1185 | 0.2371 | 0.3556 | 0.4742 | 0.5927 | 0.7112 | 0.8298 | 0.9483 | 1.0669 | 0.1674 | 52 |
| 0.1188 | 0.2376 | 0.3565 | 0.4753 | 0.5941 | 0.7129 | 0.8317 | 0.9506 | 1.0694 | 0.1678 | 53 |
| 0.1191 | 0.2382 | 0.3573 | 0.4764 | 0.5955 | 0.7146 | 0.8337 | 0.9528 | 1.0719 | 0.1682 | 54 |
| 0.1194 | 0.2388 | 0.3581 | 0.4775 | 0.5969 | 0.7163 | 0.8357 | 0.9550 | 1.0744 | 0.1686 | 55 |
| 0.1197 | 0.2393 | 0.3590 | 0.4786 | 0.5983 | 0.7180 | 0.8376 | 0.9573 | 1.0769 | 0.1690 | 56 |
| 0.1199 | 0.2399 | 0.3598 | 0.4798 | 0.5997 | 0.7197 | 0.8396 | 0.9596 | 1.0795 | 0.1694 | 57 |
| 0.1202 | 0.2405 | 0.3607 | 0.4809 | 0.6011 | 0.7214 | 0.8416 | 0.9618 | 1.0821 | 0.1698 | 58 |
| 0.1205 | 0.2410 | 0.3615 | 0.4820 | 0.6025 | 0.7231 | 0.8436 | 0.9641 | 1.0846 | 0.1702 | 59 |
| 0.1208 | 0.2416 | 0.3624 | 0.4832 | 0.6040 | 0.7247 | 0.8455 | 0.9663 | 1.0871 | 0.1706 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | n      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9838 | 1.9675 | 2.9513 | 3.9351 | 4.9188 | 5.9026 | 6.8864 | 7.8702 | 8.8539 | 1.3866 |
| 01 | 0.9837 | 1.9674 | 2.9511 | 3.9348 | 4.9185 | 5.9022 | 6.8859 | 7.8696 | 8.8533 | 1.3866 |
| 02 | 0.9836 | 1.9673 | 2.9509 | 3.9345 | 4.9181 | 5.9018 | 6.8854 | 7.8690 | 8.8526 | 1.3865 |
| 03 | 0.9835 | 1.9671 | 2.9507 | 3.9342 | 4.9178 | 5.9013 | 6.8849 | 7.8684 | 8.8520 | 1.3865 |
| 04 | 0.9835 | 1.9670 | 2.9505 | 3.9339 | 4.9174 | 5.9009 | 6.8844 | 7.8679 | 8.8514 | 1.3864 |
| 05 | 0.9834 | 1.9668 | 2.9502 | 3.9337 | 4.9171 | 5.9005 | 6.8839 | 7.8673 | 8.8507 | 1.3864 |
| 06 | 0.9833 | 1.9667 | 2.9500 | 3.9334 | 4.9167 | 5.9001 | 6.8834 | 7.8667 | 8.8501 | 1.3863 |
| 07 | 0.9833 | 1.9665 | 2.9498 | 3.9331 | 4.9164 | 5.8996 | 6.8829 | 7.8662 | 8.8494 | 1.3863 |
| 08 | 0.9832 | 1.9664 | 2.9496 | 3.9328 | 4.9160 | 5.8992 | 6.8824 | 7.8656 | 8.8488 | 1.3862 |
| 09 | 0.9831 | 1.9663 | 2.9494 | 3.9325 | 4.9156 | 5.8988 | 6.8819 | 7.8650 | 8.8482 | 1.3862 |
| 10 | 0.9831 | 1.9661 | 2.9492 | 3.9322 | 4.9153 | 5.8983 | 6.8814 | 7.8645 | 8.8475 | 1.3861 |
| 11 | 0.9830 | 1.9660 | 2.9490 | 3.9319 | 4.9149 | 5.8979 | 6.8809 | 7.8639 | 8.8469 | 1.3861 |
| 12 | 0.9829 | 1.9658 | 2.9487 | 3.9316 | 4.9146 | 5.8975 | 6.8804 | 7.8633 | 8.8462 | 1.3860 |
| 13 | 0.9828 | 1.9657 | 2.9485 | 3.9314 | 4.9142 | 5.8970 | 6.8799 | 7.8627 | 8.8456 | 1.3860 |
| 14 | 0.9828 | 1.9655 | 2.9483 | 3.9311 | 4.9138 | 5.8966 | 6.8794 | 7.8621 | 8.8449 | 1.3859 |
| 15 | 0.9827 | 1.9654 | 2.9481 | 3.9308 | 4.9135 | 5.8962 | 6.8789 | 7.8616 | 8.8442 | 1.3859 |
| 16 | 0.9826 | 1.9652 | 2.9479 | 3.9305 | 4.9131 | 5.8957 | 6.8783 | 7.8610 | 8.8436 | 1.3858 |
| 17 | 0.9825 | 1.9651 | 2.9476 | 3.9302 | 4.9127 | 5.8953 | 6.8778 | 7.8604 | 8.8429 | 1.3858 |
| 18 | 0.9825 | 1.9650 | 2.9474 | 3.9299 | 4.9124 | 5.8949 | 6.8773 | 7.8598 | 8.8423 | 1.3857 |
| 19 | 0.9824 | 1.9648 | 2.9472 | 3.9296 | 4.9120 | 5.8944 | 6.8768 | 7.8592 | 8.8416 | 1.3857 |
| 20 | 0.9823 | 1.9647 | 2.9470 | 3.9293 | 4.9117 | 5.8940 | 6.8763 | 7.8586 | 8.8410 | 1.3856 |
| 21 | 0.9823 | 1.9645 | 2.9468 | 3.9290 | 4.9113 | 5.8935 | 6.8758 | 7.8580 | 8.8403 | 1.3856 |
| 22 | 0.9822 | 1.9644 | 2.9465 | 3.9287 | 4.9109 | 5.8931 | 6.8753 | 7.8573 | 8.8396 | 1.3855 |
| 23 | 0.9821 | 1.9642 | 2.9463 | 3.9284 | 4.9105 | 5.8926 | 6.8747 | 7.8566 | 8.8390 | 1.3855 |
| 24 | 0.9820 | 1.9641 | 2.9461 | 3.9281 | 4.9102 | 5.8922 | 6.8742 | 7.8560 | 8.8383 | 1.3854 |
| 25 | 0.9820 | 1.9639 | 2.9459 | 3.9278 | 4.9098 | 5.8918 | 6.8737 | 7.8555 | 8.8376 | 1.3854 |
| 26 | 0.9819 | 1.9638 | 2.9457 | 3.9275 | 4.9094 | 5.8913 | 6.8732 | 7.8550 | 8.8370 | 1.3853 |
| 27 | 0.9818 | 1.9636 | 2.9454 | 3.9272 | 4.9091 | 5.8909 | 6.8727 | 7.8545 | 8.8363 | 1.3853 |
| 28 | 0.9817 | 1.9635 | 2.9452 | 3.9269 | 4.9087 | 5.8904 | 6.8722 | 7.8539 | 8.8356 | 1.3852 |
| 29 | 0.9817 | 1.9633 | 2.9450 | 3.9266 | 4.9083 | 5.8900 | 6.8716 | 7.8533 | 8.8349 | 1.3852 |
| 30 | 0.9816 | 1.9632 | 2.9448 | 3.9263 | 4.9079 | 5.8895 | 6.8711 | 7.8527 | 8.8343 | 1.3851 |
| 31 | 0.9815 | 1.9630 | 2.9445 | 3.9260 | 4.9076 | 5.8891 | 6.8706 | 7.8521 | 8.8336 | 1.3851 |
| 32 | 0.9814 | 1.9629 | 2.9443 | 3.9257 | 4.9072 | 5.8886 | 6.8700 | 7.8515 | 8.8329 | 1.3850 |
| 33 | 0.9814 | 1.9627 | 2.9441 | 3.9254 | 4.9068 | 5.8882 | 6.8695 | 7.8509 | 8.8322 | 1.3850 |
| 34 | 0.9813 | 1.9626 | 2.9438 | 3.9251 | 4.9064 | 5.8877 | 6.8690 | 7.8503 | 8.8315 | 1.3849 |
| 35 | 0.9812 | 1.9624 | 2.9436 | 3.9248 | 4.9060 | 5.8872 | 6.8684 | 7.8497 | 8.8309 | 1.3849 |
| 36 | 0.9811 | 1.9623 | 2.9434 | 3.9245 | 4.9057 | 5.8868 | 6.8679 | 7.8490 | 8.8302 | 1.3848 |
| 37 | 0.9811 | 1.9621 | 2.9432 | 3.9242 | 4.9053 | 5.8863 | 6.8674 | 7.8484 | 8.8295 | 1.3848 |
| 38 | 0.9810 | 1.9620 | 2.9429 | 3.9239 | 4.9049 | 5.8859 | 6.8669 | 7.8478 | 8.8288 | 1.3847 |
| 39 | 0.9809 | 1.9618 | 2.9427 | 3.9236 | 4.9045 | 5.8854 | 6.8663 | 7.8472 | 8.8281 | 1.3847 |
| 40 | 0.9808 | 1.9617 | 2.9425 | 3.9233 | 4.9041 | 5.8850 | 6.8658 | 7.8466 | 8.8274 | 1.3846 |
| 41 | 0.9807 | 1.9615 | 2.9422 | 3.9230 | 4.9037 | 5.8845 | 6.8652 | 7.8460 | 8.8267 | 1.3845 |
| 42 | 0.9807 | 1.9613 | 2.9420 | 3.9227 | 4.9034 | 5.8840 | 6.8647 | 7.8454 | 8.8260 | 1.3845 |
| 43 | 0.9806 | 1.9612 | 2.9418 | 3.9224 | 4.9030 | 5.8836 | 6.8642 | 7.8448 | 8.8253 | 1.3844 |
| 44 | 0.9805 | 1.9610 | 2.9416 | 3.9221 | 4.9026 | 5.8831 | 6.8636 | 7.8441 | 8.8247 | 1.3844 |
| 45 | 0.9804 | 1.9609 | 2.9413 | 3.9218 | 4.9022 | 5.8826 | 6.8631 | 7.8435 | 8.8240 | 1.3843 |
| 46 | 0.9804 | 1.9607 | 2.9411 | 3.9214 | 4.9018 | 5.8822 | 6.8625 | 7.8429 | 8.8233 | 1.3842 |
| 47 | 0.9803 | 1.9606 | 2.9409 | 3.9211 | 4.9014 | 5.8817 | 6.8620 | 7.8423 | 8.8226 | 1.3842 |
| 48 | 0.9802 | 1.9604 | 2.9406 | 3.9208 | 4.9010 | 5.8812 | 6.8614 | 7.8416 | 8.8219 | 1.3841 |
| 49 | 0.9801 | 1.9603 | 2.9404 | 3.9205 | 4.9006 | 5.8808 | 6.8609 | 7.8410 | 8.8212 | 1.3841 |
| 50 | 0.9801 | 1.9601 | 2.9402 | 3.9202 | 4.9003 | 5.8803 | 6.8604 | 7.8404 | 8.8205 | 1.3840 |
| 51 | 0.9800 | 1.9599 | 2.9399 | 3.9199 | 4.8999 | 5.8798 | 6.8598 | 7.8398 | 8.8197 | 1.3840 |
| 52 | 0.9799 | 1.9598 | 2.9397 | 3.9196 | 4.8995 | 5.8794 | 6.8592 | 7.8391 | 8.8190 | 1.3839 |
| 53 | 0.9798 | 1.9596 | 2.9394 | 3.9193 | 4.8991 | 5.8789 | 6.8587 | 7.8385 | 8.8183 | 1.3838 |
| 54 | 0.9797 | 1.9595 | 2.9392 | 3.9189 | 4.8987 | 5.8784 | 6.8581 | 7.8379 | 8.8176 | 1.3838 |
| 55 | 0.9797 | 1.9593 | 2.9390 | 3.9186 | 4.8983 | 5.8779 | 6.8576 | 7.8372 | 8.8169 | 1.3837 |
| 56 | 0.9796 | 1.9592 | 2.9387 | 3.9183 | 4.8979 | 5.8775 | 6.8570 | 7.8366 | 8.8162 | 1.3836 |
| 57 | 0.9795 | 1.9590 | 2.9385 | 3.9180 | 4.8975 | 5.8770 | 6.8565 | 7.8360 | 8.8155 | 1.3836 |
| 58 | 0.9794 | 1.9588 | 2.9383 | 3.9177 | 4.8971 | 5.8765 | 6.8559 | 7.8353 | 8.8148 | 1.3835 |
| 59 | 0.9793 | 1.9587 | 2.9380 | 3.9173 | 4.8967 | 5.8760 | 6.8554 | 7.8347 | 8.8140 | 1.3835 |
| 60 | 0.9793 | 1.9585 | 2.9378 | 3.9170 | 4.8963 | 5.8755 | 6.8548 | 7.8341 | 8.8133 | 1.3834 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1208 | 0.2416 | 0.3624 | 0.4832 | 0.6040 | 0.7247 | 0.8455 | 0.9663 | 1.0871 | 0.1706 | 00 |
| 0.1211 | 0.2421 | 0.3632 | 0.4843 | 0.6054 | 0.7264 | 0.8475 | 0.9686 | 1.0896 | 0.1710 | 01 |
| 0.1214 | 0.2427 | 0.3641 | 0.4854 | 0.6068 | 0.7281 | 0.8495 | 0.9709 | 1.0922 | 0.1714 | 02 |
| 0.1216 | 0.2433 | 0.3649 | 0.4866 | 0.6082 | 0.7298 | 0.8515 | 0.9731 | 1.0948 | 0.1718 | 03 |
| 0.1219 | 0.2438 | 0.3658 | 0.4877 | 0.6106 | 0.7315 | 0.8534 | 0.9754 | 1.0973 | 0.1722 | 04 |
| 0.1222 | 0.2444 | 0.3666 | 0.4888 | 0.6110 | 0.7332 | 0.8554 | 0.9776 | 1.0998 | 0.1726 | 05 |
| 0.1225 | 0.2450 | 0.3674 | 0.4899 | 0.6124 | 0.7349 | 0.8574 | 0.9798 | 1.1023 | 0.1730 | 06 |
| 0.1228 | 0.2455 | 0.3683 | 0.4910 | 0.6138 | 0.7366 | 0.8593 | 0.9821 | 1.1048 | 0.1734 | 07 |
| 0.1230 | 0.2461 | 0.3691 | 0.4922 | 0.6152 | 0.7382 | 0.8613 | 0.9843 | 1.1074 | 0.1738 | 08 |
| 0.1233 | 0.2467 | 0.3700 | 0.4933 | 0.6166 | 0.7400 | 0.8633 | 0.9866 | 1.1100 | 0.1743 | 09 |
| 0.1236 | 0.2472 | 0.3708 | 0.4944 | 0.6180 | 0.7417 | 0.8653 | 0.9889 | 1.1125 | 0.1747 | 10 |
| 0.1239 | 0.2478 | 0.3717 | 0.4956 | 0.6194 | 0.7433 | 0.8672 | 0.9911 | 1.1150 | 0.1751 | 11 |
| 0.1242 | 0.2483 | 0.3725 | 0.4967 | 0.6209 | 0.7450 | 0.8692 | 0.9934 | 1.1175 | 0.1755 | 12 |
| 0.1245 | 0.2489 | 0.3734 | 0.4978 | 0.6223 | 0.7467 | 0.8712 | 0.9956 | 1.1201 | 0.1759 | 13 |
| 0.1247 | 0.2495 | 0.3742 | 0.4989 | 0.6237 | 0.7484 | 0.8731 | 0.9978 | 1.1226 | 0.1763 | 14 |
| 0.1250 | 0.2500 | 0.3750 | 0.5000 | 0.6251 | 0.7501 | 0.8751 | 1.0001 | 1.1251 | 0.1767 | 15 |
| 0.1253 | 0.2506 | 0.3759 | 0.5012 | 0.6265 | 0.7518 | 0.8771 | 1.0024 | 1.1277 | 0.1771 | 16 |
| 0.1256 | 0.2512 | 0.3767 | 0.5023 | 0.6279 | 0.7535 | 0.8791 | 1.0046 | 1.1302 | 0.1775 | 17 |
| 0.1259 | 0.2517 | 0.3776 | 0.5034 | 0.6293 | 0.7552 | 0.8810 | 1.0069 | 1.1327 | 0.1779 | 18 |
| 0.1261 | 0.2523 | 0.3784 | 0.5046 | 0.6307 | 0.7568 | 0.8830 | 1.0091 | 1.1353 | 0.1783 | 19 |
| 0.1264 | 0.2528 | 0.3793 | 0.5057 | 0.6321 | 0.7585 | 0.8849 | 1.0114 | 1.1378 | 0.1787 | 20 |
| 0.1267 | 0.2534 | 0.3801 | 0.5068 | 0.6335 | 0.7602 | 0.8869 | 1.0136 | 1.1403 | 0.1791 | 21 |
| 0.1270 | 0.2540 | 0.3809 | 0.5079 | 0.6349 | 0.7619 | 0.8889 | 1.0158 | 1.1428 | 0.1795 | 22 |
| 0.1273 | 0.2545 | 0.3818 | 0.5090 | 0.6363 | 0.7636 | 0.8908 | 1.0181 | 1.1453 | 0.1799 | 23 |
| 0.1275 | 0.2551 | 0.3826 | 0.5102 | 0.6377 | 0.7652 | 0.8928 | 1.0203 | 1.1479 | 0.1803 | 24 |
| 0.1278 | 0.2556 | 0.3835 | 0.5113 | 0.6391 | 0.7669 | 0.8947 | 1.0226 | 1.1504 | 0.1807 | 25 |
| 0.1281 | 0.2562 | 0.3843 | 0.5124 | 0.6405 | 0.7686 | 0.8967 | 1.0248 | 1.1529 | 0.1811 | 26 |
| 0.1284 | 0.2568 | 0.3852 | 0.5136 | 0.6419 | 0.7703 | 0.8987 | 1.0271 | 1.1555 | 0.1815 | 27 |
| 0.1287 | 0.2573 | 0.3860 | 0.5147 | 0.6433 | 0.7720 | 0.9007 | 1.0294 | 1.1580 | 0.1819 | 28 |
| 0.1289 | 0.2579 | 0.3868 | 0.5158 | 0.6447 | 0.7737 | 0.9026 | 1.0316 | 1.1605 | 0.1823 | 29 |
| 0.1292 | 0.2585 | 0.3877 | 0.5169 | 0.6461 | 0.7754 | 0.9046 | 1.0338 | 1.1631 | 0.1827 | 30 |
| 0.1295 | 0.2590 | 0.3885 | 0.5180 | 0.6475 | 0.7771 | 0.9066 | 1.0361 | 1.1656 | 0.1831 | 31 |
| 0.1298 | 0.2596 | 0.3894 | 0.5192 | 0.6489 | 0.7787 | 0.9085 | 1.0383 | 1.1681 | 0.1835 | 32 |
| 0.1301 | 0.2601 | 0.3902 | 0.5203 | 0.6503 | 0.7804 | 0.9105 | 1.0406 | 1.1706 | 0.1839 | 33 |
| 0.1303 | 0.2607 | 0.3910 | 0.5214 | 0.6517 | 0.7821 | 0.9124 | 1.0428 | 1.1731 | 0.1843 | 34 |
| 0.1306 | 0.2613 | 0.3919 | 0.5225 | 0.6532 | 0.7838 | 0.9144 | 1.0450 | 1.1757 | 0.1847 | 35 |
| 0.1309 | 0.2618 | 0.3927 | 0.5236 | 0.6546 | 0.7855 | 0.9164 | 1.0473 | 1.1782 | 0.1852 | 36 |
| 0.1312 | 0.2624 | 0.3936 | 0.5248 | 0.6560 | 0.7871 | 0.9183 | 1.0495 | 1.1807 | 0.1856 | 37 |
| 0.1315 | 0.2629 | 0.3944 | 0.5259 | 0.6574 | 0.7888 | 0.9203 | 1.0518 | 1.1832 | 0.1860 | 38 |
| 0.1318 | 0.2635 | 0.3953 | 0.5270 | 0.6588 | 0.7905 | 0.9223 | 1.0540 | 1.1858 | 0.1864 | 39 |
| 0.1320 | 0.2641 | 0.3961 | 0.5281 | 0.6602 | 0.7922 | 0.9242 | 1.0562 | 1.1883 | 0.1868 | 40 |
| 0.1323 | 0.2646 | 0.3969 | 0.5292 | 0.6616 | 0.7939 | 0.9262 | 1.0585 | 1.1908 | 0.1872 | 41 |
| 0.1326 | 0.2652 | 0.3978 | 0.5304 | 0.6630 | 0.7955 | 0.9281 | 1.0607 | 1.1933 | 0.1876 | 42 |
| 0.1329 | 0.2657 | 0.3986 | 0.5315 | 0.6644 | 0.7972 | 0.9301 | 1.0630 | 1.1958 | 0.1880 | 43 |
| 0.1332 | 0.2663 | 0.3995 | 0.5326 | 0.6658 | 0.7989 | 0.9321 | 1.0652 | 1.1984 | 0.1884 | 44 |
| 0.1334 | 0.2669 | 0.4003 | 0.5337 | 0.6672 | 0.8006 | 0.9340 | 1.0674 | 1.2009 | 0.1888 | 45 |
| 0.1337 | 0.2674 | 0.4011 | 0.5348 | 0.6686 | 0.8023 | 0.9360 | 1.0697 | 1.2034 | 0.1892 | 46 |
| 0.1340 | 0.2680 | 0.4020 | 0.5360 | 0.6700 | 0.8039 | 0.9379 | 1.0719 | 1.2059 | 0.1896 | 47 |
| 0.1343 | 0.2685 | 0.4028 | 0.5371 | 0.6714 | 0.8056 | 0.9399 | 1.0742 | 1.2084 | 0.1900 | 48 |
| 0.1346 | 0.2691 | 0.4037 | 0.5382 | 0.6728 | 0.8073 | 0.9419 | 1.0764 | 1.2110 | 0.1904 | 49 |
| 0.1348 | 0.2697 | 0.4045 | 0.5393 | 0.6742 | 0.8090 | 0.9438 | 1.0786 | 1.2135 | 0.1908 | 50 |
| 0.1351 | 0.2702 | 0.4053 | 0.5404 | 0.6756 | 0.8107 | 0.9458 | 1.0809 | 1.2160 | 0.1912 | 51 |
| 0.1354 | 0.2708 | 0.4062 | 0.5416 | 0.6770 | 0.8123 | 0.9477 | 1.0831 | 1.2185 | 0.1916 | 52 |
| 0.1357 | 0.2713 | 0.4070 | 0.5427 | 0.6783 | 0.8140 | 0.9497 | 1.0854 | 1.2210 | 0.1920 | 53 |
| 0.1359 | 0.2719 | 0.4078 | 0.5438 | 0.6797 | 0.8157 | 0.9516 | 1.0876 | 1.2235 | 0.1924 | 54 |
| 0.1362 | 0.2725 | 0.4087 | 0.5449 | 0.6811 | 0.8174 | 0.9536 | 1.0898 | 1.2261 | 0.1928 | 55 |
| 0.1365 | 0.2730 | 0.4095 | 0.5460 | 0.6825 | 0.8191 | 0.9556 | 1.0921 | 1.2286 | 0.1932 | 56 |
| 0.1368 | 0.2736 | 0.4104 | 0.5472 | 0.6839 | 0.8207 | 0.9575 | 1.0943 | 1.2311 | 0.1936 | 57 |
| 0.1371 | 0.2741 | 0.4112 | 0.5483 | 0.6853 | 0.8224 | 0.9595 | 1.0966 | 1.2336 | 0.1940 | 58 |
| 0.1374 | 0.2747 | 0.4121 | 0.5494 | 0.6867 | 0.8241 | 0.9615 | 1.0988 | 1.2362 | 0.1944 | 59 |
| 0.1376 | 0.2753 | 0.4129 | 0.5505 | 0.6881 | 0.8258 | 0.9634 | 1.1010 | 1.2387 | 0.1948 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9793 | 1.9585 | 2.9378 | 3.9170 | 4.8963 | 5.8755 | 6.8548 | 7.8341 | 8.8133 | 1.3864 |
| 01 | 0.9792 | 1.9584 | 2.9375 | 3.9167 | 4.8959 | 5.8751 | 6.8542 | 7.8334 | 8.8126 | 1.3863 |
| 02 | 0.9791 | 1.9582 | 2.9373 | 3.9164 | 4.8955 | 5.8746 | 6.8537 | 7.8328 | 8.8119 | 1.3862 |
| 03 | 0.9790 | 1.9580 | 2.9370 | 3.9161 | 4.8951 | 5.8741 | 6.8531 | 7.8321 | 8.8111 | 1.3862 |
| 04 | 0.9789 | 1.9579 | 2.9368 | 3.9157 | 4.8947 | 5.8736 | 6.8525 | 7.8315 | 8.8104 | 1.3861 |
| 05 | 0.9789 | 1.9577 | 2.9366 | 3.9154 | 4.8943 | 5.8731 | 6.8520 | 7.8308 | 8.8097 | 1.3861 |
| 06 | 0.9788 | 1.9575 | 2.9363 | 3.9151 | 4.8939 | 5.8726 | 6.8514 | 7.8302 | 8.8090 | 1.3860 |
| 07 | 0.9787 | 1.9574 | 2.9361 | 3.9148 | 4.8935 | 5.8722 | 6.8508 | 7.8295 | 8.8082 | 1.3860 |
| 08 | 0.9786 | 1.9572 | 2.9358 | 3.9144 | 4.8931 | 5.8717 | 6.8503 | 7.8289 | 8.8075 | 1.3859 |
| 09 | 0.9785 | 1.9571 | 2.9356 | 3.9141 | 4.8927 | 5.8712 | 6.8497 | 7.8282 | 8.8068 | 1.3859 |
| 10 | 0.9785 | 1.9569 | 2.9354 | 3.9138 | 4.8923 | 5.8707 | 6.8492 | 7.8276 | 8.8061 | 1.3858 |
|    |        |        |        |        |        |        |        |        |        |        |
| 11 | 0.9784 | 1.9567 | 2.9351 | 3.9135 | 4.8918 | 5.8702 | 6.8486 | 7.8269 | 8.8053 | 1.3858 |
| 12 | 0.9783 | 1.9566 | 2.9349 | 3.9131 | 4.8914 | 5.8697 | 6.8480 | 7.8263 | 8.8046 | 1.3857 |
| 13 | 0.9782 | 1.9564 | 2.9346 | 3.9128 | 4.8910 | 5.8692 | 6.8474 | 7.8256 | 8.8038 | 1.3856 |
| 14 | 0.9781 | 1.9562 | 2.9344 | 3.9125 | 4.8906 | 5.8687 | 6.8468 | 7.8250 | 8.8031 | 1.3856 |
| 15 | 0.9780 | 1.9561 | 2.9341 | 3.9122 | 4.8902 | 5.8682 | 6.8463 | 7.8243 | 8.8023 | 1.3855 |
| 16 | 0.9780 | 1.9559 | 2.9339 | 3.9118 | 4.8898 | 5.8677 | 6.8457 | 7.8236 | 8.8016 | 1.3854 |
| 17 | 0.9779 | 1.9557 | 2.9336 | 3.9115 | 4.8894 | 5.8672 | 6.8451 | 7.8230 | 8.8009 | 1.3854 |
| 18 | 0.9778 | 1.9556 | 2.9334 | 3.9112 | 4.8890 | 5.8667 | 6.8445 | 7.8223 | 8.8001 | 1.3853 |
| 19 | 0.9777 | 1.9554 | 2.9331 | 3.9108 | 4.8885 | 5.8662 | 6.8440 | 7.8217 | 8.7994 | 1.3853 |
| 20 | 0.9776 | 1.9553 | 2.9329 | 3.9105 | 4.8881 | 5.8657 | 6.8434 | 7.8210 | 8.7986 | 1.3852 |
|    |        |        |        |        |        |        |        |        |        |        |
| 21 | 0.9775 | 1.9551 | 2.9326 | 3.9102 | 4.8877 | 5.8652 | 6.8428 | 7.8203 | 8.7979 | 1.3852 |
| 22 | 0.9775 | 1.9549 | 2.9324 | 3.9098 | 4.8873 | 5.8647 | 6.8422 | 7.8197 | 8.7971 | 1.3851 |
| 23 | 0.9774 | 1.9547 | 2.9321 | 3.9095 | 4.8869 | 5.8642 | 6.8416 | 7.8190 | 8.7964 | 1.3850 |
| 24 | 0.9773 | 1.9546 | 2.9319 | 3.9092 | 4.8864 | 5.8637 | 6.8410 | 7.8183 | 8.7956 | 1.3850 |
| 25 | 0.9772 | 1.9544 | 2.9316 | 3.9088 | 4.8860 | 5.8632 | 6.8404 | 7.8176 | 8.7948 | 1.3849 |
| 26 | 0.9771 | 1.9542 | 2.9314 | 3.9085 | 4.8856 | 5.8627 | 6.8398 | 7.8170 | 8.7941 | 1.3849 |
| 27 | 0.9770 | 1.9541 | 2.9311 | 3.9081 | 4.8852 | 5.8622 | 6.8393 | 7.8163 | 8.7933 | 1.3848 |
| 28 | 0.9770 | 1.9539 | 2.9309 | 3.9078 | 4.8848 | 5.8617 | 6.8387 | 7.8156 | 8.7926 | 1.3847 |
| 29 | 0.9769 | 1.9537 | 2.9306 | 3.9075 | 4.8843 | 5.8612 | 6.8381 | 7.8149 | 8.7918 | 1.3847 |
| 30 | 0.9768 | 1.9536 | 2.9304 | 3.9071 | 4.8839 | 5.8607 | 6.8375 | 7.8143 | 8.7911 | 1.3846 |
|    |        |        |        |        |        |        |        |        |        |        |
| 31 | 0.9767 | 1.9534 | 2.9301 | 3.9068 | 4.8835 | 5.8602 | 6.8369 | 7.8136 | 8.7903 | 1.3846 |
| 32 | 0.9766 | 1.9532 | 2.9298 | 3.9064 | 4.8831 | 5.8597 | 6.8363 | 7.8129 | 8.7895 | 1.3845 |
| 33 | 0.9765 | 1.9531 | 2.9296 | 3.9061 | 4.8826 | 5.8592 | 6.8357 | 7.8122 | 8.7887 | 1.3844 |
| 34 | 0.9764 | 1.9529 | 2.9293 | 3.9058 | 4.8822 | 5.8586 | 6.8351 | 7.8115 | 8.7880 | 1.3844 |
| 35 | 0.9764 | 1.9527 | 2.9291 | 3.9054 | 4.8818 | 5.8581 | 6.8345 | 7.8108 | 8.7872 | 1.3843 |
| 36 | 0.9763 | 1.9525 | 2.9288 | 3.9051 | 4.8813 | 5.8576 | 6.8339 | 7.8102 | 8.7864 | 1.3843 |
| 37 | 0.9762 | 1.9524 | 2.9285 | 3.9047 | 4.8809 | 5.8571 | 6.8333 | 7.8095 | 8.7856 | 1.3842 |
| 38 | 0.9761 | 1.9522 | 2.9283 | 3.9044 | 4.8805 | 5.8566 | 6.8327 | 7.8088 | 8.7849 | 1.3841 |
| 39 | 0.9760 | 1.9520 | 2.9280 | 3.9040 | 4.8801 | 5.8561 | 6.8321 | 7.8081 | 8.7841 | 1.3841 |
| 40 | 0.9759 | 1.9519 | 2.9278 | 3.9037 | 4.8796 | 5.8556 | 6.8315 | 7.8074 | 8.7833 | 1.3840 |
|    |        |        |        |        |        |        |        |        |        |        |
| 41 | 0.9758 | 1.9517 | 2.9275 | 3.9034 | 4.8792 | 5.8550 | 6.8309 | 7.8067 | 8.7826 | 1.3840 |
| 42 | 0.9758 | 1.9515 | 2.9273 | 3.9030 | 4.8788 | 5.8545 | 6.8303 | 7.8060 | 8.7818 | 1.3839 |
| 43 | 0.9757 | 1.9513 | 2.9270 | 3.9027 | 4.8783 | 5.8540 | 6.8296 | 7.8053 | 8.7810 | 1.3838 |
| 44 | 0.9756 | 1.9512 | 2.9267 | 3.9023 | 4.8779 | 5.8535 | 6.8290 | 7.8046 | 8.7802 | 1.3838 |
| 45 | 0.9755 | 1.9510 | 2.9265 | 3.9020 | 4.8774 | 5.8529 | 6.8284 | 7.8039 | 8.7794 | 1.3837 |
| 46 | 0.9754 | 1.9508 | 2.9262 | 3.9016 | 4.8770 | 5.8524 | 6.8278 | 7.8032 | 8.7786 | 1.3837 |
| 47 | 0.9753 | 1.9506 | 2.9259 | 3.9013 | 4.8766 | 5.8519 | 6.8272 | 7.8025 | 8.7778 | 1.3836 |
| 48 | 0.9752 | 1.9505 | 2.9257 | 3.9009 | 4.8761 | 5.8514 | 6.8266 | 7.8018 | 8.7770 | 1.3835 |
| 49 | 0.9751 | 1.9503 | 2.9254 | 3.9006 | 4.8757 | 5.8508 | 6.8260 | 7.8011 | 8.7763 | 1.3835 |
| 50 | 0.9751 | 1.9501 | 2.9252 | 3.9002 | 4.8753 | 5.8503 | 6.8254 | 7.8004 | 8.7755 | 1.3834 |
|    |        |        |        |        |        |        |        |        |        |        |
| 51 | 0.9750 | 1.9499 | 2.9249 | 3.8999 | 4.8748 | 5.8498 | 6.8247 | 7.7997 | 8.7747 | 1.3834 |
| 52 | 0.9749 | 1.9497 | 2.9246 | 3.8995 | 4.8744 | 5.8492 | 6.8241 | 7.7990 | 8.7739 | 1.3833 |
| 53 | 0.9748 | 1.9496 | 2.9244 | 3.8991 | 4.8739 | 5.8487 | 6.8235 | 7.7983 | 8.7731 | 1.3832 |
| 54 | 0.9747 | 1.9494 | 2.9241 | 3.8988 | 4.8735 | 5.8482 | 6.8229 | 7.7976 | 8.7723 | 1.3832 |
| 55 | 0.9746 | 1.9492 | 2.9238 | 3.8984 | 4.8730 | 5.8476 | 6.8222 | 7.7969 | 8.7715 | 1.3831 |
| 56 | 0.9745 | 1.9490 | 2.9236 | 3.8981 | 4.8726 | 5.8471 | 6.8216 | 7.7961 | 8.7707 | 1.3831 |
| 57 | 0.9744 | 1.9489 | 2.9233 | 3.8977 | 4.8721 | 5.8466 | 6.8210 | 7.7954 | 8.7699 | 1.3830 |
| 58 | 0.9743 | 1.9487 | 2.9230 | 3.8974 | 4.8717 | 5.8460 | 6.8204 | 7.7947 | 8.7691 | 1.3829 |
| 59 | 0.9743 | 1.9485 | 2.9228 | 3.8970 | 4.8713 | 5.8455 | 6.8198 | 7.7940 | 8.7683 | 1.3829 |
| 60 | 0.9742 | 1.9483 | 2.9225 | 3.8966 | 4.8708 | 5.8450 | 6.8191 | 7.7933 | 8.7675 | 1.3828 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1376 | 0.2753 | 0.4129 | 0.5505 | 0.6881 | 0.8258 | 0.9634 | 1.1010 | 1.2387 | 0.1948 | 00 |
| 0.1380 | 0.2758 | 0.4137 | 0.5516 | 0.6895 | 0.8275 | 0.9654 | 1.1033 | 1.2412 | 0.1952 | 01 |
| 0.1382 | 0.2764 | 0.4145 | 0.5527 | 0.6909 | 0.8291 | 0.9673 | 1.1055 | 1.2437 | 0.1956 | 02 |
| 0.1385 | 0.2769 | 0.4154 | 0.5538 | 0.6923 | 0.8308 | 0.9692 | 1.1077 | 1.2462 | 0.1960 | 03 |
| 0.1387 | 0.2775 | 0.4162 | 0.5550 | 0.6937 | 0.8324 | 0.9712 | 1.1099 | 1.2487 | 0.1965 | 04 |
| 0.1390 | 0.2780 | 0.4171 | 0.5561 | 0.6951 | 0.8341 | 0.9731 | 1.1122 | 1.2512 | 0.1969 | 05 |
| 0.1393 | 0.2786 | 0.4179 | 0.5572 | 0.6965 | 0.8358 | 0.9751 | 1.1144 | 1.2537 | 0.1973 | 06 |
| 0.1396 | 0.2792 | 0.4187 | 0.5583 | 0.6979 | 0.8375 | 0.9771 | 1.1166 | 1.2562 | 0.1977 | 07 |
| 0.1399 | 0.2797 | 0.4196 | 0.5594 | 0.6993 | 0.8392 | 0.9790 | 1.1189 | 1.2587 | 0.1981 | 08 |
| 0.1401 | 0.2803 | 0.4204 | 0.5606 | 0.7007 | 0.8408 | 0.9810 | 1.1211 | 1.2613 | 0.1985 | 09 |
| 0.1404 | 0.2808 | 0.4213 | 0.5617 | 0.7021 | 0.8425 | 0.9829 | 1.1234 | 1.2638 | 0.1989 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1407 | 0.2814 | 0.4221 | 0.5628 | 0.7035 | 0.8441 | 0.9849 | 1.1256 | 1.2663 | 0.1993 | 11 |
| 0.1410 | 0.2819 | 0.4229 | 0.5639 | 0.7049 | 0.8458 | 0.9868 | 1.1278 | 1.2688 | 0.1997 | 12 |
| 0.1413 | 0.2825 | 0.4238 | 0.5650 | 0.7063 | 0.8475 | 0.9888 | 1.1300 | 1.2713 | 0.2001 | 13 |
| 0.1415 | 0.2831 | 0.4246 | 0.5661 | 0.7077 | 0.8492 | 0.9907 | 1.1322 | 1.2738 | 0.2005 | 14 |
| 0.1418 | 0.2836 | 0.4254 | 0.5672 | 0.7091 | 0.8509 | 0.9927 | 1.1345 | 1.2763 | 0.2009 | 15 |
| 0.1421 | 0.2842 | 0.4263 | 0.5684 | 0.7104 | 0.8525 | 0.9946 | 1.1367 | 1.2788 | 0.2013 | 16 |
| 0.1424 | 0.2847 | 0.4271 | 0.5695 | 0.7118 | 0.8542 | 0.9966 | 1.1390 | 1.2813 | 0.2017 | 17 |
| 0.1426 | 0.2853 | 0.4279 | 0.5706 | 0.7132 | 0.8558 | 0.9985 | 1.1412 | 1.2838 | 0.2021 | 18 |
| 0.1429 | 0.2858 | 0.4288 | 0.5717 | 0.7146 | 0.8575 | 1.0005 | 1.1434 | 1.2863 | 0.2025 | 19 |
| 0.1432 | 0.2864 | 0.4296 | 0.5728 | 0.7160 | 0.8592 | 1.0024 | 1.1456 | 1.2888 | 0.2029 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1435 | 0.2870 | 0.4304 | 0.5739 | 0.7174 | 0.8609 | 1.0044 | 1.1478 | 1.2913 | 0.2033 | 21 |
| 0.1438 | 0.2875 | 0.4313 | 0.5750 | 0.7188 | 0.8626 | 1.0063 | 1.1501 | 1.2938 | 0.2037 | 22 |
| 0.1440 | 0.2881 | 0.4321 | 0.5762 | 0.7202 | 0.8642 | 1.0083 | 1.1523 | 1.2963 | 0.2041 | 23 |
| 0.1443 | 0.2886 | 0.4329 | 0.5773 | 0.7216 | 0.8659 | 1.0102 | 1.1545 | 1.2988 | 0.2045 | 24 |
| 0.1446 | 0.2892 | 0.4338 | 0.5784 | 0.7230 | 0.8675 | 1.0121 | 1.1567 | 1.3013 | 0.2049 | 25 |
| 0.1449 | 0.2897 | 0.4346 | 0.5795 | 0.7243 | 0.8692 | 1.0141 | 1.1590 | 1.3038 | 0.2053 | 26 |
| 0.1451 | 0.2903 | 0.4354 | 0.5806 | 0.7257 | 0.8709 | 1.0160 | 1.1612 | 1.3063 | 0.2057 | 27 |
| 0.1454 | 0.2909 | 0.4363 | 0.5817 | 0.7271 | 0.8726 | 1.0180 | 1.1634 | 1.3088 | 0.2061 | 28 |
| 0.1457 | 0.2914 | 0.4371 | 0.5828 | 0.7285 | 0.8742 | 1.0199 | 1.1656 | 1.3113 | 0.2065 | 29 |
| 0.1460 | 0.2920 | 0.4379 | 0.5839 | 0.7299 | 0.8759 | 1.0219 | 1.1678 | 1.3138 | 0.2069 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1463 | 0.2925 | 0.4388 | 0.5850 | 0.7313 | 0.8776 | 1.0238 | 1.1701 | 1.3163 | 0.2073 | 31 |
| 0.1465 | 0.2931 | 0.4396 | 0.5862 | 0.7327 | 0.8792 | 1.0258 | 1.1723 | 1.3188 | 0.2077 | 32 |
| 0.1468 | 0.2936 | 0.4404 | 0.5873 | 0.7341 | 0.8809 | 1.0277 | 1.1745 | 1.3213 | 0.2081 | 33 |
| 0.1471 | 0.2942 | 0.4413 | 0.5884 | 0.7355 | 0.8825 | 1.0296 | 1.1767 | 1.3238 | 0.2085 | 34 |
| 0.1474 | 0.2947 | 0.4421 | 0.5895 | 0.7368 | 0.8842 | 1.0316 | 1.1790 | 1.3263 | 0.2089 | 35 |
| 0.1476 | 0.2953 | 0.4429 | 0.5906 | 0.7382 | 0.8859 | 1.0335 | 1.1812 | 1.3288 | 0.2093 | 36 |
| 0.1479 | 0.2958 | 0.4438 | 0.5917 | 0.7396 | 0.8875 | 1.0355 | 1.1834 | 1.3313 | 0.2097 | 37 |
| 0.1482 | 0.2964 | 0.4446 | 0.5928 | 0.7410 | 0.8892 | 1.0374 | 1.1856 | 1.3338 | 0.2101 | 38 |
| 0.1485 | 0.2970 | 0.4454 | 0.5939 | 0.7424 | 0.8909 | 1.0394 | 1.1878 | 1.3363 | 0.2105 | 39 |
| 0.1488 | 0.2975 | 0.4463 | 0.5950 | 0.7438 | 0.8926 | 1.0413 | 1.1901 | 1.3388 | 0.2110 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1490 | 0.2981 | 0.4471 | 0.5961 | 0.7452 | 0.8942 | 1.0432 | 1.1923 | 1.3413 | 0.2114 | 41 |
| 0.1493 | 0.2986 | 0.4479 | 0.5972 | 0.7466 | 0.8959 | 1.0452 | 1.1945 | 1.3438 | 0.2118 | 42 |
| 0.1496 | 0.2992 | 0.4488 | 0.5984 | 0.7479 | 0.8975 | 1.0471 | 1.1967 | 1.3463 | 0.2122 | 43 |
| 0.1499 | 0.2997 | 0.4496 | 0.5995 | 0.7493 | 0.8992 | 1.0491 | 1.1989 | 1.3488 | 0.2126 | 44 |
| 0.1501 | 0.3003 | 0.4504 | 0.6006 | 0.7507 | 0.9008 | 1.0510 | 1.2011 | 1.3513 | 0.2130 | 45 |
| 0.1504 | 0.3008 | 0.4513 | 0.6017 | 0.7521 | 0.9025 | 1.0529 | 1.2034 | 1.3538 | 0.2134 | 46 |
| 0.1507 | 0.3014 | 0.4521 | 0.6028 | 0.7535 | 0.9042 | 1.0549 | 1.2056 | 1.3563 | 0.2138 | 47 |
| 0.1510 | 0.3019 | 0.4529 | 0.6039 | 0.7549 | 0.9058 | 1.0568 | 1.2078 | 1.3588 | 0.2142 | 48 |
| 0.1513 | 0.3025 | 0.4538 | 0.6050 | 0.7563 | 0.9075 | 1.0588 | 1.2100 | 1.3613 | 0.2146 | 49 |
| 0.1515 | 0.3031 | 0.4546 | 0.6061 | 0.7576 | 0.9092 | 1.0607 | 1.2122 | 1.3638 | 0.2150 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1518 | 0.3036 | 0.4554 | 0.6072 | 0.7590 | 0.9108 | 1.0626 | 1.2144 | 1.3663 | 0.2154 | 51 |
| 0.1521 | 0.3042 | 0.4562 | 0.6083 | 0.7604 | 0.9125 | 1.0646 | 1.2166 | 1.3687 | 0.2158 | 52 |
| 0.1524 | 0.3047 | 0.4571 | 0.6094 | 0.7618 | 0.9142 | 1.0665 | 1.2189 | 1.3712 | 0.2162 | 53 |
| 0.1526 | 0.3053 | 0.4579 | 0.6105 | 0.7632 | 0.9158 | 1.0684 | 1.2211 | 1.3737 | 0.2166 | 54 |
| 0.1529 | 0.3058 | 0.4587 | 0.6116 | 0.7646 | 0.9175 | 1.0704 | 1.2233 | 1.3762 | 0.2170 | 55 |
| 0.1532 | 0.3064 | 0.4596 | 0.6128 | 0.7660 | 0.9191 | 1.0723 | 1.2255 | 1.3787 | 0.2174 | 56 |
| 0.1535 | 0.3069 | 0.4604 | 0.6139 | 0.7673 | 0.9208 | 1.0742 | 1.2277 | 1.3812 | 0.2178 | 57 |
| 0.1537 | 0.3075 | 0.4612 | 0.6150 | 0.7687 | 0.9224 | 1.0762 | 1.2299 | 1.3837 | 0.2182 | 58 |
| 0.1540 | 0.3080 | 0.4621 | 0.6161 | 0.7701 | 0.9241 | 1.0781 | 1.2321 | 1.3862 | 0.2186 | 59 |
| 0.1543 | 0.3086 | 0.4629 | 0.6172 | 0.7715 | 0.9257 | 1.0800 | 1.2343 | 1.3886 | 0.2190 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9742 | 1.9483 | 2.9225 | 3.8966 | 4.8708 | 5.8450 | 6.8191 | 7.7933 | 8.7675 | 1.3828 |
| 01 | 0.9741 | 1.9481 | 2.9222 | 3.8963 | 4.8704 | 5.8444 | 6.8185 | 7.7926 | 8.7666 | 1.3827 |
| 02 | 0.9740 | 1.9480 | 2.9219 | 3.8959 | 4.8699 | 5.8439 | 6.8179 | 7.7918 | 8.7658 | 1.3826 |
| 03 | 0.9739 | 1.9478 | 2.9217 | 3.8956 | 4.8695 | 5.8433 | 6.8172 | 7.7911 | 8.7650 | 1.3826 |
| 04 | 0.9738 | 1.9476 | 2.9214 | 3.8952 | 4.8690 | 5.8428 | 6.8166 | 7.7904 | 8.7642 | 1.3825 |
| 05 | 0.9737 | 1.9474 | 2.9211 | 3.8948 | 4.8686 | 5.8423 | 6.8160 | 7.7897 | 8.7634 | 1.3825 |
| 06 | 0.9736 | 1.9472 | 2.9209 | 3.8945 | 4.8681 | 5.8417 | 6.8153 | 7.7890 | 8.7626 | 1.3824 |
| 07 | 0.9735 | 1.9471 | 2.9206 | 3.8941 | 4.8676 | 5.8412 | 6.8147 | 7.7882 | 8.7618 | 1.3824 |
| 08 | 0.9734 | 1.9469 | 2.9203 | 3.8938 | 4.8672 | 5.8406 | 6.8141 | 7.7875 | 8.7609 | 1.3823 |
| 09 | 0.9733 | 1.9467 | 2.9200 | 3.8934 | 4.8667 | 5.8401 | 6.8134 | 7.7868 | 8.7601 | 1.3822 |
| 10 | 0.9733 | 1.9465 | 2.9198 | 3.8930 | 4.8663 | 5.8395 | 6.8128 | 7.7861 | 8.7593 | 1.3821 |
| 11 | 0.9732 | 1.9463 | 2.9195 | 3.8927 | 4.8658 | 5.8390 | 6.8122 | 7.7853 | 8.7585 | 1.3821 |
| 12 | 0.9731 | 1.9461 | 2.9192 | 3.8923 | 4.8654 | 5.8384 | 6.8115 | 7.7846 | 8.7577 | 1.3820 |
| 13 | 0.9730 | 1.9460 | 2.9189 | 3.8919 | 4.8649 | 5.8379 | 6.8109 | 7.7838 | 8.7568 | 1.3819 |
| 14 | 0.9729 | 1.9458 | 2.9187 | 3.8916 | 4.8644 | 5.8373 | 6.8102 | 7.7831 | 8.7560 | 1.3819 |
| 15 | 0.9728 | 1.9456 | 2.9184 | 3.8912 | 4.8640 | 5.8368 | 6.8096 | 7.7824 | 8.7552 | 1.3818 |
| 16 | 0.9727 | 1.9454 | 2.9181 | 3.8908 | 4.8635 | 5.8362 | 6.8089 | 7.7816 | 8.7543 | 1.3818 |
| 17 | 0.9726 | 1.9452 | 2.9178 | 3.8904 | 4.8631 | 5.8357 | 6.8083 | 7.7809 | 8.7535 | 1.3817 |
| 18 | 0.9725 | 1.9450 | 2.9176 | 3.8901 | 4.8626 | 5.8351 | 6.8076 | 7.7802 | 8.7527 | 1.3816 |
| 19 | 0.9724 | 1.9449 | 2.9173 | 3.8897 | 4.8621 | 5.8346 | 6.8070 | 7.7794 | 8.7518 | 1.3816 |
| 20 | 0.9723 | 1.9447 | 2.9170 | 3.8893 | 4.8617 | 5.8340 | 6.8063 | 7.7787 | 8.7510 | 1.3815 |
| 21 | 0.9722 | 1.9445 | 2.9167 | 3.8890 | 4.8612 | 5.8334 | 6.8057 | 7.7779 | 8.7502 | 1.3814 |
| 22 | 0.9721 | 1.9443 | 2.9164 | 3.8886 | 4.8607 | 5.8329 | 6.8050 | 7.7772 | 8.7493 | 1.3814 |
| 23 | 0.9721 | 1.9441 | 2.9162 | 3.8882 | 4.8603 | 5.8323 | 6.8044 | 7.7764 | 8.7485 | 1.3813 |
| 24 | 0.9720 | 1.9439 | 2.9159 | 3.8878 | 4.8598 | 5.8318 | 6.8037 | 7.7757 | 8.7476 | 1.3813 |
| 25 | 0.9719 | 1.9437 | 2.9156 | 3.8875 | 4.8593 | 5.8312 | 6.8031 | 7.7749 | 8.7468 | 1.3812 |
| 26 | 0.9718 | 1.9435 | 2.9153 | 3.8871 | 4.8589 | 5.8306 | 6.8024 | 7.7742 | 8.7460 | 1.3811 |
| 27 | 0.9717 | 1.9434 | 2.9150 | 3.8867 | 4.8584 | 5.8301 | 6.8018 | 7.7734 | 8.7451 | 1.3811 |
| 28 | 0.9716 | 1.9432 | 2.9148 | 3.8863 | 4.8579 | 5.8295 | 6.8011 | 7.7727 | 8.7443 | 1.3810 |
| 29 | 0.9715 | 1.9430 | 2.9145 | 3.8860 | 4.8575 | 5.8290 | 6.8004 | 7.7719 | 8.7434 | 1.3810 |
| 30 | 0.9714 | 1.9428 | 2.9142 | 3.8856 | 4.8570 | 5.8284 | 6.7998 | 7.7712 | 8.7426 | 1.3809 |
| 31 | 0.9713 | 1.9426 | 2.9139 | 3.8852 | 4.8565 | 5.8278 | 6.7991 | 7.7704 | 8.7417 | 1.3808 |
| 32 | 0.9712 | 1.9424 | 2.9136 | 3.8848 | 4.8560 | 5.8272 | 6.7984 | 7.7697 | 8.7409 | 1.3808 |
| 33 | 0.9711 | 1.9422 | 2.9133 | 3.8844 | 4.8556 | 5.8267 | 6.7976 | 7.7689 | 8.7400 | 1.3807 |
| 34 | 0.9710 | 1.9420 | 2.9130 | 3.8841 | 4.8551 | 5.8261 | 6.7971 | 7.7681 | 8.7391 | 1.3806 |
| 35 | 0.9709 | 1.9418 | 2.9128 | 3.8837 | 4.8546 | 5.8255 | 6.7964 | 7.7674 | 8.7383 | 1.3806 |
| 36 | 0.9708 | 1.9417 | 2.9125 | 3.8833 | 4.8541 | 5.8250 | 6.7958 | 7.7666 | 8.7374 | 1.3805 |
| 37 | 0.9707 | 1.9415 | 2.9122 | 3.8829 | 4.8537 | 5.8244 | 6.7951 | 7.7658 | 8.7366 | 1.3804 |
| 38 | 0.9706 | 1.9413 | 2.9119 | 3.8825 | 4.8532 | 5.8238 | 6.7944 | 7.7651 | 8.7357 | 1.3804 |
| 39 | 0.9705 | 1.9411 | 2.9116 | 3.8822 | 4.8527 | 5.8232 | 6.7938 | 7.7643 | 8.7349 | 1.3803 |
| 40 | 0.9704 | 1.9409 | 2.9113 | 3.8818 | 4.8522 | 5.8227 | 6.7931 | 7.7636 | 8.7340 | 1.3802 |
| 41 | 0.9703 | 1.9407 | 2.9110 | 3.8814 | 4.8517 | 5.8221 | 6.7924 | 7.7628 | 8.7331 | 1.3802 |
| 42 | 0.9703 | 1.9405 | 2.9108 | 3.8810 | 4.8513 | 5.8215 | 6.7918 | 7.7620 | 8.7323 | 1.3801 |
| 43 | 0.9702 | 1.9403 | 2.9105 | 3.8806 | 4.8508 | 5.8209 | 6.7911 | 7.7612 | 8.7314 | 1.3800 |
| 44 | 0.9701 | 1.9401 | 2.9102 | 3.8802 | 4.8503 | 5.8203 | 6.7904 | 7.7604 | 8.7305 | 1.3799 |
| 45 | 0.9700 | 1.9399 | 2.9099 | 3.8798 | 4.8498 | 5.8198 | 6.7897 | 7.7597 | 8.7296 | 1.3799 |
| 46 | 0.9699 | 1.9397 | 2.9096 | 3.8794 | 4.8493 | 5.8192 | 6.7890 | 7.7589 | 8.7288 | 1.3798 |
| 47 | 0.9698 | 1.9395 | 2.9093 | 3.8791 | 4.8488 | 5.8186 | 6.7884 | 7.7581 | 8.7279 | 1.3797 |
| 48 | 0.9697 | 1.9393 | 2.9090 | 3.8787 | 4.8483 | 5.8180 | 6.7877 | 7.7573 | 8.7270 | 1.3797 |
| 49 | 0.9696 | 1.9391 | 2.9087 | 3.8783 | 4.8479 | 5.8174 | 6.7870 | 7.7566 | 8.7261 | 1.3796 |
| 50 | 0.9695 | 1.9389 | 2.9084 | 3.8779 | 4.8474 | 5.8168 | 6.7863 | 7.7558 | 8.7253 | 1.3795 |
| 51 | 0.9694 | 1.9388 | 2.9081 | 3.8775 | 4.8469 | 5.8163 | 6.7856 | 7.7550 | 8.7244 | 1.3795 |
| 52 | 0.9693 | 1.9386 | 2.9078 | 3.8771 | 4.8464 | 5.8157 | 6.7849 | 7.7542 | 8.7235 | 1.3794 |
| 53 | 0.9692 | 1.9384 | 2.9075 | 3.8767 | 4.8459 | 5.8151 | 6.7843 | 7.7534 | 8.7226 | 1.3793 |
| 54 | 0.9691 | 1.9382 | 2.9072 | 3.8763 | 4.8454 | 5.8145 | 6.7836 | 7.7526 | 8.7217 | 1.3792 |
| 55 | 0.9690 | 1.9380 | 2.9069 | 3.8759 | 4.8449 | 5.8139 | 6.7829 | 7.7519 | 8.7208 | 1.3792 |
| 56 | 0.9689 | 1.9378 | 2.9066 | 3.8755 | 4.8444 | 5.8133 | 6.7822 | 7.7511 | 8.7199 | 1.3791 |
| 57 | 0.9688 | 1.9376 | 2.9064 | 3.8751 | 4.8439 | 5.8127 | 6.7815 | 7.7503 | 8.7191 | 1.3790 |
| 58 | 0.9687 | 1.9374 | 2.9061 | 3.8747 | 4.8434 | 5.8121 | 6.7808 | 7.7495 | 8.7182 | 1.3789 |
| 59 | 0.9686 | 1.9372 | 2.9058 | 3.8744 | 4.8429 | 5.8115 | 6.7801 | 7.7487 | 8.7173 | 1.3789 |
| 60 | 0.9685 | 1.9370 | 2.9055 | 3.8740 | 4.8424 | 5.8109 | 6.7794 | 7.7479 | 8.7164 | 1.3788 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1543 | 0.3086 | 0.4629 | 0.6172 | 0.7715 | 0.9257 | 1.0800 | 1.2343 | 1.3886 | 0.2190 | 00 |
| 0.1546 | 0.3091 | 0.4637 | 0.6183 | 0.7729 | 0.9274 | 1.0820 | 1.2365 | 1.3911 | 0.2194 | 01 |
| 0.1548 | 0.3097 | 0.4645 | 0.6194 | 0.7742 | 0.9290 | 1.0839 | 1.2387 | 1.3936 | 0.2198 | 02 |
| 0.1551 | 0.3102 | 0.4654 | 0.6205 | 0.7756 | 0.9307 | 1.0858 | 1.2410 | 1.3961 | 0.2202 | 03 |
| 0.1554 | 0.3108 | 0.4662 | 0.6216 | 0.7770 | 0.9324 | 1.0878 | 1.2432 | 1.3986 | 0.2206 | 04 |
| 0.1557 | 0.3113 | 0.4670 | 0.6227 | 0.7784 | 0.9340 | 1.0897 | 1.2454 | 1.4010 | 0.2210 | 05 |
| 0.1559 | 0.3119 | 0.4678 | 0.6238 | 0.7797 | 0.9357 | 1.0916 | 1.2476 | 1.4035 | 0.2214 | 06 |
| 0.1562 | 0.3124 | 0.4687 | 0.6249 | 0.7811 | 0.9373 | 1.0936 | 1.2498 | 1.4060 | 0.2218 | 07 |
| 0.1565 | 0.3130 | 0.4695 | 0.6260 | 0.7825 | 0.9390 | 1.0955 | 1.2520 | 1.4085 | 0.2222 | 08 |
| 0.1568 | 0.3136 | 0.4703 | 0.6271 | 0.7839 | 0.9407 | 1.0975 | 1.2542 | 1.4110 | 0.2226 | 09 |
| 0.1571 | 0.3141 | 0.4712 | 0.6282 | 0.7853 | 0.9423 | 1.0994 | 1.2564 | 1.4135 | 0.2230 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1573 | 0.3147 | 0.4720 | 0.6293 | 0.7866 | 0.9440 | 1.1013 | 1.2586 | 1.4160 | 0.2234 | 11 |
| 0.1576 | 0.3152 | 0.4728 | 0.6304 | 0.7880 | 0.9456 | 1.1032 | 1.2608 | 1.4184 | 0.2238 | 12 |
| 0.1579 | 0.3158 | 0.4736 | 0.6315 | 0.7894 | 0.9473 | 1.1052 | 1.2630 | 1.4209 | 0.2242 | 13 |
| 0.1582 | 0.3163 | 0.4745 | 0.6326 | 0.7908 | 0.9489 | 1.1071 | 1.2652 | 1.4234 | 0.2246 | 14 |
| 0.1584 | 0.3169 | 0.4753 | 0.6337 | 0.7922 | 0.9506 | 1.1090 | 1.2674 | 1.4259 | 0.2250 | 15 |
| 0.1587 | 0.3174 | 0.4761 | 0.6348 | 0.7935 | 0.9523 | 1.1110 | 1.2697 | 1.4284 | 0.2254 | 16 |
| 0.1590 | 0.3180 | 0.4769 | 0.6359 | 0.7949 | 0.9539 | 1.1129 | 1.2719 | 1.4308 | 0.2258 | 17 |
| 0.1593 | 0.3185 | 0.4778 | 0.6370 | 0.7963 | 0.9556 | 1.1148 | 1.2741 | 1.4333 | 0.2262 | 18 |
| 0.1595 | 0.3191 | 0.4786 | 0.6381 | 0.7977 | 0.9572 | 1.1167 | 1.2763 | 1.4358 | 0.2266 | 19 |
| 0.1598 | 0.3196 | 0.4794 | 0.6392 | 0.7991 | 0.9589 | 1.1187 | 1.2785 | 1.4383 | 0.2270 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1601 | 0.3202 | 0.4802 | 0.6403 | 0.8004 | 0.9605 | 1.1206 | 1.2807 | 1.4407 | 0.2274 | 21 |
| 0.1604 | 0.3207 | 0.4811 | 0.6414 | 0.8018 | 0.9622 | 1.1225 | 1.2829 | 1.4432 | 0.2278 | 22 |
| 0.1606 | 0.3213 | 0.4819 | 0.6425 | 0.8032 | 0.9638 | 1.1244 | 1.2851 | 1.4457 | 0.2282 | 23 |
| 0.1609 | 0.3218 | 0.4827 | 0.6436 | 0.8046 | 0.9655 | 1.1264 | 1.2873 | 1.4482 | 0.2287 | 24 |
| 0.1612 | 0.3224 | 0.4835 | 0.6447 | 0.8059 | 0.9671 | 1.1283 | 1.2895 | 1.4506 | 0.2291 | 25 |
| 0.1615 | 0.3229 | 0.4844 | 0.6458 | 0.8073 | 0.9688 | 1.1302 | 1.2917 | 1.4531 | 0.2295 | 26 |
| 0.1617 | 0.3235 | 0.4852 | 0.6469 | 0.8087 | 0.9704 | 1.1321 | 1.2939 | 1.4556 | 0.2299 | 27 |
| 0.1620 | 0.3240 | 0.4860 | 0.6480 | 0.8100 | 0.9721 | 1.1341 | 1.2961 | 1.4581 | 0.2303 | 28 |
| 0.1623 | 0.3246 | 0.4868 | 0.6491 | 0.8114 | 0.9737 | 1.1360 | 1.2983 | 1.4605 | 0.2307 | 29 |
| 0.1626 | 0.3251 | 0.4877 | 0.6502 | 0.8128 | 0.9754 | 1.1379 | 1.3005 | 1.4630 | 0.2311 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1628 | 0.3257 | 0.4885 | 0.6513 | 0.8142 | 0.9770 | 1.1398 | 1.3027 | 1.4655 | 0.2315 | 31 |
| 0.1631 | 0.3262 | 0.4893 | 0.6524 | 0.8155 | 0.9787 | 1.1418 | 1.3049 | 1.4680 | 0.2319 | 32 |
| 0.1634 | 0.3268 | 0.4901 | 0.6535 | 0.8169 | 0.9803 | 1.1437 | 1.3071 | 1.4704 | 0.2323 | 33 |
| 0.1637 | 0.3273 | 0.4910 | 0.6546 | 0.8183 | 0.9819 | 1.1456 | 1.3092 | 1.4729 | 0.2327 | 34 |
| 0.1639 | 0.3279 | 0.4918 | 0.6557 | 0.8196 | 0.9836 | 1.1475 | 1.3114 | 1.4754 | 0.2331 | 35 |
| 0.1642 | 0.3284 | 0.4926 | 0.6568 | 0.8210 | 0.9852 | 1.1494 | 1.3136 | 1.4778 | 0.2335 | 36 |
| 0.1645 | 0.3290 | 0.4934 | 0.6579 | 0.8224 | 0.9869 | 1.1514 | 1.3158 | 1.4803 | 0.2339 | 37 |
| 0.1648 | 0.3295 | 0.4943 | 0.6590 | 0.8238 | 0.9885 | 1.1533 | 1.3180 | 1.4828 | 0.2343 | 38 |
| 0.1650 | 0.3301 | 0.4951 | 0.6601 | 0.8251 | 0.9902 | 1.1552 | 1.3202 | 1.4853 | 0.2347 | 39 |
| 0.1653 | 0.3306 | 0.4959 | 0.6612 | 0.8265 | 0.9918 | 1.1571 | 1.3224 | 1.4877 | 0.2351 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1656 | 0.3311 | 0.4967 | 0.6623 | 0.8279 | 0.9934 | 1.1590 | 1.3246 | 1.4901 | 0.2355 | 41 |
| 0.1658 | 0.3317 | 0.4975 | 0.6634 | 0.8292 | 0.9951 | 1.1609 | 1.3268 | 1.4926 | 0.2359 | 42 |
| 0.1661 | 0.3322 | 0.4984 | 0.6645 | 0.8306 | 0.9967 | 1.1629 | 1.3290 | 1.4951 | 0.2363 | 43 |
| 0.1664 | 0.3328 | 0.4992 | 0.6656 | 0.8320 | 0.9984 | 1.1648 | 1.3312 | 1.4976 | 0.2367 | 44 |
| 0.1667 | 0.3333 | 0.5000 | 0.6667 | 0.8334 | 1.0000 | 1.1667 | 1.3334 | 1.5000 | 0.2371 | 45 |
| 0.1669 | 0.3339 | 0.5008 | 0.6678 | 0.8347 | 1.0016 | 1.1686 | 1.3355 | 1.5025 | 0.2375 | 46 |
| 0.1672 | 0.3344 | 0.5017 | 0.6689 | 0.8361 | 1.0033 | 1.1705 | 1.3378 | 1.5050 | 0.2379 | 47 |
| 0.1675 | 0.3350 | 0.5025 | 0.6700 | 0.8375 | 1.0049 | 1.1724 | 1.3399 | 1.5074 | 0.2383 | 48 |
| 0.1678 | 0.3355 | 0.5033 | 0.6711 | 0.8388 | 1.0066 | 1.1743 | 1.3421 | 1.5098 | 0.2387 | 49 |
| 0.1680 | 0.3361 | 0.5041 | 0.6722 | 0.8402 | 1.0082 | 1.1763 | 1.3443 | 1.5123 | 0.2391 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.1683 | 0.3366 | 0.5049 | 0.6732 | 0.8416 | 1.0099 | 1.1782 | 1.3465 | 1.5148 | 0.2395 | 51 |
| 0.1686 | 0.3372 | 0.5057 | 0.6743 | 0.8429 | 1.0115 | 1.1801 | 1.3487 | 1.5172 | 0.2399 | 52 |
| 0.1689 | 0.3377 | 0.5066 | 0.6754 | 0.8443 | 1.0132 | 1.1820 | 1.3509 | 1.5197 | 0.2403 | 53 |
| 0.1691 | 0.3383 | 0.5074 | 0.6765 | 0.8457 | 1.0148 | 1.1839 | 1.3531 | 1.5222 | 0.2407 | 54 |
| 0.1694 | 0.3388 | 0.5082 | 0.6776 | 0.8470 | 1.0165 | 1.1859 | 1.3553 | 1.5247 | 0.2411 | 55 |
| 0.1697 | 0.3394 | 0.5090 | 0.6787 | 0.8484 | 1.0181 | 1.1878 | 1.3574 | 1.5271 | 0.2415 | 56 |
| 0.1700 | 0.3399 | 0.5099 | 0.6798 | 0.8498 | 1.0197 | 1.1897 | 1.3596 | 1.5296 | 0.2419 | 57 |
| 0.1702 | 0.3404 | 0.5107 | 0.6809 | 0.8511 | 1.0213 | 1.1916 | 1.3618 | 1.5320 | 0.2423 | 58 |
| 0.1705 | 0.3410 | 0.5115 | 0.6820 | 0.8525 | 1.0230 | 1.1935 | 1.3640 | 1.5345 | 0.2427 | 59 |
| 0.1708 | 0.3415 | 0.5123 | 0.6831 | 0.8539 | 1.0246 | 1.1954 | 1.3662 | 1.5369 | 0.2431 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9685 | 1.9370 | 2.9055 | 3.8740 | 4.8424 | 5.8109 | 6.7794 | 7.7479 | 8.7164 | 1.3788 |
| 01 | 0.9684 | 1.9368 | 2.9052 | 3.8736 | 4.8419 | 5.8103 | 6.7787 | 7.7471 | 8.7155 | 1.3787 |
| 02 | 0.9683 | 1.9366 | 2.9049 | 3.8732 | 4.8414 | 5.8097 | 6.7780 | 7.7463 | 8.7146 | 1.3786 |
| 03 | 0.9682 | 1.9364 | 2.9046 | 3.8728 | 4.8409 | 5.8091 | 6.7773 | 7.7455 | 8.7137 | 1.3786 |
| 04 | 0.9681 | 1.9362 | 2.9043 | 3.8724 | 4.8404 | 5.8085 | 6.7766 | 7.7447 | 8.7128 | 1.3785 |
| 05 | 0.9680 | 1.9360 | 2.9040 | 3.8720 | 4.8399 | 5.8079 | 6.7759 | 7.7439 | 8.7119 | 1.3784 |
| 06 | 0.9679 | 1.9358 | 2.9037 | 3.8716 | 4.8394 | 5.8073 | 6.7752 | 7.7431 | 8.7110 | 1.3783 |
| 07 | 0.9678 | 1.9356 | 2.9034 | 3.8712 | 4.8389 | 5.8067 | 6.7745 | 7.7423 | 8.7101 | 1.3783 |
| 08 | 0.9677 | 1.9354 | 2.9031 | 3.8707 | 4.8384 | 5.8061 | 6.7738 | 7.7415 | 8.7092 | 1.3782 |
| 09 | 0.9676 | 1.9352 | 2.9028 | 3.8703 | 4.8379 | 5.8055 | 6.7731 | 7.7407 | 8.7083 | 1.3781 |
| 10 | 0.9675 | 1.9350 | 2.9025 | 3.8699 | 4.8374 | 5.8049 | 6.7724 | 7.7399 | 8.7074 | 1.3780 |
| 11 | 0.9674 | 1.9348 | 2.9022 | 3.8695 | 4.8369 | 5.8043 | 6.7717 | 7.7391 | 8.7065 | 1.3780 |
| 12 | 0.9673 | 1.9346 | 2.9019 | 3.8691 | 4.8364 | 5.8037 | 6.7710 | 7.7383 | 8.7056 | 1.3779 |
| 13 | 0.9672 | 1.9344 | 2.9015 | 3.8687 | 4.8359 | 5.8031 | 6.7703 | 7.7375 | 8.7046 | 1.3778 |
| 14 | 0.9671 | 1.9342 | 2.9012 | 3.8683 | 4.8354 | 5.8025 | 6.7696 | 7.7366 | 8.7037 | 1.3777 |
| 15 | 0.9670 | 1.9340 | 2.9009 | 3.8679 | 4.8349 | 5.8019 | 6.7689 | 7.7358 | 8.7028 | 1.3776 |
| 16 | 0.9669 | 1.9338 | 2.9006 | 3.8675 | 4.8344 | 5.8011 | 6.7681 | 7.7350 | 8.7019 | 1.3776 |
| 17 | 0.9668 | 1.9336 | 2.9003 | 3.8671 | 4.8339 | 5.8007 | 6.7674 | 7.7342 | 8.7010 | 1.3775 |
| 18 | 0.9667 | 1.9333 | 2.9000 | 3.8667 | 4.8334 | 5.8000 | 6.7667 | 7.7334 | 8.7001 | 1.3774 |
| 19 | 0.9666 | 1.9331 | 2.8997 | 3.8663 | 4.8329 | 5.7994 | 6.7660 | 7.7326 | 8.6991 | 1.3773 |
| 20 | 0.9665 | 1.9329 | 2.8994 | 3.8659 | 4.8324 | 5.7988 | 6.7653 | 7.7318 | 8.6982 | 1.3773 |
| 21 | 0.9664 | 1.9327 | 2.8991 | 3.8655 | 4.8318 | 5.7982 | 6.7646 | 7.7309 | 8.6973 | 1.3772 |
| 22 | 0.9663 | 1.9325 | 2.8988 | 3.8651 | 4.8313 | 5.7976 | 6.7638 | 7.7301 | 8.6964 | 1.3771 |
| 23 | 0.9662 | 1.9323 | 2.8985 | 3.8646 | 4.8308 | 5.7970 | 6.7631 | 7.7293 | 8.6954 | 1.3770 |
| 24 | 0.9661 | 1.9321 | 2.8982 | 3.8642 | 4.8303 | 5.7963 | 6.7624 | 7.7285 | 8.6945 | 1.3769 |
| 25 | 0.9660 | 1.9319 | 2.8979 | 3.8638 | 4.8298 | 5.7957 | 6.7617 | 7.7276 | 8.6936 | 1.3769 |
| 26 | 0.9659 | 1.9317 | 2.8976 | 3.8634 | 4.8293 | 5.7951 | 6.7610 | 7.7268 | 8.6927 | 1.3768 |
| 27 | 0.9657 | 1.9315 | 2.8972 | 3.8630 | 4.8287 | 5.7945 | 6.7602 | 7.7260 | 8.6917 | 1.3767 |
| 28 | 0.9656 | 1.9313 | 2.8969 | 3.8626 | 4.8282 | 5.7939 | 6.7595 | 7.7252 | 8.6908 | 1.3766 |
| 29 | 0.9655 | 1.9311 | 2.8966 | 3.8622 | 4.8277 | 5.7932 | 6.7588 | 7.7243 | 8.6899 | 1.3765 |
| 30 | 0.9654 | 1.9309 | 2.8963 | 3.8617 | 4.8272 | 5.7926 | 6.7581 | 7.7235 | 8.6889 | 1.3765 |
| 31 | 0.9653 | 1.9307 | 2.8960 | 3.8613 | 4.8267 | 5.7920 | 6.7573 | 7.7227 | 8.6880 | 1.3764 |
| 32 | 0.9652 | 1.9305 | 2.8957 | 3.8609 | 4.8261 | 5.7914 | 6.7566 | 7.7218 | 8.6870 | 1.3763 |
| 33 | 0.9651 | 1.9302 | 2.8954 | 3.8605 | 4.8256 | 5.7907 | 6.7559 | 7.7210 | 8.6861 | 1.3762 |
| 34 | 0.9650 | 1.9300 | 2.8951 | 3.8601 | 4.8251 | 5.7901 | 6.7551 | 7.7201 | 8.6852 | 1.3761 |
| 35 | 0.9649 | 1.9298 | 2.8947 | 3.8597 | 4.8246 | 5.7895 | 6.7544 | 7.7193 | 8.6842 | 1.3761 |
| 36 | 0.9648 | 1.9296 | 2.8944 | 3.8592 | 4.8240 | 5.7888 | 6.7537 | 7.7185 | 8.6833 | 1.3760 |
| 37 | 0.9647 | 1.9294 | 2.8941 | 3.8588 | 4.8235 | 5.7882 | 6.7529 | 7.7176 | 8.6823 | 1.3759 |
| 38 | 0.9646 | 1.9292 | 2.8938 | 3.8584 | 4.8230 | 5.7876 | 6.7522 | 7.7168 | 8.6814 | 1.3759 |
| 39 | 0.9645 | 1.9290 | 2.8935 | 3.8580 | 4.8225 | 5.7870 | 6.7515 | 7.7159 | 8.6804 | 1.3758 |
| 40 | 0.9644 | 1.9288 | 2.8932 | 3.8576 | 4.8219 | 5.7863 | 6.7507 | 7.7151 | 8.6795 | 1.3757 |
| 41 | 0.9643 | 1.9286 | 2.8928 | 3.8571 | 4.8214 | 5.7857 | 6.7500 | 7.7143 | 8.6785 | 1.3756 |
| 42 | 0.9642 | 1.9284 | 2.8925 | 3.8567 | 4.8209 | 5.7851 | 6.7492 | 7.7134 | 8.6776 | 1.3755 |
| 43 | 0.9641 | 1.9281 | 2.8922 | 3.8563 | 4.8203 | 5.7844 | 6.7485 | 7.7126 | 8.6766 | 1.3755 |
| 44 | 0.9640 | 1.9279 | 2.8919 | 3.8558 | 4.8198 | 5.7838 | 6.7477 | 7.7117 | 8.6757 | 1.3754 |
| 45 | 0.9639 | 1.9277 | 2.8916 | 3.8554 | 4.8193 | 5.7831 | 6.7470 | 7.7108 | 8.6747 | 1.3753 |
| 46 | 0.9638 | 1.9275 | 2.8912 | 3.8550 | 4.8187 | 5.7825 | 6.7462 | 7.7100 | 8.6737 | 1.3752 |
| 47 | 0.9636 | 1.9273 | 2.8909 | 3.8546 | 4.8182 | 5.7819 | 6.7455 | 7.7091 | 8.6728 | 1.3752 |
| 48 | 0.9635 | 1.9271 | 2.8906 | 3.8541 | 4.8177 | 5.7812 | 6.7448 | 7.7083 | 8.6718 | 1.3751 |
| 49 | 0.9634 | 1.9269 | 2.8903 | 3.8537 | 4.8172 | 5.7806 | 6.7440 | 7.7074 | 8.6709 | 1.3750 |
| 50 | 0.9633 | 1.9266 | 2.8900 | 3.8533 | 4.8166 | 5.7799 | 6.7433 | 7.7066 | 8.6699 | 1.3749 |
| 51 | 0.9632 | 1.9264 | 2.8896 | 3.8529 | 4.8161 | 5.7793 | 6.7425 | 7.7057 | 8.6689 | 1.3748 |
| 52 | 0.9631 | 1.9262 | 2.8893 | 3.8524 | 4.8155 | 5.7786 | 6.7417 | 7.7049 | 8.6680 | 1.3748 |
| 53 | 0.9630 | 1.9260 | 2.8890 | 3.8520 | 4.8150 | 5.7780 | 6.7410 | 7.7040 | 8.6670 | 1.3747 |
| 54 | 0.9629 | 1.9258 | 2.8887 | 3.8516 | 4.8145 | 5.7773 | 6.7402 | 7.7031 | 8.6660 | 1.3746 |
| 55 | 0.9628 | 1.9256 | 2.8883 | 3.8511 | 4.8139 | 5.7767 | 6.7395 | 7.7023 | 8.6650 | 1.3745 |
| 56 | 0.9627 | 1.9254 | 2.8880 | 3.8507 | 4.8134 | 5.7761 | 6.7387 | 7.7014 | 8.6641 | 1.3744 |
| 57 | 0.9626 | 1.9251 | 2.8877 | 3.8503 | 4.8128 | 5.7754 | 6.7380 | 7.7005 | 8.6631 | 1.3744 |
| 58 | 0.9625 | 1.9249 | 2.8874 | 3.8498 | 4.8123 | 5.7748 | 6.7372 | 7.6997 | 8.6621 | 1.3743 |
| 59 | 0.9624 | 1.9247 | 2.8871 | 3.8494 | 4.8118 | 5.7741 | 6.7365 | 7.6988 | 8.6612 | 1.3742 |
| 60 | 0.9622 | 1.9245 | 2.8867 | 3.8490 | 4.8112 | 5.7735 | 6.7357 | 7.6979 | 8.6602 | 1.3742 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | /  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1708 | 0.3415 | 0.5123 | 0.6831 | 0.8539 | 1.0246 | 1.1954 | 1.3662 | 1.5369 | 0.2431 | 00 |
| 0.1710 | 0.3421 | 0.5131 | 0.6842 | 0.8552 | 1.0262 | 1.1973 | 1.3683 | 1.5394 | 0.2435 | 01 |
| 0.1713 | 0.3426 | 0.5140 | 0.6853 | 0.8566 | 1.0279 | 1.1992 | 1.3705 | 1.5419 | 0.2439 | 02 |
| 0.1716 | 0.3432 | 0.5148 | 0.6864 | 0.8580 | 1.0295 | 1.2011 | 1.3727 | 1.5443 | 0.2443 | 03 |
| 0.1719 | 0.3437 | 0.5156 | 0.6875 | 0.8593 | 1.0312 | 1.2030 | 1.3749 | 1.5468 | 0.2447 | 04 |
| 0.1721 | 0.3443 | 0.5164 | 0.6886 | 0.8607 | 1.0328 | 1.2050 | 1.3771 | 1.5493 | 0.2451 | 05 |
| 0.1724 | 0.3448 | 0.5173 | 0.6896 | 0.8620 | 1.0345 | 1.2069 | 1.3793 | 1.5517 | 0.2455 | 06 |
| 0.1727 | 0.3454 | 0.5180 | 0.6907 | 0.8634 | 1.0361 | 1.2088 | 1.3814 | 1.5541 | 0.2459 | 07 |
| 0.1730 | 0.3459 | 0.5189 | 0.6918 | 0.8648 | 1.0377 | 1.2107 | 1.3836 | 1.5566 | 0.2463 | 08 |
| 0.1732 | 0.3464 | 0.5197 | 0.6929 | 0.8661 | 1.0393 | 1.2126 | 1.3858 | 1.5590 | 0.2467 | 09 |
| 0.1735 | 0.3470 | 0.5205 | 0.6940 | 0.8675 | 1.0410 | 1.2145 | 1.3880 | 1.5615 | 0.2471 | 10 |
| 0.1738 | 0.3475 | 0.5213 | 0.6951 | 0.8688 | 1.0426 | 1.2164 | 1.3902 | 1.5639 | 0.2475 | 11 |
| 0.1740 | 0.3481 | 0.5221 | 0.6962 | 0.8702 | 1.0442 | 1.2183 | 1.3923 | 1.5664 | 0.2479 | 12 |
| 0.1743 | 0.3486 | 0.5229 | 0.6973 | 0.8716 | 1.0459 | 1.2202 | 1.3945 | 1.5688 | 0.2483 | 13 |
| 0.1746 | 0.3492 | 0.5238 | 0.6984 | 0.8729 | 1.0475 | 1.2221 | 1.3967 | 1.5713 | 0.2487 | 14 |
| 0.1749 | 0.3497 | 0.5246 | 0.6994 | 0.8743 | 1.0492 | 1.2240 | 1.3989 | 1.5737 | 0.2491 | 15 |
| 0.1751 | 0.3503 | 0.5254 | 0.7005 | 0.8757 | 1.0508 | 1.2259 | 1.4010 | 1.5762 | 0.2495 | 16 |
| 0.1754 | 0.3508 | 0.5262 | 0.7016 | 0.8770 | 1.0524 | 1.2278 | 1.4032 | 1.5786 | 0.2499 | 17 |
| 0.1757 | 0.3513 | 0.5270 | 0.7027 | 0.8784 | 1.0540 | 1.2297 | 1.4054 | 1.5810 | 0.2503 | 18 |
| 0.1759 | 0.3519 | 0.5278 | 0.7038 | 0.8797 | 1.0557 | 1.2316 | 1.4076 | 1.5835 | 0.2507 | 19 |
| 0.1762 | 0.3524 | 0.5287 | 0.7049 | 0.8811 | 1.0573 | 1.2335 | 1.4098 | 1.5860 | 0.2511 | 20 |
| 0.1765 | 0.3530 | 0.5295 | 0.7060 | 0.8824 | 1.0589 | 1.2354 | 1.4119 | 1.5884 | 0.2515 | 21 |
| 0.1768 | 0.3535 | 0.5303 | 0.7070 | 0.8838 | 1.0606 | 1.2373 | 1.4141 | 1.5908 | 0.2519 | 22 |
| 0.1770 | 0.3541 | 0.5311 | 0.7081 | 0.8852 | 1.0622 | 1.2392 | 1.4162 | 1.5933 | 0.2523 | 23 |
| 0.1773 | 0.3546 | 0.5319 | 0.7092 | 0.8865 | 1.0638 | 1.2411 | 1.4184 | 1.5957 | 0.2527 | 24 |
| 0.1776 | 0.3552 | 0.5327 | 0.7103 | 0.8879 | 1.0655 | 1.2430 | 1.4206 | 1.5982 | 0.2531 | 25 |
| 0.1778 | 0.3557 | 0.5335 | 0.7114 | 0.8892 | 1.0671 | 1.2449 | 1.4228 | 1.6006 | 0.2535 | 26 |
| 0.1781 | 0.3562 | 0.5344 | 0.7125 | 0.8906 | 1.0687 | 1.2468 | 1.4250 | 1.6031 | 0.2539 | 27 |
| 0.1784 | 0.3568 | 0.5352 | 0.7136 | 0.8920 | 1.0703 | 1.2487 | 1.4271 | 1.6055 | 0.2543 | 28 |
| 0.1787 | 0.3573 | 0.5360 | 0.7146 | 0.8933 | 1.0720 | 1.2506 | 1.4293 | 1.6079 | 0.2547 | 29 |
| 0.1789 | 0.3579 | 0.5368 | 0.7157 | 0.8947 | 1.0736 | 1.2525 | 1.4314 | 1.6104 | 0.2551 | 30 |
| 0.1792 | 0.3584 | 0.5376 | 0.7168 | 0.8960 | 1.0752 | 1.2544 | 1.4336 | 1.6128 | 0.2555 | 31 |
| 0.1795 | 0.3590 | 0.5384 | 0.7179 | 0.8974 | 1.0769 | 1.2563 | 1.4358 | 1.6153 | 0.2559 | 32 |
| 0.1797 | 0.3595 | 0.5392 | 0.7190 | 0.8987 | 1.0785 | 1.2582 | 1.4380 | 1.6177 | 0.2563 | 33 |
| 0.1800 | 0.3600 | 0.5401 | 0.7201 | 0.9001 | 1.0801 | 1.2601 | 1.4402 | 1.6202 | 0.2567 | 34 |
| 0.1803 | 0.3606 | 0.5409 | 0.7212 | 0.9014 | 1.0817 | 1.2620 | 1.4423 | 1.6226 | 0.2571 | 35 |
| 0.1806 | 0.3611 | 0.5417 | 0.7222 | 0.9028 | 1.0834 | 1.2639 | 1.4445 | 1.6250 | 0.2575 | 36 |
| 0.1808 | 0.3617 | 0.5425 | 0.7233 | 0.9041 | 1.0850 | 1.2658 | 1.4466 | 1.6275 | 0.2579 | 37 |
| 0.1811 | 0.3622 | 0.5433 | 0.7244 | 0.9055 | 1.0866 | 1.2677 | 1.4488 | 1.6299 | 0.2583 | 38 |
| 0.1814 | 0.3627 | 0.5441 | 0.7255 | 0.9069 | 1.0882 | 1.2696 | 1.4510 | 1.6323 | 0.2587 | 39 |
| 0.1816 | 0.3633 | 0.5449 | 0.7266 | 0.9082 | 1.0898 | 1.2715 | 1.4531 | 1.6348 | 0.2591 | 40 |
| 0.1819 | 0.3638 | 0.5457 | 0.7276 | 0.9096 | 1.0915 | 1.2734 | 1.4553 | 1.6372 | 0.2595 | 41 |
| 0.1822 | 0.3644 | 0.5465 | 0.7287 | 0.9109 | 1.0931 | 1.2753 | 1.4574 | 1.6396 | 0.2599 | 42 |
| 0.1825 | 0.3649 | 0.5474 | 0.7298 | 0.9123 | 1.0947 | 1.2772 | 1.4596 | 1.6421 | 0.2603 | 43 |
| 0.1827 | 0.3654 | 0.5482 | 0.7309 | 0.9136 | 1.0963 | 1.2790 | 1.4618 | 1.6445 | 0.2607 | 44 |
| 0.1830 | 0.3660 | 0.5490 | 0.7320 | 0.9150 | 1.0979 | 1.2809 | 1.4639 | 1.6469 | 0.2611 | 45 |
| 0.1833 | 0.3665 | 0.5498 | 0.7330 | 0.9163 | 1.0996 | 1.2828 | 1.4661 | 1.6493 | 0.2615 | 46 |
| 0.1835 | 0.3671 | 0.5506 | 0.7341 | 0.9177 | 1.1012 | 1.2847 | 1.4682 | 1.6518 | 0.2619 | 47 |
| 0.1838 | 0.3676 | 0.5514 | 0.7352 | 0.9190 | 1.1028 | 1.2866 | 1.4704 | 1.6542 | 0.2623 | 48 |
| 0.1841 | 0.3681 | 0.5522 | 0.7363 | 0.9204 | 1.1044 | 1.2885 | 1.4726 | 1.6566 | 0.2627 | 49 |
| 0.1843 | 0.3687 | 0.5530 | 0.7374 | 0.9217 | 1.1061 | 1.2904 | 1.4748 | 1.6591 | 0.2631 | 50 |
| 0.1846 | 0.3692 | 0.5538 | 0.7384 | 0.9231 | 1.1077 | 1.2923 | 1.4769 | 1.6615 | 0.2635 | 51 |
| 0.1849 | 0.3698 | 0.5546 | 0.7395 | 0.9244 | 1.1093 | 1.2942 | 1.4790 | 1.6639 | 0.2639 | 52 |
| 0.1852 | 0.3703 | 0.5555 | 0.7406 | 0.9258 | 1.1109 | 1.2961 | 1.4812 | 1.6664 | 0.2643 | 53 |
| 0.1854 | 0.3708 | 0.5563 | 0.7417 | 0.9271 | 1.1125 | 1.2979 | 1.4834 | 1.6688 | 0.2647 | 54 |
| 0.1857 | 0.3714 | 0.5571 | 0.7428 | 0.9285 | 1.1141 | 1.2998 | 1.4855 | 1.6712 | 0.2651 | 55 |
| 0.1860 | 0.3719 | 0.5579 | 0.7438 | 0.9298 | 1.1158 | 1.3017 | 1.4877 | 1.6736 | 0.2655 | 56 |
| 0.1862 | 0.3725 | 0.5587 | 0.7449 | 0.9312 | 1.1174 | 1.3036 | 1.4898 | 1.6761 | 0.2659 | 57 |
| 0.1865 | 0.3730 | 0.5595 | 0.7460 | 0.9325 | 1.1190 | 1.3055 | 1.4920 | 1.6785 | 0.2663 | 58 |
| 0.1868 | 0.3735 | 0.5603 | 0.7471 | 0.9339 | 1.1206 | 1.3074 | 1.4942 | 1.6809 | 0.2667 | 59 |
| 0.1870 | 0.3741 | 0.5611 | 0.7482 | 0.9352 | 1.1222 | 1.3093 | 1.4963 | 1.6834 | 0.2671 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10     |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9622 | 1.9245 | 2.8867 | 3.8490 | 4.8112 | 5.7735 | 6.7357 | 7.6979 | 8.6602 | 1.3742 |
| 01 | 0.9621 | 1.9243 | 2.8864 | 3.8485 | 4.8107 | 5.7728 | 6.7349 | 7.6971 | 8.6592 | 1.3741 |
| 02 | 0.9620 | 1.9240 | 2.8861 | 3.8481 | 4.8101 | 5.7721 | 6.7342 | 7.6962 | 8.6582 | 1.3740 |
| 03 | 0.9619 | 1.9238 | 2.8857 | 3.8477 | 4.8096 | 5.7715 | 6.7334 | 7.6953 | 8.6572 | 1.3739 |
| 04 | 0.9618 | 1.9236 | 2.8854 | 3.8472 | 4.8090 | 5.7708 | 6.7326 | 7.6944 | 8.6562 | 1.3738 |
| 05 | 0.9617 | 1.9234 | 2.8851 | 3.8468 | 4.8085 | 5.7702 | 6.7319 | 7.6936 | 8.6553 | 1.3738 |
| 06 | 0.9616 | 1.9232 | 2.8848 | 3.8463 | 4.8079 | 5.7695 | 6.7311 | 7.6927 | 8.6543 | 1.3737 |
| 07 | 0.9615 | 1.9230 | 2.8844 | 3.8459 | 4.8074 | 5.7689 | 6.7303 | 7.6918 | 8.6533 | 1.3736 |
| 08 | 0.9614 | 1.9227 | 2.8841 | 3.8455 | 4.8068 | 5.7682 | 6.7296 | 7.6909 | 8.6523 | 1.3735 |
| 09 | 0.9613 | 1.9225 | 2.8838 | 3.8450 | 4.8063 | 5.7675 | 6.7288 | 7.6901 | 8.6513 | 1.3734 |
| 10 | 0.9611 | 1.9223 | 2.8834 | 3.8446 | 4.8057 | 5.7669 | 6.7280 | 7.6892 | 8.6503 | 1.3734 |
| 11 | 0.9610 | 1.9221 | 2.8831 | 3.8441 | 4.8052 | 5.7662 | 6.7273 | 7.6883 | 8.6493 | 1.3733 |
| 12 | 0.9609 | 1.9218 | 2.8828 | 3.8437 | 4.8046 | 5.7655 | 6.7265 | 7.6874 | 8.6483 | 1.3732 |
| 13 | 0.9608 | 1.9216 | 2.8824 | 3.8433 | 4.8041 | 5.7649 | 6.7257 | 7.6865 | 8.6473 | 1.3731 |
| 14 | 0.9607 | 1.9214 | 2.8821 | 3.8428 | 4.8035 | 5.7642 | 6.7249 | 7.6856 | 8.6463 | 1.3730 |
| 15 | 0.9606 | 1.9212 | 2.8818 | 3.8424 | 4.8030 | 5.7635 | 6.7241 | 7.6847 | 8.6453 | 1.3730 |
| 16 | 0.9605 | 1.9210 | 2.8814 | 3.8419 | 4.8024 | 5.7629 | 6.7234 | 7.6838 | 8.6443 | 1.3729 |
| 17 | 0.9604 | 1.9207 | 2.8811 | 3.8415 | 4.8018 | 5.7622 | 6.7226 | 7.6830 | 8.6433 | 1.3728 |
| 18 | 0.9603 | 1.9205 | 2.8808 | 3.8410 | 4.8013 | 5.7615 | 6.7218 | 7.6821 | 8.6423 | 1.3727 |
| 19 | 0.9601 | 1.9203 | 2.8804 | 3.8405 | 4.8007 | 5.7609 | 6.7210 | 7.6812 | 8.6413 | 1.3726 |
| 20 | 0.9600 | 1.9201 | 2.8801 | 3.8401 | 4.8002 | 5.7602 | 6.7202 | 7.6803 | 8.6403 | 1.3726 |
| 21 | 0.9599 | 1.9198 | 2.8798 | 3.8397 | 4.7996 | 5.7595 | 6.7195 | 7.6794 | 8.6393 | 1.3725 |
| 22 | 0.9598 | 1.9196 | 2.8794 | 3.8392 | 4.7990 | 5.7589 | 6.7187 | 7.6785 | 8.6383 | 1.3724 |
| 23 | 0.9597 | 1.9194 | 2.8791 | 3.8388 | 4.7985 | 5.7582 | 6.7179 | 7.6776 | 8.6373 | 1.3723 |
| 24 | 0.9596 | 1.9192 | 2.8788 | 3.8383 | 4.7979 | 5.7575 | 6.7171 | 7.6767 | 8.6363 | 1.3722 |
| 25 | 0.9595 | 1.9189 | 2.8784 | 3.8379 | 4.7974 | 5.7568 | 6.7163 | 7.6758 | 8.6352 | 1.3722 |
| 26 | 0.9594 | 1.9187 | 2.8781 | 3.8374 | 4.7968 | 5.7562 | 6.7155 | 7.6749 | 8.6342 | 1.3721 |
| 27 | 0.9592 | 1.9185 | 2.8777 | 3.8370 | 4.7962 | 5.7555 | 6.7147 | 7.6740 | 8.6332 | 1.3720 |
| 28 | 0.9591 | 1.9183 | 2.8774 | 3.8365 | 4.7957 | 5.7548 | 6.7139 | 7.6731 | 8.6322 | 1.3719 |
| 29 | 0.9590 | 1.9180 | 2.8771 | 3.8361 | 4.7951 | 5.7541 | 6.7131 | 7.6722 | 8.6312 | 1.3718 |
| 30 | 0.9589 | 1.9178 | 2.8767 | 3.8356 | 4.7945 | 5.7534 | 6.7124 | 7.6713 | 8.6302 | 1.3718 |
| 31 | 0.9588 | 1.9176 | 2.8764 | 3.8352 | 4.7940 | 5.7528 | 6.7116 | 7.6704 | 8.6291 | 1.3717 |
| 32 | 0.9587 | 1.9174 | 2.8760 | 3.8347 | 4.7934 | 5.7521 | 6.7108 | 7.6694 | 8.6281 | 1.3716 |
| 33 | 0.9586 | 1.9171 | 2.8757 | 3.8343 | 4.7928 | 5.7514 | 6.7100 | 7.6685 | 8.6271 | 1.3715 |
| 34 | 0.9585 | 1.9169 | 2.8754 | 3.8338 | 4.7923 | 5.7507 | 6.7092 | 7.6676 | 8.6261 | 1.3714 |
| 35 | 0.9583 | 1.9167 | 2.8750 | 3.8333 | 4.7917 | 5.7500 | 6.7084 | 7.6667 | 8.6250 | 1.3714 |
| 36 | 0.9582 | 1.9164 | 2.8747 | 3.8329 | 4.7911 | 5.7493 | 6.7076 | 7.6658 | 8.6240 | 1.3713 |
| 37 | 0.9581 | 1.9162 | 2.8743 | 3.8324 | 4.7905 | 5.7487 | 6.7068 | 7.6649 | 8.6230 | 1.3712 |
| 38 | 0.9580 | 1.9160 | 2.8740 | 3.8320 | 4.7900 | 5.7480 | 6.7060 | 7.6640 | 8.6219 | 1.3711 |
| 39 | 0.9579 | 1.9158 | 2.8736 | 3.8315 | 4.7894 | 5.7473 | 6.7052 | 7.6630 | 8.6209 | 1.3710 |
| 40 | 0.9578 | 1.9155 | 2.8733 | 3.8311 | 4.7888 | 5.7466 | 6.7044 | 7.6621 | 8.6199 | 1.3710 |
| 41 | 0.9577 | 1.9153 | 2.8730 | 3.8306 | 4.7883 | 5.7459 | 6.7036 | 7.6612 | 8.6189 | 1.3709 |
| 42 | 0.9575 | 1.9151 | 2.8726 | 3.8301 | 4.7877 | 5.7452 | 6.7027 | 7.6603 | 8.6178 | 1.3708 |
| 43 | 0.9574 | 1.9148 | 2.8723 | 3.8297 | 4.7871 | 5.7445 | 6.7019 | 7.6593 | 8.6168 | 1.3707 |
| 44 | 0.9573 | 1.9146 | 2.8719 | 3.8292 | 4.7865 | 5.7438 | 6.7011 | 7.6584 | 8.6157 | 1.3706 |
| 45 | 0.9572 | 1.9144 | 2.8716 | 3.8287 | 4.7859 | 5.7431 | 6.7003 | 7.6575 | 8.6147 | 1.3706 |
| 46 | 0.9571 | 1.9141 | 2.8712 | 3.8283 | 4.7854 | 5.7424 | 6.6995 | 7.6566 | 8.6136 | 1.3705 |
| 47 | 0.9570 | 1.9139 | 2.8709 | 3.8278 | 4.7848 | 5.7417 | 6.6987 | 7.6556 | 8.6126 | 1.3704 |
| 48 | 0.9568 | 1.9137 | 2.8705 | 3.8274 | 4.7842 | 5.7410 | 6.6979 | 7.6547 | 8.6116 | 1.3703 |
| 49 | 0.9567 | 1.9134 | 2.8702 | 3.8269 | 4.7836 | 5.7403 | 6.6971 | 7.6538 | 8.6105 | 1.3702 |
| 50 | 0.9566 | 1.9132 | 2.8698 | 3.8264 | 4.7830 | 5.7396 | 6.6962 | 7.6529 | 8.6095 | 1.3702 |
| 51 | 0.9565 | 1.9130 | 2.8695 | 3.8260 | 4.7824 | 5.7389 | 6.6954 | 7.6519 | 8.6084 | 1.3701 |
| 52 | 0.9564 | 1.9127 | 2.8691 | 3.8255 | 4.7819 | 5.7382 | 6.6946 | 7.6510 | 8.6073 | 1.3700 |
| 53 | 0.9563 | 1.9125 | 2.8688 | 3.8250 | 4.7813 | 5.7375 | 6.6938 | 7.6500 | 8.6063 | 1.3699 |
| 54 | 0.9561 | 1.9123 | 2.8684 | 3.8245 | 4.7807 | 5.7368 | 6.6930 | 7.6491 | 8.6052 | 1.3698 |
| 55 | 0.9560 | 1.9120 | 2.8681 | 3.8241 | 4.7801 | 5.7361 | 6.6921 | 7.6482 | 8.6042 | 1.3698 |
| 56 | 0.9559 | 1.9118 | 2.8677 | 3.8236 | 4.7795 | 5.7354 | 6.6913 | 7.6472 | 8.6031 | 1.3697 |
| 57 | 0.9558 | 1.9116 | 2.8674 | 3.8231 | 4.7789 | 5.7347 | 6.6905 | 7.6463 | 8.6021 | 1.3696 |
| 58 | 0.9557 | 1.9113 | 2.8670 | 3.8227 | 4.7783 | 5.7340 | 6.6897 | 7.6453 | 8.6010 | 1.3695 |
| 59 | 0.9556 | 1.9111 | 2.8667 | 3.8222 | 4.7778 | 5.7333 | 6.6889 | 7.6444 | 8.6000 | 1.3694 |
| 60 | 0.9554 | 1.9109 | 2.8663 | 3.8217 | 4.7772 | 5.7326 | 6.6880 | 7.6435 | 8.5989 | 1.3694 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.1870 | 0.3741 | 0.5611 | 0.7482 | 0.9352 | 1.1222 | 1.3093 | 1.4963 | 1.6834 | 0.2671 | 00 |
| 0.1873 | 0.3746 | 0.5619 | 0.7492 | 0.9366 | 1.1239 | 1.3112 | 1.4985 | 1.6858 | 0.2675 | 01 |
| 0.1876 | 0.3752 | 0.5627 | 0.7503 | 0.9379 | 1.1255 | 1.3131 | 1.5006 | 1.6882 | 0.2679 | 02 |
| 0.1878 | 0.3757 | 0.5635 | 0.7514 | 0.9392 | 1.1271 | 1.3149 | 1.5028 | 1.6906 | 0.2683 | 03 |
| 0.1881 | 0.3762 | 0.5644 | 0.7525 | 0.9406 | 1.1287 | 1.3168 | 1.5050 | 1.6931 | 0.2687 | 04 |
| 0.1884 | 0.3768 | 0.5652 | 0.7536 | 0.9420 | 1.1303 | 1.3187 | 1.5071 | 1.6955 | 0.2691 | 05 |
| 0.1887 | 0.3773 | 0.5660 | 0.7546 | 0.9433 | 1.1319 | 1.3206 | 1.5093 | 1.6979 | 0.2695 | 06 |
| 0.1889 | 0.3778 | 0.5668 | 0.7557 | 0.9446 | 1.1335 | 1.3224 | 1.5114 | 1.7003 | 0.2699 | 07 |
| 0.1892 | 0.3784 | 0.5676 | 0.7568 | 0.9460 | 1.1351 | 1.3243 | 1.5135 | 1.7027 | 0.2703 | 08 |
| 0.1895 | 0.3789 | 0.5684 | 0.7578 | 0.9473 | 1.1368 | 1.3262 | 1.5157 | 1.7051 | 0.2707 | 09 |
| 0.1897 | 0.3795 | 0.5692 | 0.7589 | 0.9487 | 1.1384 | 1.3281 | 1.5178 | 1.7076 | 0.2711 | 10 |
| 0.1900 | 0.3800 | 0.5700 | 0.7600 | 0.9500 | 1.1400 | 1.3300 | 1.5200 | 1.7100 | 0.2715 | 11 |
| 0.1903 | 0.3805 | 0.5708 | 0.7611 | 0.9513 | 1.1416 | 1.3319 | 1.5222 | 1.7124 | 0.2719 | 12 |
| 0.1905 | 0.3811 | 0.5716 | 0.7622 | 0.9527 | 1.1432 | 1.3338 | 1.5243 | 1.7149 | 0.2723 | 13 |
| 0.1908 | 0.3816 | 0.5724 | 0.7632 | 0.9540 | 1.1448 | 1.3357 | 1.5265 | 1.7173 | 0.2727 | 14 |
| 0.1911 | 0.3821 | 0.5732 | 0.7643 | 0.9554 | 1.1464 | 1.3375 | 1.5286 | 1.7197 | 0.2731 | 15 |
| 0.1913 | 0.3827 | 0.5740 | 0.7654 | 0.9567 | 1.1480 | 1.3394 | 1.5307 | 1.7221 | 0.2735 | 16 |
| 0.1916 | 0.3832 | 0.5748 | 0.7664 | 0.9580 | 1.1497 | 1.3413 | 1.5329 | 1.7245 | 0.2739 | 17 |
| 0.1919 | 0.3838 | 0.5756 | 0.7675 | 0.9594 | 1.1513 | 1.3432 | 1.5350 | 1.7269 | 0.2743 | 18 |
| 0.1921 | 0.3843 | 0.5764 | 0.7686 | 0.9607 | 1.1529 | 1.3450 | 1.5372 | 1.7293 | 0.2747 | 19 |
| 0.1924 | 0.3848 | 0.5773 | 0.7697 | 0.9621 | 1.1545 | 1.3469 | 1.5394 | 1.7317 | 0.2751 | 20 |
| 0.1927 | 0.3854 | 0.5781 | 0.7707 | 0.9634 | 1.1561 | 1.3488 | 1.5415 | 1.7341 | 0.2755 | 21 |
| 0.1930 | 0.3859 | 0.5789 | 0.7718 | 0.9648 | 1.1577 | 1.3507 | 1.5436 | 1.7366 | 0.2759 | 22 |
| 0.1932 | 0.3864 | 0.5797 | 0.7729 | 0.9661 | 1.1593 | 1.3525 | 1.5458 | 1.7390 | 0.2763 | 23 |
| 0.1935 | 0.3870 | 0.5805 | 0.7740 | 0.9674 | 1.1609 | 1.3544 | 1.5479 | 1.7414 | 0.2767 | 24 |
| 0.1938 | 0.3875 | 0.5813 | 0.7750 | 0.9688 | 1.1625 | 1.3563 | 1.5500 | 1.7438 | 0.2771 | 25 |
| 0.1940 | 0.3880 | 0.5821 | 0.7761 | 0.9701 | 1.1641 | 1.3581 | 1.5522 | 1.7462 | 0.2775 | 26 |
| 0.1943 | 0.3886 | 0.5829 | 0.7772 | 0.9714 | 1.1657 | 1.3600 | 1.5543 | 1.7486 | 0.2779 | 27 |
| 0.1946 | 0.3891 | 0.5837 | 0.7782 | 0.9728 | 1.1674 | 1.3619 | 1.5565 | 1.7510 | 0.2783 | 28 |
| 0.1948 | 0.3896 | 0.5845 | 0.7793 | 0.9741 | 1.1689 | 1.3637 | 1.5586 | 1.7534 | 0.2787 | 29 |
| 0.1951 | 0.3902 | 0.5853 | 0.7804 | 0.9755 | 1.1705 | 1.3656 | 1.5607 | 1.7558 | 0.2791 | 30 |
| 0.1954 | 0.3907 | 0.5861 | 0.7814 | 0.9768 | 1.1722 | 1.3675 | 1.5629 | 1.7582 | 0.2795 | 31 |
| 0.1956 | 0.3913 | 0.5869 | 0.7825 | 0.9781 | 1.1738 | 1.3694 | 1.5650 | 1.7607 | 0.2799 | 32 |
| 0.1959 | 0.3918 | 0.5877 | 0.7836 | 0.9795 | 1.1753 | 1.3712 | 1.5671 | 1.7630 | 0.2803 | 33 |
| 0.1962 | 0.3923 | 0.5885 | 0.7846 | 0.9808 | 1.1770 | 1.3731 | 1.5693 | 1.7654 | 0.2807 | 34 |
| 0.1964 | 0.3929 | 0.5893 | 0.7857 | 0.9821 | 1.1786 | 1.3750 | 1.5714 | 1.7679 | 0.2811 | 35 |
| 0.1967 | 0.3934 | 0.5901 | 0.7868 | 0.9835 | 1.1802 | 1.3769 | 1.5736 | 1.7703 | 0.2815 | 36 |
| 0.1970 | 0.3939 | 0.5909 | 0.7878 | 0.9848 | 1.1818 | 1.3787 | 1.5757 | 1.7727 | 0.2819 | 37 |
| 0.1972 | 0.3945 | 0.5917 | 0.7889 | 0.9861 | 1.1834 | 1.3806 | 1.5778 | 1.7751 | 0.2823 | 38 |
| 0.1975 | 0.3950 | 0.5925 | 0.7900 | 0.9875 | 1.1850 | 1.3825 | 1.5800 | 1.7775 | 0.2827 | 39 |
| 0.1978 | 0.3955 | 0.5933 | 0.7910 | 0.9888 | 1.1866 | 1.3843 | 1.5821 | 1.7798 | 0.2831 | 40 |
| 0.1980 | 0.3961 | 0.5941 | 0.7921 | 0.9901 | 1.1882 | 1.3862 | 1.5842 | 1.7823 | 0.2835 | 41 |
| 0.1983 | 0.3966 | 0.5949 | 0.7932 | 0.9915 | 1.1898 | 1.3881 | 1.5864 | 1.7847 | 0.2839 | 42 |
| 0.1986 | 0.3971 | 0.5957 | 0.7942 | 0.9928 | 1.1914 | 1.3899 | 1.5885 | 1.7871 | 0.2843 | 43 |
| 0.1988 | 0.3977 | 0.5965 | 0.7953 | 0.9941 | 1.1930 | 1.3918 | 1.5906 | 1.7895 | 0.2847 | 44 |
| 0.1991 | 0.3982 | 0.5973 | 0.7964 | 0.9955 | 1.1946 | 1.3937 | 1.5928 | 1.7919 | 0.2851 | 45 |
| 0.1994 | 0.3987 | 0.5981 | 0.7974 | 0.9968 | 1.1962 | 1.3955 | 1.5949 | 1.7942 | 0.2855 | 46 |
| 0.1996 | 0.3993 | 0.5989 | 0.7985 | 0.9981 | 1.1978 | 1.3974 | 1.5970 | 1.7966 | 0.2859 | 47 |
| 0.1999 | 0.3998 | 0.5997 | 0.7996 | 0.9994 | 1.1993 | 1.3992 | 1.5991 | 1.7990 | 0.2863 | 48 |
| 0.2002 | 0.4003 | 0.6005 | 0.8006 | 1.0008 | 1.2010 | 1.4011 | 1.6013 | 1.8014 | 0.2867 | 49 |
| 0.2004 | 0.4009 | 0.6013 | 0.8017 | 1.0021 | 1.2026 | 1.4030 | 1.6034 | 1.8038 | 0.2871 | 50 |
| 0.2007 | 0.4014 | 0.6021 | 0.8028 | 1.0034 | 1.2041 | 1.4048 | 1.6055 | 1.8062 | 0.2875 | 51 |
| 0.2010 | 0.4019 | 0.6029 | 0.8038 | 1.0048 | 1.2057 | 1.4067 | 1.6077 | 1.8086 | 0.2879 | 52 |
| 0.2012 | 0.4024 | 0.6037 | 0.8049 | 1.0061 | 1.2073 | 1.4085 | 1.6098 | 1.8110 | 0.2883 | 53 |
| 0.2015 | 0.4030 | 0.6045 | 0.8060 | 1.0075 | 1.2089 | 1.4104 | 1.6119 | 1.8134 | 0.2887 | 54 |
| 0.2018 | 0.4035 | 0.6053 | 0.8070 | 1.0088 | 1.2105 | 1.4123 | 1.6141 | 1.8158 | 0.2891 | 55 |
| 0.2020 | 0.4040 | 0.6061 | 0.8081 | 1.0101 | 1.2121 | 1.4141 | 1.6162 | 1.8182 | 0.2895 | 56 |
| 0.2023 | 0.4046 | 0.6069 | 0.8092 | 1.0114 | 1.2137 | 1.4160 | 1.6183 | 1.8206 | 0.2899 | 57 |
| 0.2026 | 0.4051 | 0.6077 | 0.8102 | 1.0128 | 1.2153 | 1.4179 | 1.6204 | 1.8230 | 0.2903 | 58 |
| 0.2028 | 0.4056 | 0.6085 | 0.8113 | 1.0141 | 1.2169 | 1.4197 | 1.6226 | 1.8254 | 0.2907 | 59 |
| 0.2031 | 0.4062 | 0.6092 | 0.8123 | 1.0154 | 1.2185 | 1.4216 | 1.6247 | 1.8278 | 0.2911 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9554 | 1.9109 | 2.8663 | 3.8217 | 4.7772 | 5.7326 | 6.6880 | 7.6435 | 8.5989 | 1.3694 |
| 01 | 0.9553 | 1.9106 | 2.8659 | 3.8213 | 4.7766 | 5.7319 | 6.6872 | 7.6425 | 8.5978 | 1.3693 |
| 02 | 0.9552 | 1.9104 | 2.8656 | 3.8208 | 4.7760 | 5.7312 | 6.6864 | 7.6416 | 8.5968 | 1.3693 |
| 03 | 0.9551 | 1.9102 | 2.8652 | 3.8203 | 4.7754 | 5.7305 | 6.6855 | 7.6406 | 8.5957 | 1.3692 |
| 04 | 0.9550 | 1.9099 | 2.8649 | 3.8198 | 4.7748 | 5.7297 | 6.6847 | 7.6397 | 8.5946 | 1.3691 |
| 05 | 0.9548 | 1.9097 | 2.8645 | 3.8194 | 4.7742 | 5.7290 | 6.6839 | 7.6387 | 8.5936 | 1.3690 |
| 06 | 0.9547 | 1.9094 | 2.8642 | 3.8189 | 4.7736 | 5.7283 | 6.6830 | 7.6378 | 8.5925 | 1.3689 |
| 07 | 0.9546 | 1.9092 | 2.8638 | 3.8184 | 4.7730 | 5.7276 | 6.6822 | 7.6368 | 8.5914 | 1.3688 |
| 08 | 0.9545 | 1.9090 | 2.8634 | 3.8179 | 4.7724 | 5.7269 | 6.6814 | 7.6359 | 8.5903 | 1.3687 |
| 09 | 0.9544 | 1.9087 | 2.8631 | 3.8175 | 4.7718 | 5.7262 | 6.6805 | 7.6349 | 8.5893 | 1.3687 |
| 10 | 0.9542 | 1.9085 | 2.8627 | 3.8170 | 4.7712 | 5.7255 | 6.6797 | 7.6340 | 8.5882 | 1.3686 |
| 11 | 0.9541 | 1.9082 | 2.8624 | 3.8165 | 4.7706 | 5.7247 | 6.6789 | 7.6330 | 8.5871 | 1.3685 |
| 12 | 0.9540 | 1.9080 | 2.8620 | 3.8160 | 4.7700 | 5.7240 | 6.6780 | 7.6320 | 8.5860 | 1.3684 |
| 13 | 0.9539 | 1.9078 | 2.8616 | 3.8155 | 4.7694 | 5.7233 | 6.6772 | 7.6311 | 8.5849 | 1.3683 |
| 14 | 0.9538 | 1.9075 | 2.8613 | 3.8150 | 4.7688 | 5.7226 | 6.6763 | 7.6301 | 8.5839 | 1.3682 |
| 15 | 0.9536 | 1.9073 | 2.8609 | 3.8146 | 4.7682 | 5.7219 | 6.6755 | 7.6291 | 8.5828 | 1.3681 |
| 16 | 0.9535 | 1.9070 | 2.8606 | 3.8141 | 4.7676 | 5.7211 | 6.6747 | 7.6282 | 8.5817 | 1.3681 |
| 17 | 0.9534 | 1.9068 | 2.8602 | 3.8136 | 4.7670 | 5.7204 | 6.6738 | 7.6272 | 8.5806 | 1.3680 |
| 18 | 0.9533 | 1.9066 | 2.8598 | 3.8131 | 4.7664 | 5.7197 | 6.6730 | 7.6262 | 8.5795 | 1.3679 |
| 19 | 0.9532 | 1.9063 | 2.8595 | 3.8126 | 4.7658 | 5.7190 | 6.6721 | 7.6253 | 8.5784 | 1.3678 |
| 20 | 0.9530 | 1.9061 | 2.8591 | 3.8122 | 4.7652 | 5.7182 | 6.6713 | 7.6243 | 8.5774 | 1.3677 |
| 21 | 0.9529 | 1.9058 | 2.8588 | 3.8117 | 4.7646 | 5.7175 | 6.6704 | 7.6233 | 8.5763 | 1.3676 |
| 22 | 0.9528 | 1.9056 | 2.8584 | 3.8112 | 4.7640 | 5.7168 | 6.6696 | 7.6224 | 8.5752 | 1.3675 |
| 23 | 0.9527 | 1.9053 | 2.8580 | 3.8107 | 4.7634 | 5.7160 | 6.6687 | 7.6214 | 8.5741 | 1.3674 |
| 24 | 0.9526 | 1.9051 | 2.8577 | 3.8102 | 4.7628 | 5.7153 | 6.6679 | 7.6204 | 8.5730 | 1.3673 |
| 25 | 0.9524 | 1.9049 | 2.8573 | 3.8097 | 4.7622 | 5.7146 | 6.6670 | 7.6194 | 8.5719 | 1.3672 |
| 26 | 0.9523 | 1.9046 | 2.8569 | 3.8092 | 4.7615 | 5.7138 | 6.6662 | 7.6185 | 8.5708 | 1.3672 |
| 27 | 0.9522 | 1.9044 | 2.8566 | 3.8087 | 4.7609 | 5.7131 | 6.6653 | 7.6175 | 8.5697 | 1.3671 |
| 28 | 0.9521 | 1.9041 | 2.8562 | 3.8083 | 4.7603 | 5.7124 | 6.6644 | 7.6165 | 8.5686 | 1.3670 |
| 29 | 0.9519 | 1.9039 | 2.8558 | 3.8078 | 4.7597 | 5.7117 | 6.6636 | 7.6155 | 8.5675 | 1.3669 |
| 30 | 0.9518 | 1.9036 | 2.8555 | 3.8073 | 4.7591 | 5.7109 | 6.6627 | 7.6146 | 8.5664 | 1.3668 |
| 31 | 0.9517 | 1.9034 | 2.8551 | 3.8068 | 4.7585 | 5.7102 | 6.6619 | 7.6136 | 8.5653 | 1.3667 |
| 32 | 0.9516 | 1.9031 | 2.8547 | 3.8063 | 4.7579 | 5.7094 | 6.6610 | 7.6126 | 8.5642 | 1.3667 |
| 33 | 0.9514 | 1.9029 | 2.8543 | 3.8058 | 4.7572 | 5.7087 | 6.6601 | 7.6116 | 8.5630 | 1.3666 |
| 34 | 0.9513 | 1.9027 | 2.8540 | 3.8053 | 4.7566 | 5.7080 | 6.6593 | 7.6106 | 8.5619 | 1.3665 |
| 35 | 0.9512 | 1.9024 | 2.8536 | 3.8048 | 4.7560 | 5.7072 | 6.6584 | 7.6096 | 8.5608 | 1.3664 |
| 36 | 0.9511 | 1.9022 | 2.8532 | 3.8043 | 4.7554 | 5.7065 | 6.6575 | 7.6086 | 8.5597 | 1.3663 |
| 37 | 0.9510 | 1.9019 | 2.8529 | 3.8038 | 4.7548 | 5.7057 | 6.6567 | 7.6076 | 8.5586 | 1.3662 |
| 38 | 0.9508 | 1.9017 | 2.8525 | 3.8033 | 4.7542 | 5.7050 | 6.6558 | 7.6066 | 8.5575 | 1.3661 |
| 39 | 0.9507 | 1.9014 | 2.8521 | 3.8028 | 4.7535 | 5.7042 | 6.6550 | 7.6057 | 8.5564 | 1.3660 |
| 40 | 0.9506 | 1.9012 | 2.8518 | 3.8023 | 4.7529 | 5.7035 | 6.6541 | 7.6047 | 8.5553 | 1.3660 |
| 41 | 0.9505 | 1.9009 | 2.8514 | 3.8018 | 4.7523 | 5.7028 | 6.6532 | 7.6037 | 8.5541 | 1.3659 |
| 42 | 0.9503 | 1.9007 | 2.8510 | 3.8013 | 4.7517 | 5.7020 | 6.6523 | 7.6027 | 8.5530 | 1.3658 |
| 43 | 0.9502 | 1.9004 | 2.8506 | 3.8008 | 4.7510 | 5.7013 | 6.6515 | 7.6017 | 8.5519 | 1.3657 |
| 44 | 0.9501 | 1.9002 | 2.8503 | 3.8003 | 4.7504 | 5.7005 | 6.6506 | 7.6007 | 8.5508 | 1.3656 |
| 45 | 0.9500 | 1.8999 | 2.8499 | 3.7998 | 4.7498 | 5.6998 | 6.6497 | 7.5997 | 8.5496 | 1.3655 |
| 46 | 0.9498 | 1.8997 | 2.8495 | 3.7993 | 4.7492 | 5.6990 | 6.6488 | 7.5987 | 8.5485 | 1.3654 |
| 47 | 0.9497 | 1.8994 | 2.8491 | 3.7988 | 4.7485 | 5.6983 | 6.6480 | 7.5977 | 8.5474 | 1.3653 |
| 48 | 0.9496 | 1.8992 | 2.8488 | 3.7983 | 4.7479 | 5.6975 | 6.6471 | 7.5967 | 8.5463 | 1.3652 |
| 49 | 0.9495 | 1.8989 | 2.8484 | 3.7978 | 4.7473 | 5.6968 | 6.6462 | 7.5957 | 8.5451 | 1.3651 |
| 50 | 0.9493 | 1.8987 | 2.8480 | 3.7973 | 4.7467 | 5.6960 | 6.6453 | 7.5947 | 8.5440 | 1.3651 |
| 51 | 0.9492 | 1.8984 | 2.8476 | 3.7968 | 4.7460 | 5.6952 | 6.6444 | 7.5937 | 8.5429 | 1.3650 |
| 52 | 0.9491 | 1.8982 | 2.8472 | 3.7963 | 4.7454 | 5.6945 | 6.6436 | 7.5926 | 8.5417 | 1.3649 |
| 53 | 0.9490 | 1.8979 | 2.8469 | 3.7958 | 4.7448 | 5.6937 | 6.6427 | 7.5916 | 8.5406 | 1.3648 |
| 54 | 0.9488 | 1.8977 | 2.8465 | 3.7953 | 4.7441 | 5.6930 | 6.6418 | 7.5906 | 8.5395 | 1.3647 |
| 55 | 0.9487 | 1.8974 | 2.8461 | 3.7948 | 4.7435 | 5.6922 | 6.6409 | 7.5896 | 8.5383 | 1.3646 |
| 56 | 0.9486 | 1.8971 | 2.8457 | 3.7943 | 4.7429 | 5.6914 | 6.6400 | 7.5886 | 8.5372 | 1.3645 |
| 57 | 0.9484 | 1.8969 | 2.8453 | 3.7938 | 4.7422 | 5.6907 | 6.6391 | 7.5876 | 8.5360 | 1.3644 |
| 58 | 0.9483 | 1.8966 | 2.8450 | 3.7933 | 4.7416 | 5.6899 | 6.6382 | 7.5866 | 8.5349 | 1.3643 |
| 59 | 0.9482 | 1.8964 | 2.8446 | 3.7928 | 4.7410 | 5.6892 | 6.6374 | 7.5856 | 8.5338 | 1.3642 |
| 60 | 0.9481 | 1.8961 | 2.8442 | 3.7923 | 4.7403 | 5.6884 | 6.6365 | 7.5845 | 8.5326 | 1.3641 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.2031 | 0.4062 | 0.6092 | 0.8123 | 1.0154 | 1.2185 | 1.4216 | 1.6247 | 1.8278 | 0.2011 | 00 |
| 0.2033 | 0.4067 | 0.6100 | 0.8134 | 1.0167 | 1.2201 | 1.4234 | 1.6268 | 1.8302 | 0.2015 | 01 |
| 0.2036 | 0.4072 | 0.6108 | 0.8144 | 1.0181 | 1.2217 | 1.4253 | 1.6289 | 1.8325 | 0.2019 | 02 |
| 0.2039 | 0.4078 | 0.6116 | 0.8155 | 1.0194 | 1.2233 | 1.4272 | 1.6310 | 1.8349 | 0.2023 | 03 |
| 0.2041 | 0.4083 | 0.6124 | 0.8166 | 1.0207 | 1.2248 | 1.4290 | 1.6331 | 1.8373 | 0.2027 | 04 |
| 0.2044 | 0.4088 | 0.6132 | 0.8176 | 1.0221 | 1.2264 | 1.4309 | 1.6353 | 1.8397 | 0.2031 | 05 |
| 0.2047 | 0.4093 | 0.6140 | 0.8187 | 1.0234 | 1.2280 | 1.4327 | 1.6374 | 1.8420 | 0.2035 | 06 |
| 0.2049 | 0.4099 | 0.6148 | 0.8198 | 1.0247 | 1.2296 | 1.4346 | 1.6395 | 1.8444 | 0.2039 | 07 |
| 0.2052 | 0.4104 | 0.6156 | 0.8208 | 1.0260 | 1.2312 | 1.4364 | 1.6416 | 1.8468 | 0.2043 | 08 |
| 0.2055 | 0.4109 | 0.6164 | 0.8219 | 1.0273 | 1.2328 | 1.4383 | 1.6438 | 1.8492 | 0.2047 | 09 |
| 0.2057 | 0.4115 | 0.6172 | 0.8229 | 1.0287 | 1.2344 | 1.4401 | 1.6459 | 1.8516 | 0.2051 | 10 |
| 0.2060 | 0.4120 | 0.6180 | 0.8240 | 1.0300 | 1.2360 | 1.4420 | 1.6480 | 1.8540 | 0.2055 | 11 |
| 0.2063 | 0.4125 | 0.6188 | 0.8250 | 1.0313 | 1.2376 | 1.4438 | 1.6501 | 1.8564 | 0.2059 | 12 |
| 0.2065 | 0.4131 | 0.6196 | 0.8261 | 1.0326 | 1.2392 | 1.4457 | 1.6522 | 1.8588 | 0.2062 | 13 |
| 0.2068 | 0.4136 | 0.6204 | 0.8272 | 1.0340 | 1.2408 | 1.4475 | 1.6543 | 1.8611 | 0.2066 | 14 |
| 0.2071 | 0.4141 | 0.6212 | 0.8282 | 1.0353 | 1.2424 | 1.4494 | 1.6565 | 1.8635 | 0.2070 | 15 |
| 0.2073 | 0.4146 | 0.6220 | 0.8293 | 1.0366 | 1.2439 | 1.4512 | 1.6586 | 1.8659 | 0.2074 | 16 |
| 0.2076 | 0.4152 | 0.6227 | 0.8303 | 1.0379 | 1.2455 | 1.4531 | 1.6607 | 1.8682 | 0.2078 | 17 |
| 0.2078 | 0.4157 | 0.6235 | 0.8314 | 1.0392 | 1.2471 | 1.4549 | 1.6628 | 1.8706 | 0.2082 | 18 |
| 0.2081 | 0.4162 | 0.6243 | 0.8324 | 1.0406 | 1.2487 | 1.4568 | 1.6649 | 1.8730 | 0.2086 | 19 |
| 0.2084 | 0.4168 | 0.6251 | 0.8335 | 1.0419 | 1.2503 | 1.4587 | 1.6670 | 1.8754 | 0.2090 | 20 |
| 0.2086 | 0.4173 | 0.6259 | 0.8346 | 1.0432 | 1.2518 | 1.4605 | 1.6691 | 1.8778 | 0.2094 | 21 |
| 0.2089 | 0.4178 | 0.6267 | 0.8356 | 1.0445 | 1.2534 | 1.4623 | 1.6712 | 1.8801 | 0.2098 | 22 |
| 0.2092 | 0.4183 | 0.6275 | 0.8367 | 1.0458 | 1.2550 | 1.4642 | 1.6734 | 1.8825 | 0.3002 | 23 |
| 0.2094 | 0.4189 | 0.6283 | 0.8377 | 1.0472 | 1.2566 | 1.4660 | 1.6755 | 1.8849 | 0.3006 | 24 |
| 0.2097 | 0.4194 | 0.6291 | 0.8388 | 1.0485 | 1.2582 | 1.4679 | 1.6776 | 1.8873 | 0.3010 | 25 |
| 0.2100 | 0.4199 | 0.6299 | 0.8398 | 1.0498 | 1.2598 | 1.4697 | 1.6797 | 1.8896 | 0.3014 | 26 |
| 0.2102 | 0.4204 | 0.6307 | 0.8409 | 1.0511 | 1.2613 | 1.4715 | 1.6818 | 1.8920 | 0.3018 | 27 |
| 0.2105 | 0.4210 | 0.6315 | 0.8420 | 1.0524 | 1.2629 | 1.4734 | 1.6839 | 1.8944 | 0.3022 | 28 |
| 0.2107 | 0.4215 | 0.6322 | 0.8430 | 1.0537 | 1.2645 | 1.4752 | 1.6860 | 1.8967 | 0.3026 | 29 |
| 0.2110 | 0.4220 | 0.6330 | 0.8440 | 1.0551 | 1.2661 | 1.4771 | 1.6881 | 1.8991 | 0.3030 | 30 |
| 0.2113 | 0.4226 | 0.6338 | 0.8451 | 1.0564 | 1.2677 | 1.4790 | 1.6902 | 1.9015 | 0.3034 | 31 |
| 0.2115 | 0.4231 | 0.6346 | 0.8462 | 1.0577 | 1.2692 | 1.4808 | 1.6923 | 1.9039 | 0.3038 | 32 |
| 0.2118 | 0.4236 | 0.6354 | 0.8472 | 1.0590 | 1.2708 | 1.4826 | 1.6944 | 1.9062 | 0.3042 | 33 |
| 0.2121 | 0.4241 | 0.6362 | 0.8483 | 1.0603 | 1.2724 | 1.4845 | 1.6965 | 1.9086 | 0.3046 | 34 |
| 0.2123 | 0.4247 | 0.6370 | 0.8493 | 1.0616 | 1.2740 | 1.4863 | 1.6986 | 1.9110 | 0.3050 | 35 |
| 0.2126 | 0.4252 | 0.6378 | 0.8504 | 1.0630 | 1.2755 | 1.4881 | 1.7007 | 1.9133 | 0.3054 | 36 |
| 0.2129 | 0.4257 | 0.6386 | 0.8514 | 1.0643 | 1.2771 | 1.4900 | 1.7028 | 1.9157 | 0.3058 | 37 |
| 0.2131 | 0.4262 | 0.6394 | 0.8525 | 1.0656 | 1.2787 | 1.4918 | 1.7049 | 1.9181 | 0.3062 | 38 |
| 0.2134 | 0.4268 | 0.6401 | 0.8535 | 1.0669 | 1.2803 | 1.4937 | 1.7070 | 1.9204 | 0.3066 | 39 |
| 0.2136 | 0.4273 | 0.6409 | 0.8546 | 1.0682 | 1.2818 | 1.4955 | 1.7091 | 1.9228 | 0.3070 | 40 |
| 0.2139 | 0.4278 | 0.6417 | 0.8556 | 1.0695 | 1.2834 | 1.4973 | 1.7112 | 1.9251 | 0.3074 | 41 |
| 0.2142 | 0.4283 | 0.6425 | 0.8567 | 1.0708 | 1.2850 | 1.4992 | 1.7133 | 1.9275 | 0.3078 | 42 |
| 0.2144 | 0.4289 | 0.6433 | 0.8577 | 1.0721 | 1.2866 | 1.5010 | 1.7154 | 1.9299 | 0.3082 | 43 |
| 0.2147 | 0.4294 | 0.6441 | 0.8588 | 1.0735 | 1.2881 | 1.5028 | 1.7175 | 1.9322 | 0.3086 | 44 |
| 0.2150 | 0.4299 | 0.6449 | 0.8598 | 1.0748 | 1.2897 | 1.5047 | 1.7196 | 1.9346 | 0.3090 | 45 |
| 0.2152 | 0.4304 | 0.6457 | 0.8609 | 1.0761 | 1.2913 | 1.5065 | 1.7217 | 1.9370 | 0.3094 | 46 |
| 0.2155 | 0.4310 | 0.6464 | 0.8619 | 1.0774 | 1.2929 | 1.5084 | 1.7238 | 1.9393 | 0.3098 | 47 |
| 0.2157 | 0.4315 | 0.6472 | 0.8629 | 1.0787 | 1.2944 | 1.5102 | 1.7259 | 1.9417 | 0.3102 | 48 |
| 0.2160 | 0.4320 | 0.6480 | 0.8640 | 1.0800 | 1.2960 | 1.5120 | 1.7280 | 1.9440 | 0.3106 | 49 |
| 0.2163 | 0.4325 | 0.6488 | 0.8651 | 1.0813 | 1.2976 | 1.5138 | 1.7301 | 1.9464 | 0.3110 | 50 |
| 0.2165 | 0.4331 | 0.6496 | 0.8661 | 1.0826 | 1.2992 | 1.5157 | 1.7322 | 1.9487 | 0.3114 | 51 |
| 0.2168 | 0.4336 | 0.6504 | 0.8671 | 1.0839 | 1.3007 | 1.5175 | 1.7343 | 1.9511 | 0.3118 | 52 |
| 0.2170 | 0.4341 | 0.6511 | 0.8682 | 1.0852 | 1.3023 | 1.5193 | 1.7364 | 1.9534 | 0.3121 | 53 |
| 0.2173 | 0.4346 | 0.6519 | 0.8692 | 1.0866 | 1.3039 | 1.5212 | 1.7385 | 1.9558 | 0.3125 | 54 |
| 0.2176 | 0.4351 | 0.6527 | 0.8703 | 1.0879 | 1.3054 | 1.5230 | 1.7406 | 1.9581 | 0.3129 | 55 |
| 0.2178 | 0.4357 | 0.6535 | 0.8713 | 1.0892 | 1.3070 | 1.5248 | 1.7427 | 1.9605 | 0.3133 | 56 |
| 0.2181 | 0.4362 | 0.6543 | 0.8724 | 1.0905 | 1.3186 | 1.5267 | 1.7448 | 1.9629 | 0.3137 | 57 |
| 0.2184 | 0.4367 | 0.6551 | 0.8734 | 1.0918 | 1.3101 | 1.5285 | 1.7468 | 1.9652 | 0.3141 | 58 |
| 0.2186 | 0.4372 | 0.6559 | 0.8745 | 1.0931 | 1.3117 | 1.5303 | 1.7489 | 1.9676 | 0.3145 | 59 |
| 0.2189 | 0.4378 | 0.6566 | 0.8755 | 1.0944 | 1.3133 | 1.5322 | 1.7510 | 1.9699 | 0.3149 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9481 | 1.8961 | 2.8442 | 3.7923 | 4.7403 | 5.6884 | 6.6365 | 7.5845 | 8.5320 | 1.3641 |
| 01 | 0.9479 | 1.8959 | 2.8438 | 3.7918 | 4.7397 | 5.6876 | 6.6356 | 7.5835 | 8.5315 | 1.3640 |
| 02 | 0.9478 | 1.8956 | 2.8434 | 3.7912 | 4.7391 | 5.6869 | 6.6347 | 7.5825 | 8.5303 | 1.3639 |
| 03 | 0.9477 | 1.8954 | 2.8431 | 3.7907 | 4.7384 | 5.6861 | 6.6338 | 7.5815 | 8.5292 | 1.3638 |
| 04 | 0.9476 | 1.8951 | 2.8427 | 3.7902 | 4.7378 | 5.6853 | 6.6329 | 7.5804 | 8.5280 | 1.3637 |
| 05 | 0.9474 | 1.8949 | 2.8423 | 3.7897 | 4.7371 | 5.6846 | 6.6320 | 7.5794 | 8.5269 | 1.3636 |
| 06 | 0.9473 | 1.8946 | 2.8419 | 3.7892 | 4.7365 | 5.6838 | 6.6311 | 7.5784 | 8.5257 | 1.3635 |
| 07 | 0.9472 | 1.8943 | 2.8415 | 3.7887 | 4.7359 | 5.6830 | 6.6302 | 7.5774 | 8.5245 | 1.3634 |
| 08 | 0.9470 | 1.8941 | 2.8411 | 3.7882 | 4.7352 | 5.6823 | 6.6293 | 7.5763 | 8.5234 | 1.3634 |
| 09 | 0.9469 | 1.8938 | 2.8407 | 3.7877 | 4.7346 | 5.6815 | 6.6284 | 7.5753 | 8.5222 | 1.3633 |
| 10 | 0.9468 | 1.8936 | 2.8404 | 3.7871 | 4.7339 | 5.6807 | 6.6275 | 7.5743 | 8.5211 | 1.3632 |
| 11 | 0.9467 | 1.8933 | 2.8400 | 3.7866 | 4.7333 | 5.6799 | 6.6266 | 7.5733 | 8.5199 | 1.3631 |
| 12 | 0.9465 | 1.8931 | 2.8396 | 3.7861 | 4.7326 | 5.6792 | 6.6257 | 7.5722 | 8.5188 | 1.3630 |
| 13 | 0.9464 | 1.8928 | 2.8392 | 3.7856 | 4.7320 | 5.6784 | 6.6248 | 7.5712 | 8.5176 | 1.3629 |
| 14 | 0.9463 | 1.8925 | 2.8388 | 3.7851 | 4.7313 | 5.6776 | 6.6239 | 7.5702 | 8.5164 | 1.3628 |
| 15 | 0.9461 | 1.8923 | 2.8384 | 3.7846 | 4.7307 | 5.6768 | 6.6230 | 7.5691 | 8.5153 | 1.3627 |
| 16 | 0.9460 | 1.8920 | 2.8380 | 3.7840 | 4.7300 | 5.6761 | 6.6221 | 7.5681 | 8.5141 | 1.3626 |
| 17 | 0.9459 | 1.8918 | 2.8376 | 3.7835 | 4.7294 | 5.6753 | 6.6212 | 7.5670 | 8.5129 | 1.3625 |
| 18 | 0.9458 | 1.8915 | 2.8373 | 3.7830 | 4.7288 | 5.6745 | 6.6203 | 7.5660 | 8.5118 | 1.3624 |
| 19 | 0.9456 | 1.8912 | 2.8369 | 3.7825 | 4.7281 | 5.6737 | 6.6193 | 7.5650 | 8.5106 | 1.3623 |
| 20 | 0.9455 | 1.8910 | 2.8365 | 3.7820 | 4.7275 | 5.6729 | 6.6184 | 7.5639 | 8.5094 | 1.3622 |
| 21 | 0.9454 | 1.8907 | 2.8361 | 3.7814 | 4.7268 | 5.6722 | 6.6175 | 7.5629 | 8.5082 | 1.3621 |
| 22 | 0.9452 | 1.8905 | 2.8357 | 3.7809 | 4.7261 | 5.6714 | 6.6166 | 7.5618 | 8.5071 | 1.3620 |
| 23 | 0.9451 | 1.8902 | 2.8353 | 3.7804 | 4.7255 | 5.6706 | 6.6157 | 7.5608 | 8.5059 | 1.3619 |
| 24 | 0.9450 | 1.8899 | 2.8349 | 3.7799 | 4.7248 | 5.6698 | 6.6148 | 7.5597 | 8.5047 | 1.3618 |
| 25 | 0.9448 | 1.8897 | 2.8345 | 3.7793 | 4.7242 | 5.6690 | 6.6139 | 7.5587 | 8.5035 | 1.3618 |
| 26 | 0.9447 | 1.8894 | 2.8341 | 3.7788 | 4.7235 | 5.6682 | 6.6129 | 7.5576 | 8.5023 | 1.3617 |
| 27 | 0.9446 | 1.8891 | 2.8337 | 3.7783 | 4.7229 | 5.6674 | 6.6120 | 7.5566 | 8.5012 | 1.3616 |
| 28 | 0.9444 | 1.8889 | 2.8333 | 3.7778 | 4.7222 | 5.6667 | 6.6111 | 7.5555 | 8.5000 | 1.3615 |
| 29 | 0.9443 | 1.8886 | 2.8329 | 3.7772 | 4.7216 | 5.6659 | 6.6102 | 7.5545 | 8.4988 | 1.3614 |
| 30 | 0.9442 | 1.8884 | 2.8325 | 3.7767 | 4.7209 | 5.6651 | 6.6093 | 7.5534 | 8.4976 | 1.3613 |
| 31 | 0.9440 | 1.8881 | 2.8321 | 3.7762 | 4.7202 | 5.6643 | 6.6083 | 7.5524 | 8.4964 | 1.3612 |
| 32 | 0.9439 | 1.8878 | 2.8317 | 3.7757 | 4.7196 | 5.6635 | 6.6074 | 7.5513 | 8.4952 | 1.3611 |
| 33 | 0.9438 | 1.8876 | 2.8313 | 3.7751 | 4.7189 | 5.6627 | 6.6065 | 7.5503 | 8.4940 | 1.3610 |
| 34 | 0.9436 | 1.8873 | 2.8309 | 3.7746 | 4.7182 | 5.6619 | 6.6055 | 7.5492 | 8.4928 | 1.3609 |
| 35 | 0.9435 | 1.8870 | 2.8306 | 3.7741 | 4.7176 | 5.6611 | 6.6046 | 7.5481 | 8.4917 | 1.3608 |
| 36 | 0.9434 | 1.8868 | 2.8302 | 3.7735 | 4.7169 | 5.6603 | 6.6037 | 7.5471 | 8.4905 | 1.3607 |
| 37 | 0.9433 | 1.8865 | 2.8298 | 3.7730 | 4.7163 | 5.6595 | 6.6028 | 7.5460 | 8.4893 | 1.3606 |
| 38 | 0.9431 | 1.8862 | 2.8294 | 3.7725 | 4.7156 | 5.6587 | 6.6018 | 7.5449 | 8.4881 | 1.3605 |
| 39 | 0.9430 | 1.8860 | 2.8290 | 3.7719 | 4.7149 | 5.6579 | 6.6009 | 7.5439 | 8.4869 | 1.3604 |
| 40 | 0.9429 | 1.8857 | 2.8286 | 3.7714 | 4.7143 | 5.6571 | 6.6000 | 7.5428 | 8.4857 | 1.3603 |
| 41 | 0.9427 | 1.8854 | 2.8282 | 3.7709 | 4.7136 | 5.6563 | 6.5990 | 7.5418 | 8.4845 | 1.3602 |
| 42 | 0.9426 | 1.8852 | 2.8278 | 3.7703 | 4.7129 | 5.6555 | 6.5981 | 7.5407 | 8.4833 | 1.3602 |
| 43 | 0.9425 | 1.8849 | 2.8274 | 3.7698 | 4.7123 | 5.6547 | 6.5972 | 7.5396 | 8.4821 | 1.3601 |
| 44 | 0.9423 | 1.8846 | 2.8270 | 3.7693 | 4.7116 | 5.6539 | 6.5962 | 7.5385 | 8.4809 | 1.3600 |
| 45 | 0.9422 | 1.8844 | 2.8265 | 3.7687 | 4.7109 | 5.6531 | 6.5953 | 7.5375 | 8.4796 | 1.3599 |
| 46 | 0.9420 | 1.8841 | 2.8261 | 3.7682 | 4.7102 | 5.6523 | 6.5943 | 7.5364 | 8.4784 | 1.3598 |
| 47 | 0.9419 | 1.8838 | 2.8257 | 3.7677 | 4.7096 | 5.6515 | 6.5934 | 7.5353 | 8.4772 | 1.3597 |
| 48 | 0.9418 | 1.8836 | 2.8253 | 3.7671 | 4.7089 | 5.6507 | 6.5925 | 7.5342 | 8.4760 | 1.3596 |
| 49 | 0.9416 | 1.8833 | 2.8249 | 3.7666 | 4.7082 | 5.6499 | 6.5915 | 7.5332 | 8.4748 | 1.3595 |
| 50 | 0.9415 | 1.8830 | 2.8245 | 3.7660 | 4.7076 | 5.6491 | 6.5906 | 7.5321 | 8.4736 | 1.3594 |
| 51 | 0.9414 | 1.8828 | 2.8241 | 3.7655 | 4.7069 | 5.6483 | 6.5896 | 7.5310 | 8.4724 | 1.3593 |
| 52 | 0.9412 | 1.8825 | 2.8237 | 3.7650 | 4.7062 | 5.6474 | 6.5887 | 7.5299 | 8.4712 | 1.3592 |
| 53 | 0.9411 | 1.8822 | 2.8233 | 3.7644 | 4.7055 | 5.6466 | 6.5877 | 7.5288 | 8.4699 | 1.3591 |
| 54 | 0.9410 | 1.8819 | 2.8229 | 3.7639 | 4.7048 | 5.6458 | 6.5868 | 7.5278 | 8.4687 | 1.3590 |
| 55 | 0.9408 | 1.8817 | 2.8225 | 3.7633 | 4.7042 | 5.6450 | 6.5858 | 7.5267 | 8.4675 | 1.3589 |
| 56 | 0.9407 | 1.8814 | 2.8221 | 3.7628 | 4.7035 | 5.6442 | 6.5849 | 7.5256 | 8.4663 | 1.3588 |
| 57 | 0.9406 | 1.8811 | 2.8217 | 3.7623 | 4.7028 | 5.6434 | 6.5839 | 7.5245 | 8.4651 | 1.3587 |
| 58 | 0.9404 | 1.8809 | 2.8213 | 3.7617 | 4.7021 | 5.6426 | 6.5830 | 7.5234 | 8.4638 | 1.3586 |
| 59 | 0.9403 | 1.8806 | 2.8209 | 3.7612 | 4.7015 | 5.6418 | 6.5820 | 7.5223 | 8.4626 | 1.3585 |
| 60 | 0.9402 | 1.8803 | 2.8205 | 3.7606 | 4.7008 | 5.6409 | 6.5811 | 7.5212 | 8.4614 | 1.3584 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.2189 | 0.4378 | 0.6566 | 0.8755 | 1.0944 | 1.3133 | 1.5322 | 1.7510 | 1.9699 | 0.3149 | 00 |
| 0.2191 | 0.4383 | 0.6574 | 0.8766 | 1.0957 | 1.3148 | 1.5340 | 1.7531 | 1.9723 | 0.3153 | 01 |
| 0.2194 | 0.4388 | 0.6582 | 0.8776 | 1.0970 | 1.3164 | 1.5358 | 1.7552 | 1.9746 | 0.3157 | 02 |
| 0.2197 | 0.4393 | 0.6590 | 0.8786 | 1.0983 | 1.3180 | 1.5376 | 1.7573 | 1.9769 | 0.3161 | 03 |
| 0.2199 | 0.4398 | 0.6598 | 0.8797 | 1.0996 | 1.3195 | 1.5394 | 1.7594 | 1.9793 | 0.3165 | 04 |
| 0.2202 | 0.4404 | 0.6605 | 0.8807 | 1.1009 | 1.3211 | 1.5413 | 1.7614 | 1.9816 | 0.3169 | 05 |
| 0.2204 | 0.4409 | 0.6613 | 0.8818 | 1.1022 | 1.3226 | 1.5431 | 1.7635 | 1.9840 | 0.3173 | 06 |
| 0.2207 | 0.4414 | 0.6621 | 0.8828 | 1.1035 | 1.3242 | 1.5449 | 1.7656 | 1.9863 | 0.3177 | 07 |
| 0.2210 | 0.4419 | 0.6629 | 0.8838 | 1.1048 | 1.3258 | 1.5467 | 1.7677 | 1.9886 | 0.3181 | 08 |
| 0.2212 | 0.4425 | 0.6637 | 0.8849 | 1.1061 | 1.3274 | 1.5486 | 1.7698 | 1.9911 | 0.3185 | 09 |
| 0.2215 | 0.4430 | 0.6645 | 0.8860 | 1.1074 | 1.3289 | 1.5504 | 1.7719 | 1.9934 | 0.3189 | 10 |
| 0.2217 | 0.4435 | 0.6652 | 0.8870 | 1.1087 | 1.3305 | 1.5522 | 1.7740 | 1.9957 | 0.3193 | 11 |
| 0.2220 | 0.4440 | 0.6660 | 0.8880 | 1.1100 | 1.3321 | 1.5541 | 1.7761 | 1.9981 | 0.3197 | 12 |
| 0.2223 | 0.4445 | 0.6668 | 0.8891 | 1.1113 | 1.3336 | 1.5559 | 1.7782 | 2.0004 | 0.3201 | 13 |
| 0.2225 | 0.4451 | 0.6676 | 0.8901 | 1.1126 | 1.3352 | 1.5577 | 1.7802 | 2.0028 | 0.3205 | 14 |
| 0.2228 | 0.4456 | 0.6684 | 0.8912 | 1.1139 | 1.3367 | 1.5595 | 1.7823 | 2.0051 | 0.3209 | 15 |
| 0.2230 | 0.4461 | 0.6691 | 0.8922 | 1.1152 | 1.3383 | 1.5613 | 1.7844 | 2.0074 | 0.3213 | 16 |
| 0.2233 | 0.4466 | 0.6699 | 0.8932 | 1.1165 | 1.3399 | 1.5632 | 1.7865 | 2.0098 | 0.3217 | 17 |
| 0.2236 | 0.4471 | 0.6707 | 0.8943 | 1.1178 | 1.3414 | 1.5650 | 1.7886 | 2.0121 | 0.3221 | 18 |
| 0.2238 | 0.4477 | 0.6715 | 0.8953 | 1.1191 | 1.3430 | 1.5668 | 1.7906 | 2.0145 | 0.3225 | 19 |
| 0.2241 | 0.4482 | 0.6723 | 0.8964 | 1.1204 | 1.3445 | 1.5686 | 1.7927 | 2.0168 | 0.3229 | 20 |
| 0.2243 | 0.4487 | 0.6730 | 0.8974 | 1.1217 | 1.3460 | 1.5704 | 1.7947 | 2.0191 | 0.3232 | 21 |
| 0.2246 | 0.4492 | 0.6738 | 0.8984 | 1.1230 | 1.3476 | 1.5722 | 1.7968 | 2.0214 | 0.3236 | 22 |
| 0.2249 | 0.4497 | 0.6746 | 0.8994 | 1.1243 | 1.3492 | 1.5740 | 1.7989 | 2.0237 | 0.3240 | 23 |
| 0.2251 | 0.4502 | 0.6754 | 0.9005 | 1.1256 | 1.3507 | 1.5758 | 1.8010 | 2.0261 | 0.3244 | 24 |
| 0.2254 | 0.4508 | 0.6761 | 0.9015 | 1.1269 | 1.3523 | 1.5777 | 1.8030 | 2.0284 | 0.3248 | 25 |
| 0.2256 | 0.4513 | 0.6769 | 0.9026 | 1.1282 | 1.3538 | 1.5795 | 1.8051 | 2.0308 | 0.3252 | 26 |
| 0.2259 | 0.4518 | 0.6777 | 0.9036 | 1.1295 | 1.3554 | 1.5813 | 1.8072 | 2.0331 | 0.3256 | 27 |
| 0.2262 | 0.4523 | 0.6785 | 0.9046 | 1.1308 | 1.3570 | 1.5831 | 1.8093 | 2.0354 | 0.3260 | 28 |
| 0.2264 | 0.4528 | 0.6793 | 0.9057 | 1.1321 | 1.3585 | 1.5849 | 1.8114 | 2.0378 | 0.3264 | 29 |
| 0.2267 | 0.4534 | 0.6800 | 0.9067 | 1.1334 | 1.3601 | 1.5868 | 1.8134 | 2.0401 | 0.3268 | 30 |
| 0.2269 | 0.4539 | 0.6808 | 0.9078 | 1.1347 | 1.3616 | 1.5886 | 1.8155 | 2.0424 | 0.3272 | 31 |
| 0.2272 | 0.4544 | 0.6816 | 0.9088 | 1.1360 | 1.3631 | 1.5904 | 1.8175 | 2.0447 | 0.3276 | 32 |
| 0.2275 | 0.4549 | 0.6824 | 0.9098 | 1.1373 | 1.3647 | 1.5922 | 1.8196 | 2.0471 | 0.3280 | 33 |
| 0.2277 | 0.4554 | 0.6831 | 0.9108 | 1.1385 | 1.3663 | 1.5940 | 1.8217 | 2.0494 | 0.3284 | 34 |
| 0.2280 | 0.4559 | 0.6839 | 0.9119 | 1.1398 | 1.3678 | 1.5958 | 1.8238 | 2.0517 | 0.3288 | 35 |
| 0.2282 | 0.4565 | 0.6847 | 0.9129 | 1.1411 | 1.3694 | 1.5976 | 1.8258 | 2.0541 | 0.3292 | 36 |
| 0.2285 | 0.4570 | 0.6855 | 0.9140 | 1.1424 | 1.3709 | 1.5994 | 1.8279 | 2.0564 | 0.3296 | 37 |
| 0.2287 | 0.4575 | 0.6862 | 0.9150 | 1.1437 | 1.3725 | 1.6012 | 1.8300 | 2.0587 | 0.3300 | 38 |
| 0.2290 | 0.4580 | 0.6870 | 0.9160 | 1.1450 | 1.3740 | 1.6030 | 1.8320 | 2.0610 | 0.3304 | 39 |
| 0.2293 | 0.4585 | 0.6878 | 0.9170 | 1.1463 | 1.3756 | 1.6048 | 1.8341 | 2.0633 | 0.3308 | 40 |
| 0.2295 | 0.4590 | 0.6886 | 0.9181 | 1.1476 | 1.3771 | 1.6066 | 1.8361 | 2.0657 | 0.3312 | 41 |
| 0.2298 | 0.4596 | 0.6893 | 0.9191 | 1.1489 | 1.3787 | 1.6085 | 1.8382 | 2.0680 | 0.3316 | 42 |
| 0.2300 | 0.4601 | 0.6901 | 0.9202 | 1.1502 | 1.3802 | 1.6103 | 1.8403 | 2.0703 | 0.3320 | 43 |
| 0.2303 | 0.4606 | 0.6909 | 0.9212 | 1.1515 | 1.3817 | 1.6121 | 1.8423 | 2.0726 | 0.3324 | 44 |
| 0.2306 | 0.4611 | 0.6917 | 0.9222 | 1.1528 | 1.3833 | 1.6139 | 1.8444 | 2.0750 | 0.3328 | 45 |
| 0.2308 | 0.4616 | 0.6924 | 0.9232 | 1.1541 | 1.3849 | 1.6157 | 1.8465 | 2.0773 | 0.3331 | 46 |
| 0.2311 | 0.4621 | 0.6932 | 0.9243 | 1.1554 | 1.3864 | 1.6175 | 1.8486 | 2.0796 | 0.3335 | 47 |
| 0.2313 | 0.4626 | 0.6940 | 0.9253 | 1.1566 | 1.3879 | 1.6193 | 1.8506 | 2.0819 | 0.3339 | 48 |
| 0.2316 | 0.4632 | 0.6947 | 0.9263 | 1.1579 | 1.3895 | 1.6211 | 1.8527 | 2.0842 | 0.3343 | 49 |
| 0.2318 | 0.4637 | 0.6955 | 0.9274 | 1.1592 | 1.3910 | 1.6229 | 1.8547 | 2.0866 | 0.3347 | 50 |
| 0.2321 | 0.4642 | 0.6963 | 0.9284 | 1.1605 | 1.3926 | 1.6247 | 1.8568 | 2.0889 | 0.3351 | 51 |
| 0.2324 | 0.4647 | 0.6971 | 0.9294 | 1.1618 | 1.3941 | 1.6265 | 1.8588 | 2.0912 | 0.3355 | 52 |
| 0.2326 | 0.4652 | 0.6978 | 0.9304 | 1.1630 | 1.3957 | 1.6283 | 1.8609 | 2.0935 | 0.3359 | 53 |
| 0.2329 | 0.4657 | 0.6986 | 0.9315 | 1.1643 | 1.3972 | 1.6301 | 1.8630 | 2.0958 | 0.3363 | 54 |
| 0.2331 | 0.4662 | 0.6994 | 0.9325 | 1.1656 | 1.3987 | 1.6319 | 1.8650 | 2.0981 | 0.3367 | 55 |
| 0.2334 | 0.4668 | 0.7001 | 0.9335 | 1.1669 | 1.4003 | 1.6337 | 1.8670 | 2.1004 | 0.3371 | 56 |
| 0.2336 | 0.4673 | 0.7009 | 0.9346 | 1.1682 | 1.4018 | 1.6355 | 1.8691 | 2.1028 | 0.3375 | 57 |
| 0.2339 | 0.4678 | 0.7017 | 0.9356 | 1.1695 | 1.4033 | 1.6373 | 1.8711 | 2.1050 | 0.3379 | 58 |
| 0.2342 | 0.4683 | 0.7025 | 0.9366 | 1.1708 | 1.4049 | 1.6391 | 1.8732 | 2.1074 | 0.3383 | 59 |
| 0.2344 | 0.4688 | 0.7032 | 0.9376 | 1.1720 | 1.4065 | 1.6409 | 1.8753 | 2.1097 | 0.3387 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9402 | 1.8803 | 2.8205 | 3.7606 | 4.7008 | 5.6409 | 6.5811 | 7.5212 | 8.4614 | 1.3584 |
| 01 | 0.9400 | 1.8800 | 2.8201 | 3.7601 | 4.7001 | 5.6401 | 6.5801 | 7.5202 | 8.4602 | 1.3583 |
| 02 | 0.9399 | 1.8798 | 2.8196 | 3.7595 | 4.6994 | 5.6393 | 6.5792 | 7.5191 | 8.4589 | 1.3582 |
| 03 | 0.9397 | 1.8795 | 2.8192 | 3.7590 | 4.6987 | 5.6385 | 6.5782 | 7.5180 | 8.4577 | 1.3581 |
| 04 | 0.9396 | 1.8792 | 2.8188 | 3.7584 | 4.6980 | 5.6376 | 6.5773 | 7.5169 | 8.4565 | 1.3580 |
| 05 | 0.9395 | 1.8789 | 2.8184 | 3.7579 | 4.6974 | 5.6368 | 6.5763 | 7.5158 | 8.4552 | 1.3579 |
| 06 | 0.9393 | 1.8787 | 2.8180 | 3.7573 | 4.6967 | 5.6360 | 6.5753 | 7.5147 | 8.4540 | 1.3578 |
| 07 | 0.9392 | 1.8784 | 2.8176 | 3.7568 | 4.6960 | 5.6352 | 6.5744 | 7.5136 | 8.4528 | 1.3577 |
| 08 | 0.9391 | 1.8781 | 2.8172 | 3.7562 | 4.6953 | 5.6344 | 6.5734 | 7.5125 | 8.4515 | 1.3576 |
| 09 | 0.9389 | 1.8778 | 2.8168 | 3.7557 | 4.6946 | 5.6335 | 6.5725 | 7.5114 | 8.4503 | 1.3575 |
| 10 | 0.9388 | 1.8776 | 2.8164 | 3.7551 | 4.6939 | 5.6327 | 6.5715 | 7.5103 | 8.4491 | 1.3574 |
| 11 | 0.9386 | 1.8773 | 2.8159 | 3.7546 | 4.6932 | 5.6319 | 6.5705 | 7.5092 | 8.4478 | 1.3573 |
| 12 | 0.9385 | 1.8770 | 2.8155 | 3.7540 | 4.6925 | 5.6310 | 6.5696 | 7.5081 | 8.4466 | 1.3572 |
| 13 | 0.9384 | 1.8767 | 2.8151 | 3.7535 | 4.6918 | 5.6302 | 6.5686 | 7.5070 | 8.4453 | 1.3571 |
| 14 | 0.9382 | 1.8765 | 2.8147 | 3.7529 | 4.6912 | 5.6294 | 6.5676 | 7.5058 | 8.4441 | 1.3570 |
| 15 | 0.9381 | 1.8762 | 2.8143 | 3.7524 | 4.6905 | 5.6286 | 6.5666 | 7.5047 | 8.4428 | 1.3569 |
| 16 | 0.9380 | 1.8759 | 2.8139 | 3.7518 | 4.6898 | 5.6277 | 6.5657 | 7.5036 | 8.4416 | 1.3568 |
| 17 | 0.9378 | 1.8756 | 2.8134 | 3.7513 | 4.6891 | 5.6269 | 6.5647 | 7.5025 | 8.4403 | 1.3567 |
| 18 | 0.9377 | 1.8754 | 2.8130 | 3.7507 | 4.6884 | 5.6261 | 6.5637 | 7.5014 | 8.4391 | 1.3566 |
| 19 | 0.9375 | 1.8751 | 2.8126 | 3.7501 | 4.6877 | 5.6252 | 6.5628 | 7.5003 | 8.4378 | 1.3565 |
| 20 | 0.9374 | 1.8748 | 2.8122 | 3.7496 | 4.6870 | 5.6244 | 6.5618 | 7.4992 | 8.4366 | 1.3564 |
| 21 | 0.9373 | 1.8745 | 2.8118 | 3.7490 | 4.6863 | 5.6235 | 6.5608 | 7.4981 | 8.4353 | 1.3563 |
| 22 | 0.9371 | 1.8742 | 2.8114 | 3.7485 | 4.6856 | 5.6227 | 6.5598 | 7.4969 | 8.4341 | 1.3562 |
| 23 | 0.9370 | 1.8740 | 2.8109 | 3.7479 | 4.6849 | 5.6219 | 6.5588 | 7.4958 | 8.4328 | 1.3561 |
| 24 | 0.9368 | 1.8737 | 2.8105 | 3.7474 | 4.6842 | 5.6210 | 6.5579 | 7.4947 | 8.4315 | 1.3560 |
| 25 | 0.9367 | 1.8734 | 2.8101 | 3.7468 | 4.6835 | 5.6202 | 6.5569 | 7.4936 | 8.4303 | 1.3559 |
| 26 | 0.9366 | 1.8731 | 2.8097 | 3.7462 | 4.6828 | 5.6193 | 6.5559 | 7.4925 | 8.4290 | 1.3558 |
| 27 | 0.9364 | 1.8728 | 2.8093 | 3.7457 | 4.6821 | 5.6185 | 6.5549 | 7.4913 | 8.4278 | 1.3557 |
| 28 | 0.9363 | 1.8726 | 2.8088 | 3.7451 | 4.6814 | 5.6177 | 6.5539 | 7.4902 | 8.4265 | 1.3556 |
| 29 | 0.9361 | 1.8723 | 2.8084 | 3.7445 | 4.6807 | 5.6168 | 6.5530 | 7.4891 | 8.4252 | 1.3555 |
| 30 | 0.9360 | 1.8720 | 2.8080 | 3.7440 | 4.6800 | 5.6160 | 6.5520 | 7.4880 | 8.4240 | 1.3554 |
| 31 | 0.9359 | 1.8717 | 2.8076 | 3.7434 | 4.6793 | 5.6151 | 6.5510 | 7.4868 | 8.4227 | 1.3553 |
| 32 | 0.9357 | 1.8714 | 2.8071 | 3.7429 | 4.6786 | 5.6143 | 6.5500 | 7.4857 | 8.4214 | 1.3552 |
| 33 | 0.9356 | 1.8711 | 2.8067 | 3.7423 | 4.6779 | 5.6134 | 6.5490 | 7.4846 | 8.4202 | 1.3551 |
| 34 | 0.9354 | 1.8709 | 2.8063 | 3.7417 | 4.6772 | 5.6126 | 6.5480 | 7.4834 | 8.4189 | 1.3550 |
| 35 | 0.9353 | 1.8706 | 2.8059 | 3.7412 | 4.6764 | 5.6117 | 6.5470 | 7.4823 | 8.4176 | 1.3549 |
| 36 | 0.9351 | 1.8703 | 2.8054 | 3.7406 | 4.6757 | 5.6109 | 6.5460 | 7.4812 | 8.4163 | 1.3548 |
| 37 | 0.9350 | 1.8700 | 2.8050 | 3.7400 | 4.6750 | 5.6100 | 6.5450 | 7.4801 | 8.4151 | 1.3547 |
| 38 | 0.9349 | 1.8697 | 2.8046 | 3.7395 | 4.6743 | 5.6092 | 6.5441 | 7.4789 | 8.4138 | 1.3546 |
| 39 | 0.9347 | 1.8694 | 2.8042 | 3.7389 | 4.6736 | 5.6083 | 6.5431 | 7.4778 | 8.4125 | 1.3545 |
| 40 | 0.9346 | 1.8692 | 2.8037 | 3.7383 | 4.6729 | 5.6075 | 6.5421 | 7.4767 | 8.4112 | 1.3544 |
| 41 | 0.9344 | 1.8689 | 2.8033 | 3.7378 | 4.6722 | 5.6066 | 6.5411 | 7.4755 | 8.4100 | 1.3543 |
| 42 | 0.9343 | 1.8686 | 2.8029 | 3.7372 | 4.6715 | 5.6058 | 6.5401 | 7.4744 | 8.4087 | 1.3542 |
| 43 | 0.9342 | 1.8683 | 2.8025 | 3.7366 | 4.6708 | 5.6049 | 6.5391 | 7.4732 | 8.4074 | 1.3541 |
| 44 | 0.9340 | 1.8680 | 2.8020 | 3.7360 | 4.6701 | 5.6041 | 6.5381 | 7.4721 | 8.4061 | 1.3540 |
| 45 | 0.9339 | 1.8677 | 2.8016 | 3.7355 | 4.6693 | 5.6032 | 6.5371 | 7.4709 | 8.4048 | 1.3539 |
| 46 | 0.9337 | 1.8674 | 2.8012 | 3.7349 | 4.6686 | 5.6023 | 6.5361 | 7.4698 | 8.4035 | 1.3538 |
| 47 | 0.9336 | 1.8672 | 2.8007 | 3.7343 | 4.6679 | 5.6015 | 6.5351 | 7.4686 | 8.4022 | 1.3537 |
| 48 | 0.9334 | 1.8669 | 2.8003 | 3.7338 | 4.6672 | 5.6006 | 6.5341 | 7.4675 | 8.4009 | 1.3536 |
| 49 | 0.9333 | 1.8666 | 2.7999 | 3.7332 | 4.6665 | 5.5998 | 6.5331 | 7.4664 | 8.3997 | 1.3535 |
| 50 | 0.9332 | 1.8663 | 2.7995 | 3.7326 | 4.6658 | 5.5989 | 6.5321 | 7.4652 | 8.3984 | 1.3534 |
| 51 | 0.9330 | 1.8660 | 2.7990 | 3.7320 | 4.6650 | 5.5980 | 6.5311 | 7.4641 | 8.3971 | 1.3533 |
| 52 | 0.9329 | 1.8657 | 2.7986 | 3.7315 | 4.6643 | 5.5972 | 6.5300 | 7.4629 | 8.3958 | 1.3532 |
| 53 | 0.9327 | 1.8654 | 2.7982 | 3.7309 | 4.6636 | 5.5963 | 6.5290 | 7.4618 | 8.3945 | 1.3530 |
| 54 | 0.9326 | 1.8651 | 2.7977 | 3.7303 | 4.6629 | 5.5954 | 6.5280 | 7.4606 | 8.3932 | 1.3529 |
| 55 | 0.9324 | 1.8649 | 2.7973 | 3.7297 | 4.6621 | 5.5946 | 6.5270 | 7.4594 | 8.3919 | 1.3528 |
| 56 | 0.9323 | 1.8646 | 2.7969 | 3.7291 | 4.6614 | 5.5937 | 6.5260 | 7.4583 | 8.3906 | 1.3527 |
| 57 | 0.9321 | 1.8643 | 2.7964 | 3.7286 | 4.6607 | 5.5928 | 6.5250 | 7.4571 | 8.3893 | 1.3526 |
| 58 | 0.9320 | 1.8640 | 2.7960 | 3.7280 | 4.6600 | 5.5920 | 6.5240 | 7.4560 | 8.3880 | 1.3525 |
| 59 | 0.9319 | 1.8637 | 2.7956 | 3.7274 | 4.6593 | 5.5911 | 6.5230 | 7.4548 | 8.3867 | 1.3524 |
| 60 | 0.9317 | 1.8634 | 2.7951 | 3.7268 | 4.6585 | 5.5902 | 6.5219 | 7.4537 | 8.3854 | 1.3523 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.2344 | 0.4688 | 0.7032 | 0.9376 | 1.1720 | 1.4065 | 1.6409 | 1.8753 | 2.1097 | 0.3387 | 00 |
| 0.2347 | 0.4693 | 0.7040 | 0.9386 | 1.1733 | 1.4080 | 1.6426 | 1.8773 | 2.1120 | 0.3391 | 01 |
| 0.2349 | 0.4698 | 0.7048 | 0.9397 | 1.1746 | 1.4095 | 1.6444 | 1.8794 | 2.1143 | 0.3395 | 02 |
| 0.2352 | 0.4704 | 0.7055 | 0.9407 | 1.1759 | 1.4111 | 1.6462 | 1.8814 | 2.1166 | 0.3399 | 03 |
| 0.2354 | 0.4709 | 0.7063 | 0.9417 | 1.1772 | 1.4126 | 1.6480 | 1.8834 | 2.1189 | 0.3403 | 04 |
| 0.2357 | 0.4714 | 0.7071 | 0.9428 | 1.1785 | 1.4141 | 1.6498 | 1.8855 | 2.1212 | 0.3407 | 05 |
| 0.2359 | 0.4719 | 0.7078 | 0.9438 | 1.1797 | 1.4156 | 1.6516 | 1.8875 | 2.1235 | 0.3411 | 06 |
| 0.2362 | 0.4724 | 0.7086 | 0.9448 | 1.1810 | 1.4172 | 1.6534 | 1.8896 | 2.1258 | 0.3414 | 07 |
| 0.2365 | 0.4729 | 0.7094 | 0.9458 | 1.1823 | 1.4188 | 1.6552 | 1.8917 | 2.1281 | 0.3418 | 08 |
| 0.2367 | 0.4734 | 0.7101 | 0.9468 | 1.1836 | 1.4203 | 1.6570 | 1.8937 | 2.1304 | 0.3422 | 09 |
| 0.2370 | 0.4739 | 0.7109 | 0.9479 | 1.1848 | 1.4218 | 1.6588 | 1.8958 | 2.1327 | 0.3426 | 10 |
| 0.2372 | 0.4744 | 0.7117 | 0.9489 | 1.1861 | 1.4233 | 1.6606 | 1.8978 | 2.1350 | 0.3430 | 11 |
| 0.2375 | 0.4750 | 0.7124 | 0.9499 | 1.1874 | 1.4249 | 1.6624 | 1.8998 | 2.1373 | 0.3434 | 12 |
| 0.2377 | 0.4755 | 0.7132 | 0.9509 | 1.1887 | 1.4264 | 1.6641 | 1.9018 | 2.1396 | 0.3438 | 13 |
| 0.2380 | 0.4760 | 0.7140 | 0.9520 | 1.1899 | 1.4279 | 1.6659 | 1.9039 | 2.1419 | 0.3442 | 14 |
| 0.2382 | 0.4765 | 0.7147 | 0.9530 | 1.1912 | 1.4295 | 1.6677 | 1.9060 | 2.1442 | 0.3446 | 15 |
| 0.2385 | 0.4770 | 0.7155 | 0.9540 | 1.1925 | 1.4310 | 1.6695 | 1.9080 | 2.1465 | 0.3450 | 16 |
| 0.2388 | 0.4775 | 0.7163 | 0.9550 | 1.1938 | 1.4326 | 1.6713 | 1.9101 | 2.1488 | 0.3454 | 17 |
| 0.2390 | 0.4780 | 0.7170 | 0.9560 | 1.1951 | 1.4341 | 1.6731 | 1.9121 | 2.1511 | 0.3458 | 18 |
| 0.2393 | 0.4785 | 0.7178 | 0.9571 | 1.1963 | 1.4356 | 1.6749 | 1.9142 | 2.1534 | 0.3462 | 19 |
| 0.2395 | 0.4790 | 0.7186 | 0.9581 | 1.1976 | 1.4371 | 1.6767 | 1.9162 | 2.1557 | 0.3466 | 20 |
| 0.2398 | 0.4796 | 0.7193 | 0.9591 | 1.1989 | 1.4387 | 1.6785 | 1.9182 | 2.1580 | 0.3470 | 21 |
| 0.2400 | 0.4801 | 0.7201 | 0.9601 | 1.2002 | 1.4402 | 1.6802 | 1.9202 | 2.1603 | 0.3474 | 22 |
| 0.2403 | 0.4806 | 0.7209 | 0.9611 | 1.2014 | 1.4417 | 1.6820 | 1.9223 | 2.1626 | 0.3478 | 23 |
| 0.2405 | 0.4811 | 0.7216 | 0.9622 | 1.2027 | 1.4432 | 1.6838 | 1.9243 | 2.1648 | 0.3482 | 24 |
| 0.2408 | 0.4816 | 0.7224 | 0.9632 | 1.2040 | 1.4448 | 1.6856 | 1.9264 | 2.1671 | 0.3485 | 25 |
| 0.2411 | 0.4821 | 0.7232 | 0.9642 | 1.2053 | 1.4463 | 1.6874 | 1.9284 | 2.1694 | 0.3489 | 26 |
| 0.2413 | 0.4826 | 0.7239 | 0.9652 | 1.2065 | 1.4478 | 1.6891 | 1.9304 | 2.1717 | 0.3493 | 27 |
| 0.2416 | 0.4831 | 0.7247 | 0.9662 | 1.2078 | 1.4494 | 1.6909 | 1.9325 | 2.1740 | 0.3497 | 28 |
| 0.2418 | 0.4836 | 0.7254 | 0.9672 | 1.2091 | 1.4509 | 1.6927 | 1.9345 | 2.1763 | 0.3501 | 29 |
| 0.2421 | 0.4841 | 0.7262 | 0.9683 | 1.2103 | 1.4524 | 1.6945 | 1.9366 | 2.1786 | 0.3505 | 30 |
| 0.2423 | 0.4846 | 0.7270 | 0.9693 | 1.2116 | 1.4539 | 1.6962 | 1.9386 | 2.1809 | 0.3509 | 31 |
| 0.2425 | 0.4851 | 0.7277 | 0.9703 | 1.2129 | 1.4554 | 1.6980 | 1.9406 | 2.1831 | 0.3513 | 32 |
| 0.2428 | 0.4857 | 0.7285 | 0.9713 | 1.2141 | 1.4570 | 1.6998 | 1.9426 | 2.1855 | 0.3517 | 33 |
| 0.2431 | 0.4862 | 0.7292 | 0.9723 | 1.2154 | 1.4585 | 1.7016 | 1.9446 | 2.1877 | 0.3521 | 34 |
| 0.2433 | 0.4867 | 0.7299 | 0.9733 | 1.2166 | 1.4600 | 1.7033 | 1.9466 | 2.1900 | 0.3525 | 35 |
| 0.2436 | 0.4872 | 0.7307 | 0.9743 | 1.2179 | 1.4615 | 1.7051 | 1.9487 | 2.1923 | 0.3529 | 36 |
| 0.2438 | 0.4877 | 0.7315 | 0.9754 | 1.2192 | 1.4630 | 1.7069 | 1.9507 | 2.1946 | 0.3533 | 37 |
| 0.2441 | 0.4882 | 0.7323 | 0.9764 | 1.2205 | 1.4646 | 1.7087 | 1.9528 | 2.1969 | 0.3537 | 38 |
| 0.2443 | 0.4887 | 0.7330 | 0.9774 | 1.2217 | 1.4661 | 1.7104 | 1.9548 | 2.1991 | 0.3541 | 39 |
| 0.2446 | 0.4892 | 0.7338 | 0.9784 | 1.2230 | 1.4676 | 1.7122 | 1.9568 | 2.2014 | 0.3545 | 40 |
| 0.2449 | 0.4897 | 0.7346 | 0.9794 | 1.2243 | 1.4691 | 1.7140 | 1.9588 | 2.2037 | 0.3549 | 41 |
| 0.2451 | 0.4902 | 0.7353 | 0.9804 | 1.2255 | 1.4706 | 1.7157 | 1.9608 | 2.2059 | 0.3553 | 42 |
| 0.2454 | 0.4907 | 0.7361 | 0.9814 | 1.2268 | 1.4722 | 1.7175 | 1.9629 | 2.2082 | 0.3557 | 43 |
| 0.2456 | 0.4912 | 0.7368 | 0.9824 | 1.2281 | 1.4737 | 1.7193 | 1.9649 | 2.2105 | 0.3560 | 44 |
| 0.2459 | 0.4917 | 0.7376 | 0.9835 | 1.2294 | 1.4752 | 1.7211 | 1.9670 | 2.2128 | 0.3564 | 45 |
| 0.2461 | 0.4922 | 0.7384 | 0.9845 | 1.2306 | 1.4767 | 1.7228 | 1.9690 | 2.2151 | 0.3568 | 46 |
| 0.2464 | 0.4927 | 0.7391 | 0.9855 | 1.2319 | 1.4782 | 1.7246 | 1.9710 | 2.2173 | 0.3572 | 47 |
| 0.2466 | 0.4932 | 0.7399 | 0.9865 | 1.2331 | 1.4797 | 1.7263 | 1.9730 | 2.2196 | 0.3576 | 48 |
| 0.2469 | 0.4938 | 0.7406 | 0.9875 | 1.2344 | 1.4813 | 1.7281 | 1.9750 | 2.2219 | 0.3580 | 49 |
| 0.2471 | 0.4943 | 0.7414 | 0.9885 | 1.2357 | 1.4828 | 1.7299 | 1.9770 | 2.2242 | 0.3584 | 50 |
| 0.2474 | 0.4948 | 0.7421 | 0.9895 | 1.2369 | 1.4843 | 1.7317 | 1.9790 | 2.2264 | 0.3588 | 51 |
| 0.2476 | 0.4953 | 0.7429 | 0.9905 | 1.2382 | 1.4858 | 1.7334 | 1.9810 | 2.2287 | 0.3592 | 52 |
| 0.2479 | 0.4958 | 0.7436 | 0.9915 | 1.2394 | 1.4873 | 1.7352 | 1.9831 | 2.2310 | 0.3596 | 53 |
| 0.2481 | 0.4963 | 0.7444 | 0.9926 | 1.2407 | 1.4888 | 1.7370 | 1.9851 | 2.2333 | 0.3600 | 54 |
| 0.2484 | 0.4968 | 0.7452 | 0.9936 | 1.2420 | 1.4903 | 1.7387 | 1.9871 | 2.2355 | 0.3604 | 55 |
| 0.2486 | 0.4973 | 0.7459 | 0.9946 | 1.2432 | 1.4918 | 1.7405 | 1.9891 | 2.2378 | 0.3608 | 56 |
| 0.2489 | 0.4978 | 0.7467 | 0.9956 | 1.2445 | 1.4933 | 1.7422 | 1.9911 | 2.2400 | 0.3612 | 57 |
| 0.2491 | 0.4983 | 0.7474 | 0.9966 | 1.2457 | 1.4949 | 1.7440 | 1.9932 | 2.2423 | 0.3616 | 58 |
| 0.2494 | 0.4988 | 0.7482 | 0.9976 | 1.2470 | 1.4964 | 1.7458 | 1.9952 | 2.2446 | 0.3620 | 59 |
| 0.2497 | 0.4993 | 0.7490 | 0.9986 | 1.2483 | 1.4979 | 1.7476 | 1.9972 | 2.2469 | 0.3623 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9317 | 1.8634 | 2.7951 | 3.7268 | 4.6585 | 5.5902 | 6.5219 | 7.4537 | 8.3854 | 1.3523 |
| 01 | 0.9316 | 1.8631 | 2.7947 | 3.7262 | 4.6578 | 5.5894 | 6.5209 | 7.4525 | 8.3840 | 1.3522 |
| 02 | 0.9314 | 1.8628 | 2.7942 | 3.7257 | 4.6571 | 5.5885 | 6.5199 | 7.4513 | 8.3827 | 1.3521 |
| 03 | 0.9313 | 1.8625 | 2.7938 | 3.7251 | 4.6563 | 5.5876 | 6.5189 | 7.4502 | 8.3814 | 1.3520 |
| 04 | 0.9311 | 1.8622 | 2.7934 | 3.7245 | 4.6556 | 5.5867 | 6.5179 | 7.4490 | 8.3801 | 1.3519 |
| 05 | 0.9310 | 1.8620 | 2.7929 | 3.7239 | 4.6549 | 5.5859 | 6.5168 | 7.4478 | 8.3788 | 1.3518 |
| 06 | 0.9308 | 1.8617 | 2.7925 | 3.7233 | 4.6542 | 5.5850 | 6.5158 | 7.4466 | 8.3775 | 1.3517 |
| 07 | 0.9307 | 1.8614 | 2.7921 | 3.7227 | 4.6534 | 5.5841 | 6.5148 | 7.4455 | 8.3762 | 1.3516 |
| 08 | 0.9305 | 1.8611 | 2.7916 | 3.7222 | 4.6527 | 5.5832 | 6.5138 | 7.4443 | 8.3749 | 1.3515 |
| 09 | 0.9304 | 1.8608 | 2.7912 | 3.7216 | 4.6520 | 5.5824 | 6.5128 | 7.4432 | 8.3736 | 1.3514 |
| 10 | 0.9302 | 1.8605 | 2.7907 | 3.7210 | 4.6512 | 5.5815 | 6.5117 | 7.4420 | 8.3722 | 1.3513 |
| 11 | 0.9301 | 1.8602 | 2.7903 | 3.7204 | 4.6505 | 5.5806 | 6.5107 | 7.4408 | 8.3709 | 1.3512 |
| 12 | 0.9300 | 1.8599 | 2.7899 | 3.7198 | 4.6498 | 5.5797 | 6.5097 | 7.4396 | 8.3696 | 1.3511 |
| 13 | 0.9298 | 1.8596 | 2.7894 | 3.7192 | 4.6490 | 5.5788 | 6.5086 | 7.4384 | 8.3682 | 1.3510 |
| 14 | 0.9297 | 1.8593 | 2.7890 | 3.7186 | 4.6483 | 5.5779 | 6.5076 | 7.4373 | 8.3669 | 1.3509 |
| 15 | 0.9295 | 1.8590 | 2.7885 | 3.7180 | 4.6476 | 5.5771 | 6.5066 | 7.4361 | 8.3656 | 1.3508 |
| 16 | 0.9294 | 1.8587 | 2.7881 | 3.7175 | 4.6468 | 5.5762 | 6.5055 | 7.4349 | 8.3643 | 1.3507 |
| 17 | 0.9292 | 1.8584 | 2.7876 | 3.7169 | 4.6461 | 5.5753 | 6.5045 | 7.4337 | 8.3629 | 1.3506 |
| 18 | 0.9291 | 1.8581 | 2.7872 | 3.7163 | 4.6453 | 5.5744 | 6.5035 | 7.4325 | 8.3616 | 1.3504 |
| 19 | 0.9289 | 1.8578 | 2.7868 | 3.7157 | 4.6446 | 5.5735 | 6.5024 | 7.4314 | 8.3603 | 1.3503 |
| 20 | 0.9288 | 1.8575 | 2.7863 | 3.7151 | 4.6439 | 5.5726 | 6.5014 | 7.4302 | 8.3590 | 1.3502 |
| 21 | 0.9286 | 1.8572 | 2.7859 | 3.7145 | 4.6431 | 5.5717 | 6.5004 | 7.4290 | 8.3576 | 1.3501 |
| 22 | 0.9285 | 1.8570 | 2.7854 | 3.7139 | 4.6424 | 5.5709 | 6.4993 | 7.4278 | 8.3563 | 1.3500 |
| 23 | 0.9283 | 1.8567 | 2.7850 | 3.7133 | 4.6416 | 5.5700 | 6.4983 | 7.4266 | 8.3549 | 1.3499 |
| 24 | 0.9282 | 1.8564 | 2.7845 | 3.7127 | 4.6409 | 5.5691 | 6.4972 | 7.4254 | 8.3536 | 1.3498 |
| 25 | 0.9280 | 1.8561 | 2.7841 | 3.7121 | 4.6401 | 5.5682 | 6.4962 | 7.4242 | 8.3523 | 1.3497 |
| 26 | 0.9279 | 1.8558 | 2.7836 | 3.7115 | 4.6394 | 5.5673 | 6.4952 | 7.4230 | 8.3509 | 1.3496 |
| 27 | 0.9277 | 1.8555 | 2.7832 | 3.7109 | 4.6387 | 5.5664 | 6.4941 | 7.4218 | 8.3496 | 1.3495 |
| 28 | 0.9276 | 1.8552 | 2.7827 | 3.7103 | 4.6379 | 5.5655 | 6.4931 | 7.4207 | 8.3482 | 1.3494 |
| 29 | 0.9274 | 1.8549 | 2.7823 | 3.7097 | 4.6372 | 5.5646 | 6.4920 | 7.4195 | 8.3469 | 1.3493 |
| 30 | 0.9273 | 1.8546 | 2.7819 | 3.7091 | 4.6364 | 5.5637 | 6.4910 | 7.4183 | 8.3455 | 1.3491 |
| 31 | 0.9271 | 1.8543 | 2.7814 | 3.7085 | 4.6357 | 5.5628 | 6.4899 | 7.4171 | 8.3442 | 1.3490 |
| 32 | 0.9270 | 1.8540 | 2.7809 | 3.7079 | 4.6349 | 5.5619 | 6.4889 | 7.4159 | 8.3428 | 1.3489 |
| 33 | 0.9268 | 1.8537 | 2.7805 | 3.7073 | 4.6342 | 5.5610 | 6.4878 | 7.4147 | 8.3415 | 1.3488 |
| 34 | 0.9267 | 1.8534 | 2.7800 | 3.7067 | 4.6334 | 5.5601 | 6.4868 | 7.4135 | 8.3401 | 1.3487 |
| 35 | 0.9265 | 1.8531 | 2.7796 | 3.7061 | 4.6327 | 5.5592 | 6.4857 | 7.4123 | 8.3388 | 1.3486 |
| 36 | 0.9264 | 1.8528 | 2.7791 | 3.7055 | 4.6319 | 5.5583 | 6.4847 | 7.4111 | 8.3374 | 1.3485 |
| 37 | 0.9262 | 1.8525 | 2.7787 | 3.7049 | 4.6312 | 5.5574 | 6.4836 | 7.4098 | 8.3361 | 1.3484 |
| 38 | 0.9261 | 1.8522 | 2.7782 | 3.7043 | 4.6304 | 5.5565 | 6.4826 | 7.4086 | 8.3347 | 1.3483 |
| 39 | 0.9259 | 1.8519 | 2.7778 | 3.7037 | 4.6297 | 5.5556 | 6.4815 | 7.4074 | 8.3334 | 1.3482 |
| 40 | 0.9258 | 1.8516 | 2.7773 | 3.7031 | 4.6289 | 5.5547 | 6.4805 | 7.4062 | 8.3320 | 1.3480 |
| 41 | 0.9256 | 1.8513 | 2.7769 | 3.7025 | 4.6281 | 5.5538 | 6.4794 | 7.4050 | 8.3307 | 1.3479 |
| 42 | 0.9255 | 1.8510 | 2.7764 | 3.7019 | 4.6274 | 5.5529 | 6.4783 | 7.4038 | 8.3293 | 1.3478 |
| 43 | 0.9253 | 1.8506 | 2.7760 | 3.7013 | 4.6266 | 5.5519 | 6.4773 | 7.4026 | 8.3279 | 1.3477 |
| 44 | 0.9252 | 1.8503 | 2.7755 | 3.7007 | 4.6259 | 5.5510 | 6.4762 | 7.4014 | 8.3266 | 1.3476 |
| 45 | 0.9250 | 1.8500 | 2.7751 | 3.7001 | 4.6251 | 5.5501 | 6.4751 | 7.4002 | 8.3252 | 1.3475 |
| 46 | 0.9249 | 1.8497 | 2.7746 | 3.6995 | 4.6243 | 5.5492 | 6.4741 | 7.3990 | 8.3238 | 1.3474 |
| 47 | 0.9247 | 1.8494 | 2.7742 | 3.6989 | 4.6236 | 5.5483 | 6.4730 | 7.3977 | 8.3225 | 1.3473 |
| 48 | 0.9246 | 1.8491 | 2.7737 | 3.6983 | 4.6228 | 5.5474 | 6.4720 | 7.3965 | 8.3211 | 1.3472 |
| 49 | 0.9244 | 1.8488 | 2.7732 | 3.6977 | 4.6221 | 5.5465 | 6.4709 | 7.3953 | 8.3197 | 1.3470 |
| 50 | 0.9243 | 1.8485 | 2.7728 | 3.6970 | 4.6213 | 5.5456 | 6.4698 | 7.3941 | 8.3184 | 1.3469 |
| 51 | 0.9241 | 1.8482 | 2.7723 | 3.6964 | 4.6205 | 5.5447 | 6.4688 | 7.3929 | 8.3170 | 1.3468 |
| 52 | 0.9240 | 1.8479 | 2.7719 | 3.6958 | 4.6198 | 5.5437 | 6.4677 | 7.3916 | 8.3156 | 1.3467 |
| 53 | 0.9238 | 1.8476 | 2.7714 | 3.6952 | 4.6190 | 5.5428 | 6.4666 | 7.3904 | 8.3142 | 1.3466 |
| 54 | 0.9236 | 1.8473 | 2.7709 | 3.6946 | 4.6182 | 5.5419 | 6.4655 | 7.3892 | 8.3128 | 1.3465 |
| 55 | 0.9235 | 1.8470 | 2.7705 | 3.6940 | 4.6175 | 5.5410 | 6.4645 | 7.3880 | 8.3115 | 1.3464 |
| 56 | 0.9233 | 1.8467 | 2.7700 | 3.6934 | 4.6167 | 5.5401 | 6.4634 | 7.3867 | 8.3101 | 1.3463 |
| 57 | 0.9232 | 1.8464 | 2.7696 | 3.6928 | 4.6159 | 5.5391 | 6.4623 | 7.3855 | 8.3087 | 1.3461 |
| 58 | 0.9230 | 1.8461 | 2.7691 | 3.6921 | 4.6152 | 5.5382 | 6.4613 | 7.3843 | 8.3073 | 1.3460 |
| 59 | 0.9228 | 1.8458 | 2.7686 | 3.6915 | 4.6144 | 5.5373 | 6.4602 | 7.3831 | 8.3059 | 1.3459 |
| 60 | 0.9227 | 1.8455 | 2.7682 | 3.6909 | 4.6137 | 5.5364 | 6.4591 | 7.3818 | 8.3046 | 1.3458 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | c  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.2497 | 0.4993 | 0.7400 | 0.9986 | 1.2483 | 1.4979 | 1.7476 | 1.9972 | 2.2469 | 0.3623 | 00 |
| 0.2499 | 0.4998 | 0.7497 | 0.9996 | 1.2495 | 1.4994 | 1.7493 | 1.9992 | 2.2491 | 0.3627 | 01 |
| 0.2502 | 0.5003 | 0.7505 | 1.0000 | 1.2508 | 1.5009 | 1.7511 | 2.0012 | 2.2514 | 0.3631 | 02 |
| 0.2504 | 0.5008 | 0.7512 | 1.0016 | 1.2520 | 1.5024 | 1.7528 | 2.0032 | 2.2530 | 0.3635 | 03 |
| 0.2507 | 0.5013 | 0.7520 | 1.0026 | 1.2533 | 1.5040 | 1.7546 | 2.0053 | 2.2559 | 0.3639 | 04 |
| 0.2509 | 0.5018 | 0.7527 | 1.0036 | 1.2545 | 1.5055 | 1.7564 | 2.0073 | 2.2582 | 0.3643 | 05 |
| 0.2512 | 0.5023 | 0.7535 | 1.0046 | 1.2558 | 1.5070 | 1.7581 | 2.0093 | 2.2604 | 0.3647 | 06 |
| 0.2515 | 0.5028 | 0.7542 | 1.0056 | 1.2570 | 1.5084 | 1.7599 | 2.0113 | 2.2627 | 0.3651 | 07 |
| 0.2517 | 0.5033 | 0.7550 | 1.0066 | 1.2583 | 1.5100 | 1.7616 | 2.0133 | 2.2649 | 0.3655 | 08 |
| 0.2519 | 0.5038 | 0.7557 | 1.0076 | 1.2596 | 1.5115 | 1.7634 | 2.0153 | 2.2672 | 0.3659 | 09 |
| 0.2522 | 0.5043 | 0.7565 | 1.0086 | 1.2608 | 1.5130 | 1.7651 | 2.0173 | 2.2694 | 0.3663 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2524 | 0.5048 | 0.7572 | 1.0096 | 1.2621 | 1.5145 | 1.7669 | 2.0193 | 2.2717 | 0.3667 | 11 |
| 0.2527 | 0.5053 | 0.7580 | 1.0106 | 1.2633 | 1.5160 | 1.7686 | 2.0213 | 2.2739 | 0.3671 | 12 |
| 0.2529 | 0.5058 | 0.7587 | 1.0116 | 1.2646 | 1.5175 | 1.7704 | 2.0233 | 2.2762 | 0.3674 | 13 |
| 0.2532 | 0.5063 | 0.7595 | 1.0126 | 1.2658 | 1.5190 | 1.7721 | 2.0253 | 2.2784 | 0.3678 | 14 |
| 0.2534 | 0.5068 | 0.7602 | 1.0136 | 1.2671 | 1.5205 | 1.7739 | 2.0273 | 2.2807 | 0.3682 | 15 |
| 0.2537 | 0.5073 | 0.7610 | 1.0146 | 1.2683 | 1.5220 | 1.7756 | 2.0293 | 2.2829 | 0.3686 | 16 |
| 0.2539 | 0.5078 | 0.7617 | 1.0156 | 1.2696 | 1.5235 | 1.7774 | 2.0313 | 2.2852 | 0.3690 | 17 |
| 0.2542 | 0.5083 | 0.7625 | 1.0166 | 1.2708 | 1.5250 | 1.7791 | 2.0333 | 2.2874 | 0.3694 | 18 |
| 0.2544 | 0.5088 | 0.7632 | 1.0176 | 1.2721 | 1.5265 | 1.7809 | 2.0353 | 2.2897 | 0.3698 | 19 |
| 0.2547 | 0.5093 | 0.7640 | 1.0186 | 1.2733 | 1.5280 | 1.7826 | 2.0373 | 2.2919 | 0.3702 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2549 | 0.5098 | 0.7647 | 1.0196 | 1.2746 | 1.5295 | 1.7844 | 2.0393 | 2.2942 | 0.3706 | 21 |
| 0.2552 | 0.5103 | 0.7655 | 1.0206 | 1.2758 | 1.5310 | 1.7861 | 2.0413 | 2.2964 | 0.3710 | 22 |
| 0.2554 | 0.5108 | 0.7662 | 1.0216 | 1.2771 | 1.5325 | 1.7879 | 2.0433 | 2.2987 | 0.3714 | 23 |
| 0.2557 | 0.5113 | 0.7670 | 1.0226 | 1.2783 | 1.5340 | 1.7896 | 2.0453 | 2.3009 | 0.3718 | 24 |
| 0.2559 | 0.5118 | 0.7677 | 1.0236 | 1.2796 | 1.5355 | 1.7914 | 2.0473 | 2.3032 | 0.3722 | 25 |
| 0.2562 | 0.5123 | 0.7685 | 1.0246 | 1.2808 | 1.5370 | 1.7931 | 2.0493 | 2.3054 | 0.3725 | 26 |
| 0.2564 | 0.5128 | 0.7692 | 1.0256 | 1.2821 | 1.5385 | 1.7949 | 2.0513 | 2.3077 | 0.3729 | 27 |
| 0.2567 | 0.5133 | 0.7700 | 1.0266 | 1.2833 | 1.5400 | 1.7966 | 2.0533 | 2.3099 | 0.3733 | 28 |
| 0.2569 | 0.5138 | 0.7707 | 1.0276 | 1.2845 | 1.5415 | 1.7984 | 2.0553 | 2.3122 | 0.3737 | 29 |
| 0.2572 | 0.5143 | 0.7715 | 1.0286 | 1.2858 | 1.5430 | 1.8001 | 2.0573 | 2.3144 | 0.3741 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2574 | 0.5148 | 0.7722 | 1.0296 | 1.2870 | 1.5445 | 1.8019 | 2.0593 | 2.3167 | 0.3745 | 31 |
| 0.2577 | 0.5153 | 0.7730 | 1.0306 | 1.2883 | 1.5460 | 1.8036 | 2.0613 | 2.3189 | 0.3749 | 32 |
| 0.2579 | 0.5158 | 0.7737 | 1.0316 | 1.2895 | 1.5474 | 1.8053 | 2.0632 | 2.3211 | 0.3753 | 33 |
| 0.2582 | 0.5163 | 0.7745 | 1.0326 | 1.2908 | 1.5489 | 1.8071 | 2.0652 | 2.3234 | 0.3757 | 34 |
| 0.2584 | 0.5168 | 0.7752 | 1.0336 | 1.2920 | 1.5504 | 1.8088 | 2.0672 | 2.3256 | 0.3761 | 35 |
| 0.2587 | 0.5173 | 0.7760 | 1.0346 | 1.2933 | 1.5519 | 1.8106 | 2.0692 | 2.3279 | 0.3765 | 36 |
| 0.2589 | 0.5178 | 0.7767 | 1.0356 | 1.2945 | 1.5534 | 1.8123 | 2.0712 | 2.3301 | 0.3769 | 37 |
| 0.2591 | 0.5183 | 0.7774 | 1.0366 | 1.2957 | 1.5549 | 1.8140 | 2.0732 | 2.3323 | 0.3773 | 38 |
| 0.2594 | 0.5188 | 0.7782 | 1.0376 | 1.2970 | 1.5564 | 1.8158 | 2.0752 | 2.3346 | 0.3776 | 39 |
| 0.2596 | 0.5193 | 0.7789 | 1.0386 | 1.2982 | 1.5578 | 1.8175 | 2.0771 | 2.3368 | 0.3780 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2599 | 0.5198 | 0.7797 | 1.0396 | 1.2995 | 1.5593 | 1.8192 | 2.0791 | 2.3390 | 0.3784 | 41 |
| 0.2601 | 0.5203 | 0.7804 | 1.0406 | 1.3007 | 1.5608 | 1.8210 | 2.0811 | 2.3413 | 0.3788 | 42 |
| 0.2604 | 0.5208 | 0.7811 | 1.0416 | 1.3019 | 1.5623 | 1.8227 | 2.0831 | 2.3435 | 0.3792 | 43 |
| 0.2606 | 0.5213 | 0.7819 | 1.0426 | 1.3032 | 1.5638 | 1.8245 | 2.0851 | 2.3458 | 0.3796 | 44 |
| 0.2609 | 0.5218 | 0.7826 | 1.0435 | 1.3044 | 1.5653 | 1.8262 | 2.0870 | 2.3479 | 0.3800 | 45 |
| 0.2611 | 0.5223 | 0.7834 | 1.0445 | 1.3057 | 1.5668 | 1.8279 | 2.0890 | 2.3502 | 0.3804 | 46 |
| 0.2614 | 0.5228 | 0.7841 | 1.0455 | 1.3069 | 1.5683 | 1.8297 | 2.0910 | 2.3524 | 0.3808 | 47 |
| 0.2616 | 0.5233 | 0.7849 | 1.0465 | 1.3081 | 1.5698 | 1.8314 | 2.0930 | 2.3547 | 0.3812 | 48 |
| 0.2619 | 0.5237 | 0.7856 | 1.0475 | 1.3094 | 1.5712 | 1.8331 | 2.0950 | 2.3569 | 0.3816 | 49 |
| 0.2621 | 0.5242 | 0.7864 | 1.0485 | 1.3106 | 1.5727 | 1.8348 | 2.0970 | 2.3591 | 0.3820 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2624 | 0.5247 | 0.7871 | 1.0495 | 1.3118 | 1.5742 | 1.8366 | 2.0990 | 2.3613 | 0.3824 | 51 |
| 0.2626 | 0.5252 | 0.7879 | 1.0505 | 1.3131 | 1.5757 | 1.8383 | 2.1010 | 2.3636 | 0.3827 | 52 |
| 0.2629 | 0.5257 | 0.7886 | 1.0514 | 1.3143 | 1.5772 | 1.8400 | 2.1029 | 2.3658 | 0.3831 | 53 |
| 0.2631 | 0.5262 | 0.7893 | 1.0524 | 1.3155 | 1.5787 | 1.8418 | 2.1049 | 2.3680 | 0.3835 | 54 |
| 0.2634 | 0.5267 | 0.7901 | 1.0534 | 1.3168 | 1.5802 | 1.8435 | 2.1069 | 2.3702 | 0.3839 | 55 |
| 0.2636 | 0.5272 | 0.7908 | 1.0544 | 1.3180 | 1.5816 | 1.8452 | 2.1088 | 2.3724 | 0.3843 | 56 |
| 0.2638 | 0.5277 | 0.7915 | 1.0554 | 1.3192 | 1.5831 | 1.8469 | 2.1108 | 2.3746 | 0.3847 | 57 |
| 0.2641 | 0.5282 | 0.7923 | 1.0564 | 1.3205 | 1.5846 | 1.8487 | 2.1128 | 2.3769 | 0.3851 | 58 |
| 0.2643 | 0.5287 | 0.7930 | 1.0574 | 1.3217 | 1.5860 | 1.8504 | 2.1147 | 2.3791 | 0.3855 | 59 |
| 0.2646 | 0.5292 | 0.7938 | 1.0584 | 1.3230 | 1.5875 | 1.8521 | 2.1167 | 2.3813 | 0.3859 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9227 | 1.8455 | 2.7682 | 3.6909 | 4.6137 | 5.5364 | 6.4591 | 7.3818 | 8.3046 | 1.3458 |
| 01 | 0.9226 | 1.8452 | 2.7677 | 3.6903 | 4.6129 | 5.5355 | 6.4580 | 7.3806 | 8.3032 | 1.3457 |
| 02 | 0.9224 | 1.8448 | 2.7673 | 3.6897 | 4.6121 | 5.5345 | 6.4569 | 7.3794 | 8.3018 | 1.3456 |
| 03 | 0.9223 | 1.8445 | 2.7668 | 3.6891 | 4.6113 | 5.5336 | 6.4559 | 7.3781 | 8.3004 | 1.3455 |
| 04 | 0.9221 | 1.8442 | 2.7663 | 3.6884 | 4.6006 | 5.5327 | 6.4548 | 7.3769 | 8.2990 | 1.3454 |
| 05 | 0.9220 | 1.8439 | 2.7659 | 3.6878 | 4.6098 | 5.5317 | 6.4537 | 7.3757 | 8.2976 | 1.3453 |
| 06 | 0.9218 | 1.8436 | 2.7654 | 3.6872 | 4.6090 | 5.5308 | 6.4526 | 7.3744 | 8.2962 | 1.3451 |
| 07 | 0.9216 | 1.8433 | 2.7649 | 3.6866 | 4.6082 | 5.5299 | 6.4515 | 7.3732 | 8.2948 | 1.3450 |
| 08 | 0.9215 | 1.8430 | 2.7645 | 3.6860 | 4.6075 | 5.5290 | 6.4505 | 7.3719 | 8.2934 | 1.3449 |
| 09 | 0.9213 | 1.8427 | 2.7640 | 3.6854 | 4.6067 | 5.5280 | 6.4494 | 7.3707 | 8.2921 | 1.3448 |
| 10 | 0.9212 | 1.8424 | 2.7636 | 3.6847 | 4.6059 | 5.5271 | 6.4483 | 7.3695 | 8.2907 | 1.3447 |
| 11 | 0.9210 | 1.8421 | 2.7631 | 3.6841 | 4.6051 | 5.5262 | 6.4472 | 7.3682 | 8.2893 | 1.3446 |
| 12 | 0.9209 | 1.8417 | 2.7626 | 3.6835 | 4.6044 | 5.5252 | 6.4461 | 7.3670 | 8.2878 | 1.3445 |
| 13 | 0.9207 | 1.8414 | 2.7621 | 3.6829 | 4.6036 | 5.5243 | 6.4450 | 7.3657 | 8.2864 | 1.3444 |
| 14 | 0.9206 | 1.8411 | 2.7617 | 3.6822 | 4.6028 | 5.5234 | 6.4439 | 7.3645 | 8.2850 | 1.3442 |
| 15 | 0.9204 | 1.8408 | 2.7612 | 3.6816 | 4.6020 | 5.5224 | 6.4428 | 7.3632 | 8.2836 | 1.3441 |
| 16 | 0.9202 | 1.8405 | 2.7607 | 3.6810 | 4.6012 | 5.5215 | 6.4417 | 7.3620 | 8.2822 | 1.3440 |
| 17 | 0.9201 | 1.8402 | 2.7603 | 3.6804 | 4.6005 | 5.5205 | 6.4406 | 7.3607 | 8.2808 | 1.3439 |
| 18 | 0.9199 | 1.8399 | 2.7598 | 3.6797 | 4.5997 | 5.5196 | 6.4395 | 7.3595 | 8.2794 | 1.3438 |
| 19 | 0.9198 | 1.8396 | 2.7593 | 3.6791 | 4.5989 | 5.5187 | 6.4385 | 7.3582 | 8.2780 | 1.3437 |
| 20 | 0.9196 | 1.8392 | 2.7589 | 3.6785 | 4.5981 | 5.5177 | 6.4374 | 7.3570 | 8.2766 | 1.3436 |
| 21 | 0.9195 | 1.8389 | 2.7584 | 3.6779 | 4.5973 | 5.5168 | 6.4363 | 7.3557 | 8.2752 | 1.3435 |
| 22 | 0.9193 | 1.8386 | 2.7579 | 3.6772 | 4.5965 | 5.5158 | 6.4352 | 7.3545 | 8.2738 | 1.3433 |
| 23 | 0.9192 | 1.8383 | 2.7575 | 3.6766 | 4.5958 | 5.5149 | 6.4341 | 7.3532 | 8.2724 | 1.3432 |
| 24 | 0.9190 | 1.8380 | 2.7570 | 3.6760 | 4.5950 | 5.5140 | 6.4330 | 7.3519 | 8.2709 | 1.3431 |
| 25 | 0.9188 | 1.8377 | 2.7565 | 3.6753 | 4.5942 | 5.5130 | 6.4319 | 7.3507 | 8.2695 | 1.3430 |
| 26 | 0.9187 | 1.8374 | 2.7560 | 3.6747 | 4.5934 | 5.5121 | 6.4307 | 7.3494 | 8.2681 | 1.3429 |
| 27 | 0.9185 | 1.8370 | 2.7556 | 3.6741 | 4.5926 | 5.5111 | 6.4296 | 7.3482 | 8.2667 | 1.3428 |
| 28 | 0.9184 | 1.8367 | 2.7551 | 3.6735 | 4.5918 | 5.5102 | 6.4285 | 7.3469 | 8.2653 | 1.3427 |
| 29 | 0.9182 | 1.8364 | 2.7546 | 3.6728 | 4.5910 | 5.5092 | 6.4274 | 7.3456 | 8.2639 | 1.3425 |
| 30 | 0.9180 | 1.8361 | 2.7541 | 3.6722 | 4.5902 | 5.5083 | 6.4263 | 7.3444 | 8.2624 | 1.3424 |
| 31 | 0.9179 | 1.8358 | 2.7537 | 3.6716 | 4.5894 | 5.5073 | 6.4252 | 7.3431 | 8.2610 | 1.3423 |
| 32 | 0.9177 | 1.8355 | 2.7532 | 3.6709 | 4.5887 | 5.5064 | 6.4241 | 7.3418 | 8.2596 | 1.3422 |
| 33 | 0.9176 | 1.8351 | 2.7527 | 3.6703 | 4.5879 | 5.5054 | 6.4230 | 7.3406 | 8.2581 | 1.3420 |
| 34 | 0.9174 | 1.8348 | 2.7522 | 3.6696 | 4.5871 | 5.5045 | 6.4219 | 7.3393 | 8.2567 | 1.3419 |
| 35 | 0.9173 | 1.8345 | 2.7518 | 3.6690 | 4.5863 | 5.5035 | 6.4208 | 7.3380 | 8.2553 | 1.3418 |
| 36 | 0.9171 | 1.8342 | 2.7513 | 3.6684 | 4.5855 | 5.5026 | 6.4197 | 7.3368 | 8.2539 | 1.3417 |
| 37 | 0.9169 | 1.8339 | 2.7508 | 3.6677 | 4.5847 | 5.5016 | 6.4186 | 7.3355 | 8.2524 | 1.3416 |
| 38 | 0.9168 | 1.8336 | 2.7503 | 3.6671 | 4.5839 | 5.5007 | 6.4174 | 7.3342 | 8.2510 | 1.3415 |
| 39 | 0.9166 | 1.8332 | 2.7499 | 3.6665 | 4.5831 | 5.4997 | 6.4163 | 7.3329 | 8.2496 | 1.3413 |
| 40 | 0.9165 | 1.8329 | 2.7494 | 3.6658 | 4.5823 | 5.4988 | 6.4152 | 7.3317 | 8.2481 | 1.3412 |
| 41 | 0.9163 | 1.8326 | 2.7489 | 3.6652 | 4.5815 | 5.4978 | 6.4141 | 7.3304 | 8.2467 | 1.3411 |
| 42 | 0.9161 | 1.8323 | 2.7484 | 3.6646 | 4.5807 | 5.4968 | 6.4130 | 7.3291 | 8.2452 | 1.3410 |
| 43 | 0.9160 | 1.8320 | 2.7479 | 3.6639 | 4.5799 | 5.4959 | 6.4118 | 7.3278 | 8.2438 | 1.3409 |
| 44 | 0.9158 | 1.8316 | 2.7475 | 3.6633 | 4.5791 | 5.4949 | 6.4107 | 7.3265 | 8.2424 | 1.3407 |
| 45 | 0.9157 | 1.8313 | 2.7470 | 3.6626 | 4.5783 | 5.4939 | 6.4096 | 7.3253 | 8.2409 | 1.3406 |
| 46 | 0.9155 | 1.8310 | 2.7465 | 3.6620 | 4.5775 | 5.4930 | 6.4085 | 7.3240 | 8.2395 | 1.3405 |
| 47 | 0.9153 | 1.8307 | 2.7460 | 3.6613 | 4.5767 | 5.4920 | 6.4074 | 7.3227 | 8.2380 | 1.3404 |
| 48 | 0.9152 | 1.8304 | 2.7455 | 3.6607 | 4.5759 | 5.4911 | 6.4062 | 7.3214 | 8.2366 | 1.3403 |
| 49 | 0.9150 | 1.8300 | 2.7450 | 3.6601 | 4.5751 | 5.4901 | 6.4051 | 7.3201 | 8.2351 | 1.3402 |
| 50 | 0.9149 | 1.8297 | 2.7446 | 3.6594 | 4.5743 | 5.4891 | 6.4040 | 7.3188 | 8.2337 | 1.3400 |
| 51 | 0.9147 | 1.8294 | 2.7441 | 3.6588 | 4.5735 | 5.4882 | 6.4029 | 7.3176 | 8.2322 | 1.3399 |
| 52 | 0.9145 | 1.8291 | 2.7436 | 3.6581 | 4.5727 | 5.4872 | 6.4017 | 7.3163 | 8.2308 | 1.3398 |
| 53 | 0.9144 | 1.8287 | 2.7431 | 3.6575 | 4.5719 | 5.4862 | 6.4006 | 7.3150 | 8.2293 | 1.3397 |
| 54 | 0.9142 | 1.8284 | 2.7426 | 3.6568 | 4.5710 | 5.4853 | 6.3995 | 7.3137 | 8.2279 | 1.3395 |
| 55 | 0.9140 | 1.8281 | 2.7421 | 3.6562 | 4.5702 | 5.4843 | 6.3983 | 7.3124 | 8.2264 | 1.3394 |
| 56 | 0.9139 | 1.8278 | 2.7417 | 3.6555 | 4.5694 | 5.4833 | 6.3972 | 7.3111 | 8.2250 | 1.3393 |
| 57 | 0.9137 | 1.8274 | 2.7412 | 3.6549 | 4.5686 | 5.4823 | 6.3961 | 7.3098 | 8.2235 | 1.3392 |
| 58 | 0.9136 | 1.8271 | 2.7407 | 3.6542 | 4.5678 | 5.4814 | 6.3949 | 7.3085 | 8.2221 | 1.3390 |
| 59 | 0.9134 | 1.8268 | 2.7402 | 3.6536 | 4.5670 | 5.4804 | 6.3938 | 7.3072 | 8.2206 | 1.3389 |
| 60 | 0.9132 | 1.8265 | 2.7397 | 3.6530 | 4.5662 | 5.4794 | 6.3927 | 7.3059 | 8.2192 | 1.3388 |



| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.2646 | 0.5292 | 0.7938 | 1.0584 | 1.3230 | 1.5875 | 1.8521 | 2.1167 | 2.3813 | 0.3859 | 00 |
| 0.2648 | 0.5297 | 0.7945 | 1.0594 | 1.3242 | 1.5890 | 1.8539 | 2.1187 | 2.3836 | 0.3863 | 01 |
| 0.2651 | 0.5302 | 0.7952 | 1.0603 | 1.3254 | 1.5905 | 1.8556 | 2.1206 | 2.3857 | 0.3867 | 02 |
| 0.2653 | 0.5307 | 0.7960 | 1.0613 | 1.3266 | 1.5920 | 1.8573 | 2.1226 | 2.3880 | 0.3871 | 03 |
| 0.2656 | 0.5311 | 0.7967 | 1.0623 | 1.3279 | 1.5934 | 1.8590 | 2.1246 | 2.3902 | 0.3875 | 04 |
| 0.2658 | 0.5316 | 0.7975 | 1.0633 | 1.3291 | 1.5949 | 1.8607 | 2.1266 | 2.3924 | 0.3878 | 05 |
| 0.2661 | 0.5321 | 0.7982 | 1.0642 | 1.3303 | 1.5964 | 1.8624 | 2.1285 | 2.3946 | 0.3882 | 06 |
| 0.2663 | 0.5326 | 0.7989 | 1.0652 | 1.3316 | 1.5979 | 1.8642 | 2.1305 | 2.3968 | 0.3886 | 07 |
| 0.2666 | 0.5331 | 0.7997 | 1.0662 | 1.3328 | 1.5994 | 1.8659 | 2.1325 | 2.3990 | 0.3890 | 08 |
| 0.2668 | 0.5336 | 0.8004 | 1.0672 | 1.3340 | 1.6008 | 1.8676 | 2.1344 | 2.4012 | 0.3894 | 09 |
| 0.2670 | 0.5341 | 0.8011 | 1.0682 | 1.3352 | 1.6023 | 1.8693 | 2.1364 | 2.4034 | 0.3898 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2673 | 0.5346 | 0.8019 | 1.0692 | 1.3365 | 1.6037 | 1.8710 | 2.1383 | 2.4056 | 0.3902 | 11 |
| 0.2675 | 0.5351 | 0.8026 | 1.0702 | 1.3377 | 1.6052 | 1.8728 | 2.1403 | 2.4078 | 0.3906 | 12 |
| 0.2678 | 0.5356 | 0.8033 | 1.0711 | 1.3389 | 1.6067 | 1.8745 | 2.1422 | 2.4100 | 0.3910 | 13 |
| 0.2680 | 0.5361 | 0.8041 | 1.0721 | 1.3401 | 1.6082 | 1.8762 | 2.1442 | 2.4123 | 0.3914 | 14 |
| 0.2683 | 0.5365 | 0.8048 | 1.0731 | 1.3414 | 1.6096 | 1.8779 | 2.1462 | 2.4145 | 0.3917 | 15 |
| 0.2685 | 0.5370 | 0.8056 | 1.0741 | 1.3426 | 1.6111 | 1.8796 | 2.1482 | 2.4167 | 0.3921 | 16 |
| 0.2688 | 0.5375 | 0.8063 | 1.0750 | 1.3438 | 1.6126 | 1.8813 | 2.1501 | 2.4189 | 0.3925 | 17 |
| 0.2690 | 0.5380 | 0.8070 | 1.0760 | 1.3450 | 1.6141 | 1.8831 | 2.1521 | 2.4211 | 0.3929 | 18 |
| 0.2693 | 0.5385 | 0.8078 | 1.0770 | 1.3463 | 1.6155 | 1.8848 | 2.1540 | 2.4233 | 0.3933 | 19 |
| 0.2695 | 0.5390 | 0.8085 | 1.0780 | 1.3475 | 1.6170 | 1.8865 | 2.1560 | 2.4255 | 0.3937 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2697 | 0.5395 | 0.8092 | 1.0790 | 1.3487 | 1.6184 | 1.8882 | 2.1579 | 2.4277 | 0.3941 | 21 |
| 0.2700 | 0.5400 | 0.8100 | 1.0800 | 1.3499 | 1.6199 | 1.8899 | 2.1599 | 2.4299 | 0.3945 | 22 |
| 0.2702 | 0.5405 | 0.8107 | 1.0809 | 1.3512 | 1.6214 | 1.8916 | 2.1618 | 2.4321 | 0.3949 | 23 |
| 0.2705 | 0.5409 | 0.8114 | 1.0819 | 1.3524 | 1.6228 | 1.8933 | 2.1638 | 2.4343 | 0.3953 | 24 |
| 0.2707 | 0.5414 | 0.8122 | 1.0829 | 1.3536 | 1.6243 | 1.8950 | 2.1658 | 2.4365 | 0.3957 | 25 |
| 0.2710 | 0.5419 | 0.8129 | 1.0838 | 1.3548 | 1.6258 | 1.8967 | 2.1677 | 2.4387 | 0.3960 | 26 |
| 0.2712 | 0.5424 | 0.8136 | 1.0848 | 1.3560 | 1.6273 | 1.8985 | 2.1697 | 2.4409 | 0.3964 | 27 |
| 0.2715 | 0.5429 | 0.8144 | 1.0858 | 1.3573 | 1.6287 | 1.9002 | 2.1710 | 2.4431 | 0.3968 | 28 |
| 0.2717 | 0.5434 | 0.8151 | 1.0868 | 1.3585 | 1.6302 | 1.9019 | 2.1736 | 2.4453 | 0.3972 | 29 |
| 0.2719 | 0.5439 | 0.8158 | 1.0878 | 1.3597 | 1.6315 | 1.9036 | 2.1755 | 2.4475 | 0.3976 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2722 | 0.5444 | 0.8165 | 1.0887 | 1.3609 | 1.6331 | 1.9053 | 2.1775 | 2.4496 | 0.3980 | 31 |
| 0.2724 | 0.5448 | 0.8173 | 1.0897 | 1.3621 | 1.6345 | 1.9070 | 2.1794 | 2.4518 | 0.3984 | 32 |
| 0.2727 | 0.5453 | 0.8180 | 1.0907 | 1.3634 | 1.6361 | 1.9087 | 2.1814 | 2.4540 | 0.3988 | 33 |
| 0.2729 | 0.5458 | 0.8187 | 1.0916 | 1.3646 | 1.6375 | 1.9104 | 2.1833 | 2.4562 | 0.3992 | 34 |
| 0.2732 | 0.5463 | 0.8195 | 1.0926 | 1.3658 | 1.6390 | 1.9121 | 2.1853 | 2.4584 | 0.3996 | 35 |
| 0.2734 | 0.5468 | 0.8202 | 1.0936 | 1.3670 | 1.6404 | 1.9138 | 2.1872 | 2.4606 | 0.3999 | 36 |
| 0.2736 | 0.5473 | 0.8209 | 1.0946 | 1.3682 | 1.6418 | 1.9155 | 2.1891 | 2.4628 | 0.4003 | 37 |
| 0.2739 | 0.5478 | 0.8216 | 1.0955 | 1.3694 | 1.6433 | 1.9172 | 2.1911 | 2.4650 | 0.4007 | 38 |
| 0.2741 | 0.5483 | 0.8224 | 1.0965 | 1.3706 | 1.6448 | 1.9189 | 2.1930 | 2.4672 | 0.4011 | 39 |
| 0.2744 | 0.5487 | 0.8231 | 1.0975 | 1.3719 | 1.6462 | 1.9206 | 2.1950 | 2.4693 | 0.4015 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2746 | 0.5492 | 0.8238 | 1.0984 | 1.3731 | 1.6477 | 1.9223 | 2.1969 | 2.4715 | 0.4019 | 41 |
| 0.2749 | 0.5497 | 0.8246 | 1.0994 | 1.3743 | 1.6491 | 1.9240 | 2.1988 | 2.4737 | 0.4023 | 42 |
| 0.2751 | 0.5502 | 0.8253 | 1.1004 | 1.3755 | 1.6506 | 1.9257 | 2.2008 | 2.4759 | 0.4027 | 43 |
| 0.2753 | 0.5507 | 0.8260 | 1.1014 | 1.3767 | 1.6520 | 1.9274 | 2.2027 | 2.4781 | 0.4031 | 44 |
| 0.2756 | 0.5512 | 0.8267 | 1.1023 | 1.3779 | 1.6535 | 1.9291 | 2.2046 | 2.4802 | 0.4035 | 45 |
| 0.2758 | 0.5516 | 0.8275 | 1.1033 | 1.3791 | 1.6549 | 1.9308 | 2.2066 | 2.4824 | 0.4039 | 46 |
| 0.2761 | 0.5521 | 0.8282 | 1.1043 | 1.3803 | 1.6564 | 1.9325 | 2.2085 | 2.4846 | 0.4042 | 47 |
| 0.2763 | 0.5526 | 0.8289 | 1.1052 | 1.3815 | 1.6579 | 1.9342 | 2.2105 | 2.4868 | 0.4046 | 48 |
| 0.2766 | 0.5531 | 0.8297 | 1.1062 | 1.3828 | 1.6593 | 1.9359 | 2.2124 | 2.4890 | 0.4050 | 49 |
| 0.2768 | 0.5536 | 0.8304 | 1.1072 | 1.3840 | 1.6607 | 1.9375 | 2.2143 | 2.4911 | 0.4054 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2770 | 0.5541 | 0.8311 | 1.1081 | 1.3852 | 1.6622 | 1.9392 | 2.2163 | 2.4933 | 0.4058 | 51 |
| 0.2773 | 0.5546 | 0.8318 | 1.1091 | 1.3864 | 1.6637 | 1.9409 | 2.2182 | 2.4955 | 0.4062 | 52 |
| 0.2775 | 0.5550 | 0.8326 | 1.1101 | 1.3876 | 1.6651 | 1.9426 | 2.2202 | 2.4977 | 0.4066 | 53 |
| 0.2778 | 0.5555 | 0.8333 | 1.1110 | 1.3888 | 1.6666 | 1.9443 | 2.2221 | 2.4998 | 0.4070 | 54 |
| 0.2780 | 0.5560 | 0.8340 | 1.1120 | 1.3900 | 1.6680 | 1.9460 | 2.2240 | 2.5020 | 0.4074 | 55 |
| 0.2782 | 0.5565 | 0.8347 | 1.1130 | 1.3912 | 1.6695 | 1.9477 | 2.2259 | 2.5042 | 0.4078 | 56 |
| 0.2785 | 0.5570 | 0.8354 | 1.1139 | 1.3924 | 1.6709 | 1.9494 | 2.2278 | 2.5063 | 0.4081 | 57 |
| 0.2787 | 0.5574 | 0.8362 | 1.1149 | 1.3936 | 1.6723 | 1.9510 | 2.2298 | 2.5085 | 0.4085 | 58 |
| 0.2790 | 0.5579 | 0.8369 | 1.1158 | 1.3948 | 1.6738 | 1.9527 | 2.2317 | 2.5107 | 0.4089 | 59 |
| 0.2792 | 0.5584 | 0.8376 | 1.1168 | 1.3960 | 1.6752 | 1.9544 | 2.2337 | 2.5129 | 0.4093 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9132 | 1.8265 | 2.7397 | 3.6530 | 4.5662 | 5.4794 | 6.3927 | 7.3059 | 8.2192 | 1.3388 |
| 01 | 0.9131 | 1.8262 | 2.7392 | 3.6523 | 4.5654 | 5.4785 | 6.3915 | 7.3046 | 8.2177 | 1.3387 |
| 02 | 0.9129 | 1.8258 | 2.7387 | 3.6517 | 4.5646 | 5.4775 | 6.3904 | 7.3033 | 8.2162 | 1.3385 |
| 03 | 0.9127 | 1.8255 | 2.7382 | 3.6510 | 4.5637 | 5.4765 | 6.3892 | 7.3020 | 8.2147 | 1.3384 |
| 04 | 0.9126 | 1.8252 | 2.7378 | 3.6503 | 4.5629 | 5.4755 | 6.3881 | 7.3007 | 8.2133 | 1.3383 |
| 05 | 0.9124 | 1.8248 | 2.7373 | 3.6497 | 4.5621 | 5.4745 | 6.3870 | 7.2994 | 8.2118 | 1.3382 |
| 06 | 0.9123 | 1.8245 | 2.7368 | 3.6490 | 4.5613 | 5.4736 | 6.3858 | 7.2981 | 8.2103 | 1.3381 |
| 07 | 0.9121 | 1.8242 | 2.7363 | 3.6484 | 4.5605 | 5.4726 | 6.3847 | 7.2968 | 8.2089 | 1.3379 |
| 08 | 0.9119 | 1.8239 | 2.7358 | 3.6477 | 4.5597 | 5.4716 | 6.3835 | 7.2955 | 8.2074 | 1.3378 |
| 09 | 0.9118 | 1.8235 | 2.7353 | 3.6471 | 4.5589 | 5.4706 | 6.3824 | 7.2942 | 8.2059 | 1.3377 |
| 10 | 0.9116 | 1.8232 | 2.7348 | 3.6464 | 4.5580 | 5.4696 | 6.3812 | 7.2929 | 8.2045 | 1.3376 |
| 11 | 0.9114 | 1.8229 | 2.7343 | 3.6458 | 4.5572 | 5.4687 | 6.3801 | 7.2915 | 8.2030 | 1.3375 |
| 12 | 0.9113 | 1.8226 | 2.7338 | 3.6451 | 4.5564 | 5.4677 | 6.3789 | 7.2902 | 8.2015 | 1.3373 |
| 13 | 0.9111 | 1.8222 | 2.7333 | 3.6445 | 4.5556 | 5.4667 | 6.3778 | 7.2889 | 8.2000 | 1.3372 |
| 14 | 0.9109 | 1.8219 | 2.7328 | 3.6438 | 4.5547 | 5.4657 | 6.3766 | 7.2876 | 8.1985 | 1.3371 |
| 15 | 0.9108 | 1.8216 | 2.7324 | 3.6431 | 4.5539 | 5.4647 | 6.3755 | 7.2863 | 8.1971 | 1.3370 |
| 16 | 0.9106 | 1.8212 | 2.7319 | 3.6425 | 4.5531 | 5.4637 | 6.3743 | 7.2850 | 8.1956 | 1.3368 |
| 17 | 0.9105 | 1.8209 | 2.7314 | 3.6418 | 4.5523 | 5.4627 | 6.3732 | 7.2836 | 8.1941 | 1.3367 |
| 18 | 0.9103 | 1.8206 | 2.7309 | 3.6412 | 4.5515 | 5.4617 | 6.3720 | 7.2823 | 8.1926 | 1.3366 |
| 19 | 0.9101 | 1.8203 | 2.7304 | 3.6405 | 4.5506 | 5.4608 | 6.3709 | 7.2810 | 8.1911 | 1.3365 |
| 20 | 0.9100 | 1.8199 | 2.7299 | 3.6398 | 4.5498 | 5.4598 | 6.3697 | 7.2797 | 8.1897 | 1.3364 |
| 21 | 0.9098 | 1.8196 | 2.7294 | 3.6392 | 4.5490 | 5.4588 | 6.3686 | 7.2784 | 8.1882 | 1.3362 |
| 22 | 0.9096 | 1.8193 | 2.7289 | 3.6385 | 4.5482 | 5.4578 | 6.3674 | 7.2770 | 8.1867 | 1.3361 |
| 23 | 0.9095 | 1.8189 | 2.7284 | 3.6379 | 4.5473 | 5.4568 | 6.3662 | 7.2757 | 8.1852 | 1.3360 |
| 24 | 0.9093 | 1.8186 | 2.7279 | 3.6372 | 4.5465 | 5.4558 | 6.3651 | 7.2744 | 8.1837 | 1.3359 |
| 25 | 0.9091 | 1.8183 | 2.7274 | 3.6365 | 4.5457 | 5.4548 | 6.3639 | 7.2731 | 8.1822 | 1.3358 |
| 26 | 0.9090 | 1.8179 | 2.7269 | 3.6359 | 4.5448 | 5.4538 | 6.3628 | 7.2717 | 8.1807 | 1.3357 |
| 27 | 0.9088 | 1.8176 | 2.7264 | 3.6352 | 4.5440 | 5.4528 | 6.3616 | 7.2704 | 8.1792 | 1.3355 |
| 28 | 0.9086 | 1.8173 | 2.7259 | 3.6345 | 4.5432 | 5.4518 | 6.3604 | 7.2691 | 8.1777 | 1.3354 |
| 29 | 0.9085 | 1.8169 | 2.7254 | 3.6339 | 4.5423 | 5.4508 | 6.3593 | 7.2678 | 8.1762 | 1.3353 |
| 30 | 0.9083 | 1.8166 | 2.7249 | 3.6332 | 4.5415 | 5.4498 | 6.3581 | 7.2664 | 8.1747 | 1.3352 |
| 31 | 0.9081 | 1.8163 | 2.7244 | 3.6325 | 4.5407 | 5.4488 | 6.3570 | 7.2651 | 8.1732 | 1.3350 |
| 32 | 0.9080 | 1.8159 | 2.7239 | 3.6319 | 4.5398 | 5.4478 | 6.3558 | 7.2637 | 8.1717 | 1.3349 |
| 33 | 0.9078 | 1.8156 | 2.7234 | 3.6312 | 4.5390 | 5.4468 | 6.3546 | 7.2624 | 8.1702 | 1.3348 |
| 34 | 0.9076 | 1.8153 | 2.7229 | 3.6305 | 4.5382 | 5.4458 | 6.3534 | 7.2611 | 8.1687 | 1.3347 |
| 35 | 0.9075 | 1.8149 | 2.7224 | 3.6299 | 4.5373 | 5.4448 | 6.3523 | 7.2597 | 8.1672 | 1.3346 |
| 36 | 0.9073 | 1.8146 | 2.7219 | 3.6292 | 4.5365 | 5.4438 | 6.3511 | 7.2584 | 8.1657 | 1.3344 |
| 37 | 0.9071 | 1.8143 | 2.7214 | 3.6285 | 4.5357 | 5.4428 | 6.3499 | 7.2571 | 8.1642 | 1.3343 |
| 38 | 0.9070 | 1.8139 | 2.7209 | 3.6279 | 4.5348 | 5.4418 | 6.3488 | 7.2557 | 8.1627 | 1.3342 |
| 39 | 0.9068 | 1.8136 | 2.7204 | 3.6272 | 4.5340 | 5.4408 | 6.3476 | 7.2544 | 8.1612 | 1.3341 |
| 40 | 0.9066 | 1.8133 | 2.7199 | 3.6265 | 4.5332 | 5.4398 | 6.3464 | 7.2530 | 8.1597 | 1.3339 |
| 41 | 0.9065 | 1.8129 | 2.7194 | 3.6258 | 4.5323 | 5.4388 | 6.3452 | 7.2517 | 8.1581 | 1.3338 |
| 42 | 0.9063 | 1.8126 | 2.7189 | 3.6252 | 4.5315 | 5.4378 | 6.3441 | 7.2503 | 8.1566 | 1.3337 |
| 43 | 0.9061 | 1.8122 | 2.7184 | 3.6245 | 4.5306 | 5.4367 | 6.3429 | 7.2490 | 8.1551 | 1.3336 |
| 44 | 0.9060 | 1.8119 | 2.7179 | 3.6238 | 4.5298 | 5.4357 | 6.3417 | 7.2476 | 8.1536 | 1.3335 |
| 45 | 0.9058 | 1.8116 | 2.7174 | 3.6231 | 4.5289 | 5.4347 | 6.3405 | 7.2463 | 8.1521 | 1.3333 |
| 46 | 0.9056 | 1.8112 | 2.7169 | 3.6225 | 4.5281 | 5.4337 | 6.3393 | 7.2449 | 8.1506 | 1.3332 |
| 47 | 0.9054 | 1.8109 | 2.7163 | 3.6218 | 4.5272 | 5.4327 | 6.3381 | 7.2436 | 8.1490 | 1.3331 |
| 48 | 0.9053 | 1.8106 | 2.7158 | 3.6211 | 4.5264 | 5.4317 | 6.3370 | 7.2422 | 8.1475 | 1.3330 |
| 49 | 0.9051 | 1.8102 | 2.7153 | 3.6204 | 4.5256 | 5.4307 | 6.3358 | 7.2409 | 8.1460 | 1.3329 |
| 50 | 0.9049 | 1.8099 | 2.7148 | 3.6198 | 4.5247 | 5.4297 | 6.3346 | 7.2395 | 8.1445 | 1.3327 |
| 51 | 0.9048 | 1.8095 | 2.7143 | 3.6191 | 4.5239 | 5.4286 | 6.3334 | 7.2382 | 8.1430 | 1.3326 |
| 52 | 0.9046 | 1.8092 | 2.7138 | 3.6184 | 4.5230 | 5.4276 | 6.3322 | 7.2368 | 8.1414 | 1.3325 |
| 53 | 0.9044 | 1.8089 | 2.7133 | 3.6177 | 4.5222 | 5.4266 | 6.3310 | 7.2355 | 8.1399 | 1.3324 |
| 54 | 0.9043 | 1.8085 | 2.7128 | 3.6171 | 4.5213 | 5.4256 | 6.3298 | 7.2341 | 8.1384 | 1.3323 |
| 55 | 0.9041 | 1.8082 | 2.7123 | 3.6164 | 4.5205 | 5.4246 | 6.3287 | 7.2327 | 8.1368 | 1.3321 |
| 56 | 0.9039 | 1.8078 | 2.7118 | 3.6157 | 4.5196 | 5.4235 | 6.3275 | 7.2314 | 8.1353 | 1.3320 |
| 57 | 0.9038 | 1.8075 | 2.7113 | 3.6150 | 4.5188 | 5.4225 | 6.3263 | 7.2300 | 8.1338 | 1.3319 |
| 58 | 0.9036 | 1.8072 | 2.7107 | 3.6143 | 4.5179 | 5.4215 | 6.3251 | 7.2287 | 8.1322 | 1.3318 |
| 59 | 0.9034 | 1.8068 | 2.7102 | 3.6137 | 4.5171 | 5.4205 | 6.3239 | 7.2273 | 8.1307 | 1.3316 |
| 60 | 0.9032 | 1.8065 | 2.7097 | 3.6130 | 4.5162 | 5.4195 | 6.3227 | 7.2259 | 8.1292 | 1.3315 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      | '  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.2792 | 0.5584 | 0.8376 | 1.1168 | 1.3960 | 1.6752 | 1.9544 | 2.2337 | 2.5129 | 0.4093 | 00 |
| 0.2794 | 0.5589 | 0.8383 | 1.1178 | 1.3972 | 1.6767 | 1.9561 | 2.2356 | 2.5150 | 0.4097 | 01 |
| 0.2797 | 0.5594 | 0.8391 | 1.1187 | 1.3984 | 1.6781 | 1.9578 | 2.2375 | 2.5172 | 0.4101 | 02 |
| 0.2799 | 0.5599 | 0.8398 | 1.1197 | 1.3996 | 1.6796 | 1.9595 | 2.2394 | 2.5193 | 0.4105 | 03 |
| 0.2802 | 0.5603 | 0.8405 | 1.1207 | 1.4008 | 1.6810 | 1.9612 | 2.2414 | 2.5215 | 0.4109 | 04 |
| 0.2804 | 0.5608 | 0.8412 | 1.1216 | 1.4020 | 1.6825 | 1.9629 | 2.2433 | 2.5237 | 0.4113 | 05 |
| 0.2806 | 0.5613 | 0.8419 | 1.1226 | 1.4032 | 1.6839 | 1.9645 | 2.2452 | 2.5258 | 0.4116 | 06 |
| 0.2809 | 0.5618 | 0.8427 | 1.1236 | 1.4044 | 1.6853 | 1.9662 | 2.2471 | 2.5280 | 0.4120 | 07 |
| 0.2811 | 0.5623 | 0.8434 | 1.1245 | 1.4056 | 1.6868 | 1.9679 | 2.2490 | 2.5302 | 0.4124 | 08 |
| 0.2814 | 0.5627 | 0.8441 | 1.1255 | 1.4068 | 1.6882 | 1.9696 | 2.2510 | 2.5323 | 0.4128 | 09 |
| 0.2816 | 0.5632 | 0.8448 | 1.1264 | 1.4080 | 1.6897 | 1.9713 | 2.2529 | 2.5345 | 0.4132 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2818 | 0.5637 | 0.8455 | 1.1274 | 1.4092 | 1.6911 | 1.9729 | 2.2548 | 2.5366 | 0.4136 | 11 |
| 0.2821 | 0.5642 | 0.8463 | 1.1284 | 1.4104 | 1.6925 | 1.9746 | 2.2567 | 2.5388 | 0.4140 | 12 |
| 0.2823 | 0.5647 | 0.8470 | 1.1293 | 1.4116 | 1.6940 | 1.9763 | 2.2586 | 2.5409 | 0.4144 | 13 |
| 0.2826 | 0.5651 | 0.8477 | 1.1303 | 1.4128 | 1.6954 | 1.9780 | 2.2606 | 2.5431 | 0.4148 | 14 |
| 0.2828 | 0.5656 | 0.8484 | 1.1312 | 1.4140 | 1.6969 | 1.9797 | 2.2625 | 2.5453 | 0.4151 | 15 |
| 0.2830 | 0.5661 | 0.8491 | 1.1322 | 1.4152 | 1.6983 | 1.9813 | 2.2644 | 2.5474 | 0.4155 | 16 |
| 0.2833 | 0.5666 | 0.8499 | 1.1332 | 1.4164 | 1.6997 | 1.9830 | 2.2663 | 2.5496 | 0.4159 | 17 |
| 0.2835 | 0.5670 | 0.8506 | 1.1341 | 1.4176 | 1.7011 | 1.9847 | 2.2682 | 2.5517 | 0.4163 | 18 |
| 0.2838 | 0.5675 | 0.8513 | 1.1351 | 1.4188 | 1.7026 | 1.9863 | 2.2701 | 2.5539 | 0.4167 | 19 |
| 0.2840 | 0.5680 | 0.8520 | 1.1360 | 1.4200 | 1.7040 | 1.9880 | 2.2720 | 2.5560 | 0.4171 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2842 | 0.5685 | 0.8527 | 1.1370 | 1.4212 | 1.7054 | 1.9907 | 2.2739 | 2.5582 | 0.4175 | 21 |
| 0.2845 | 0.5690 | 0.8534 | 1.1379 | 1.4224 | 1.7069 | 1.9914 | 2.2758 | 2.5603 | 0.4179 | 22 |
| 0.2847 | 0.5694 | 0.8542 | 1.1389 | 1.4236 | 1.7083 | 1.9930 | 2.2778 | 2.5625 | 0.4183 | 23 |
| 0.2850 | 0.5699 | 0.8549 | 1.1398 | 1.4248 | 1.7098 | 1.9947 | 2.2797 | 2.5646 | 0.4186 | 24 |
| 0.2852 | 0.5704 | 0.8556 | 1.1408 | 1.4260 | 1.7112 | 1.9964 | 2.2816 | 2.5668 | 0.4190 | 25 |
| 0.2854 | 0.5709 | 0.8563 | 1.1417 | 1.4272 | 1.7126 | 1.9980 | 2.2834 | 2.5689 | 0.4194 | 26 |
| 0.2857 | 0.5713 | 0.8570 | 1.1427 | 1.4284 | 1.7140 | 1.9997 | 2.2854 | 2.5710 | 0.4198 | 27 |
| 0.2859 | 0.5718 | 0.8577 | 1.1436 | 1.4296 | 1.7155 | 2.0014 | 2.2873 | 2.5732 | 0.4202 | 28 |
| 0.2861 | 0.5723 | 0.8584 | 1.1446 | 1.4307 | 1.7169 | 2.0030 | 2.2892 | 2.5753 | 0.4208 | 29 |
| 0.2864 | 0.5728 | 0.8592 | 1.1456 | 1.4319 | 1.7183 | 2.0047 | 2.2911 | 2.5775 | 0.4210 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2866 | 0.5732 | 0.8599 | 1.1465 | 1.4331 | 1.7197 | 2.0063 | 2.2930 | 2.5796 | 0.4214 | 31 |
| 0.2869 | 0.5737 | 0.8606 | 1.1474 | 1.4343 | 1.7212 | 2.0080 | 2.2949 | 2.5818 | 0.4217 | 32 |
| 0.2871 | 0.5742 | 0.8613 | 1.1484 | 1.4355 | 1.7226 | 2.0097 | 2.2968 | 2.5839 | 0.4221 | 33 |
| 0.2873 | 0.5747 | 0.8620 | 1.1494 | 1.4367 | 1.7240 | 2.0114 | 2.2987 | 2.5861 | 0.4225 | 34 |
| 0.2876 | 0.5752 | 0.8627 | 1.1503 | 1.4379 | 1.7255 | 2.0131 | 2.3006 | 2.5882 | 0.4229 | 35 |
| 0.2878 | 0.5756 | 0.8634 | 1.1512 | 1.4390 | 1.7269 | 2.0147 | 2.3025 | 2.5903 | 0.4233 | 36 |
| 0.2880 | 0.5761 | 0.8641 | 1.1522 | 1.4402 | 1.7283 | 2.0163 | 2.3044 | 2.5924 | 0.4237 | 37 |
| 0.2883 | 0.5766 | 0.8649 | 1.1532 | 1.4414 | 1.7297 | 2.0180 | 2.3063 | 2.5946 | 0.4241 | 38 |
| 0.2885 | 0.5770 | 0.8656 | 1.1541 | 1.4426 | 1.7311 | 2.0196 | 2.3082 | 2.5967 | 0.4245 | 39 |
| 0.2888 | 0.5775 | 0.8663 | 1.1550 | 1.4438 | 1.7326 | 2.0213 | 2.3101 | 2.5988 | 0.4249 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2890 | 0.5780 | 0.8670 | 1.1560 | 1.4450 | 1.7340 | 2.0230 | 2.3120 | 2.6010 | 0.4252 | 41 |
| 0.2892 | 0.5785 | 0.8677 | 1.1569 | 1.4462 | 1.7354 | 2.0246 | 2.3139 | 2.6031 | 0.4256 | 42 |
| 0.2895 | 0.5789 | 0.8684 | 1.1579 | 1.4474 | 1.7368 | 2.0263 | 2.3158 | 2.6052 | 0.4260 | 43 |
| 0.2897 | 0.5794 | 0.8691 | 1.1588 | 1.4485 | 1.7383 | 2.0280 | 2.3177 | 2.6074 | 0.4264 | 44 |
| 0.2899 | 0.5799 | 0.8698 | 1.1598 | 1.4497 | 1.7397 | 2.0296 | 2.3196 | 2.6095 | 0.4268 | 45 |
| 0.2902 | 0.5804 | 0.8705 | 1.1607 | 1.4509 | 1.7411 | 2.0313 | 2.3215 | 2.6116 | 0.4272 | 46 |
| 0.2904 | 0.5808 | 0.8713 | 1.1617 | 1.4521 | 1.7425 | 2.0329 | 2.3233 | 2.6138 | 0.4276 | 47 |
| 0.2907 | 0.5813 | 0.8720 | 1.1626 | 1.4533 | 1.7439 | 2.0345 | 2.3252 | 2.6159 | 0.4280 | 48 |
| 0.2909 | 0.5818 | 0.8727 | 1.1636 | 1.4544 | 1.7453 | 2.0362 | 2.3271 | 2.6180 | 0.4283 | 49 |
| 0.2911 | 0.5823 | 0.8734 | 1.1645 | 1.4556 | 1.7468 | 2.0379 | 2.3290 | 2.6202 | 0.4287 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.2914 | 0.5827 | 0.8741 | 1.1654 | 1.4568 | 1.7482 | 2.0395 | 2.3309 | 2.6223 | 0.4291 | 51 |
| 0.2916 | 0.5832 | 0.8748 | 1.1664 | 1.4580 | 1.7496 | 2.0412 | 2.3328 | 2.6244 | 0.4295 | 52 |
| 0.2918 | 0.5837 | 0.8755 | 1.1673 | 1.4591 | 1.7510 | 2.0428 | 2.3346 | 2.6265 | 0.4299 | 53 |
| 0.2921 | 0.5841 | 0.8762 | 1.1683 | 1.4603 | 1.7524 | 2.0445 | 2.3365 | 2.6286 | 0.4303 | 54 |
| 0.2923 | 0.5846 | 0.8769 | 1.1692 | 1.4615 | 1.7538 | 2.0461 | 2.3384 | 2.6307 | 0.4307 | 55 |
| 0.2925 | 0.5851 | 0.8776 | 1.1702 | 1.4627 | 1.7552 | 2.0478 | 2.3403 | 2.6329 | 0.4311 | 56 |
| 0.2928 | 0.5856 | 0.8783 | 1.1711 | 1.4639 | 1.7567 | 2.0495 | 2.3422 | 2.6350 | 0.4315 | 57 |
| 0.2930 | 0.5860 | 0.8790 | 1.1720 | 1.4651 | 1.7581 | 2.0511 | 2.3441 | 2.6371 | 0.4318 | 58 |
| 0.2932 | 0.5865 | 0.8797 | 1.1730 | 1.4662 | 1.7595 | 2.0527 | 2.3460 | 2.6392 | 0.4322 | 59 |
| 0.2935 | 0.5870 | 0.8804 | 1.1739 | 1.4674 | 1.7609 | 2.0544 | 2.3478 | 2.6413 | 0.4326 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | a      |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.9032 | 1.8065 | 2.7097 | 3.6130 | 4.5162 | 5.4195 | 6.3227 | 7.2259 | 8.1292 | 1.3315 |
| 01 | 0.9031 | 1.8061 | 2.7092 | 3.6123 | 4.5154 | 5.4184 | 6.3215 | 7.2246 | 8.1276 | 1.3314 |
| 02 | 0.9029 | 1.8058 | 2.7087 | 3.6116 | 4.5145 | 5.4174 | 6.3203 | 7.2232 | 8.1261 | 1.3312 |
| 03 | 0.9027 | 1.8055 | 2.7082 | 3.6109 | 4.5136 | 5.4164 | 6.3191 | 7.2218 | 8.1246 | 1.3311 |
| 04 | 0.9026 | 1.8051 | 2.7077 | 3.6102 | 4.5128 | 5.4153 | 6.3179 | 7.2205 | 8.1230 | 1.3310 |
| 05 | 0.9024 | 1.8048 | 2.7072 | 3.6095 | 4.5119 | 5.4143 | 6.3167 | 7.2191 | 8.1215 | 1.3309 |
| 06 | 0.9022 | 1.8044 | 2.7066 | 3.6089 | 4.5111 | 5.4133 | 6.3155 | 7.2177 | 8.1199 | 1.3308 |
| 07 | 0.9020 | 1.8041 | 2.7061 | 3.6082 | 4.5102 | 5.4123 | 6.3143 | 7.2163 | 8.1184 | 1.3306 |
| 08 | 0.9019 | 1.8037 | 2.7056 | 3.6075 | 4.5094 | 5.4112 | 6.3131 | 7.2150 | 8.1168 | 1.3305 |
| 09 | 0.9017 | 1.8034 | 2.7051 | 3.6068 | 4.5085 | 5.4102 | 6.3119 | 7.2136 | 8.1153 | 1.3304 |
| 10 | 0.9015 | 1.8031 | 2.7046 | 3.6061 | 4.5076 | 5.4092 | 6.3107 | 7.2122 | 8.1138 | 1.3302 |
| 11 | 0.9014 | 1.8027 | 2.7041 | 3.6054 | 4.5068 | 5.4081 | 6.3095 | 7.2108 | 8.1122 | 1.3301 |
| 12 | 0.9012 | 1.8024 | 2.7035 | 3.6047 | 4.5059 | 5.4071 | 6.3083 | 7.2095 | 8.1106 | 1.3300 |
| 13 | 0.9010 | 1.8020 | 2.7030 | 3.6040 | 4.5050 | 5.4061 | 6.3071 | 7.2081 | 8.1091 | 1.3298 |
| 14 | 0.9008 | 1.8017 | 2.7025 | 3.6033 | 4.5042 | 5.4050 | 6.3059 | 7.2067 | 8.1075 | 1.3297 |
| 15 | 0.9007 | 1.8013 | 2.7020 | 3.6027 | 4.5033 | 5.4040 | 6.3046 | 7.2053 | 8.1060 | 1.3296 |
| 16 | 0.9005 | 1.8010 | 2.7015 | 3.6020 | 4.5025 | 5.4029 | 6.3034 | 7.2039 | 8.1044 | 1.3294 |
| 17 | 0.9003 | 1.8006 | 2.7010 | 3.6013 | 4.5016 | 5.4019 | 6.3022 | 7.2025 | 8.1029 | 1.3293 |
| 18 | 0.9001 | 1.8003 | 2.7004 | 3.6006 | 4.5007 | 5.4009 | 6.3010 | 7.2012 | 8.1013 | 1.3292 |
| 19 | 0.9000 | 1.7999 | 2.6999 | 3.5999 | 4.4999 | 5.3998 | 6.2998 | 7.1998 | 8.0998 | 1.3291 |
| 20 | 0.8998 | 1.7996 | 2.6994 | 3.5992 | 4.4990 | 5.3988 | 6.2986 | 7.1984 | 8.0982 | 1.3289 |
| 21 | 0.8996 | 1.7993 | 2.6989 | 3.5985 | 4.4981 | 5.3978 | 6.2974 | 7.1970 | 8.0966 | 1.3288 |
| 22 | 0.8995 | 1.7989 | 2.6984 | 3.5978 | 4.4973 | 5.3967 | 6.2962 | 7.1956 | 8.0951 | 1.3287 |
| 23 | 0.8993 | 1.7986 | 2.6978 | 3.5971 | 4.4964 | 5.3957 | 6.2949 | 7.1942 | 8.0935 | 1.3285 |
| 24 | 0.8991 | 1.7982 | 2.6973 | 3.5964 | 4.4955 | 5.3946 | 6.2937 | 7.1928 | 8.0919 | 1.3284 |
| 25 | 0.8989 | 1.7979 | 2.6968 | 3.5957 | 4.4946 | 5.3936 | 6.2925 | 7.1914 | 8.0904 | 1.3283 |
| 26 | 0.8988 | 1.7975 | 2.6963 | 3.5950 | 4.4938 | 5.3925 | 6.2913 | 7.1900 | 8.0888 | 1.3281 |
| 27 | 0.8986 | 1.7972 | 2.6957 | 3.5943 | 4.4929 | 5.3915 | 6.2901 | 7.1886 | 8.0872 | 1.3280 |
| 28 | 0.8984 | 1.7968 | 2.6952 | 3.5936 | 4.4920 | 5.3904 | 6.2888 | 7.1873 | 8.0857 | 1.3279 |
| 29 | 0.8982 | 1.7965 | 2.6947 | 3.5929 | 4.4912 | 5.3894 | 6.2876 | 7.1859 | 8.0841 | 1.3278 |
| 30 | 0.8981 | 1.7961 | 2.6942 | 3.5922 | 4.4903 | 5.3884 | 6.2864 | 7.1845 | 8.0825 | 1.3276 |
| 31 | 0.8979 | 1.7958 | 2.6937 | 3.5915 | 4.4894 | 5.3873 | 6.2852 | 7.1831 | 8.0810 | 1.3275 |
| 32 | 0.8977 | 1.7954 | 2.6931 | 3.5908 | 4.4885 | 5.3862 | 6.2840 | 7.1817 | 8.0794 | 1.3274 |
| 33 | 0.8975 | 1.7951 | 2.6926 | 3.5901 | 4.4877 | 5.3852 | 6.2827 | 7.1803 | 8.0778 | 1.3272 |
| 34 | 0.8974 | 1.7947 | 2.6921 | 3.5894 | 4.4868 | 5.3841 | 6.2815 | 7.1789 | 8.0762 | 1.3271 |
| 35 | 0.8972 | 1.7944 | 2.6915 | 3.5887 | 4.4859 | 5.3831 | 6.2803 | 7.1775 | 8.0746 | 1.3269 |
| 36 | 0.8970 | 1.7940 | 2.6910 | 3.5880 | 4.4850 | 5.3820 | 6.2790 | 7.1760 | 8.0731 | 1.3268 |
| 37 | 0.8968 | 1.7937 | 2.6905 | 3.5873 | 4.4842 | 5.3810 | 6.2778 | 7.1746 | 8.0715 | 1.3267 |
| 38 | 0.8967 | 1.7933 | 2.6900 | 3.5866 | 4.4833 | 5.3799 | 6.2766 | 7.1732 | 8.0699 | 1.3265 |
| 39 | 0.8965 | 1.7930 | 2.6894 | 3.5859 | 4.4824 | 5.3789 | 6.2754 | 7.1718 | 8.0683 | 1.3264 |
| 40 | 0.8963 | 1.7926 | 2.6889 | 3.5852 | 4.4815 | 5.3778 | 6.2741 | 7.1704 | 8.0667 | 1.3263 |
| 41 | 0.8961 | 1.7923 | 2.6884 | 3.5845 | 4.4806 | 5.3768 | 6.2729 | 7.1690 | 8.0651 | 1.3262 |
| 42 | 0.8960 | 1.7919 | 2.6879 | 3.5838 | 4.4798 | 5.3757 | 6.2717 | 7.1676 | 8.0636 | 1.3260 |
| 43 | 0.8958 | 1.7915 | 2.6873 | 3.5831 | 4.4789 | 5.3746 | 6.2704 | 7.1662 | 8.0620 | 1.3259 |
| 44 | 0.8956 | 1.7912 | 2.6868 | 3.5824 | 4.4780 | 5.3736 | 6.2692 | 7.1648 | 8.0604 | 1.3258 |
| 45 | 0.8954 | 1.7908 | 2.6863 | 3.5817 | 4.4771 | 5.3725 | 6.2679 | 7.1634 | 8.0588 | 1.3257 |
| 46 | 0.8952 | 1.7905 | 2.6857 | 3.5810 | 4.4762 | 5.3715 | 6.2667 | 7.1619 | 8.0572 | 1.3255 |
| 47 | 0.8951 | 1.7901 | 2.6852 | 3.5803 | 4.4753 | 5.3704 | 6.2655 | 7.1605 | 8.0556 | 1.3254 |
| 48 | 0.8949 | 1.7898 | 2.6847 | 3.5796 | 4.4744 | 5.3693 | 6.2642 | 7.1591 | 8.0540 | 1.3253 |
| 49 | 0.8947 | 1.7894 | 2.6841 | 3.5789 | 4.4736 | 5.3683 | 6.2630 | 7.1577 | 8.0524 | 1.3251 |
| 50 | 0.8945 | 1.7891 | 2.6836 | 3.5781 | 4.4727 | 5.3672 | 6.2618 | 7.1563 | 8.0508 | 1.3250 |
| 51 | 0.8944 | 1.7887 | 2.6831 | 3.5774 | 4.4718 | 5.3661 | 6.2605 | 7.1549 | 8.0492 | 1.3249 |
| 52 | 0.8942 | 1.7884 | 2.6825 | 3.5767 | 4.4709 | 5.3651 | 6.2593 | 7.1534 | 8.0476 | 1.3247 |
| 53 | 0.8940 | 1.7880 | 2.6820 | 3.5760 | 4.4700 | 5.3640 | 6.2580 | 7.1520 | 8.0460 | 1.3246 |
| 54 | 0.8938 | 1.7876 | 2.6815 | 3.5753 | 4.4691 | 5.3629 | 6.2568 | 7.1506 | 8.0444 | 1.3245 |
| 55 | 0.8936 | 1.7873 | 2.6809 | 3.5746 | 4.4682 | 5.3619 | 6.2555 | 7.1492 | 8.0428 | 1.3243 |
| 56 | 0.8935 | 1.7869 | 2.6804 | 3.5739 | 4.4673 | 5.3608 | 6.2543 | 7.1477 | 8.0412 | 1.3242 |
| 57 | 0.8933 | 1.7866 | 2.6799 | 3.5732 | 4.4664 | 5.3597 | 6.2530 | 7.1463 | 8.0396 | 1.3241 |
| 58 | 0.8931 | 1.7862 | 2.6793 | 3.5724 | 4.4656 | 5.3587 | 6.2518 | 7.1449 | 8.0380 | 1.3239 |
| 59 | 0.8929 | 1.7859 | 2.6788 | 3.5717 | 4.4647 | 5.3576 | 6.2505 | 7.1435 | 8.0364 | 1.3238 |
| 60 | 0.8928 | 1.7855 | 2.6783 | 3.5710 | 4.4638 | 5.3565 | 6.2493 | 7.1420 | 8.0348 | 1.3237 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.2935 | 0.5870 | 0.8804 | 1.1739 | 1.4674 | 1.7609 | 2.0544 | 2.3478 | 2.6413 | 0.4326 | 00 |
| 0.2937 | 0.5874 | 0.8811 | 1.1749 | 1.4686 | 1.7623 | 2.0560 | 2.3497 | 2.6434 | 0.4330 | 01 |
| 0.2940 | 0.5879 | 0.8819 | 1.1758 | 1.4698 | 1.7637 | 2.0577 | 2.3516 | 2.6456 | 0.4334 | 02 |
| 0.2942 | 0.5884 | 0.8826 | 1.1768 | 1.4709 | 1.7651 | 2.0593 | 2.3535 | 2.6477 | 0.4338 | 03 |
| 0.2944 | 0.5888 | 0.8833 | 1.1777 | 1.4721 | 1.7665 | 2.0609 | 2.3554 | 2.6498 | 0.4342 | 04 |
| 0.2947 | 0.5893 | 0.8840 | 1.1786 | 1.4733 | 1.7679 | 2.0626 | 2.3573 | 2.6519 | 0.4346 | 05 |
| 0.2949 | 0.5898 | 0.8847 | 1.1796 | 1.4744 | 1.7693 | 2.0642 | 2.3591 | 2.6540 | 0.4349 | 06 |
| 0.2951 | 0.5902 | 0.8854 | 1.1805 | 1.4756 | 1.7707 | 2.0659 | 2.3610 | 2.6561 | 0.4353 | 07 |
| 0.2954 | 0.5907 | 0.8861 | 1.1814 | 1.4768 | 1.7721 | 2.0675 | 2.3629 | 2.6582 | 0.4357 | 08 |
| 0.2956 | 0.5912 | 0.8868 | 1.1824 | 1.4780 | 1.7735 | 2.0691 | 2.3647 | 2.6603 | 0.4361 | 09 |
| 0.2958 | 0.5917 | 0.8875 | 1.1833 | 1.4791 | 1.7750 | 2.0708 | 2.3666 | 2.6625 | 0.4365 | 10 |
| 0.2961 | 0.5921 | 0.8882 | 1.1842 | 1.4803 | 1.7764 | 2.0724 | 2.3685 | 2.6645 | 0.4369 | 11 |
| 0.2963 | 0.5926 | 0.8889 | 1.1852 | 1.4815 | 1.7778 | 2.0740 | 2.3703 | 2.6666 | 0.4373 | 12 |
| 0.2965 | 0.5931 | 0.8896 | 1.1861 | 1.4826 | 1.7792 | 2.0757 | 2.3722 | 2.6688 | 0.4377 | 13 |
| 0.2968 | 0.5935 | 0.8903 | 1.1870 | 1.4838 | 1.7806 | 2.0773 | 2.3741 | 2.6709 | 0.4380 | 14 |
| 0.2970 | 0.5940 | 0.8910 | 1.1880 | 1.4850 | 1.7820 | 2.0790 | 2.3760 | 2.6730 | 0.4384 | 15 |
| 0.2972 | 0.5945 | 0.8917 | 1.1889 | 1.4861 | 1.7834 | 2.0806 | 2.3778 | 2.6751 | 0.4388 | 16 |
| 0.2975 | 0.5949 | 0.8924 | 1.1898 | 1.4873 | 1.7848 | 2.0822 | 2.3797 | 2.6771 | 0.4392 | 17 |
| 0.2977 | 0.5954 | 0.8931 | 1.1908 | 1.4885 | 1.7862 | 2.0838 | 2.3815 | 2.6792 | 0.4396 | 18 |
| 0.2979 | 0.5959 | 0.8938 | 1.1917 | 1.4896 | 1.7876 | 2.0855 | 2.3834 | 2.6813 | 0.4400 | 19 |
| 0.2982 | 0.5963 | 0.8945 | 1.1926 | 1.4908 | 1.7890 | 2.0871 | 2.3853 | 2.6834 | 0.4404 | 20 |
| 0.2984 | 0.5968 | 0.8952 | 1.1936 | 1.4920 | 1.7904 | 2.0887 | 2.3871 | 2.6855 | 0.4407 | 21 |
| 0.2986 | 0.5973 | 0.8959 | 1.1945 | 1.4931 | 1.7918 | 2.0904 | 2.3890 | 2.6876 | 0.4411 | 22 |
| 0.2989 | 0.5977 | 0.8966 | 1.1954 | 1.4943 | 1.7932 | 2.0920 | 2.3909 | 2.6897 | 0.4415 | 23 |
| 0.2991 | 0.5982 | 0.8973 | 1.1964 | 1.4955 | 1.7946 | 2.0936 | 2.3927 | 2.6918 | 0.4419 | 24 |
| 0.2993 | 0.5987 | 0.8980 | 1.1973 | 1.4966 | 1.7960 | 2.0953 | 2.3946 | 2.6939 | 0.4423 | 25 |
| 0.2996 | 0.5991 | 0.8987 | 1.1982 | 1.4978 | 1.7974 | 2.0969 | 2.3965 | 2.6960 | 0.4427 | 26 |
| 0.2998 | 0.5996 | 0.8994 | 1.1992 | 1.4989 | 1.7987 | 2.0985 | 2.3983 | 2.6981 | 0.4431 | 27 |
| 0.3000 | 0.6000 | 0.9001 | 1.2001 | 1.5001 | 1.8001 | 2.1001 | 2.4002 | 2.7002 | 0.4435 | 28 |
| 0.3003 | 0.6005 | 0.9008 | 1.2010 | 1.5013 | 1.8015 | 2.1018 | 2.4020 | 2.7023 | 0.4438 | 29 |
| 0.3005 | 0.6010 | 0.9015 | 1.2020 | 1.5024 | 1.8029 | 2.1034 | 2.4039 | 2.7044 | 0.4442 | 30 |
| 0.3007 | 0.6014 | 0.9022 | 1.2029 | 1.5036 | 1.8043 | 2.1050 | 2.4058 | 2.7065 | 0.4446 | 31 |
| 0.3009 | 0.6019 | 0.9028 | 1.2038 | 1.5047 | 1.8057 | 2.1066 | 2.4076 | 2.7085 | 0.4450 | 32 |
| 0.3012 | 0.6024 | 0.9035 | 1.2047 | 1.5059 | 1.8071 | 2.1083 | 2.4094 | 2.7106 | 0.4454 | 33 |
| 0.3014 | 0.6028 | 0.9042 | 1.2056 | 1.5071 | 1.8085 | 2.1099 | 2.4113 | 2.7127 | 0.4458 | 34 |
| 0.3016 | 0.6033 | 0.9049 | 1.2066 | 1.5082 | 1.8099 | 2.1115 | 2.4132 | 2.7148 | 0.4462 | 35 |
| 0.3019 | 0.6038 | 0.9056 | 1.2075 | 1.5094 | 1.8113 | 2.1132 | 2.4150 | 2.7169 | 0.4466 | 36 |
| 0.3021 | 0.6042 | 0.9063 | 1.2084 | 1.5105 | 1.8127 | 2.1148 | 2.4169 | 2.7190 | 0.4469 | 37 |
| 0.3023 | 0.6047 | 0.9070 | 1.2094 | 1.5117 | 1.8140 | 2.1164 | 2.4187 | 2.7211 | 0.4473 | 38 |
| 0.3026 | 0.6051 | 0.9077 | 1.2103 | 1.5128 | 1.8154 | 2.1180 | 2.4206 | 2.7231 | 0.4477 | 39 |
| 0.3028 | 0.6056 | 0.9084 | 1.2112 | 1.5140 | 1.8168 | 2.1196 | 2.4214 | 2.7252 | 0.4481 | 40 |
| 0.3030 | 0.6061 | 0.9091 | 1.2121 | 1.5152 | 1.8182 | 2.1212 | 2.4242 | 2.7273 | 0.4485 | 41 |
| 0.3033 | 0.6065 | 0.9098 | 1.2130 | 1.5163 | 1.8196 | 2.1228 | 2.4261 | 2.7294 | 0.4489 | 42 |
| 0.3035 | 0.6070 | 0.9105 | 1.2140 | 1.5175 | 1.8210 | 2.1245 | 2.4280 | 2.7315 | 0.4493 | 43 |
| 0.3037 | 0.6074 | 0.9112 | 1.2149 | 1.5186 | 1.8223 | 2.1261 | 2.4298 | 2.7335 | 0.4496 | 44 |
| 0.3040 | 0.6079 | 0.9119 | 1.2158 | 1.5198 | 1.8237 | 2.1277 | 2.4316 | 2.7356 | 0.4500 | 45 |
| 0.3042 | 0.6084 | 0.9125 | 1.2167 | 1.5209 | 1.8251 | 2.1293 | 2.4334 | 2.7376 | 0.4504 | 46 |
| 0.3044 | 0.6088 | 0.9132 | 1.2176 | 1.5221 | 1.8265 | 2.1309 | 2.4353 | 2.7397 | 0.4508 | 47 |
| 0.3046 | 0.6093 | 0.9139 | 1.2186 | 1.5232 | 1.8279 | 2.1325 | 2.4372 | 2.7418 | 0.4512 | 48 |
| 0.3049 | 0.6098 | 0.9146 | 1.2195 | 1.5244 | 1.8293 | 2.1341 | 2.4390 | 2.7439 | 0.4516 | 49 |
| 0.3051 | 0.6102 | 0.9153 | 1.2204 | 1.5255 | 1.8306 | 2.1357 | 2.4408 | 2.7459 | 0.4520 | 50 |
| 0.3053 | 0.6107 | 0.9160 | 1.2214 | 1.5267 | 1.8320 | 2.1374 | 2.4427 | 2.7480 | 0.4524 | 51 |
| 0.3056 | 0.6111 | 0.9167 | 1.2223 | 1.5278 | 1.8334 | 2.1390 | 2.4446 | 2.7501 | 0.4527 | 52 |
| 0.3058 | 0.6116 | 0.9174 | 1.2232 | 1.5290 | 1.8348 | 2.1406 | 2.4464 | 2.7521 | 0.4531 | 53 |
| 0.3060 | 0.6120 | 0.9181 | 1.2241 | 1.5301 | 1.8361 | 2.1422 | 2.4482 | 2.7542 | 0.4535 | 54 |
| 0.3063 | 0.6125 | 0.9188 | 1.2250 | 1.5313 | 1.8375 | 2.1438 | 2.4500 | 2.7563 | 0.4539 | 55 |
| 0.3065 | 0.6130 | 0.9194 | 1.2259 | 1.5324 | 1.8389 | 2.1454 | 2.4518 | 2.7583 | 0.4543 | 56 |
| 0.3067 | 0.6134 | 0.9201 | 1.2268 | 1.5336 | 1.8403 | 2.1470 | 2.4537 | 2.7604 | 0.4547 | 57 |
| 0.3069 | 0.6139 | 0.9208 | 1.2278 | 1.5347 | 1.8416 | 2.1486 | 2.4555 | 2.7625 | 0.4551 | 58 |
| 0.3072 | 0.6143 | 0.9215 | 1.2287 | 1.5358 | 1.8430 | 2.1502 | 2.4574 | 2.7645 | 0.4555 | 59 |
| 0.3074 | 0.6148 | 0.9222 | 1.2296 | 1.5370 | 1.8444 | 2.1518 | 2.4592 | 2.7666 | 0.4558 | 60 |

|    | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10     |
|----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 00 | 0.8928 | 1.7855 | 2.6783 | 3.5710 | 4.4638 | 5.3565 | 6.2493 | 7.1420 | 8.0348 | 1.3237 |
| 01 | 0.8926 | 1.7851 | 2.6777 | 3.5703 | 4.4629 | 5.3554 | 6.2480 | 7.1406 | 8.0332 | 1.3236 |
| 02 | 0.8924 | 1.7848 | 2.6772 | 3.5696 | 4.4620 | 5.3544 | 6.2468 | 7.1392 | 8.0316 | 1.3234 |
| 03 | 0.8922 | 1.7844 | 2.6766 | 3.5689 | 4.4611 | 5.3533 | 6.2455 | 7.1377 | 8.0299 | 1.3233 |
| 04 | 0.8920 | 1.7841 | 2.6761 | 3.5681 | 4.4602 | 5.3522 | 6.2443 | 7.1363 | 8.0283 | 1.3232 |
| 05 | 0.8919 | 1.7837 | 2.6756 | 3.5674 | 4.4593 | 5.3511 | 6.2430 | 7.1349 | 8.0267 | 1.3230 |
| 06 | 0.8917 | 1.7834 | 2.6750 | 3.5667 | 4.4584 | 5.3501 | 6.2417 | 7.1334 | 8.0251 | 1.3229 |
| 07 | 0.8915 | 1.7830 | 2.6745 | 3.5660 | 4.4575 | 5.3490 | 6.2405 | 7.1320 | 8.0235 | 1.3228 |
| 08 | 0.8913 | 1.7826 | 2.6740 | 3.5653 | 4.4566 | 5.3479 | 6.2392 | 7.1305 | 8.0219 | 1.3226 |
| 09 | 0.8911 | 1.7823 | 2.6734 | 3.5646 | 4.4557 | 5.3468 | 6.2380 | 7.1291 | 8.0203 | 1.3225 |
| 10 | 0.8910 | 1.7819 | 2.6729 | 3.5638 | 4.4548 | 5.3458 | 6.2367 | 7.1277 | 8.0186 | 1.3224 |
| 11 | 0.8908 | 1.7816 | 2.6723 | 3.5631 | 4.4539 | 5.3447 | 6.2354 | 7.1262 | 8.0170 | 1.3222 |
| 12 | 0.8906 | 1.7812 | 2.6718 | 3.5624 | 4.4530 | 5.3436 | 6.2342 | 7.1248 | 8.0154 | 1.3221 |
| 13 | 0.8904 | 1.7808 | 2.6712 | 3.5617 | 4.4521 | 5.3425 | 6.2329 | 7.1233 | 8.0137 | 1.3220 |
| 14 | 0.8902 | 1.7805 | 2.6707 | 3.5609 | 4.4512 | 5.3414 | 6.2316 | 7.1219 | 8.0121 | 1.3218 |
| 15 | 0.8901 | 1.7801 | 2.6702 | 3.5602 | 4.4503 | 5.3403 | 6.2304 | 7.1204 | 8.0105 | 1.3217 |
| 16 | 0.8899 | 1.7797 | 2.6696 | 3.5595 | 4.4494 | 5.3392 | 6.2291 | 7.1190 | 8.0089 | 1.3215 |
| 17 | 0.8897 | 1.7794 | 2.6691 | 3.5588 | 4.4485 | 5.3382 | 6.2279 | 7.1175 | 8.0072 | 1.3214 |
| 18 | 0.8895 | 1.7790 | 2.6685 | 3.5580 | 4.4476 | 5.3371 | 6.2266 | 7.1161 | 8.0056 | 1.3213 |
| 19 | 0.8893 | 1.7787 | 2.6680 | 3.5573 | 4.4467 | 5.3360 | 6.2253 | 7.1146 | 8.0040 | 1.3211 |
| 20 | 0.8892 | 1.7783 | 2.6675 | 3.5566 | 4.4458 | 5.3349 | 6.2241 | 7.1132 | 8.0024 | 1.3210 |
| 21 | 0.8890 | 1.7779 | 2.6669 | 3.5559 | 4.4448 | 5.3338 | 6.2228 | 7.1117 | 8.0007 | 1.3209 |
| 22 | 0.8888 | 1.7776 | 2.6664 | 3.5551 | 4.4439 | 5.3327 | 6.2215 | 7.1103 | 7.9991 | 1.3207 |
| 23 | 0.8886 | 1.7772 | 2.6658 | 3.5544 | 4.4430 | 5.3316 | 6.2202 | 7.1088 | 7.9974 | 1.3206 |
| 24 | 0.8884 | 1.7768 | 2.6653 | 3.5537 | 4.4421 | 5.3305 | 6.2190 | 7.1074 | 7.9958 | 1.3205 |
| 25 | 0.8882 | 1.7765 | 2.6647 | 3.5530 | 4.4412 | 5.3294 | 6.2177 | 7.1059 | 7.9942 | 1.3203 |
| 26 | 0.8881 | 1.7761 | 2.6642 | 3.5522 | 4.4403 | 5.3283 | 6.2164 | 7.1045 | 7.9925 | 1.3202 |
| 27 | 0.8879 | 1.7758 | 2.6636 | 3.5515 | 4.4394 | 5.3273 | 6.2151 | 7.1030 | 7.9909 | 1.3201 |
| 28 | 0.8877 | 1.7754 | 2.6631 | 3.5508 | 4.4385 | 5.3262 | 6.2139 | 7.1015 | 7.9892 | 1.3199 |
| 29 | 0.8875 | 1.7750 | 2.6625 | 3.5500 | 4.4376 | 5.3251 | 6.2126 | 7.1001 | 7.9876 | 1.3198 |
| 30 | 0.8873 | 1.7747 | 2.6620 | 3.5493 | 4.4366 | 5.3240 | 6.2113 | 7.0986 | 7.9860 | 1.3197 |
| 31 | 0.8871 | 1.7743 | 2.6614 | 3.5486 | 4.4357 | 5.3229 | 6.2100 | 7.0972 | 7.9843 | 1.3195 |
| 32 | 0.8870 | 1.7739 | 2.6609 | 3.5478 | 4.4348 | 5.3218 | 6.2087 | 7.0957 | 7.9827 | 1.3194 |
| 33 | 0.8868 | 1.7736 | 2.6603 | 3.5471 | 4.4339 | 5.3207 | 6.2075 | 7.0942 | 7.9810 | 1.3193 |
| 34 | 0.8866 | 1.7732 | 2.6598 | 3.5464 | 4.4330 | 5.3196 | 6.2062 | 7.0928 | 7.9794 | 1.3191 |
| 35 | 0.8864 | 1.7728 | 2.6592 | 3.5456 | 4.4321 | 5.3185 | 6.2049 | 7.0913 | 7.9777 | 1.3190 |
| 36 | 0.8862 | 1.7725 | 2.6587 | 3.5449 | 4.4311 | 5.3174 | 6.2036 | 7.0898 | 7.9761 | 1.3189 |
| 37 | 0.8860 | 1.7721 | 2.6581 | 3.5442 | 4.4302 | 5.3163 | 6.2023 | 7.0884 | 7.9744 | 1.3187 |
| 38 | 0.8859 | 1.7717 | 2.6576 | 3.5434 | 4.4293 | 5.3152 | 6.2010 | 7.0869 | 7.9727 | 1.3186 |
| 39 | 0.8857 | 1.7714 | 2.6570 | 3.5427 | 4.4284 | 5.3141 | 6.1997 | 7.0854 | 7.9711 | 1.3185 |
| 40 | 0.8855 | 1.7710 | 2.6565 | 3.5420 | 4.4275 | 5.3130 | 6.1985 | 7.0840 | 7.9694 | 1.3183 |
| 41 | 0.8853 | 1.7706 | 2.6559 | 3.5412 | 4.4265 | 5.3119 | 6.1972 | 7.0825 | 7.9678 | 1.3182 |
| 42 | 0.8851 | 1.7702 | 2.6554 | 3.5405 | 4.4256 | 5.3107 | 6.1959 | 7.0810 | 7.9661 | 1.3181 |
| 43 | 0.8849 | 1.7699 | 2.6548 | 3.5398 | 4.4247 | 5.3096 | 6.1946 | 7.0795 | 7.9645 | 1.3179 |
| 44 | 0.8848 | 1.7695 | 2.6543 | 3.5390 | 4.4238 | 5.3085 | 6.1933 | 7.0780 | 7.9628 | 1.3178 |
| 45 | 0.8846 | 1.7691 | 2.6537 | 3.5383 | 4.4229 | 5.3074 | 6.1920 | 7.0766 | 7.9611 | 1.3177 |
| 46 | 0.8844 | 1.7688 | 2.6532 | 3.5375 | 4.4219 | 5.3063 | 6.1907 | 7.0751 | 7.9595 | 1.3175 |
| 47 | 0.8842 | 1.7684 | 2.6526 | 3.5368 | 4.4210 | 5.3052 | 6.1894 | 7.0736 | 7.9578 | 1.3174 |
| 48 | 0.8840 | 1.7680 | 2.6520 | 3.5361 | 4.4201 | 5.3041 | 6.1881 | 7.0721 | 7.9561 | 1.3173 |
| 49 | 0.8838 | 1.7677 | 2.6515 | 3.5353 | 4.4192 | 5.3030 | 6.1868 | 7.0706 | 7.9545 | 1.3171 |
| 50 | 0.8836 | 1.7673 | 2.6509 | 3.5346 | 4.4182 | 5.3019 | 6.1855 | 7.0692 | 7.9528 | 1.3170 |
| 51 | 0.8835 | 1.7669 | 2.6504 | 3.5338 | 4.4173 | 5.3008 | 6.1842 | 7.0677 | 7.9511 | 1.3169 |
| 52 | 0.8833 | 1.7665 | 2.6498 | 3.5331 | 4.4164 | 5.2996 | 6.1829 | 7.0662 | 7.9495 | 1.3167 |
| 53 | 0.8831 | 1.7662 | 2.6493 | 3.5324 | 4.4154 | 5.2985 | 6.1816 | 7.0647 | 7.9478 | 1.3166 |
| 54 | 0.8829 | 1.7658 | 2.6487 | 3.5316 | 4.4145 | 5.2974 | 6.1803 | 7.0632 | 7.9461 | 1.3165 |
| 55 | 0.8827 | 1.7654 | 2.6481 | 3.5309 | 4.4136 | 5.2963 | 6.1790 | 7.0617 | 7.9444 | 1.3163 |
| 56 | 0.8825 | 1.7651 | 2.6476 | 3.5301 | 4.4127 | 5.2952 | 6.1777 | 7.0602 | 7.9428 | 1.3162 |
| 57 | 0.8823 | 1.7647 | 2.6470 | 3.5294 | 4.4117 | 5.2941 | 6.1764 | 7.0588 | 7.9411 | 1.3160 |
| 58 | 0.8822 | 1.7643 | 2.6465 | 3.5286 | 4.4108 | 5.2929 | 6.1751 | 7.0573 | 7.9394 | 1.3159 |
| 59 | 0.8820 | 1.7639 | 2.6459 | 3.5279 | 4.4099 | 5.2918 | 6.1738 | 7.0558 | 7.9377 | 1.3158 |
| 60 | 0.8818 | 1.7636 | 2.6454 | 3.5271 | 4.4089 | 5.2907 | 6.1725 | 7.0543 | 7.9361 | 1.3156 |

| 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | b      |    |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|----|
| 0.3074 | 0.6148 | 0.9222 | 1.2296 | 1.5370 | 1.8444 | 2.1518 | 2.4592 | 2.7666 | 0.4558 | 00 |
| 0.3076 | 0.6153 | 0.9229 | 1.2305 | 1.5381 | 1.8458 | 2.1534 | 2.4610 | 2.7687 | 0.4562 | 01 |
| 0.3079 | 0.6157 | 0.9236 | 1.2314 | 1.5393 | 1.8472 | 2.1550 | 2.4629 | 2.7707 | 0.4566 | 02 |
| 0.3081 | 0.6162 | 0.9243 | 1.2324 | 1.5404 | 1.8485 | 2.1566 | 2.4647 | 2.7728 | 0.4570 | 03 |
| 0.3083 | 0.6166 | 0.9249 | 1.2333 | 1.5416 | 1.8499 | 2.1582 | 2.4665 | 2.7748 | 0.4573 | 04 |
| 0.3085 | 0.6171 | 0.9256 | 1.2342 | 1.5427 | 1.8512 | 2.1598 | 2.4683 | 2.7769 | 0.4577 | 05 |
| 0.3088 | 0.6175 | 0.9263 | 1.2351 | 1.5439 | 1.8526 | 2.1614 | 2.4702 | 2.7789 | 0.4581 | 06 |
| 0.3090 | 0.6180 | 0.9270 | 1.2360 | 1.5450 | 1.8540 | 2.1630 | 2.4720 | 2.7810 | 0.4585 | 07 |
| 0.3092 | 0.6185 | 0.9277 | 1.2369 | 1.5461 | 1.8554 | 2.1646 | 2.4738 | 2.7831 | 0.4589 | 08 |
| 0.3095 | 0.6189 | 0.9284 | 1.2378 | 1.5473 | 1.8568 | 2.1662 | 2.4757 | 2.7851 | 0.4593 | 09 |
| 0.3097 | 0.6194 | 0.9290 | 1.2387 | 1.5484 | 1.8581 | 2.1678 | 2.4775 | 2.7871 | 0.4596 | 10 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.3099 | 0.6198 | 0.9297 | 1.2396 | 1.5495 | 1.8595 | 2.1694 | 2.4793 | 2.7892 | 0.4600 | 11 |
| 0.3101 | 0.6203 | 0.9304 | 1.2405 | 1.5507 | 1.8608 | 2.1710 | 2.4811 | 2.7913 | 0.4604 | 12 |
| 0.3104 | 0.6207 | 0.9311 | 1.2415 | 1.5518 | 1.8622 | 2.1726 | 2.4830 | 2.7933 | 0.4608 | 13 |
| 0.3106 | 0.6212 | 0.9318 | 1.2424 | 1.5530 | 1.8636 | 2.1742 | 2.4848 | 2.7953 | 0.4612 | 14 |
| 0.3108 | 0.6216 | 0.9325 | 1.2433 | 1.5541 | 1.8649 | 2.1758 | 2.4866 | 2.7974 | 0.4616 | 15 |
| 0.3110 | 0.6221 | 0.9331 | 1.2442 | 1.5552 | 1.8663 | 2.1773 | 2.4884 | 2.7994 | 0.4619 | 16 |
| 0.3113 | 0.6226 | 0.9338 | 1.2451 | 1.5564 | 1.8677 | 2.1789 | 2.4902 | 2.8015 | 0.4623 | 17 |
| 0.3115 | 0.6230 | 0.9345 | 1.2460 | 1.5575 | 1.8690 | 2.1805 | 2.4920 | 2.8035 | 0.4627 | 18 |
| 0.3117 | 0.6235 | 0.9352 | 1.2469 | 1.5587 | 1.8704 | 2.1821 | 2.4938 | 2.8056 | 0.4631 | 19 |
| 0.3120 | 0.6239 | 0.9359 | 1.2478 | 1.5598 | 1.8718 | 2.1837 | 2.4957 | 2.8076 | 0.4635 | 20 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.3122 | 0.6244 | 0.9365 | 1.2487 | 1.5609 | 1.8731 | 2.1853 | 2.4975 | 2.8096 | 0.4639 | 21 |
| 0.3124 | 0.6248 | 0.9372 | 1.2496 | 1.5620 | 1.8745 | 2.1869 | 2.4993 | 2.8117 | 0.4642 | 22 |
| 0.3126 | 0.6253 | 0.9379 | 1.2505 | 1.5632 | 1.8758 | 2.1885 | 2.5011 | 2.8137 | 0.4646 | 23 |
| 0.3129 | 0.6257 | 0.9386 | 1.2514 | 1.5643 | 1.8772 | 2.1900 | 2.5029 | 2.8157 | 0.4650 | 24 |
| 0.3131 | 0.6262 | 0.9393 | 1.2524 | 1.5654 | 1.8785 | 2.1916 | 2.5047 | 2.8178 | 0.4654 | 25 |
| 0.3133 | 0.6266 | 0.9399 | 1.2533 | 1.5666 | 1.8799 | 2.1932 | 2.5065 | 2.8198 | 0.4658 | 26 |
| 0.3135 | 0.6271 | 0.9406 | 1.2542 | 1.5677 | 1.8812 | 2.1948 | 2.5083 | 2.8219 | 0.4662 | 27 |
| 0.3138 | 0.6275 | 0.9413 | 1.2551 | 1.5688 | 1.8826 | 2.1964 | 2.5101 | 2.8239 | 0.4665 | 28 |
| 0.3140 | 0.6280 | 0.9420 | 1.2560 | 1.5700 | 1.8839 | 2.1979 | 2.5119 | 2.8259 | 0.4669 | 29 |
| 0.3142 | 0.6284 | 0.9427 | 1.2569 | 1.5711 | 1.8853 | 2.1995 | 2.5138 | 2.8280 | 0.4673 | 30 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.3144 | 0.6289 | 0.9433 | 1.2578 | 1.5722 | 1.8867 | 2.2011 | 2.5156 | 2.8300 | 0.4677 | 31 |
| 0.3147 | 0.6293 | 0.9440 | 1.2587 | 1.5734 | 1.8880 | 2.2027 | 2.5174 | 2.8320 | 0.4681 | 32 |
| 0.3149 | 0.6298 | 0.9447 | 1.2596 | 1.5745 | 1.8894 | 2.2043 | 2.5192 | 2.8341 | 0.4685 | 33 |
| 0.3151 | 0.6302 | 0.9454 | 1.2605 | 1.5756 | 1.8907 | 2.2058 | 2.5210 | 2.8361 | 0.4689 | 34 |
| 0.3153 | 0.6307 | 0.9460 | 1.2614 | 1.5767 | 1.8921 | 2.2074 | 2.5228 | 2.8381 | 0.4692 | 35 |
| 0.3156 | 0.6311 | 0.9467 | 1.2623 | 1.5779 | 1.8934 | 2.2090 | 2.5246 | 2.8401 | 0.4696 | 36 |
| 0.3158 | 0.6316 | 0.9474 | 1.2632 | 1.5790 | 1.8948 | 2.2106 | 2.5264 | 2.8422 | 0.4700 | 37 |
| 0.3160 | 0.6320 | 0.9481 | 1.2641 | 1.5801 | 1.8961 | 2.2122 | 2.5282 | 2.8442 | 0.4704 | 38 |
| 0.3162 | 0.6325 | 0.9487 | 1.2650 | 1.5812 | 1.8975 | 2.2137 | 2.5300 | 2.8462 | 0.4708 | 39 |
| 0.3165 | 0.6329 | 0.9494 | 1.2659 | 1.5824 | 1.8988 | 2.2153 | 2.5318 | 2.8482 | 0.4712 | 40 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.3167 | 0.6334 | 0.9501 | 1.2668 | 1.5835 | 1.9002 | 2.2169 | 2.5336 | 2.8503 | 0.4715 | 41 |
| 0.3169 | 0.6338 | 0.9508 | 1.2677 | 1.5846 | 1.9015 | 2.2184 | 2.5354 | 2.8523 | 0.4719 | 42 |
| 0.3171 | 0.6343 | 0.9514 | 1.2686 | 1.5857 | 1.9029 | 2.2200 | 2.5372 | 2.8543 | 0.4723 | 43 |
| 0.3174 | 0.6347 | 0.9521 | 1.2695 | 1.5868 | 1.9042 | 2.2216 | 2.5390 | 2.8563 | 0.4727 | 44 |
| 0.3176 | 0.6352 | 0.9528 | 1.2704 | 1.5880 | 1.9055 | 2.2231 | 2.5407 | 2.8583 | 0.4731 | 45 |
| 0.3178 | 0.6356 | 0.9535 | 1.2713 | 1.5891 | 1.9069 | 2.2247 | 2.5425 | 2.8604 | 0.4735 | 46 |
| 0.3180 | 0.6361 | 0.9541 | 1.2722 | 1.5902 | 1.9082 | 2.2263 | 2.5443 | 2.8624 | 0.4739 | 47 |
| 0.3183 | 0.6365 | 0.9548 | 1.2731 | 1.5913 | 1.9096 | 2.2279 | 2.5461 | 2.8644 | 0.4742 | 48 |
| 0.3185 | 0.6370 | 0.9555 | 1.2740 | 1.5924 | 1.9109 | 2.2294 | 2.5479 | 2.8664 | 0.4746 | 49 |
| 0.3187 | 0.6374 | 0.9561 | 1.2748 | 1.5936 | 1.9123 | 2.2310 | 2.5497 | 2.8684 | 0.4750 | 50 |
|        |        |        |        |        |        |        |        |        |        |    |
| 0.3189 | 0.6379 | 0.9568 | 1.2757 | 1.5947 | 1.9136 | 2.2326 | 2.5515 | 2.8704 | 0.4754 | 51 |
| 0.3192 | 0.6383 | 0.9575 | 1.2766 | 1.5958 | 1.9150 | 2.2341 | 2.5533 | 2.8724 | 0.4758 | 52 |
| 0.3194 | 0.6388 | 0.9581 | 1.2775 | 1.5969 | 1.9163 | 2.2357 | 2.5551 | 2.8744 | 0.4761 | 53 |
| 0.3196 | 0.6392 | 0.9588 | 1.2784 | 1.5980 | 1.9177 | 2.2373 | 2.5569 | 2.8765 | 0.4765 | 54 |
| 0.3198 | 0.6397 | 0.9595 | 1.2793 | 1.5991 | 1.9190 | 2.2388 | 2.5586 | 2.8785 | 0.4769 | 55 |
| 0.3201 | 0.6401 | 0.9602 | 1.2802 | 1.6003 | 1.9203 | 2.2404 | 2.5604 | 2.8805 | 0.4773 | 56 |
| 0.3203 | 0.6405 | 0.9608 | 1.2811 | 1.6014 | 1.9216 | 2.2419 | 2.5622 | 2.8825 | 0.4777 | 57 |
| 0.3205 | 0.6410 | 0.9615 | 1.2820 | 1.6025 | 1.9230 | 2.2435 | 2.5640 | 2.8845 | 0.4781 | 58 |
| 0.3207 | 0.6414 | 0.9622 | 1.2829 | 1.6036 | 1.9243 | 2.2450 | 2.5658 | 2.8865 | 0.4784 | 59 |
| 0.3209 | 0.6419 | 0.9628 | 1.2838 | 1.6047 | 1.9257 | 2.2465 | 2.5675 | 2.8885 | 0.4788 | 60 |

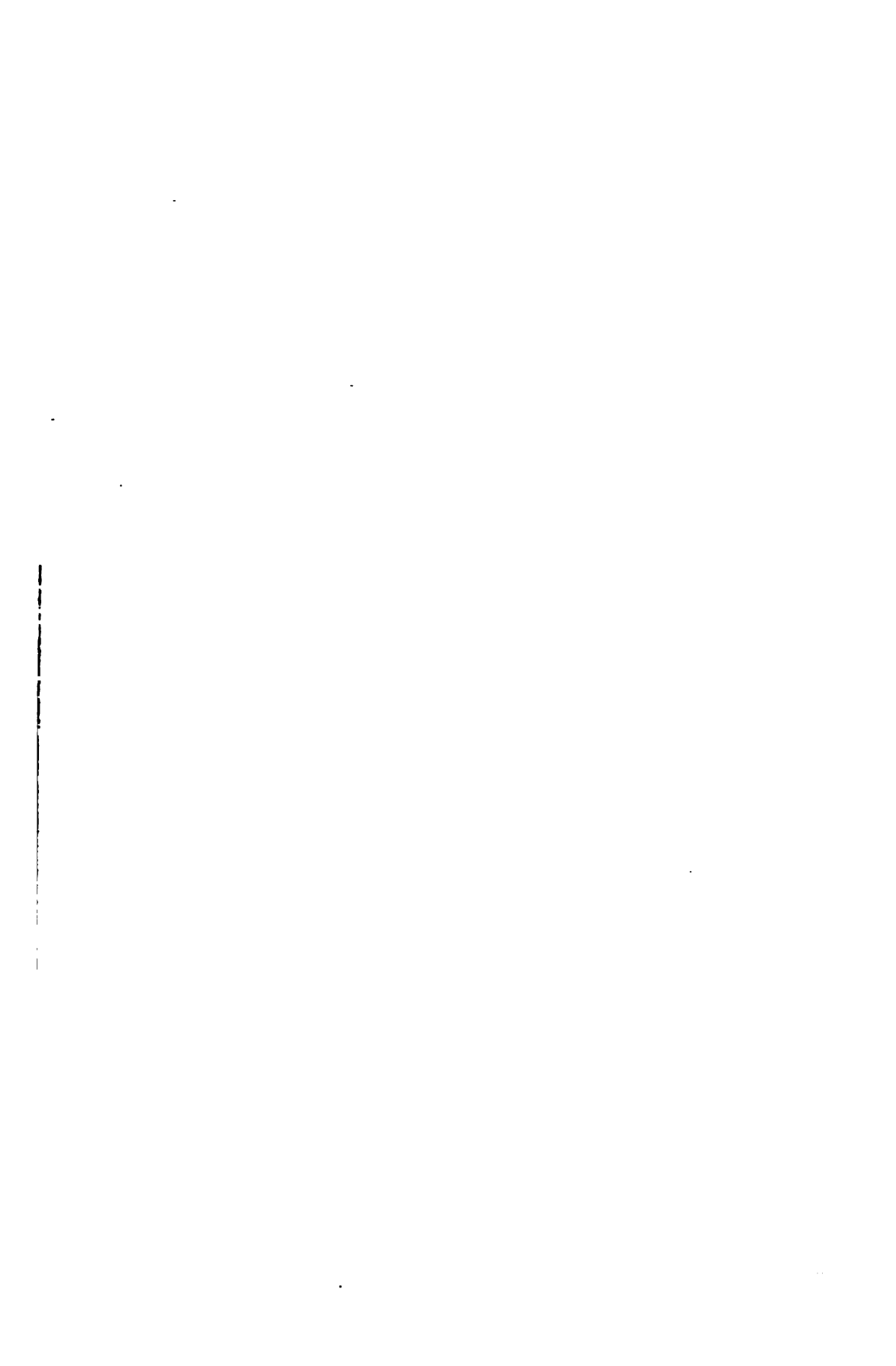
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